

# Proprieties of FEL radiation at SPARX

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# Outline

- Objectives & Resources
  - Beam parameters
  - Undulator
- SASE
  - Longitudinal coherence
  - Transverse coherence
  - Main parameters & constraints
- Seeded FEL configurations
  - Seeding with HHG in gas
    - Short pulses
    - Coherence
  - Seeding in “superradiant mode” – generation of fs soft x ray pulses
- Pointing stability
- Conclusions

# Objectives

- Input from the last SPARX workshop:

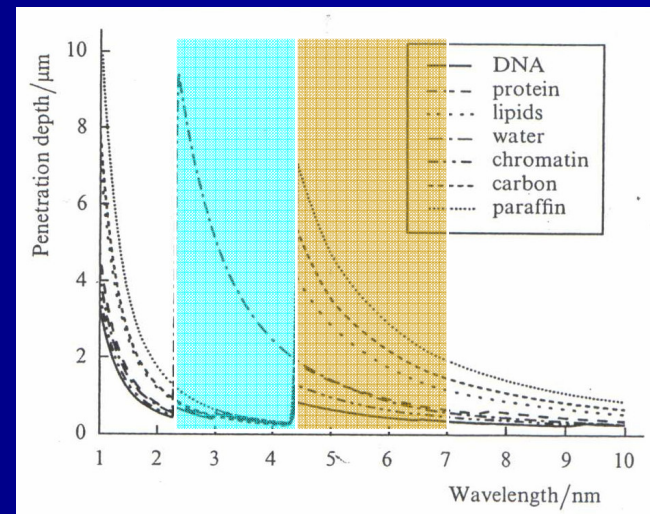
Wavelength range as close as possible to the water window ( $\sim 2.5 - 4.5$  nm)

... and to the carbon window

- Flexible design:

SASE & Seeded configurations

- Improve coherence length
- Short pulses (fs range)
- Increase wavelength operation range



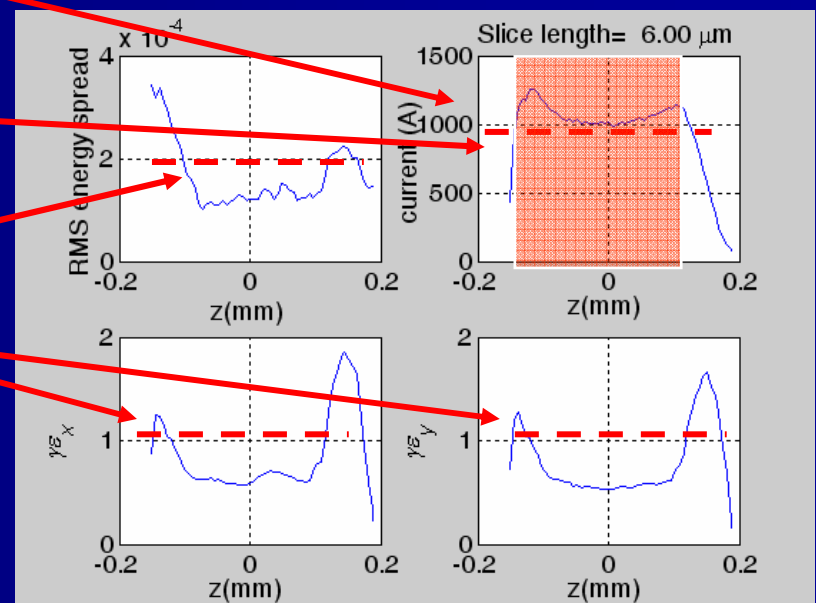
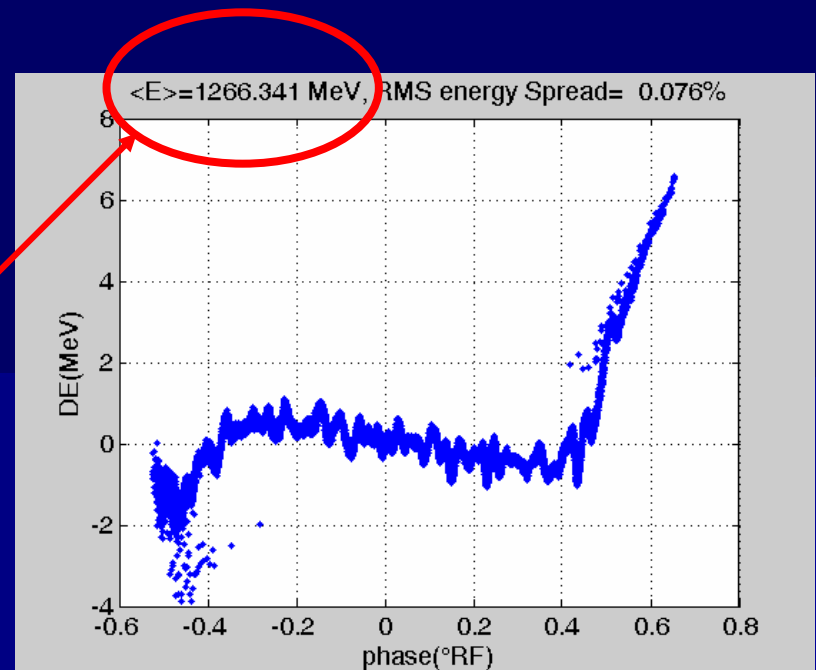
# Resources

- Upgraded DaΦne linac
  - Beam energy 1 – 1.5 GeV (possible extensions to higher energy)
  - State of the art beam brightness
- SPARC Undulator
  - 6 sections 77 periods 2.8 cm

# e-beam @ the UM

C. Ronsivalle –  
C. Vaccarezza BD 11/4/2005

- Beam energy 1.25 GeV
- Flat longitudinal current profile  $\sim 1$  kA
- Pulse Duration  $\sim 300$   $\mu$ m  $\sim 1$  ps
- Slice energy spread  $< 2 \cdot 10^{-4}$
- Slice emittances  $< 1$  mm-mrad



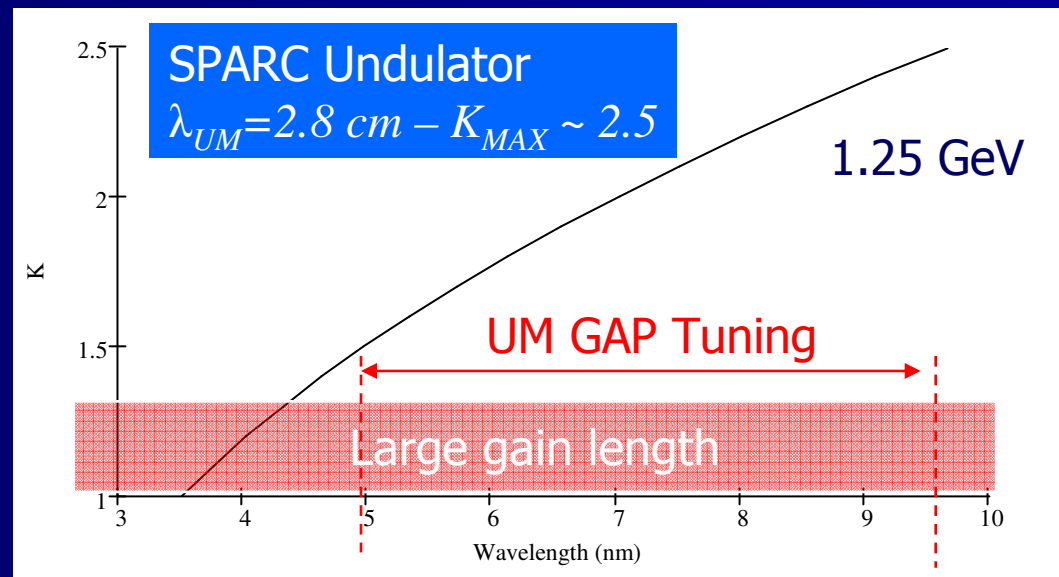
# SPARC Undulator 2.8 cm period

## Reference:

Beam Energy	1.25 GeV
Peak Current	1 kA
Slice energy spread	$< 2 \cdot 10^{-4}$
Slice emittance	$< 1$ mm-mrad

## Resonance condition

$$\lambda_{FEL} = \frac{\lambda_{UM}}{2\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$



# SPARC Undulator 2.8 cm period

## Reference:

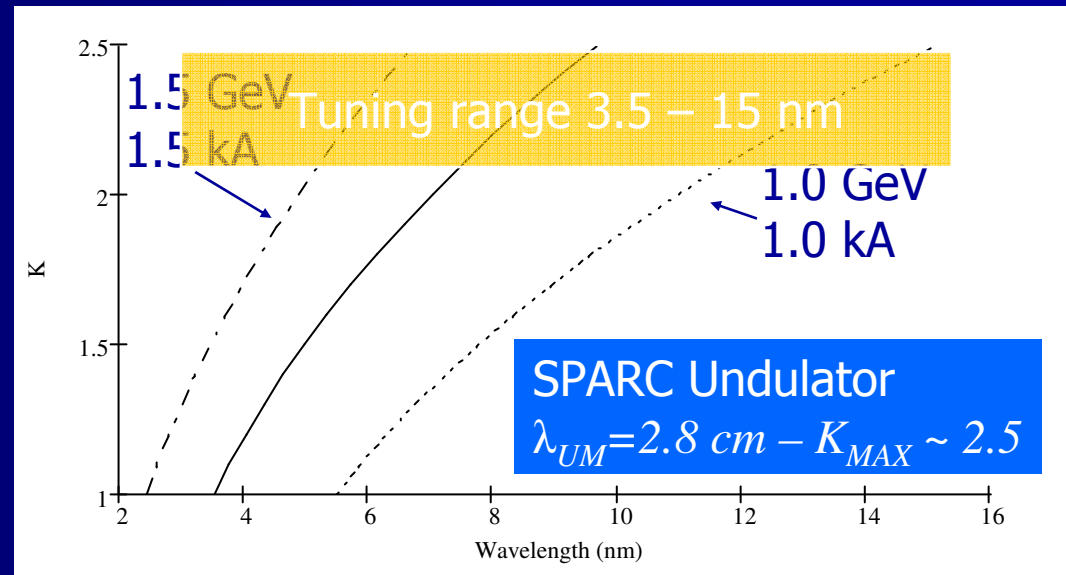
Beam Energy	1.25 GeV
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## Resonance condition

$$\lambda_{FEL} = \frac{\lambda_{UM}}{2\gamma^2} \left( 1 + \frac{K^2}{2} \right)$$

**Low Energy :** 1.0GeV & 1.0kA

**High Energy :** 1.5GeV & 1.5kA



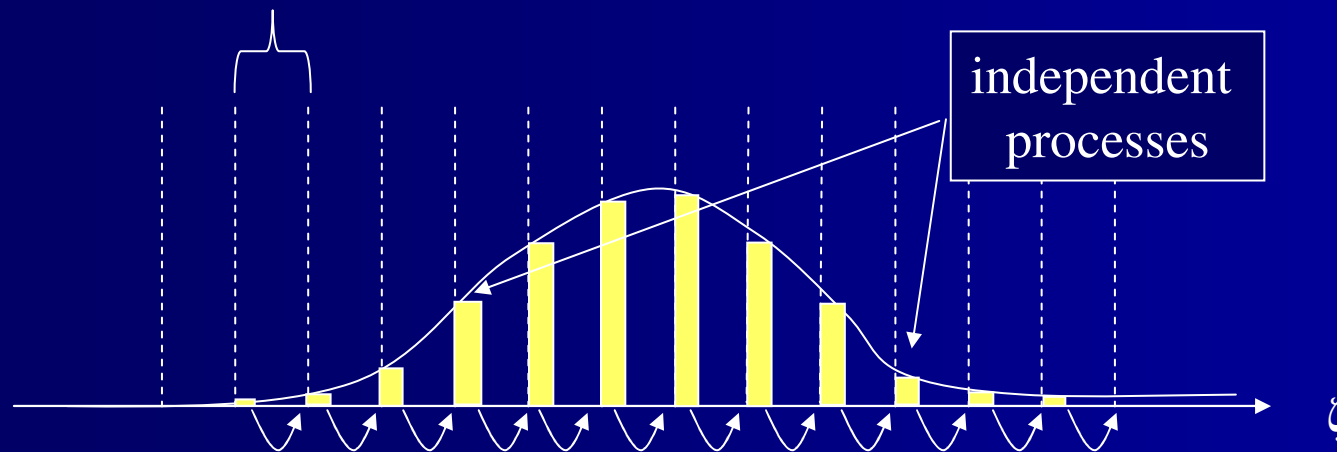
Wavelength tuning range - 15 – 4 nm

**SASE**



# SASE & Spikes

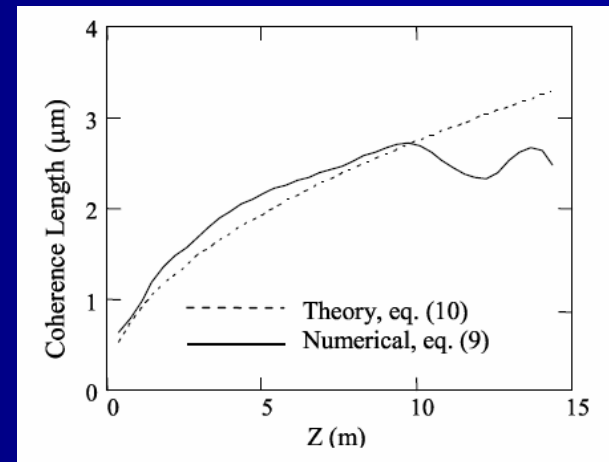
Slippage length  $\approx N\lambda_0$

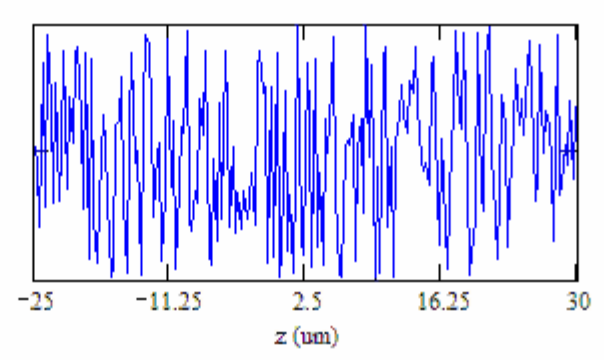
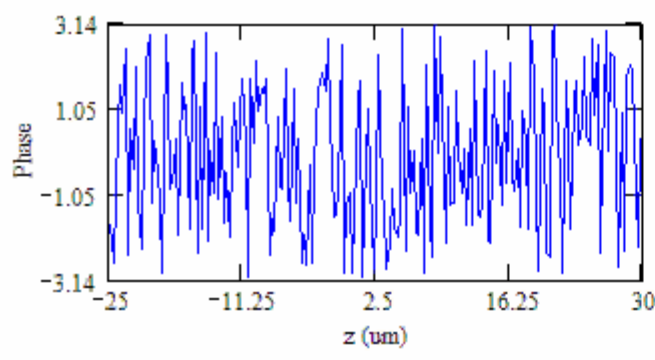
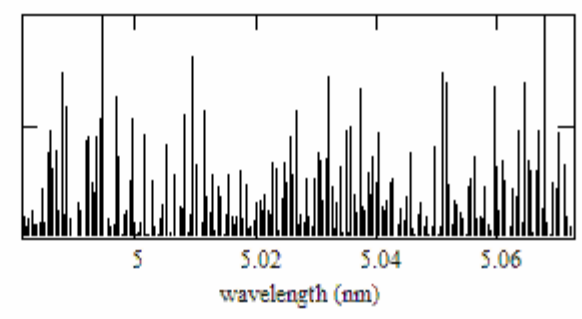
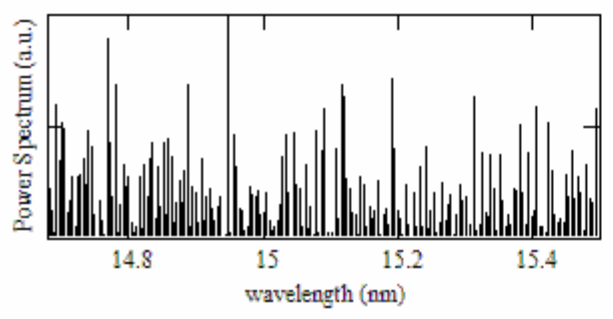
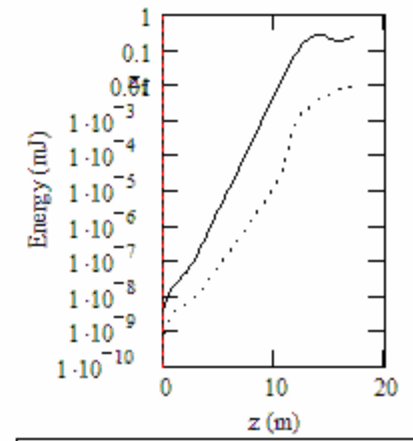
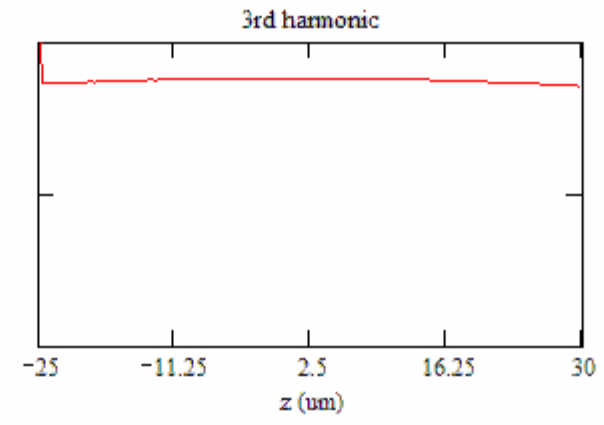
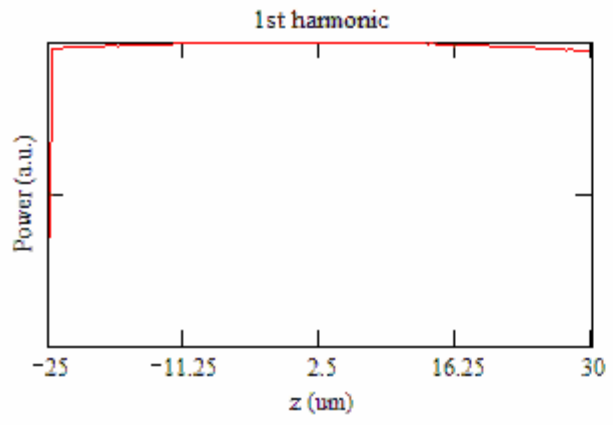


- The radiation “slips” over the electrons for a distance  $N\lambda_0$



$$z_c = \frac{1}{6} \frac{\lambda_0}{\rho} \sqrt{\frac{z}{2\pi L_g}}$$





**Main parameters at**  
 $f = 0$  , or  $z_f = 0$  m  
 $P_{in} = 0$  W  
 $Energy_{f,0} = 4.684 \times 10^{-9}$  mJ  
 $Energy_{f,2} = 8.398 \times 10^{-10}$  mJ  
 $\frac{1}{c} \cdot length_{rms_{f,0}} = 0.053$  ps  
 $\frac{1}{c} \cdot length_{rms_{f,2}} = 0.053$  ps  
 $width_{rms_{f,0}} \cdot \frac{\lambda_0 n_u}{c} = 1.639\%$   
 $width_{rms_{f,2}} \cdot \frac{\lambda_0 n_u}{c \cdot 3} = 0.155\%$   
 $dfl_1 = 4.198$   
 $dfl_3 = 7.55$

## **$M$ longitudinal independent modes**

Cooperation length  $L_c = \lambda/4\pi\rho$

Number of modes  $M \sim L_c / L_b$  ( $L_b$  - bunch length)

$$\rho \sim 10^{-3}$$

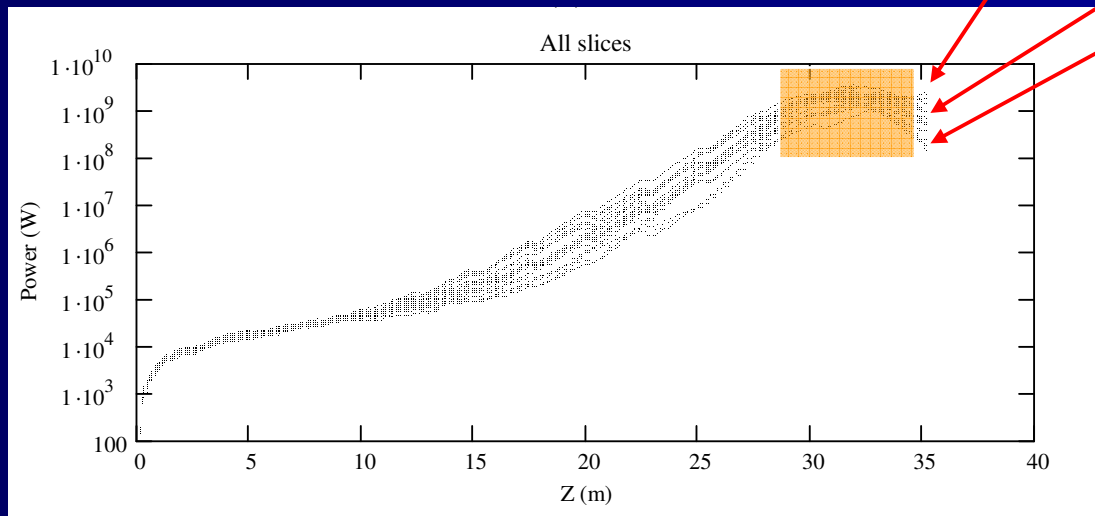
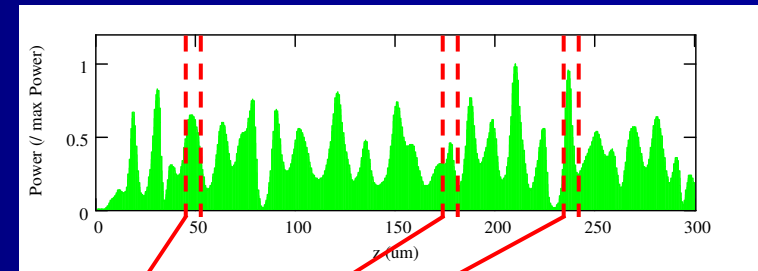
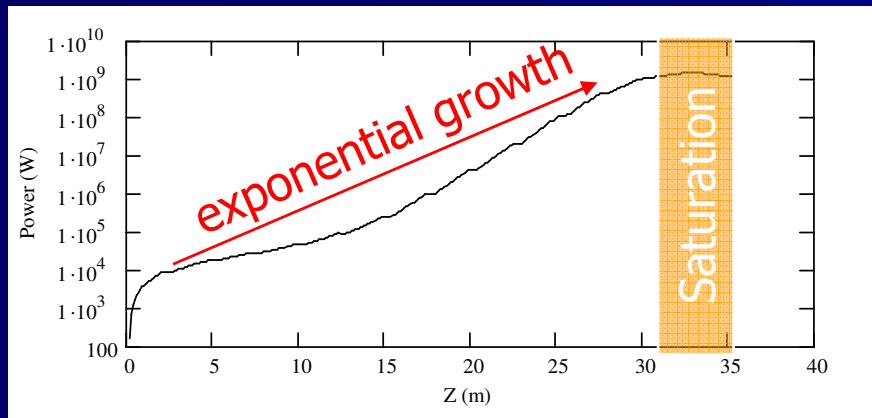
$$\lambda \sim 5 - 10 \text{ nm}$$

$$L_b \sim 0.5 - 1 \text{ ps}$$

$$L_c \sim 100 \lambda$$

$$\text{Shot to shot fluctuations} \sim 1/\sqrt{M} \approx 5\%$$

# Saturation of different slices

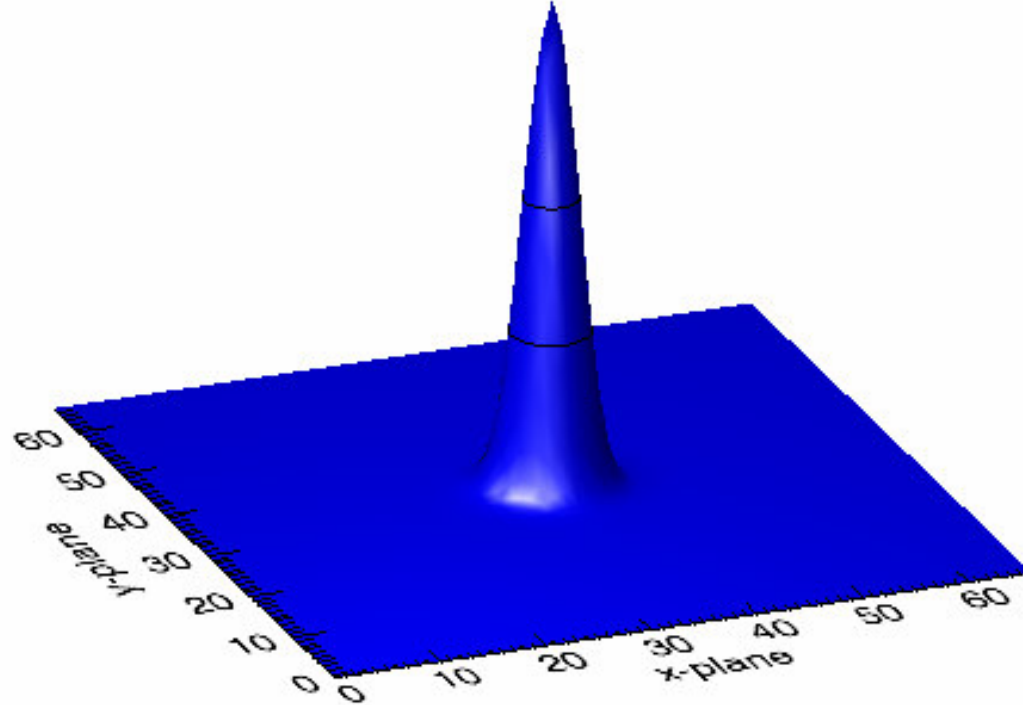


Independent slices saturate at different positions

The integrated source has an increased longitudinal extension

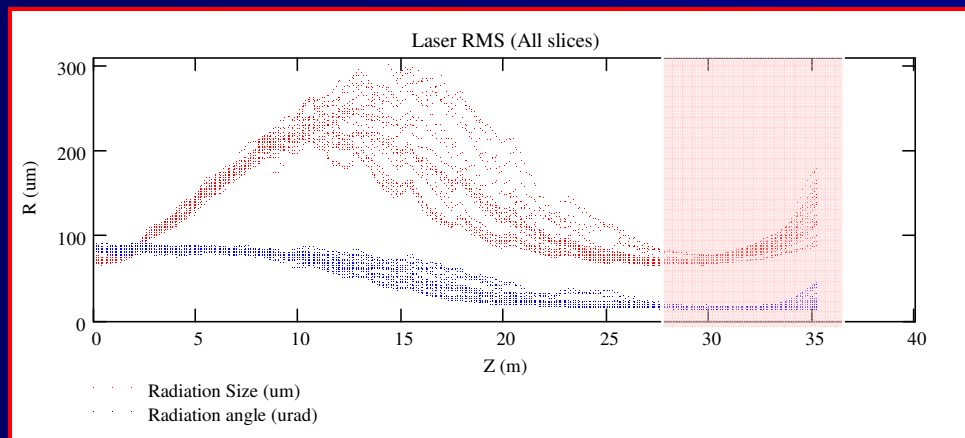
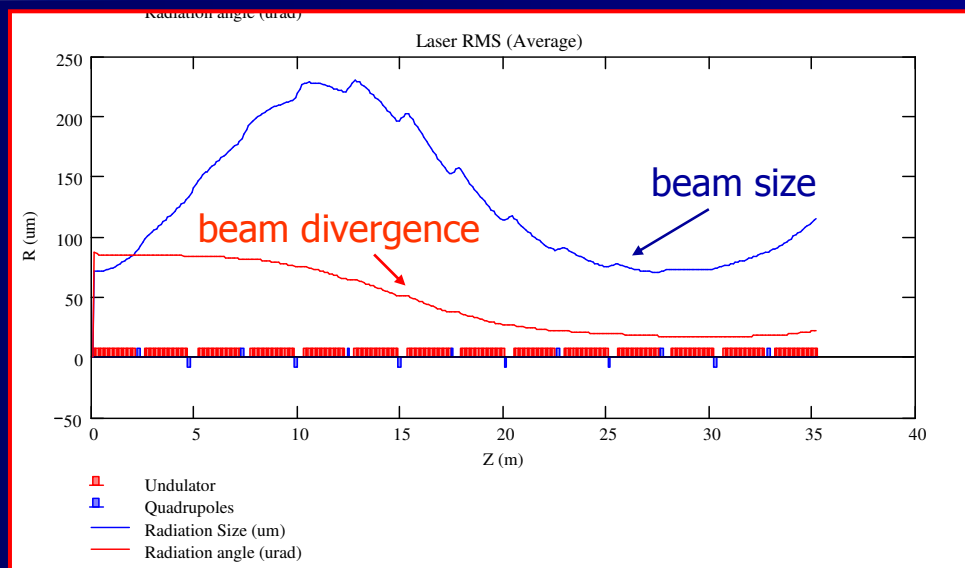
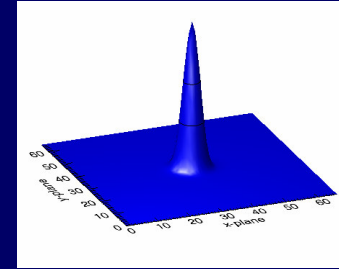
# Transverse plane

SASE - transverse profile @ 4.5 nm (far field)



GENESIS 1.3 – Averaged over long. slices at 33 m

# Transverse plane



Spiking effects in the transverse plane

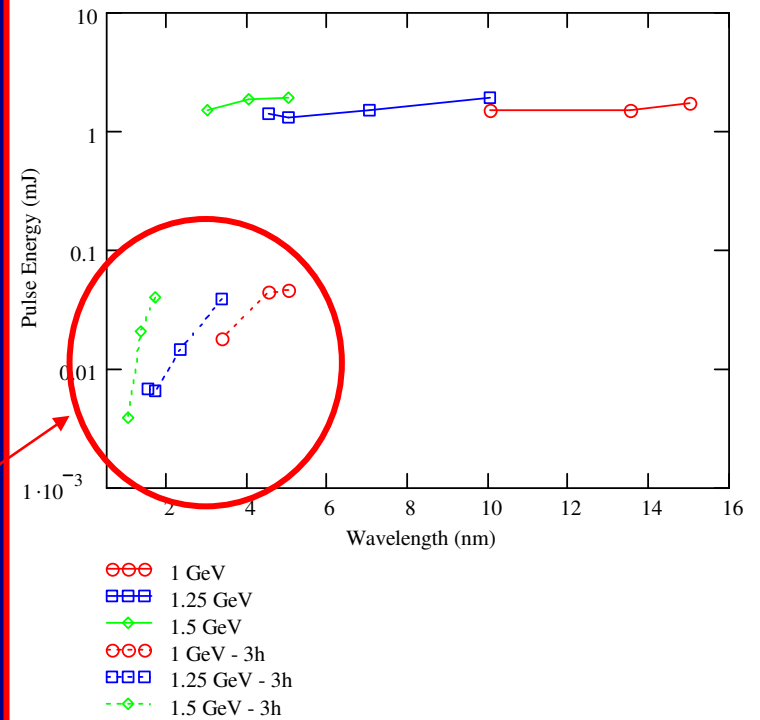
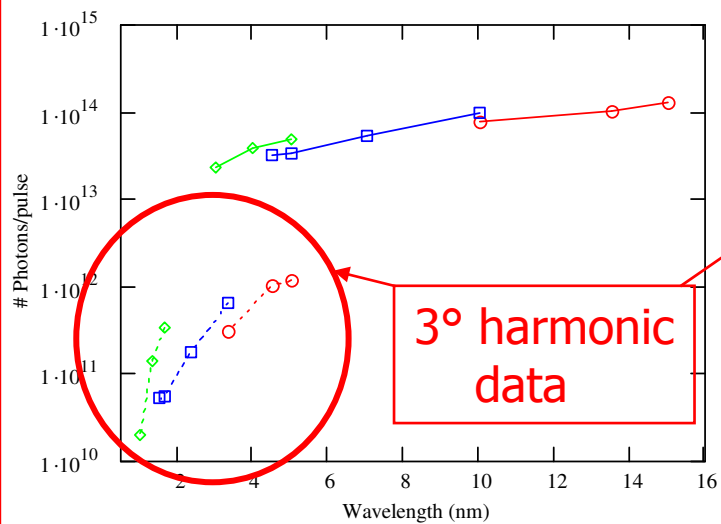
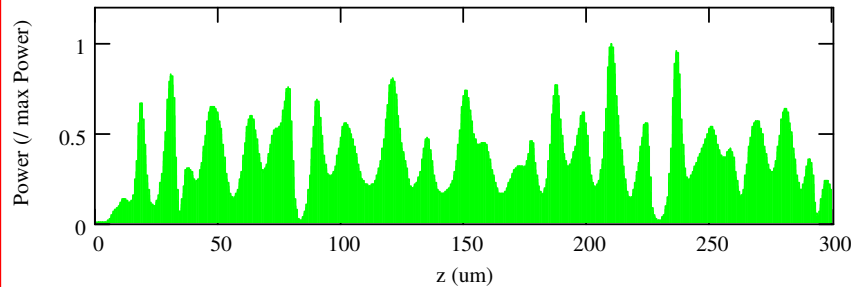
The integrated source has an extension "larger" than the diffraction limit

$$\sigma\sigma' = \frac{\lambda}{4\pi}$$

# SASE – Performances

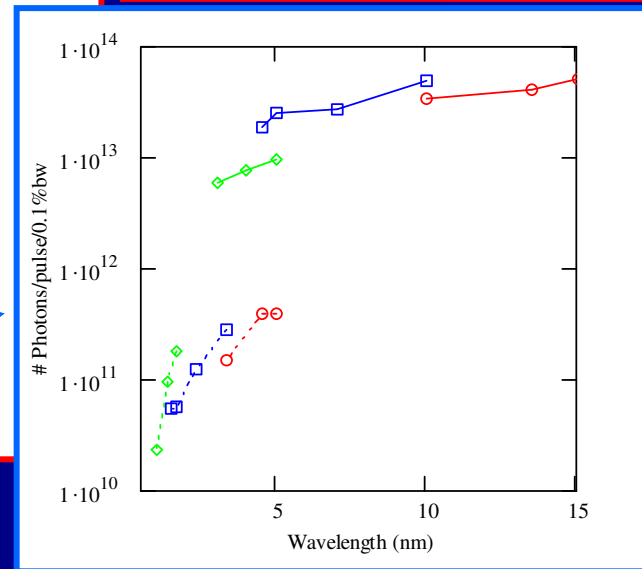
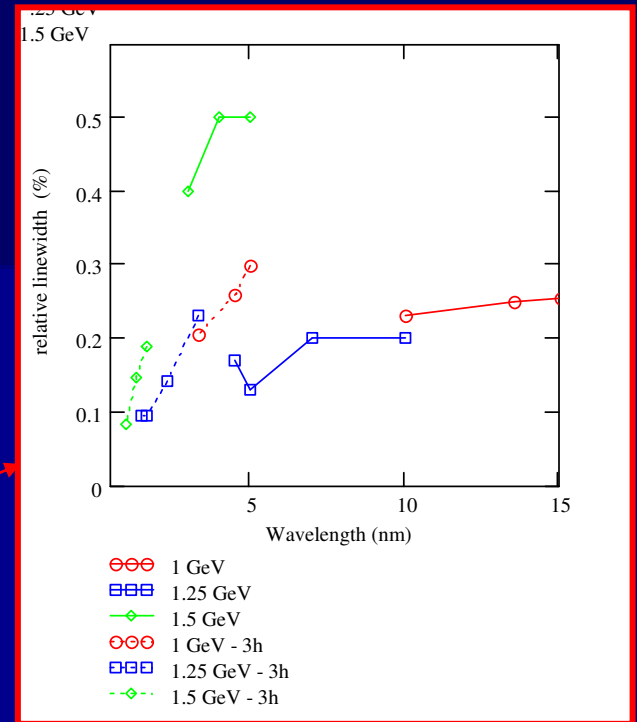
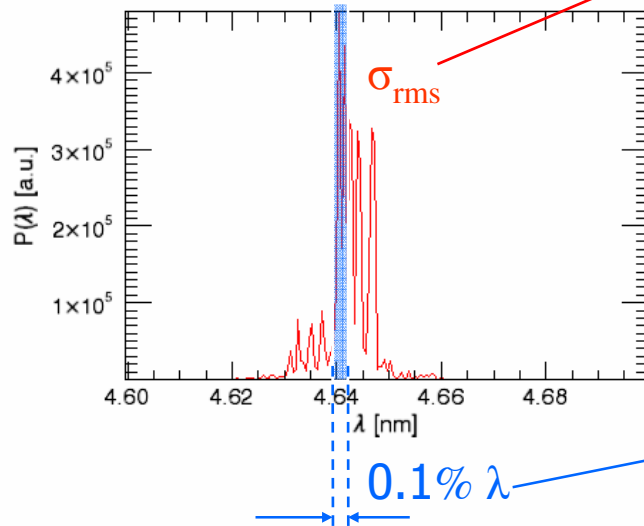
*Simulations made with GENESIS 1.3 + Perseo for the high order harmonics*

## SASE PULSE (4.5nm – 33m)



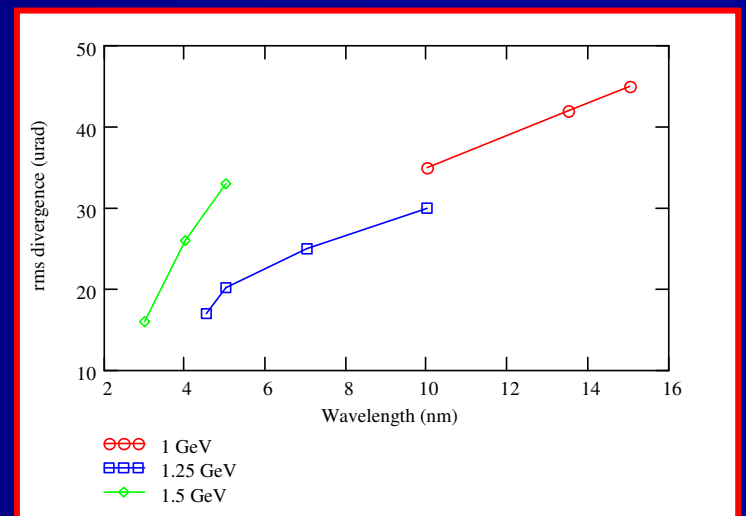
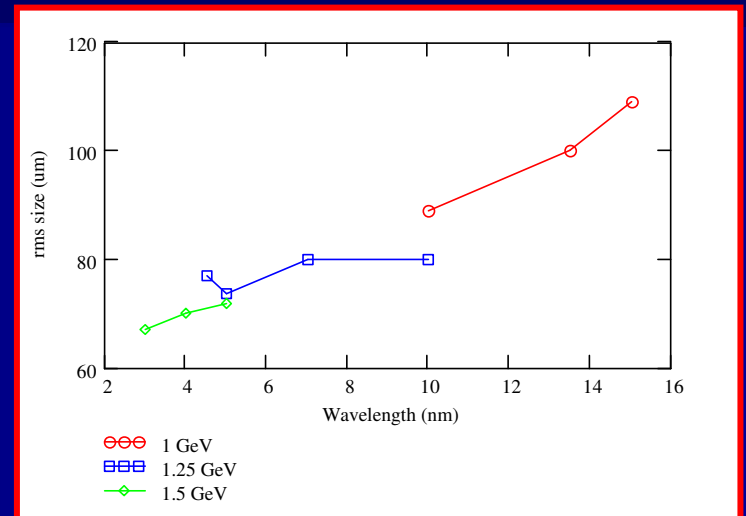
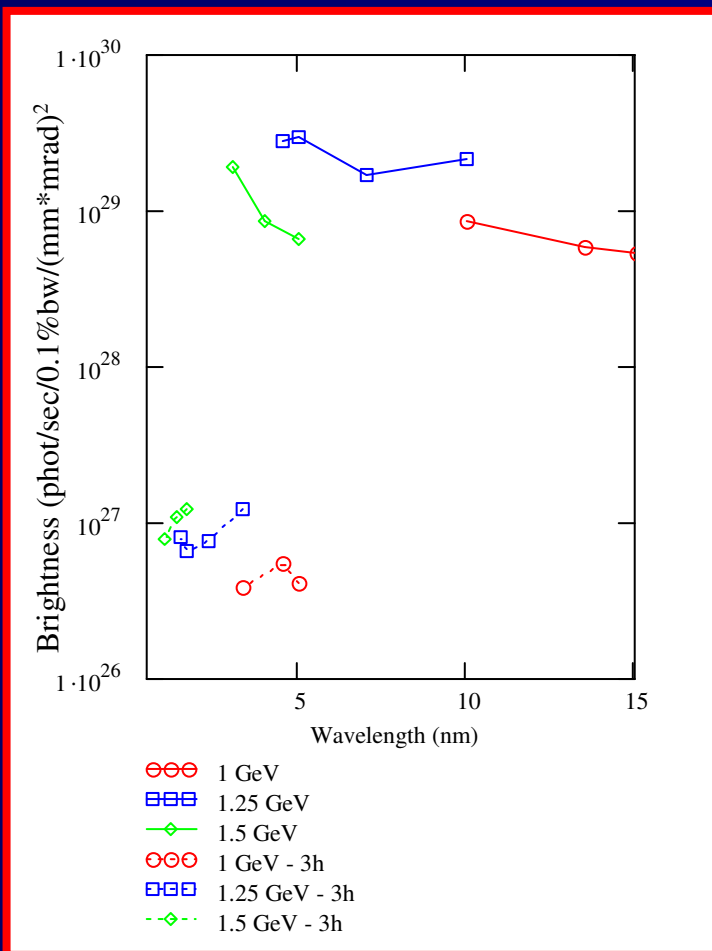
# Spectrum

SASE Spectrum @ 4.5 nm – 33m

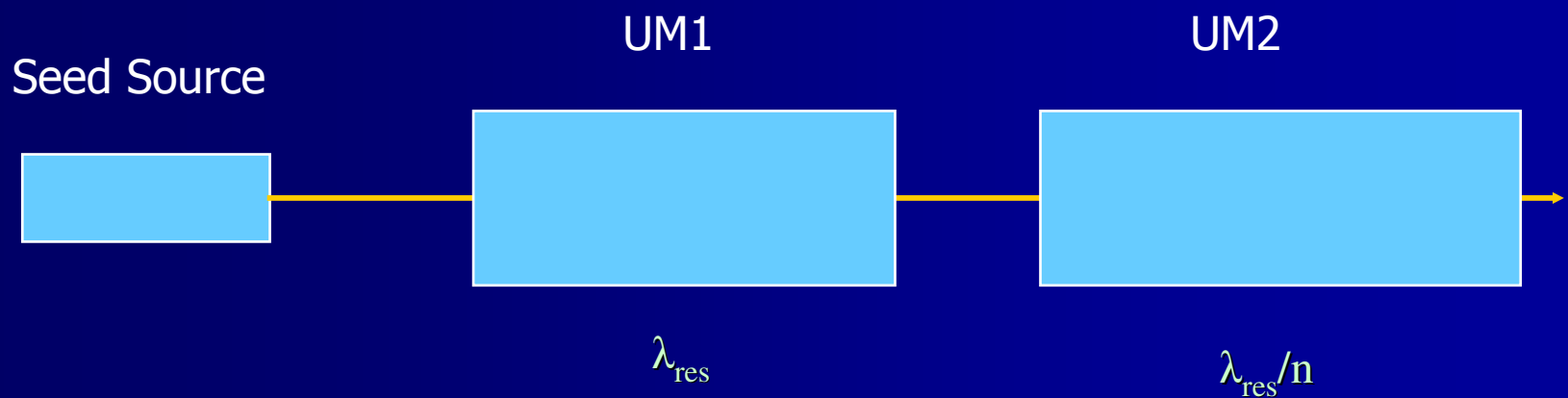




# Brightness

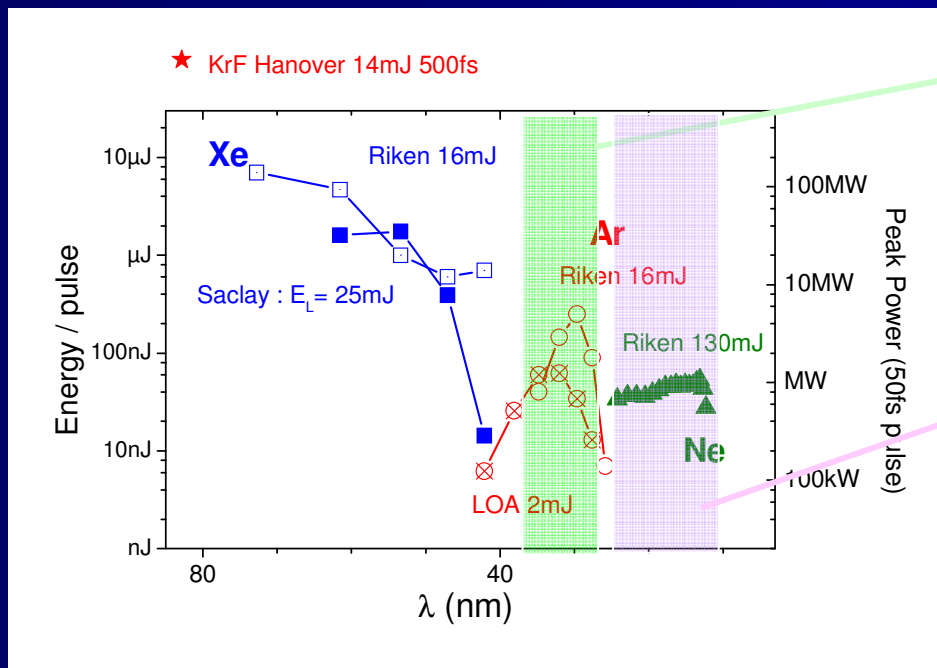


# SEEDING & Harmonic Gen.



# Seed Sources

- 3<sup>o</sup> harm of Ti:Sa 260 (→ 180 nm) + multiple stages cascade
- HHG in gas + cascade



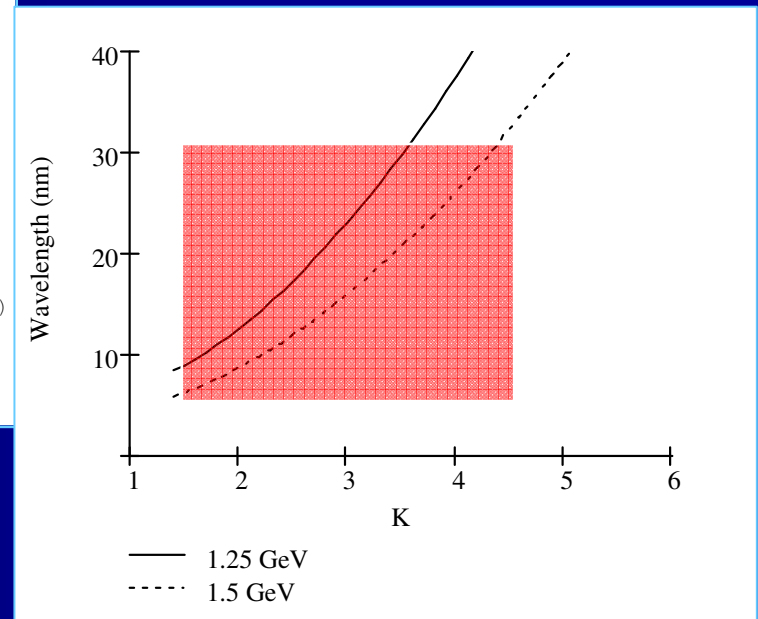
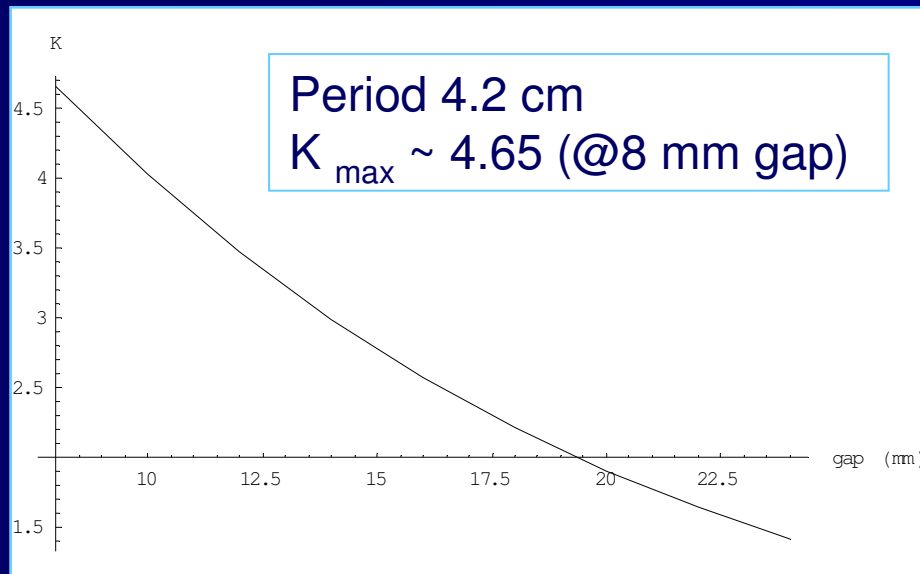
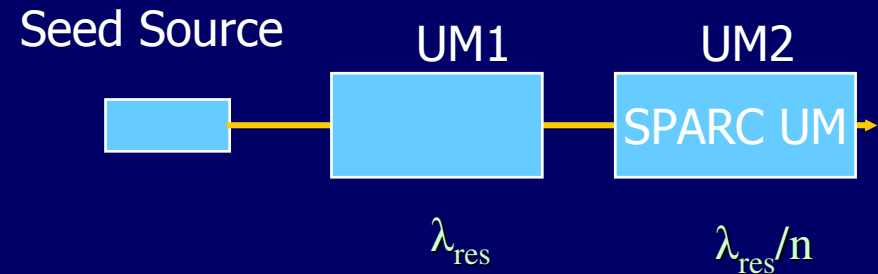
→ Ar

$\lambda \sim 28-32 \text{ nm}$   
 $E \sim 0.3 - 0.4 \mu\text{J}$   
 $P \sim 5-10 \text{ MW}$

→ Ne:

$\lambda \sim 10-15 \text{ nm}$   
 $E \sim 30 \text{ nJ}$   
 $P \sim 1 \text{ MW}$

# Modulator



Can be used as :

- a **sub-harmonic modulator** for the SPARC undulator at large K (seeding)
- an **additional undulator to increase the SPARC UM length** at small K (SASE)

# Seeding with Ne @ 13.5 nm

Ne (after matching to the e-beam)

$\lambda \sim 13.5$  nm

$E \sim 2$  nJ

$P \sim 35$  kW

$\delta t \sim 50$  fs  $\sim 6$   $\mu$ m



$\lambda_u = 4.2$  cm

$K = 3$

5 UM

48 periods each

$\lambda_{res} \sim 13.5$  nm

$\lambda_u = 2.8$  cm

$K = 1.887$

2 UM 77 periods each

$\lambda_{res} \sim 4.5$  nm

Energy 100  $\mu$ J

N ph.  $2.5 \times 10^{12}$

Linewidth  $1.5 \times 10^{-4}$

Coher. Len. 16  $\mu$ m

$\lambda_u = 2.8$  cm

$K = 0.88$

4 UM 77 periods each

$\lambda_{res} \sim 2.26$  nm

Energy 4  $\mu$ J

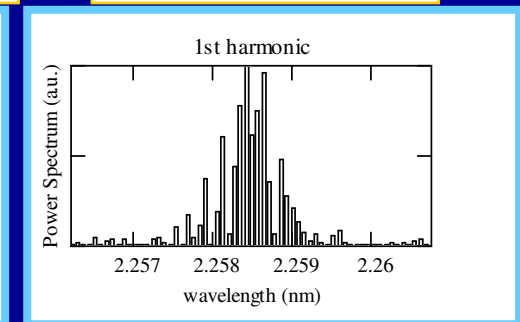
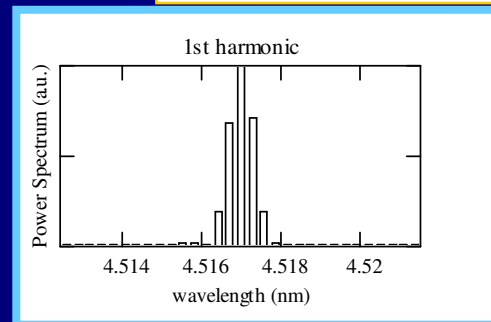
N ph.  $5 \times 10^{10}$

Linewidth  $3 \times 10^{-4}$

Coher. len. 5  $\mu$ m

Beam Energy  
Peak Current  
Slice en. spread  
Slice emittance

1.5 GeV  
1.5 kA  
 $< 2 \times 10^{-4}$   
 $< 1$  mm-mrad



# Seeding to increase longitudinal coherence: HHG in Ar + Monochromator

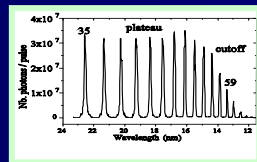
Ar

$\lambda \sim 30 \text{ nm}$

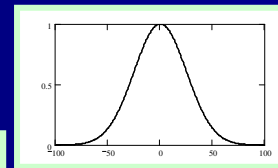
$E \sim 0.4 \mu\text{J}$

$P \sim 8 \text{ MW}$

$\delta t \sim 50 \text{ fs} \sim 6 \mu\text{m}$



Monochromator



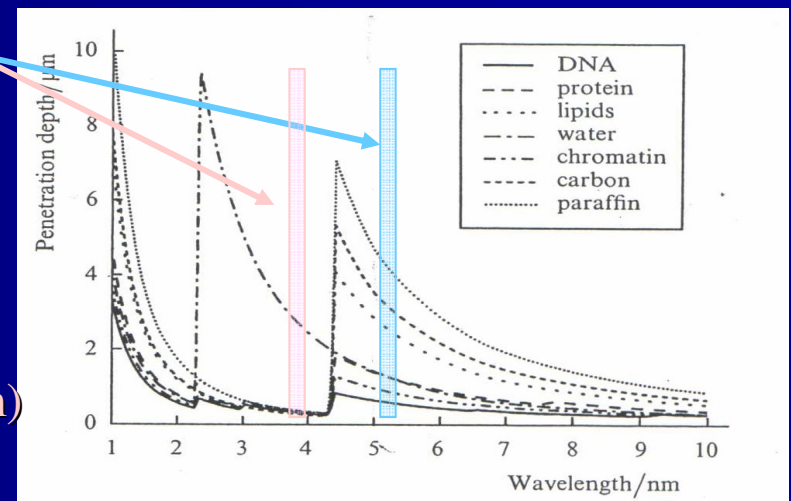
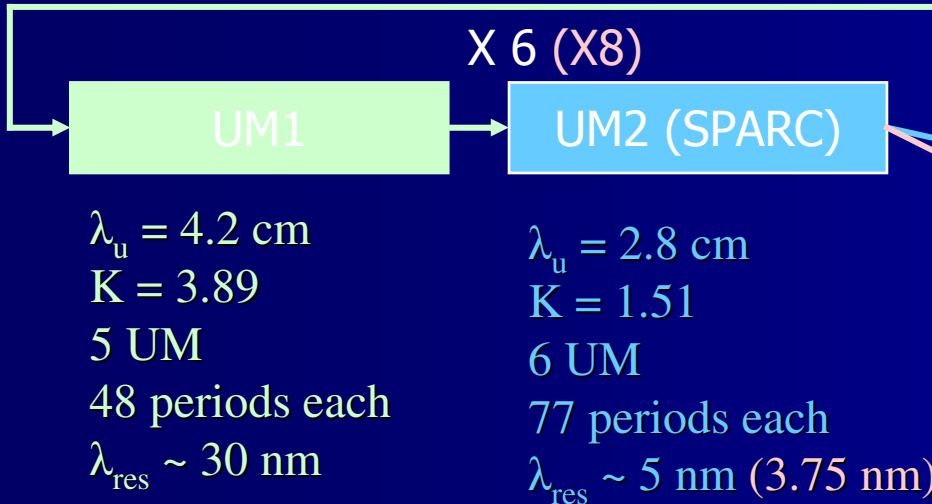
$\lambda \sim 30 \text{ nm}$

$E_f = \eta_m E_i \sim 0.6 \text{ nJ}$

$P_f \sim 3 \text{ kW}$

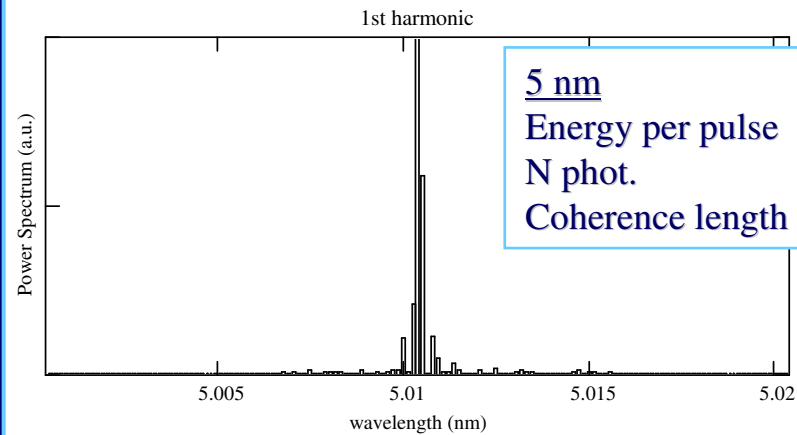
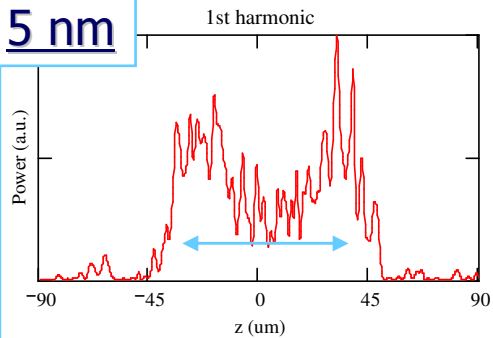
$c\delta t_f \sim 60 \mu\text{m}$

$$\eta_m = 0.08 \times 0.5 \times 0.25 \times \delta t_i / \delta t_f$$



# HHG in Ar + monochromator cont.

5 nm



5 nm

Energy per pulse

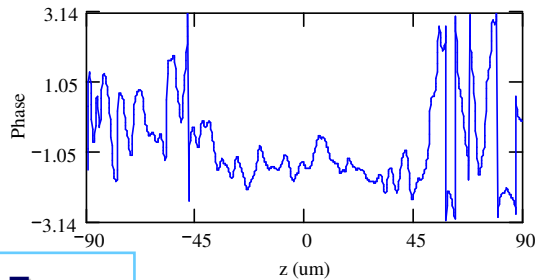
~ 100  $\mu$ J

N phot.

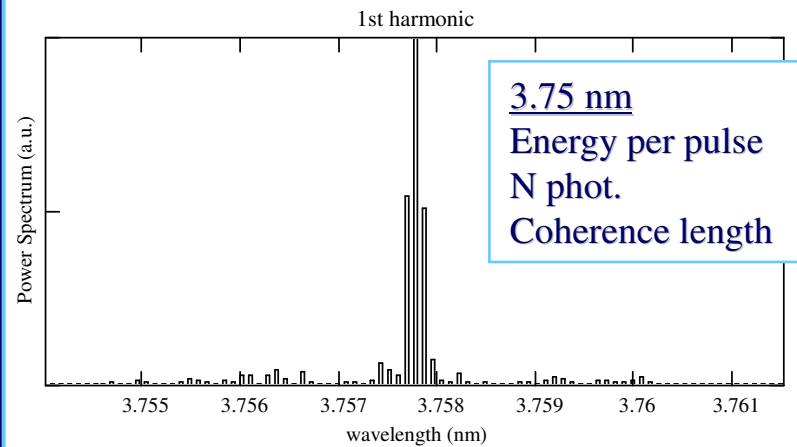
~  $2 \times 10^{12}$

Coherence length

~ 45  $\mu$ m



5 nm



3.75 nm

Energy per pulse

~ 10  $\mu$ J

N phot.

~  $1 \times 10^{11}$

Coherence length

~ 30  $\mu$ m

# Very short pulse generation

Submitted to Journal of Applied Physics - <http://jap.aip.org>

Non linear Pulse Evolution in Seeded Free-Electron Laser Amplifiers  
and in Free-Electron Laser Cascades

L. Giannessi,<sup>1</sup> P. Musumeci,<sup>2</sup> and S. Spampinati<sup>1</sup>

## Superradiance + Multiple stages cascaded FEL

- **Simpler cascade scheme** with many stages (no Fresh bunch required)
- **Reduced sensitivity** to tolerances and fluctuations
- **Pulse shape determined by FEL dynamics**
- **Sub-fs pulses**



# Superradiant Cascade

**Ti:Sa 3° harm (after matching to the e-beam)**

$\lambda \sim 266 \text{ nm}$

$E \sim 3.8 \mu\text{J}$

$P \sim 225 \text{ MW}$

$\delta t \sim 16 \text{ fs}$

**PRE MOD.**

X 8

**UM1 MOD.**

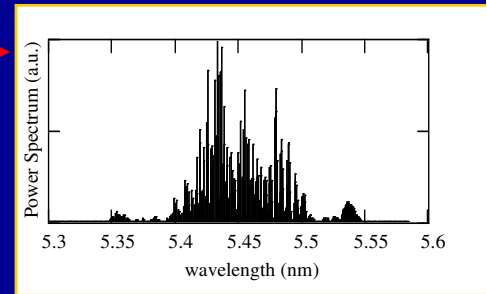
X 6

**UM1 MOD.**

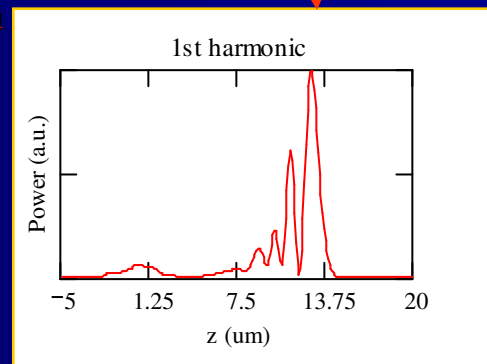
$\lambda_u = 10 \text{ cm}$   
 $K = 9.5$   
 50 periods  
 $\lambda_{\text{res}} \sim 260 \text{ nm}$

$\lambda_u = 4.2 \text{ cm}$   
 $K = 4.9$   
 2x48 periods  
 $\lambda_{\text{res}} \sim 35 \text{ nm}$

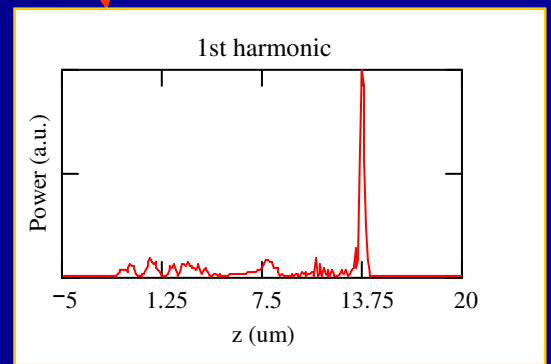
$\lambda_u = 4.2 \text{ cm}$   
 $K = 1.5$   
 3x48 periods  
 $\lambda_{\text{res}} \sim 5 \text{ nm}$



Beam Energy 1.5 GeV  
 Peak Current 1.8 kA  
 Slice en. spread  $< 1.3 \cdot 10^{-4}$   
 Slice emittance  $< 1 \text{ mm-mrad}$



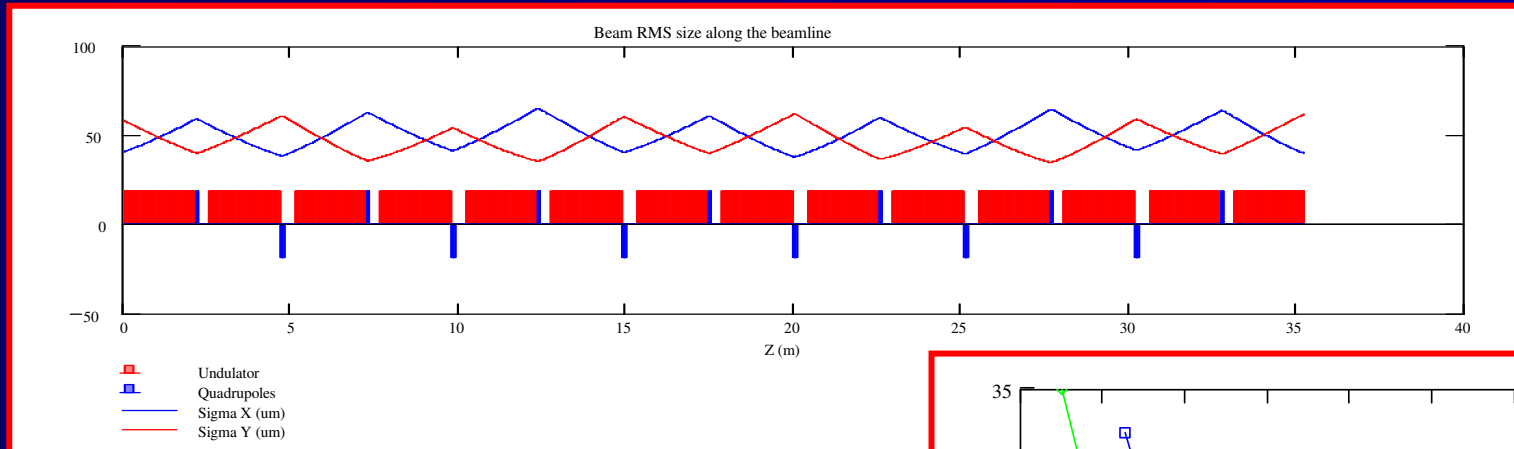
Energy 40  $\mu\text{J}$   
 N ph.  $7 \times 10^{12}$   
 Duration 4.3 fs (fwhm)



Energy 1.6  $\mu\text{J}$   
 N ph.  $4 \times 10^{10}$   
 Duration 1 fs (fwhm)

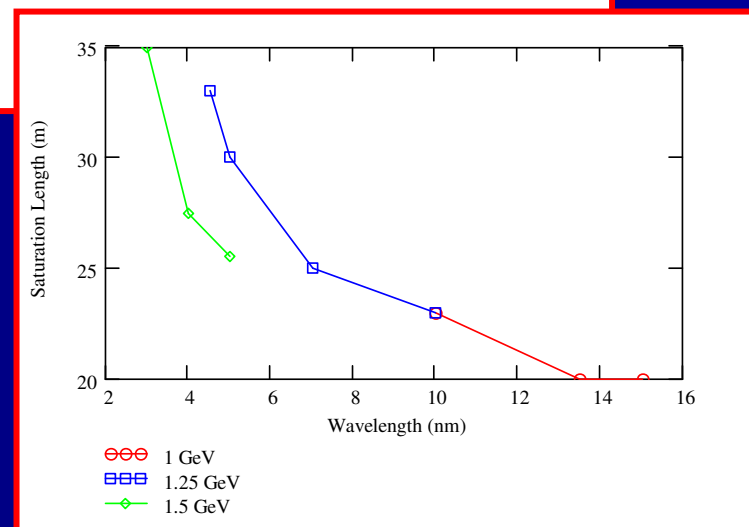
# Undulator optics & saturation length

- SPARC Undulator sections 2.156 m + 40 cm gaps



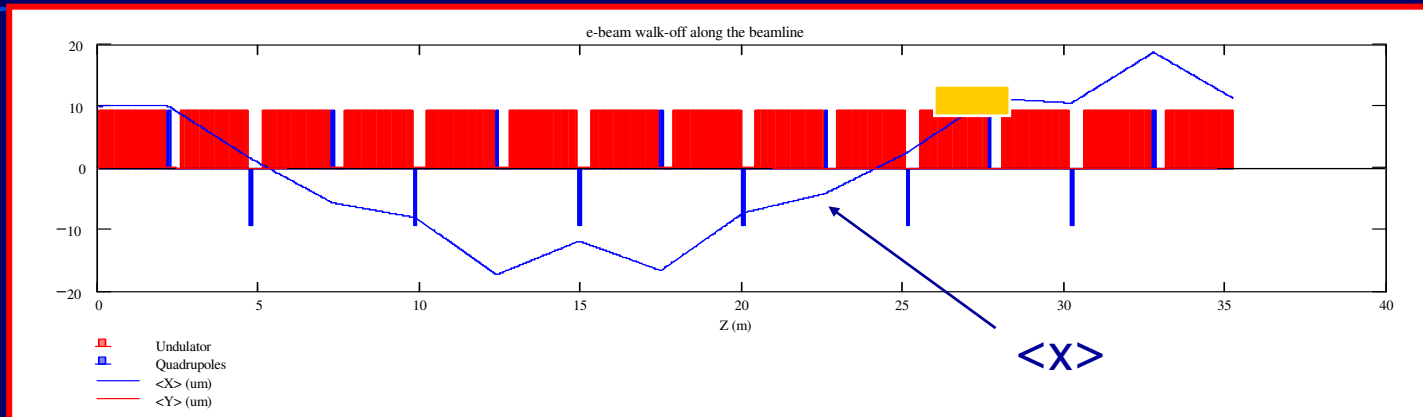
Average beta 6 m

The saturation length with the Modulator + Sparc undulator is 10-20 % larger



# Pointing Stability

$\Delta x = 10 \mu\text{m}$

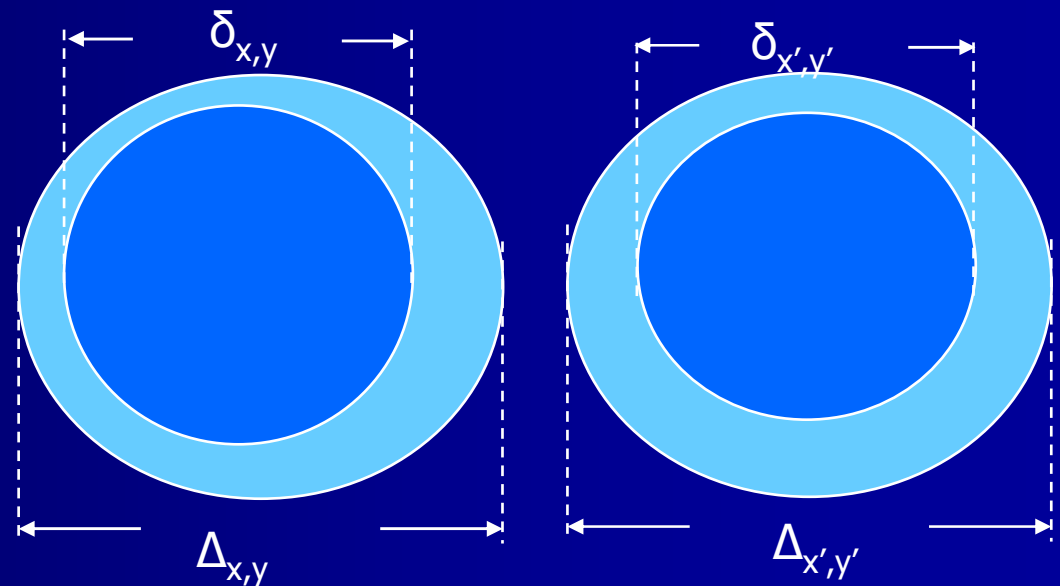


$\delta_{x,y,x',y'} = \text{source size}$

$$\Delta_{x,y,x',y'} = [(\delta_{x,y,x',y'})^2 + (J_{x,y,x',y'})^2]^{1/2}$$

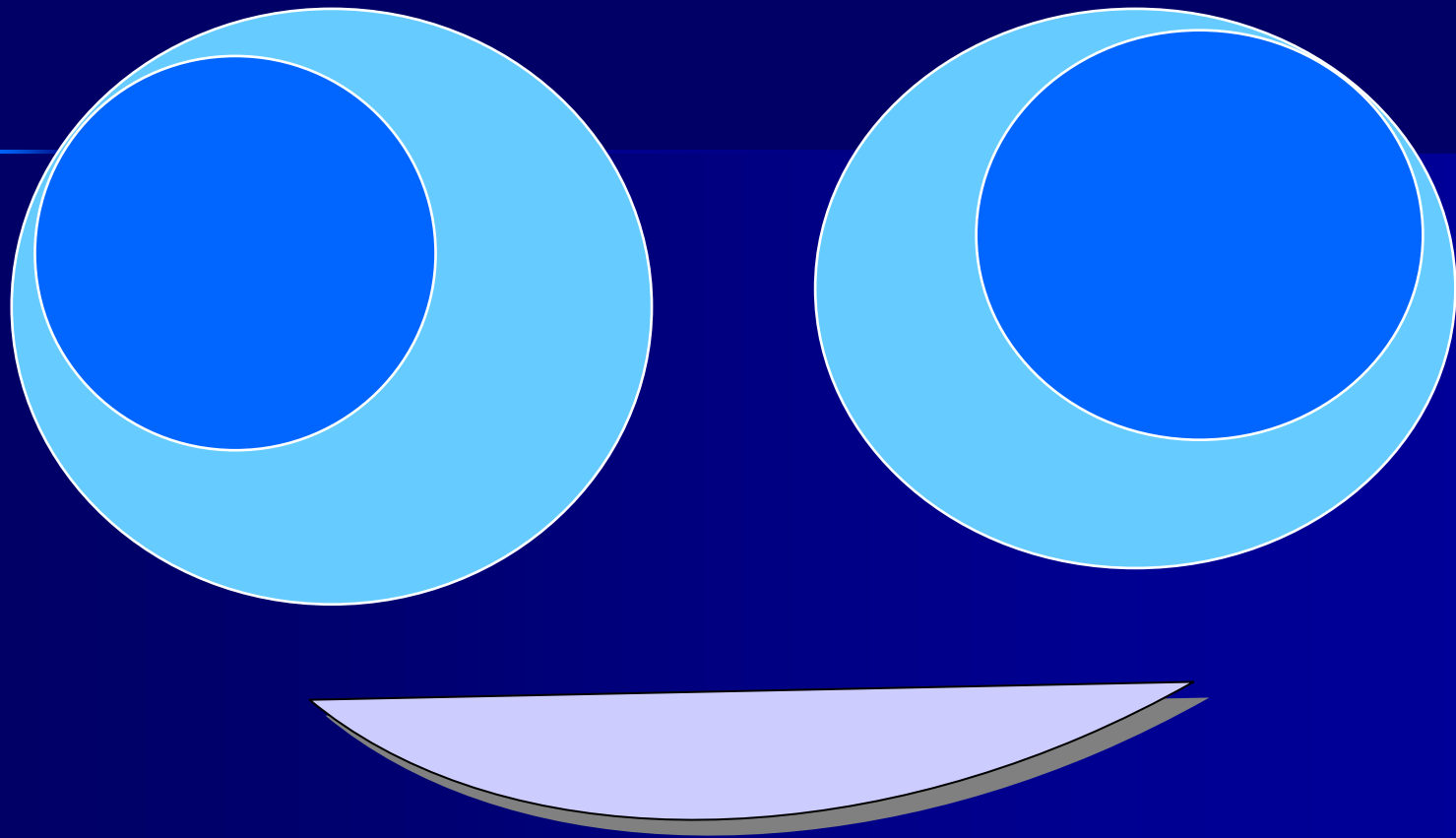
Beta=6m,  $\Delta x = 10 \mu\text{m}$

$J_{x,y} \sim 15 \mu\text{m}$   
 $J_{x',y'} \sim 4 \mu\text{rad}$



# Conclusions

- Several sample configurations have been analysed
  - SASE in the range 3 – 15 nm
  - Seeded with cascade from Ne@13.5nm
  - Seeded with cascade from Ar@30nm+monochromator
  - Seeded in superradiant mode for very short pulses
- This is a preliminary study
  - The linac configuration is still under study,
  - The simulations parameters have been only partially optimized
- The **experience @ SPARC in the UV – VUV is fundamental** for testing many of the ideas about seeding and cascaded FEL configurations



**... buon lavoro**