

**PHOKHARA 2008**  
**a report**  
**on the status of the program**

**H. CZYŻ, IF, UŚ, Katowice,**      **BEIJING 2008**

**in collaboration with**

**A. Grzelińska, J. H. Kühn, E. Nowak-Kubat,  
G. Rodrigo and A. Wapienik**

# The outline of the talk

The radiative return: a primer

- ▶ motivation
- ▶ theoretical basis
- ▶ radiative return: a tool in hadronic physics
- ▶ FSR: problems and how to deal with them
- ▶  $\pi\pi/\mu\mu$

PHOKHARA and its tests

The implemented hadronic currents

Plans

# The reason we need $R(s)$

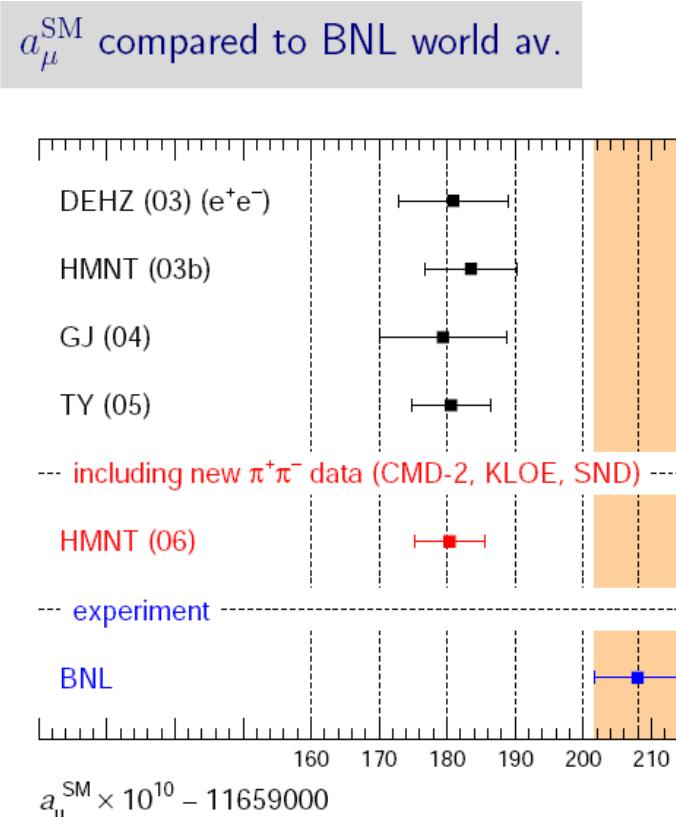
$$a_\mu^{\text{had,LO}} = \frac{\alpha^2}{3\pi^2} \int_{4m_\pi^2}^\infty \frac{ds}{s} K(s) R(s)$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma_{\text{point}}}$$

One has to measure :

$$\sigma(e^+e^- \rightarrow \text{hadrons})$$

# $a_\mu$ , T. Teubner, Liverpool



DEHZ 06:  $180.5 \pm 5.6$  [3.3  $\sigma$ ]  
 Jegerlehner 06:  $179.3 \pm 6.8$  [3.2  $\sigma$ ]

.. Discrepancy increased .. still not fully conclusive .. constrain SUSY ..

## Recent changes

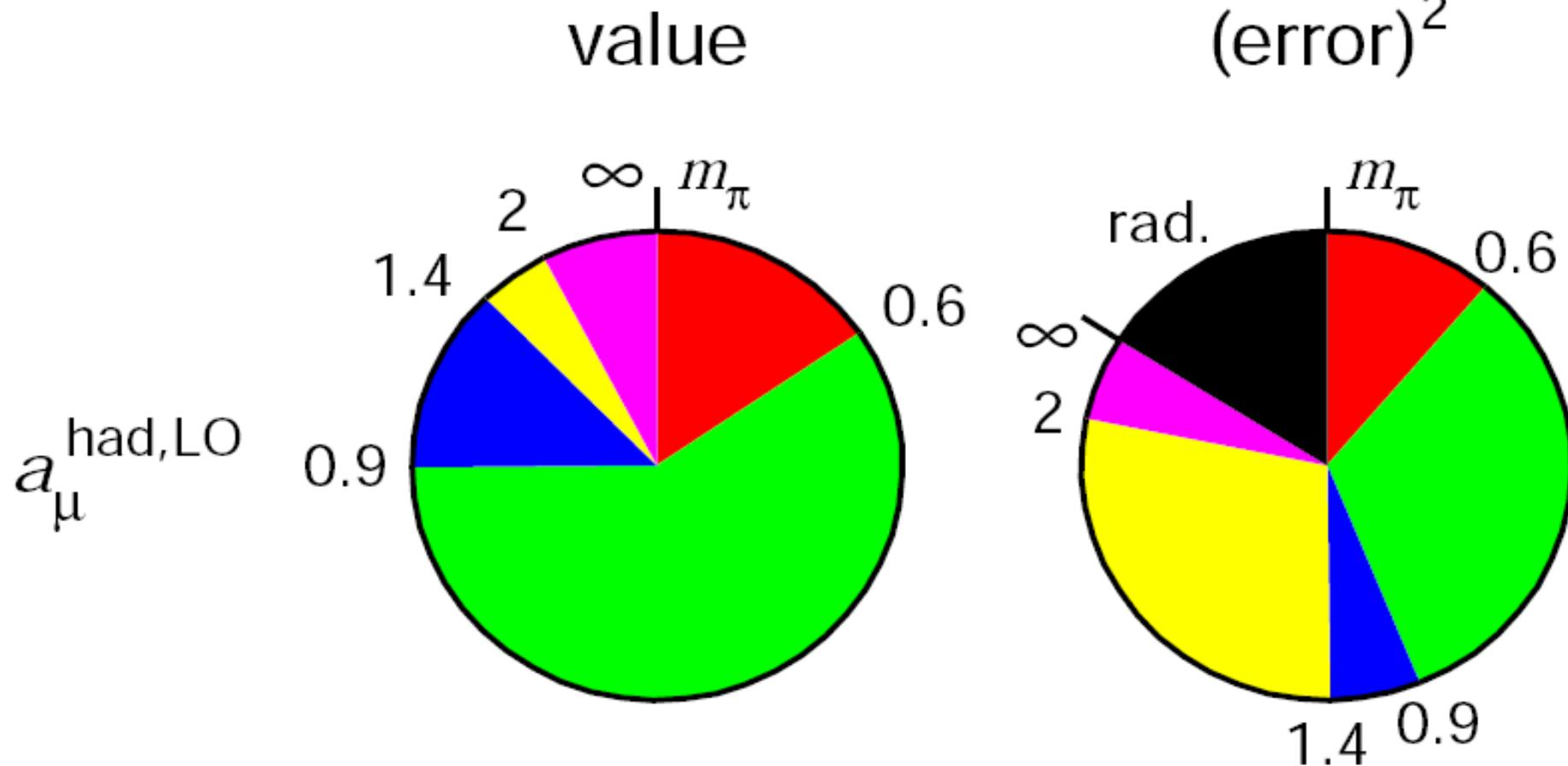
**TH:** Update of QED, up to 5-loop, new  $\alpha$ :  
 was:  $(116\ 584\ 719.35 \pm 1.43) \cdot 10^{-11}$   
 → is now:  $(116\ 584\ 718.09 \pm 0.16) \cdot 10^{-11}$

**TH:** Improved LO hadr. (from  $e^+e^-$ ):  
 Now, with new CMD-2, SND, KLOE:  
 $(6924 \pm 64) \cdot 10^{-11} \rightarrow (6894 \pm 46) \cdot 10^{-11}$

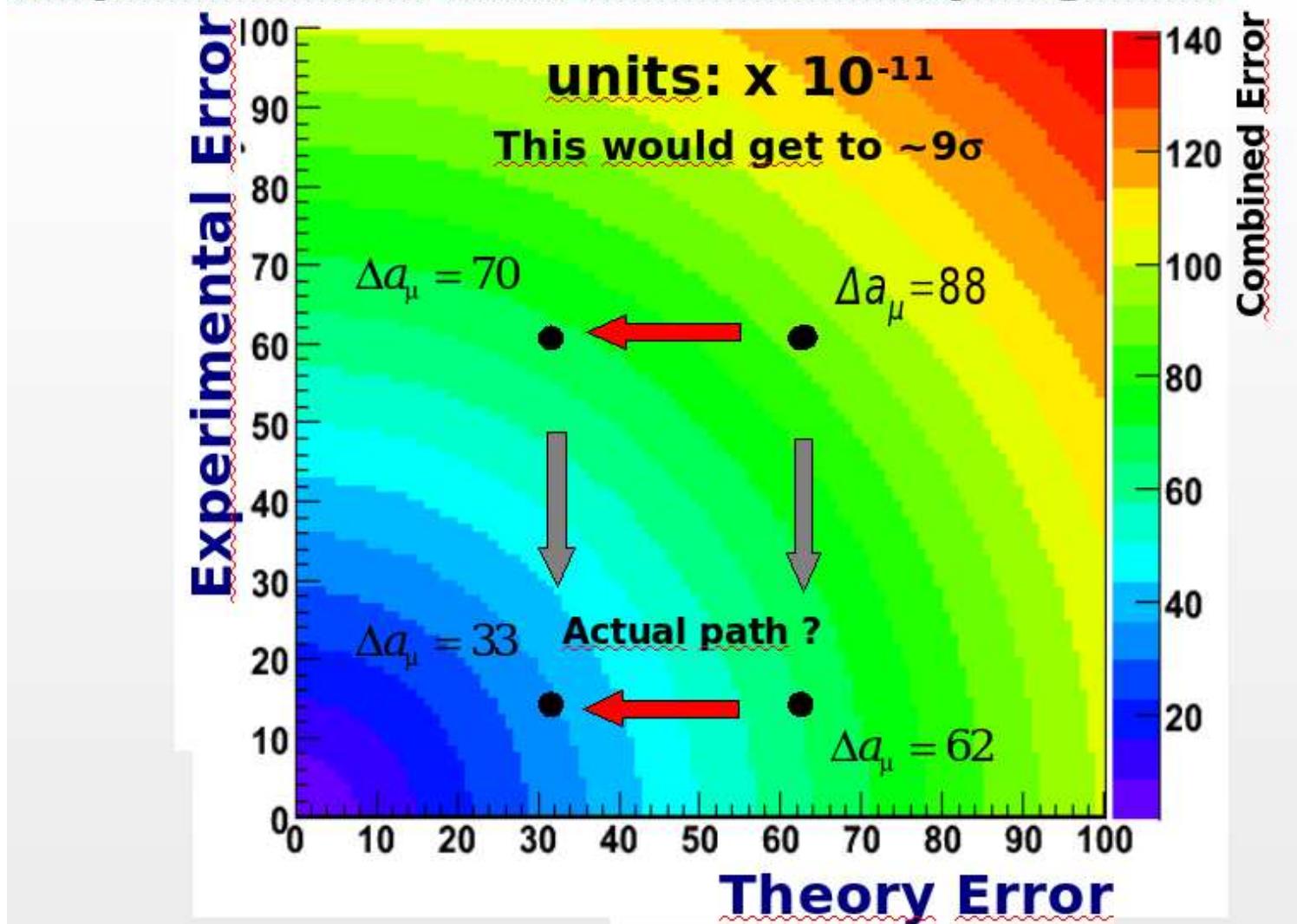
**EXP:** BNL's '01  $\mu^-$  data [PRL92(2004)161802]:  
 $a_{\mu^-} = 11\ 659\ 214(8)(3) \times 10^{-10}$  (0.7 ppm)  
 →  $a_\mu = 116\ 592\ 080(63) \times 10^{-11}$  (0.5 ppm)

► With this input HMNT get:  
 $a_\mu^{\text{EXP}} - a_\mu^{\text{TH}} = (27.6 \pm 8.1) \cdot 10^{-10}$ ,  $\sim 3.4\sigma$

# $a_\mu$ , T. Teubner, Liverpool



$\Delta a_\mu$  improvement requires both experimental and theoretical progress



## Conclusions and Prospects

At present, large  $N_c$  results agree within  $1\ \sigma$  ✓

$$a_\mu^{\text{lbl}} = (11.0 \pm 4.0) \times 10^{-10}$$

More work needed to have the hadronic light-by-light contribution to muon  $g - 2$  with reduced uncertainty •

Goal: To have under control model dependences •

# $a_\mu$ , BaBar preliminary

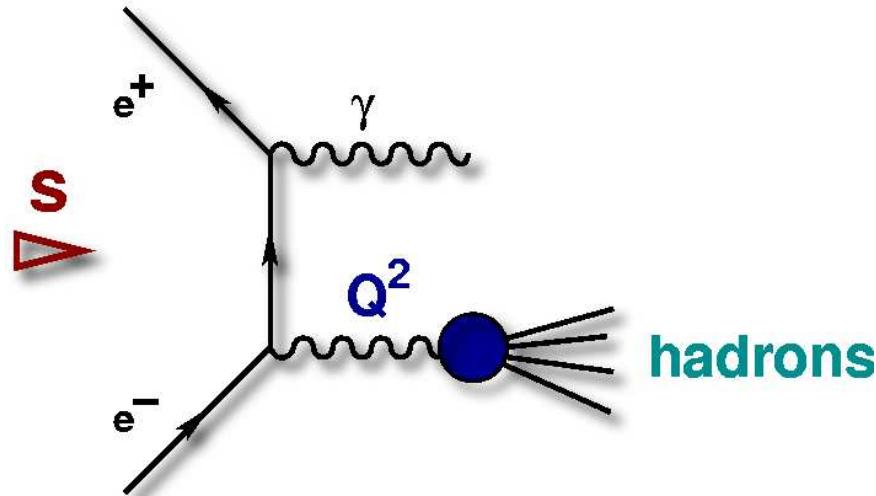
## Conclusions

- BaBar analysis of  $\pi\pi$  and  $\mu\mu$  ISR processes completed
- Precision goal has been achieved: 0.6% in  $\rho$  region (0.6-0.9 GeV)
- Absolute  $\mu\mu$  cross section agrees with NLO QED within 1.2%
- Preliminary results available for  $\pi\pi$  in the range 0.5-3 GeV
- Structures observed in pion form factor at large masses
- Comparison with results from earlier experiments
  - discrepancy with CMD-2 and SND mostly below  $\rho$
  - large disagreement with KLOE
  - better agreement with  $\tau$  results, especially Belle
- Contribution to  $a_\mu$  from BaBar agrees better with  $\tau$  results
- Deviation between BNL measurement and theory prediction significantly reduced using BaBar  $\pi\pi$  data
- $a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (27.5 \pm 8.4) \times 10^{-10} \Rightarrow (14.0 \pm 8.4) \times 10^{-10}$
- Wait for final results and contributions of multi-hadronic modes

# THE RADIATIVE RETURN METHOD

$$d\sigma(e^+e^- \rightarrow \text{hadrons} + \gamma(\text{ISR})) =$$

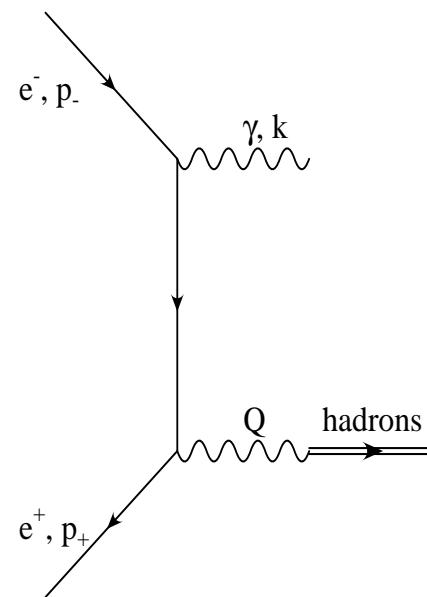
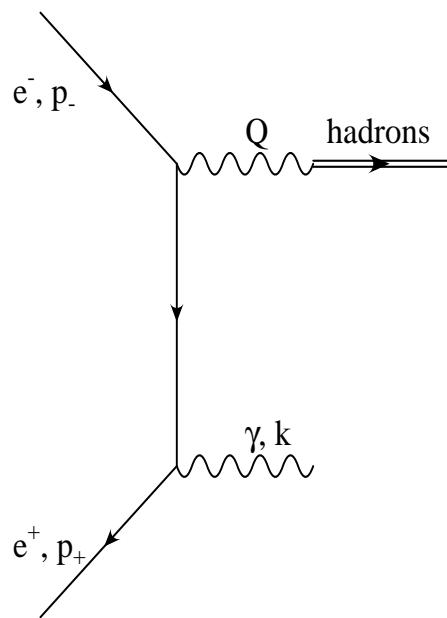
$$H(Q^2, \theta_\gamma) d\sigma(e^+e^- \rightarrow \text{hadrons})(s = Q^2)$$



- ▶ measurement of  $R(s)$  over the full range of energies, from threshold up to  $\sqrt{s}$
- ▶ large luminosities of factories compensate  $\alpha/\pi$  from photon radiation
- ▶ radiative corrections essential (NLO,...)

High precision measurement of the hadronic cross-section  
at meson-factories

# BASIC IDEA - more details



$$\mathcal{M} \sim \bar{v}(p_+) \left[ \gamma^\nu \frac{1}{p_- - k' - m} \epsilon^*(k) + \epsilon^*(k) \frac{1}{k' - p_+ - m} \gamma^\nu \right] u(p_-)$$

$$\frac{1}{Q^2} J_\nu^{em} .$$

# BASIC IDEA - more details

$$\mathcal{M} \sim \bar{v}(p_+) \left[ \gamma^\nu \frac{1}{\not{p}_- - \not{k}' - m} \epsilon^*(k) + \epsilon^*(k) \frac{1}{\not{k}' - \not{p}_+ - m} \gamma^\nu \right] u(p_-)$$

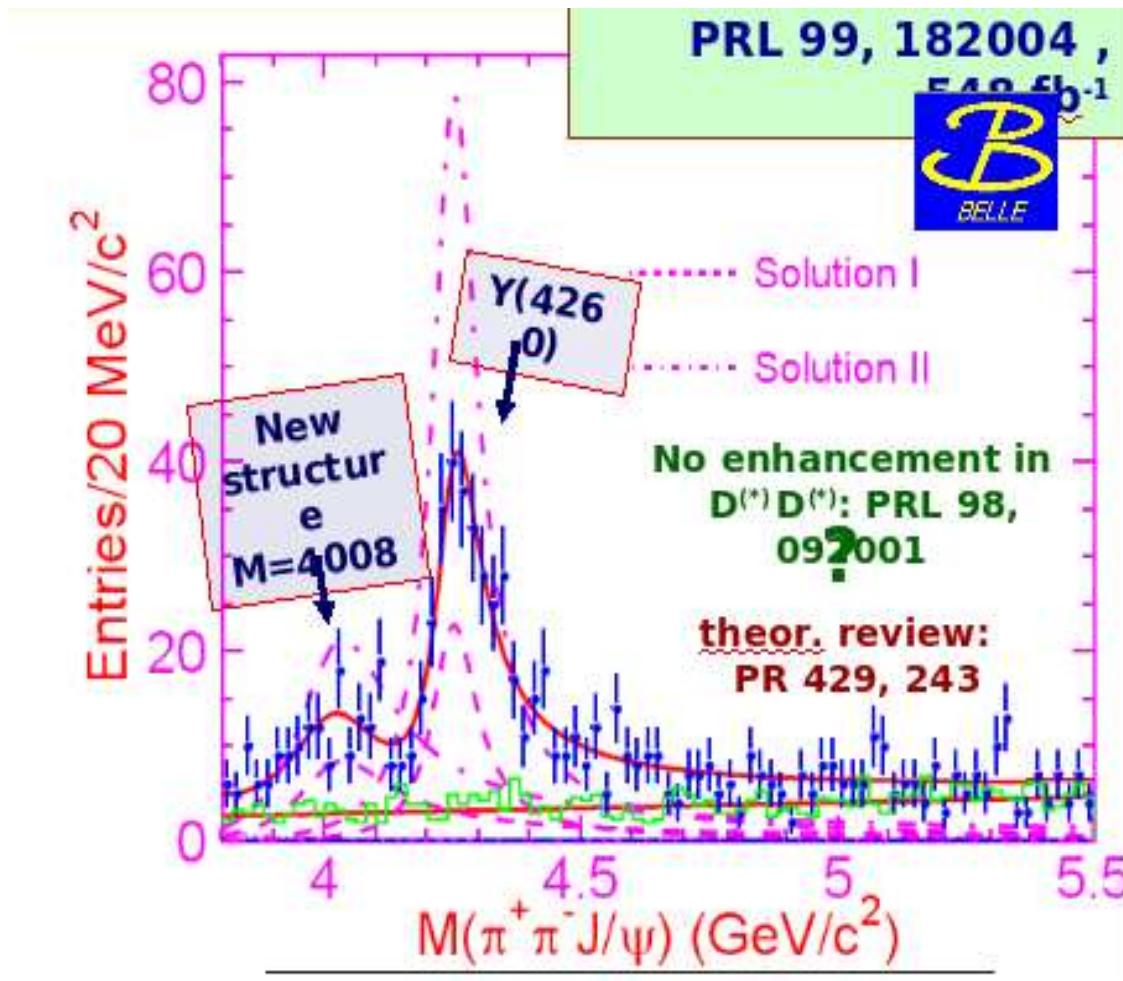
$$\frac{1}{Q^2} J_\nu^{em}.$$

$$\int J_\mu^{em} (J_\nu^{em})^* d\Phi_n(Q; q_1, \dots, q_n) =$$

$$\frac{1}{6\pi} (Q_\mu Q_\nu - g_{\mu\nu} Q^2) R(Q^2)$$

$$d\sigma(e^+e^- \rightarrow \text{hadrons} + \gamma) = H(Q^2, \theta_\gamma) d\sigma(e^+e^- \rightarrow \text{hadrons})$$

# Radiative return: a tool in hadronic physics



# From EVA to PHOKHARA

**EVA:**  $e^+e^- \rightarrow \pi^+\pi^-\gamma$

- tagged photon ( $\theta_\gamma > \theta_{cut}$ )
- ISR at LO + Structure Function
- FSR: point-like pions

[Binner et al.]

$e^+e^- \rightarrow 4\pi + \gamma$

- ISR at LO + Structure Function

[Czyż, Kühn, 2000]

H.C., A. Grzelinska,

J. H. Kühn, E. Nowak-Kubat,

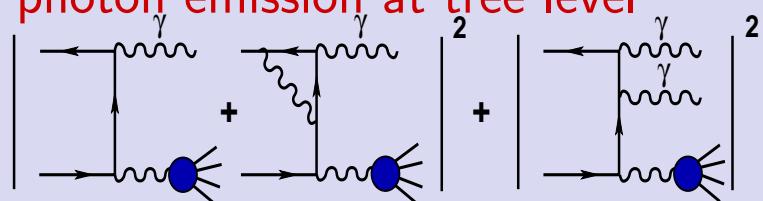
G. Rodrigo, A. Wapienik

**PHOKHARA 6.0:**  $\pi^+\pi^-$ ,  
 $\mu^+\mu^-$ ,  $4\pi$ ,  $\bar{N}N$ ,  $3\pi$ ,  $KK$ ,  
 $\Lambda(\rightarrow \dots) \bar{\Lambda}(\rightarrow \dots)$

- **ISR at NLO:** virtual corrections

to one photon events and two

photon emission at tree level



- FSR at NLO:  $\pi^+\pi^-$ ,  $\mu^+\mu^-$ ,  $K^+K^-$
- tagged or untagged photons
- Modular structure

<http://ific.uv.es/~rodrigo/phokhara/>

# Differential luminosity:

$$\frac{d\sigma}{dQ^2} (e^+ e^- \rightarrow \gamma + \text{had}(Q^2)) = \sigma (e^+ e^- \rightarrow \text{had}(Q^2))$$
$$\times \frac{\alpha}{\pi s} \left\{ \begin{array}{l} \frac{s^2+Q^4}{s(s-Q^2)} (\log(s/m_e^2) - 1) \\ \frac{s^2+Q^4}{s(s-Q^2)} \log \left( \frac{1+\cos\theta_{min}}{1-\cos\theta_{min}} \right) - \frac{s-Q^2}{s} \cos\theta_{min} \end{array} \right\}$$

$$\frac{dL}{dQ^2} (Q^2, s) = \frac{\alpha}{\pi s} \left\{ \dots \right\} L(\text{at } s)$$

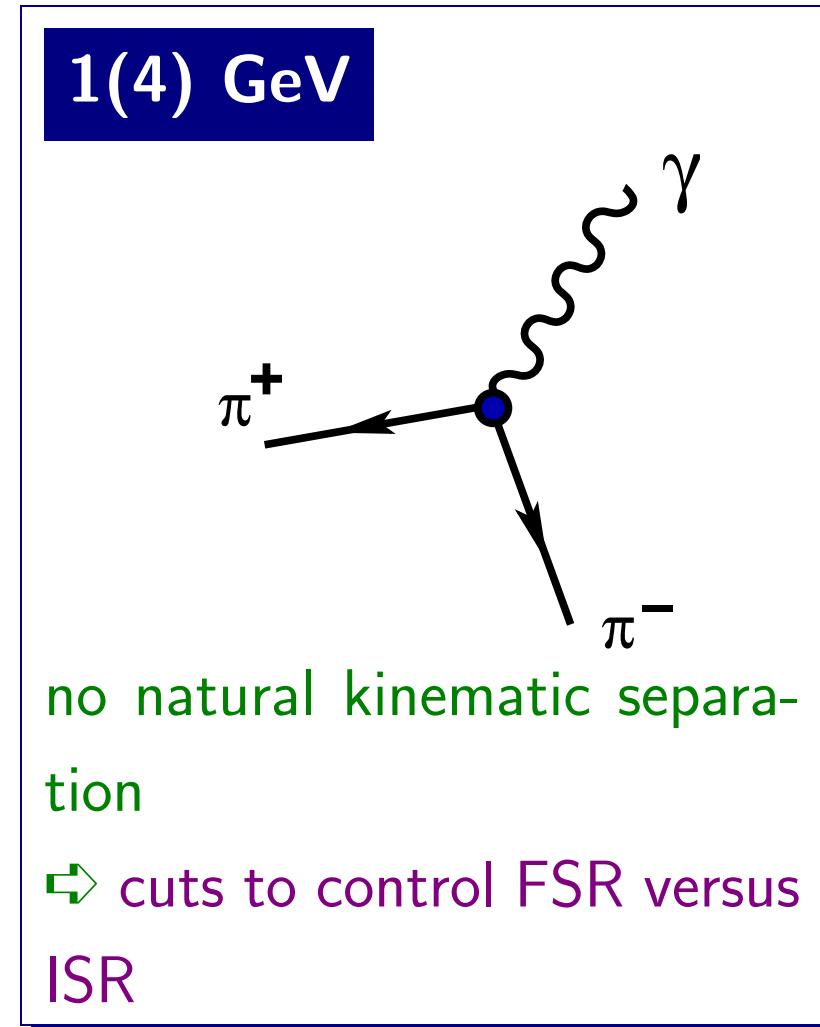
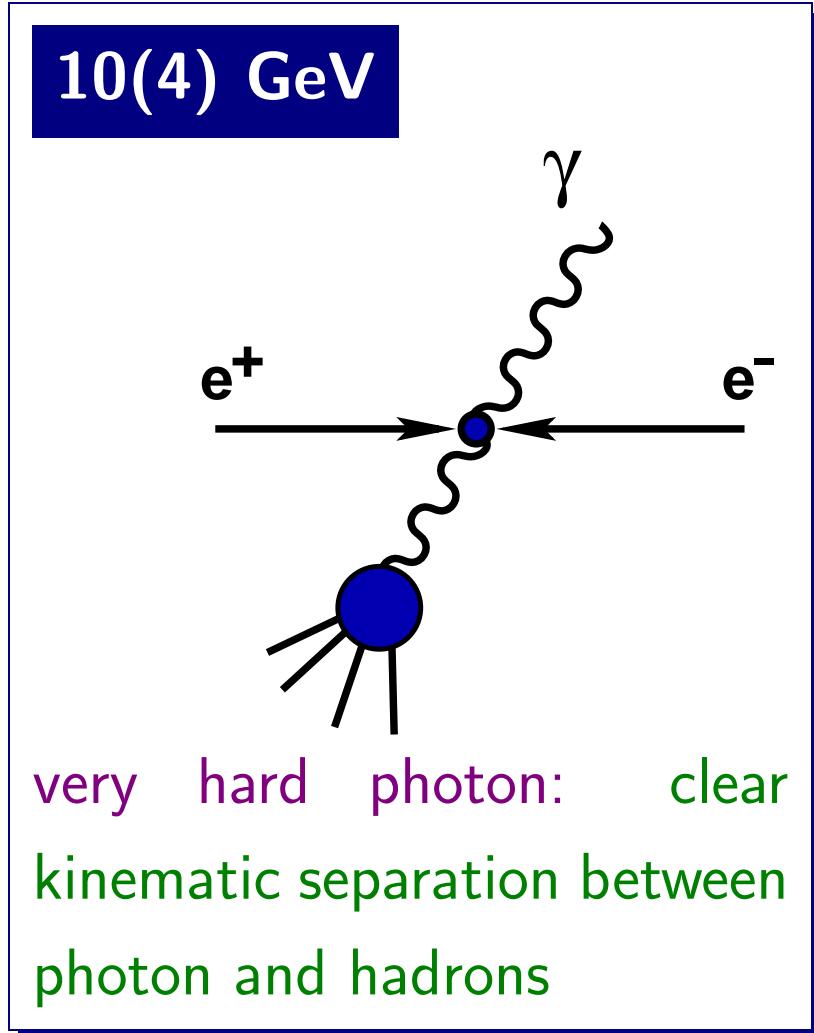
# Differential luminosity

$\theta_{min} = 20^\circ$ ,  $L(s) = 20 \text{ fb}^{-1}$ ,  $\Delta Q^2 = 0.1 GeV^2$

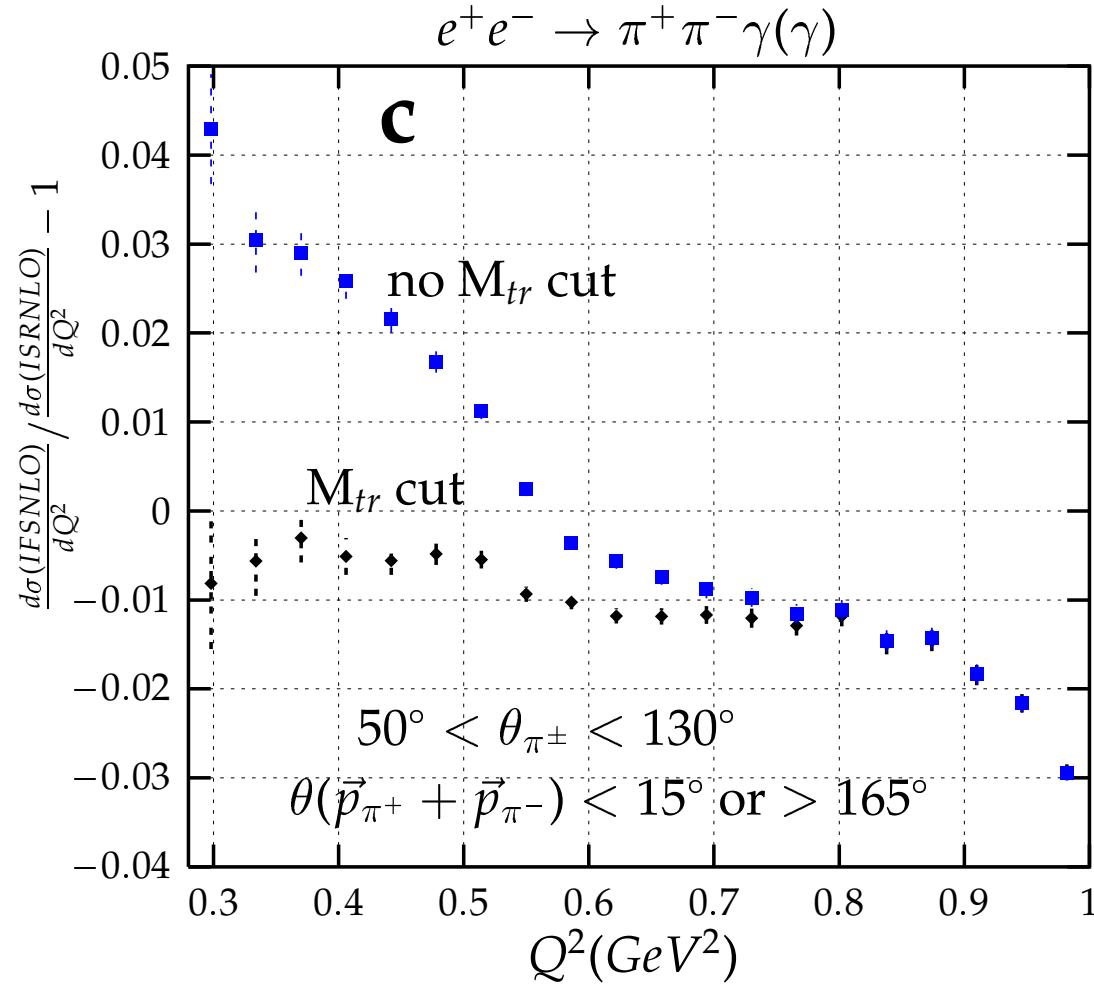
$$\frac{dL}{dQ^2}(Q^2, s) \Delta Q^2 \quad [pb^{-1}]$$

	$\sqrt{s} \text{ [GeV]}$			
$\sqrt{Q^2} \text{ [GeV]}$		0.7	1	2
	2	3.7	4.9	-
	3	1.4	1.6	3.6
	3.77	0.88	0.94	1.5

# DAΦNE versus B and c -factories: configurations in the cms - frame



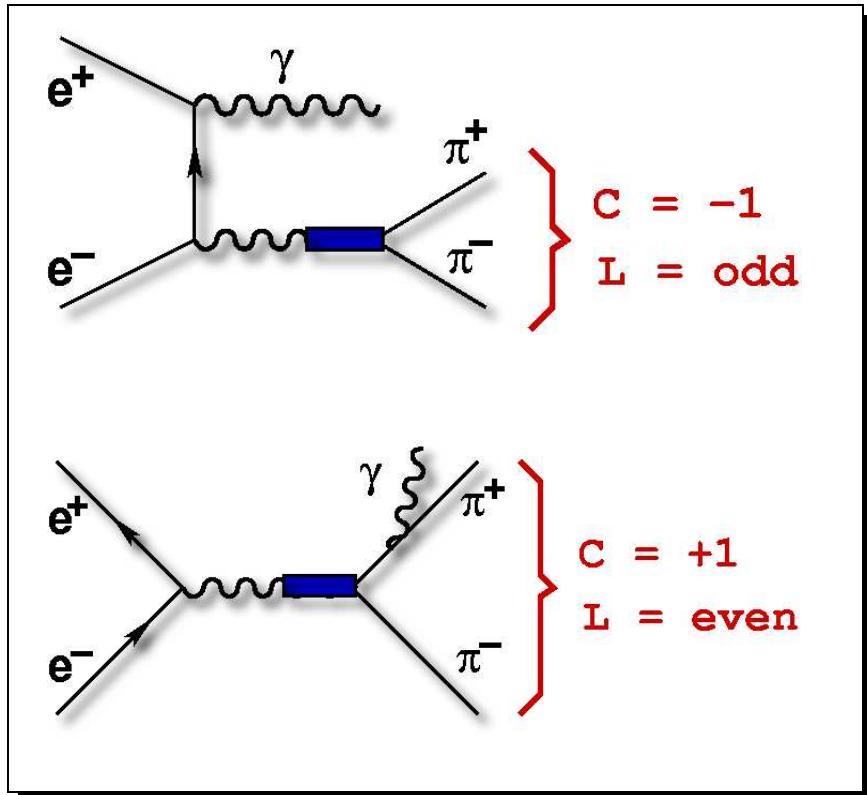
# Solution I: kill FSR



KLOE: small angle analysis

# Solution II: test of a FSR model

interference:

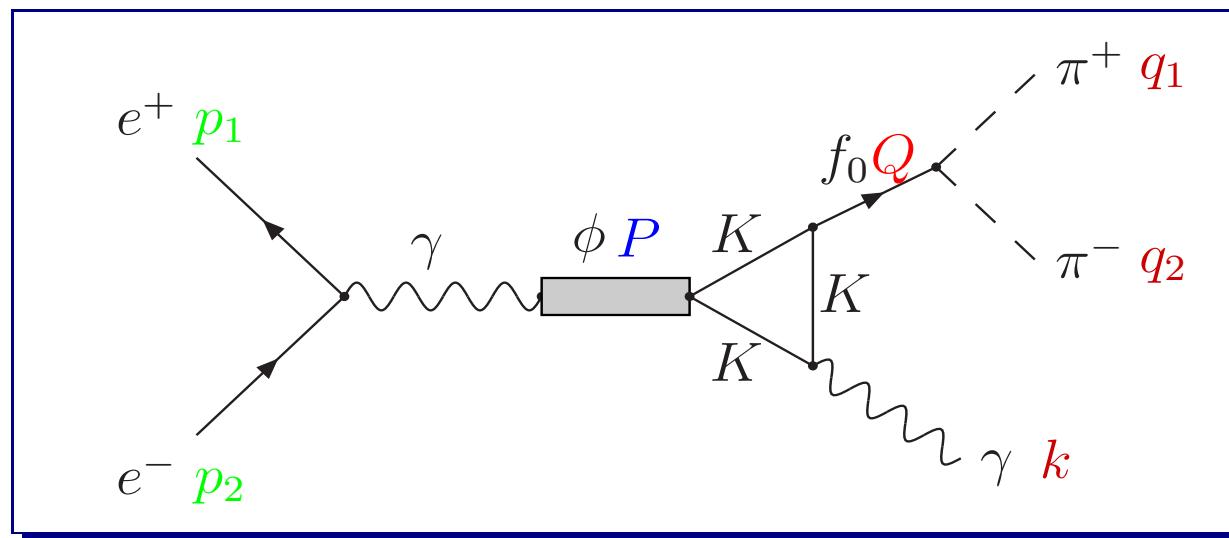
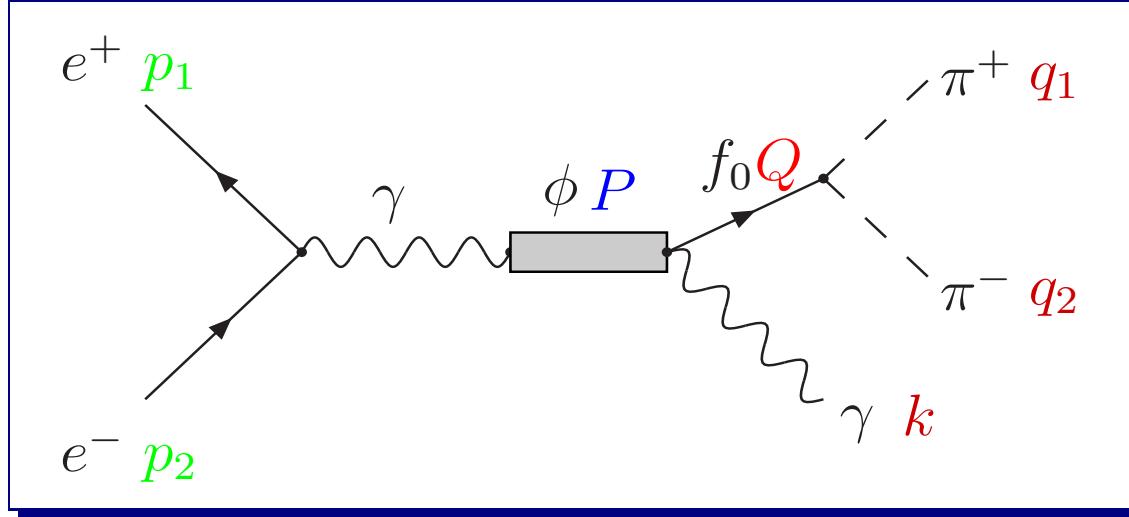


- ➡ interference odd  
under  $\pi^+ \leftrightarrow \pi^-$
- ➡ asymmetric differential  
distribution:  $\int \text{interf.} = 0$

$$A(\theta) = \frac{N^{\pi^+}(\theta) - N^{\pi^-}(\theta)}{N^{\pi^+}(\theta) + N^{\pi^-}(\theta)}$$

# FSR at KLOE, additional contributions:

$$e^+ e^- \rightarrow \phi^* \rightarrow (f_0(980)_{f_0} + f_0(600)_\sigma) \gamma \rightarrow \pi \pi \gamma$$



# Charge asymmetries

⇒ forward-backward asymmetry defined for  $\pi^+$

$$\mathcal{A}_{FB}(Q^2) = \frac{N(\theta_{\pi^+} > 90^\circ) - N(\theta_{\pi^+} < 90^\circ)}{N(\theta_{\pi^+} > 90^\circ) + N(\theta_{\pi^+} < 90^\circ)}(Q^2)$$

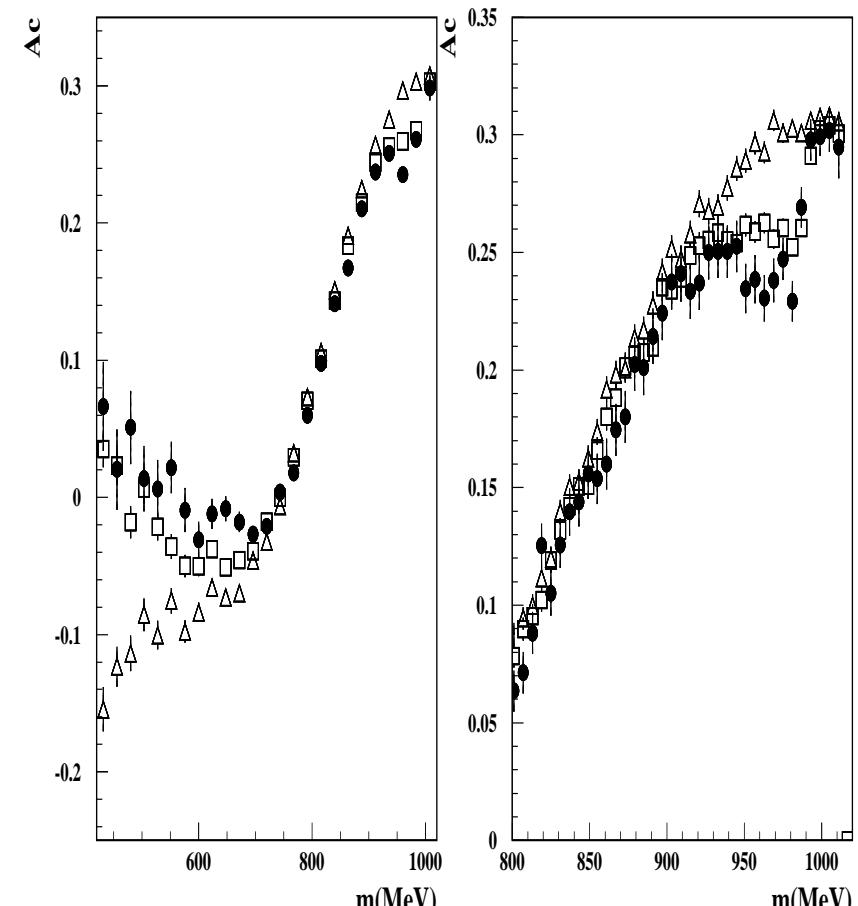
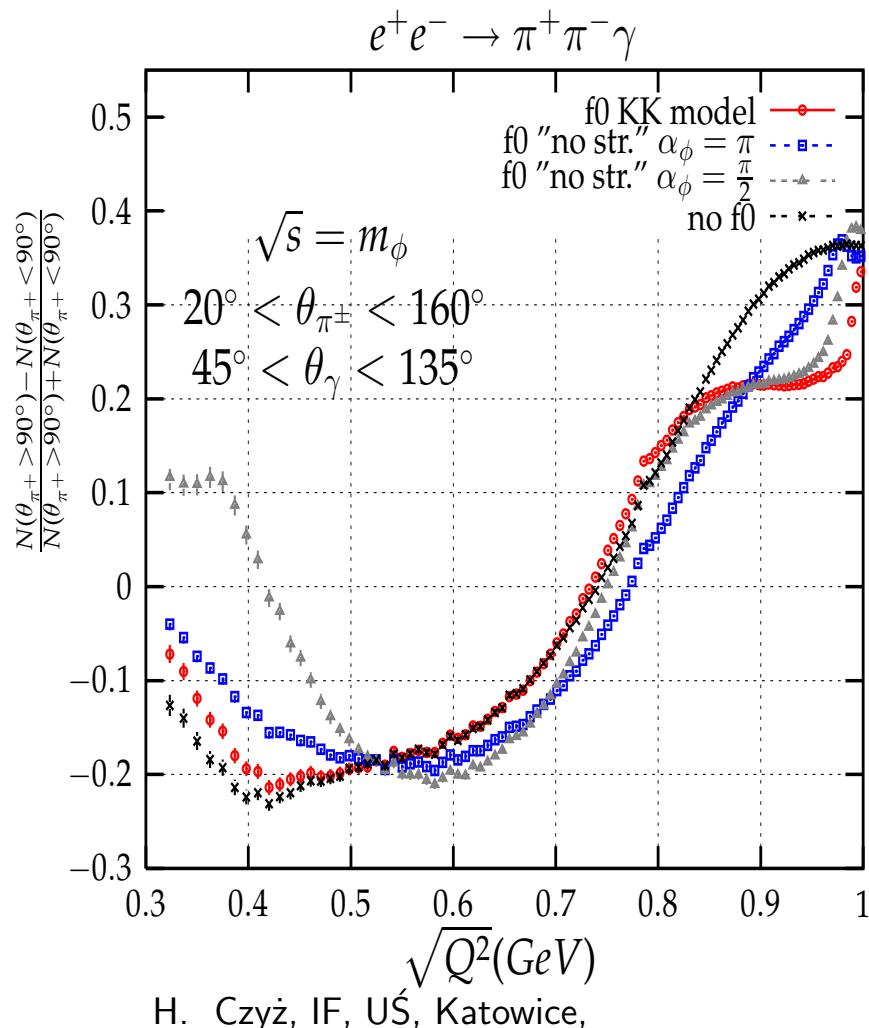
⇒ charge asymmetry

$$\mathcal{A}_C(\theta_\pi) = \frac{N(\pi^+) - N(\pi^-)}{N(\pi^+) + N(\pi^-)}(\theta_\pi)$$

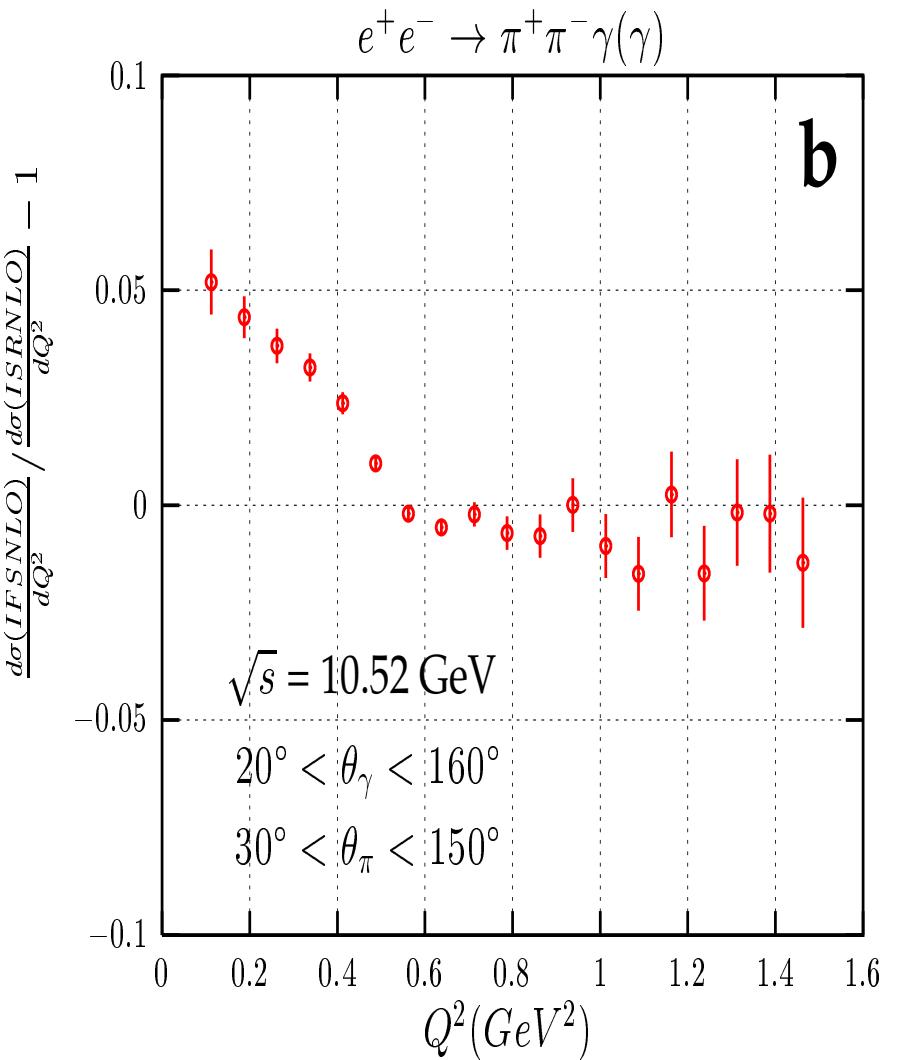
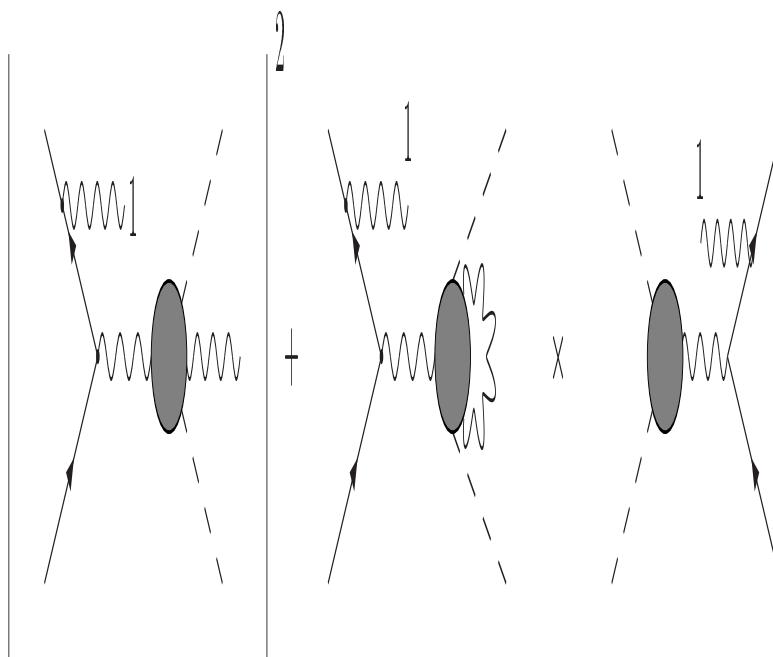
# Test of a FSR model

H. Czyż, A. Grzelińska and J. H. Kühn, Phys.Lett.B611:116,2005

KLOE Collaboration: Phys.Lett.B634:148,2006



# FSR at NLO

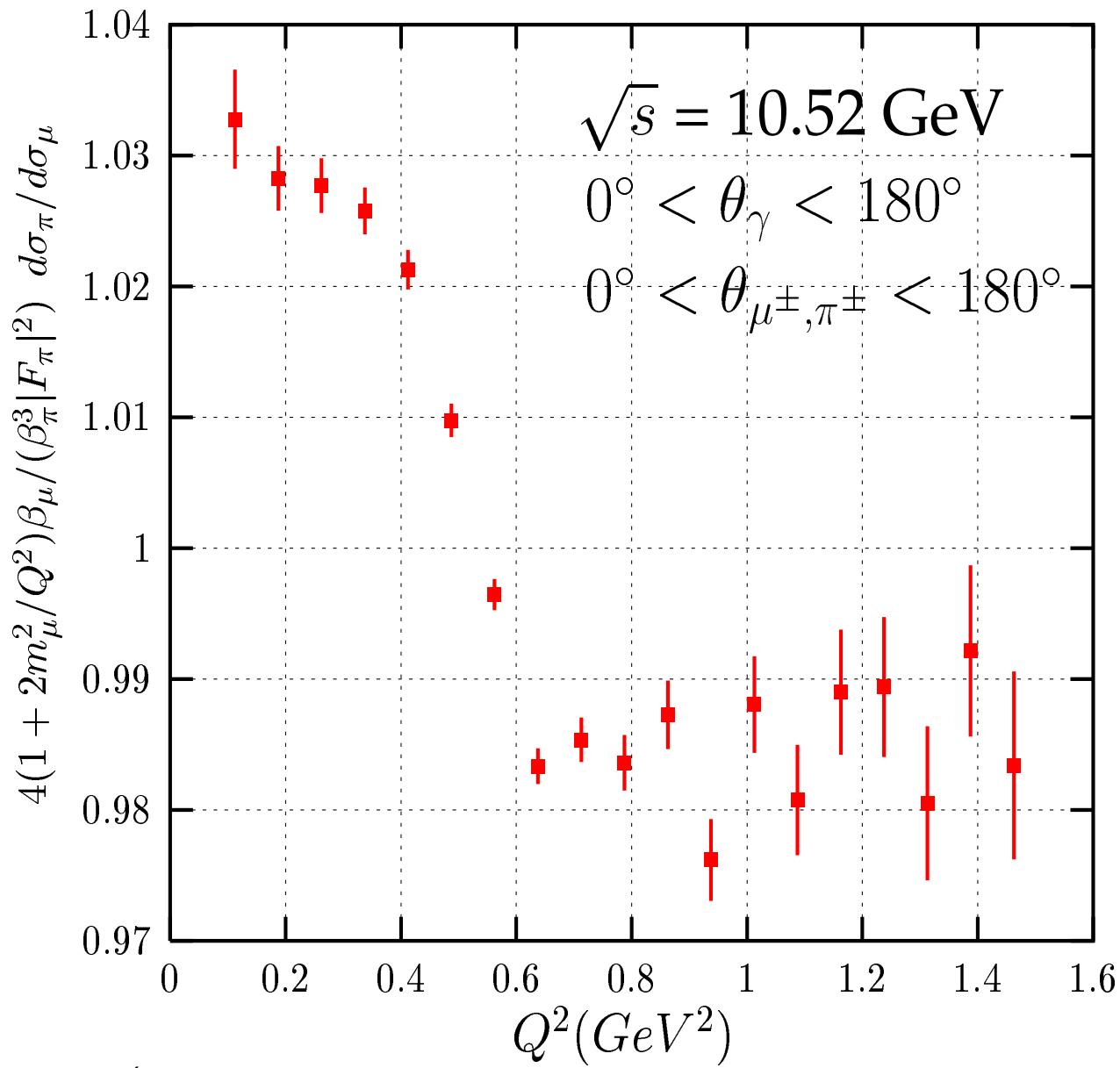


# $\pi\pi / \mu\mu$ ratio

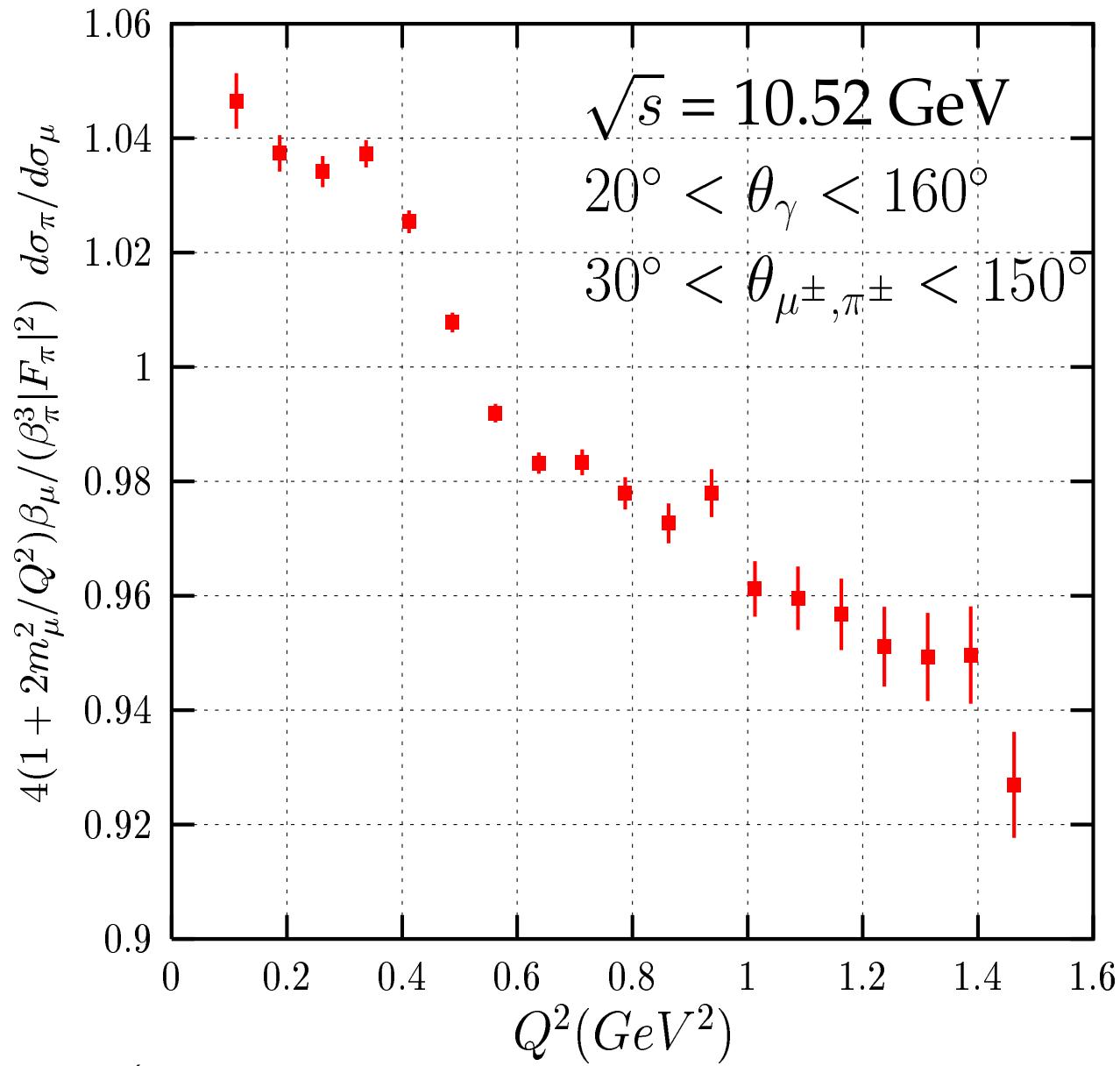
H. C., A. Grzelinska, J. H. Kuhn and G. Rodrigo  
Eur.Phys.J.C39:411-420,2005.

$$\mathcal{R}(Q^2) = \frac{4(1 + \frac{2m_\mu^2}{Q^2})\beta_\mu \frac{d\sigma_\pi}{dQ^2}}{\beta_\pi^3 |F_\pi(Q^2)|^2 \frac{d\sigma_\mu}{dQ^2}},$$

# $\pi\pi / \mu\mu$ ratio: FSRNLO



# $\pi\pi / \mu\mu$ ratio: FSRNLO



# From EVA to ...

$$e^+e^- \rightarrow 4\pi + \gamma$$

- ISR at LO + Structure Function

[Czyż, Kühn]

$$e^+e^- \rightarrow hadrons + \gamma$$

- upgraded by BaBar - AfkQED not public (?)
- PHOTOS [Barberio et al.] for FSR

$$\text{EVA: } e^+e^- \rightarrow \pi^+\pi^-\gamma$$

- tagged photon ( $\theta_\gamma > \theta_{cut}$ )
- ISR at LO + Structure Function
- FSR: point-like pions

[Binner et al.]

$$e^+e^- \rightarrow \pi^{+,0}\pi^{-,0} + \gamma$$

- FASTERD: FSR studies

[Panchari, Shekhovtsova, Venanzoni]

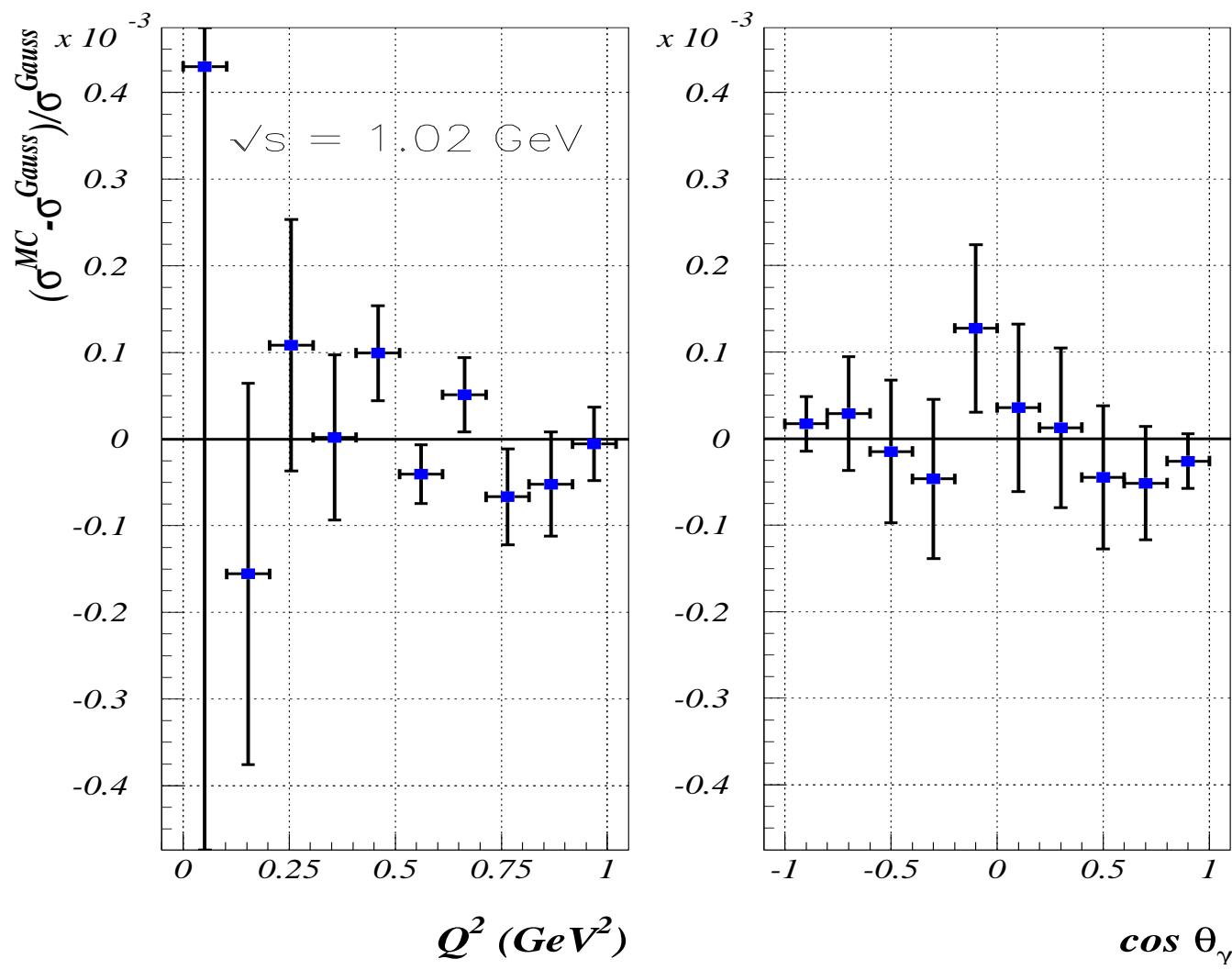
# PHOKHARA tests

- ⇒ matrix elements tests
- ⇒ generation tests
- ⇒ KKMC comparison + ...

S. Jadach, B. F. L. Ward and Z. Wąs, CPC 130:260,2000.

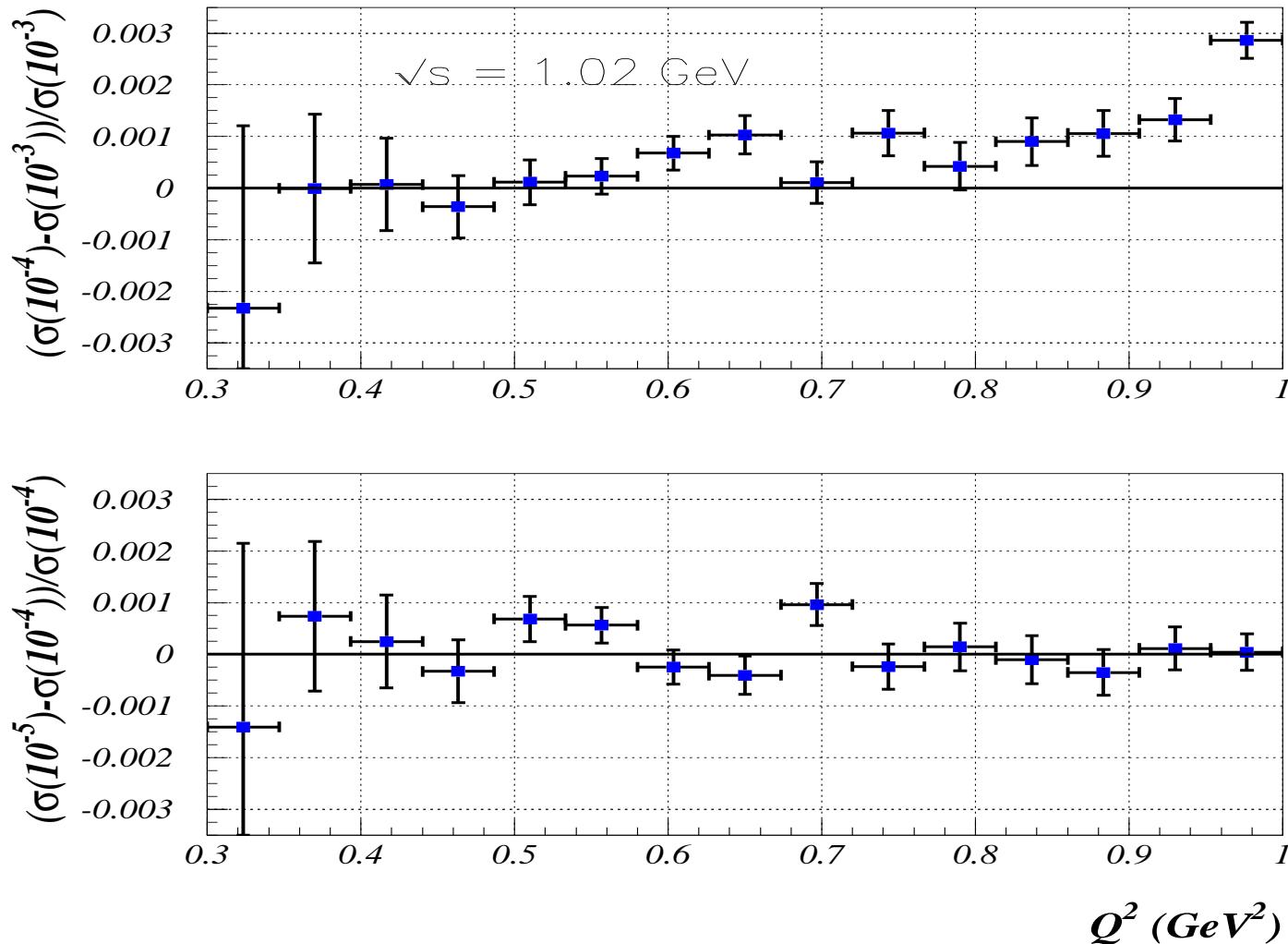
# PHOKHARA generation tests

G. Rodrigo, H.C., J.H. Kühn and M. Szopa, EPJ C24:71, 2002



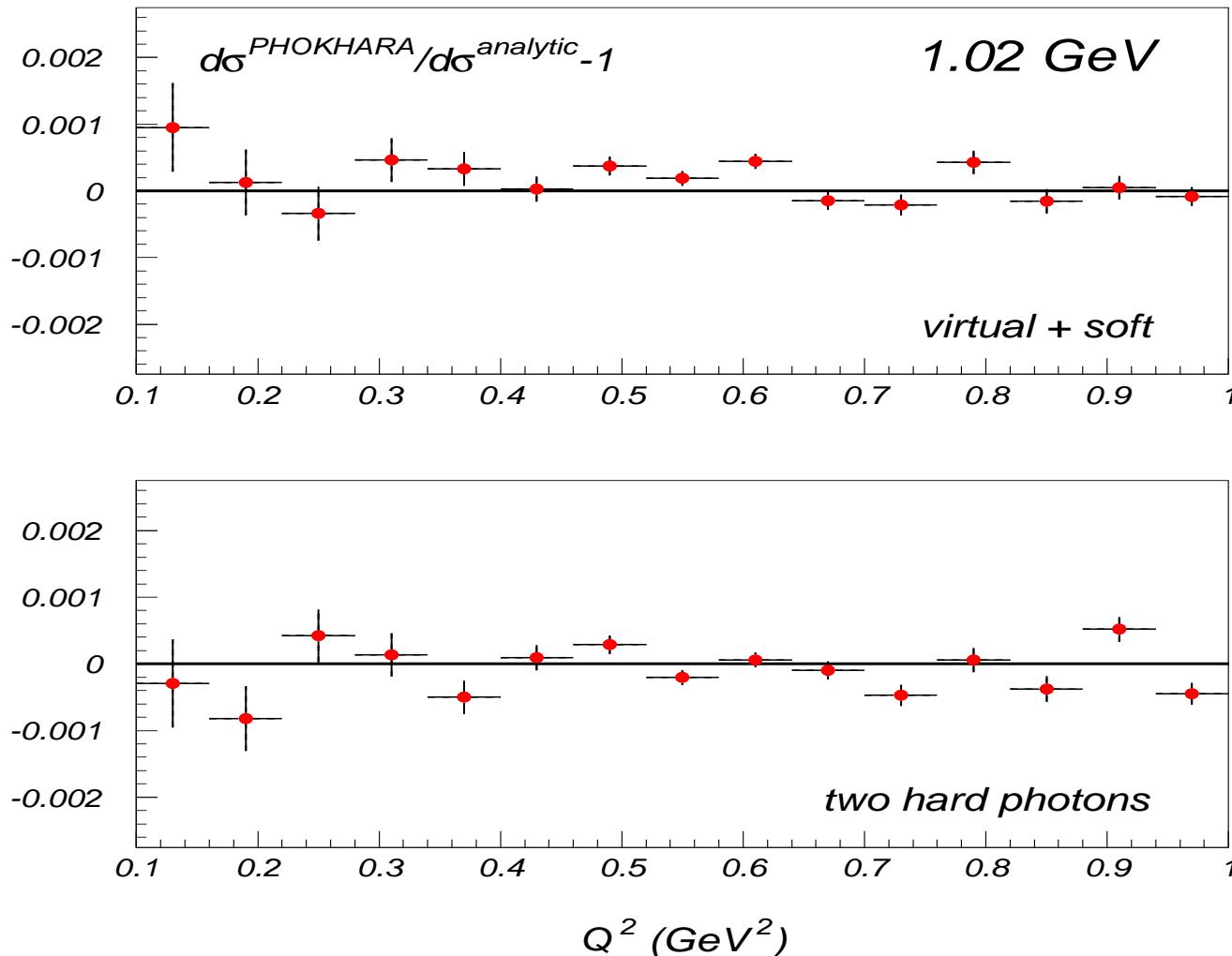
# PHOKHARA generation tests

G. Rodrigo, H.C., J.H. Kühn and M. Szopa, EPJ.C24:71,2002.



# PHOKHARA generation tests

H.C., A. Grzelińska, J.H. Kühn and G. Rodrigo, EPJ.C27:563,2003



S. Jadach, B. F. L. Ward and Z. Wąs

- ▶ YFS exponentation
- ▶ high accuracy only for muon pairs
- ▶ can we hope for: upgrades ???

## Summary

- We found very good agreement of KKMC and PHOKHARA to within 0.2% for  $\mu$ -pair final states for pure ISR
- Discrepancy of order 1-2% between KKMC and PHOKHARA or even larger at low mass, was found for  $\pi$ -pair final state.
- This is due to use of the inferior EEX matrix element in KKMC instead of CEEX.
- NB. We know how to upgrade ISR in KKMC to CEEX level for any hadronic final state...

# Dubna - Novosibirsk papers 2003

A. B. Arbuzov, E. Bartos (Bratislava),  
V. V. Bytev, E. A. Kuraev, Z. K. Silagadze

- ▶ muon and pion pairs
- ▶ analytic formulae based on RG - SF
- ▶ Comparisons with PHOKHARA planned  
first results in January 2009 ??

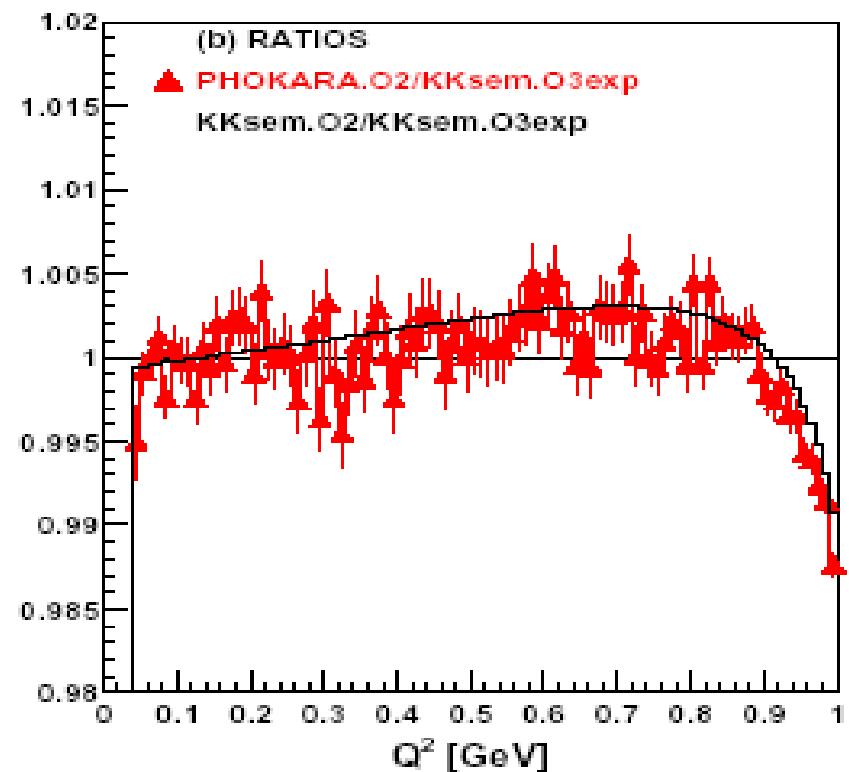
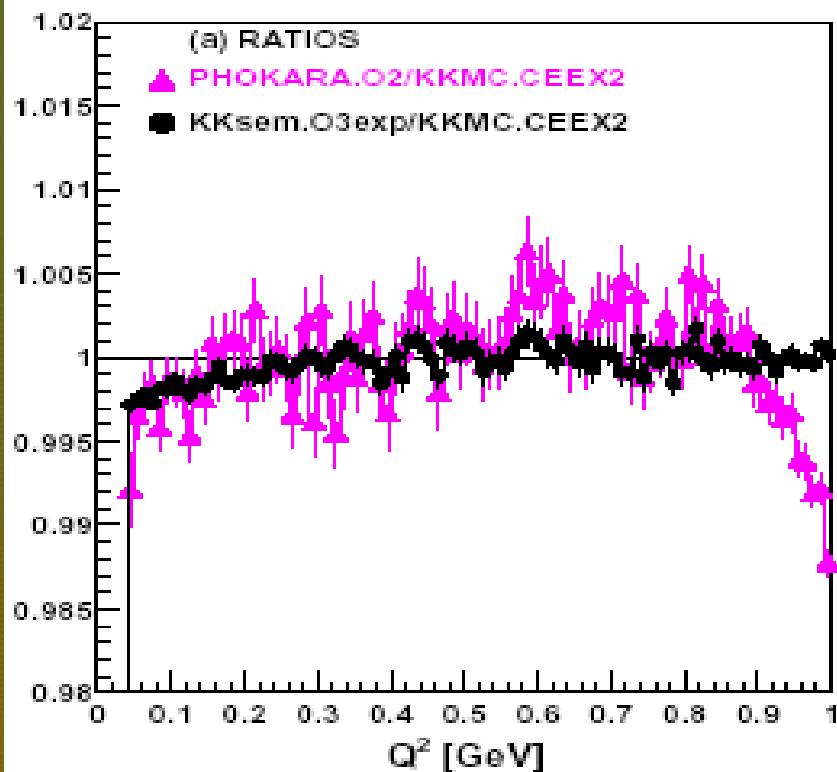
A. B. Arbuzov, G. V. Fedotovich,  
E. A. Kuraev, F. V. Ignatov,  
and A. L. Sibidanov,

EPJ.C46:689,2006.

- ▶ Comparisons with PHOKHARA planned  
first results in January 2009 ??

# S.Jadach: KKMC

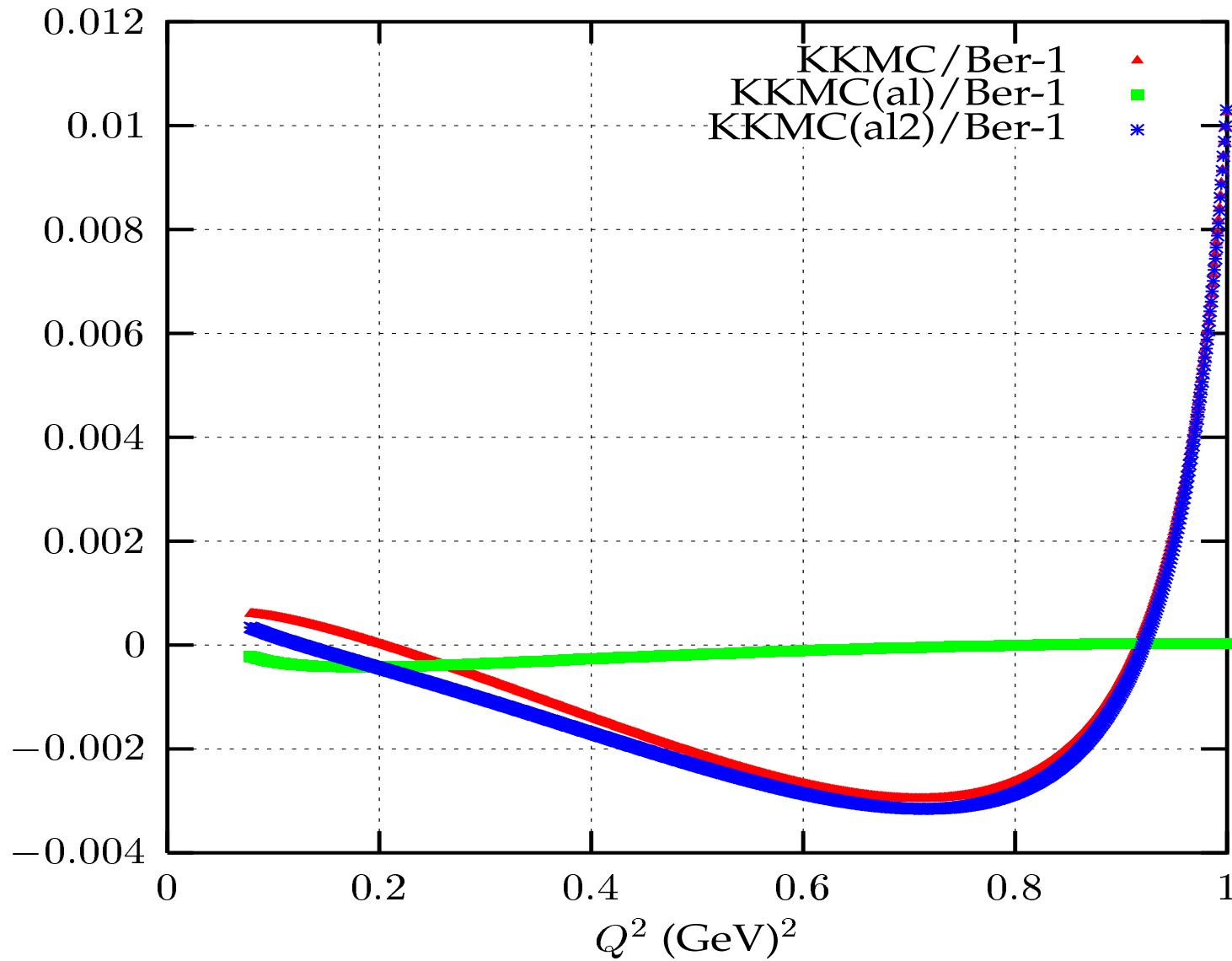
PHOKHARA included in the game,  $\mu$ -pairs again



PHOKHARA agrees to within 0.3% with KKMC and KKsem.

Discrepancy at high  $Q^2$  reflects lack of exponentiation in PHOKHARA

# PHOKHARA vs. KKMC cnd.



# KKMC vs. PHOKHARA - ISR virt. corr.

C. Glosser, S. Jadach, B. F. L. Ward and S. A. Yost  
Phys. Lett. B 605 (2005) 123;  
Phys. Rev. D 73 (2006) 073001

► a precision  $1.5 \cdot 10^{-5}$

► not direct tests

# PHOKHARA: ISR tests summary

- ⇒ technical precision: few  $\times 10^{-4}$
- ⇒ 'physical' precision: 0.5%
- ⇒ plans: accuracy  $\sim 0.2\%$

# FF separation at B-factories

H.C., J. H. Kühn, E. Nowak and G. Rodrigo, Eur.Phys.J.C35(2004)527

Electromagnetic current describing production of baryon-antibaryon pair

$$J_\mu = -ie \cdot \bar{u}(q_2) \left( F_1^N(Q^2) \gamma_\mu - \frac{F_2^N(Q^2)}{4m_N} [\gamma_\mu, Q] \right) v(q_1),$$

$$G_M^N = F_1^N + F_2^N, \quad G_E^N = F_1^N + \tau F_2^N,$$

$$\tau = Q^2/4m_N^2, \quad Q = q_1 + q_2$$

# FF separation at B-factories

H.C., J. H. Kühn, E. Nowak and G. Rodrigo, Eur.Phys.J.C35(2004)527

AT LO ISR :  $e^+ + e^- \rightarrow \bar{N} + N + \gamma$ .

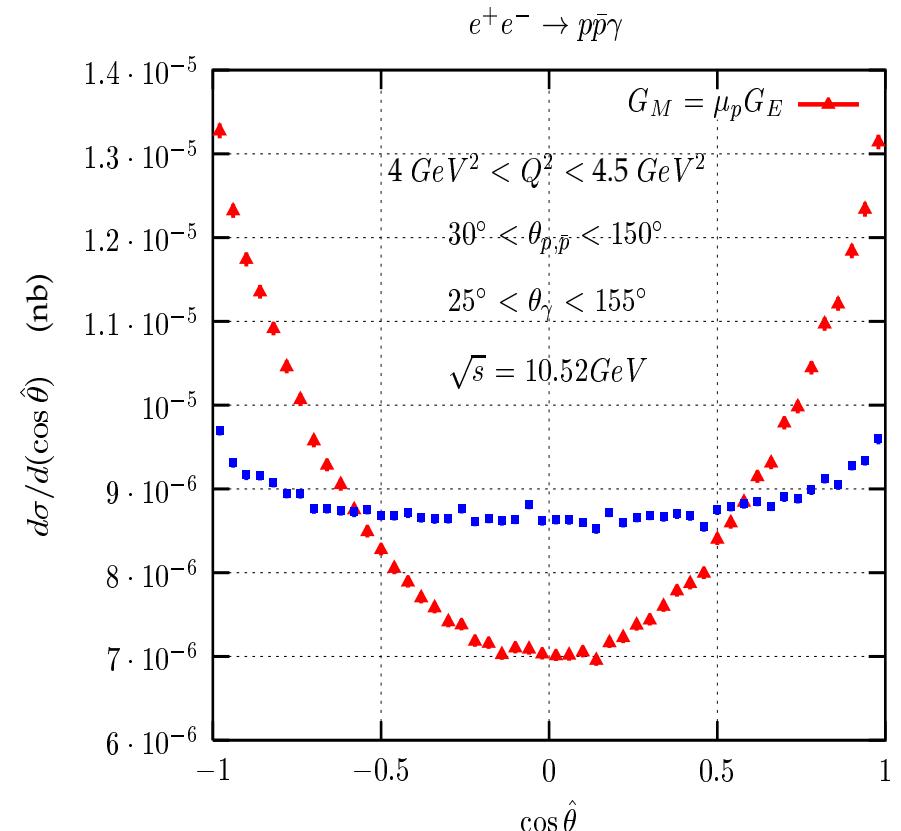
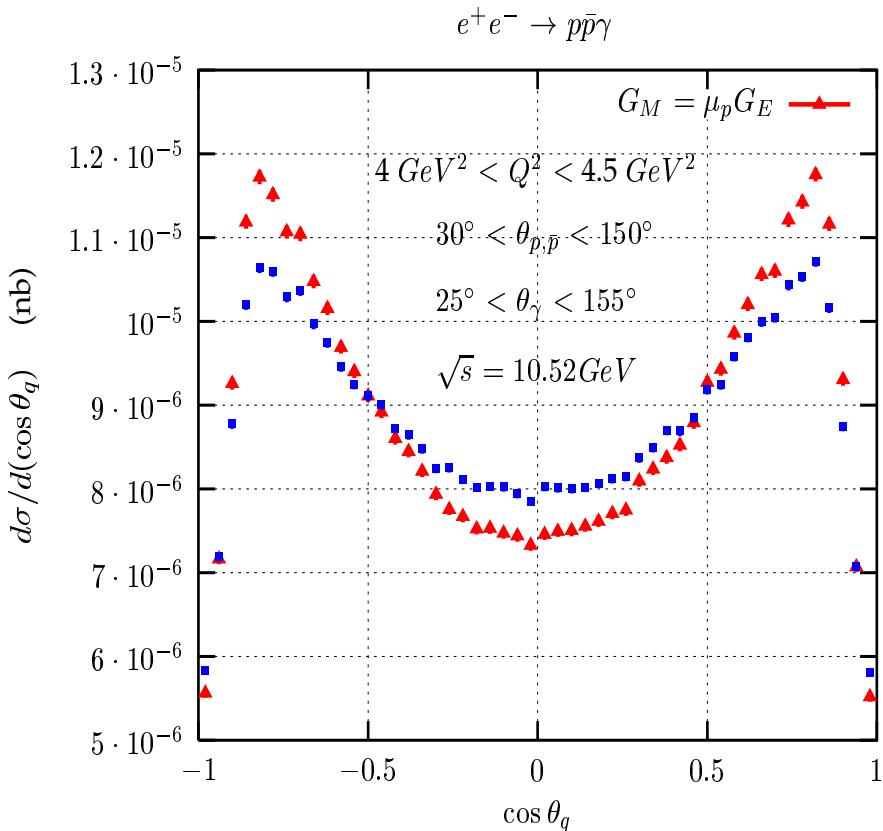
$$d\sigma = \frac{1}{2s} L_{\mu\nu} H^{\mu\nu} dLips(p_1 + p_2; q_1, q_2, k)$$

$$H_{\mu\nu} = 2|G_M^N|^2(Q_\mu Q_\nu - g_{\mu\nu}Q^2)$$

$$- \frac{8\tau}{\tau - 1} \left( |G_M^N|^2 - \frac{1}{\tau} |G_E^N|^2 \right) q_\mu q_\nu$$

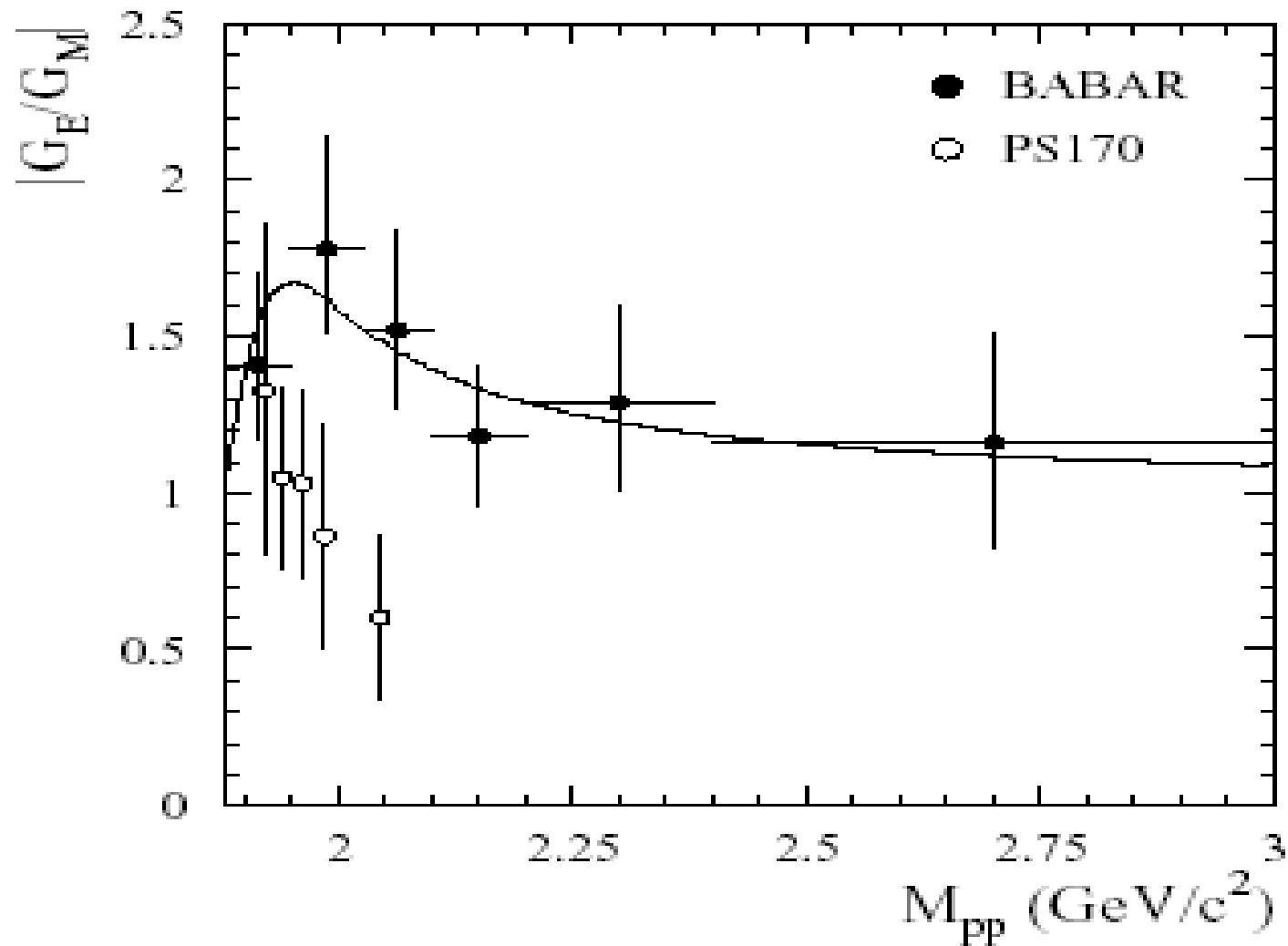
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H.C., J. H. Kühn, E. Nowak and G. Rodrigo, Eur.Phys.J.C35(2004)527



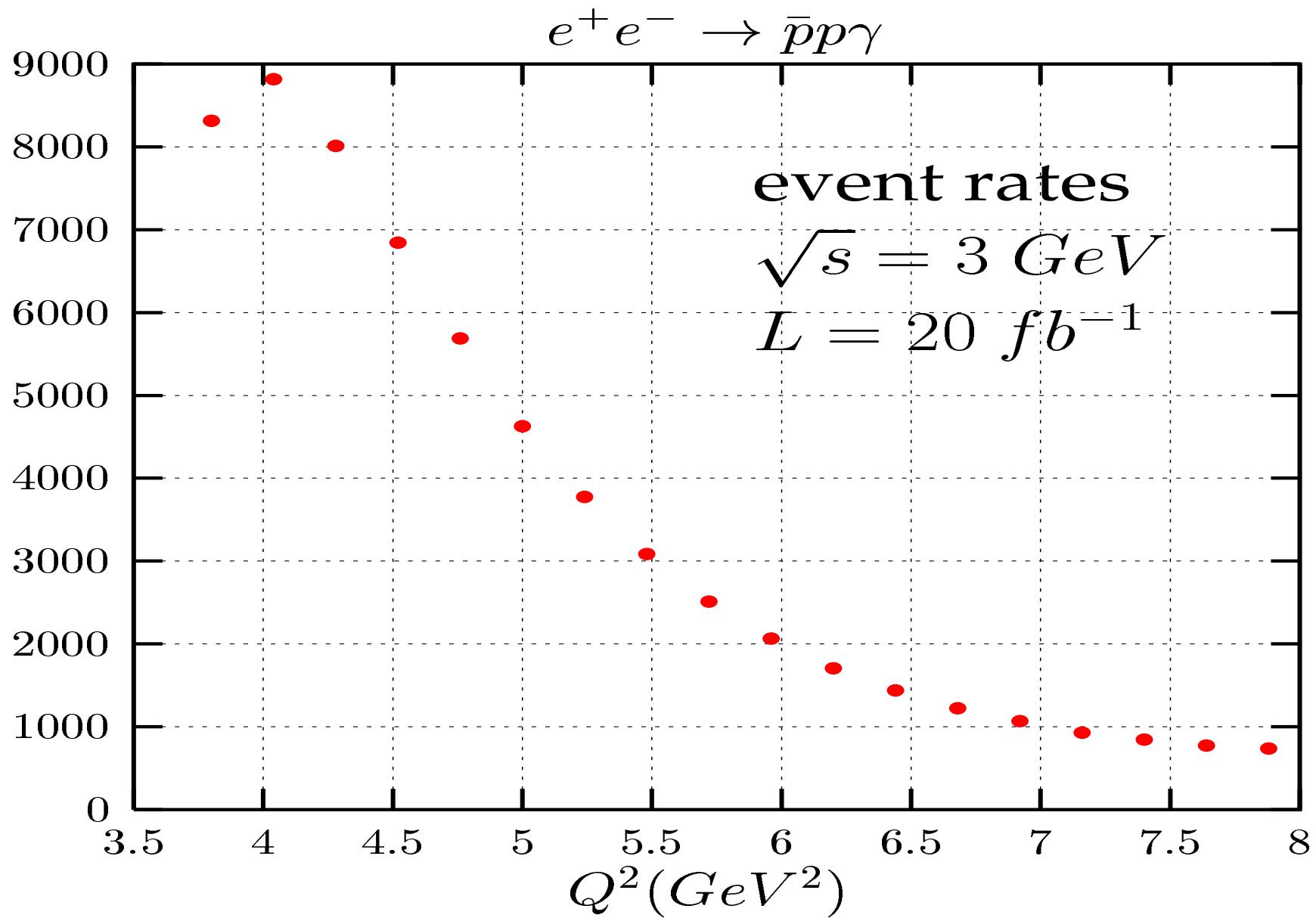
about 2000 events per  $100 \text{ fb}^{-1}$

# nucleon FF



BaBar: Phys.Rev.D73:012005,2006.

# nucleon FF at $\sqrt{s} = 3 \text{ GeV}$



# $\Lambda$ formfactors

$$e^+ e^- \rightarrow \Lambda(q_2, S_2) \bar{\Lambda}(q_1, S_1)$$

$$e^+ e^- \rightarrow \Lambda(q_2, S_2) \bar{\Lambda}(q_1, S_1) \gamma_{ISR}$$

$$J_\mu = -ie \cdot \bar{u}(q_2, S_2)$$

$$\left( F_1^\Lambda(Q^2) \gamma_\mu - \frac{F_2^\Lambda(Q^2)}{4m_\Lambda} [\gamma_\mu, Q] \right) v(q_1, S_1)$$

# The polarized cross section

$$d\sigma(e^+e^- \rightarrow \bar{\Lambda}\Lambda) = \frac{1}{2s} L_{\mu\nu}^0 H^{\mu\nu} d\Phi_2(p_1 + p_2; q_1, q_2)$$

$$\begin{aligned} L_{\mu\nu}^0 H^{\mu\nu} = & \\ & 4\pi^2 \alpha^2 \left\{ |G_M|^2 (1 + \cos^2 \theta_{\bar{\Lambda}}) + \frac{1}{\tau} |G_E|^2 \sin^2 \theta_{\bar{\Lambda}} \right. \\ & + \textcolor{red}{Im}(G_M G_E^*)/\sqrt{\tau} \sin(2\theta_{\bar{\Lambda}}) \left( S_{\Lambda}^y + S_{\bar{\Lambda}}^y \right) \\ & - \textcolor{red}{Re}(G_M G_E^*)/\sqrt{\tau} \sin(2\theta_{\bar{\Lambda}}) \left( S_{\Lambda}^z S_{\bar{\Lambda}}^x + S_{\bar{\Lambda}}^z S_{\Lambda}^x \right) \\ & + \left( \frac{1}{\tau} |G_E|^2 + |G_M|^2 \right) \sin^2 \theta_{\bar{\Lambda}} S_{\bar{\Lambda}}^x S_{\Lambda}^x \\ & + \left( \frac{1}{\tau} |G_E|^2 - |G_M|^2 \right) \sin^2 \theta_{\bar{\Lambda}} S_{\bar{\Lambda}}^y S_{\Lambda}^y \\ & \left. - \left( \frac{1}{\tau} |G_E|^2 \sin^2 \theta_{\bar{\Lambda}} - |G_M|^2 (1 + \cos^2 \theta_{\bar{\Lambda}}) \right) S_{\bar{\Lambda}}^z S_{\Lambda}^z \right\} \end{aligned}$$

$$Im(G_M G_E^*) / \sqrt{\tau} \sin(2\theta_{\bar{\Lambda}}) \left( S_{\Lambda}^y + S_{\bar{\Lambda}}^y \right)$$

and

$$Re(G_M G_E^*) / \sqrt{\tau} \sin(2\theta_{\bar{\Lambda}}) \left( S_{\Lambda}^z S_{\bar{\Lambda}}^x + S_{\bar{\Lambda}}^z S_{\Lambda}^x \right)$$

$$G_M = |G_M| e^{i\phi_M}$$

$$G_E = |G_E| e^{i\phi_E}$$

$$Re(G_M G_E^*) = |G_M| |G_E| \cos(\phi_M - \phi_E)$$

$$Im(G_M G_E^*) = |G_M| |G_E| \sin(\phi_M - \phi_E)$$

$$\boxed{\phi_M - \phi_E = \Delta\phi}$$

- relative phase between electric  
and magnetic form factors

# The subsequent two body decays of $\Lambda$ s

The measurement of the subsequent two body decays:

$$\Lambda \rightarrow \pi^- p$$

and

$$\bar{\Lambda} \rightarrow \pi^+ \bar{p}$$

allow for a spin analysis of the decaying  $\Lambda$ s.

$$R_\Lambda = 1 - \alpha_\Lambda \bar{S}_\Lambda \cdot \bar{n}_{\pi^-}$$

The decay distribution:

The spin vector is replaced by:

$$\bar{S}_\Lambda \rightarrow -\alpha_\Lambda \bar{n}_{\pi^-} \text{ and } \bar{S}_{\bar{\Lambda}} \rightarrow -\alpha_{\bar{\Lambda}} \bar{n}_{\pi^+}$$

$$e^+ e^- \rightarrow \bar{\Lambda}(\rightarrow \pi^+ \bar{p}) \Lambda(\rightarrow \pi^- p)$$

using the narrow width approximation

$$\begin{aligned} d\sigma (e^+ e^- \rightarrow \bar{\Lambda}(\rightarrow \pi^+ \bar{p}) \Lambda(\rightarrow \pi^- p)) &= \\ d\sigma (e^+ e^- \rightarrow \bar{\Lambda}\Lambda) (S_{\Lambda,\bar{\Lambda}} \rightarrow \mp \alpha_\Lambda n_{\pi^\mp}) & \\ \times d\Phi_2(q_1; p_{\pi^+}, p_{\bar{p}}) d\Phi_2(q_2; p_{\pi^-}, p_p) & \\ \times \text{Br}(\bar{\Lambda} \rightarrow \pi^+ \bar{p}) \text{Br}(\Lambda \rightarrow \pi^- p) & \end{aligned}$$

$$n_{\pi^+}(n_{\pi^-}) = (0, \bar{n}_{\pi^+}) ((0, \bar{n}_{\pi^-})) \text{ in the } \bar{\Lambda} \text{ (\Lambda) rest frame}$$

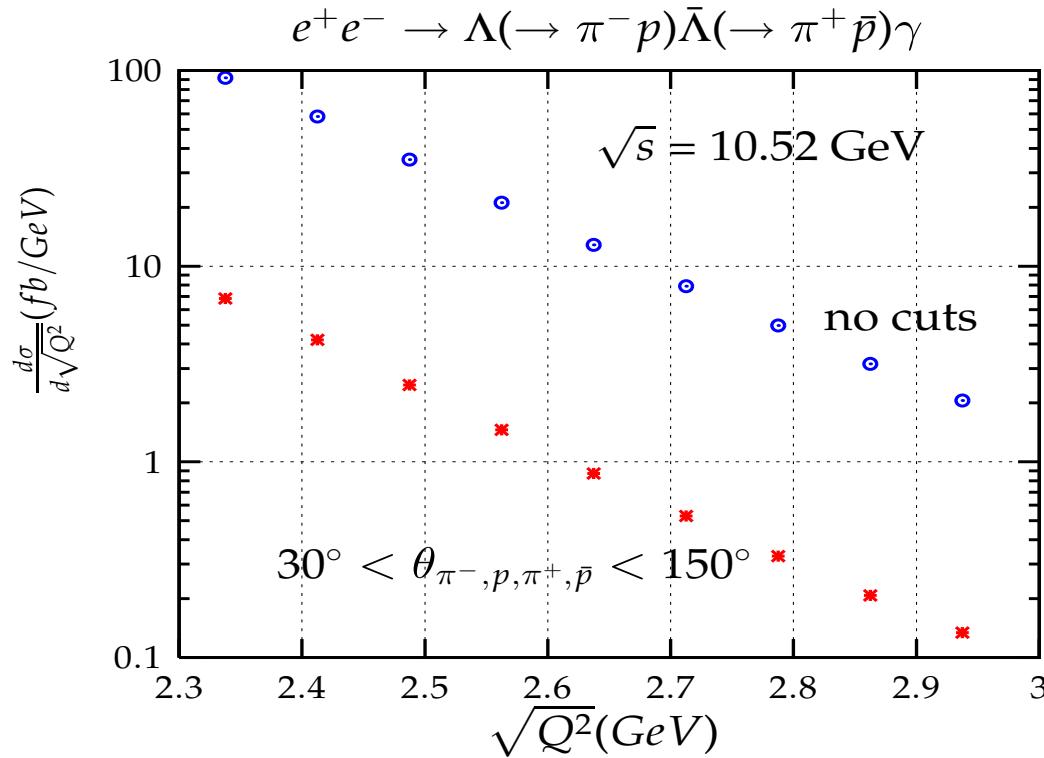
# The cross section with ISR photon emision

$$L^{ij} H_{ij} \simeq \frac{(4\pi\alpha)^3}{4Q^2 y_1 y_2} (1 + \cos^2 \theta_\gamma) \left\{ \begin{aligned} & |G_M|^2 (1 + \cos^2 \theta_{\bar{\Lambda}}) \\ & + \frac{1}{\tau} |G_E|^2 \sin^2 \theta_{\bar{\Lambda}} - \alpha_\Lambda \frac{\text{Im}(G_M G_E^*)}{\sqrt{\tau}} \sin(2\theta_{\bar{\Lambda}}) \left( n_{\pi^-}^y - n_{\pi^+}^y \right) \\ & + \alpha_\Lambda^2 \frac{\text{Re}(G_M G_E^*)}{\sqrt{\tau}} \sin(2\theta_{\bar{\Lambda}}) \left( n_{\pi^-}^z n_{\pi^+}^x + n_{\pi^+}^z n_{\pi^-}^x \right) \\ & - \alpha_\Lambda^2 \left( \frac{1}{\tau} |G_E|^2 + |G_M|^2 \right) \sin^2 \theta_{\bar{\Lambda}} \quad n_{\pi^+}^x n_{\pi^-}^x \\ & - \alpha_\Lambda^2 \left( \frac{1}{\tau} |G_E|^2 - |G_M|^2 \right) \sin^2 \theta_{\bar{\Lambda}} \quad n_{\pi^+}^y n_{\pi^-}^y \\ & + \alpha_\Lambda^2 \left( \frac{1}{\tau} |G_E|^2 \sin^2 \theta_{\bar{\Lambda}} - |G_M|^2 (1 + \cos^2 \theta_{\bar{\Lambda}}) \right) \quad n_{\pi^+}^z n_{\pi^-}^z \end{aligned} \right\}$$

$\theta_{\bar{\Lambda}}$  -  $\bar{Q}$  rest frame with the z-axis opposite to the photon direction

# The cross section

FF from Körner et al. Phys. Rev. D 16 (1977) 2165



At  $B$ -factories we expect about 130 events per  $100 \text{ fb}^{-1}$ .

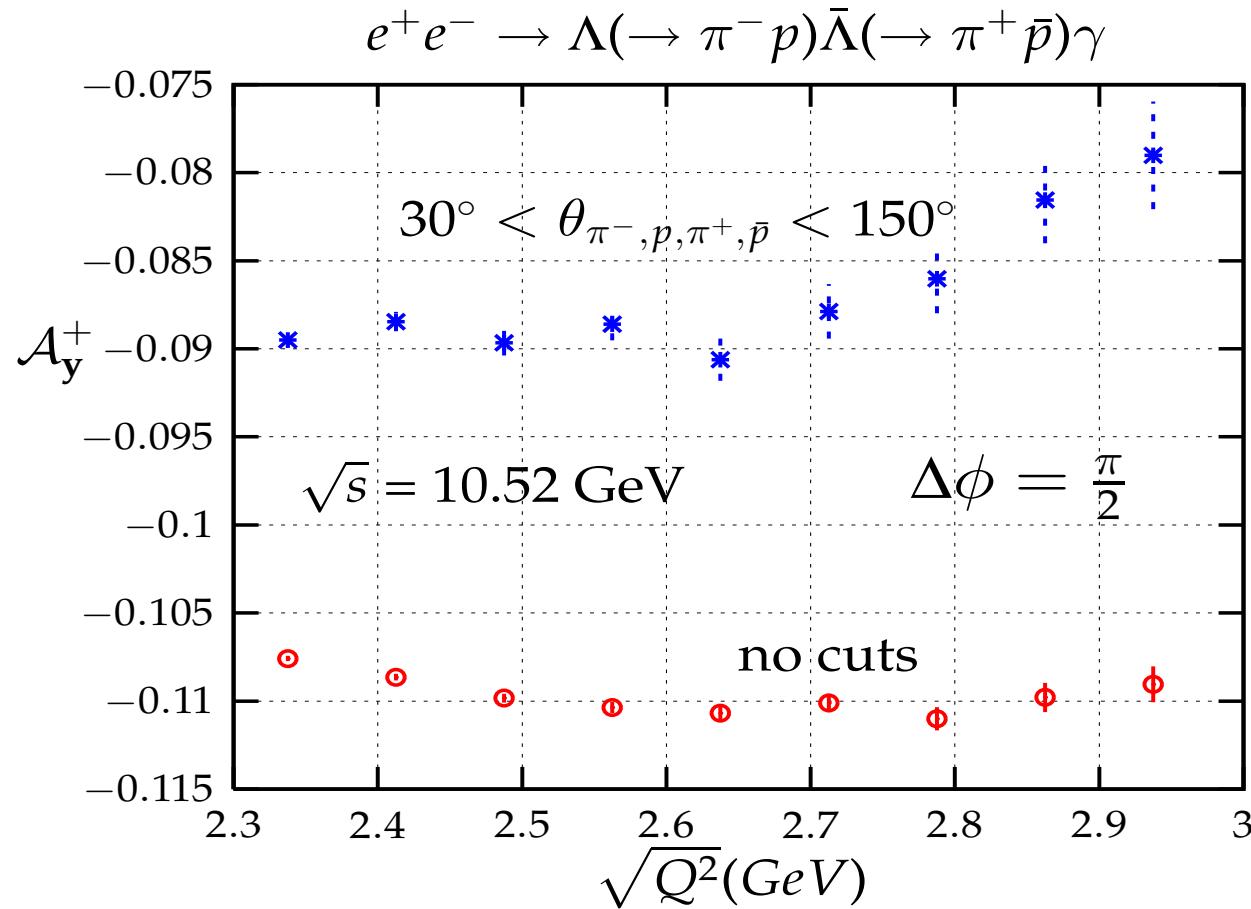
At  $\sqrt{s} = 3.77 \text{ GeV}$  we expect about 220 events per  $10 \text{ fb}^{-1}$ .

# Asymmetry

$$\mathcal{A}_y^\pm = \frac{d\sigma(a^\pm > 0) - d\sigma(a^\pm < 0)}{d\sigma(a^\pm > 0) + d\sigma(a^\pm < 0)}$$

$$a^{+(-)} = \sin(2\theta_{\bar{\Lambda}}) n_{\pi^+(\pi^-)}^y$$

# Asymmetry

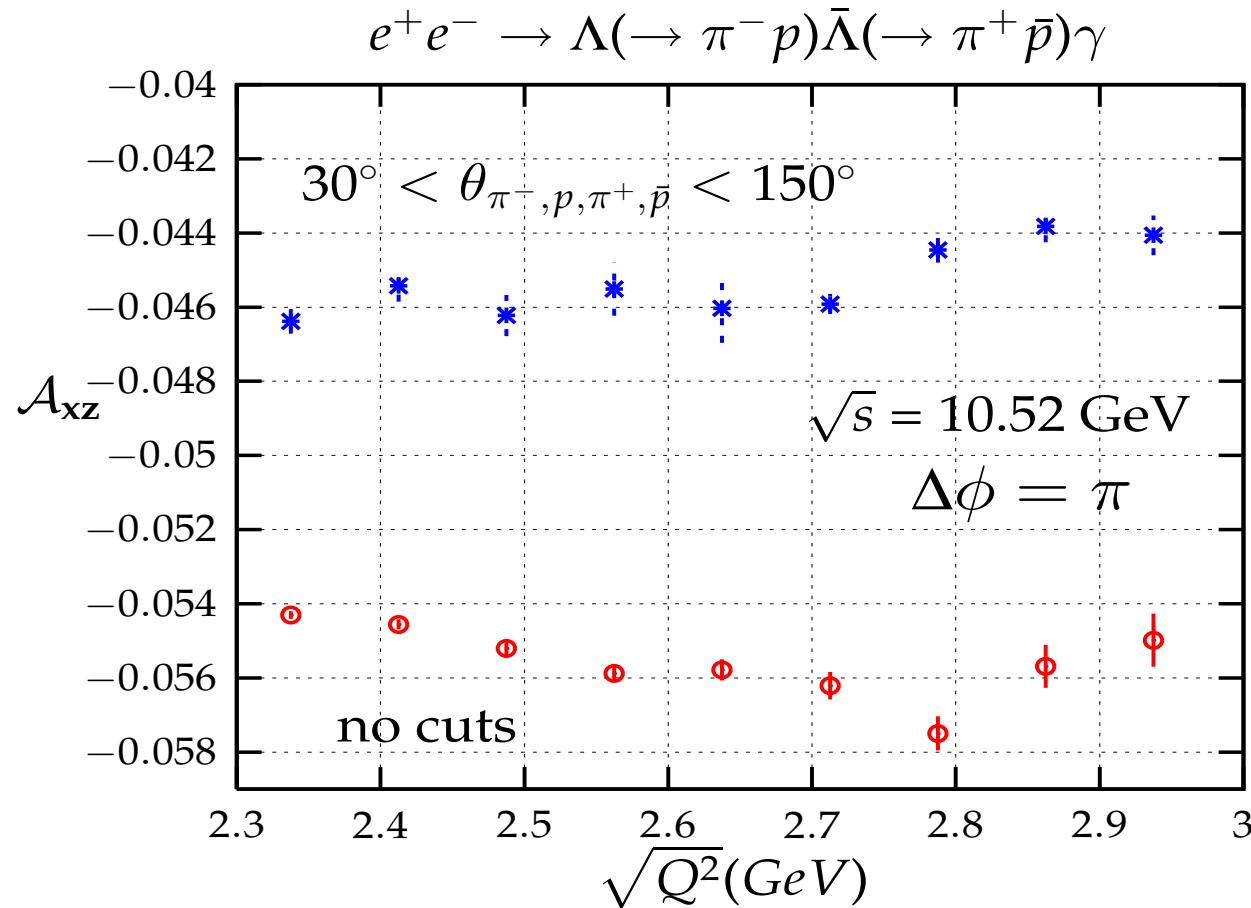


# Spin correlations

$$\mathcal{A}_{xz} = \frac{d\sigma(\tilde{a}>0) - d\sigma(\tilde{a}<0)}{d\sigma(\tilde{a}>0) + d\sigma(\tilde{a}<0)}$$

$$\tilde{a} = \sin(2\theta_{\bar{\Lambda}}) \times \left( n_{\pi^-}^z n_{\pi^+}^x + n_{\pi^+}^z n_{\pi^-}^x \right)$$

# Spin correlations



# The cross section

BABAR Collaboration, Phys.Rev.D76:092006,2007.

$$|G_E/G_M| = 1.73^{+0.99}_{-0.57} \text{ for } \sqrt{Q^2}: 2.23 - 2.40 \text{ GeV}$$

$$|G_E/G_M| = 0.71^{+0.66}_{-0.71} \text{ for } \sqrt{Q^2}: 2.40 - 2.80 \text{ GeV}$$

$$-0.76 < \sin(\Delta\phi) < 0.98$$

# Summary

► PHOKHARA: ISR accuracy 0.5%

► aim: ISR accuracy  $\sim 0.2\%$

soon PHOKHARA7.0 with:

► new  $4\pi$ ,  $J/\psi$  and  $\psi(2S)$

We look forward for fruitfull collaboration  
between BESIII and PHOKHARA team