## A three-module course on quantum field theory

## I. Renormalization of $\phi^4$ , $\phi^3$ and QED

- UV divergent amplitudes at one loop of  $\phi^4$  and  $\phi^3$
- QED gauge invariance
  - Wilson lines
- Renormalization of QED
  - quantization of the photon and Faddeev-Popov ghosts
  - Ward identities
  - one-loop UV divergent amplitudes and counterterms
  - effective charge and electron-photon vertex
  - electron anomalous magnetic moment
- Wilson's picture of renormalization
- Massless theories
- Callan-Symanzik (CS) equation and  $\beta$  and  $\gamma$  functions for
  - $\phi^4$  and  $\phi^3$
  - massless QED
- $\bullet\,$  resummation of leading logs
- running of the coupling constant
  - asymptotic freedom of  $\phi^3$
- fixed points and anomalous dimensions
- local operators
- mass operators and Wilson-Fischer fixed point

Prerequisites to the first module

- canonical quantization
- path-integral quantization
- Feynman rules
- LSZ reduction

## II. Parton model and QCD

- 🖝 Parton model
  - Deep Inelastic Scattering (DIS)
    - parton distributions
    - sum rules
  - charged and neutral currents
    - helicity amplitudes
- 🗢 QCD
  - Colour algebra
  - Gauge symmetry
    - connections, comparators, Wilson loops
  - Renormalization of the Yang-Mills theories
    - Ward identities and unitarity: Feynman ghosts
    - quantization of the gluon and Faddeev-Popov ghosts
    - one loop UV divergent amplitudes and counterterms
    - the  $\beta$  function
      - $\ast\,$  running of the coupling constant
      - \* asymptotic freedom
  - Chiral symmetry breaking
    - Pions as Goldstone bosons
    - chiral perturbation theory
  - Heavy quark effective symmetry
- Perturbative QCD
  - $e^+e^- \rightarrow \text{hadrons}$ 
    - $-\,$  the R ratio
    - Callan-Symanzik equation
    - final states
      - $\ast\,$  infrared and collinear divergences
        - $\cdot$  Bloch-Nordsieck theorem
        - $\cdot\,$  KLN theorem
      - $\ast\,$  eikonal rules and jets
      - \* event shape variables
  - Drell-Yan scattering
  - hadron-hadron collisions
  - modern techniques for the computation of scattering amplitudes
    - colour decomposition
    - helicity amplitudes
  - DIS
    - Altarelli-Parisi evolution
    - Parton distributions
  - Renormalization of the quark mass
  - Renormalization of weak decays
  - OPE
    - $e^+e^- \rightarrow hadrons$
    - DIS

## III. Symmetry breaking in QFT

- global symmetries
- spontaneous global symmetry breaking
  - Goldstone theorem
  - chiral symmetry breaking
    - $\ast\,$  low-energy QCD
    - \* linear sigma models
- gauge symmetries
- spontaneous gauge symmetry breaking
  - Higgs mechanism
  - Standard Model
- custodial symmetry
- renormalization of spontaneously broken gauge symmetries