G. Parisi: SOME REMARKS ON THE ELECTRONIC STATES IN DISORDERED MATERIALS.
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ABSTRACT.

In this paper we recall how the field theory formalism is very useful for computing the density of electronic levels in disordered materials and we stress those characteristics of the associated field theory which are peculiar of this model. In particular we show that the localization transition associated to the mobility edge has rather strange properties from the point of view of pure field theory: a sound computation of the critical exponents associated to the mobility edge is rather difficult, due to this unusual behaviour.

1. - INTRODUCTION.

After the first paper by Anderson (1958) on localization of electrons, a lot of work has been done on the electronic structure of amorphous materials (for a review see Thouless 1974 and 1978). If one neglects the electron-electron interaction, the problem is reduced to the computation of the levels of the Schrödinger operator

\[ H_R = -\Delta + V(x), \]  

where \( V(x) \) is a random potential dependent on the atomic structure of the material, and \( \Delta \) is the D-dimensional Laplacian. In the simp
least approach one studies only the case where $V(x)$ is a white noise, i.e. it has a Gaussian distribution with covariance:

$$\langle V(x)V(y) \rangle = g \delta^D(x - y) ,$$

where $g$ plays the role of coupling constant. In the rest of this paper we will consider only this case.

The goal consists in computing the Green functions of the operator $H_R$ after the mean over the random potential $V(x)$. From the knowledge of the Green functions, one can extract physically interesting informations as the density of states, the conductivity of the system and the nature of the electronic states (localized or extended states).

A possible approach to this problem consists in mapping it on the problem of computing the Green functions of an appropriate field theory. This approach has been very succesfully, especially for the computation of the density of states; unfortunately not so many progresses have been done in studying the behaviour of the conductivity near the mobility edge which separates localized from extended states. Indeed the localization transition, which is the field theoretical equivalent of the mobility edge, has rather unique characteristics which are not shared any "real" transition. Most of the troubles are due to the fact that the equivalent model of field theory is not a true field theory, but it is the analytic continuation in a parameter of a bona fide field theory: in doing the analytic continuation most of the physical intuition we have gathered, may be lost (especially inequalities coming from positivity) and rather paradoxical situations can be reached (That happens in the theory of spin glasses: see Parisi 1979 and 1980).

The aim of this paper is to underline these difficulties and to stress the points in which the localization transition differs from a normal transition.
In Section 2 we review the general field theoretical formalism we use, while in Section 3 we show how this formalism can be successfully used to compute the density of levels. In Section 4 we study the appropriate perturbative expansion for the conductivity and we see how long range correlations are present in the conducting phase. In the last Section we discuss and present the results obtained in the previous Sections.

2. - THE FIELD THEORY FORMALISM.

We want to have a representation for the following quantities:

\[ G_R(x - y) = \langle G^V(x, y) \rangle ; \]
\[ |G_R^2(x - y) = \langle |G^V(x, y)|^2 \rangle ; \] (3)
\[ G^V(x, y) = \langle x \big| (H_R - E)^{-1} y \big| \rangle , \]

where the bracket denotes the mean over the random potential V.

From their knowledge one can compute the density of states \( \rho \) and the conductivity \( \sigma \), e.g.:

\[ \rho = \text{Im} G_R(0) \] (4)

At this end we must consider the 0(N) invariant Lagrangian:

\[ \mathcal{L}(x) = \sum_i \left[ (\partial_{\mu} \phi_i)^2 - |E \phi_i|^2 \right] - g \left( \sum_i |\phi_i|^2 \right)^2 \] (5)

where \( \phi_i \) are N components fields. The generating functional of the correlation functions of the \( \phi \) field is given by:

\[ Z\{J\} \propto \int d\phi \exp \left[ - \int dx \left( \mathcal{L}(x) + \sum_i J_i(x) \phi_i(x) \right) \right] \] (6)

Using symmetry arguments one finds that the two fields correlation function satisfies the relation (Economu and Cohen 1970; Nitzen et al. 1977, Thouless 1975, Aharony and Imry 1977):
\[ \langle \phi_i(x) \phi_j(y) \rangle = G(x - y) \delta_{i,j} \]  

(7)

The theory (in particular \( G(x) \)) is well defined for any integer value of \( N \); an analytic continuation in \( N \) to non-integer values can be done: for \( N = 0 \) one finds that

\[ G_R(x) = G(x) \]  

(8)

This result is very useful because it allows us to use the whole technology developed in the study of standard field theory, in particular the Feynman diagrammatic expansion and the renormalization group.

In the same spirit one can introduce the Lagrangian

\[ \mathcal{L}(x) = \frac{1}{2} \sum_i \left[ (\partial_\mu \phi_i^+)^2 + (\partial_\mu \phi_i^-)^2 - E(\phi_i^+)^2 \right] - \frac{1}{2} \mathcal{E}(\phi_i^-)^2 - \sum_i \left[ N \left( (\phi_i^+)^2 + (\phi_i^-)^2 \right) \right] \]  

(9)

\( E \) is a priori complex parameter and \( \mathcal{E} \) denotes its complex conjugate. In the limit \( n \to 0 \) the correlation function of the field \( \phi^+ \) are identical to those of the field \( \phi^- \); moreover one finds that:

\[ \langle \phi_i^+(x) \phi_k^+(y) \rangle = \langle \phi_i^-(x) \phi_k^-(y) \rangle ; \]

(10)

\[ \sum_i \langle \phi_i^+(x) \phi_i^-(y) \rangle \phi_i^+(y) \phi_i^-(y) = \delta_{ij} \left| G_R^2(x - y) \right| \]

The Green function \( \left| G_R^2(x) \right| \) is needed to study the presence of localized states: one expect that, if and only if localized states are present, the function \( \left| \psi_R^2(x) \right| \) defined by

\[ \lim_{\text{Im} E \to 0} \left| G_R^2(x) \right| \text{Im} E = \left| \psi_R^2(x) \right| \]  

(11)

is non-trivial: \( \left| \psi_R^2(x) \right| \) represent the square of the wave function of localized states.
The transition, as function of the energy, from extended to localized states is characterized by the divergence of the correlation functions in the configuration space. This divergence, which is foreign to all the tradition in field theory is possible here also because the functional integral in eq. (6) is not well defined as it stands (the coupling constant has the wrong sign!) and it can be defined only after a rotation of the path of integration in the functional space.

Let us present an example, which will be useful later, of the way in which well known relation can be obtained in this formalism. We start from the relation:

\[
\frac{1}{H_R - E} - \frac{1}{H_R - \bar{E}} = -2 \text{Im} E / (H_R - E)(H_R - \bar{E}). \tag{12}
\]

If we bracket it with \( \langle x | \frac{1}{|x\rangle} \) and we use the completeness of the states, we find

\[
G^V(x, x | E) - G^V(xx | \bar{E}) = -2 \text{Im} E \int G^V(x, y | E) G^V(y, x | \bar{E}) \, d^Dy \tag{13}
\]

where we have written explicitely the dependence on the Energy (E) of the Green functions (it was implicit in eq. (3)). After the integration over the random field \( V \), we get (Velicky 1969):

\[
G_R(0 | E) - \overline{G_R(0 | \bar{E})} = -2 \text{Im} E \int |G^2_R(y) \, d^Dy \tag{14}
\]

How to recover eq. (4)? If \( \text{Im} E = 0 \) the Lagrangian (9) would be invariant under a global 0(2) transformation\((\star)\); its infinitesimal form being

\[
\delta \phi^+(x) = \phi^-(x), \quad \delta \phi^-(x) = -\phi^+(x). \tag{15}
\]

(\(\star\)) - After that this paper has been completed, a paper has been published (Wegner 1979) in which eq. (14) is derived from the Ward identities of the 0(2) symmetry. However the conclusion of this paper on the behaviour of the mobility edge are different from ours.
It is now a simple exercise in functional integral representations to derive Ward identity relation in presence of a symmetry breaking term (Jona Lasinio 1964, Parisi and Testa 1970). In this particular instance the symmetry breaking term is

$$\sum_{i=1}^{N} \int \left[ (\phi_i^+(y))^2 - (\phi_i^-(y))^2 \right] d^D y$$

(16)

and one of the corresponding Ward identities is:

$$\langle \phi_k^+(x) \phi_j^+(z) \rangle - \langle \phi_k^-(x) \phi_j^-(z) \rangle =$$

$$= -2 \text{Im} E \sum_{i=1}^{N} \int \langle \phi_k^+(x) \phi_j^-(z) \phi_i^+(y) \phi_i^-(y) \rangle dy .$$

(17)

Using the relations (7-10) eq. (14) follows from eq. (17). If the density of states \( g(E) \) is different from zero, as it happens for all possible real values of the energy, the 0(2) symmetry is spontaneously broken and the integral in the r.h.s. of eq. (4) is divergent, signaling the presence of long range correlations, which may manifest themselves with a Goldstone Boson. In reality (but we are not going to use this observation) the full symmetry group for \( \text{Im} E = 0 \) is 0(2N) which breaks down to 0(N) x 0(N); the group which is spontaneously broken is larger than 0(2), at least for \( N \) greater than 1.

3. - THE DENSITY OF LEVELS.

Let us consider the Lagrangian (6) using the standard Feynman diagram technique the Green functions can be expanded in series of the coupling constant g. No problems arise in perturbation theory when \( E \) is negative (positive mass). When \( E \) is positive the mass in the Lagrangian becomes negative: in a conventional field theory one would shift the field in order to obtain a positive renormalized mass; here nothing of this kind happens and the Green functions for positive \( E \) are computed as analytic continuation from negative \( E \).

The final Green functions are no more real; their imaginary part is
connected to the density of states of $H_R$. Using this technique one finds

$$
\varrho(E) = \frac{D-2}{E^2} \frac{D-4}{F(g \cdot E^{-2})} \theta(E) . \tag{18}
$$

Eq. (18) is correct only if we take care of a finite number of orders of the perturbative expansion. The effect of mass renormalization would shift the value $E_c$ which separates the two regions where $\varrho(E) = 0$ and $\varrho(E) \neq 0$ respectively. Eq. (18) should be substituted by:

$$
\varrho(E) = \frac{D-2}{\text{Im}(E_c - E)^2} \frac{D-4}{F(g \cdot (E - E_c))} \tag{19}
$$

The first non trivial problem consists in computing the behaviour of $\varrho(E)$ near $E_c$. As we shall see later, the situation is more complex and the solution of this problem is irrelevant to physics.

In the coherent phase approximation (CPA) (Sovens 1967, Elliott et al. 1974) one finds for negative $E$ that the Fourier transform $G(p)$ of $G(x)$ satisfies the equation

$$
G(p) = \frac{1}{(p^2 + m^2)^2}, \tag{20}
$$

$$
-E = m^2 - g(m^{D-2} \Lambda^{D-2})
$$

where $\Lambda$ is a cutoff at large frequencies (if the Laplacian is written as a finite difference operator on a lattice with spacing $a$ (see Thouless et Elzain 1978) $\Lambda \propto a^{-1}$), and we have neglected all the proportionality factors.

As well known the solution of eq. (20) gives

$$
\varrho \sim (E - E_c)^{2a} \theta(E - E_c) \quad (a = \frac{1}{2}) \tag{21}
$$

for $E \sim E_c$. The sign of $g$ is crucial. Now when eq. (21) can be trusted? At the transition point $m^2$ remains different from zero, however the propagator

$$
G_{\rho^2}(K) = \int d^D K \langle \rho^2 \rho^2 \rangle , \tag{22}
$$
has a pole at $k^2 = 0$, corresponding to a zero mass bound state. Indeed in the field theory language the $\phi^4$ interaction is attractive and not repulsive as usual: a two particle bound state is produced and by decreasing the mass of the particles ($m^2$), the mass of the bound state become zero when $m^2 \neq 0$. The only infrared singularities are produced by the self interactions of this bound state. This problem can be easily studied using the standard machinery (Aharony and Imry 1977): one introduces a field $q_{ij} = \phi_i \phi_j$, one derives an effective Lagrangian for the field $q_{ij}$: an interaction proportional to $q^3$ is present, strongly suggesting that eq. (21) holds only for $D > D_S = 6$ and that $\alpha$ can be expanded in powers of $\epsilon = D_S - D$ when $D < D_S$. Some explicit work is needed to verify that there are no difficulties which would forbid the realization of this program, in particular if $D_S$ is equal to 6, and not to 8, as happens in some polymers systems (Lubenski and Isaacson 1978).

We do not enter in the details because this problem is purely academic. Indeed the unconventional sign of the coupling constant in eq. (6) makes the Lagrangian unbounded from below also for $E < 0$. As a consequence, the perturbative expansion cannot be Borel summed, and the Green functions have an imaginary part proportional to $\exp(-\frac{1}{g})$ also for $E < 0$. This imaginary part can be computed semiclassically (Thouless and Elzain 1978, Cardy 1978), following the pioneering work of Zittart and Langer (1967), Halperin and Lax (1966, 1967). This effect will give an imaginary part to $E_c$, shifting it in the second sheet, the singularity at $E_c$ becomes an unphysical one and it has a small influence on the "observable" behaviour of $\rho(E)$ for real $E$. This last quantity can be easily computed by matching the small coupling expansion with the non perturbative results proportional to $\exp(-\frac{1}{g})$. The first computation in this direction has been done by Thouless and Elzain (1978). In these last years many progresses have been done in the understanding of the mutual relations among large order behaviour of the perturbative expansion, the semiclassical non perturbative con-
tributions and the singularities of the Borel transform with respect to the coupling constant (see for a review Parisi 1977 and Zinn Justin 1977), consequently the matching of the two expansions can be done with good precision (the results for the prefactor can be found in Brezin and Parisi 1980). It seems that, if no unforeseen difficulties are present, the computation of \( \varrho(E) \) at all the energies should be more a less straightforward. This is in contrast with the situation concerning localized states, as we will see in the next Section.

4. - THE CONDUCTING PHASE.

Let us study the Lagrangian (9). It is believed that for real \( E \) two regimes are possible, for \( E \) less than \( E_L \) only localized states are present, while for \( E > E_L \) the states are extended and the conductivity \( \sigma \) is different from zero; we recall that the conductivity is given by the Kubo-Greenwood formula (Edwards 1958):

\[
\sigma = \lim_{\varepsilon \to 0} \varepsilon^2 \int d^D x \varepsilon^2 \left| G^2 \right|_R(x), \quad \text{Im} E = \varepsilon .
\]

(23)

At zero order in perturbation theory (\( g = 0 \)) :

\[
\left| G^2 \right|_R(x) \sim \frac{1}{x^{D-1}} \exp \varepsilon \left| x \right| ,
\]

(24)

and the conductivity \( \sigma \) is infinite, as it should be, in absence of impurities. The presence of long range correlations implies that perturbation theory should be used with caution, especially at low momenta.

In the language of relativistic field theory the long range behaviour \( \left| G^2 \right|_R(x) \) is due to a pinching singularity at small \( k \) when \( \varepsilon \) becomes zero. Indeed the Fourier transform \( \left| \tilde{G}^2 \right|_R(K) \) is given by

\[
\left| \tilde{G}^2 \right|_R(K) = \int \frac{d^D p}{[(K + p)^2 - E][p^2 - E]} \left\{ G(K + p) \right\}^2 .
\]

(25)

\[
= \int d^D p G(K + p) \overline{G}(p) .
\]
In the other words when $\varepsilon \to 0$, pinching diagrams are the substitute of zero mass particles. When $g$ is different from zero, the Greens functions $G$ becomes imaginary ($\text{Im} m^2 \neq 0$) and the pinching diagrams, although dominant do not correspond any more to long range correlations, however, the Ward identity (17) implies that

$$|G_R^2(0)| \propto \frac{Q(E)}{\varepsilon}$$  \hspace{1cm} (26)

If the function $|G_R^2(K)|$ is not divergent in the limit $\varepsilon \to 0$ at $K \neq 0$, eq. (26) implies the presence of long range correlations for $\varepsilon \to 0$. In this case one would expect that

$$|\tilde{G}_R^2(K)| \propto \frac{1}{K^2} \quad \text{for} \quad \varepsilon = 0$$  \hspace{1cm} (27)

as it normally happens in theories with spontaneously broken symmetries.

One must be rather careful in setting a perturbative expansion in this phase. It is well known that the standard $g$ expansion cannot be used (Langer and Neal 1966): the behaviour of $|\tilde{G}_R^2(K)|$ changes from $1/K$ at $g = 0$ to $1/K^2$ at $g \neq 0$.

The presence of this $g$ dependent crossover region in momentum space induces infrared divergences in the standard perturbative expansion, i.e. the final result will be not a $C^\infty$ function of $g$.

Also if we take care of this effect, the very presence of long range correlations may produce infrared divergences if $D < 4$. However the long range correlations are connected to the spontaneous breakdown of the $O(2)$ symmetry. The Ward identities tell us that these modes decouples in the low momenta region (Adler's zeros) (for a review see Adler and Dashen 1968) and they do not contribute to infrared divergences as far as $D > 2$ (This is the well known situation for Heisemberg ferromagnets (Brezin et Zinn Justin 1976); eq. (27) becomes now:

$$|G_R^2| \propto \frac{1}{K^2} + \frac{1}{K^D}$$  \hspace{1cm} (28)
Is clear that finite results may be obtained only if we take care simultaneously of all the Ward identities of the theory and of the presence of two different regimes at small $K$ for $g = 0$ and $g \neq 0$.

We do not want to discuss how this expansion may be realized. This is a technical problem which can be studied using one of the many field theoretical techniques we have at our disposal. The real unsolved problem consists in controlling the situation for $D = 2$. Wegner 1979, suggests that the usual theorems on absence of spontaneously symmetry breaking imply that the $O(2)$ Goldstone modes must be absent. How can it happen as far as $g(E) \neq 0$? The only possibility would be that

$$
\lim_{\epsilon \to 0} \epsilon | \tilde{G}_{R}^2(K) | \neq 0 \quad \text{for} \quad K \neq 0 .
$$

(29)

The divergence of eq. (26) would not imply a singularity at $K = 0$.

It is usually believed that if eq. (29) holds, the states are localized and the conductivity is equal to 0. Following Wegner we would conclude that for $D = 2$ the states are always localized, as it has been suggested by other authors on different grounds.

However we must always remember that our field theory is only an analytic continuation of a bona fide field theory and one should be very careful in doing analytic continuation of inequalities.

For example if we consider a spin model, invariant under the group $O(n)$, there is a transition where the symmetry breaks down to $O(n - 1)$, the number of Goldstone Boson is $n - 1$ and one would argue that in dimensions 2 a transition of conventional type would be possible only for $n = 1$. However we know that for $n = 0$ the spin model corresponds to the self-avoiding walk (De Gennes 1972) which possesses no anomalous behaviour in $D = 2$, although $-1$ Goldstone Bosons would be present below the transition$^{(+)}$.

$^{(+)}$ - The author thanks De Cloiseaux and Sourlas for enlightening discussions on this point.
Now it is believed that in any dimensions for large negative \( E \) all the states contributing to \( \Phi \) are localized and eq. (29) holds. This result is confirmed by explicite computations (Cardy 1978) done using the semiclassical approach, in which one finds for large negative \( E \):

\[
\left| \frac{\nabla G}{R(K)} \right|^2_{R(K)} \sim \left| \Psi_{R(K)} \right|^2(1 + \frac{n}{2})^{-2 < n < 2}
\]

(30)

Where eq. (30) holds also for \( n \neq 0 \). Eq. (29) may be satisfied only if \( n = 0 \). In these semiclassical computations the factors \( 1/\epsilon \) arise from the integration over the collective coordinates of the instanton in the group space, or in the language of Zittart and Langer as a pinching contribution in the collective coordinates.

More precisely, if one takes care of the correct complex integration path in functional space, the \( O(2) \) group looks like more the \( O(1,1) \) group i.e. a non compact group. The integration over this non compact group gives the terms divergent when \( \epsilon \rightarrow 0 \), i.e. the integration is damped by the terms proportional to \( \epsilon \). Indeed the divergence of the Green functions below \( E_L \) in a new phenomenon in field theory and it is connected to the presence of this non compact symmetry group.

If eq. (29) holds for \( E < E_L \), the absence of conduction for a 2-dimensional system would imply that

\[
E_L \rightarrow + \infty \quad \text{if} \quad D \rightarrow 2^*.
\]

(31)

\( E_L \) denotes the mobility edge and we expect that

\[
\sigma \sim (E - E_L)^\gamma.
\]

Unfortunately there is no known method to compute \( \gamma \).

If we work in perturbation theory in \( g \), \( E_L = E_c \) and the critical exponents \( \gamma, \alpha \), etc, can be easily computed. In this scheme \( \varphi(E) = 0, E < E_L \), i.e. no state, neither localized, nor extended is present for \( E < E_c \).
Including the effect of semiclassical configuration one would obtain \( E_c - E_L \sim \exp(-1/g) \), and the exponent \( \gamma \) is fixed by the behaviour in the region where the semiclassical configurations are important.

Long range correlations, Goldstone Bosons, semiclassical configurations and the \( n = 0 \) limit are all crucial ingredients for understanding the localization transition and one should take care of all of them together. It is still an open problem to understand how it can be done, in particular if in higher dimensional spaces the system simplifies and \( \gamma \) can be computed exactly.

In order to underline those difficulties which are peculiar of this problem, it is useful (following Nitzan, Freed and Cohen 1977) to introduce the fields:

\[
\psi_a^1 = \exp(i\pi/4) \theta_a^1, \quad \psi_a^2 = \exp(-i\pi/4) \theta_a^2. \tag{32}
\]

The Lagrangian (10) becomes now:

\[
\frac{1}{2} \sum_1^n a \left[ (\partial_\mu \psi_a^1)^2 + E(\psi_a^1)^2 - (\partial_\mu \psi_a^2)^2 - E(\psi_a^2)^2 \right]
\]

\[
- \frac{1}{2} \sum_1^n a \left[ (\psi_a^1)^2 + (\psi_a^2)^2 \right] + g \left\{ \sum_1^n a \left[ (\psi_a^1)^2 - (\psi_a^2)^2 \right] \right\}^2. \tag{33}
\]

The corresponding functional integral is now convergent for \( \epsilon > 0 \): the introduction of the fields \( \psi^1 \) and \( \psi^2 \) corresponds to fix the correct integration path in functional space. Apart from the imaginary factor in front of the kinetical term, (33) looks like a conventional Lagrangian; however in the limit \( \epsilon \to 0 \), it becomes invariant under the \( O(n,n) \) group, i.e. the group of linear transformations on 2n-dimensional space which leave invariant the form:

\[
\sum_1^n a \left[ (\psi_a^1)^2 - (\psi_a^2)^2 \right].
\]
As mentioned before, the $0(n,n)$ group contains as a subgroup for $n \geq 1$, the group $0(1,1)$, i.e. the two dimensional Lorentz group.

We face the problem of the restoration of the $0(n,n)$ symmetry which is spontaneously broken in the conducting phase. If the symmetry is unbroken, some of the Green function will diverge when $\varepsilon \to 0$ as a consequence of the non compacteness of the symmetry group: an infinite contribution comes from the integration region where $(\psi^1)^2$ and $(\psi^2)^2$ are both large, but $(\psi^1)^2 - (\psi^2)^2$ remains small. The contribution of this integration region is clearly depressed for $\varepsilon > 0$.

In other words, the necessity of performing a contour rotation in order to define the integrals for negative $g$, transforms the symmetry group from $0(2n)$ to $0(n,n)$ and the non compacteness of the symmetry group is the origine of the pathologies of the model (e.g. the divergences of the Green functions for $\varepsilon \to 0$); of course also the unusual properties of the $0(2n)$ and $0(n,n)$ groups, in the limit $n \to 0$, contribute to the peculiar properties of the localization transition.

In order to get a deeper insight of the problem, it is convenient to introduce the fields

$$Q_{a,b}^{i,K} = \psi^i_a \psi^K_b$$

$i, K = 1, 2$  \hspace{1cm} $a, b = 1, n$

transforming under the tensor representation of the $0(n,n)$ group, and to use the standard methods to derive an effective Lagrangian for the fields $Q_{a,b}^{i,K}$. One could try to investigate on the behaviour of the system near dimensions 2 by studying if and how the arguments of Wegner 1979 must be modified; alternatively one could write the most general cubic effective Lagrangian and try to use the standard machinery of the renormalization group to study the critical behaviour near 6 dimensions.

Both approach seem quite promising but they gives beyond the aim of this paper, i.e. to underline the peculiarities that the localization transitions acquires when we try to describe it in a field theoretical language.
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