

ISTITUTO NAZIONALE DI FISICA NUCLEARE  
Laboratori Nazionali di Frascati

LNF-78/35

J.Berger, J.Duflo, L.Goldzahl, J.Oostens, F.Plouin, F.L.  
Fabbri, P.Picozza, L.Satta, C.Le Brun and D.Legrand:  
SHARP BACKWARD PEAK IN  $p\text{-}{}^4\text{He}$  ELASTIC SCATTERING  
AT 1.05 GeV

Estratto da :

Phys. Rev. Letters 41, 152 (1978)

## Sharp Backward Peak in $p\text{-}{}^4\text{He}$ Elastic Scattering at 1.05 GeV

J. Berger, J. Duflo, L. Goldzahl, J. Oostens,<sup>(a)</sup> and F. Plouin  
*Institut National de Physique Nucléaire et de Physique des Particules,  
 Laboratoire National Saturne, Saclay, France*

and

F. L. Fabbri, P. Picozza, and L. Satta  
*Istituto Nazionale di Fisica Nucleare, Laboratori Nazionali di Frascati, Frascati, Italy*

and

C. Le Brun  
*Université de Caen, Caen, France*

and

D. Legrand

*Département de Physique Nucléaire et Moyenne Energie, Centre d'Etudes Nucléaires de Saclay, Saclay, France*  
 (Received 21 November 1977)

$p\text{-}{}^4\text{He}$  elastic scattering has been measured at 1.05-GeV incident proton energy, close to  $180^\circ$  in the center of mass. The steep backward peak observed at lower energies is still present, but its slope appears to decrease.

Our previous results on elastic  $p\text{-}{}^4\text{He}$  scattering at intermediate energies and at angles close to  $180^\circ$  in center-of-mass system revealed the occurrence of a sharp rise in the differential cross section, which became steeper as the energy increased.<sup>1</sup> Various theoretical models have tried to explain this backward peak by either actual nucleon-nucleon interaction in a non-eikonal scattering approach,<sup>2</sup> or triton exchange,<sup>3-5</sup> or addition of an exchange term in a Glauber model.<sup>6</sup>

The data in Ref. 1 were acquired with incident  $\alpha$  particles on a hydrogen target to take advantage of the wide coverage of the kinematics: The scattered  $\alpha$ 's are fast and confined into a cone  $14.6^\circ$  wide. At the higher energy, when cross sections fall to the nanobarn/steradian level, background problems associated with the empty-target effect become important. However, a useful coverage of the interesting region close to  $180^\circ$  in the c.m. system can still be obtained by returning to the more classical method of using a proton beam and a liquid-helium target. Indeed, around 1-GeV proton kinetic energy and above, the  $\alpha$ 's recoiling from backscattering protons have enough energy to be detected with full efficiency in our spectrometer. Besides, the higher intensity of the proton beam could offset to a certain extent the decrease in cross section. When tried, this method displayed very little background associated with the walls of the target.

Except for the installation of a liquid helium target, and the use of a proton beam, the apparatus was the same double-focusing spectrometer used in Ref. 1 and described in detail elsewhere.<sup>7</sup> The fact that the recoiling  ${}^4\text{He}$  is detected ensures the elastic character of the reaction.

The differential cross sections in the c.m. system are presented in Fig. 1, as a function both of  $\cos\theta_{\text{c.m.}}$  and of the invariant quantity  $u - u_{\text{max}}$ . The numerical values are listed in Table I. It is noteworthy to point out that the smallness of the background has allowed us to make a measurement at  $\theta_{\text{c.m.}} = 180^\circ$ .

We show in Fig. 2 the present data with our earlier results at different energies.<sup>1,8</sup> The results of Comparat *et al.*<sup>9</sup> at 156 MeV and of Aslanides *et al.*<sup>10</sup> at 1.05 GeV are also shown. The cross sections are given as a function of  $t$ . In the following, when comparing different experiments, we will use in the case of incident  $\alpha$  particles the equivalent proton laboratory kinetic energy (i.e., giving for  $p\alpha$  scattering the same c.m. energy as in  $\alpha p$  case); when needed, the c.m. momentum will be also given. One can note in Fig. 2 that a sharp peak exists near  $180^\circ$  in the c.m. system except at 198 and 438 MeV. Outside the backward region,  $d\sigma/dt$  is to a large extent energy invariant, as confirmed also by the results at 788 MeV,<sup>11</sup> and it can be described by Glauber-like<sup>12,13</sup> models.

At the intermediate energies Gurvitz *et al.*<sup>13</sup> described the large-angle  $p\text{-}{}^4\text{He}$  scattering using

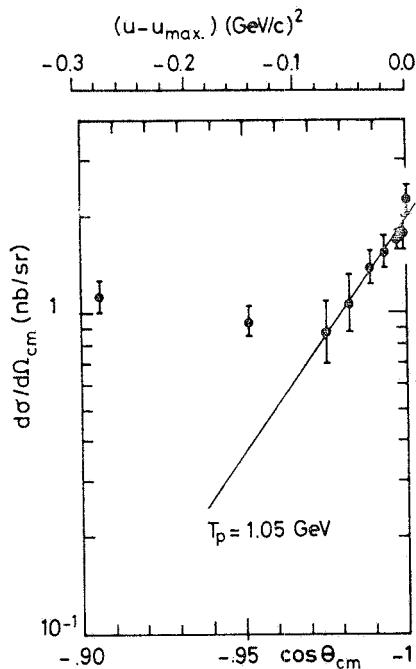


FIG. 1. c.m. differential cross section for  $p-{}^4\text{He}$  elastic scattering as a function of  $\cos\theta_{\text{c.m.}}$  and of the invariant quantity  $u - u_{\text{max}}$ . The solid line is the result of the parametrization discussed in the text.

the actual nucleon-nucleon interaction. At backward angles the rise of the  $I=0$  NN interaction causes the single scattering to dominate again and a peak is predicted.<sup>2</sup> This method does not account simultaneously for large angles and backward scattering.<sup>2</sup> Kopeliovich and Potashnikova<sup>3</sup> predicted a backward peak using the exchange of a triton. This model was developed by Lesniak *et al.*<sup>5</sup> who introduced absorption for the incident and the scattered particles. They used an Eckart parametrization of the  ${}^4\text{He}$  single-particle wave function. This calculation, not involving  $t$ -channel contributions, reproduces our results at 438 and 638 MeV for  $\theta_{\text{c.m.}} \gtrsim 140^\circ$ . Also at intermediate energies, Dymarz and Małecki<sup>6</sup> used a Glauber model where a Majorana exchange potential is added to the equivalent potential of Ref. 1. The results of this calculation are satisfactory at 438 and 638 MeV, but difficulties appear at 1.05 GeV. It can be remarked that at low energies Thomson *et al.*<sup>14</sup> have shown, using the resonating-group properties, that the  $n-{}^4\text{He}$  backward scattering contains a heavy-particle exchange which can be described equivalently with a Majorana potential. This method gave satisfactory results between 30 and 156 MeV in the  $p-{}^4\text{He}$  case.<sup>9,15,16</sup>

In order to investigate the energy behavior of

TABLE I. Center-of-mass differential cross section for  $p + {}^4\text{He} \rightarrow {}^4\text{He} + p$  at  $T_p = 1.05$  GeV. The errors shown do not include an overall 10% uncertainty accountable to the acceptance determination and to the incident flux calibration.

$\theta_{\text{lab}}({}^4\text{He})$ (deg)	$\cos\theta_{\text{c.m.}}$ proton	$u - u_{\text{max}}$ [(GeV/c) <sup>2</sup> ]	$d\sigma/d\Omega_{\text{c.m.}}$ (nb/sr)
0.25	-0.999 96	-0.000 12	$2.21 \pm 0.22$
1.23	-0.998 98	-0.002 94	$1.74 \pm 0.19$
2.20	-0.996 75	-0.009 38	$1.69 \pm 0.10$
3.18	-0.9932	-0.0196	$1.53 \pm 0.17$
4.15	-0.9884	-0.0333	$1.39 \pm 0.16$
5.13	-0.9824	-0.0509	$1.07 \pm 0.19$
6.10	-0.9751	-0.0718	$0.87 \pm 0.17$
8.54	-0.9514	-0.1401	$0.93 \pm 0.10$
11.95	-0.9058	-0.2718	$1.17 \pm 0.11$

the backward cross sections we parametrized them as a function of the c.m. solid angle  $\Omega_{\text{c.m.}}$ :

$$\begin{aligned} & d\sigma/d\Omega_{\text{c.m.}} \\ &= (d\sigma/d\Omega_{\text{c.m.}})_{180^\circ} \exp[\xi(\Omega_{\text{c.m.}} - 4\pi)]. \end{aligned} \quad (1)$$

The result of such a fit to our present data is shown in Fig. 1. We calculated also the slope  $\xi$  for a compilation ranging from  $T_p \approx 1.997$  to 156 MeV<sup>9,15,17-23</sup> and for our previous data.<sup>1</sup> The parameter  $\xi$  has the advantage of being insensitive to normalization uncertainties between different experiments. Figure 3(a) shows the variation of the  $\xi$  value as a function of the c.m. momentum in the energy range  $1.997 \text{ MeV} \lesssim T_p \lesssim 1.05 \text{ GeV}$  ( $49 \text{ MeV}/c \lesssim P_{\text{c.m.}} \lesssim 1192 \text{ MeV}/c$ ). Three different domains appear. In the low-energy region,  $T_p \lesssim 156 \text{ MeV}$  ( $P_{\text{c.m.}} \lesssim 438 \text{ MeV}/c$ ), the slope  $\xi$  is positive. One observes a discontinuity in the energy variation of  $\xi$  at  $T_p = 23.4 \text{ MeV}$  due to the 16.7-MeV excitation energy of  ${}^5\text{Li}$ . Around 30–40 MeV the variation of  $\xi$  can be linked to the structure observed in the  $d-{}^3\text{He}$  elastic scattering.<sup>19</sup> In the intermediate region,  $156 \text{ MeV} \lesssim T_p \lesssim 500 \text{ MeV}$  ( $168 \text{ MeV}/c \lesssim P_{\text{c.m.}} \lesssim 800 \text{ MeV}/c$ ), the slope is close to zero, which seems to be supported by the preliminary data of Cameron *et al.*<sup>24</sup> At higher energies,  $T_p \gtrsim 500 \text{ MeV}$  ( $P_{\text{c.m.}} \gtrsim 800 \text{ MeV}/c$ ),  $\xi$  is again positive. In our previous results<sup>1</sup> the slope, also shown in Fig. 3(a), was found to increase with energy up to 840 MeV. Our present experiment at 1.05 GeV shows that this trend has been reversed.

To get a general description of the backward  $p-{}^4\text{He}$  scattering up to our present energy 1.05

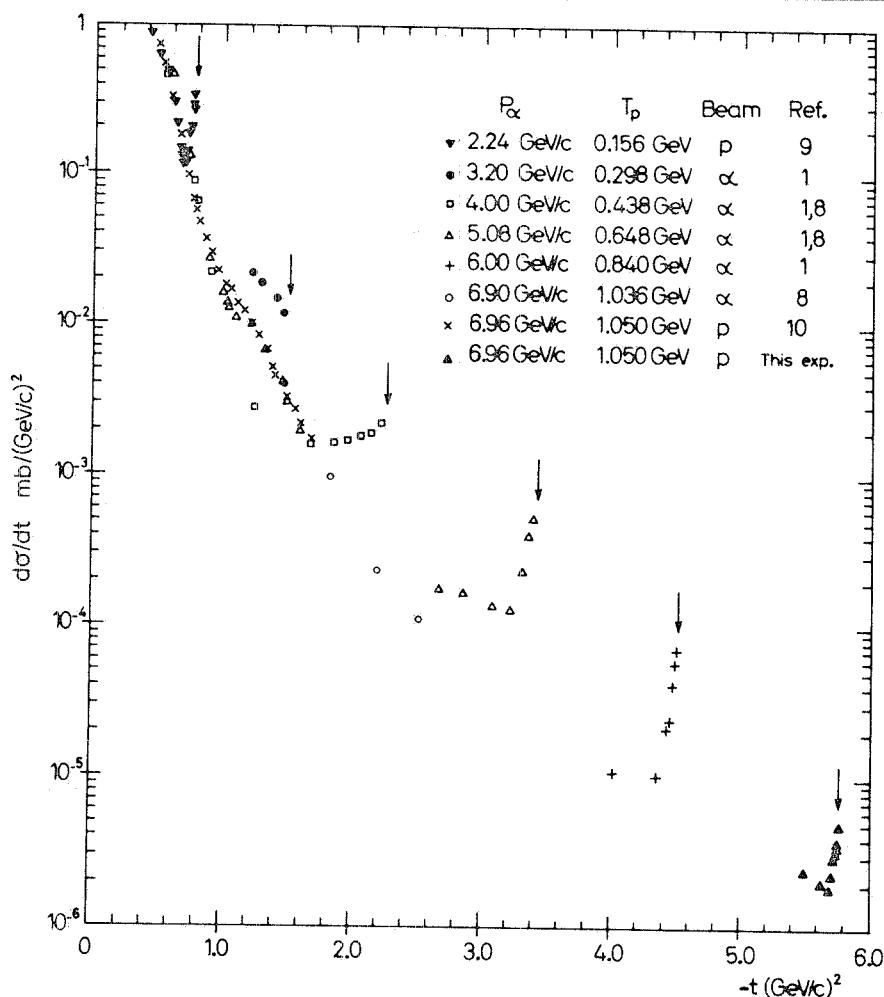


FIG. 2. Summary of high- $t$  data for  $p-^4\text{He}$  elastic scattering. The arrows indicate the  $t$  value for  $\theta_{\text{c.m.}} = 180^\circ$ .

GeV, we have calculated the Born triton-exchange differential cross section which is proportional<sup>5</sup> to  $(k_\alpha^2 + Q^2)^2 [H(Q)]^4$ ;  $k_\alpha^2 = -2\mu\epsilon_s$ ,  $\mu$  and  $\epsilon_s$  being, respectively, the proton-triton reduced mass and separation energy;  $H(Q)$  is the Fourier transform of the  ${}^4\text{He}$  single-particle wave function, and  $Q$ , the momentum of the exchanged triton, is related to the c.m. momentum and scattering angle by

$$Q^2 = \left(\frac{3}{4}P_{\text{c.m.}}\right)^2 + \frac{1}{2}P_{\text{c.m.}}^2(1 + \cos\theta_{\text{c.m.}}). \quad (2)$$

Our Born calculation, not including absorption corrections, leads to cross sections of about one order of magnitude above the experimental data; however, the main features of the backward scattering are qualitatively reproduced. Figure 3(a) shows the calculated slope of the backward cross sections, one can see that the  $\xi$  variation is fairly well predicted in the whole energy range. In particular at 298 MeV the calculated cross section decreases approaching  $180^\circ$  ( $\xi < 0$ ). As an

essential parameter of this calculation is the wave function  $H(Q)$ , the agreement observed in the Fig. 3(a) shows that  $H(Q)$  seems to play an important role in the backward  $p-{}^4\text{He}$  elastic scattering. To illustrate this fact,  $H(Q)$  has been drawn in Fig. 3(b) in its usual momentum representation: The  $\xi$  values are calculated over small  $\cos\theta_{\text{c.m.}}$  regions near  $180^\circ$ , the related  $Q$ 's in the Born cross section are near  $Q(180^\circ) = \frac{3}{4}P_{\text{c.m.}}$ , and hence the  $Q$  scale has been determined from the  $P_{\text{c.m.}}$  scale of Fig. 3(a) using this relation. Then, at the same time, Fig. 3(b) shows the momentum representation of  $H(Q)$  and the values of  $H(Q)$  used in the Born calculation at a given  $P_{\text{c.m.}}$ ; as a consequence this allows to see that there is a correspondence between  $H(Q)$  and the  $\xi$  variation. All the observed trends relate the experimental behavior of the  $p-{}^4\text{He}$  backward elastic scattering to the general features of the triton-exchange mechanism.

We acknowledge the cooperation of the crew and

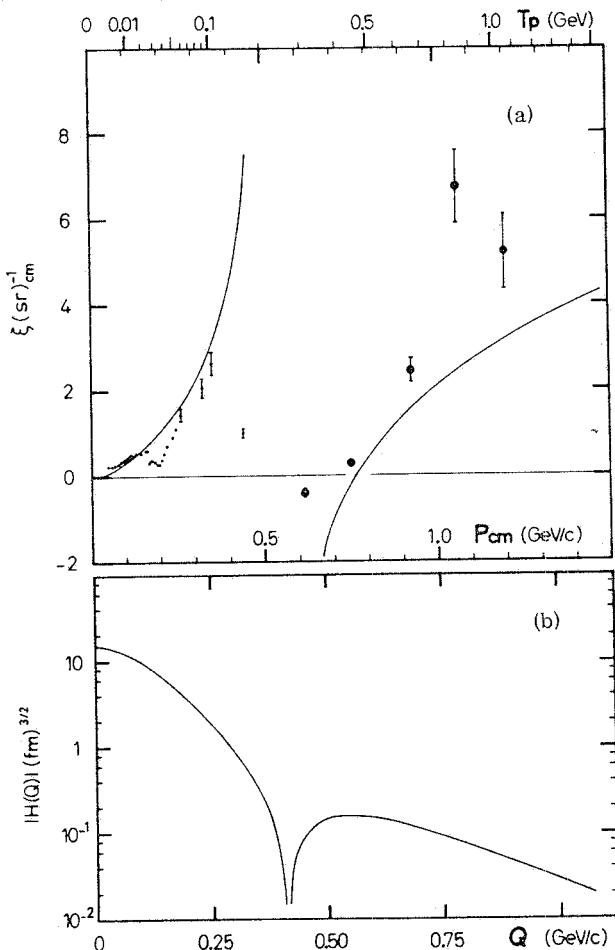


FIG. 3. (a) Slope parameter  $\xi$  as a function of the c.m. momentum,  $P_{\text{c.m.}}$ . The slope resulting from the triton-exchange Born approximation (Ref. 5) (solid line) has been calculated in the angular range of the backward peaks, and has been multiplied by the constant factor 3.5 for the sake of comparison. (b) Absolute value of  $H(Q)$ . The  $Q$  scale is drawn using the formula (2) in the text, the value of  $Q$  corresponding to a given  $P_{\text{c.m.}}$ , being  $Q(180^\circ) = \frac{3}{4}P_{\text{c.m.}}$ . However, at a given incident energy, formula (2) shows that  $Q$  increases as  $\theta_{\text{c.m.}}$  goes away from  $180^\circ$ . Then the Born cross section (Refs. 4 and 5), proportional to  $(k_\alpha^2 + Q^2)^2 [H(Q)]^4$ , has a backward peak [i.e., solid curve  $\xi > 0$  in (a)] for  $Q$  values near  $\theta_{\text{c.m.}} = 180^\circ$ , where  $|H(Q)|$  decreases.

staff of Saturne I, under the direction of Dr. B. Thévenet. We are grateful to Dr. O. Lombard and Dr. A. Małekki for helpful discussions. A liquid helium target of the Département de Physique Nucléaire à Haute Energie was kindly made available to us by Dr. P. Catillon. The technical support of Mr. P. Guillouet and Mr. G. Simonneau is hereby acknowledged.

<sup>(a)</sup>Present address: Physics Department, University of California at Los Angeles, Los Angeles, Calif. 90024.

<sup>1</sup>J. Berger *et al.*, Phys. Lett. **63B**, 111 (1976).

<sup>2</sup>S. A. Gurvitz *et al.*, Ann. Phys. (N.Y.) **90**, 346 (1976).

<sup>3</sup>B. Z. Kopeliovich and I. K. Potashnikova, Yad. Fiz. **13**, 1032 (1971) [Sov. J. Nucl. Phys. **13**, 592 (1971)].

<sup>4</sup>G. J. Igo, in *High Energy Physics and Nuclear Structure—1975*, AIP Conference Proceedings No. 26, edited by D. E. Nagle, A. S. Goldhaber, C. K. Hargrove, R. L. Burman, and B. G. Storms (American Institute of Physics, New York, 1975), p. 77.

<sup>5</sup>H. Lesniak *et al.*, Nucl. Phys. **A267**, 503 (1976).

<sup>6</sup>R. Dymarz and A. Małekki, in *Proceedings of the Seventh International Conference on High Energy Physics and Nuclear Structure, Zurich, 1977*, edited by M. P. Locher (Birkhäuser-Verlag, Basel and Stuttgart, 1978), p. 199.

<sup>7</sup>G. Bizard *et al.*, Nucl. Phys. **A235**, 461 (1977).

<sup>8</sup>J. Berger *et al.*, Phys. Lett. **37**, 1195 (1976).

<sup>9</sup>V. Comparat *et al.*, Phys. Rev. C **12**, 251 (1975).

<sup>10</sup>E. Aslanides *et al.*, Phys. Lett. **68B**, 221 (1977).

<sup>11</sup>C. A. Whitten *et al.*, Ref. 6, p. 220.

<sup>12</sup>R. Dymarz and A. Małekki, Phys. Lett. **66B**, 413 (1977).

<sup>13</sup>S. A. Gurvitz *et al.*, Ann. Phys. (N.Y.) **94**, 223 (1975).

<sup>14</sup>D. R. Thompson *et al.*, Phys. Rev. C **4**, 306 (1971).

<sup>15</sup>L. G. Votta *et al.*, Phys. Rev. C **10**, 520 (1974).

<sup>16</sup>D. R. Thompson *et al.*, Phys. Rev. C **16**, 1 (1977).

<sup>17</sup>A. C. L. Barnard *et al.*, Nucl. Phys. **50**, 604 (1964).

<sup>18</sup>D. Garreta *et al.*, Nucl. Phys. **A132**, 204 (1969).

<sup>19</sup>A. D. Bacher *et al.*, Phys. Rev. C **5**, 1147 (1972).

<sup>20</sup>S. N. Bunker *et al.*, Nucl. Phys. **A133**, 537 (1969).

<sup>21</sup>B. W. Davies *et al.*, Nucl. Phys. **A97**, 241 (1967).

<sup>22</sup>S. Hayakawa *et al.*, J. Phys. Soc. Jpn. **19**, 2004 (1964).

<sup>23</sup>N. P. Goldstein *et al.*, Can. J. Phys. **48**, 2629 (1970).

<sup>24</sup>J. M. Cameron *et al.*, Ref. 6, p. 194.

