# ISTITUTO NAZIONALE DI FISICA NUCLEARE 

Sezione di Trieste

INFN/AE-90/15
22 novembre 1990
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# MANIFESTATIONS OF HEAVY EXTRA NEUTRAL $E_{6}$ GAUGE BOSONS IN $e^{+} e^{-} \rightarrow W^{+} W^{-}$at LEP II 

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#### Abstract

We have studied the manifestations of a new neutral gauge boson ( $Z^{\prime}$ ) with $M_{Z^{\prime}}>\sqrt{s}$, which might exist in $E_{6}$ models, in the proceps $e^{+} e^{-} \rightarrow W^{+} W^{-}$at LEP II. We have found that the differential cross section is quite sensitive to the existence of a heavy $Z^{\prime}$. In particular, $d \sigma / d \cos \theta$ should show the effect of heavier $Z^{\prime}$ bosons with $M_{Z^{\prime}}>350 \mathrm{GeV}$ as an enhanced effect due to the $Z-Z^{\prime}$ mixing.


[^0]Recently there has been renewed interest [1-4] in the possibility of producing two-gauge boson final states in both $e^{+} e^{-}$and in hadron colliders. In the Standard Model (SM), such processes can be used as direct tests of non-abelian gauge boson selfcouplings. In scenarios with extended gauge and scalar sectors, such as $E_{6}$ superstringinspired models [5], the production and decay of new neutral gauge bosons ( $Z^{\prime}$ ) into such final states can probe $Z-Z^{\prime}$ mixing as well as trilinear gauge boson couplings.

In this paper we shall discuss the angular distribution of $W$ pairs produced at the CERN $e^{+} e^{-}$collider LEP II $(\sqrt{s}=200 \mathrm{GeV})$ in the process

$$
\begin{equation*}
e^{+}+e^{-} \rightarrow W^{+}+W^{-} \tag{1}
\end{equation*}
$$

in particular the deviations that can be expected from the SM, and how these could be enhanced by the mechanism of $Z-Z^{\prime}$ mixing for larger values of the $Z^{\prime}$ mass. We shall assume that the mass of this particle is higher than the maximum machine energy $\sqrt{s}=200 \mathrm{GeV}$, so that only indirect $Z^{\prime}$ evidence can be looked for. We anticipate that, although our investigation will be performed for all values $M_{Z^{\prime}}>$ 200 GeV , we shall be particularly interested to the range $M_{Z^{\prime}}>350 \mathrm{GeV}$, where $Z^{\prime}$ effects to reaction (1) turn out to be most significant, and which might be difficult to probe directly even at the TEVATRON Collider experiments [6]. Having high luminosity ( $L=5 \cdot 10^{31} \mathrm{~cm}^{-2} \mathrm{sec}^{-1}$ ), and being in the clean environment of $e^{+} e^{-}$, LEP II will undoubtedly give us a lot of useful information on the physics beyond the SM. For definiteness we will consider in what follows only one class of extended electroweak theories, namely that originating from the breaking of $E_{6}$ in superstringinspired models [5] via the chain

$$
\begin{align*}
E_{6} \rightarrow S O(10) \times U(1)_{\Psi} & \rightarrow S U(5) \times U(1)_{\chi} \times U(1)_{\Psi}  \tag{2}\\
& \rightarrow S U(3)_{c} \times S U(2)_{L} \times U(1)_{Y} \times U(1)_{\alpha}
\end{align*}
$$

From the phenomenological point of view this class of models represents quite a natural scheme, in the context of grand unification, where to accomodate both the SM and an extra $Z^{\prime}$ gauge boson.

We define the physical $Z_{1}$ and $Z_{2}$ states in terms of the gauge $Z$ and $Z^{\prime}$ ones:

$$
\begin{align*}
& Z_{1}=Z \cos \Phi+Z^{\prime} \sin \Phi \\
& Z_{2}=-Z \sin \Phi+Z^{\prime} \cos \Phi \tag{3}
\end{align*}
$$

The lightest extra $Z^{\prime}$ boson will be a linear combination of the generators of the two additional $U(1)$ 's: $Z^{\prime}=Z_{\Psi} \cos \alpha+Z_{\chi} \sin \alpha$. Specific choices of $\alpha$ correspond to different
symmetry breaking patterns which can be related to different subgroup chains, so that the angle $\alpha$ characterizes the direction of the $Z^{\prime}$-related generator in the $E_{6}$ group space. If $E_{6}$ is broken to a rank- 6 group the mixing angle $\alpha$ is in general unconstrained, while in the case $E_{6}$ is broken to a rank- 5 group at the unification scale in superstring theories $\alpha$ is uniquely determined and has the value $\alpha=\arctan \sqrt{3 / 5}=37.8^{\circ}\left(Z_{\eta}\right)$. The values $\alpha=0^{\circ}, \alpha=90^{\circ}$ correspond to pure $Z_{\Psi}$ and $Z_{\chi}$. There is also the special value $\alpha=\arctan (-\sqrt{5 / 3})=127.8^{\circ}\left(Z_{I}\right)$, corresponding to an extra $S U(2)$ group at electroweak energies [5]. Note that all the conclusions valid for the $\chi$ model would also apply to the left-right symmetric model with $g_{R}^{2} \simeq \frac{1}{2} g_{L}^{2}[7,8]$.

The mixing angle $\Phi$ is constrained by existing data, and such constraints critically depend on the value of $\alpha[9-14]$. The situation could be roughly summarized by saying that in general $|\Phi|$ should be limited to the range $|\Phi| \leq 0.05$, although for some values of $\alpha$ the constraints from the LEP data could be even more severe [14]. However, in the case of the $\eta$ model, the experimental constraint is much weaker, because the effects of mixing and of $Z_{\eta}$ exchange tend to cancel each other for large negative mixing angles, so that $|\Phi| \leq 0.1$ could be allowed.

To discuss the influence of the extra $Z_{2}$ boson on the process (1), we separately consider the effects of the indirect modification of the SM couplings to the ordinary $Z$ boson (mainly that of the $e^{+} e^{-}$, and to a much smaller extent that of the $W^{+} W^{-}$ pairs) due to $Z-Z^{\prime}$ mixing, and the direct contribution to the cross section from the virtual $Z_{2}$ exchange diagram. We refer to them as the mixing effect and as the virtual effect respectively, although clearly the latter also implicitly depends on the $Z-Z^{\prime}$ mixing which generates the $\left(W^{+} W^{-} Z^{\prime}\right)$ couplings [15-18].

Starting with the mixing effect, it physically corresponds to the case where the $Z_{2}$ bosons are heavy enough that one can neglect their (virtual) propagator contribution. In this situation the process (1) is described (in the Born approximation) by the same three diagrams as it is in the SM [19-21]: the t-channel $\nu$ exchange and the the s-channel exchanges of neutral gauge bosons $\gamma$ and $Z_{1}$. Thus, to evaluate the effects of the $Z_{2}$ boson, we can use the formulae presented in Ref.[20] in the tree-level approximation to the SM, and make the following replacements of the electron couplings [8]:

$$
\begin{align*}
& v \rightarrow v_{1}=v \cos \Phi+c v^{\prime} \sin \Phi \simeq v+c v^{\prime} \Phi \\
& a \rightarrow a_{1}=a \cos \Phi+c a^{\prime} \sin \Phi \simeq a+c a^{\prime} \Phi \tag{5}
\end{align*}
$$

where

$$
\begin{align*}
v & =-\frac{1}{2}+2 \sin ^{2} \theta_{W}, \quad a=-\frac{1}{2}, \quad c=2 \sqrt{\frac{5}{3}} \sin \theta_{W}  \tag{6}\\
v^{\prime} & =-\frac{\sin \alpha}{\sqrt{10}}, \quad a^{\prime}=\frac{\cos \alpha}{2 \sqrt{6}}-\frac{\sin \alpha}{2 \sqrt{10}}
\end{align*}
$$

The relative contribution of the $Z_{2}$ boson to the differential cross section of process (1) is defined as:

$$
\begin{equation*}
\delta_{W}=\frac{\frac{d \sigma}{d \cos \theta}-\frac{d \sigma^{S M}}{d \cos \theta}}{\frac{d \sigma^{S M}}{d \cos \theta}} \tag{7}
\end{equation*}
$$

( $\theta$ being the angle between the $e^{-}$and the $W^{-}$momenta). Evidently, the contributions to the numerator of Eq.(7) are due to the presence of the "modified" $Z_{1}$ boson exchange diagrams:

$$
\begin{equation*}
\delta_{W}=\frac{\Delta \bar{\sigma}_{\gamma Z}}{\bar{\sigma}^{S M}}+\frac{\Delta \bar{\sigma}_{\nu Z}}{\bar{\sigma}^{S M}}+\frac{\Delta \bar{\sigma}_{Z Z}}{\bar{\sigma}^{S M}} \tag{8}
\end{equation*}
$$

where we use the following notation:

$$
\begin{align*}
\bar{\sigma}_{i j}^{S M} & =\frac{d \sigma_{i j}^{S M}}{d \cos \theta}, & \Delta \bar{\sigma}_{\gamma Z}=\bar{\sigma}_{\gamma Z_{1}}-\bar{\sigma}_{\gamma Z}^{S M}  \tag{9}\\
\Delta \bar{\sigma}_{\nu Z} & =\bar{\sigma}_{\nu Z_{1}}-\bar{\sigma}_{\nu Z}^{S M}, & \Delta \bar{\sigma}_{Z Z}=\bar{\sigma}_{Z_{1} Z_{1}}-\bar{\sigma}_{Z Z}^{S M}
\end{align*}
$$

The modification to the $\left(Z W^{+} W^{-}\right)$vertex is negligible in practice as it is proportional to $\cos \Phi$.

Following Ref.[20], we take into account that

$$
\begin{equation*}
\bar{\sigma}_{\gamma Z} \propto v, \quad \bar{\sigma}_{\nu Z} \propto v+a, \quad \bar{\sigma}_{Z Z} \propto v^{2}+a^{2} \tag{10}
\end{equation*}
$$

and similarly

$$
\bar{\sigma}_{\gamma Z_{1}} \propto v_{1}, \quad \bar{\sigma}_{\nu Z_{1}} \propto v_{1}+a_{1}, \quad \bar{\sigma}_{Z_{1} Z_{1}} \propto v_{1}^{2}+a_{1}^{2}
$$

Replacing Eqs.(9) and (10-10') into Eq.(8), we can express $\delta_{W}$ as follows:

$$
\begin{equation*}
\delta_{W}=c\left[\left(\frac{v^{\prime}}{v}\right) R_{\gamma Z}^{S M}+\left(\frac{v^{\prime}+a^{\prime}}{v+a}\right) R_{\nu Z}^{S M}+2\left(\frac{v v^{\prime}+a a^{\prime}}{v^{2}+a^{2}}\right) R_{Z Z}^{S M}\right] \Phi \tag{11}
\end{equation*}
$$

where $R_{i j}^{S M}=\frac{\bar{\sigma}_{i j}^{S M}}{\bar{\sigma} S M}$ are the contributions to the differential cross section of process (1) in the $S M$, coming from the individual diagrams as well as from the interference terms. For brevity we omit the explicit form of the various $R_{i j}^{S M}$, and limit ourselves to represent their behaviour with the scattering angle $\theta$ in Fig.(1). One we can see
that the effect is maximal in the backward direction $\cos \theta=-1(\sqrt{s}=200 \mathrm{GeV})$, and moreover that in this region the $\nu-Z$ and the $Z-Z$ contributions are by themselves several times greater than the differential cross section as given by the sum of all contributions.

We now evaluate numerically Eq.(11) in the $\Psi, \eta$ and $\chi$ models. One finds, at $\cos \theta=-1$ and $\sin ^{2} \theta_{W}=0.23, M_{Z_{1}}=91.1 \mathrm{GeV}, M_{W}=80 \mathrm{GeV}:$

$$
\delta_{W}=\Phi \begin{cases}+0.80 & (\Psi)  \tag{12}\\ -0.95 & (\eta) \\ -2.52 & (\chi)\end{cases}
$$

(for the model $I$ the result is similar to that for the model $\chi$ ).
Eq.(12) shows the sensitivity of $\delta_{W}$ on the mixing angle $\Phi$ and on the various models. This is even more explicitly displayed in Fig.(2), which essentially shows the dependence of $\delta_{W}$ at $\cos \theta=-1$ on the various values of $\alpha$.

Concerning the angular behaviour of $\left|\delta_{W}\right|$, it is found to have a maximum at $\cos \theta=-1$, where however the cross section is smallest, and to be smaller than the maximum at $\cos \theta=1$, where the cross section is largest. To discuss the size of this mixing effect, taking into account the $\theta$ dependence and the experimental conditions available at LEP II, we can define as an example the ratio:

$$
\begin{equation*}
r=\frac{\Delta \bar{\sigma}}{\delta \bar{\sigma}} \tag{13}
\end{equation*}
$$

where $\Delta \bar{\sigma}$ is the numerator of Eq.(7) and $\delta \bar{\sigma}$ is the statistical uncertainty obtainable on the measured differential cross section. Assuming an integrated luminosity of $500 \mathrm{pb}^{-1}$ in one year run, with $\frac{d \sigma}{d \cos \theta} \simeq 1.5 p b$ at $\cos \theta=-1$ one may expect a sample of about 750 events in that direction, sufficient for $3.5 \%$ measurement. Conversely, with $\frac{d \sigma}{d \cos \theta} \simeq 40 \mathrm{pb}$ at $\cos \theta=1,0.7 \%$ measurements should be possible in the forward region. In Fig.(3) is represented the behaviour of $r$ as a function of $\cos \theta$ in the case of the $\eta$ model, for two choices of the mixing angle $\Phi$ compatible with the present experimental limits. Since we are obviously interested in $r>1$, the most favorable region to look for deviations from the SM is the backward direction. Another point to be noticed is that $r$ changes sign around $\cos \theta \simeq 0.7$ : this makes the total cross section (integrated over $\cos \theta$ ) less convenient to search for this kind of effect, since there is a cancellation. Analogous results are found for the other models considered here.

Coming now to the second effect mentioned at the beginning, the virtual one, this turns out to somewhat decrease the mixing effect discussed above, by an amount
which depends on the value of $M_{Z_{2}}$. This is due to the fact that the two contributions have opposite signs, and consequently show a partial cancellation. The resulting values (mixing plus virtual contributions) of $\delta_{W}$ at $\cos \theta=-1$ are represented as a function of $M_{Z_{2}}$ in Fig.(4). The increasing behaviour reflects the above mentioned cancellation, which becomes less and less effective as being suppressed for increasing $M_{Z_{2}}$ by the propagator effect, so that in principle the curve should flatten to the pure mixing contribution for infinite $M_{Z_{2}}$. However, we should keep in mind, in this regard, that the curves in Fig.(4) should not be naively extrapolated to the asymptotic values of $M_{Z_{2}}$, because the maximum allowed values of $|\Phi|$ also depend on $M_{Z_{2}}$ [13].

Fig.(4) qualitatively shows that the reaction (1) at LEP II should be sensitive to values of the $Z_{2}$ mass larger than (say) 300 GeV , in the optimistic case in which the mixing angle $\Phi$ takes the maximum values presently allowed for the various models. In particular, $Z_{2}$ boson effects would be clearly seen, within the assumed statistical uncertainty, for the $\eta(\chi)$ models at $|\Phi| \approx 0.1$ (0.05) and $M_{Z_{2}} \geq 300 \mathrm{GeV}$, and also at $|\Phi| \geq 0.03(0.015)$ for $M_{Z_{2}} \geq 450 \mathrm{GeV}$.

The range $M_{Z_{2}}<350 \mathrm{GeV}$ should be more conveniently probed either at the TEVATRON Collider or by $e^{+} e^{-} \rightarrow f \bar{f}$ at LEP II [22-24]. In fact the latter reaction is mostly sensitive to the virtual propagator effect rather than to the mixing angle $\Phi$, and in that sense it can be considered as complementary to the process (1).

In summary, the angular distribution of the final $W$ bosons in reaction (1) at LEP II should allow to test $Z-Z^{\prime}$ mixing in $E_{6}$ extensions of the SM, by the enhancement mechanism discussed above. In particular, it might be useful in order to improve the bounds on the mixing angle, especially for the upper range of $Z_{2}$ masses considered in Fig.(4). The enhancement mechanism noted here, based on the dominance of individual contributions to the cross section, could play an interesting role also in other kinds of physical effects beyond the Standard Model.

## Acknowledgements

One of the authors (A.A.P.) would like to express his gratitude to Prof. G.Furlan for continuous encouragement and help, to Profs. G.Costa and I.S.Satsunkevich for helpful discussions and criticism, and to A.Feeley for a careful reading of the manuscript.

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## Figure captions

Fig.(1) : The ratios $R_{i j}^{S M}$ of Eq.(11) as a function of $\cos \theta$ at $\sqrt{s}=200 \mathrm{GeV}: R_{Z Z}^{S M}$ (1); $R_{\nu Z}^{S M}(2) ; R_{\gamma Z}^{S M}$ (3); $R_{Z Z}^{S M}+R_{\nu Z}^{S M}+R_{\gamma Z}^{S M}$ (4).

Fig.(2) : $\delta_{W}$ (Eq.(11)) as a function of the mixing angle $\Phi$ at $\cos \theta=-1, \sqrt{s}=200 \mathrm{GeV}$ for the $\Psi(1), \eta(2), \chi(3)$ and $I(4)$ models.

Fig.(3) : $r$ (Eq.(13)) as a function of $\cos \theta$ for the $\eta$ model at $\sqrt{s}=200 \mathrm{GeV}, \Phi=-0.1$ (1) and $\Phi=-0.05$ (2).

Fig.(4) : $\delta_{W}$ as a function of $M_{Z_{2}}$ at $\cos \theta=-1, \sqrt{s}=200 \mathrm{GeV}$, for the $\chi$ model with $\Phi=-0.05(1), \Phi=-0.01$ (2) and for the $\eta$ model with $\Phi=-0.1(3), \Phi=-0.05$ (4).


Fig. - 1


Fig. - 2


Fig. - 3


Fig. - 4


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