



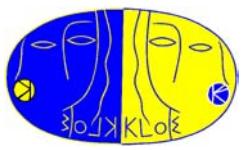
Kaon interferometry at KLOE: status and perspectives

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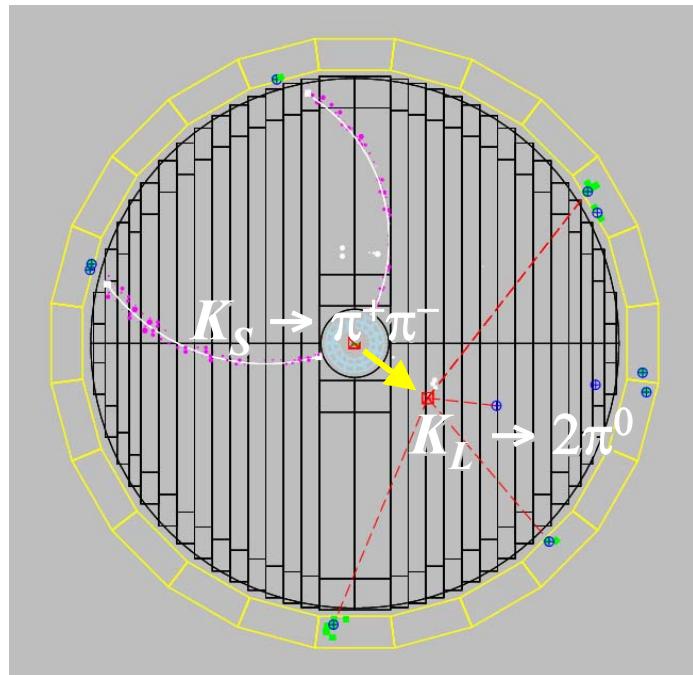


Workshop on e^+e^- in the 1-2 GeV range: Physics and Accelerator Prospects
10-13 September 2003 - Alghero, Italy



Neutral kaons at a ϕ -factory

- $e^+e^- \rightarrow \phi \quad \sigma_\phi \sim 3 \text{ } \mu\text{b}$
 $W = m_\phi = 1019.4 \text{ MeV}$
- $\text{BR}(\phi \rightarrow K^+K^-) = 49.2\%$
- $\text{BR}(\phi \rightarrow K^0\bar{K}^0) = 33.8\%$
- $\text{BR}(\phi \rightarrow \pi^+\pi^-\pi^0) = 15.5\%$
- $\text{BR}(\phi \rightarrow \eta\gamma) = 1.3\%$



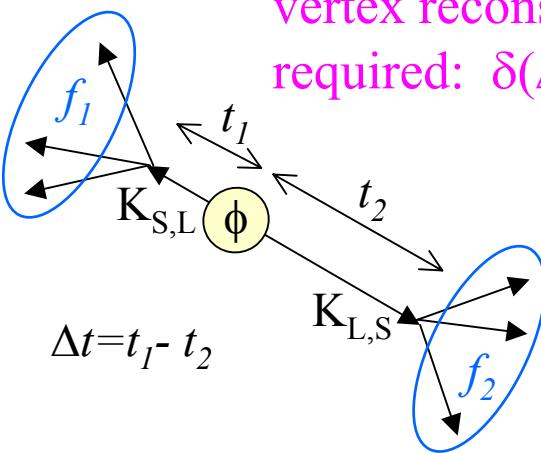
$\sim 10^6$ neutral kaon pairs per pb⁻¹
produced in an antisymmetric quantum state $J^{PC} = 1^{--}$:

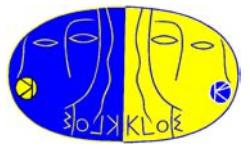
$$|i\rangle = \frac{1}{\sqrt{2}} [|K^0(\vec{p})\rangle |\bar{K}^0(-\vec{p})\rangle - |\bar{K}^0(\vec{p})\rangle |K^0(-\vec{p})\rangle]$$

$$= \frac{N}{\sqrt{2}} [|K_s(\vec{p})\rangle |K_l(-\vec{p})\rangle - |K_l(\vec{p})\rangle |K_s(-\vec{p})\rangle]$$

$$p_K = 110 \text{ MeV/c} \quad \lambda_S = 6 \text{ mm} \quad \lambda_L = 3.5 \text{ m}$$

For interferometry a good K decay vertex reconstruction capability is required: $\delta(\Delta t) \leq 1 \tau_S$





Kaon interferometry: what can be measured

Double differential time distribution:

$$I(f_1, t_1; f_2, t_2) = C_{12} \left\{ |\eta_1|^2 e^{-\Gamma_L t_1 - \Gamma_S t_2} + |\eta_2|^2 e^{-\Gamma_S t_1 - \Gamma_L t_2} - 2|\eta_1||\eta_2| e^{-(\Gamma_S + \Gamma_L)(t_1 + t_2)/2} \cos[\Delta m(t_1 - t_2) + \phi_2 - \phi_1] \right\}$$

where $t_1(t_2)$ is the time of one (the other) kaon decay into $f_1(f_2)$ final state and:

$$\eta_i = |\eta_i| e^{i\phi_i} = \langle f_i | K_L \rangle / \langle f_i | K_S \rangle \quad C_{12} = \frac{N^2}{2} \left| \langle f_1 | K_S \rangle \langle f_2 | K_S \rangle \right|^2$$

$$f_i = \pi^+ \pi^-, \pi^0 \pi^0, \pi l \nu, \pi^+ \pi^- \pi^0, 3\pi^0, \pi^+ \pi^- \gamma \dots \text{etc}$$

characteristic interference term
at a ϕ -factory => interferometry

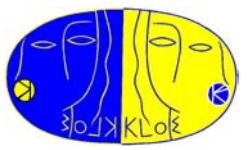
Integrating in $(t_1 + t_2)$ we get the time difference ($\Delta t = t_1 - t_2$) distribution (1-dim plot):

$$I(f_1, f_2; \Delta t \geq 0) = \frac{C_{12}}{\Gamma_S + \Gamma_L} \left[|\eta_1|^2 e^{-\Gamma_L \Delta t} + |\eta_2|^2 e^{-\Gamma_S \Delta t} - 2|\eta_1||\eta_2| e^{-(\Gamma_S + \Gamma_L)\Delta t/2} \cos(\Delta m \Delta t + \phi_2 - \phi_1) \right]$$

$$\text{for } \Delta t < 0 \quad \Delta t \rightarrow |\Delta t| \quad \text{and } 1 \leftrightarrow 2$$

From these distributions for various final states f_i we can measure the following quantities:

$$\Gamma_S, \Gamma_L, \Delta m, |\eta_i|, \arg(\eta_i) = \phi_i$$



Kaon interferometry: main observables

mode

$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$$

measured quantity

$$I(\pi^+ \pi^-, \pi^+ \pi^-; \Delta t)$$

parameters

$$\Delta m \quad (\Gamma_s \quad \Gamma_L)$$

$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^0 \pi^0$$

$$A(\Delta t) = \frac{I(\pi^+ \pi^-, \pi^0 \pi^0; \Delta t > 0) - I(\pi^+ \pi^-, \pi^0 \pi^0; \Delta t < 0)}{I(\pi^+ \pi^-, \pi^0 \pi^0; \Delta t > 0) + I(\pi^+ \pi^-, \pi^0 \pi^0; \Delta t < 0)}$$

$$\Re\left(\frac{\varepsilon'}{\varepsilon}\right) \quad \Im\left(\frac{\varepsilon'}{\varepsilon}\right)$$

$$\phi \rightarrow K_S K_L \rightarrow \pi \ell \nu \pi \ell \nu$$

$$A_{CPT}(\Delta t) = \frac{I(\pi^- e^+ \nu, \pi^+ e^- \bar{\nu}; \Delta t > 0) - I(\pi^- e^+ \nu, \pi^+ e^- \bar{\nu}; \Delta t < 0)}{I(\pi^- e^+ \nu, \pi^+ e^- \bar{\nu}; \Delta t > 0) + I(\pi^- e^+ \nu, \pi^+ e^- \bar{\nu}; \Delta t < 0)}$$

$$\Re \delta_K - \Re\left(\frac{d^*}{a}\right)$$

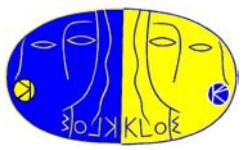
$$\Im \delta_K + \Im\left(\frac{c^*}{a}\right)$$

$$\phi \rightarrow K_S K_L \rightarrow \pi \pi \pi \ell \nu$$

$$A(\Delta t) = \frac{I(\pi^- e^+ \nu, \pi^+ \pi^-; \Delta t) - I(\pi^+ e^- \bar{\nu}, \pi^+ \pi^-; \Delta t)}{I(\pi^- e^+ \nu, \pi^+ \pi^-; \Delta t) + I(\pi^+ e^- \bar{\nu}, \pi^+ \pi^-; \Delta t)}$$

$$A_L = 2(\Re \varepsilon_K - \Re \delta_K + \Re b/a + \Re d^*/a)$$

$$\phi_{\pi\pi}$$



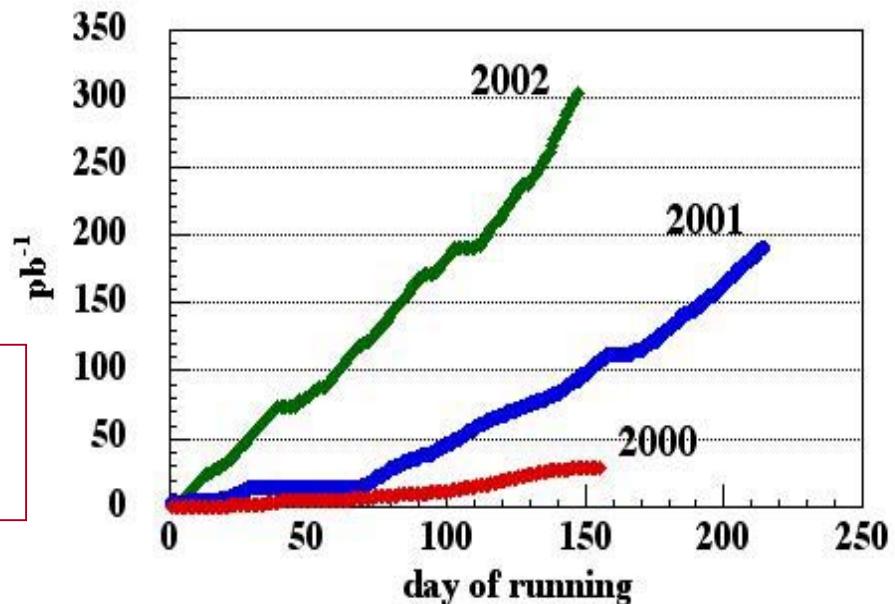
KLOE data taking history

Year	$\int L dt$	pb ⁻¹ /day		
		average	peak	
2000	25 pb ⁻¹	0.1	0.4	First published results
2001	170 pb ⁻¹	0.7	1.8	Luminosity improved but high background Further analyses published
2002	280 pb ⁻¹	2.0	4.5	Higher luminosity and background reduced Analysis in progress

in 2002

$$L_{peak} = 7.8 \times 10^{31} \text{ cm}^{-2} \text{ s}^{-1}$$

An upgrade of the machine has been done.
An increase in luminosity ($> \times 2$)
is expected in the next data taking.



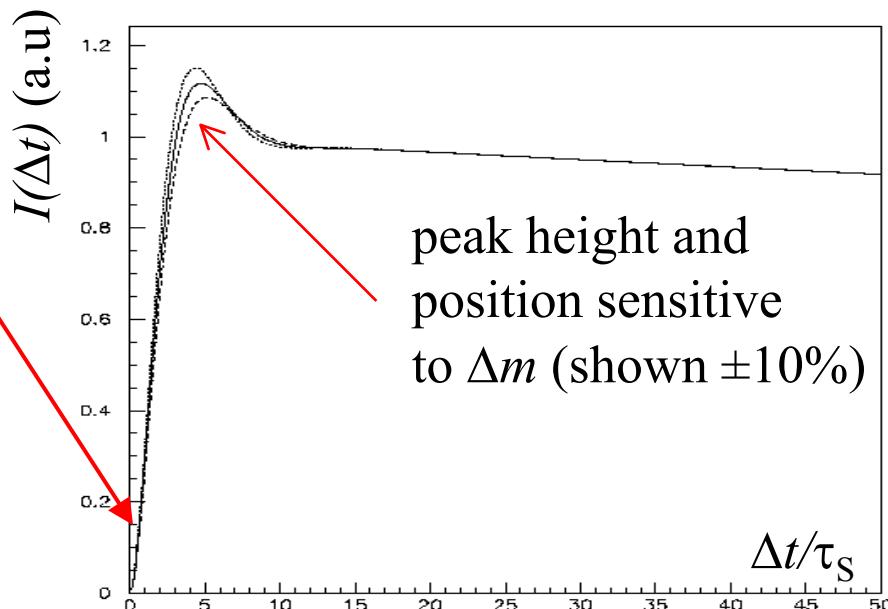


$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$

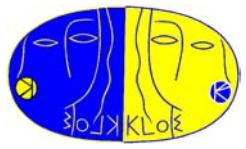
- Same final state for both kaons: $f_1 = f_2 = \pi^+ \pi^-$ ($\pi^0 \pi^0$ or $\pi l \nu -$ same charge leptons)

$$I(\pi^+ \pi^-, \pi^+ \pi^-; |\Delta t|) \propto e^{-\Gamma_L |\Delta t|} + e^{-\Gamma_S |\Delta t|} - 2e^{-(\Gamma_S + \Gamma_L)|\Delta t|/2} \cos(\Delta m |\Delta t|)$$

no simultaneous decays
($\Delta t=0$) in the same
final state due to the
destructive
quantum interference
between the two kaons



- no $\eta_{\pi\pi}$ dependence (only in the scale factor)
- fitting the Δt measured distribution Δm can be evaluated

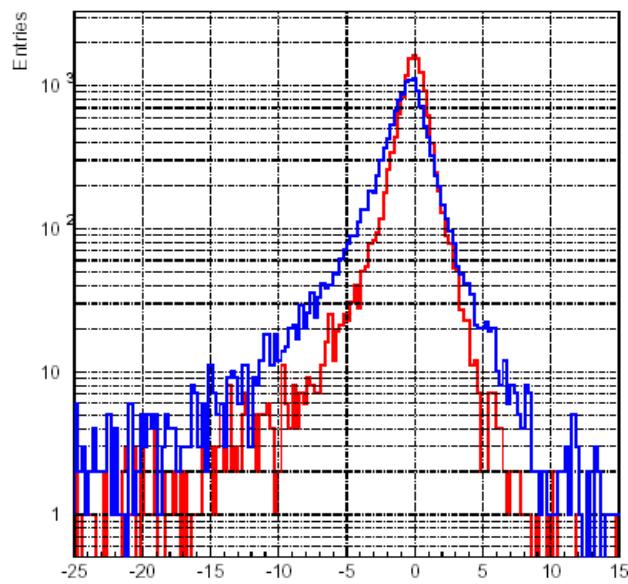


$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$$

A kinematic fit is performed to improve the vertex and Δt resolution:

MC results : before fit

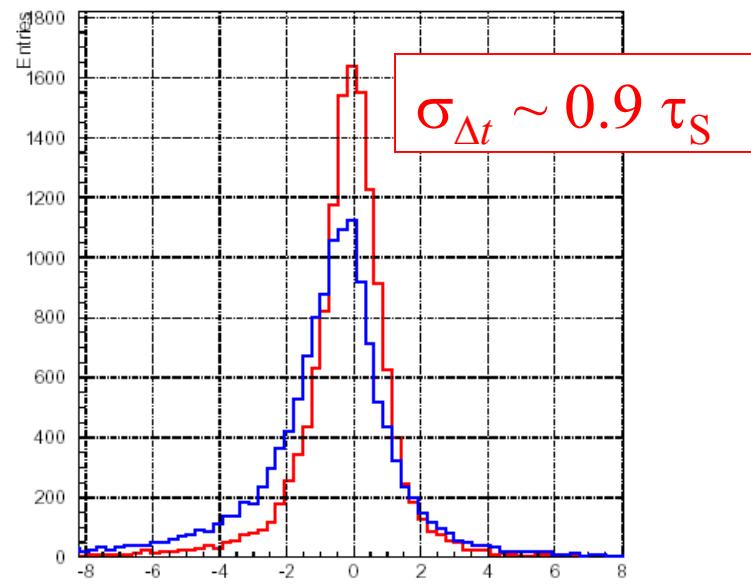
log scale

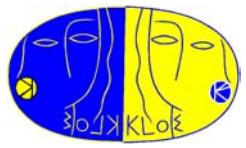


$|\Delta t|_{rec} - |\Delta t|_{true}$ in τ_S units

after fit

linear scale





$$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$$

Fit including Δt resolution and efficiency effects + regeneration:

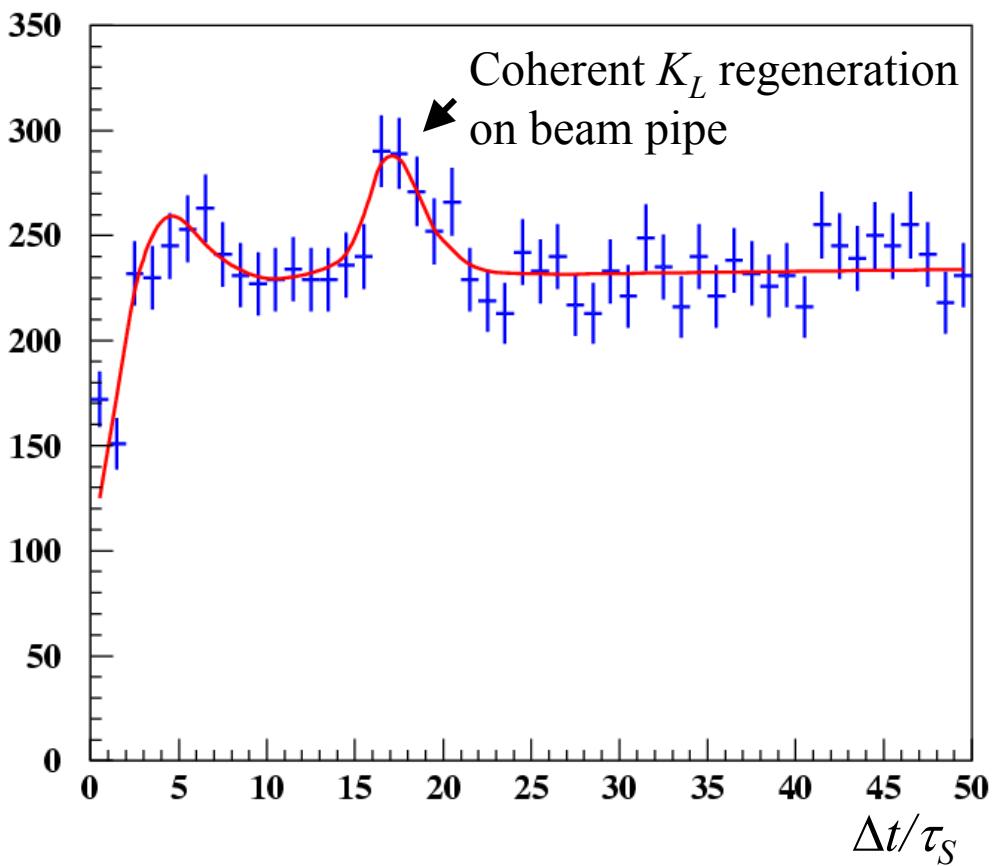
Γ_S, Γ_L fixed from PDG

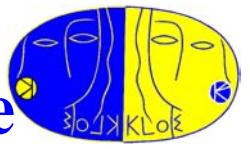
KLOE preliminary
340 pb⁻¹ (2001 + 2002 data)

$$\Delta m = (5.64 \pm 0.37) \times 10^{-11} \hbar \text{ s}^{-1}$$

PDG '02: $(5.301 \pm 0.016) \times 10^{-11} \hbar \text{ s}^{-1}$

At a new ϕ -factory with 500 fb⁻¹:
 $\delta \Delta m \sim 0.009 \times 10^{-11} \hbar \text{ s}^{-1}$





$\phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- \pi^+ \pi^-$: measurement of decoherence

$$I(\pi^+ \pi^-, \pi^+ \pi^-; |\Delta t|) \propto e^{-\Gamma_L |\Delta t|} + e^{-\Gamma_S |\Delta t|} - 2 \cdot (1 - \zeta) \cdot e^{-(\Gamma_S + \Gamma_L)|\Delta t|/2} \cos(\Delta m |\Delta t|)$$

interference term modified introducing a decoherence parameter ζ :

$\zeta = 0$ → "orthodox" QM

$\zeta = 1$ → Furry's hypothesis (spontaneous factorization) [W.Furry, P.R.49 (1936) 393]

decoherence ζ depends on the basis in which is written the initial state (QM not!):

$$K_S K_L - K_L K_S \quad \text{or} \quad K^0 \bar{K}^0 - \bar{K}^0 K^0 \quad \dots$$

For a generic basis $\{K_\alpha, K_\beta\}$ we can write:

$$I(f_1, t_1; f_2, t_2) = \frac{1}{2} \left[\left| \langle f_1 | K_\alpha(t_1) \rangle \langle f_2 | K_\beta(t_2) \rangle \right|^2 + \left| \langle f_1 | K_\beta(t_1) \rangle \langle f_2 | K_\alpha(t_2) \rangle \right|^2 - 2 \cdot (1 - \zeta_{K_\alpha, K_\beta}) \cdot \Re \left(\langle f_1 | K_\beta(t_1) \rangle \langle f_2 | K_\alpha(t_2) \rangle \langle f_1 | K_\alpha(t_1) \rangle^* \langle f_2 | K_\beta(t_2) \rangle^* \right) \right]$$

R.A. Bertlmann et al., Phys. Rev. D60 (1999) 114032
using CPLEAR data obtain:

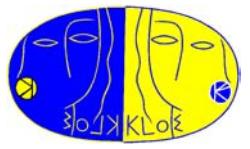
$$\zeta_{K_S, K_L} = 0.13 \pm 0.16$$

$$\zeta_{K^0, \bar{K}^0} = 0.4 \pm 0.7$$

KLOE VERY PRELIMINARY (340 pb⁻¹):

$$\zeta_{K_S K_L} = 0.12 \pm 0.08$$

$$\zeta_{K^0 \bar{K}^0} = (0.8 \pm 0.5) \times 10^{-5}$$



Background due to $\phi \rightarrow (f_0 + a_0)\gamma \rightarrow K^0\bar{K}^0\gamma$

$$\phi \rightarrow (f_0 + a_0)\gamma \rightarrow K^0\bar{K}^0\gamma$$

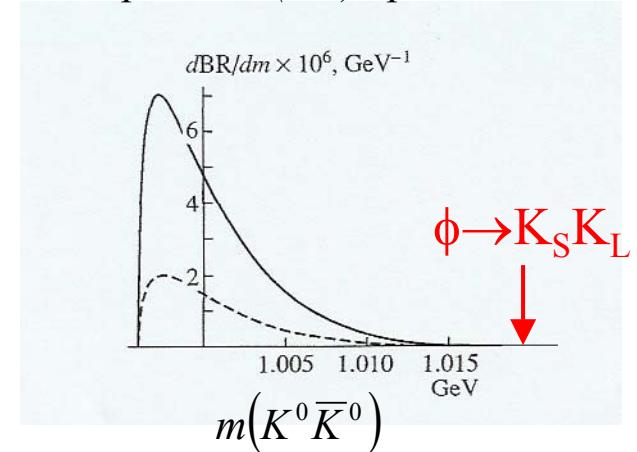
the kaon pair is in a C-even state:

$$|i\rangle = \frac{1}{\sqrt{2}} \{ K^0\bar{K}^0 + \bar{K}^0K^0 \} \approx \frac{1}{\sqrt{2}} \{ K_SK_S - K_LK_L \}$$

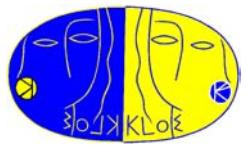
Recent evaluations of $\phi \rightarrow (f_0 + a_0)\gamma \rightarrow K^0\bar{K}^0\gamma$ report a BR in the range $(1 \div 4) \times 10^{-8}$
 [1] J.A. Oller, Nucl.Phys. A714 (2003) 161 ; [2] N.N. Achasov, V.V. Gubin, Phys. Rev D64 (2001)
 094016 ; Phys.Atom.Nucl. 65 (2002) 1939]

The most recent one based on KLOE results on $\phi \rightarrow \pi^0\pi^0\gamma$ and $\phi \rightarrow \eta\pi^0\gamma$.

expected $m(KK)$ spectrum



The impact of this background on the interferometry measurements is negligible at KLOE
...and also at a new 500 fb⁻¹ ϕ -factory

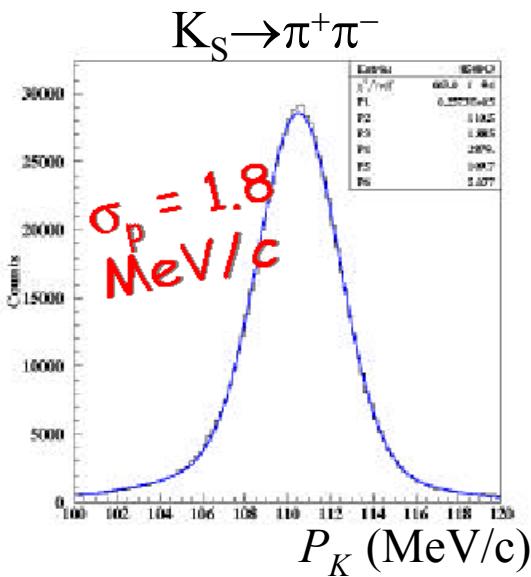


Background due to $\phi \rightarrow (f_0 + a_0)\gamma \rightarrow K^0\bar{K}^0\gamma$

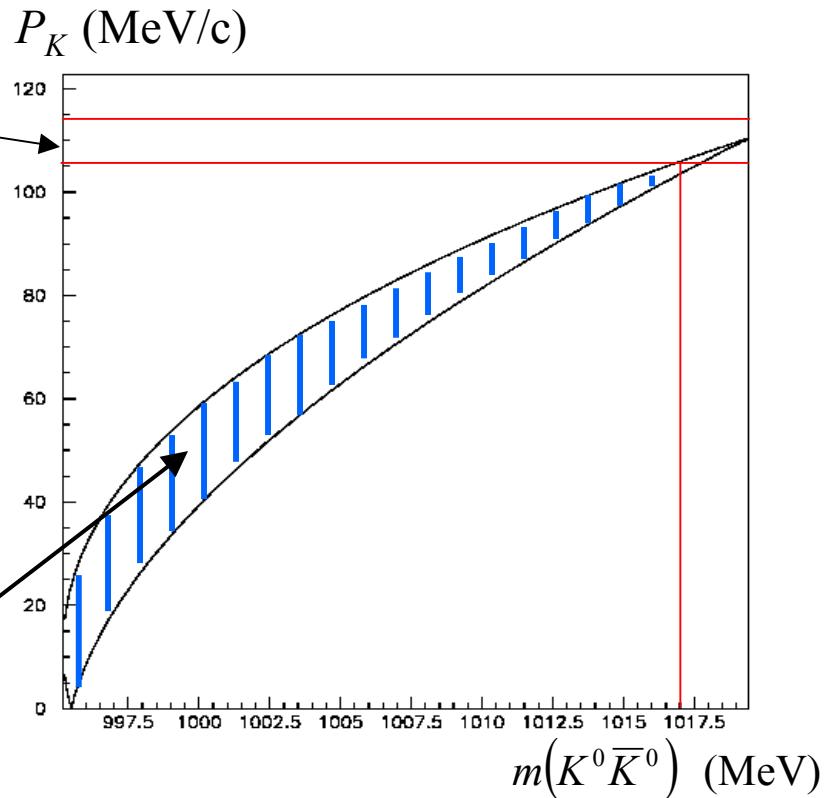
This background can be largely reduced exploiting:

1. different spatial behaviour of decay distributions
2. detection of the radiated photon with $E_\gamma \sim 20 MeV}$
3. measurement of at least one kaon momentum (e.g. in ε'/ε measurements)

A 3σ cut on P_K will select $m(K^0\bar{K}^0) > 1017$ MeV

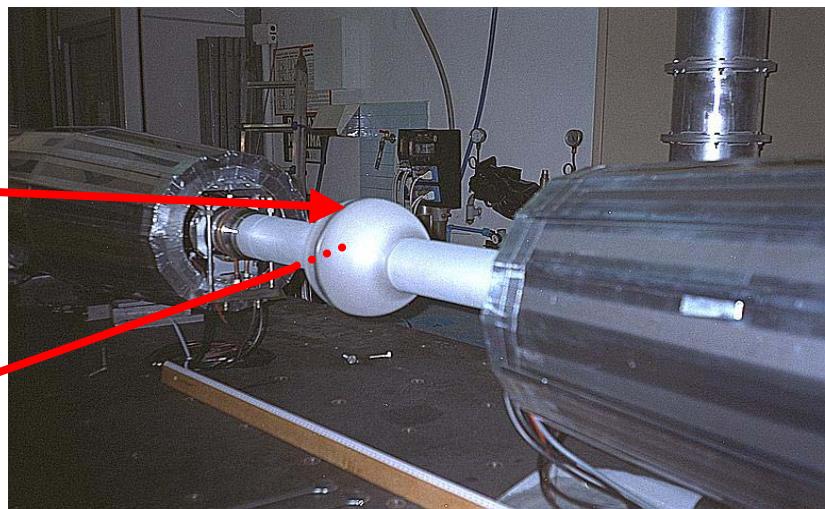
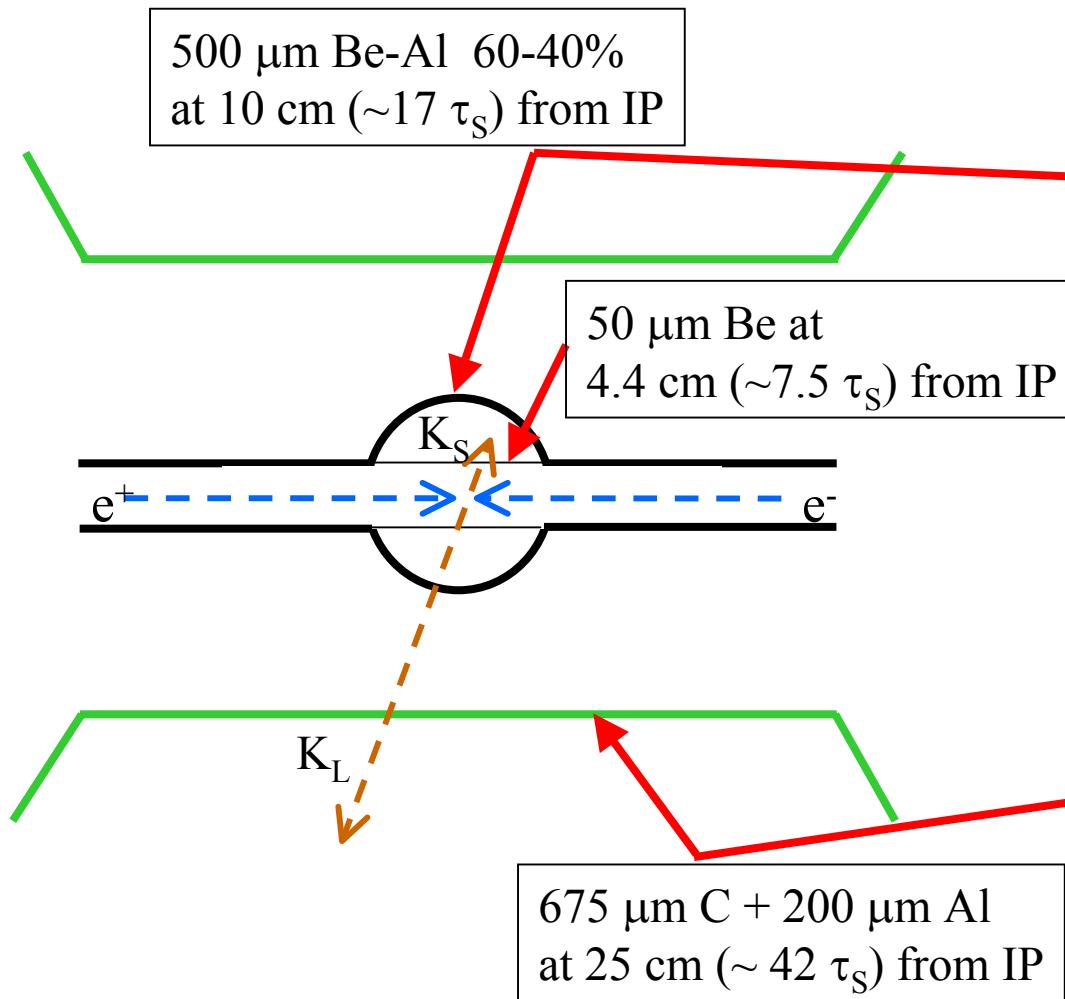


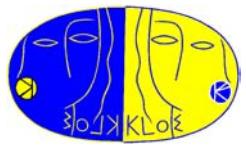
Kaon momentum is kinematically limited inside this band



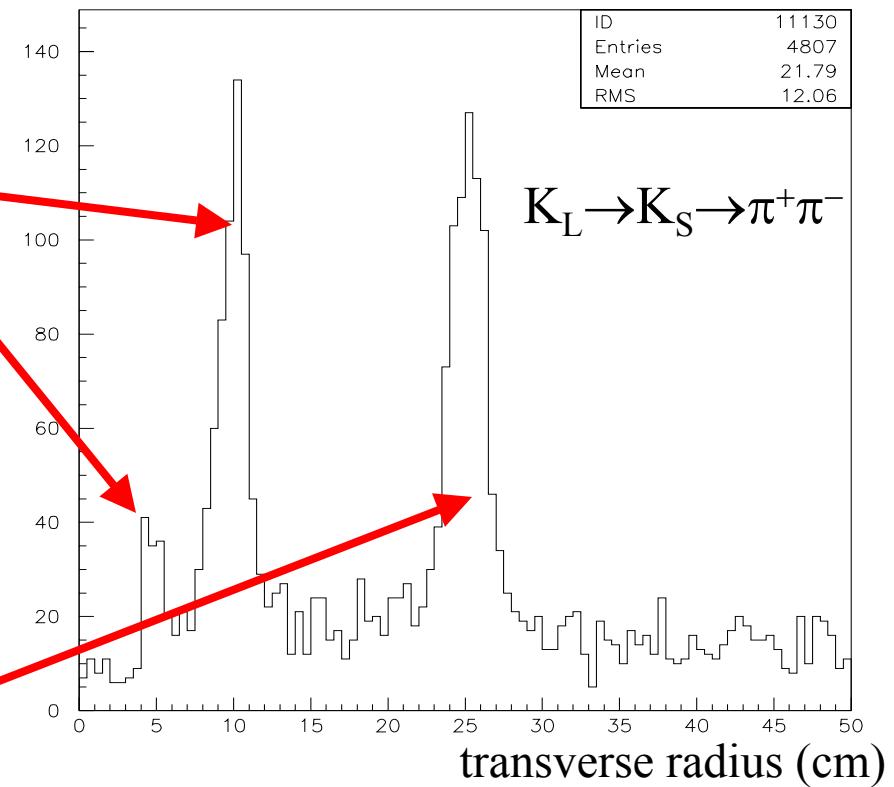
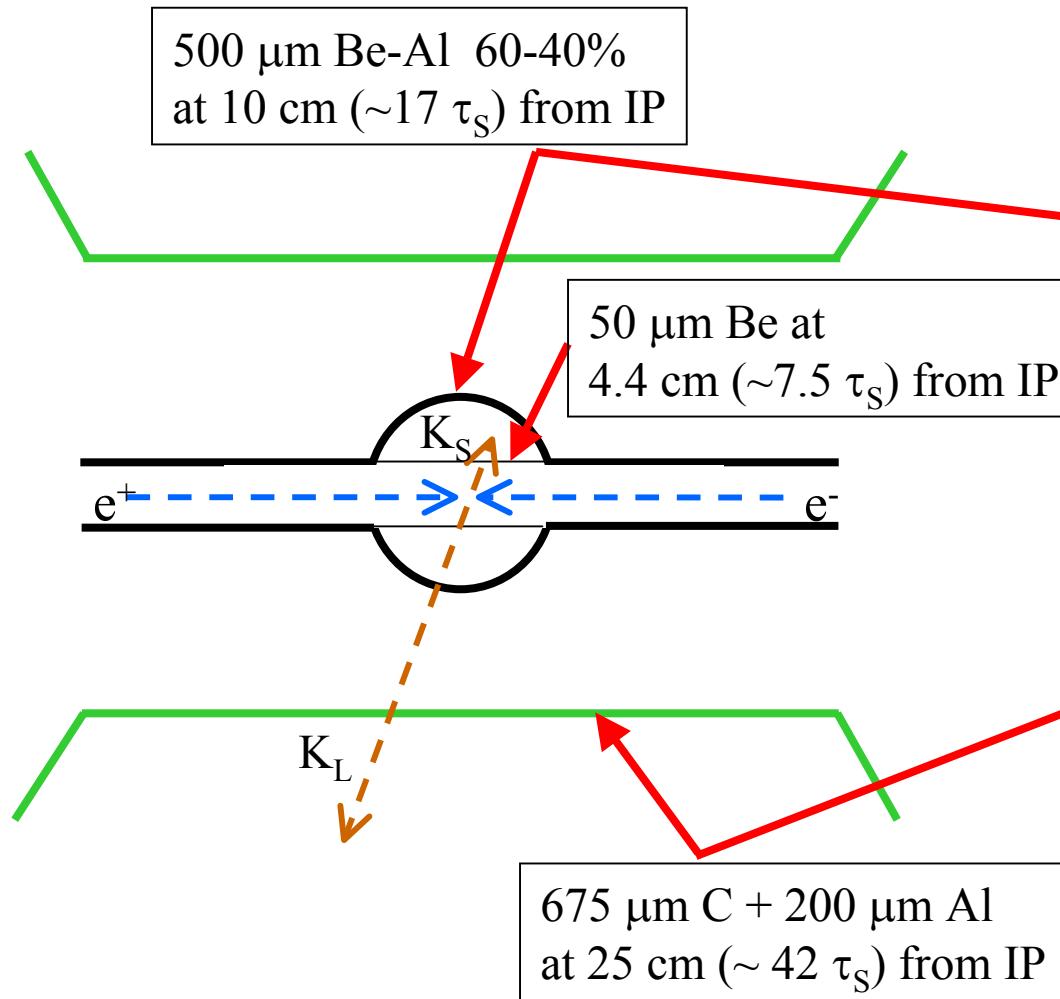


Regenerators

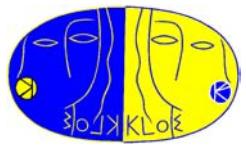




Regenerators



Incoherent Regeneration

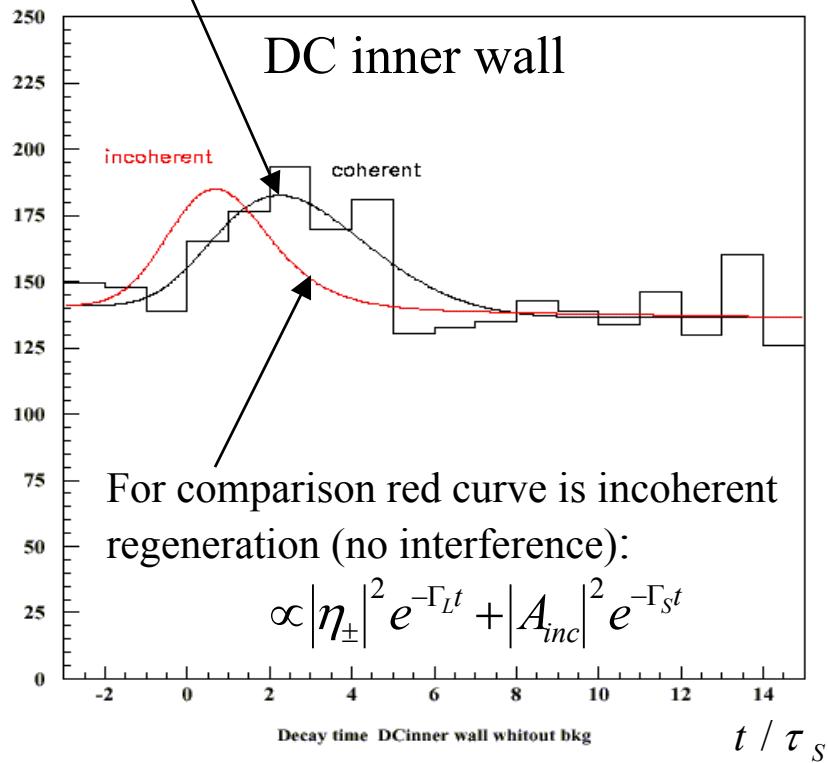


Coherent regeneration

Coherent regeneration can occur only in the strictly forward direction:

$$|K_L\rangle \rightarrow |K_L\rangle + \rho_{coh} |K_S\rangle \quad \rho_{coh} = |\rho_{coh}| e^{i\phi_{coh}} \text{ is the regeneration parameter}$$

$$I(\pi^+ \pi^-, t) = \left| \langle \pi^+ \pi^- | K_S \rangle \right|^2 \left[|\eta_\pm|^2 e^{-\Gamma_L t} + |\rho_{coh}|^2 e^{-\Gamma_S t} + 2|\eta_\pm||\rho_{coh}| e^{-(\Gamma_S + \Gamma_L)t/2} \cos(\Delta m t + \phi_{coh} - \phi_\pm) \right]$$

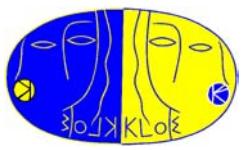


This interference term is important for thin regenerators, i.e. when $|\rho_{coh}| \sim |\eta_\pm|$ as for the beam pipe and inner DC wall

- incoherent regeneration subtracted
- fit including t resolution effects
- preliminary KLOE results (340 pb^{-1})
(DC inner wall):

$$|\rho_{coh}| = (16.6 \pm 6.6) \times 10^{-4}$$

$$\phi_{coh} = -1.19 \pm 0.27 \text{ rad}$$



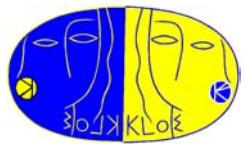
Near future

- KLOE is refining analysis tools for interferometry
- need at least $10 \times$ more data to begin interferometry program
- Examples of estimated uncertainty @ 10 fb^{-1} are:

$$\text{on } \Re\left(\frac{\varepsilon'}{\varepsilon}\right) \quad \Re\delta - \Re\left(\frac{d^*}{a}\right) \quad \sim 5 \times 10^{-4}$$

$$\text{on } \Im\left(\frac{\varepsilon'}{\varepsilon}\right) \quad \Im\delta + \Im\left(\frac{c^*}{a}\right) \quad \sim 20 \times (5 \times 10^{-4})$$

- Measurements of ***Im*** parts are less precise (w.r.t. ***Re***) mainly because of
 - less statistics (interference term lasts $\sim 2\tau_s$)
 - decay vertex resolution effects



Future

At a new ϕ -factory providing an integrated luminosity of $\sim 500 \text{ fb}^{-1}$:

- Knowledge of Δm , Γ_S , Γ_L improved
- Measurement of the ***Im*** of CP and CPT parameters at a precision level comparable with present one on ***Re*** might be feasible
- Interferometry with rarer final state should be feasible (or improved)
- Several proposed QM tests at a ϕ -factory - almost all requiring very high statistics - could be possible