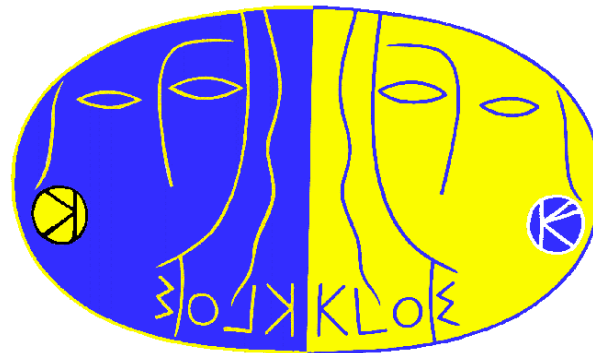


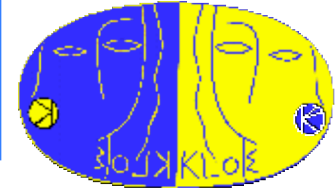
# *Measurement of the $e^+e^-$ hadronic cross section at DAΦNE via radiative return*

**Stefan E. Müller**  
**Institut für Exp. Kernphysik,**  
**Universität Karlsruhe**  
*(for the KLOE collaboration)*

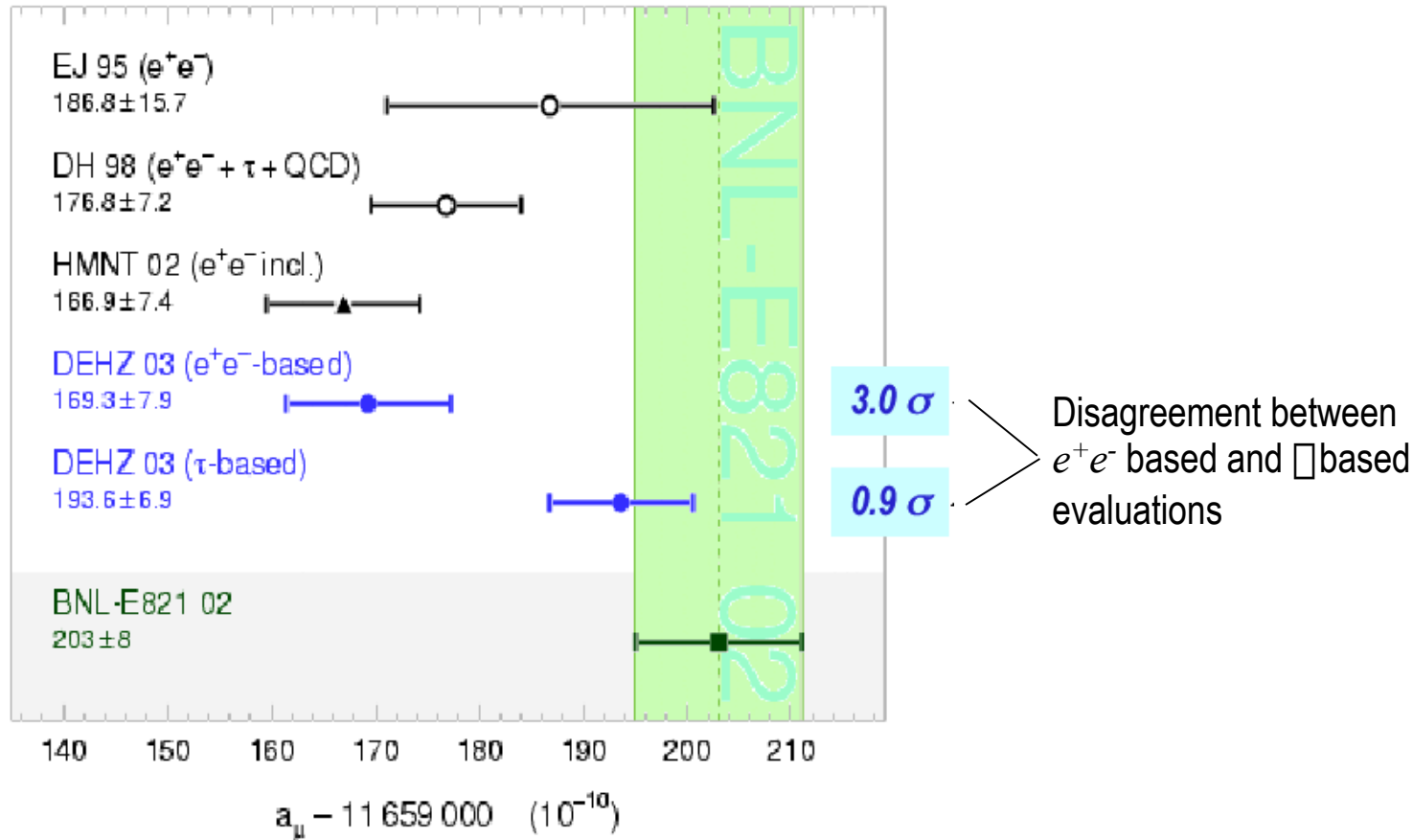


*Photon 2003 - International conference on the structure  
and interactions of the photon*  
*Frascati, 7.-11. April 2003*

# Status on $(g-2)_\mu$ :

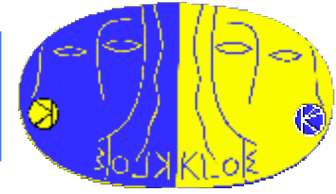


Davier, Eidelman, Höcker, Zhang: hep-ph/0208177v3

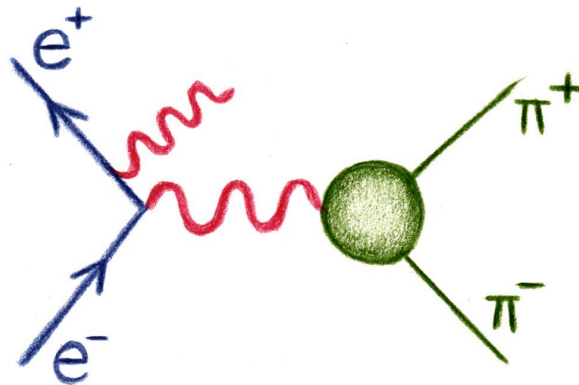


- The nature of the difference in the two theoretical evaluations of  $a_\mu^{\text{had}}$  has to be understood in order to claim a discrepancy between (SM-)theory and experiment
- More and better information on the **hadronic contribution** to the SM calculation of  $a_\mu$  could help to clarify this difference and (together with a further reduction of the experimental error) give the discrepancy between theory and experiment a higher significance

# $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ with ISR:



Particle factories have the opportunity to measure the cross section  $\sigma(e^+e^- \rightarrow \text{hadrons})$  as a function of the hadronic c.m.s energy  $M_{\text{hadrons}}^2$  by using the radiative return.



$$\frac{d\sigma(e^+e^- \rightarrow \text{hadrons} + \gamma)}{dM_{\text{hadrons}}^2}$$

This method (S. Binner, J.H. Kühn, K. Melnikov, Phys. Lett. B 459, 1999) is a complementary approach to the standard energy scan.

## advantage

Data comes as by-product of standard program

Systematic errors from **Luminosity**, **s**, ...  
**enter only once** for each point of  $M_{\text{hadrons}}^2$

## disadvantage

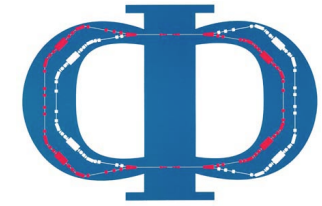
Requires precise calculations of Initial State Rad.

→ **EVA + Phokhara MC Generator**

Requires good suppression (or understanding)  
of Final State Rad.

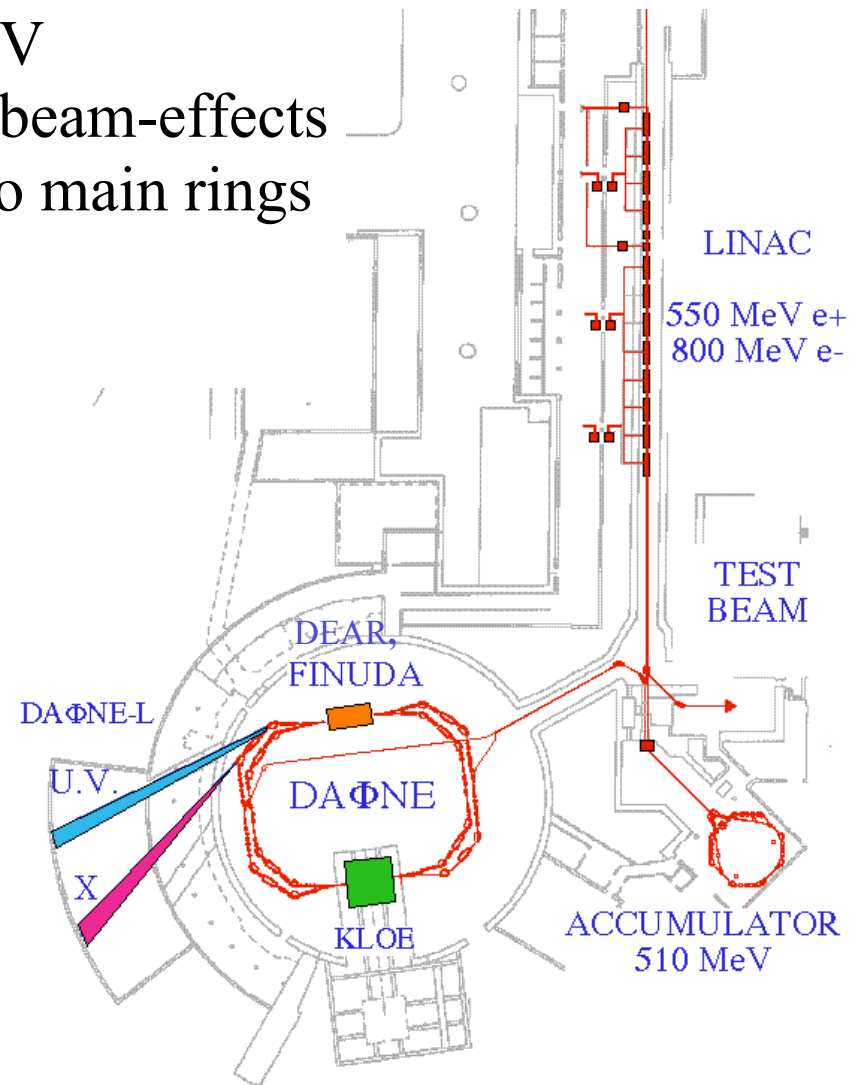
# DAΦNE: A $\Phi$ -Factory

(Double Annular  $\Phi$ -Factory for Nice Experiments)

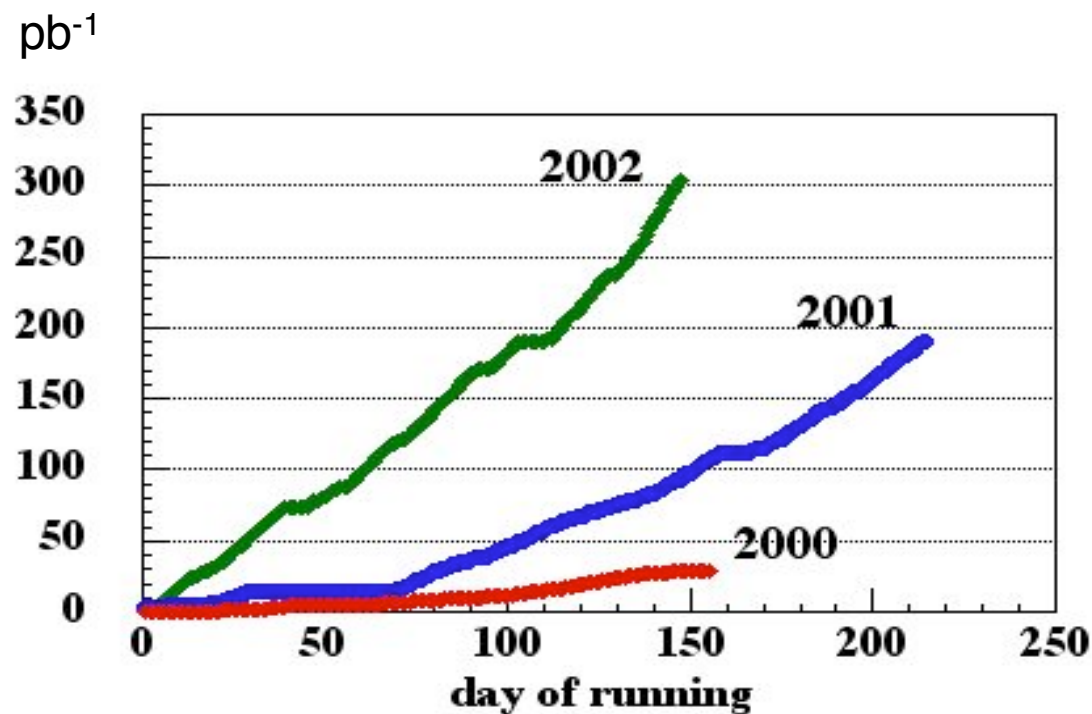
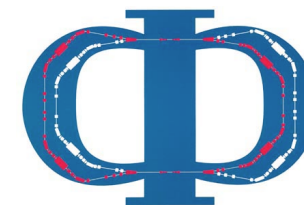


- $e^+e^-$  - collider with  $\sqrt{s} = m_\Phi \approx 1.020$  GeV
- two separate rings to minimize beam-beam-effects
- accumulator for efficient injection into main rings
- two interaction points:  
KLOE and DEAR/FINUDA

<i>BR's for selected <math>\Phi</math> decays</i>	
$K^+K^-$	49.1%
$K_S K_L$	34.1%
$\pi\pi + \pi^+\pi^-\pi^0$	15.5%



# DAΦNE: Performance



**2000 run : 25 pb<sup>-1</sup>**  $7.5 \times 10^7$  □

**2001 run: 190 pb<sup>-1</sup>**  $5.7 \times 10^8$  □

**2002 run: 300 pb<sup>-1</sup>**  $9.0 \times 10^8$  □

DAΦNE Backgr. reduced

Peak Luminosity@KLOE IP:

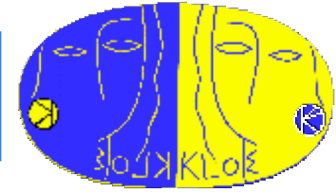
$7.8 \cdot 10^{31} \text{cm}^{-2}\text{s}^{-1}$

max int. Luminosity in one day:

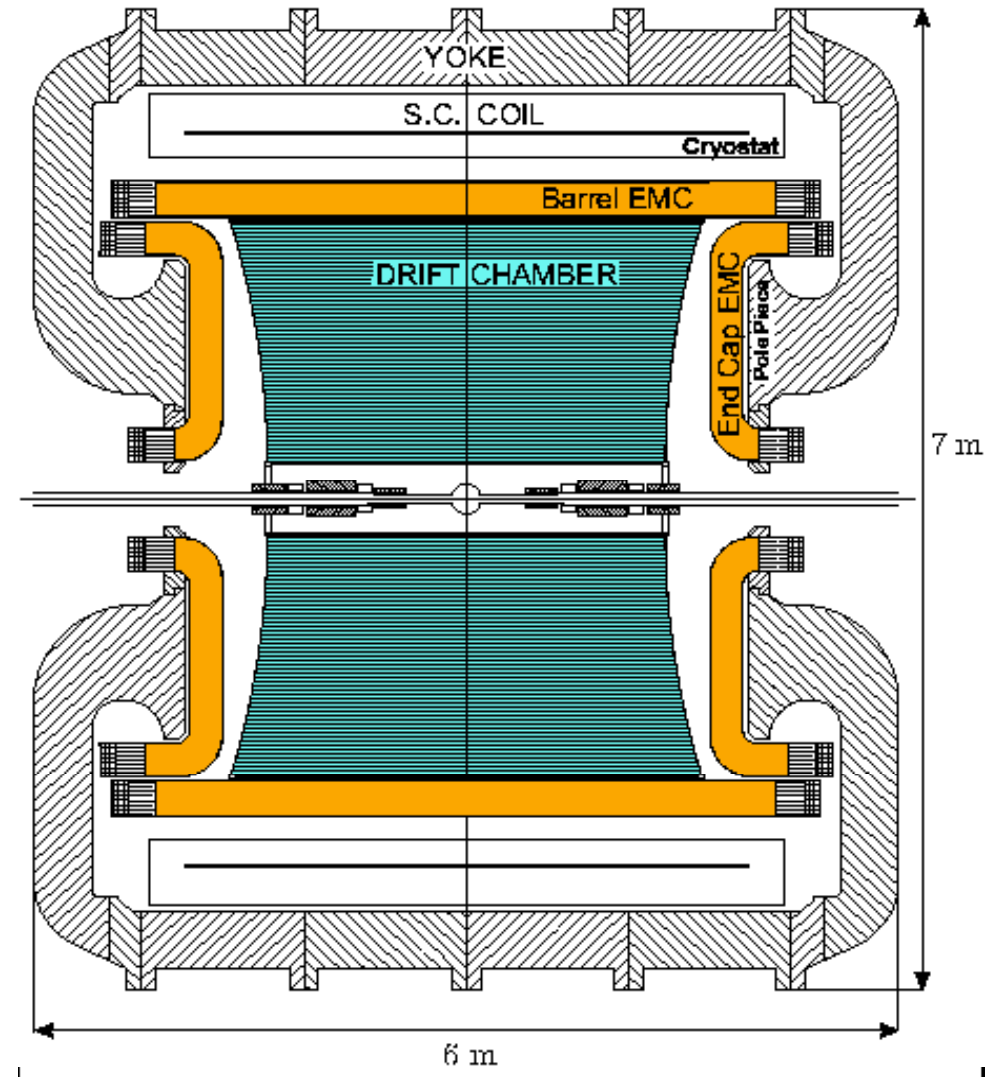
$4.5 \text{ pb}^{-1}$

# KLOE:

(KLOng Experiment)

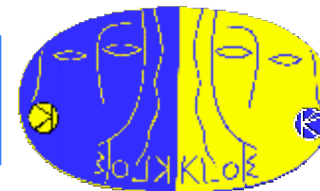


- **Magnet:**  
Superconducting coil ( $B=0.5$  T)
- **EM Calorimeter:**  
Lead/Scintillating fibres  
4880 PM
- **Driftchamber:**  
12582 Sense Wires  
52140 wires in total
- **Beryllium Beampipe:**  
 $R=10$  cm, 0.5 mm thick



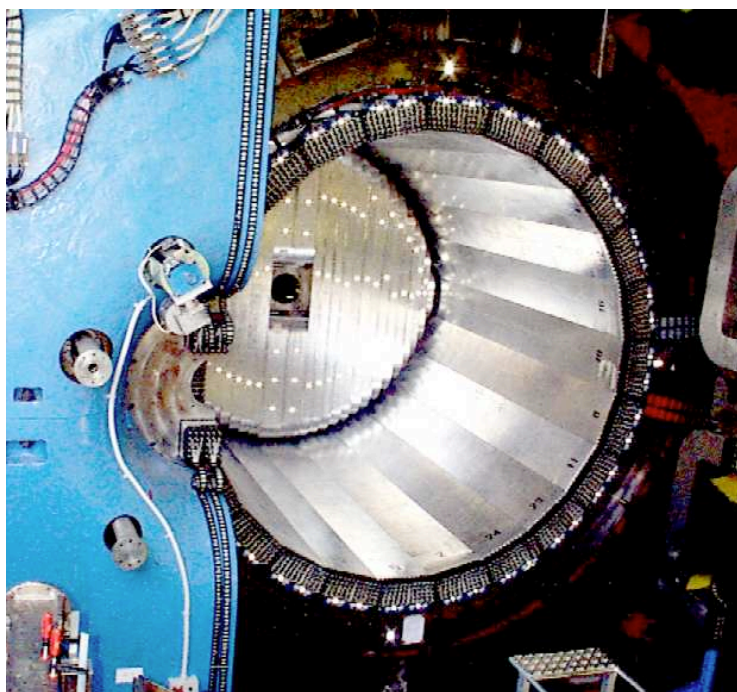


# KLOE:



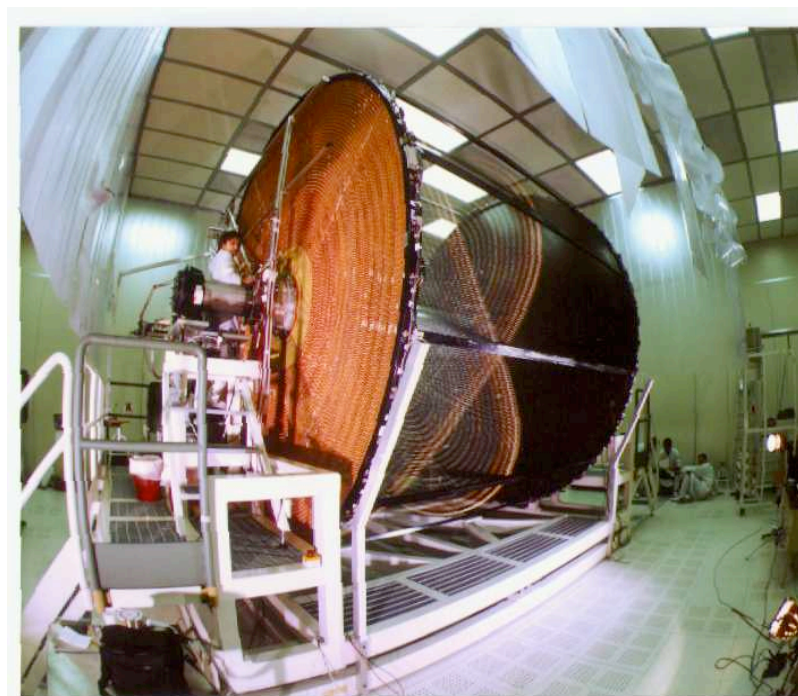
$$\sigma_E/E = 5.7\% / \sqrt{E(\text{GeV})}$$
$$\sigma_T = 54 \text{ ps} / \sqrt{E(\text{GeV})} \oplus 50 \text{ ps}$$

(Bunch length contribution subtracted from constant term)



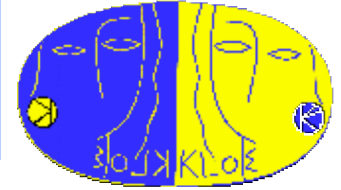
Electromagnetic calorimeter

Driftchamber



$$\sigma_p/p = 0.4\% \text{ (for } 90^\circ \text{ tracks)}$$
$$\sigma_{xy} \approx 150 \text{ } \mu\text{m}, \sigma_z \approx 2 \text{ mm}$$

# Signal selection:



**Pion tracks** are measured at angles  
 $40^\circ < \theta < 140^\circ$

**Photons** are required to be within  
 $\theta < 15^\circ$  and  $\theta > 165^\circ$

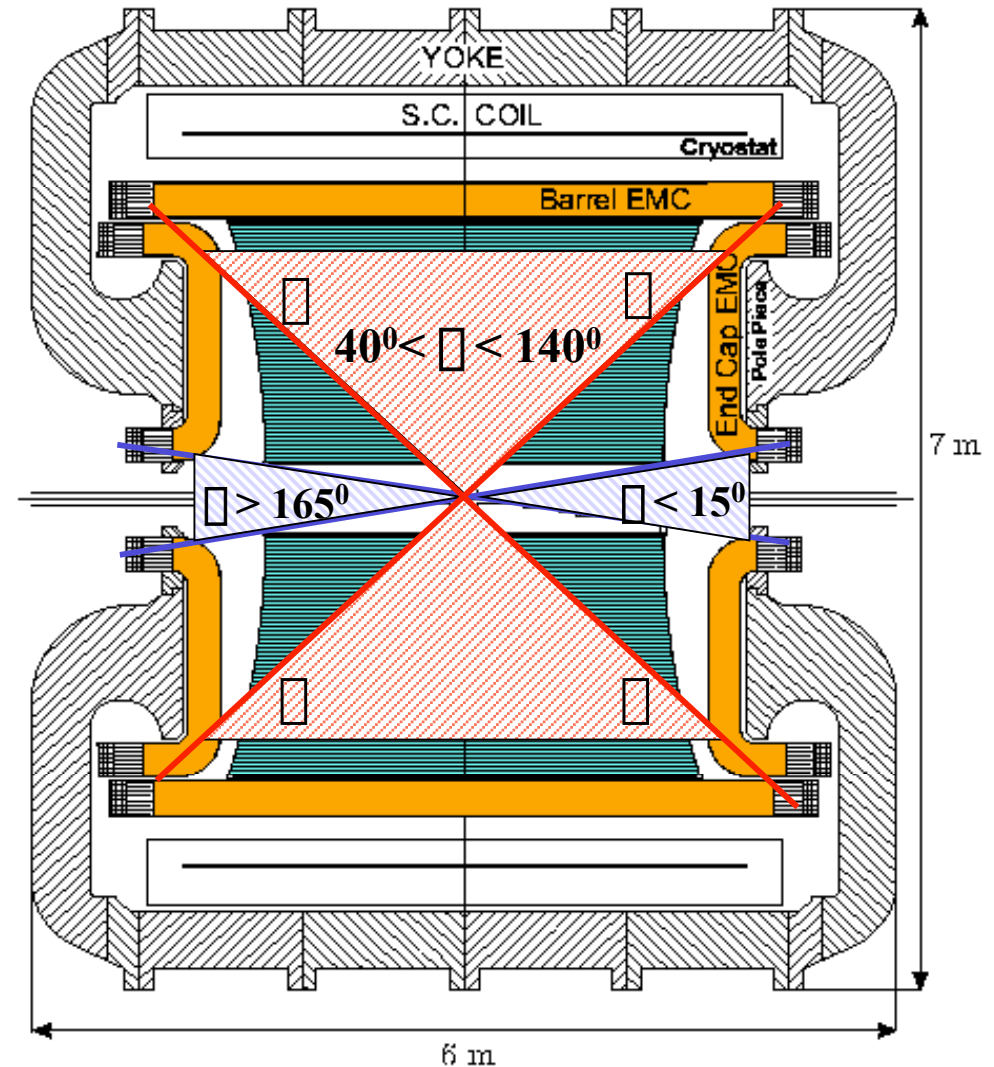
Photons cannot be detected efficiently with EmC,

untagged measurement in which we cut on the direction of the missing momentum

The choice of this kinematical region was motivated by:

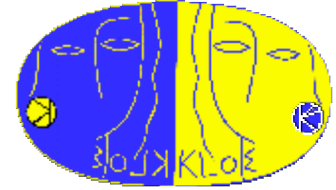
- small relative contribution of **FSR**
- reduced background contamination:

- $e^+e^- \rightarrow \pi^+\pi^-$   $e^+e^- \rightarrow \pi^+\pi^-$
- $e^+e^- \rightarrow \pi^+\pi^- \pi^0$   $\pi^+\pi^-\pi^0$
- $e^+e^- \rightarrow \pi^+\pi^- \pi^+\pi^-$   $\pi^+\pi^-\pi^+\pi^-$

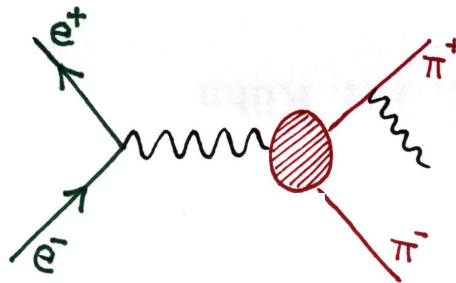




# FSR suppression:

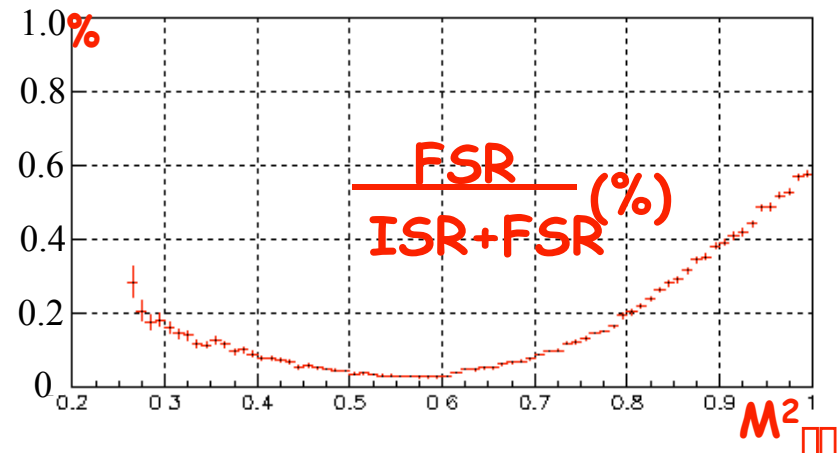
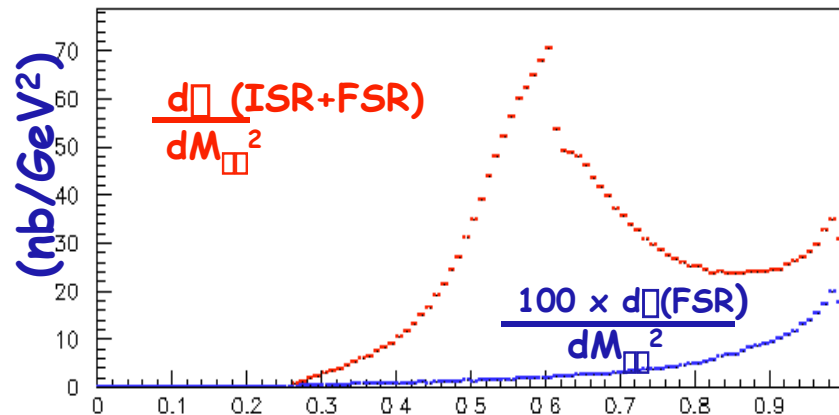


Our approach is to treat **F**inal **S**tate **R**adiation of the pions as a „background“ and suppress it in the measurement using kinematical cuts.



**I**nitial **S**tate **R**adiation and **F**inal **S**tate **R**adiation contribution have been evaluated with MC (**B**inner, **K**ühn, **M**elnikov, *Phys. Lett. B* 459, 1999):

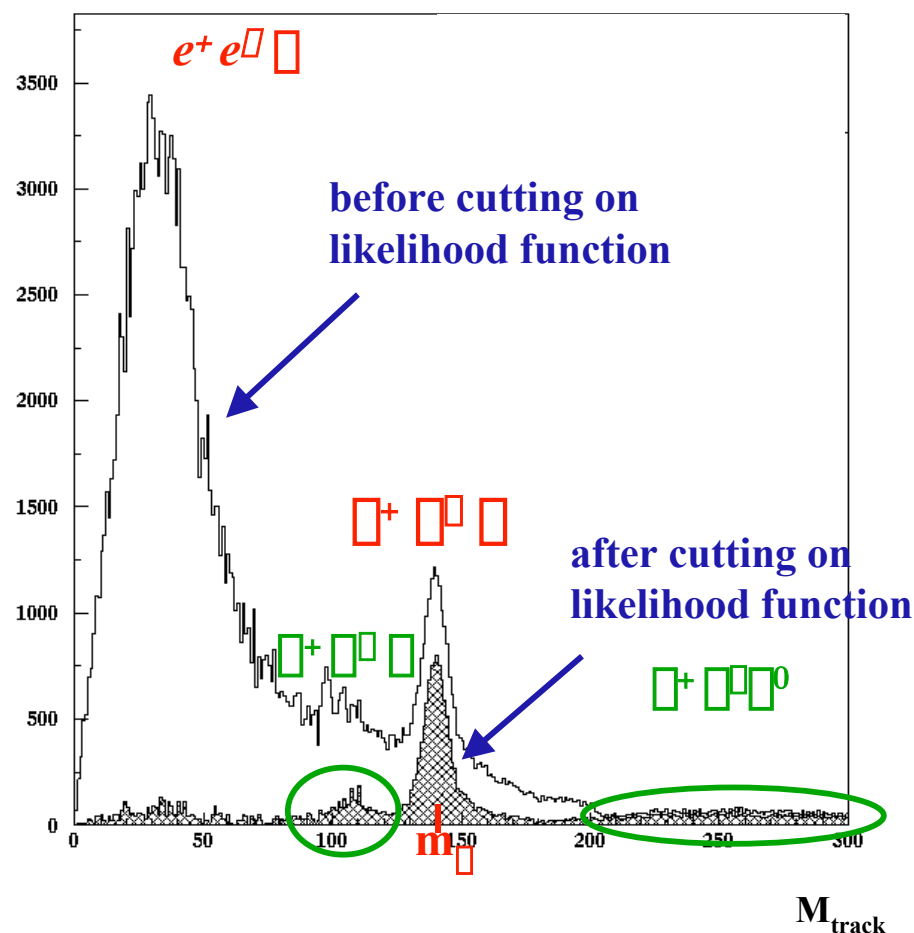
Contribution of **FSR** <1% for our selection cuts (i.e. model dependence negligible)



To reduce Bhabha contamination, a  **$\mu$ -e-separation** is performed using a Likelihood function based on:

- TOF of charged clusters
- Shape and energy deposition of the “charged” cluster

The event is selected if one of the charged tracks is identified to be a pion.



# Background subtraction:

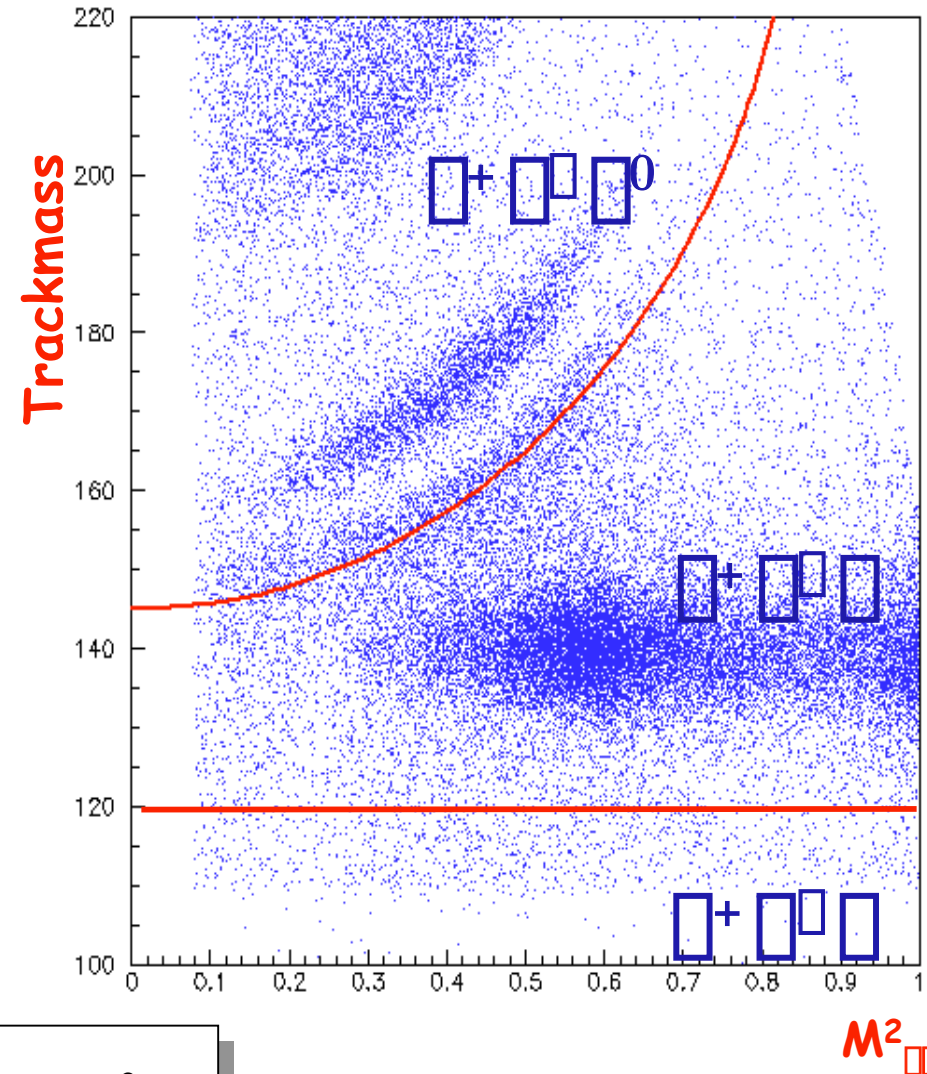


The signal is further selected by performing a cut in the kinetical variable **trackmass** in order to reduce  $\pi^+ \pi^- \pi^0$  **background**

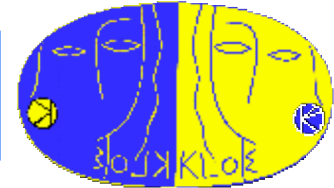
$\pi^+ \pi^- \pi^0$  background  
( $M_{\text{track}} \approx 105 \text{ MeV}$ ) is  
rejected by a cut on  $M_{\text{track}} = 120 \text{ MeV}$

The trackmass is the particle mass for the two tracks obtained by using the 4-momentum-conservation and the assumption that both particles have the same mass  $M_{\text{trk}}$ :

$$q^2 = \left[ M_{\pi}^2 + \sqrt{\vec{p}_1^2 + M_{\text{trk}}^2} \right]^2 - (\vec{p}_1 + \vec{p}_2)^2 = 0$$



# $M_{\pi\pi}^2$ - Spectrum:



In a preliminary attempt to extract the pion form factor, we analyzed **73 pb<sup>-1</sup>** of 2001 data according to the analysis items discussed

after selection: **1 100 000 events**

statistical error/bin < 1%  
for  $M_{\pi\pi}^2 > 0.45 \text{ GeV}^2$

$$\frac{dN_{\pi\pi}}{dM_{\pi\pi}^2} = \frac{N^{\text{obs}} - N^{\text{bkg}}}{M_{\pi\pi}^2} \cdot \frac{1}{\epsilon_{\text{Select.}}} \cdot \frac{1}{L}$$

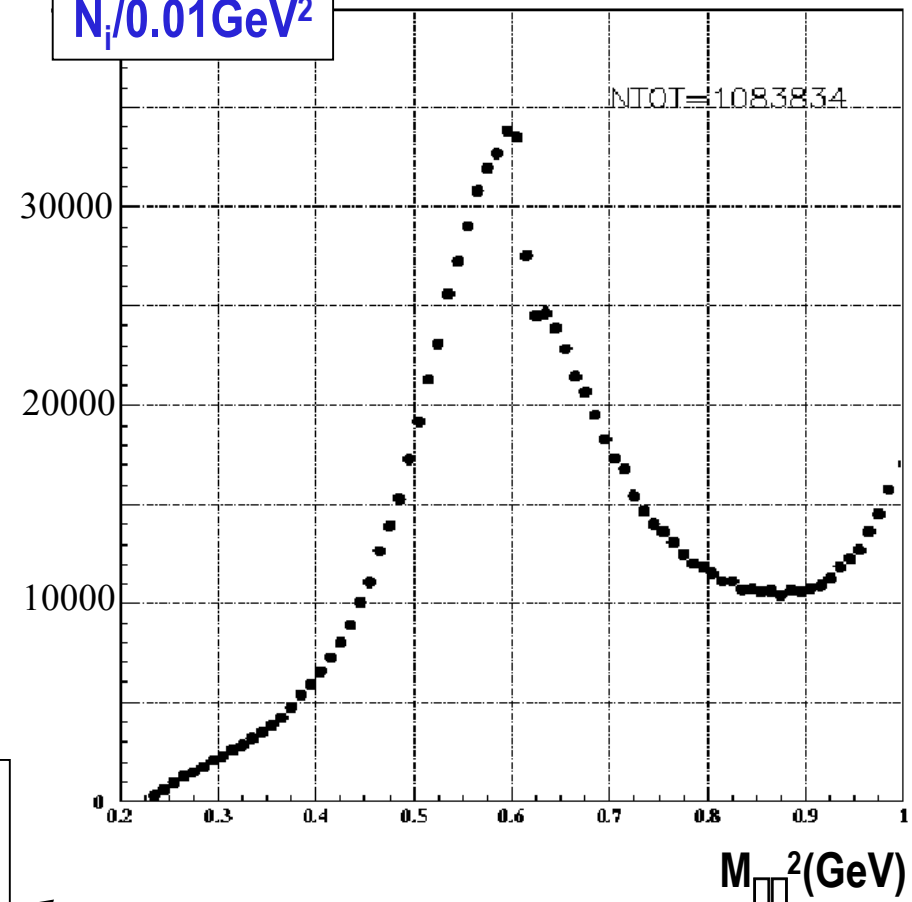
Signal

Background

Selection efficiency

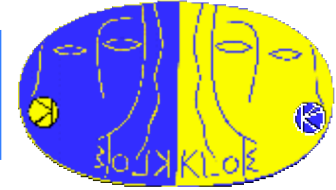
KLOE ππ events after selection -73pb<sup>-1</sup>

$N_i/0.01\text{GeV}^2$



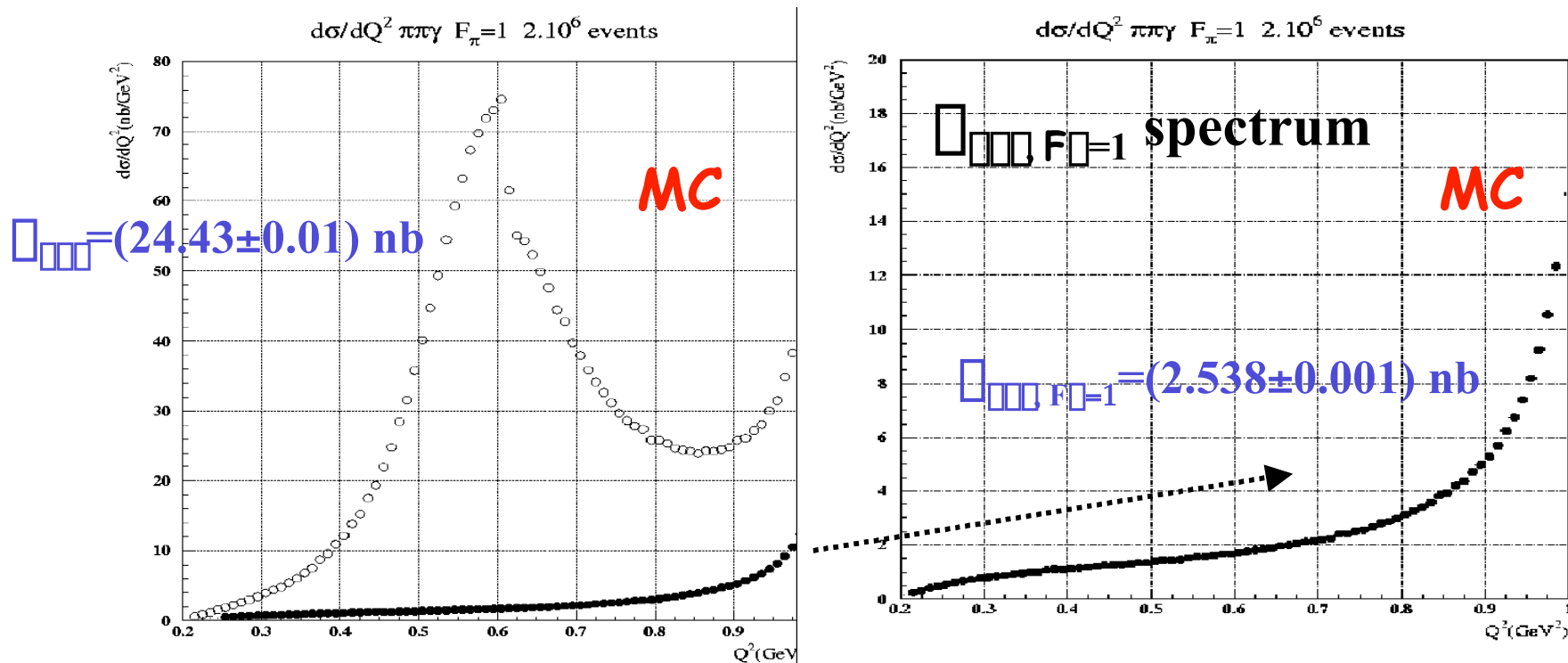
Luminosity

# Extraction of pion form factor:



We divide the  $\pi^+\pi^-\pi^0$  cross section by the cross section  $\pi^+\pi^-\pi^0$  for “pointlike” pions which is obtained from the MC generator by setting  $F_\pi = 1$ .

$$|F_\pi(M_{\pi\pi}^2)|^2 = \frac{d\sigma_{\pi\pi\pi}(M_{\pi\pi}^2)}{d\sigma_{\pi\pi\pi, F_\pi=1}(M_{\pi\pi}^2)}$$



$\sigma_{\pi\pi\pi} F_\pi=1$  was computed with  $2 \cdot 10^6$  events of Monte Carlo with  $F_\pi=1$ ,

with the acceptance cuts of the analysis:  $\eta < 15^\circ$  ( $\eta > 165^\circ$ ),  $40^\circ < \theta < 140^\circ$

# Pion form factor:

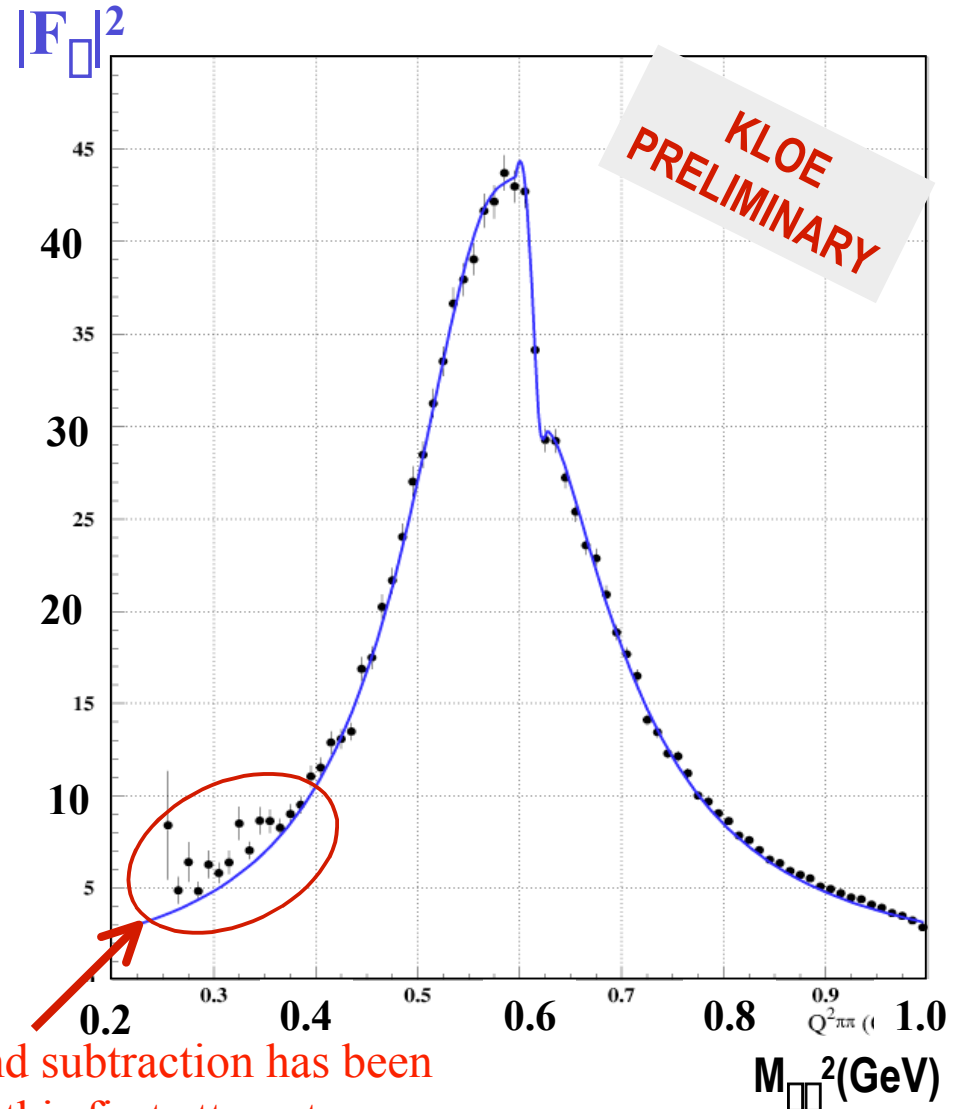


Correcting for efficiencies, normalising to luminosity and dividing the spectrum  $d\Gamma/dM_{\pi\pi}^2$  by the radiation function  $H(M_{\pi\pi}^2)$ , we get a preliminary extraction of the pion form factor.

The next step is to refine the analysis with the full statistics of 2001 (ca. 170 pb<sup>-1</sup>).

Current work is focused on:

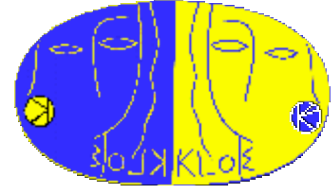
- Efficiency estimation
- Luminosity
- Detector resolution (unfolding)
- Residual background subtraction



No background subtraction has been performed on this first attempt

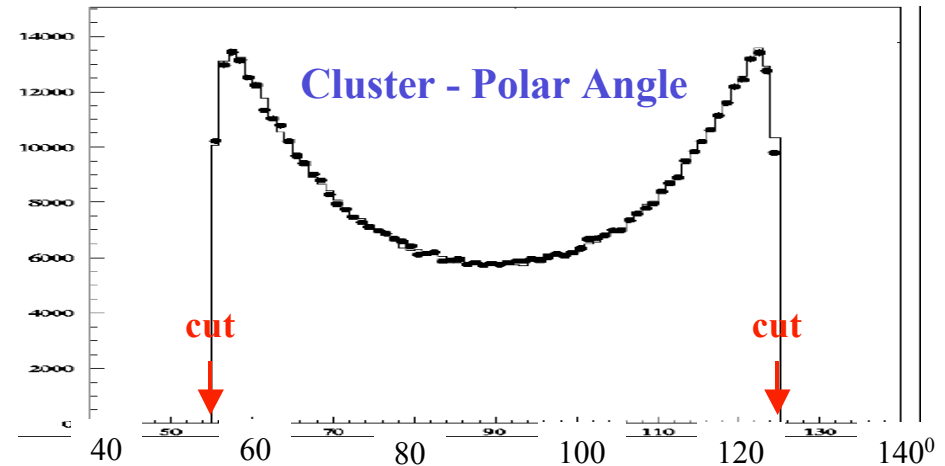


# Luminosity:



KLOE uses “Large Angle Bhabhas”  
( $\sigma_{\text{eff}} = 430 \text{ nb}$ ) to measure the luminosity:

- $55^\circ < \theta_{+-} < 125^\circ$
- $A_{\text{coll.}} < 9^\circ$
- $E_{+-} \geq 400 \text{ MeV}$

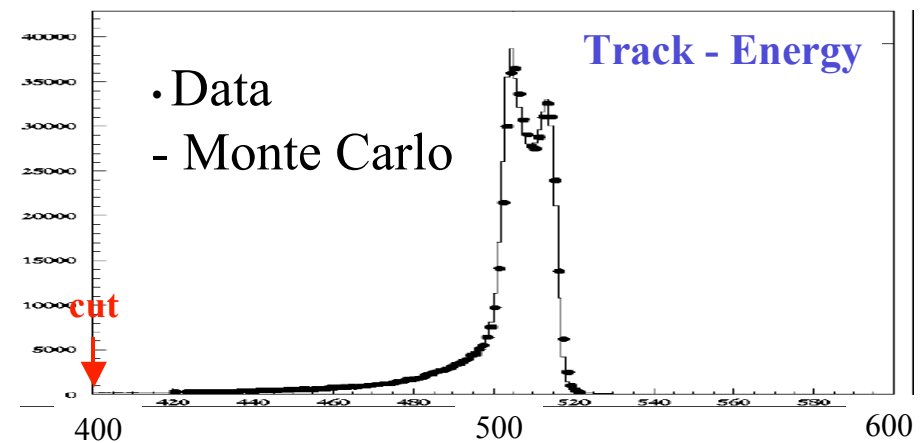


$$\int L dt = \frac{N_{\text{Bhabhas}}(\theta) \cdot (1 - \epsilon_{\text{Background}})}{\sigma^{\text{MC}}(E)}$$

Bhabha - Candidates

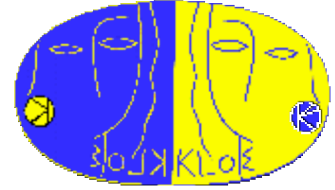
Theoret. Generators  
with rad. corrections

Background  
( $\pi\pi$  ...)



MeV

# Luminosity:



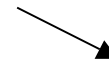
We use **2 independent theoretical generators** to calculate the effective cross section for the actual selection cuts:

- 1) **Berends** (Drago, Venanzoni)
- 2) **BABAYAGA** (Calame, Montagna)\*

**Agreement =  $(0.1 \pm 0.1)\%$**

\* C.M.C. Calame et.al.  
Nucl. Phys., B 584 (2000)

## Systematics



**Difference DATA-MC:**  
Acceptance  
Efficiencies (EmC, DC)

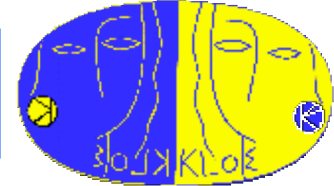
**Running Conditions:**  
Changing  $s$ ,  $p_{\perp}$ , beam position  
Calibration of EmC and Drift  
Chamber

**No limitation for luminosity precision < 1% found**

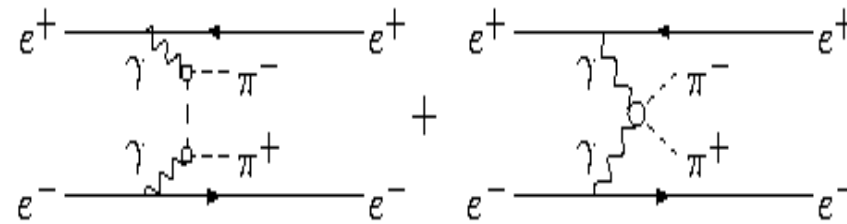


final precision is currently under evaluation

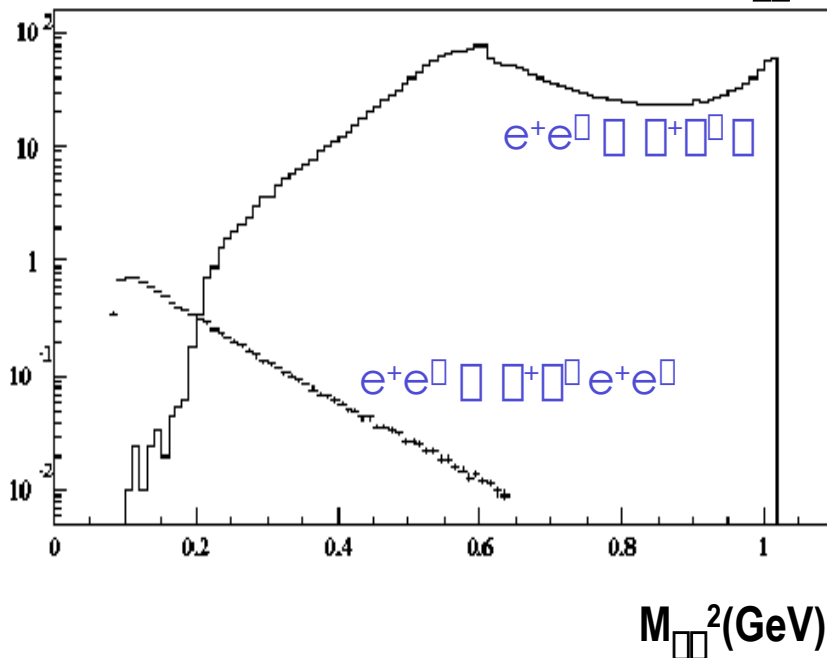
# Background: $e^+e^- \rightarrow e^+e^- \pi^+\pi^-$



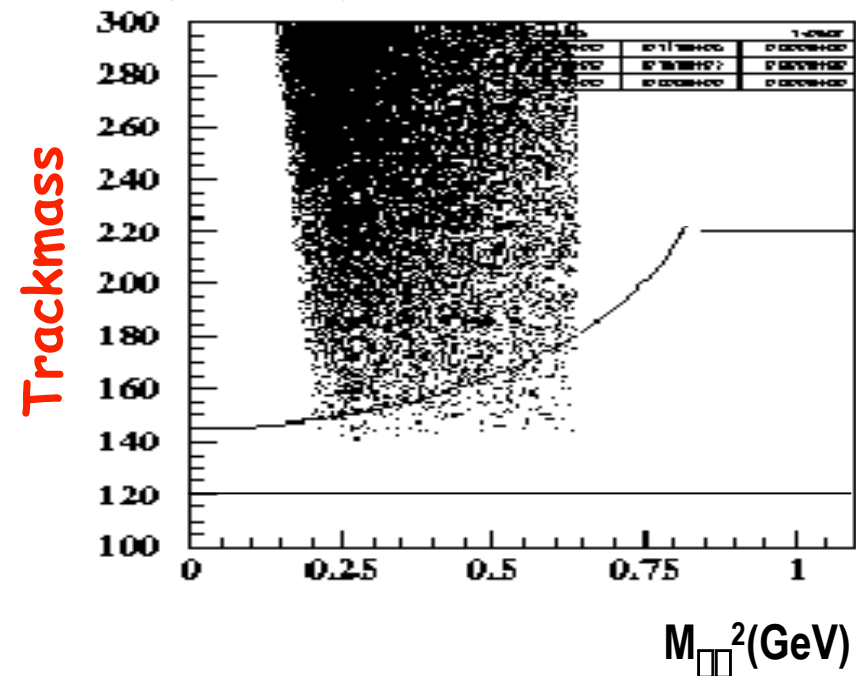
This process could create a background for our analysis if the electron and the positron go along the beampipe and can not be detected.



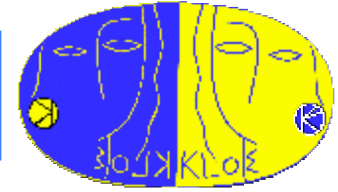
From MC, we expect a background contribution at low values of  $M_{\pi\pi}^2$



The background is completely rejected by the trackmass cut:



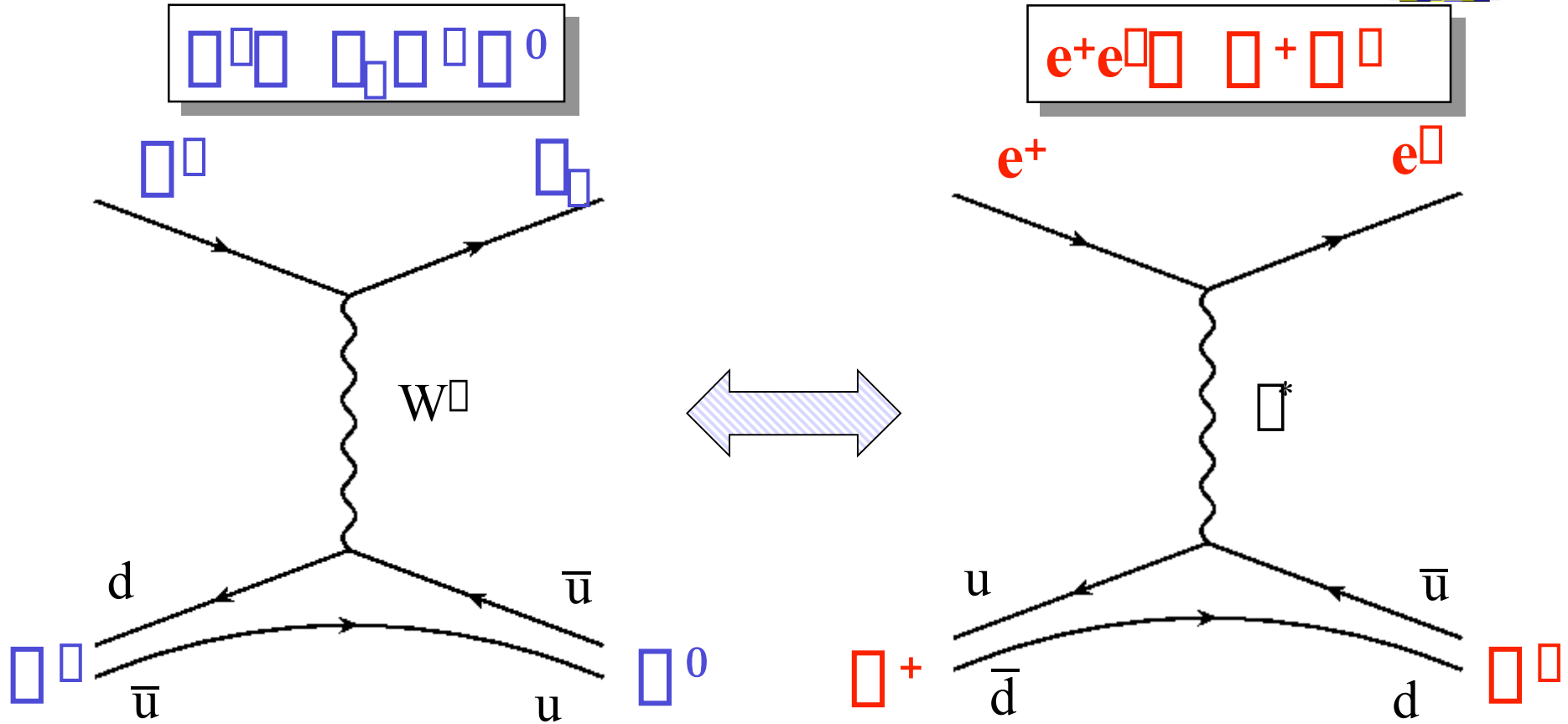
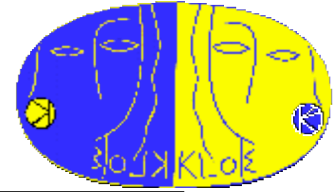
# Conclusions:



- Last year we have performed an „attempt“ on  $73\text{pb}^{-1}$  of data in order to test a method of getting the pion form factor from a measurement utilizing the radiative return
- Already with this reduced data sample, there are no limitations by statistics
- Now we are refining this measurement using the full statistics from 2001 ( $170\text{pb}^{-1}$ ) and evaluating systematics of the measurement (background contaminations, detector resolution etc).

**We are in the final phase towards a publication of our results!**

# $\rho$ decays:

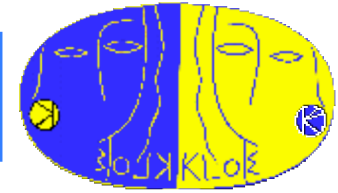


Isospin invariance assumed, one can relate the isovector cross sections  $\sigma(e^+e^- \rightarrow \rho^+ \pi^-)$  to the  $\rho$  spectral function  $V_{\rho\rho^0}$  :

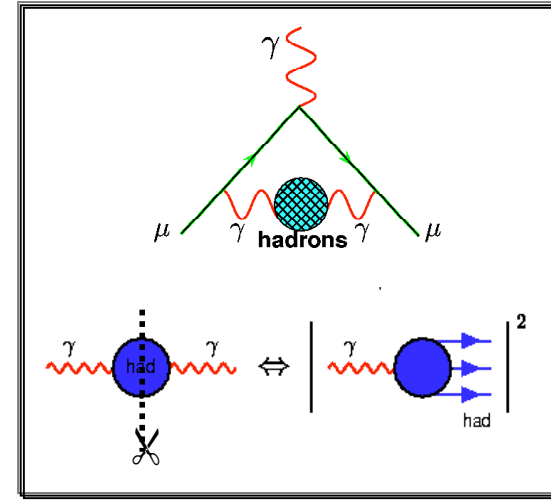
$$\sigma_{e^+e^- \rightarrow \rho^+ \pi^-}^{I=1} = \frac{4\pi^2}{s} V_{\rho\rho^0} \quad , \quad \sqrt{s} \approx M_\rho$$

Isospin symmetry breaking effects have to be taken into account!

# Dispersion integral:



$a_{\Box}^{\text{hadr}}$  can be expressed in terms of  $\Box(e^+e^- \rightarrow \text{hadrons})$  by the use of a **dispersion integral**:

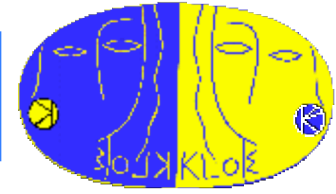


$$a_{\Box}^{\text{hadr}} = \frac{1}{4\Box^3} \int_{4m_{\Box}^2}^{E_{\text{Cut}}^2} ds \Box^{\text{hadr,exp}}(s) K(s) + \int_{E_{\text{Cut}}^2}^{\infty} ds \Box^{\text{hadr,pQCD}}(s) K(s)$$

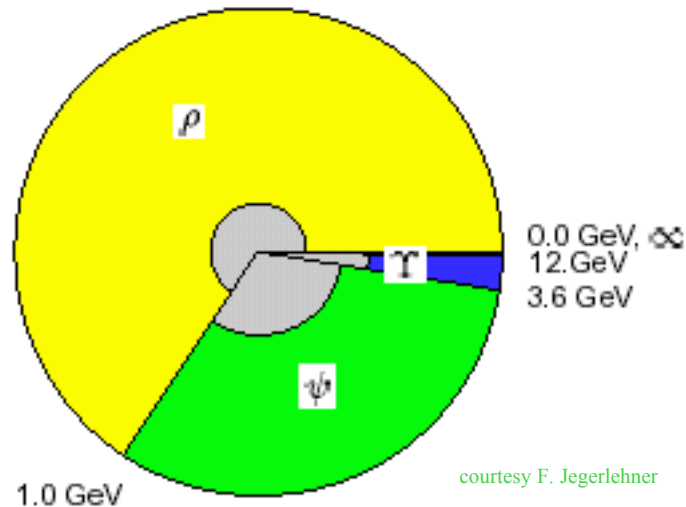
- $E_{\text{cut}}$  is the threshold energy above which pQCD is possible
- $s$  is the c.o.m.-energy squared of the hadronic system
- $K(s)$  is a steady function that goes with  $1/s$ ,  
*enhancing low energy contributions of  $\Box^{\text{hadr}}(s)$*



# Low energy contribution:



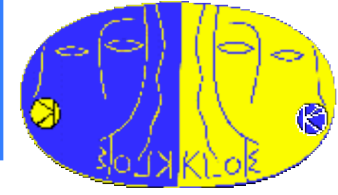
The region around the energy of the  $\rho$ -meson adds with ca. 72% to the total value of  $a_{\mu}^{\text{hadr}}$ . [Jegerlehner; hep-ph/0104304]



The  $\rho$ -meson decays to 100% in  $\pi^+\pi^-$ , so in this energy region the analysis efforts concentrate on the determination of

$$\sigma(e^+e^- \rightarrow \pi^+\pi^-)$$

# Status on $(g-2)_\mu$ :



The current status of  $a_\mu$  from experiment and (SM-) theory:

$a_\mu^{\text{exp}}$

$$(g_\mu - 2)/2 = (11\,659\,203.0 \pm 8.0) \times 10^{-10}$$

E821, hep-ex/0208001

$a_\mu^{\text{theor, SM}}$

$$(g_\mu - 2)/2 = a_\mu^{\text{QED}} + a_\mu^{\text{had}} + a_\mu^{\text{weak}}$$

$$a_\mu^{\text{QED}} = (11\,658\,470.6 \pm 0.3) \times 10^{-10}$$

$$a_\mu^{\text{weak}} = (15.2 \pm 0.1) \times 10^{-10}$$

$$a_\mu^{\text{had}} \left\{ \begin{array}{l} = (707.6 \pm 6.9) \times 10^{-10} \\ = (683.3 \pm 7.8) \times 10^{-10} \end{array} \right.$$

Nucl. Phys. B (Proc. Suppl.) 76, 245

KPPdR hep-ph/0205102

based on  $\pi$  decays

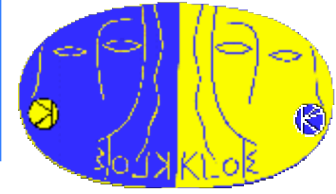
DEHZ hep-ph/0208177 v3

based on  $e^+e^-$  data

$$a_\mu^{\text{exp}} - a_\mu^{\text{theor, SM}} = 0.9 - 3.0 \times \text{difference}$$

- The nature of the difference in the two evaluations of  $a_\mu^{\text{had}}$  is currently not understood
- The reduction of the error on the **hadronic contribution** to the SM calculation of  $a_\mu$  could (together with a further reduction of the experimental error) give this discrepancy between theory and experiment a higher significance

$a_{\pi}^{\text{had}}:$



$$a_{\pi}^{\text{had}} = a_{\pi}^{\text{had}}(\text{lo}) + a_{\pi}^{\text{had}}(\text{nlo}) + a_{\pi}^{\text{had}}(\text{lbl})$$

(see Davier, Eidelmann, Höcker, Zhang hep-ph/0208177)

$$a_{\pi}^{\text{had}}(\text{lo}) \begin{cases} = (709.0 \pm 5.9) \times 10^{-10} \\ = (684.7 \pm 7.0) \times 10^{-10} \end{cases}$$

$\pi$  based  
e+e- based

$$a_{\pi}^{\text{had}}(\text{nlo}) = (-10.0 \pm 0.6) \times 10^{-10}$$

Krause, hep-ph/9607259

$$a_{\pi}^{\text{had}}(\text{lbl}) = (+8.6 \pm 3.5) \times 10^{-10}$$

KN, hep-ph/0111058  
BPP, hep-ph/0112255  
HK, hep-ph/0112102

$$a_{\pi}^{\text{had}} \begin{cases} = (707.6 \pm 6.9) \times 10^{-10} \\ = (683.3 \pm 7.8) \times 10^{-10} \end{cases}$$

$\pi$  based  
e+e- based

$$d\sigma/dM_{\pi\pi}^2:$$



**DATA** compared with the MC

(MC output has been interfaced with the detector simulation program)

Only statistical errors have been taken into account!

