
Kaon physics

XXVI Physics in Collision

Buzios, Brasil

6-9 July 2006

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Plenty of new results on kaon physics since PIC05:

KLOE:

- $\text{BR}(\text{K}_L \rightarrow \pi^+\pi^-)$
- $\text{K}_L e3$ form factors
- $\text{BR}(\text{K}_S \rightarrow \pi e \nu)$ and A_S
- $\Gamma(\text{K}_S \rightarrow \pi^+\pi^-(\gamma))/\Gamma(\text{K}_S \rightarrow \pi^0\pi^0)$
- $\text{BR}(\text{K}^+ \rightarrow \mu^+\nu)$
- K^\pm semileptonic decays
- K^\pm lifetime

NA48:

- CP violation in $\text{K}^\pm \rightarrow 3\pi$
- $\pi\pi$ scattering lengths from $\text{K}^\pm \rightarrow \pi^\pm\pi^0\pi^0$
- $\text{K}_S \rightarrow \pi^+\pi^-\pi^0$
- $\Gamma(\text{K}_{e2}^\pm)/\Gamma(\text{K}_{\mu2}^\pm)$

KTEV:

- $\text{BR}(\text{K}_L \rightarrow \pi^+\pi^-\gamma)$
- Hadronic radiative decays of K_L with virtual photons ($\text{K}_L \rightarrow \pi\pi\gamma^*$ and $\text{K}_L \rightarrow \pi\pi\pi\gamma^*$)

In this talk focus on:

- Direct CP violation in charged decays and **(totally unexpected)** $\pi\pi$ scattering lengths from $\text{K}^\pm \rightarrow \pi^\pm\pi^0\pi^0$ decays
- V_{us} measurement and unitarity test of CKM matrix.
- Determination of CP and CPT violation parameters using the Bell-Steinberger relation.
- μ/e universality in $\text{K}_{\ell 2}^\pm$ decays
- Status of rare K decays ($\text{K} \rightarrow \pi\nu\nu$) measurements.



Direct CP violation in $K^\pm_{3\pi}$ decays

- Compare the Dalitz plot density for K^+ and K^- , in the $K^\pm 3\pi$ decay modes:
 - $\text{BR}(K^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = 5.57\%$ (charged)
 - $\text{BR}(K^\pm \rightarrow \pi^\pm \pi^0 \pi^0) = 1.73\%$. (neutral)
- Matrix element:
 - $|M(u,v)|^2 \sim 1 + gu + hu^2 + kv^2$
 - $g_{\text{ch}} = -0.2154 \pm 0.0035$
 - $g_{\text{n}} = +0.638 \pm 0.020$.
 - $|h|$ and $|k|$ ($\sim 10^{-2}$) negligible wrt g
- The slope asymmetry is the direct CP-violation quantity: $A_g = (g_+ - g_-)/(g_+ + g_-) \neq 0$
- SM estimates vary within an order of magnitude (few $10^{-6} \dots 8 \times 10^{-5}$). Models beyond SM predict substantial enhancement.
- Data-taking 2003:
 - 1.61×10^9 events selected.

Lorentz-invariants:

$$s_i = (P_K - P_{\pi_i})^2, \quad i=1,2,3 \quad (3=\text{odd } \pi);$$

$$s_0 = (s_1 + s_2 + s_3)/3;$$

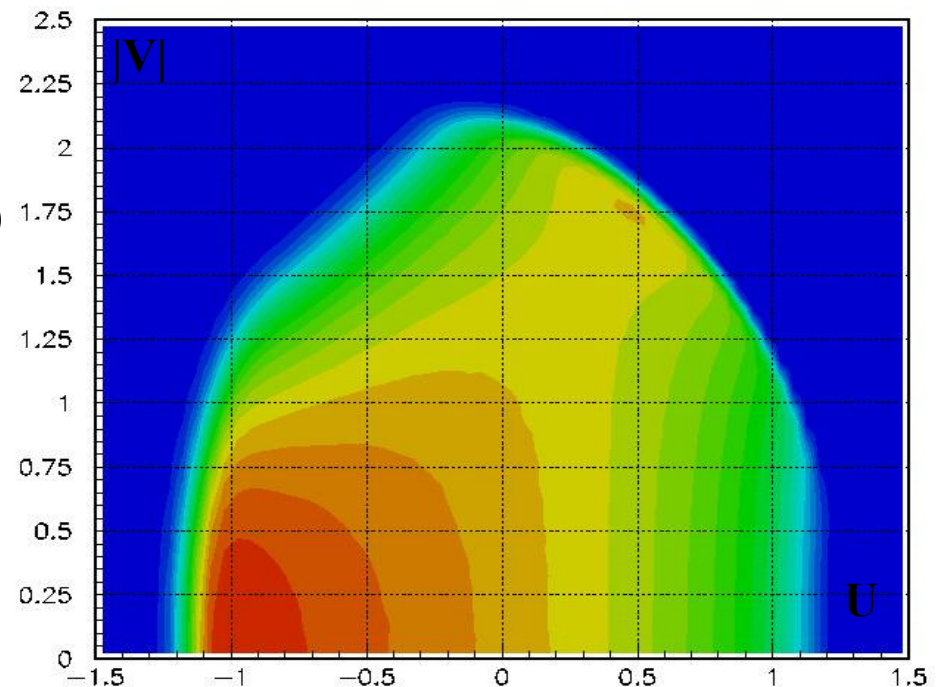
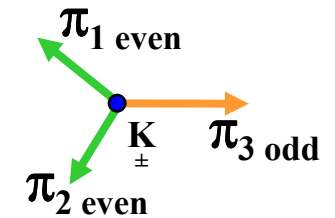
$$u = (s_3 - s_0)/m_\pi^2;$$

$$v = (s_2 - s_1)/m_\pi^2.$$

Kaon rest frame:

$$u = 2m_K \cdot (m_K/3 - E_{\text{odd}})/m_\pi^2;$$

$$v = 2m_K \cdot (E_1 - E_2)/m_\pi^2.$$



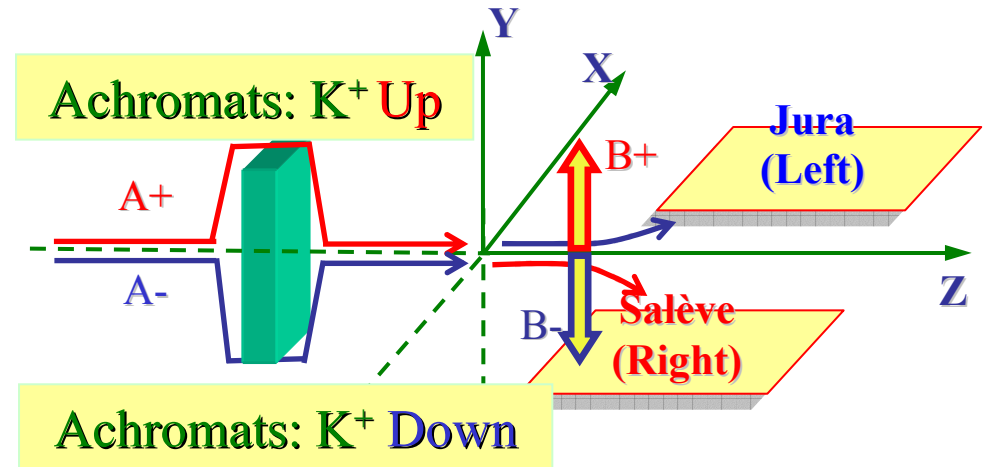


Direct CP violation in $K^{\pm}_3\pi$ decays

- Careful control of detector (Δg_{LR}) and of beamline (Δg_{UD}) asymmetries.

$BR(K^{\pm} \rightarrow \pi^{\pm} \pi^+ \pi^-)$

- Slope difference:
 $\Delta g = (-0.7 \pm 1.0) \times 10^{-4}$
- Charge asymmetry:
 $A_g = (1.7 \pm 2.9) \times 10^{-4}$

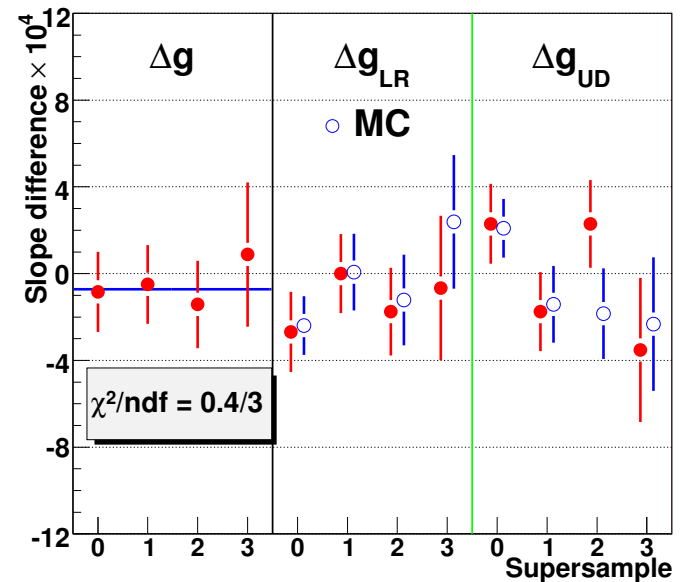


$BR(K^{\pm} \rightarrow \pi^{\pm} \pi^0 \pi^0)$: small BR and acceptance, larger slope.

- Slope difference:
 $\Delta g = (2.2 \pm 3.1) \times 10^{-4}$
- Charge asymmetry (using $g_0=0.638$):
 $A_g^0 = (1.8 \pm 2.6) \times 10^{-4}$

- Errors dominated by statistics
- Order of magnitude improvement

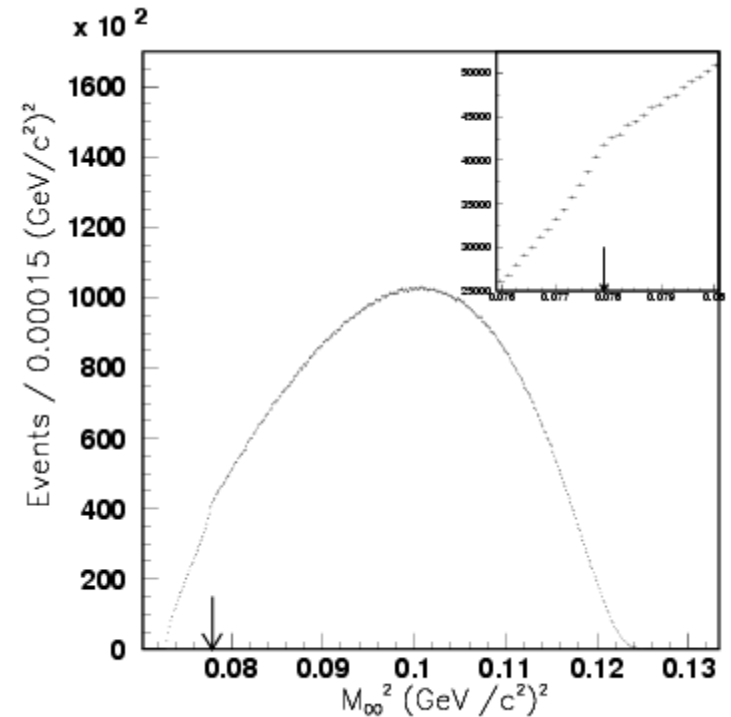
hep-ex/0602014; PLB 634 (2006)



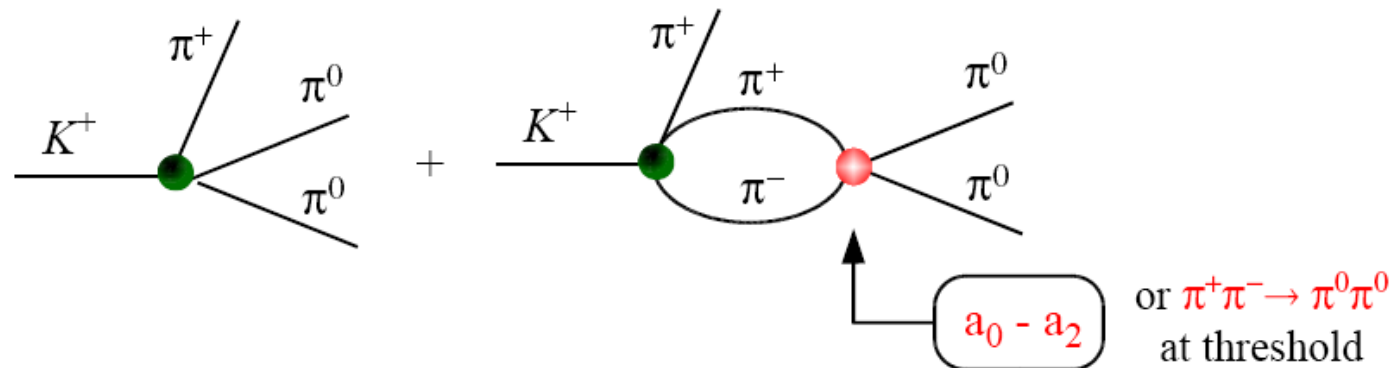


Cusp-like effect in $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ decays

The high resolution of the NA48/2 experiment has allowed to observe –for the first time– a subtle and interesting phenomenon in $K^\pm \rightarrow 3\pi$ decays: anomaly in the $\pi^0\pi^0$ (M_{00}^2) invariant mass distribution in the region $M_{00} = 2m_{\pi^\pm}$.



The origin of this discontinuity is due to the following interference/re-scattering effect:

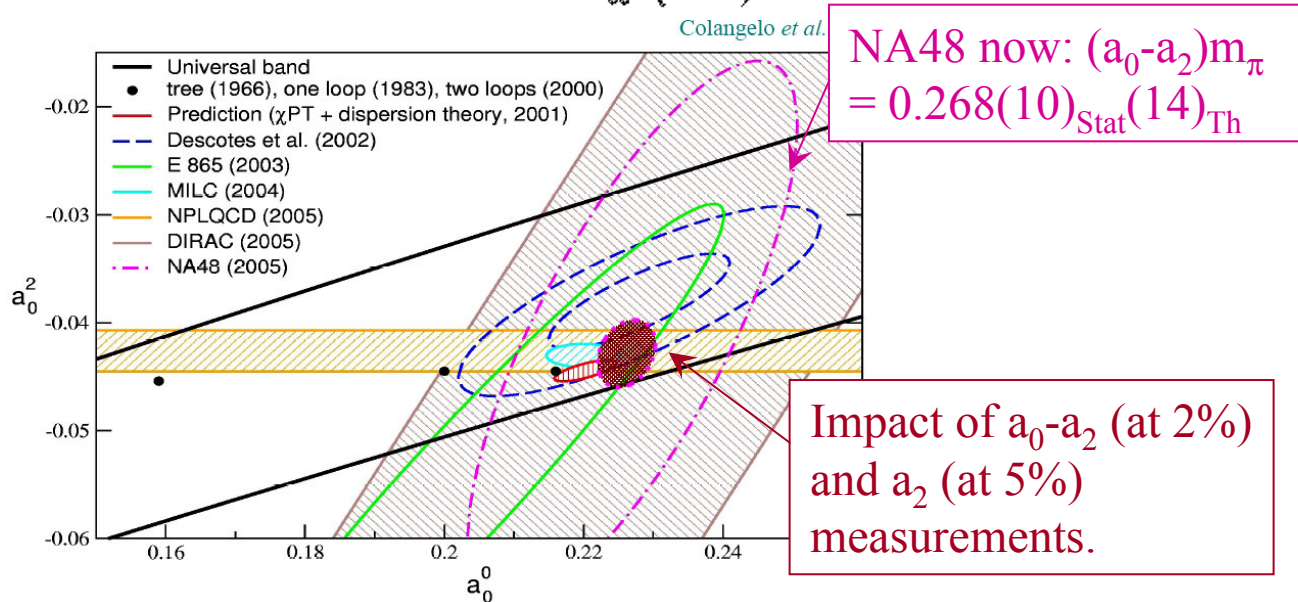
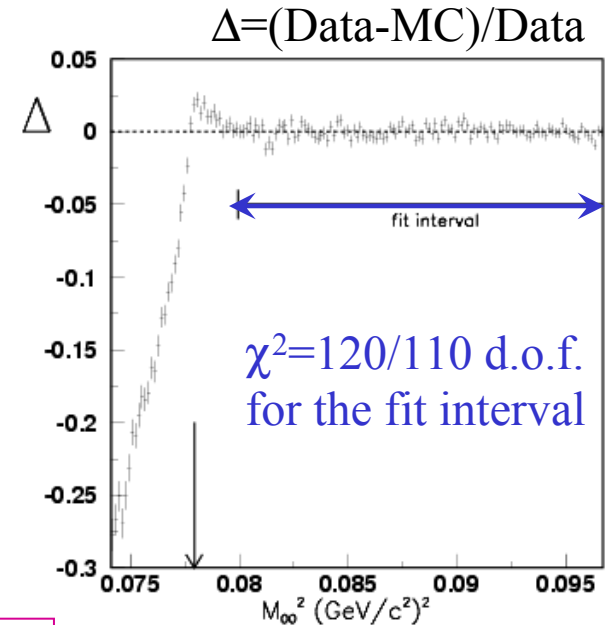
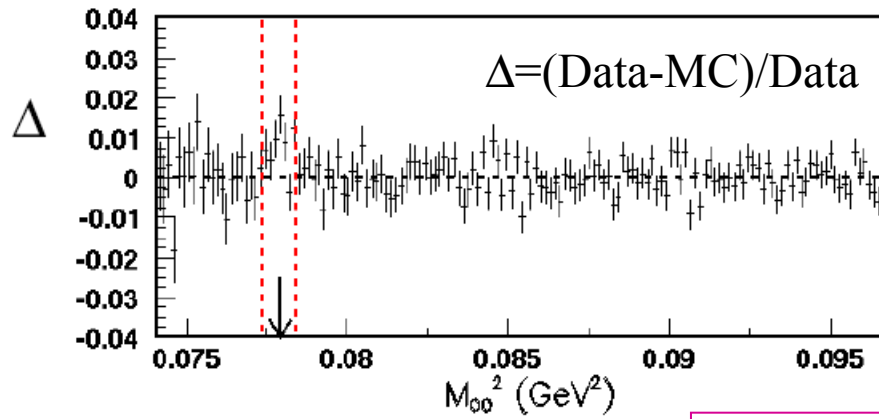


From this effect a new way to measure $a_0 - a_2$, important parameters of the χ_{PT} .



Cusp-like effect in $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ decays

- Without the re-scattering effect: $\chi^2=13\,574/148$ d.o.f
- With re-scattering plus pionium: $\chi^2=141/139$ d.o.f



In a few years this method could provide the most precise determination of S-wave $\pi\pi$ scattering lengths (better than from $K_{\ell 4}$ decays).

Unitarity test of CKM matrix – V_{us}

- Universality of weak interactions + 3 generations:

$$V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

- Most precise **test of unitarity** possible at present comes from 1st row:

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \sim |V_{ud}|^2 + |V_{us}|^2 \equiv 1 - \Delta$$

Can test if $\Delta = 0$ at 10^{-3} level:

from super-allowed nuclear β -decays: $2|V_{ud}|\delta V_{ud} = 0.0005$

from semileptonic kaon decays: $2|V_{us}|\delta V_{us} = 0.0009$

- **Extract $|V_{us}|$ from K_{l3} decays (e.m. effects must be included):**

$$\Gamma(K \rightarrow \pi \ell \nu(\gamma)) \propto |V_{us} f_+^{K0\pi-}(0)|^2 I(\lambda_t) S_{EW}(1 + \delta_{EM} + \delta_{SU(2)})$$

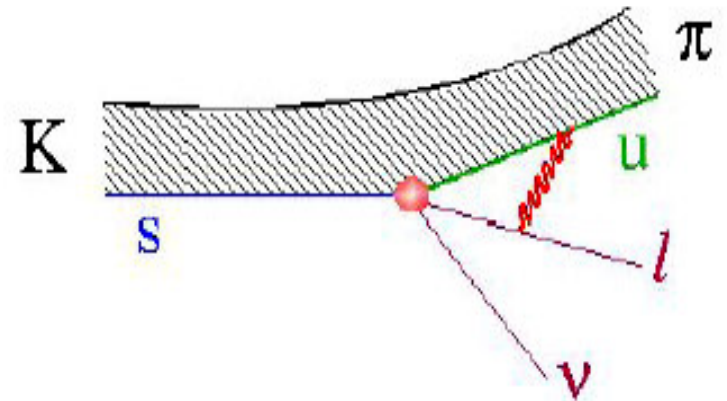
Relative uncertainty:
$$\frac{\delta|V_{us}|}{|V_{us}|} = 0.5 \frac{\delta\Gamma}{\Gamma} \oplus 0.5 \frac{\delta I(\lambda_t)}{I(\lambda_t)} \oplus \frac{\delta f_+^{K0\pi-}(0)}{f_+^{K0\pi-}(0)}$$

Details on the V_{us} extraction

$$\Gamma_{K\ell 3} = \frac{G_F^2 M_K^5}{192\pi^3} S_{EW} (1 + \delta_K^\ell) C^2 |V_{us}|^2 f_+^2(0) I_K^\ell$$

Theoretical inputs

- $f_+(0)$ form factor at zero momentum transfer: pure theory calculation (χ_{PT} , lattice) presently known at 1% level.
- S_{EW} short distance corrections (1.0232)
- $C = 1$ ($2^{-1/2}$) for neutral (charged) kaon decays
- δ_K^ℓ electromagnetic and isospin breaking (K^\pm only) effects presently known at the 0.1% level.



Experimental inputs

- $I_K^\ell = I(\lambda_+, \lambda_0, 0)$ phase space integral; depends on the decay mode $K^{\pm,0}(e3)$, $K^{\pm,0}(\mu3)$
- λ_+, λ_0 slopes (momentum dependence of the vector and scalar form factors)
- $\Gamma_{K\ell 3}$ (BR and lifetime)
- **Measure all inputs: branching ratios, lifetimes, and form factors.**

Experimental inputs for V_{us} : 2003-2006



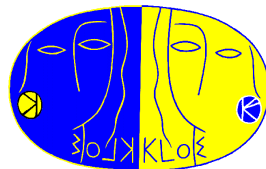
$\text{BR}(K^\pm \rightarrow \pi^0 e \nu)$



K_L dominant BR's
 K_L semileptonic form factor slopes



$\text{BR}(K_L \rightarrow \pi e \nu)$
 K_L semileptonic form factor slopes
 $\text{BR}(K^\pm \rightarrow \pi^0 e^\pm \nu)$

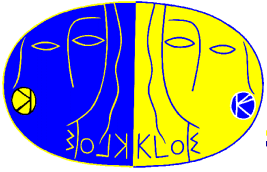


$\text{BR}(K_S \rightarrow \pi e \nu)$
 K_L dominant BR's
 K_L lifetime
 $K_L e3$ form factor slopes

K^\pm semileptonic BR's
 $\text{BR}(K^+ \rightarrow \mu^+ \nu(\gamma))$
 K^\pm lifetime



$\text{BR}(K^- \rightarrow \pi^0 e \nu)$
 K^- semileptonic form factor slopes



K physics at KLOE - tagging

Kaon physics at a ϕ -factory has some peculiar characteristics:

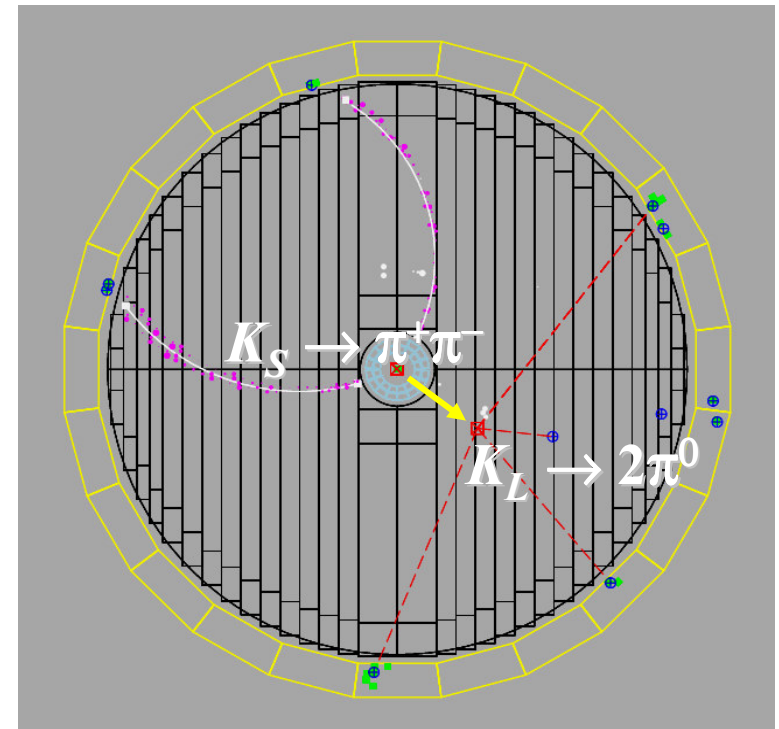
- $K_S K_L$ ($K^+ K^-$) produced from ϕ are in a pure $J^{PC} = 1^{--}$ state:

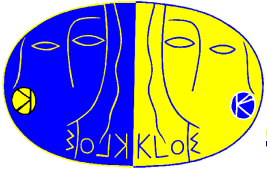
$$K_S, K^+ \longleftarrow \phi \longrightarrow K_L, K^-$$

$$\frac{1}{\sqrt{2}} (|K_L, \mathbf{p}\rangle |K_S, -\mathbf{p}\rangle - |K_L, -\mathbf{p}\rangle |K_S, \mathbf{p}\rangle)$$

- Allows interference measurements of $K_S K_L$ system
- Observation of $K_{S,L}$ signals presence of $K_{L,S}$; $K^{+,-}$ signals $K^{-,+}$
- Allow **absolute** branching ratio measurement, by means of a tag technique.
- Pure K_S beam
- $K_{S,L}$ momentum measured from tag kaon ($K_{L,S}$):
 $K_{S,L}$ angular resolution: $\sim 1^\circ$; $K_{S,L}$ momentum resolution: ~ 1 MeV
- Kaon momentum ($p_L \sim 110$ MeV, $p_\perp \sim 127$ MeV) is an excellent lever arm for lifetime measurements (acceptance about 0.5λ).

ϕ decay mode	BR
$K^+ K^-$	49.1%
$K_S K_L$	34.1%





K^\pm lifetime

- τ_\pm PDG entries: discrepancies between in-flight and at-rest measurements; discrepancies between different stoppers in at-rest measurements.

Tag events with $K^\pm \rightarrow \mu^\pm \nu$ decay

Identify a kaon decay vertex on the opposite side

- **1st method: obtain τ_\pm from the K decay length**

Measure the kaon decay length taking into account the energy loss: $\tau_K = \sum_i \Delta L_i / (\beta_i \gamma_i c)$

$$\tau_\pm = 12.367 \pm 0.044_{\text{stat}} \pm 0.065_{\text{syst}} \text{ ns}$$

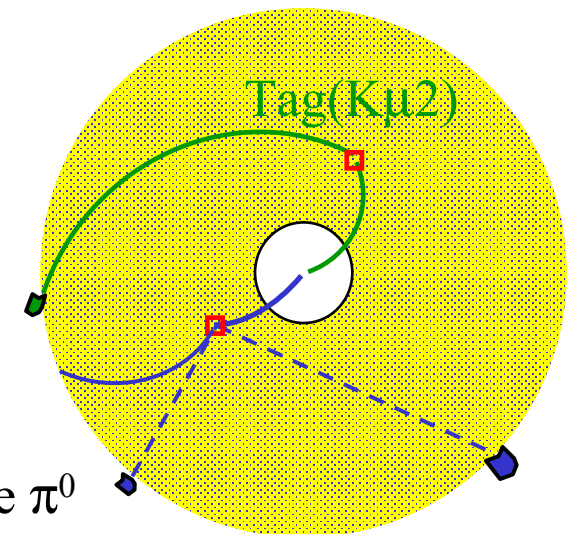
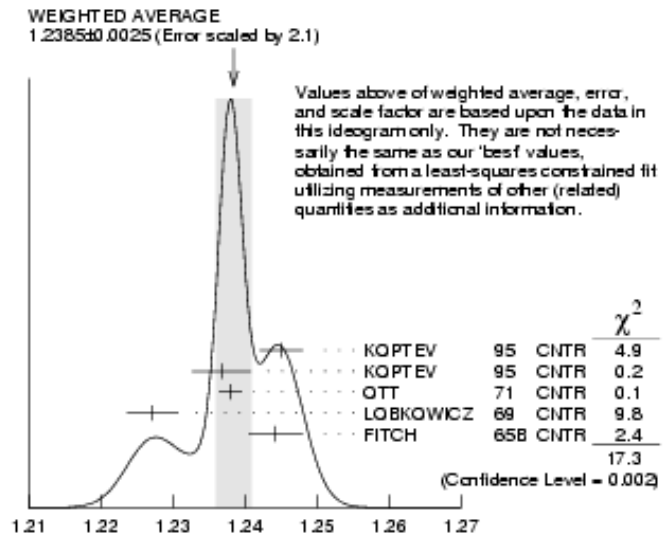
(preliminary)

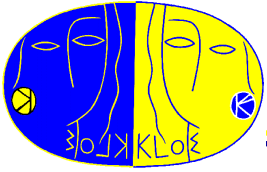
- **2nd method: obtain τ_\pm from the K decay time**

Use only $K^\pm \rightarrow \pi^\pm \pi^0$ decays

Measure the kaon decay time: $\tau_K = (t_\gamma - R_\gamma/c) / \gamma_K$, using the π^0 (in progress).

Comparison of the two methods allows to keep systematics under control





Dominant K_L BR's and K_L lifetime

- Using also the constraint $\sum \text{BR}(K_L) = 1$:

$$\begin{aligned} \text{BR}(K_L \rightarrow \pi e \nu(\gamma)) &= 0.4007 \pm 0.0006_{\text{stat}} \pm 0.0014_{\text{syst}} \\ \text{BR}(K_L \rightarrow \pi \mu \nu(\gamma)) &= 0.2698 \pm 0.0006_{\text{stat}} \pm 0.0014_{\text{syst}} \\ \text{BR}(K_L \rightarrow 3\pi^0) &= 0.1997 \pm 0.0005_{\text{stat}} \pm 0.0019_{\text{syst}} \\ \text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0(\gamma)) &= 0.1263 \pm 0.0005_{\text{stat}} \pm 0.0011_{\text{syst}} \end{aligned}$$

$$\tau_L = 50.72 \pm 0.17 \pm 0.33 \text{ ns}$$

- Direct measurement of K_L lifetime using $K_L \rightarrow \pi^0 \pi^0 \pi^0$ decays:

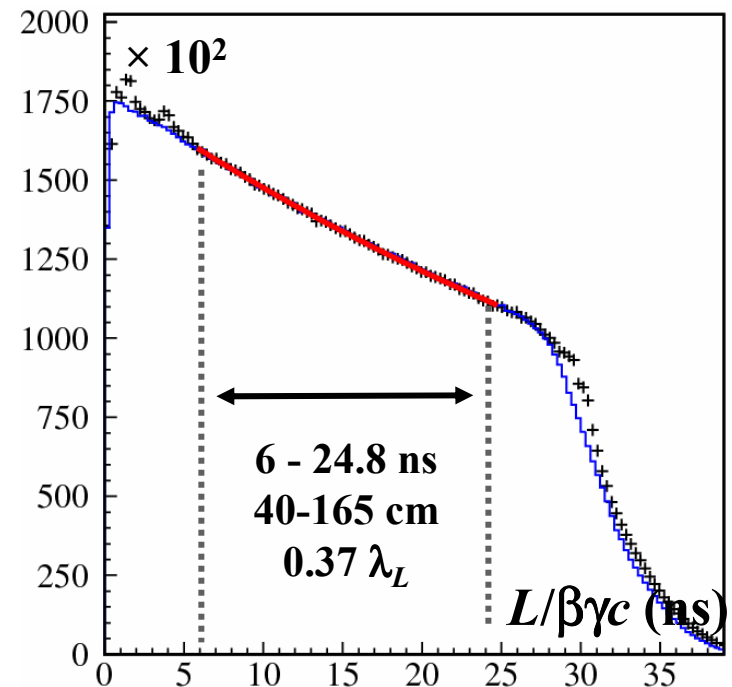
$$\tau_L = 50.92 \pm 0.17 \pm 0.25 \text{ ns}$$

- Average of KLOE results:

$$\tau_L = 50.84 \pm 0.23 \text{ ns}$$

- cf. Vosburg'72: $\tau_L = 51.54 \pm 0.44 \text{ ns}$, a factor $\times 2$ better

Published
PLB608(2005)199
PLB626(2005)15



K_L semileptonic branching ratios



- KTeV measured 5 K_L decay ratios of 6 decay modes which account for 99.93% of K_L decays
- The ratios can be combined to extract BRs of the 6 main K_L decay modes. (PRD 70 (2004))



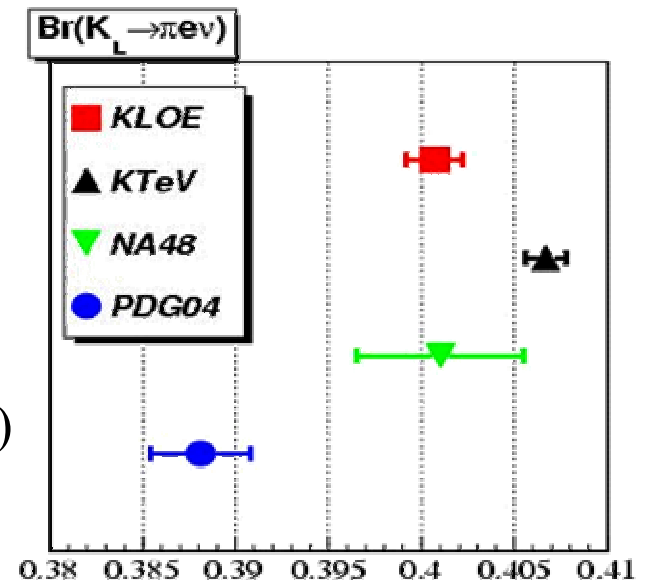
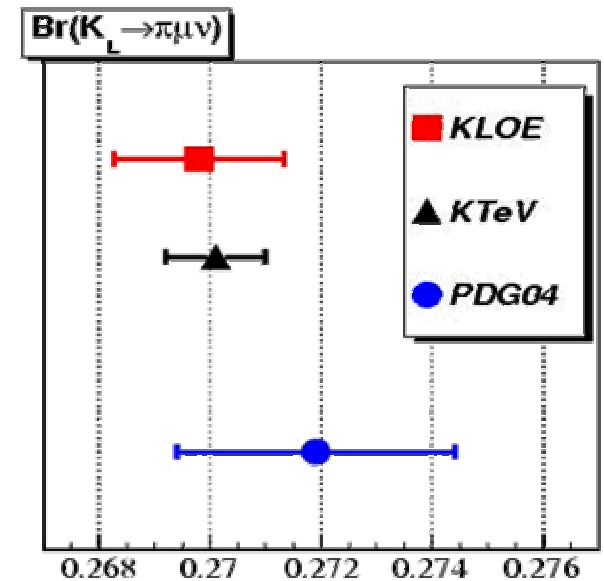
- Preliminary result (HEP2005) with 6×10^6 K_{e3} events.
- Measure ratio of BRs:

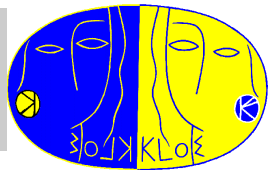
$$\text{BR}(K_L \rightarrow \pi e \nu) / \text{BR}(2 \text{ track}) = 0.4978 \pm 0.0035$$

$$\text{BR}(2 \text{ track}) \approx 1 - \text{BR}(K_L \rightarrow 3\pi^0)$$

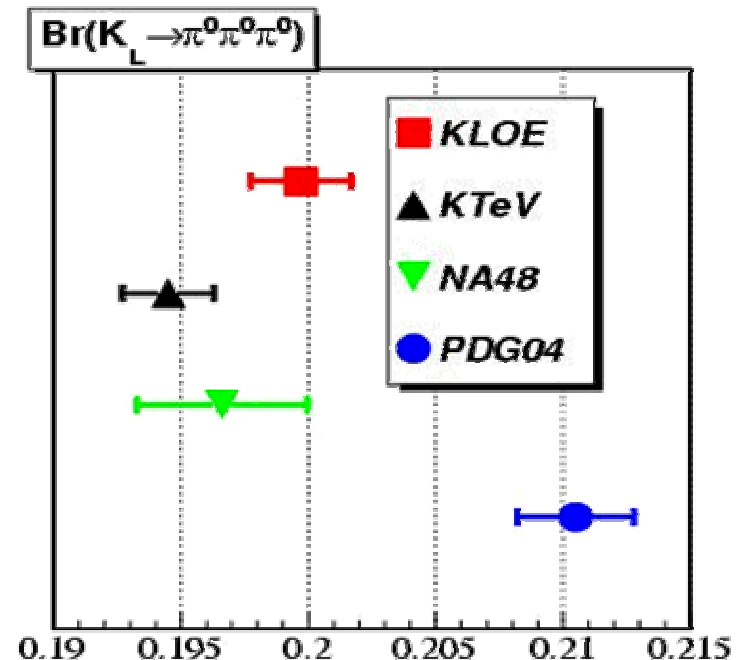
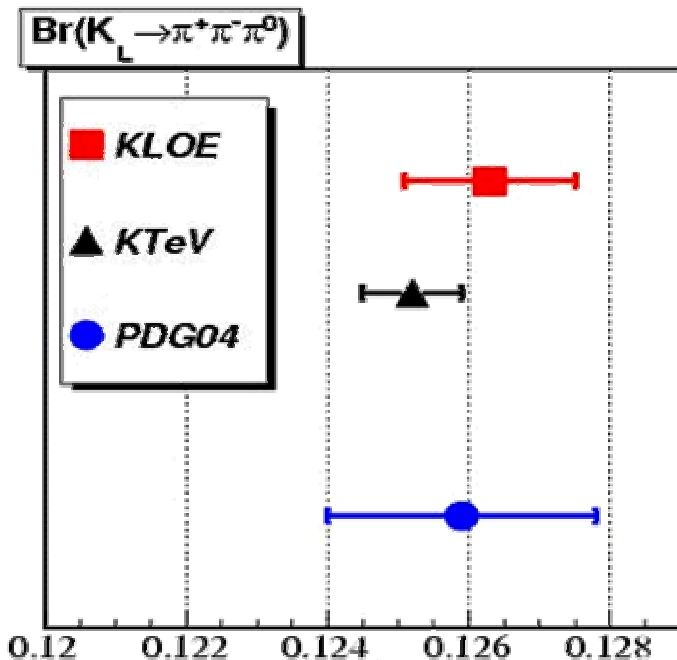
Using PDG-KTeV average for $\text{BR}(K_L 3\pi^0) = 0.1992(70)$

$$\text{BR}(K_L \rightarrow \pi e \nu) = \mathbf{0.4010 \pm 0.0028_{\text{exp}} \pm 0.0035_{\text{norm}}}$$





$K_L \rightarrow \pi\pi\pi$ branching ratios

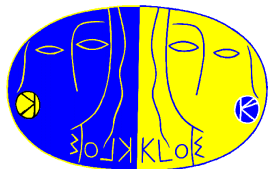


NA48 preliminary measurement of $\text{BR}(K_L \rightarrow 3\pi^0)$

Extracted from $\text{BR}(K_L \rightarrow 3\pi^0)/\text{BR}(K_S \rightarrow 2\pi^0)$

$\text{BR}(K_L \rightarrow 3\pi^0) = 0.1966 \pm 0.0006 \pm 0.0033$ (PDG value for $\text{BR}(K_S \rightarrow 2\pi^0)$)

$BR(K^\pm \rightarrow \pi^0 \ell^\pm \nu)$ preliminary results



KLOE preliminary:

- **Absolute** BR measurement of both $K^\pm \rightarrow \pi^0 e^\pm \nu$ and $K^\pm \rightarrow \pi^0 \mu^\pm \nu$ decay modes.
- $BR(K^\pm \rightarrow \pi^0 e^\pm \nu) = (5.047 \pm 0.019_{\text{stat}} \pm 0.039_{\text{syst}})\%$
- $BR(K^\pm \rightarrow \pi^0 \mu^\pm \nu) = (3.310 \pm 0.016_{\text{stat}} \pm 0.045_{\text{syst}})\%$

PDG (pre E865)
(4.87 ± 0.06)%
E865(2003)
(5.13 ± 0.10)%



NA48 preliminary:

- Measurement of $BR(K^\pm \rightarrow \pi^0 e \nu) / BR(K^\pm \rightarrow \pi^\pm \pi^0)$
- $BR(K^\pm \rightarrow \pi^0 e \nu) = (5.14 \pm 0.02_{\text{stat}} \pm 0.06_{\text{syst}})\%$



ISTRA+ preliminary:

- Measurement of $BR(K^- \rightarrow \pi^0 e^- \nu) / BR(K^- \rightarrow \pi^- \pi^0)$
- $BR(K^- \rightarrow \pi^0 e \nu) = (5.22 \pm 0.11)\%$

Note: **NA48/2** and **ISTRA+** values depend on $BR(K^\pm \rightarrow \pi^\pm \pi^0)$. Post-PDG'04 results for Ke3 (**E865**) and $K\mu 2$ (**KLOE**) decrease $BR(K^\pm \rightarrow \pi^\pm \pi^0)$ by $\sim 1\%$ from global fit to K^\pm BRs

$K_{\ell 3}$ form factor slopes

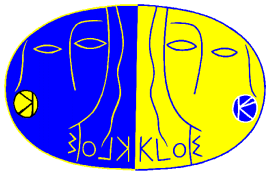
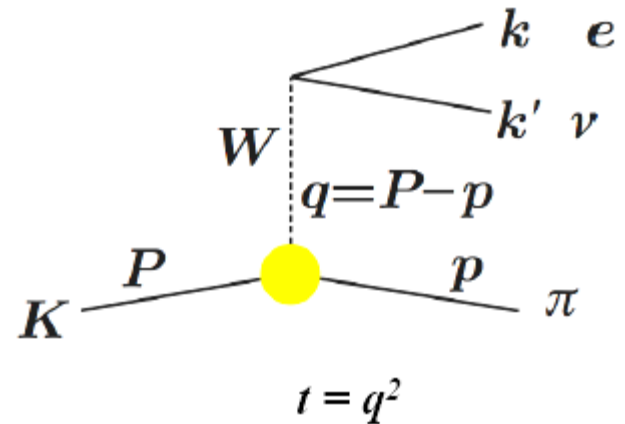
In the extraction of V_{us} : needed for evaluation of phase-space integrals I_K^{ℓ}
 Fit of momentum transfer spectrum with different hypothesis on form factor $f_+(t)/f_+(0)$:

Linear: $1 + \lambda'_+ t$

Quadratic: $1 + \lambda'_+ t/m_{\pi^+}^2 + 1/2 \lambda''_+ (t/m_{\pi^+}^2)^2$

Pole model: $M_V^2/(M_V^2-t)$,

Taylor exp. with $\lambda'_+ = (m_{\pi}/M_V)^2$, $\lambda''_+ = 2 \lambda'_+{}^2$



KLOE Published PLB 636 (2006) 166

- **328 pb⁻¹, 2 × 10⁶ Ke3 decays**
- Momentum transfer **t measured** from π and K_L momenta: $\sigma_t/m_{\pi}^2 \sim 0.3$.
- Separate measurement for each charge state ($e^-\pi^+, e^+\pi^-$) to check systematics.

Quadratic:

$$\lambda'_+ = (25.5 \pm 1.5 \pm 1.0) \times 10^{-3}$$

$$\lambda''_+ = (1.4 \pm 0.7 \pm 0.4) \times 10^{-3}$$

$$\rho(\lambda'_+, \lambda''_+) = -0.95$$

Pole model:

$$m_V = (870 \pm 7) \text{ MeV}$$

$K_{\ell 3}$ form factor slopes



KTeV (PRD 70 (2004))

Measured in K^0_{e3} and $K^0_{\mu 3}$ decays.

Uses quadratic parameterization

Slopes consistent for the two decay modes

$$\lambda_0 = (13.72 \pm 1.31) \times 10^{-3}$$



NA48 preliminary (HEP2005) 289

K^0_{e3} and $K^0_{\mu 3}$ Linear fit

no evidence for quadratic term

$$\lambda_0 = (12.0 \pm 1.7) \times 10^{-3}$$

compatible with KTeV

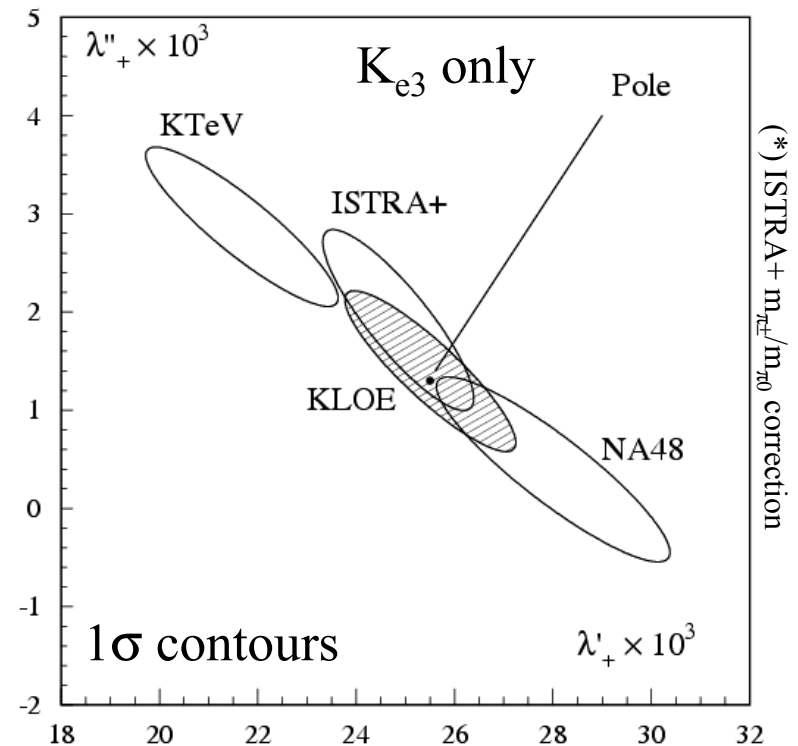


ISTRA+ (PLB 581 (2004), PLB 589 (2004))

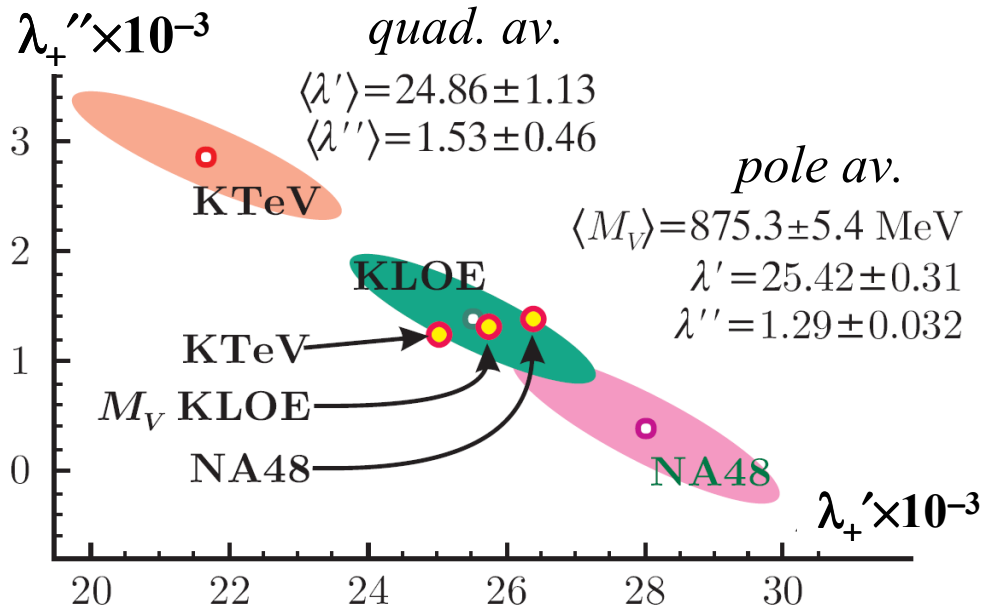
K^{\pm}_{e3} quadratic fit

2σ significance for the non linear term

$$K^{\pm}_{\mu 3} \text{ quadratic fit } \lambda_0 = (17.11 \pm 2.31) \times 10^{-3}$$



K_{Le3} form factor slopes

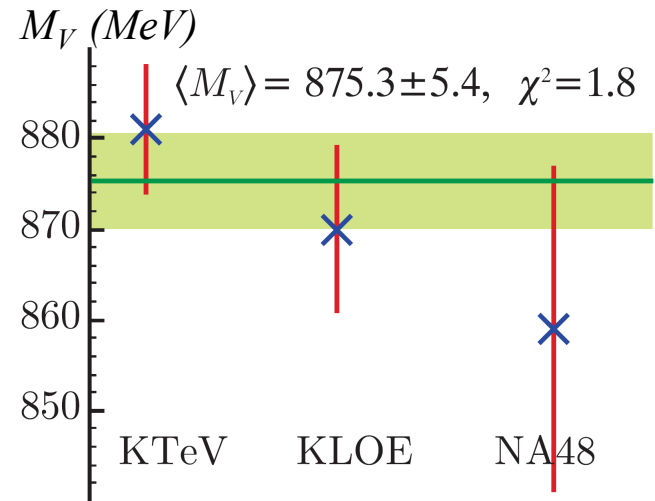


Good agreement between experiments, if correlation between λ' and λ'' is taken into account:

- quad $\chi^2/\text{dof} = 4.4/4$
- pole $\chi^2/\text{dof} = 1.8/2$

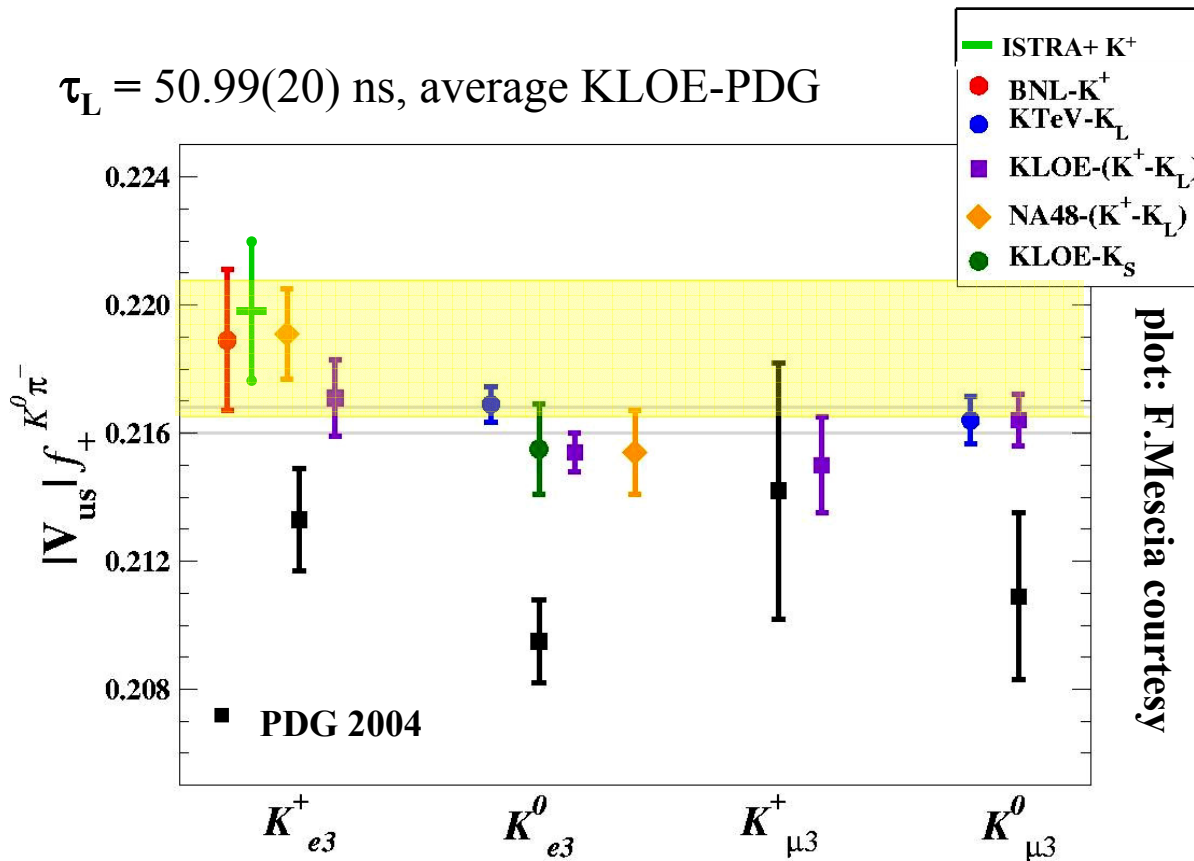
• Phase space integral $I(\lambda)$ depends on the parameterization:

	$(I_{\text{Pole}} - I_{\text{Quad}}) / I_{\text{Quad}}$
KLOE	0.5×10^{-3}
KTeV	6.0×10^{-3}
World av.	0.3×10^{-3}



plots: P. Franzini courtesy

V_{us} from all results



$$\langle V_{us} \times f_+(0) \rangle_{\text{WORD AV.}} = 0.2164(4)$$

- CKM unitarity within $\sim 1\sigma$

Slopes

$$\lambda'_+ = 0.02542(31)$$

$$\lambda''_+ = 0.00129(3)$$

(Pole model: KLOE,
KTeV, and NA48 av.)

$$\lambda_0 = 0.01587(95)$$

(KTeV and ISTR+ av.)

From unitarity

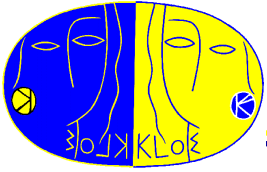
- $f_+(0) = 0.961(8)$

Leutwyler and Roos Z.
[Phys. C25, 91, 1984]

- $V_{ud} = 0.97377(27)$

Marciano and Sirlin
[Phys.Rev.Lett.96 032002,2006]

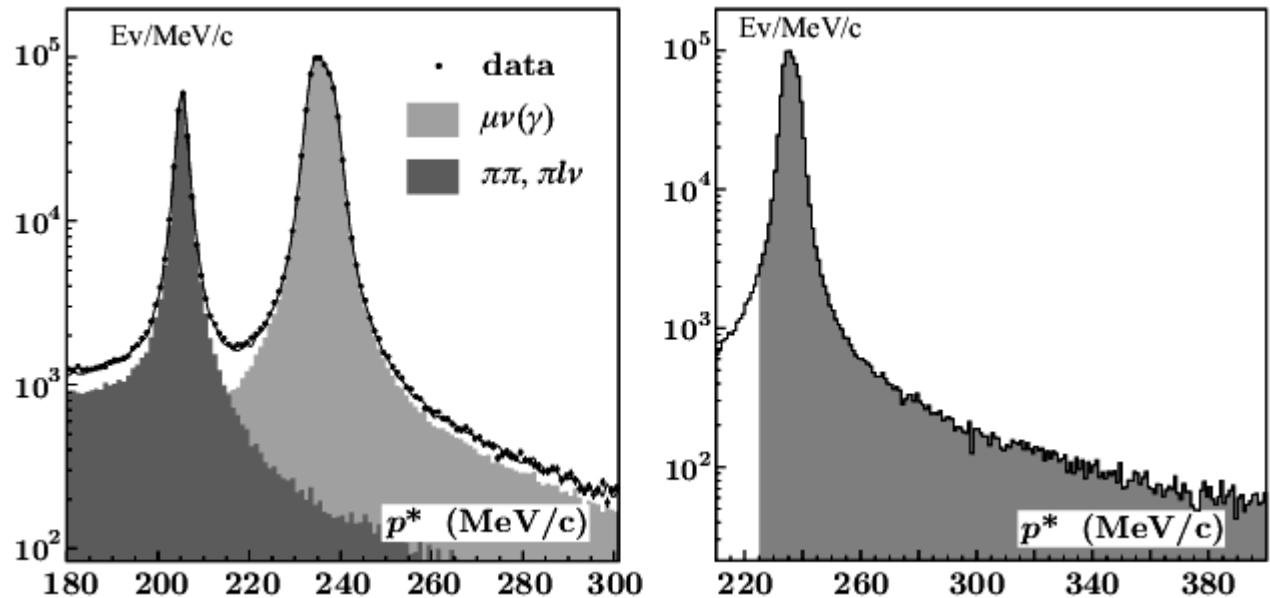
$$V_{us} \times f_+(0) = 0.2187(22)$$



Measurement of $BR(K^+ \rightarrow \mu^+ \nu(\gamma))$

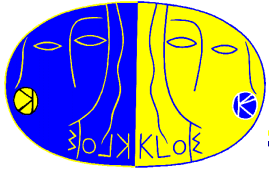
- The ratio $|V_{us}|/|V_{ud}|$ can be extracted from the ratio of μ decays of kaons and pions: $\Gamma(K \rightarrow \mu \nu(\gamma))/\Gamma(\pi \rightarrow \mu \nu(\gamma)) \propto |V_{us}|^2/|V_{ud}|^2 f_K^2/f_\pi^2$
- From lattice calculations: $f_K/f_\pi = 1.198(3)^{(+16}_{-5)}$ (MILC Coll. PoS (LAT2005) 025)
- $K\ell 3$ -independent V_{us} determination

- Tag from $K^- \rightarrow \mu^- \nu$. Subtraction of $\pi^+\pi^0$, $\pi^0 l^+ \nu$ background.
- Count events in (225,400) MeV window of the momentum distribution in K rest frame.



$$BR(K^+ \rightarrow \mu^+ \nu(\gamma)) = 0.6366 \pm 0.0009_{\text{stat.}} \pm 0.0015_{\text{syst.}}$$

Published
PLB632(2006) 76



The $V_{us} - V_{ud}$ plane

- Using $f_K/f_\pi = 1.198(3)^{+16}_{-5}$ from MILC Coll. (2005) and KLOE BR($K^+ \rightarrow \mu^+\nu$) we get $V_{us}/V_{ud} = 0.2294 \pm 0.0026$

- $V_{us} = 0.2248 \pm 0.0020$
K_{l3} KLOE, using $f_+(0) = 0.961(8)$
- $V_{ud} = 0.97377 \pm 0.00027$
Marciano and Sirlin
Phys.Rev.Lett.96 032002,2006

Fit of the above results:

$$V_{us} = 0.2242 \pm 0.0016$$

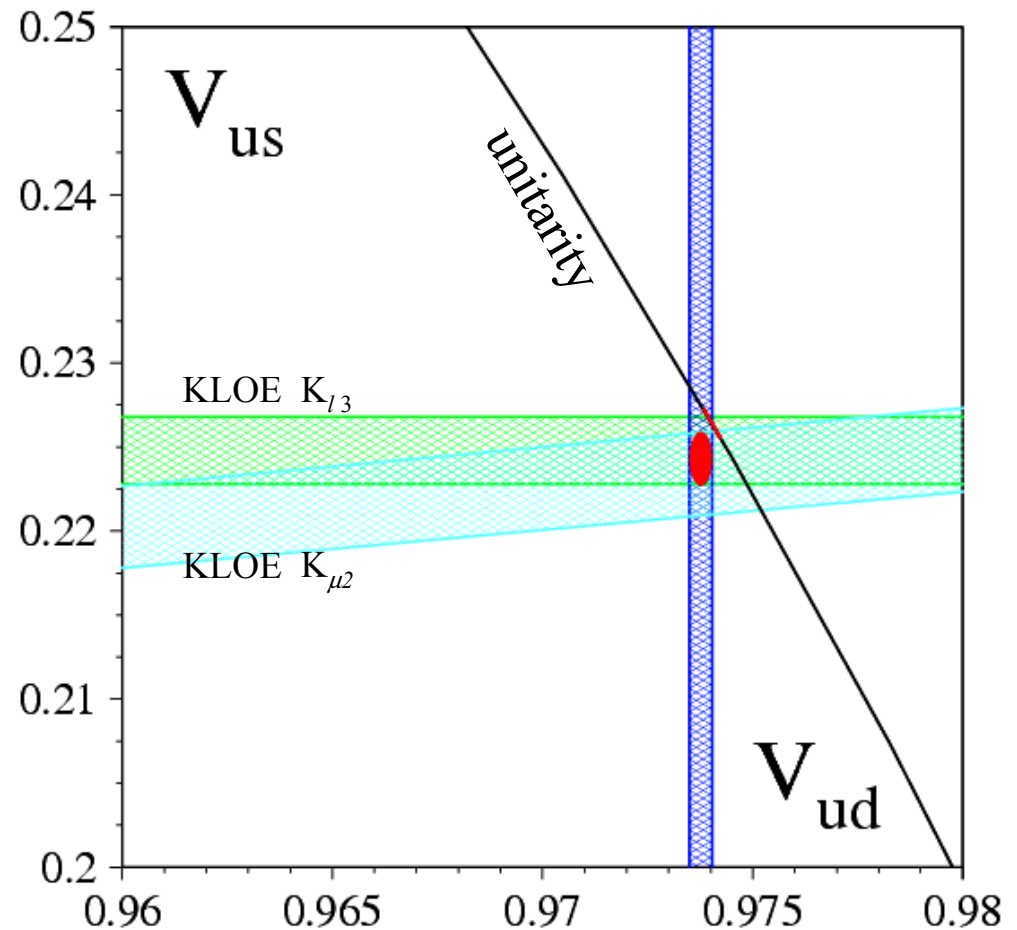
$$V_{ud} = 0.97377 \pm 0.00027$$

$$P(\chi^2) = 0.8$$

Fit assuming unitarity:

$$V_{us} = 0.2264 \pm 0.0009$$

$$P(\chi^2) = 0.1$$



CPT symmetry

- CPT symmetry is linked to the basic mathematical tools that we use in particle physics: QFT + Lorentz invariance + Locality \rightarrow CPT
- These tools have intrinsic limitations (we are not able to include gravity in a consistent way) and we should expect CPT violation at some level
- It's hard to define a reference scale/size for CPT violation (no consistent and predictive theory without these tools)
- Phenomenologically driven search i.e. reference scale set by the most significant experimental bounds
- The **neutral kaon system** is an ideal testing ground:
 - Charge asymmetries of the semileptonic decays.
 - The unitarity (Bell-Steinberger) relation.

The unitarity and the Bell-Steinberger relation

Even if CPT is violated, we can assume that unitarity (i.e. the conservation of the probability) is conserved.

Expressing the neutral kaon decay amplitudes in the K_L - K_S basis: $K_S \propto K_+ + (\epsilon - \delta)K_-$; $K_L \propto K_- + (\epsilon + \delta)K_+$,
 ϵ and δ : CP and CPT violation parameters

$$\begin{aligned}\Gamma_{K^0} = \Gamma_{11} &= \sum_f \mathcal{A}(K^0 \rightarrow f) \mathcal{A}(K^0 \rightarrow f)^* \\ \Gamma_{\bar{K}^0} = \Gamma_{22} &= \sum_f \mathcal{A}(\bar{K}^0 \rightarrow f) \mathcal{A}(\bar{K}^0 \rightarrow f)^* \\ \Gamma_{12} &= \sum_f \mathcal{A}(K^0 \rightarrow f) \mathcal{A}(\bar{K}^0 \rightarrow f)^* \\ \Gamma_{21} &= \sum_f \mathcal{A}(\bar{K}^0 \rightarrow f) \mathcal{A}(K^0 \rightarrow f)^*\end{aligned}$$

$$\left[\frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right] \frac{\text{Re}(\epsilon) - i \text{Im}(\delta)}{1 + |\epsilon|^2} = \frac{1}{\Gamma_S - \Gamma_L} \sum A_L(f) A_S^*(f) = \sum_f \alpha_f$$

This is an exact relation: phase convention independent, no approximations in the CPT limit (δ treated as small parameter and expanded to 1st non trivial order).

- Experimental inputs: Γ_S , Γ_L , m_S , m_L , and α_f $\phi_{SW} = \arctan\left[\frac{2(m_L - m_S)}{\Gamma_S - \Gamma_L}\right] \approx 43.4^\circ$
- Two physical outputs: $\text{Re } \epsilon$ and $\text{Im } \delta$:

If $\text{Im } \delta \neq 0$: CPT violation, unitarity violation, new exotic invisible final states.

$$\delta = \frac{i(m_{K_0} - m_{\bar{K}_0}) + \frac{1}{2}(\Gamma_{K_0} - \Gamma_{\bar{K}_0})}{\Gamma_S - \Gamma_L} \cos \phi_{SW} e^{i\phi_{SW}} [1 + O(\epsilon)]$$

- If $\Delta\Gamma=0$ (CPT conserved in the decay): $|\Delta m/m_{K_0}| \approx 3 \times 10^{-14} |\text{Im } \delta|$

Details on definition of decay amplitudes

$$\left[\frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right] \frac{\text{Re}(\epsilon) - i \text{Im}(\delta)}{1 + |\epsilon|^2} = \sum_f \alpha_f$$

$\pi\pi$ decays: $\alpha_{+-} = \eta_{+-} \text{Br}(\mathbf{K}_S \rightarrow \pi^+ \pi^-)$

$$\alpha_{00} = \eta_{00} \text{Br}(\mathbf{K}_S \rightarrow \pi^0 \pi^0)$$

$$\alpha_{+-\gamma} = \eta_{+-\gamma} \text{Br}(\mathbf{K}_S \rightarrow \pi^+ \pi^- \gamma)$$

$\pi\pi\pi$ decays: $\alpha_{+-0} = \tau_S/\tau_L \eta_{+-0}^* \text{Br}(\mathbf{K}_L \rightarrow \pi^+ \pi^- \pi^0)$

$$\alpha_{000} = \tau_S/\tau_L \eta_{000}^* \text{Br}(\mathbf{K}_L \rightarrow \pi^0 \pi^0 \pi^0)$$

CPT-violation in decay



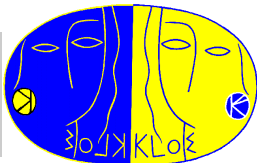
Semileptonic decays: $\alpha_{kl3} = 2\tau_S/\tau_L \text{Br}(\mathbf{K}_L l3) [\text{Re} \epsilon - \text{Re} y - i(\text{Im} \delta + \text{Im} x_+)]$

$$= 2\tau_S/\tau_L \text{Br}(\mathbf{K}_L l3) [(\mathbf{A}_S + \mathbf{A}_L)/4 - i(\text{Im} \delta + \text{Im} x_+)]$$

from “ $(\mathbf{A}_S - \mathbf{A}_L)$
and CPLEAR”



Other decays contribute less than 10^{-6}



Inputs to $B-S$ relation

input	value	Used sources
τ_S	0.08958 ± 0.00006 ns	PDG (*) [3]
τ_L	50.84 ± 0.23 ns	KLOE [4,5]
$\Gamma(K_S \rightarrow \pi^+ \pi^-) / \Gamma(K_S \rightarrow \pi^0 \pi^0)$	2.2549 ± 0.0054	KLOE [6]
$\text{BR}(K_L \rightarrow \pi^+ \pi^-)$	$(1.965 \pm 0.010) \times 10^{-3}$	KLOE [7], KTeV [8]
$\text{BR}(K_L \rightarrow \pi^0 \pi^0)$	$(0.865 \pm 0.010) \times 10^{-3}$	KTeV [8]
$\text{BR}(K_S \rightarrow \pi^+ \pi^- \gamma)_{DE}$	$< 1.8 \times 10^{-4}$ 95%CL	E731 [11]
$\text{BR}(K_L \rightarrow \pi^+ \pi^- \gamma)_{DE}$	$(31 \pm 1) \times 10^{-6}$	KTeV [10]
$\text{BR}(K_L \rightarrow \pi l \nu)$	0.6705 ± 0.0022	KLOE [5]
η_{+-0}	$(-2 \pm 7)10^{-3} + i(-2 \pm 9)10^{-3}$	CPLEAR [13]
$\text{BR}(K_L \rightarrow \pi^+ \pi^- \pi^0)$	0.1263 ± 0.0012	KLOE [5]
$\text{BR}(K_S \rightarrow 3\pi^0)$	$< 1.2 \cdot 10^{-7}$ 90%CL	KLOE [12]
$\text{BR}(K_L \rightarrow 3\pi^0)$	0.1997 ± 0.0020	KLOE [5]
Φ_{+-}	$(43.4 \pm 0.7)^\circ$	PDG (*) [3]
Φ_{00}	$(43.7 \pm 0.8)^\circ$	PDG (*) [3]
Φ_{SW}	$(43.51 \pm 0.06)^\circ$	PDG [3]
$\Phi^{000}, \Phi^{+-\gamma}$	$[0, 2\pi]$	
A_L	$(3.32 \pm 0.06) \times 10^{-3}$	PDG [3]
A_S	$(1.5 \pm 10.0) \times 10^{-3}$	KLOE [14]
$\text{Im}(x_+)$	$(0.8 \pm 0.7) \times 10^{-3}$	CPLEAR [13], KLOE [14], PDG [3]

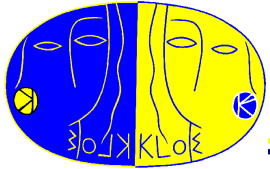
• 2006 results

• Quantities evaluated without assuming CPT invariance.

• $\text{Im } x_+ = (1.2 \pm 2.2) \times 10^{-2}$ by CPLEAR.

A combined fit of CPLEAR data with KLOE-KTeV ($A_S - A_L$) gives a $\times 3$ improvement

$\text{Im } x_+ = (0.8 \pm 0.7) \times 10^{-2}$



K_S physics

$$\text{BR}(K_S \rightarrow \pi^+\pi^-(\gamma))/\text{BR}(K_S \rightarrow \pi^0\pi^0)$$

- Fixes $\text{BR}(K_S \rightarrow \pi^+\pi^-(\gamma))$, used to normalize $\text{BR}(K_S \rightarrow \pi e \nu)$

$$R_{\pi\pi} = 2.2549 \pm 0.0054 \text{ (hep-ex/0601025, subm. EPJC)}$$

Fractional error 0.24%

$$\text{BR}(K_S \rightarrow \pi^+e^+\nu)/\text{BR}(K_S \rightarrow \pi^+\pi^-(\gamma))$$

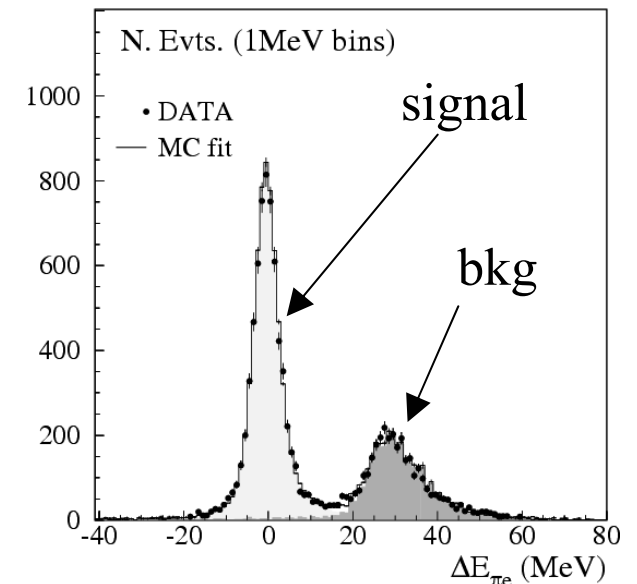
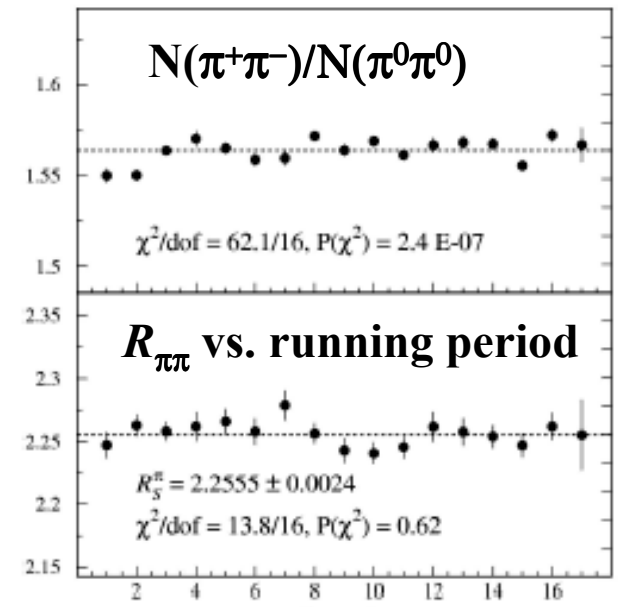
- TOF e/π identification, fit to $E_{\text{miss}}-P_{\text{miss}}$ spectrum
- Normalize to $\pi^+\pi^-$ counts in the same dataset.
- Separate measurement for each charge state ($e^-\pi^+, e^+\pi^-$)

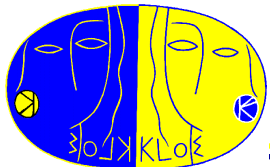
$$\text{BR}(\pi e \nu) = (7.046 \pm 0.077 \pm 0.049) \times 10^{-4}$$

Fractional error 1.3% = 1.1%_{STAT} \oplus 0.7%_{SYST}

$$K_{Se3} \text{ form factor slope: } \lambda_+ = (33.9 \pm 4.1) \times 10^{-3}$$

First measurement, compatible with K_L





CPT test from A_S and A_L

- Sensitivity to CPT violating effects through charge asymmetry of the semileptonic neutral kaon decays:

$$A_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow \pi e^+ \nu) - \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})}{\Gamma(K_{S,L} \rightarrow \pi e^+ \nu) + \Gamma(K_{S,L} \rightarrow \pi^+ e^- \bar{\nu})} \quad \begin{aligned} A_S &= 2(\text{Re } \varepsilon + \text{Re } \delta - \text{Re } y + \text{Re } x_-) \\ A_L &= 2(\text{Re } \varepsilon - \text{Re } \delta - \text{Re } y - \text{Re } x_-) \end{aligned}$$

- A_L already measured by KTeV (2002): $A_L = (3.322 \pm 0.058 \pm 0.047) 10^{-3}$
- A_S measured for the first time by KLOE (2006): $A_S = (1.5 \pm 9.6 \pm 2.9) 10^{-3}$

- $A_S - A_L = 4(\text{Re } \delta + \text{Re } x_-) \neq 0$ implies CPT and $\Delta S = \Delta Q$ rule violation

Re δ : CPLEAR $\sigma = 3.4 \times 10^{-4}$

Re $x_- = (-0.8 \pm 2.5) 10^{-3}$

Factor 5 of improvement wrt current most precise

measurement: CPLEAR, $\sigma = 1.3 \times 10^{-2}$

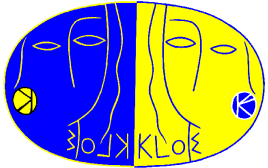
- $A_S + A_L = 4(\text{Re } \varepsilon - \text{Re } y) \neq 0$ implies CPT violation

Re ε from PDG not assuming CPT

Re $y = (0.4 \pm 2.5) 10^{-3}$

Comparable with best result: CPLEAR from unitarity, $\sigma = 3.1 \times 10^{-3}$.

$K_L \rightarrow \pi^+ \pi^-$



$$\text{BR}(K_L \rightarrow \pi^+ \pi^- (\gamma_{\text{IB+DE}}))$$

KLOE: PID using decay kinematics.

Normalize to $K_L \mu 3$ events

$$\text{BR}(K_L \rightarrow \pi^+ \pi^- (\gamma_{\text{IB+DE}})) = (1.963 \pm 0.021) \times 10^{-3} \text{ PLB638}$$

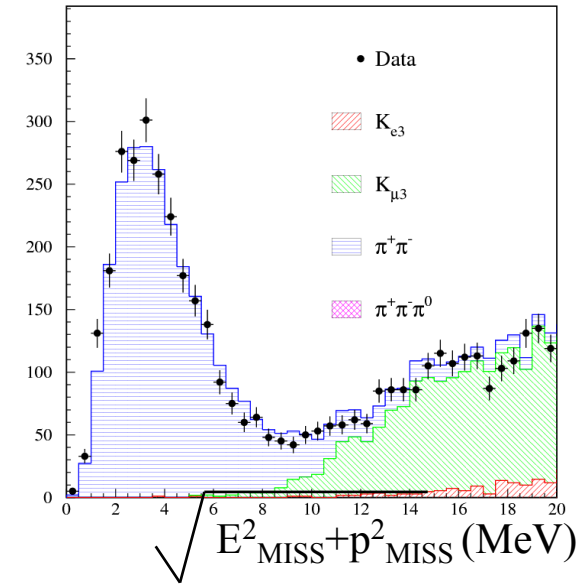
$$\text{Fractional error } 1.1\% = 0.6\%_{\text{STAT}} \oplus 0.9\%_{\text{SYST}}$$

In agreement with KTeV 2004 BR = $1.975(12) \times 10^{-3}$

It confirms the 4σ discrepancy with PDG04

$$|\eta_{+-}| = (2.216 \pm 0.013) \times 10^{-3}$$

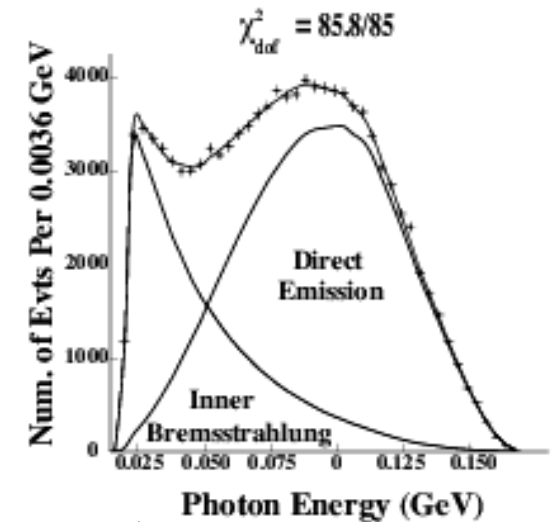
BR($K_S \rightarrow \pi\pi$) and τ_L from KLOE, τ_S from PDG04



$$\text{BR}(K_L \rightarrow \pi^+ \pi^- (\gamma_{\text{DE}}))$$

- 1997 dataset of E832 (collected during ϵ'/ϵ data taking)
- After all analysis cuts 112.1×10^3 candidates with an estimated background of 671 events, mostly $K_L \mu 3$ and $K_L e 3$ decays.

$$\text{BR}(K_L^0 \rightarrow \pi^+ \pi^- (\gamma_{\text{DE}})) = (29 \pm 1) \times 10^{-6}; \text{ hep-ex/0604035 (subm. PLB)}$$



$K_S \rightarrow \pi^0 \pi^0 \pi^0$ decays

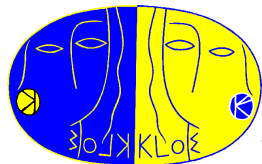
Observation of $K_S \rightarrow 3\pi^0$ signals CP violation in mixing and/or decay:

SM prediction: $\Gamma_S = \Gamma_L |\eta|^2$, giving $\text{BR}(K_S \rightarrow 3\pi^0) = 1.9 \times 10^{-9}$



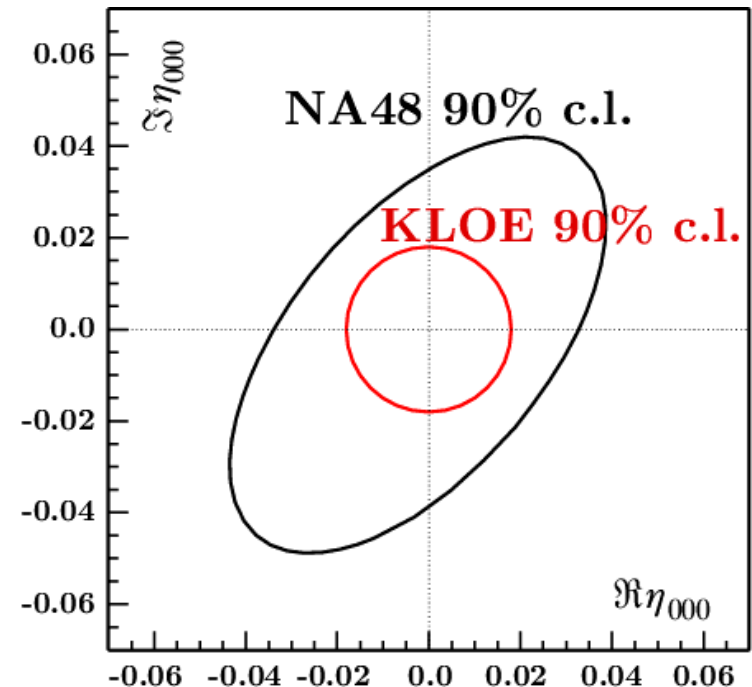
NA48: Measures directly η_{000} through the $K \rightarrow 3\pi^0$ rate as a function of the proper time.

- $\eta_{000} = (-0.002 \pm 0.019) + i(-0.003 \pm 0.021)$



KLOE:

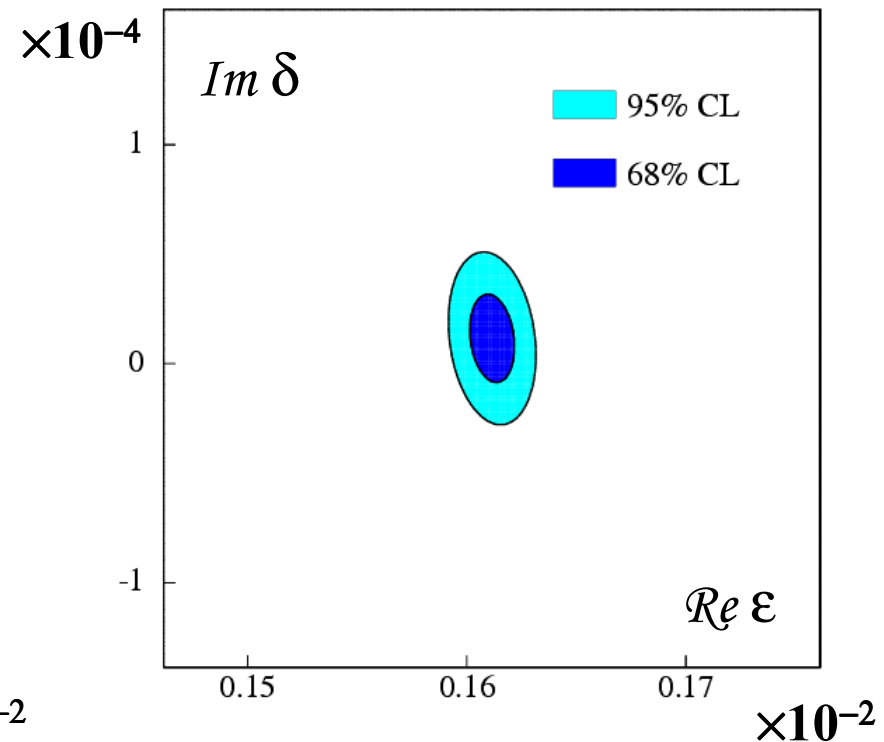
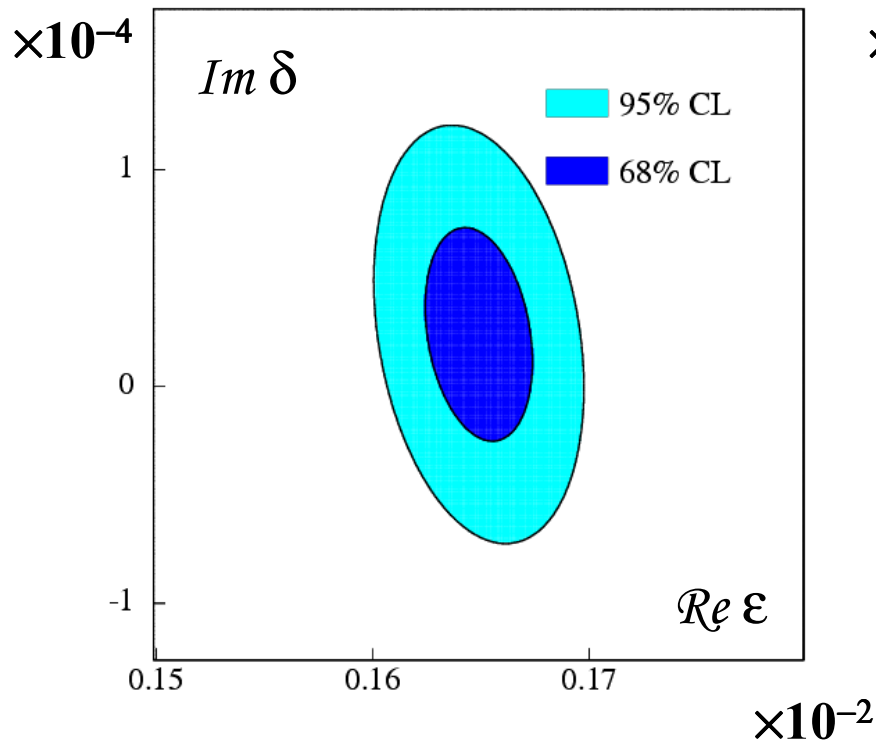
- Direct search for $K_S \rightarrow 3\pi^0$ decays
- Normalize to the $K_S \rightarrow 2\pi^0$ in the same data sample
- $\text{BR}(K_S \rightarrow 3\pi^0) \leq 1.2 \times 10^{-7}$, 90% C.L.
- $\eta_{000} \leq 0.018$



$$\alpha_{000} = \tau_S / \tau_L \eta_{000}^* \text{B}(K_L \rightarrow \pi^0 \pi^0 \pi^0) \leq 0.010, 95\% \text{ C.L.}$$

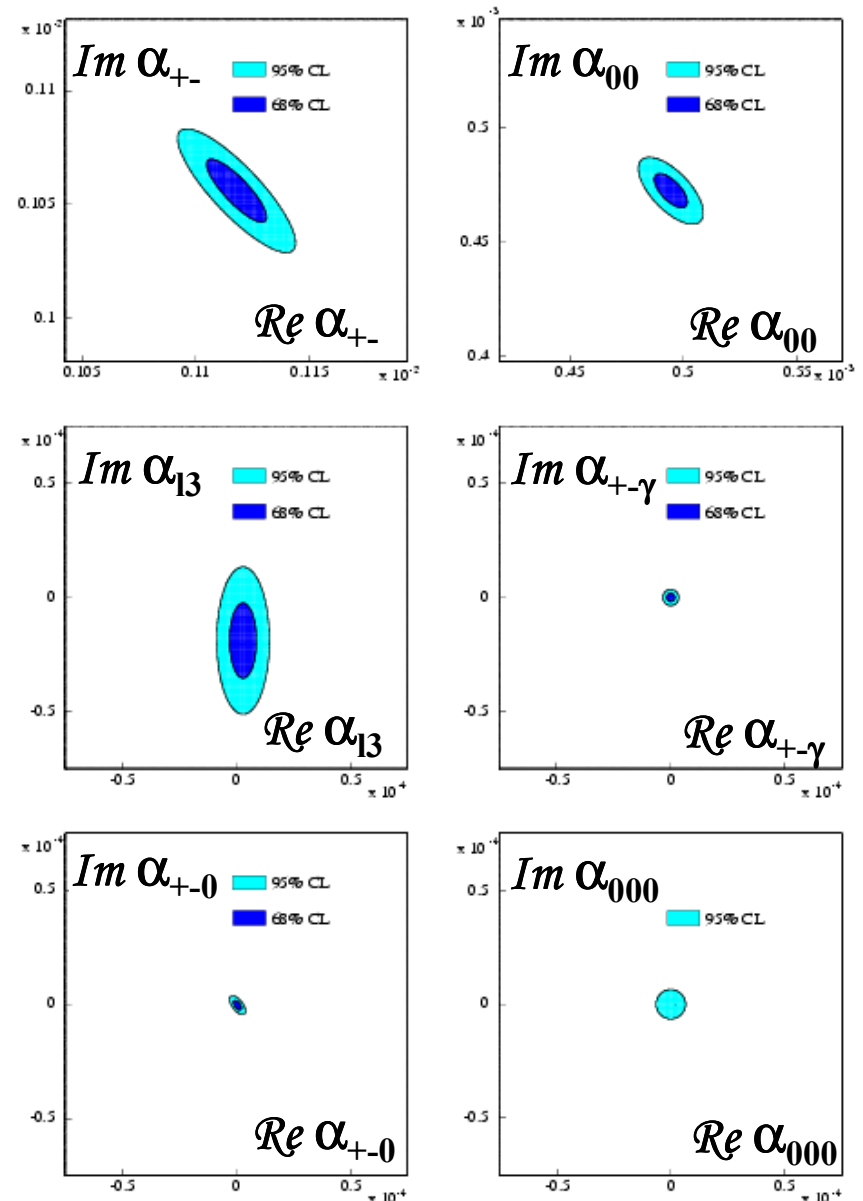
CPT test from unitarity: result

$$\left[\frac{\Gamma_S + \Gamma_L}{\Gamma_S - \Gamma_L} + i \tan \phi_{SW} \right] \frac{\text{Re}(\epsilon) - i \text{Im}(\delta)}{1 + |\epsilon|^2} = \sum_f \alpha_f$$



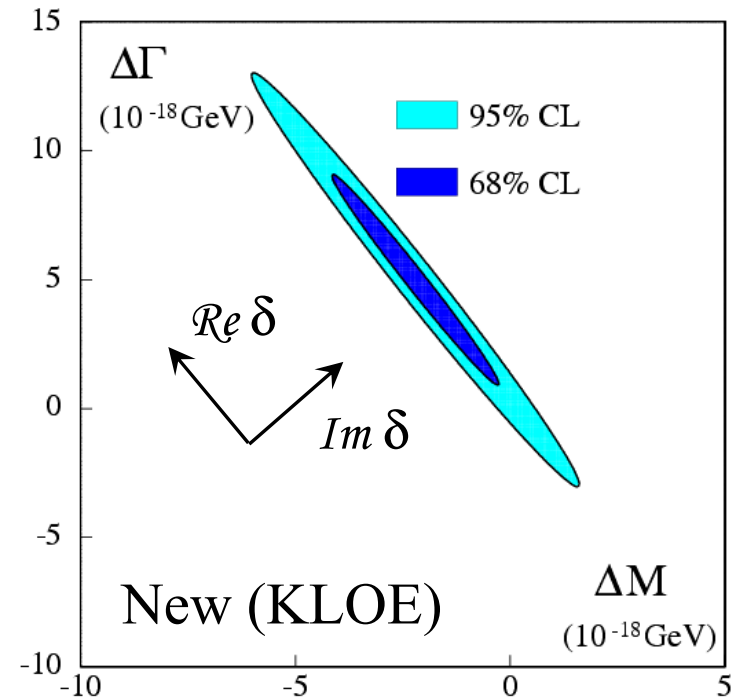
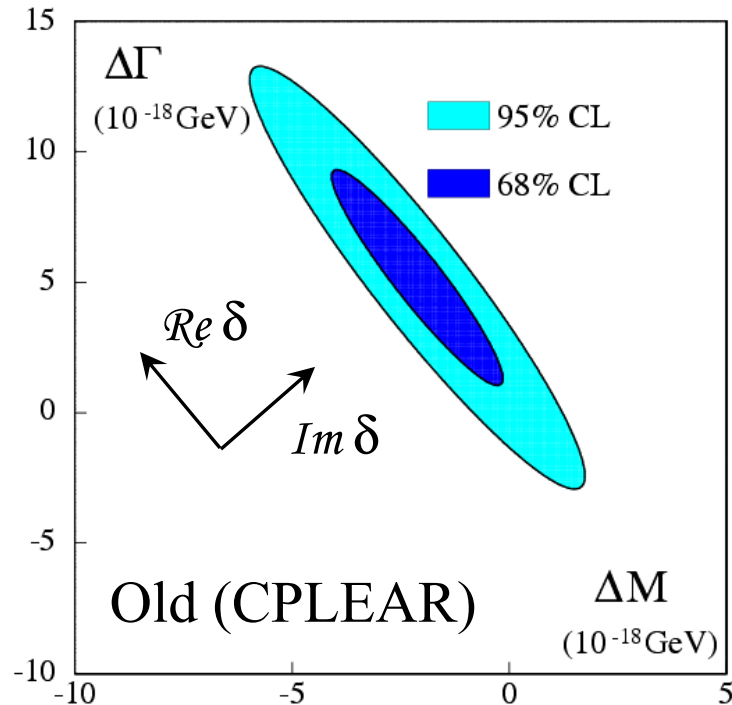
Inputs to B - S : summary

- Before, the accuracy on $\text{Re } \epsilon$ and $\text{Im } \delta$ was dominated by the poor knowledge of η_{000}
- Thanks to the KLOE measurements of η_{000} and A_S , the accuracy on $\text{Re } \epsilon$ and $\text{Im } \delta$ improved of a factor ~ 2.5 .
- The limiting quantities are $\text{Im } x_+$ and ϕ_{+-} for $\text{Im } \delta$
 η_{+-} and η_{00} for $\text{Re } \epsilon$.
- The semileptonic sector contributes by 15% and induces a small correlation between $\text{Re } \epsilon$ and $\text{Im } \delta$.



CPT test: $\Delta\Gamma$ vs Δm

From $Im \delta$ and $Re \delta$ it is possible to extract limits on $\Delta m = (m_{K^0} - m_{\bar{K}^0})$
and $\Delta\Gamma = (\Gamma_{K^0} - \Gamma_{\bar{K}^0})$



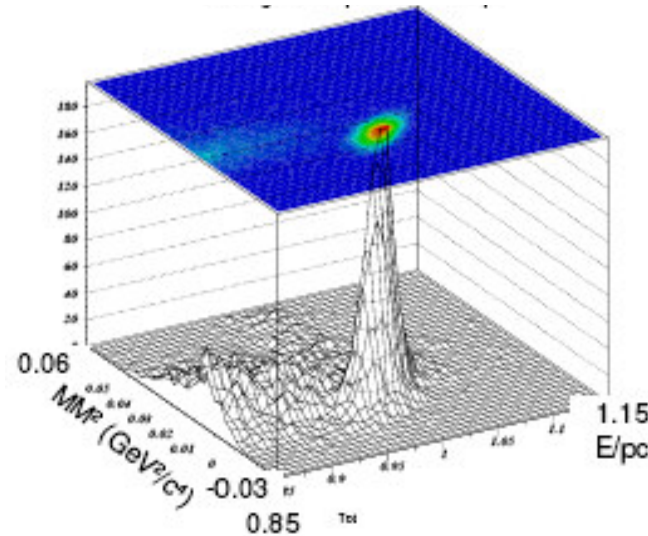
Assuming no CPT violation in the decay ($\Delta\Gamma = 0$) obtain the limit on the neutral kaon mass difference:

$$-4 \times 10^{-19} \text{ GeV} < m_{K^0} - m_{\bar{K}^0} < 7 \times 10^{-19} \text{ GeV}$$



$$R_K = \Gamma(K^+ \rightarrow e^+ \nu) / \Gamma(K^+ \rightarrow \mu^+ \nu)$$

- Present measurement come from 3 experiments of '70. Low energy K^+ beam stopped in a target, decay at rest.
- 2003 data set
 K_{e2}^\pm signature: $E/p=1$ & $m_v^2=0$
 $N_{TOT} = 5329 (73)$; $Bkg = 659 (26)$
 $N_{SIG} = 4670 (77)^{(+29}_{-8)}_{SYST}$
- Preliminary (EPS05) NA48/2 measurement.



	$R_K \times 10^5$
PDG average	2.45 (11)
SM prediction	2.472 (1)
NA48/2 (2003)	2.416 (43)_{STAT}(24)_{SYST}

Future:

- **NA48/2** 2004 statistics: about $\times 2$ of 2003
 - **KLOE** complete data set (2.5 fb^{-1})
- Slight discrepancy between R_K measurement and the SM prediction
 - 2-body K decays are suppressed (helicity) in SM but generally unsuppressed in SM-extensions (hep-ph/0511289):

$$R_K = (1 + \Delta r^{e-\mu}_{NP}) \frac{\Gamma(K \rightarrow e \nu_e)_{SM}}{\Gamma(K \rightarrow \mu \nu_\mu)_{SM}}$$

CKM unitarity and $K \rightarrow \pi \nu \bar{\nu}$ decays

- “Golden-plated decays”: $\text{BR}(K \rightarrow \pi \nu \bar{\nu})$ can be predicted in the SM framework with very high theoretical accuracy and may provide grounds for precision tests of the flavor structure of the SM

- $\mathbf{K}_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ and $\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu}$ completely determine the Unitarity Triangle.

- Comparison with Unitarity Triangle from B sector could provide decisive tests in the flavor physics: new physics may differentiate between K and B measurement

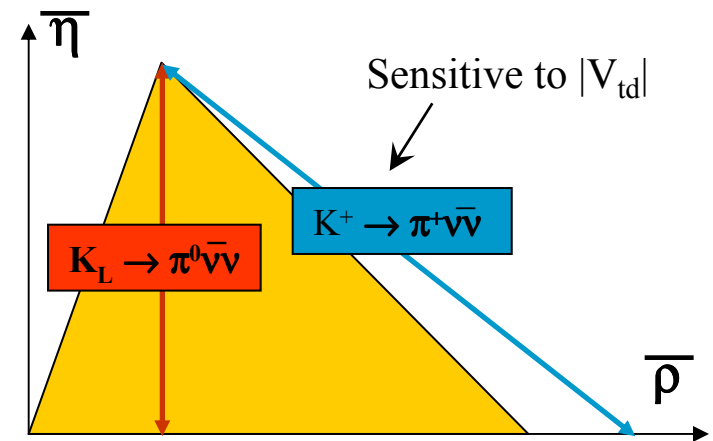
- The *a priori* unknown hadronic matrix element obtained from $K \rightarrow \pi e \nu$ decays.

- **SM predictions:**

$$\text{Br}(\mathbf{K}^+ \rightarrow \pi^+ \nu \bar{\nu}) \approx (1.6 \times 10^{-5}) |V_{cb}|^4 (\rho \eta^2 + (\rho_c - \rho)^2) \rightarrow (8.0 \pm 1.1) \times 10^{-11}$$

$$\text{Br}(\mathbf{K}_L^0 \rightarrow \pi^0 \nu \bar{\nu}) \approx (7.6 \times 10^{-5}) |V_{cb}|^4 \eta^2 \rightarrow (3.0 \pm 0.6) \times 10^{-11}$$

- Combined $\mathbf{K} \rightarrow \pi \nu \bar{\nu}$ measurement determine $(\sin 2\beta)_K$ without being affected by the $|V_{cb}|$ uncertainty.



$K_L \rightarrow \pi^0 \nu \nu$: reminder and outlook

KEK-E391a Upper Limit

No events in the signal box; S.E.S.= 1.17×10^{-7}

$\text{BR}(K_L^0 \rightarrow \pi^0 \nu \nu) < 2.86 \times 10^{-7}$ 90%CL

Preliminary (KAON2005) $\times 6$ improvement over KTeV one day special run

$\times 2$ improvement over published limit (KTeV Dalitz technique)

KOPIO @ BNL stopped

In Japan a step by step approach is followed:

KEK:

E391a has completed data taking (three runs).

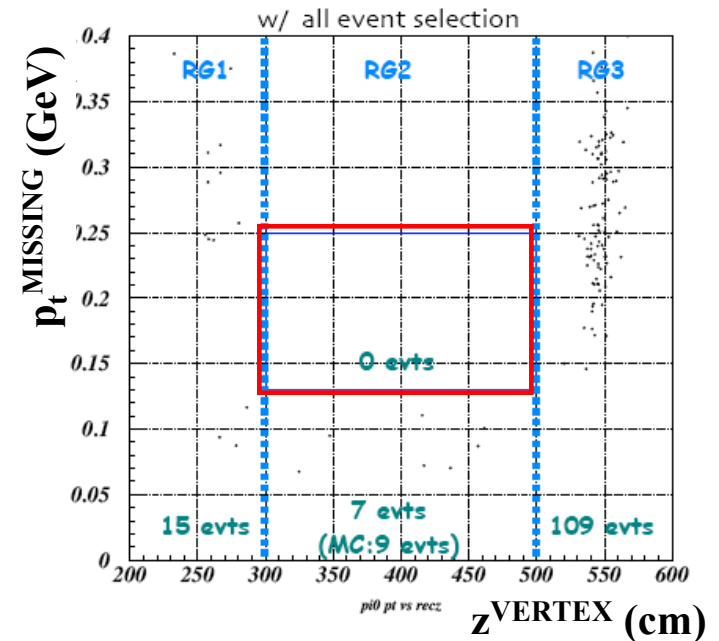
They aim to reach the Grossman-Nir bound from the accumulated data.

J-PARC:

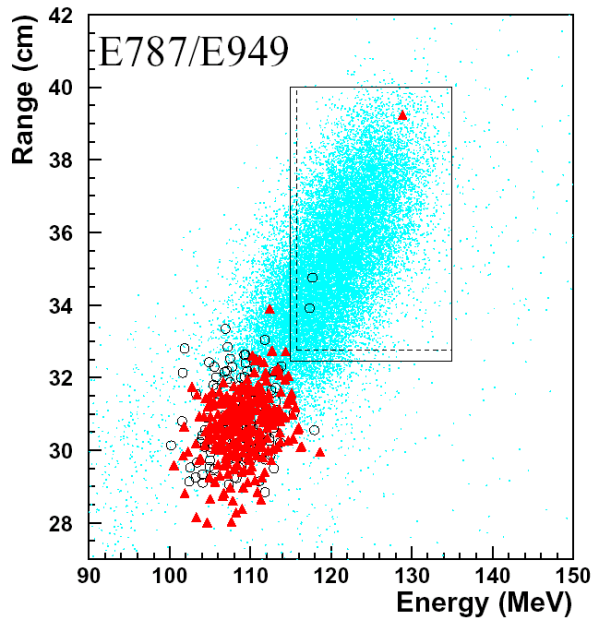
A proposal is being prepared for the new J-PARC hadron facility:

Step I: move the E391a detector at J-PARC

Step II: build a new detector and a dedicated beamline to be able reach about 100 SM events



$K^+ \rightarrow \pi^+ \nu \bar{\nu}$: reminder and outlook



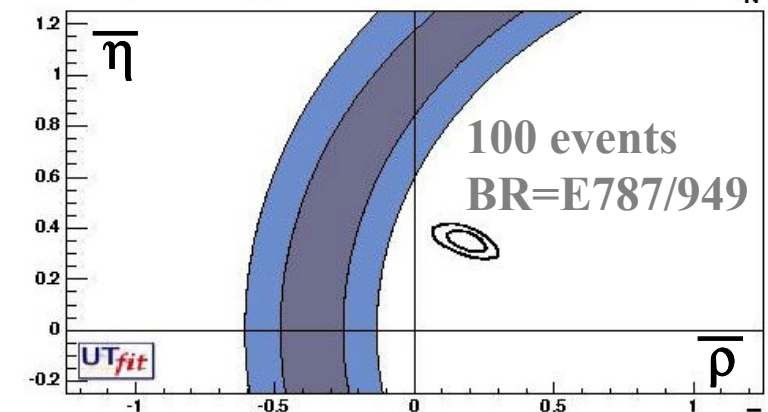
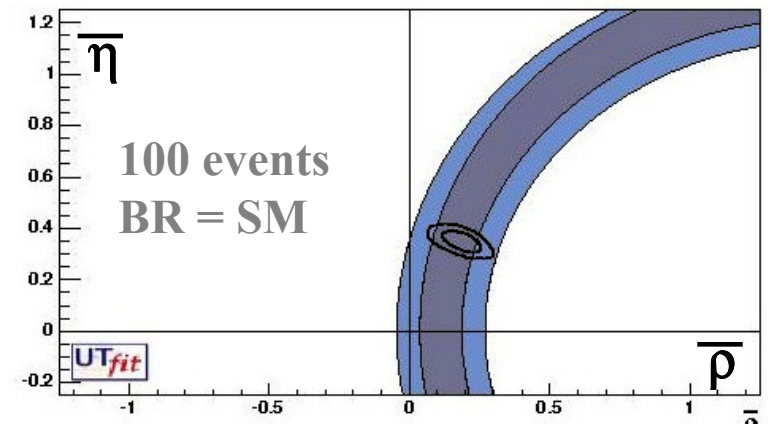
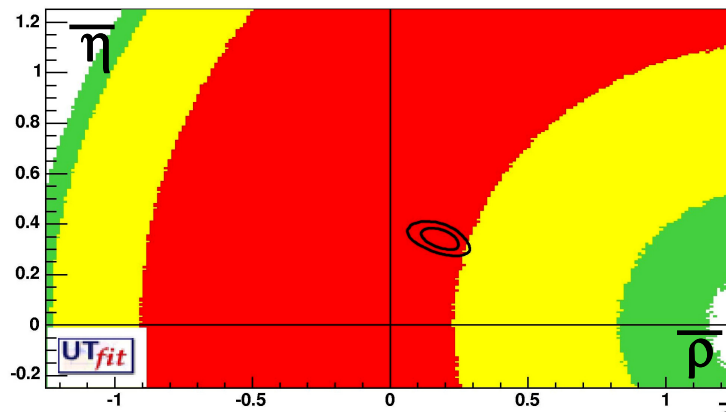
BNL-E787/E949:

Stopped K^+ , $\sim 0.1\%$ acceptance

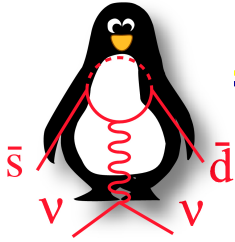
$$\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = 1.47^{+1.30}_{-0.89} 10^{-10}$$

hep-ex/0403036 PRL93 (2004)

- Current constraint on (ρ, η) plane:

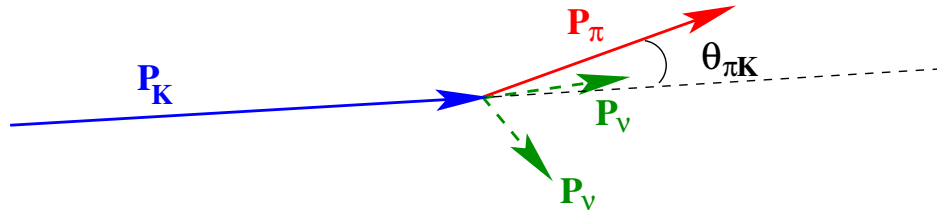


P326



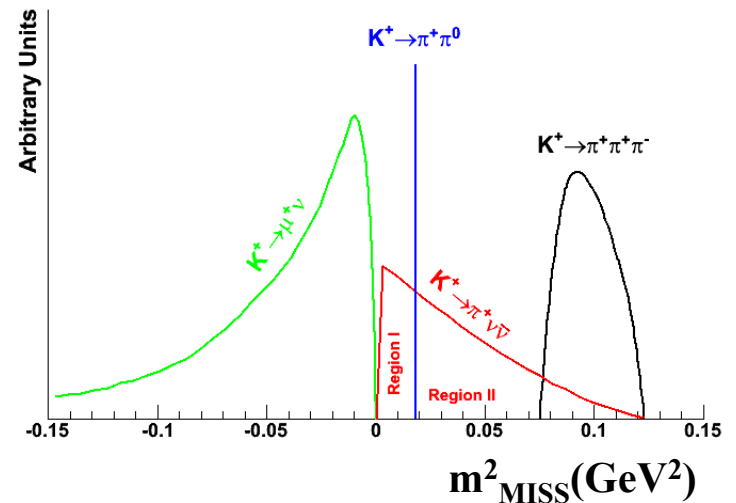
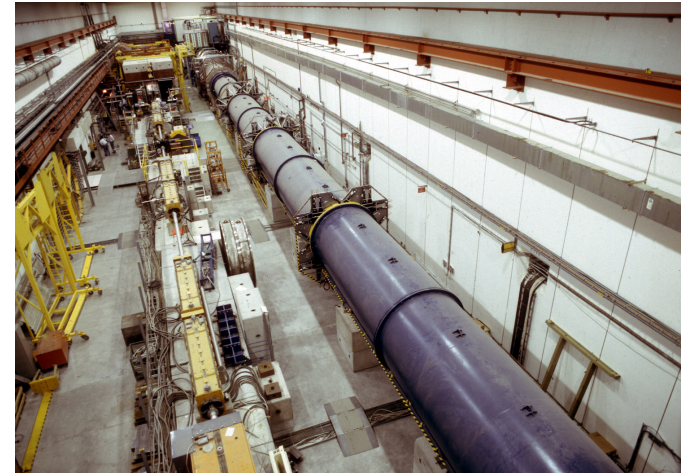
P326 (a.k.a. NA48/3)

- Proposal to measure the rare decay **BR(K⁺→π⁺νν)** at the CERN SPS (CERN-SPS-2005-013, SPSC-P-326)
- Aims to receive full approval by end of 2006... to be able to start data taking some time in 2009-2010



- Kinematic rejection (m^2_{MISS})+photon veto+PID.
- To reject $K^+ \rightarrow \pi\pi^0$ events: 10^{-8} π^0 rejection. (require single photon rejection 10^{-5} for $E_\gamma > 1$ GeV)
- GIGA-tracker.
- **Expect ~100 events in two year with ~10% of background.**

$K^+ \rightarrow \pi^+ \nu \nu$: outlook



Region I: $0 < m^2_{\text{miss}} < 0.01 \text{ GeV}^2$

Region II: $0.026 < m^2_{\text{miss}} < 0.068 \text{ GeV}^2$

Conclusions

Plenty of new results in **kaon physics** since PIC05.

- Totally unexpected $\pi\pi$ scattering length measurement from $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ decays
- Precise bounds on direct CP-violation measured in $K \rightarrow 3\pi$ charged kaons decays.
- New V_{us} world average. Unitarity of CKM matrix tested at 1σ level.
- New determination of CP and CPT parameters: the accuracy on $\text{Re } \varepsilon$ and $\text{Im } \delta$ improved of a factor ~ 2.5 .
- Renewed interest in $K^\pm \rightarrow \ell^\pm \nu$ decays as new physics probe.
- Status and perspectives of the $K \rightarrow \pi \nu \nu$ measurements.

Kaons offer a unique playground to test SM and to shed light on physics beyond SM.

Thanks to G.Isidori and F.Mescia for illuminating discussions in preparing this talk.

Spare slides

Extraction of $\delta_0 - \delta_2$

Cirigliano et al. '04 (EPJC 33 369)

Using KLOE '02 result for $\Gamma(\pi^+\pi^-)/\Gamma(\pi^0\pi^0)$:

Isospin-conserving treatment:

$\Gamma(K_S \rightarrow \pi\pi)$ fully inclusive of $\pi\pi\gamma$ channel

$$\chi_0 - \chi_2 \\ (48.6 \pm 2.6)^\circ$$

Isospin breaking in amplitudes (mainly EM):

$$A_I \rightarrow A_I + \delta A_I$$

A_0, A_2 amplitudes mixed

$\Delta I = 5/2$ component introduced

Small contribution from strong isospin breaking

$$\chi_0 - \chi_2 \\ (54.6 \pm 2.2_{\text{exp}} \pm 0.9_{\text{th}})^\circ$$



Isospin breaking in final state phase shifts:

$$\delta_I = \chi_I - \gamma_I$$

$$\delta_0 - \delta_2 = (-6 \pm 3)^\circ \quad [\chi\text{PT } O(e^2p^2)]$$

$$\delta_0 - \delta_2 \\ (60.8 \pm 2.2_{\text{exp}} \pm 3.1_{\text{th}})^\circ$$

For comparison:

χPT estimate (Gasser & Meissner '91)

$\pi\pi$ scattering (Colangelo et al. '01 $a_0 - a_2 = 0.265 \pm 0.004$)

(Peláez & Ynduráin '04 $a_0 - a_2 = 0.277 \pm 0.014$)

$$\delta_0 - \delta_2 \\ (45 \pm 6)^\circ$$

$$(47.7 \pm 1.5)^\circ$$

$$(52.9 \pm 1.6)^\circ$$

Generators for radiative K decays

Generators for neutral kaon decays include radiation, no cutoff energy

- Full $O(\alpha)$ amplitudes (real and virtual contributions) summed to all orders in α by exponentiation (soft-photon approximation)
- Carefully checked against all available data and calculations

$$\frac{BR(K_L \rightarrow \pi e \nu \gamma, E_\gamma > 30 \text{ MeV } \theta_{e\gamma} > 20^\circ)}{BR(K_L \rightarrow \pi e \nu)} =$$

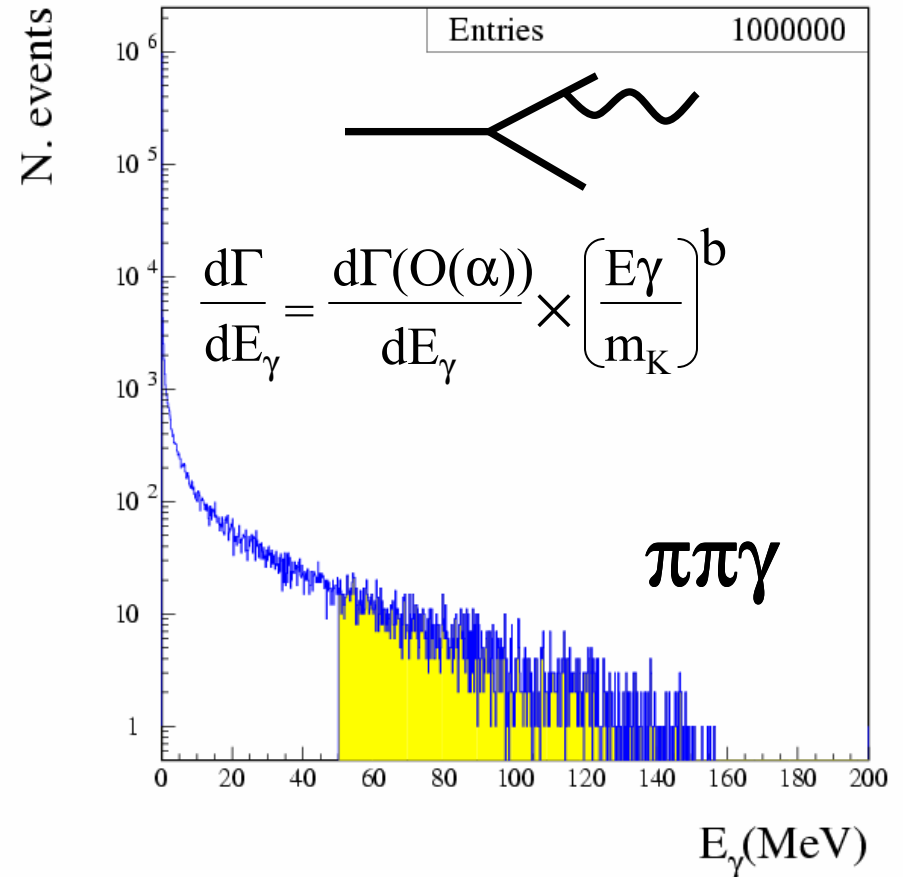
$$kTeV \quad (0.908 \pm 0.015) \times 10^{-2}$$

$$Bijnens \textit{ et al} \quad 0.93 \times 10^{-2}$$

$$MC \quad 0.93 \times 10^{-2}$$

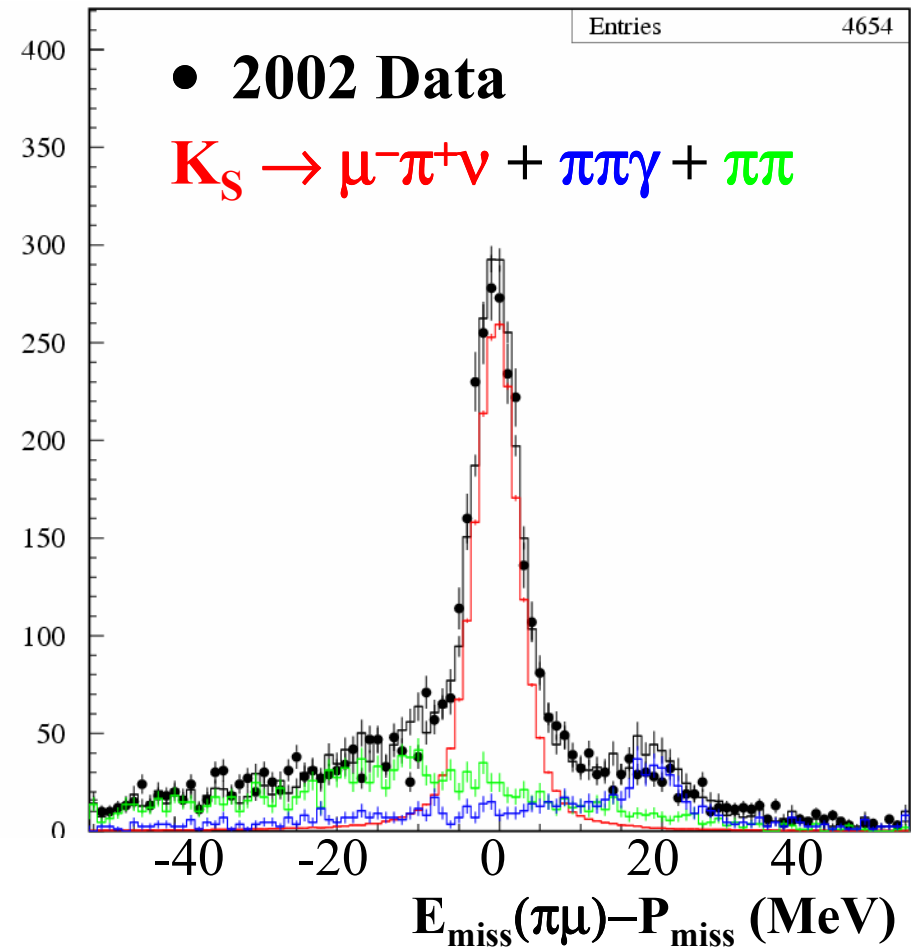
$$\frac{BR(K_S \rightarrow \pi\pi\gamma, E_\gamma > 50 \text{ MeV})}{BR(K_S \rightarrow \pi\pi)} = \begin{array}{ll} E731 & (2.56 \pm 0.09) \times 10^{-3} \\ MC & 2.6 \times 10^{-3} \end{array}$$

KLOE Note 194
(<http://www.lnf.infn.it/kloe>)



$K_S \rightarrow \pi\mu\nu$: first observation

- Measurement never done before
- More difficult than K_{Se3} :
 - 1) Lower BR: expect 4×10^{-4}
 - 2) Background events from $K_S \rightarrow \pi\pi$, $\pi \rightarrow \mu\nu$: same PIDs of the signal
- Event counting from the fit to $E_{\text{miss}}(\pi\mu) - P_{\text{miss}}$ distribution
- Efficiency estimate from $K_{L\mu3}$ early decays and from MC + data control samples.
- Selected about 4500 events per charge in $\sim 400 \text{ pb}^{-1}$. ($\sim 3\%$ stat error)

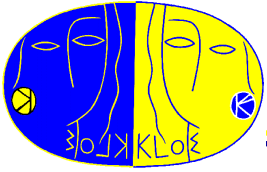


Situation before 2004

Apart from unitarity problem, V_{us} seemed to be well understood before the new data has arrived:

- Measured with $K_L e3$ ($0.2182 \pm 0.0012_{\text{exp}}$), $K^\pm e3$ ($0.2208 \pm 0.0016_{\text{exp}}$) and Hyperon decays (0.2176 ± 0.0026). The most precise measurement came from $K_L e3$ decays.
- $K_L e3$ branching fraction is extracted from various measurements of **36** different experiments performed between 1967-1995, they show good internal agreement
- $f_+(t)$ form factor is measured by ~ 10 experiments, well described by linear λ^+ term. The value of λ^+ is consistent between K^\pm (0.028 ± 0.003) and K_L (0.030 ± 0.002) as well as with theory (chiral QCD) expectations (~ 0.028).
- $f_+(0)$ is calculated by Leutweyler and Roos in 1984, their analysis shows that $K^\pm e3$ and $K_L e3$ data are consistent.

The only problem in this picture was BNL E865 determination of V_{us} based on $K^\pm e3$ data (PRL **91** 261802, published on 31 Dec 2003) which triggered a lot of new experimental activity.



Dominant K_L branching ratios

Absolute BR measurements to 0.5-1%

from '01-'02 data set (328 pb^{-1})

K_L tagged by $K_S \rightarrow \pi^+\pi^-$:

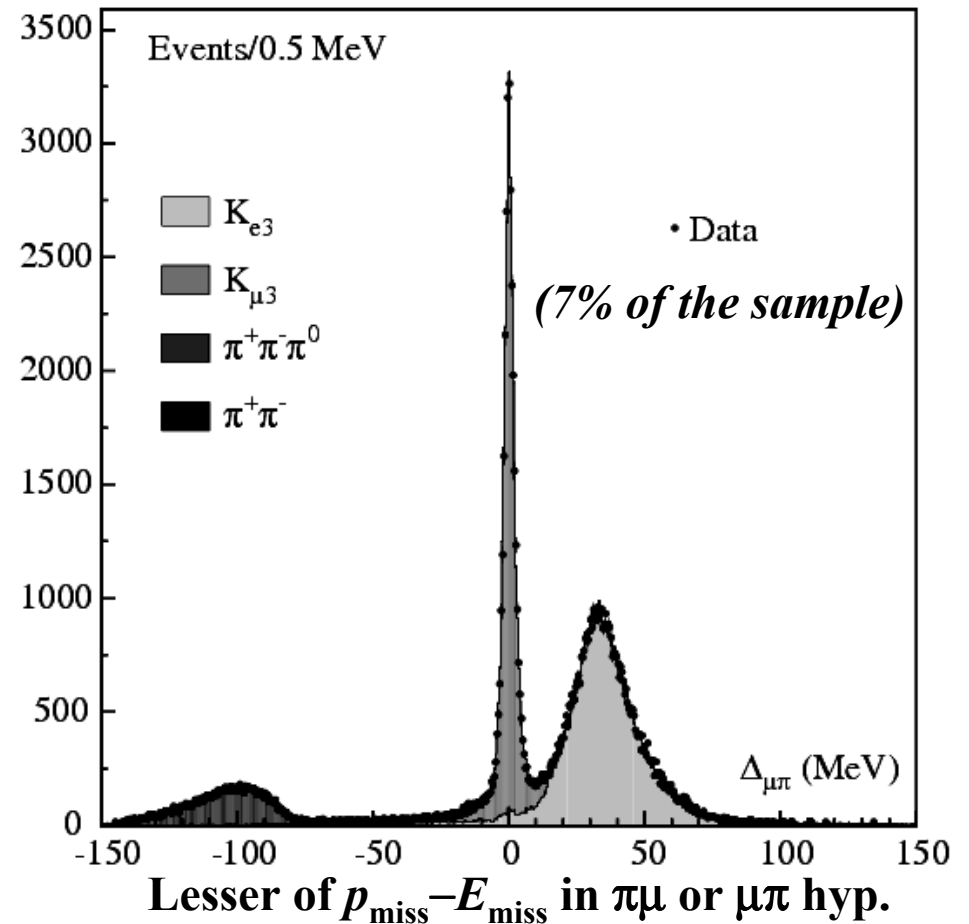
- 13×10^6 for the measurement
- 4×10^6 used to evaluate efficiencies

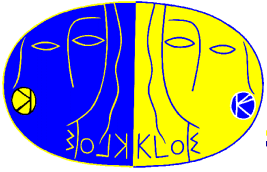
BR's to $\pi e \nu$, $\pi \mu \nu$, and $\pi^+\pi^-\pi^0$:

- K_L vertex reconstructed in DC
- PID using decay kinematics
- Fit with MC spectra including radiative processes and optimized EmC response to $\mu/\pi/K_L$

BR to $\pi^0\pi^0\pi^0$:

- Photon vertex reconstructed by TOF using EmC (3 clusters)
- $E_{\text{rec}} = 99\%$, background $< 1\%$





Direct measurement of K_L lifetime

Measure using $K_L \rightarrow \pi^0\pi^0\pi^0$

- Require ≥ 3 γ 's
- $\varepsilon(L_K) \sim 99\%$, uniform in L
- $\sigma_L(\gamma\gamma) \sim 2.5$ cm
- Background $\sim 1.3\%$

Use $K_L \rightarrow \pi^+\pi^-\pi^0$ to determine:

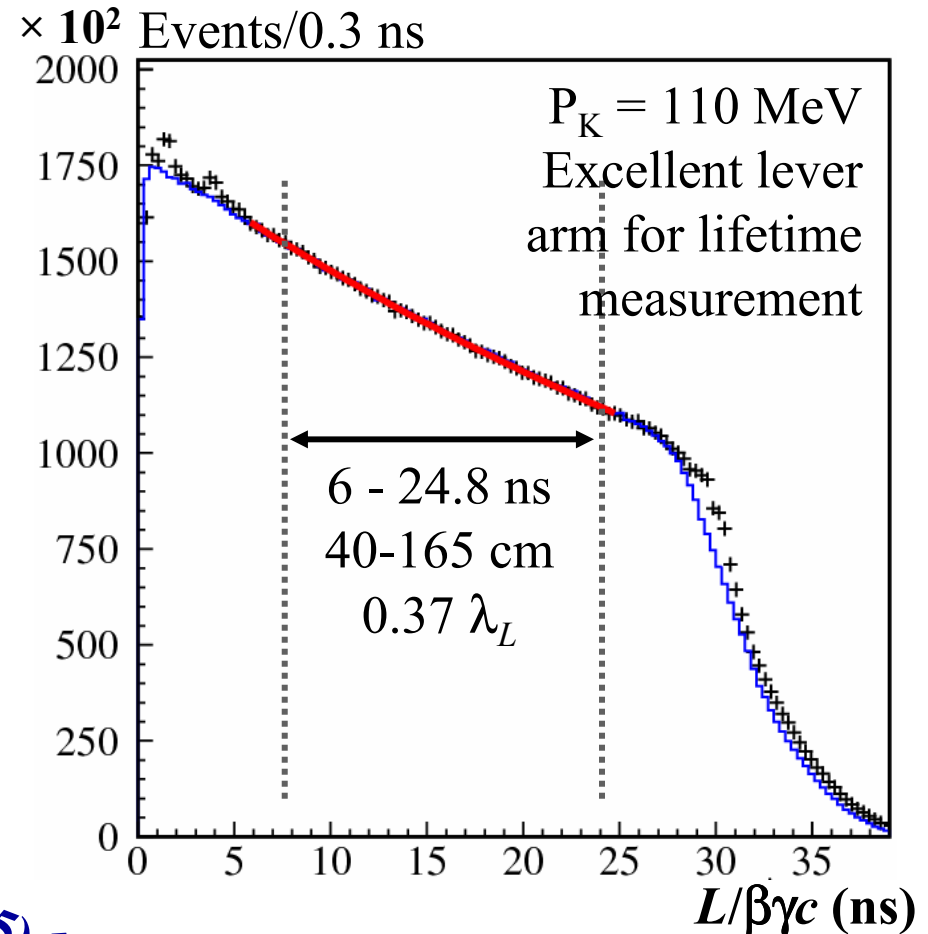
- EmC time scale
- Photon vertex efficiency

KLOE 400 pb⁻¹:

$10^7 K_L \rightarrow \pi^0\pi^0\pi^0$ evts

*Published
PLB626(2005) 15*

$\tau_L = 50.92 \pm 0.17 \pm 0.25$ ns



Average with result from K_L BR's:

$\tau_L = 50.84 \pm 0.23$ ns

Vosburg, '72:

$\tau_L = 51.54 \pm 0.44$ ns

V_{us} from KLOE results

	$K_L e3$	$K_L \mu3$	$K_S e3$	$K^\pm e3$	$K^\pm \mu3$
BR	0.4007(15)	0.2698(15)	$7.046(91) \times 10^{-4}$	0.05047(46)	0.03310(40)
τ	50.84(23) ns		89.58(6) ps	12.384(24) ns	

Slopes

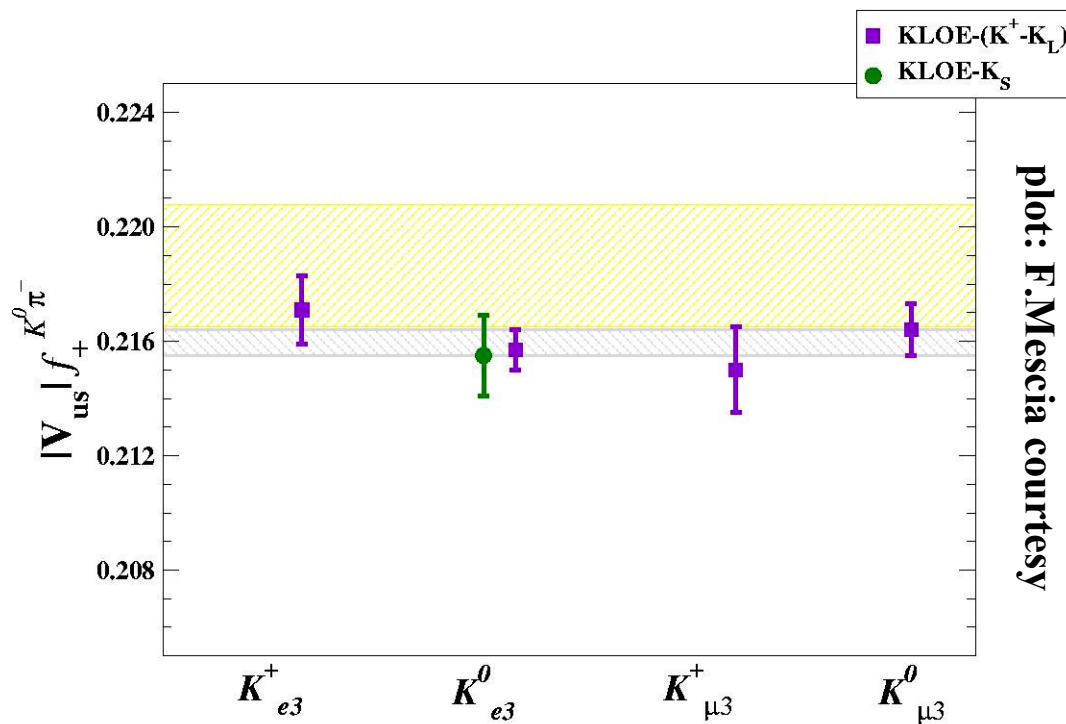
$$\lambda'_+ = 0.02542(31)$$

$$\lambda''_+ = 0.00129(3)$$

(Pole model: KLOE, KTeV, and NA48 ave.)

$$\lambda_0 = 0.01587(95)$$

(KTeV and Istra+ ave.)



$$\langle V_{us} \times f_+(0) \rangle_{\text{KLOE AV.}} = 0.2160(5)$$

CKM unitarity within $\sim 1\sigma$

From unitarity

- $f_+(0) = 0.961(8)$

Leutwyler and Roos Z. [Phys. C25, 91, 1984]

- $V_{ud} = 0.97377(27)$

Marciano and Sirlin [Phys.Rev.Lett.96 032002,2006]

$$V_{us} \times f_+(0) = 0.2187(22)$$

Dominant K_L branching ratios

- KTeV measures 5 K_L decay ratios of 6 decay modes:

$$\Gamma(e3)/\Gamma(\mu3), \Gamma(\pi^+\pi^-\pi^0)/\Gamma(e3), \Gamma(\pi^0\pi^0\pi^0)/\Gamma(e3), \Gamma(\pi^+\pi^-)/\Gamma(e3), \Gamma(\pi^0\pi^0)/\Gamma(\pi^0\pi^0\pi^0)$$

- These 6 decay modes account for 99.93% of K_L decays and the ratio can be combined to extract BR, i.e.:

$$B_{Ke3} = \frac{0.9993}{1 + \frac{\Gamma_{K\mu3}}{\Gamma_{Ke3}} + \frac{\Gamma_{000}}{\Gamma_{Ke3}} + \frac{\Gamma_{+-0}}{\Gamma_{Ke3}} + \frac{\Gamma_{+-}}{\Gamma_{Ke3}} + \frac{\Gamma_{00}}{\Gamma_{Ke3}}} \quad [\text{PRD 70 (2004)}]$$

- Results are:

$$\text{BR}(K_L \rightarrow \pi e \nu) = 0.4067 \pm 0.0011$$

$$\text{BR}(K_L \rightarrow \pi \mu \nu) = 0.2701 \pm 0.0009$$

$$\text{BR}(K_L \rightarrow \pi \pi \pi^0) = 0.1252 \pm 0.0007$$

$$\text{BR}(K_L \rightarrow \pi^0 \pi^0 \pi^0) = 0.1945 \pm 0.0018$$

$$\text{BR}(K_L \rightarrow \pi^+ \pi^-) = (1.975 \pm 0.012) \times 10^{-3}$$

$$\text{BR}(K_L \rightarrow \pi^0 \pi^0) = (0.865 \pm 0.010) \times 10^{-3}$$

Kaon radiative decays: summary

- Hadronic radiative decays of neutral kaons with real and virtual photons give insight into structure of the kaon
- Summary status of the results presented in La Thuile 2006

Real γ	Virtual $\gamma^* \rightarrow e^+e^-$
$K_L \rightarrow \pi^0\pi^0\gamma$ Preliminary results	$K_L \rightarrow \pi^0\pi^0e^+e^-$ Published
$K_L \rightarrow \pi^+\pi^-\gamma$ New Preliminary results	$K_L \rightarrow \pi^+\pi^-e^+e^-$ New results, accepted in PRL
$K_L \rightarrow \pi^+\pi^-\pi^0\gamma$ New Preliminary results	$K_L \rightarrow \pi^+\pi^-\pi^0e^+e^-$ New Preliminary results
$K_L \rightarrow \pi^0\pi^0\pi^0\gamma$ Analysis in progress	$K_L \rightarrow \pi^0\pi^0\pi^0e^+e^-$ Analysis in progress

Kaon radiative decays: summary

Hadronic radiative decays of neutral kaons with real and virtual photons give insight into structure of the kaon

$$\mathbf{K}_L^0 \rightarrow \pi^+ \pi^- \gamma$$

$$g_{M1} = 1.198 \pm 0.035 \text{ (stat)} \pm 0.086 \text{ (syst)}$$

$$a_1/a_2 = -0.738 \pm 0.007 \text{ (stat)} \pm 0.018 \text{ (syst)}$$

$$g_{E1} < 0.21 \text{ (90\% CL)}$$

$$\mathbf{BR}(\mathbf{K}_L^0 \rightarrow \pi^0 \pi^0 \gamma) < 2.52 \cdot 10^{-7} \text{ 90\%CL}$$

$$\mathbf{BR}(\mathbf{K}_L^0 \rightarrow \pi e^+ e^-, M_{ee} > 5 \text{ MeV}) = 1.606 \pm 0.012 \text{ (stat)}^{+0.026}_{-0.016} \text{ (syst)} \pm 0.045 \text{ (ext.) } 10^{-5}$$

$$\mathbf{BR}(\pi^0 \square e^+ e^-, X > 0.95) = 6.56 \pm 0.26 \text{ (stat)} \pm 0.23 \text{ (syst)} 10^{-8}$$

$$\mathbf{K}_L^0 \rightarrow e^+ e^- \gamma$$

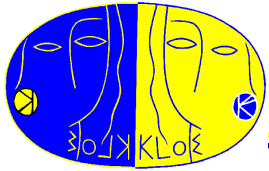
$$\mathbf{BR}(\mathbf{K}_L^0 \rightarrow e^+ e^- \gamma) = 9.25 \pm 0.03 \text{ (stat)} \pm 0.07 \text{ (syst)} \pm 0.26 \text{ (ext)} 10^{-6}$$

$$C \alpha K^* = -0.517 \pm 0.030 \text{ (fit)} \pm 0.022 \text{ (syst)}$$

$$\alpha_{\text{DIP}} = -1.729 \pm 0.043 \text{ (fit)} \pm 0.028 \text{ (syst)}$$

$$\mathbf{BR}(\mathbf{K}_L^0 \rightarrow \pi^+ \pi^- \pi^0 \gamma) = 1.70 \pm 0.03 \text{ (stat)} \pm 0.04 \text{ (syst)} \pm 0.03 \text{ (norm)} 10^{-4}$$

$$\mathbf{BR}(\mathbf{K}_L^0 \rightarrow \pi^+ \pi^- \pi^0 e^+ e^-, E_{ee} > 20 \text{ MeV}/c^2) = 1.60 \pm 0.18 \text{ (stat)} 10^{-7}$$

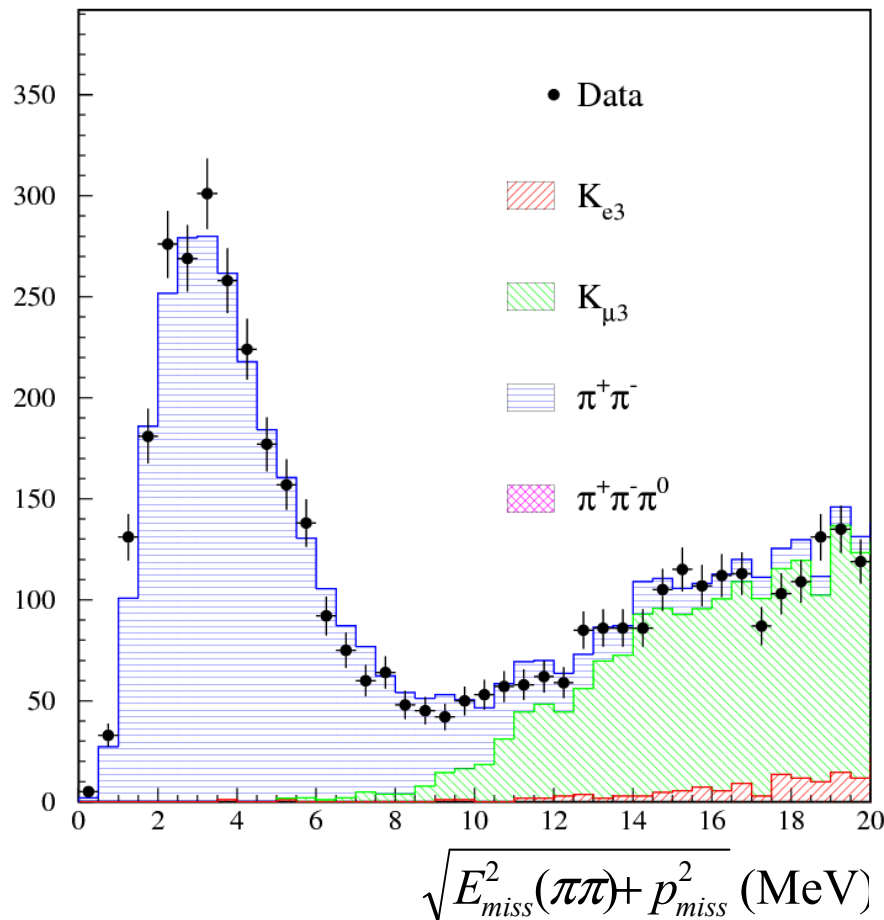


$BR(K_L \rightarrow \pi^+ \pi^- (\gamma_{IB}))$

PID using decay kinematics
 Normalize to $K_L \rightarrow \pi \mu \nu$ events

$$BR = (1.963 \pm 0.012 \pm 0.017) \times 10^{-3}$$

$$\sigma_{rel}: 1.1\% = 0.6\%_{stat} \oplus 0.9\%_{syst}$$



- in agreement with KTeV 2004
 $BR = (1.975 \pm 0.012) \times 10^{-3}$
- it confirms the 4- σ discrepancy with PDG04 = $(2.080 \pm 0.025) \times 10^{-3}$
- we get:

$$|\eta_{+-}| = (2.216 \pm 0.013) \times 10^{-3}$$
 [$BR(K_S \rightarrow \pi\pi)$ and τ_L from KLOE, τ_S from PDG04]

$$PDG04: |\epsilon| = (2.280 \pm 0.013) \times 10^{-3}$$

PLB638 (hep-ex/0603041)

Lepton Universality from $KTeV$

Consistency of BRs and Form Factors results with lepton universality.

Compare Γ 's for K_{e3} and $K_{\mu3}$:

$$\Gamma_{Kl3} = \frac{G_F^2 M_K^5}{192\pi^3} S_{EW} \left(1 + \delta_K^l\right) |V_{us}|^2 |f_+^2(0)| I_K^l$$

$$\left[\frac{\Gamma_{K\mu3}}{\Gamma_{Ke3}} \right]_{PRED} = \left(\frac{1 + \delta_K^\mu}{1 + \delta_K^e} \right) \left(\frac{I_K^\mu}{I_K^e} \right)$$

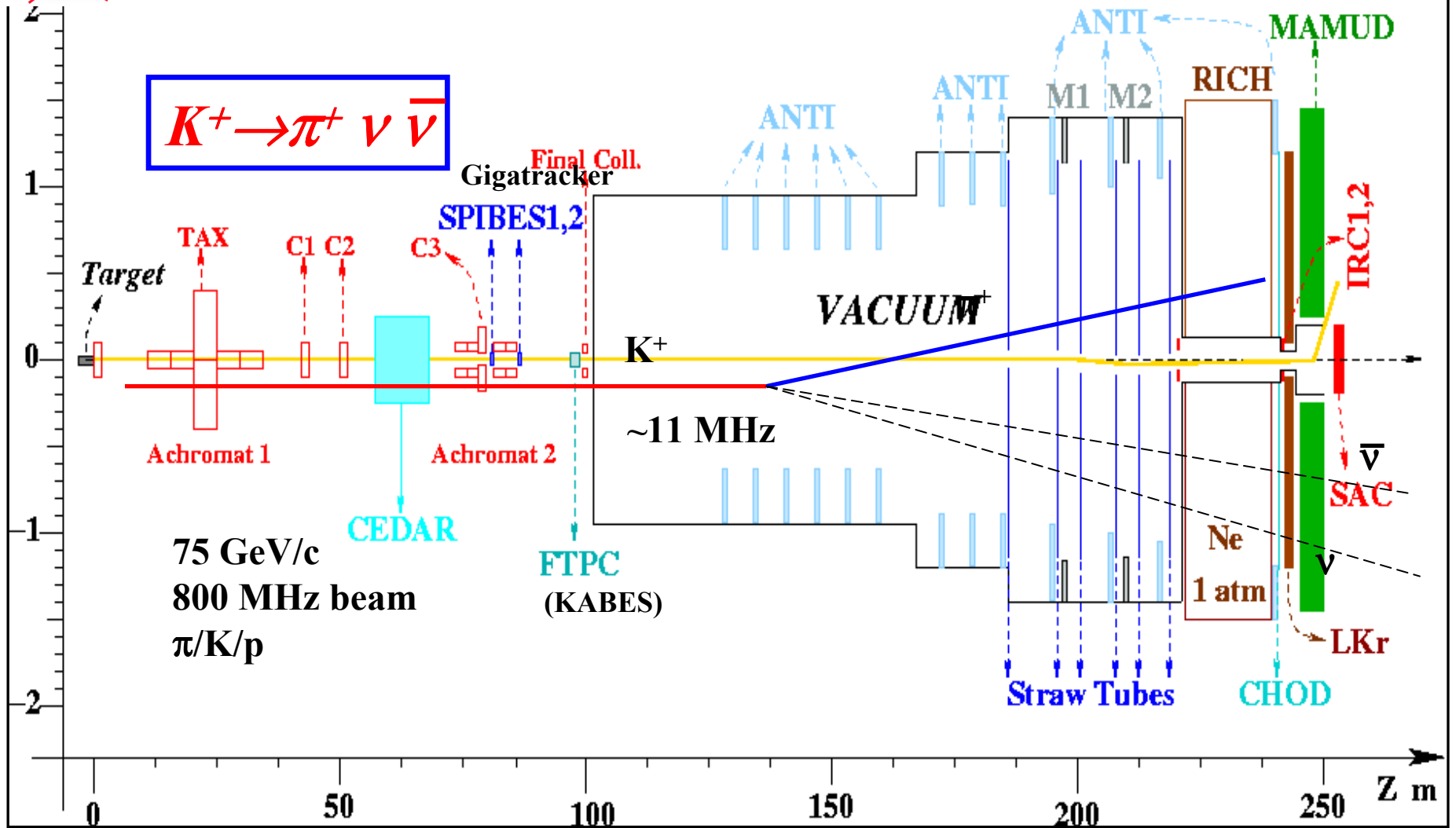
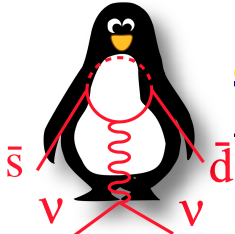
1.0058(10)
from T. Andre

0.6622(18)
from $KTeV$

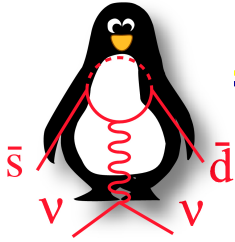
$$\left[\frac{\Gamma_{K\mu3}}{\Gamma_{Ke3}} \right]_{MEAS} / \left[\frac{\Gamma_{K\mu3}}{\Gamma_{Ke3}} \right]_{PRED} = 0.9969 \pm 0.0048 = \left(\frac{G_F^\mu}{G_F^e} \right)$$

Same test with PDG values gives 1.0270 ± 0.0182

P-326 Detector Layout



P326



Signal & bkg from K decays/year*

	Total	Region I	Region II
Signal (SM)	65	16	49
$K^+ \rightarrow \pi^+ \pi^0$	2.7 ± 0.2	1.7 ± 0.2	1.0 ± 0.1
$K_{\mu 2}$	1.2 ± 0.3	1.1 ± 0.3	< 0.1
$K_{e 4}$	2 ± 2	negligible	2 ± 2
$K^+ \rightarrow \pi^+ \pi^+ \pi^-$ and other 3-tracks bkg.	1 ± 1	negligible	1 ± 1
$K_{\pi 2} \gamma$	1.3 ± 0.4	negligible	1.3 ± 0.4
$K_{\mu 2} \gamma$	0.4 ± 0.1	0.2 ± 0.1	0.2 ± 0.1
$K_{e 3}, K_{\mu 3},$ others	negligible	–	–
Total bkg	9 ± 3	3.0 ± 0.2	6 ± 3

*Before taxes. Proposal quotes 40 evt/year @BR=10⁻¹⁰

- SPS used as **LHC injector** (so it will run in the future)
- **No flagrant** time overlap with CNGS
- P-326 **fully compatible** with the rest of CERN fixed target because P-326 needs only ~1/20 of the SPS protons
- Beam time estimates based on **decennial** NA48 experience at SPS