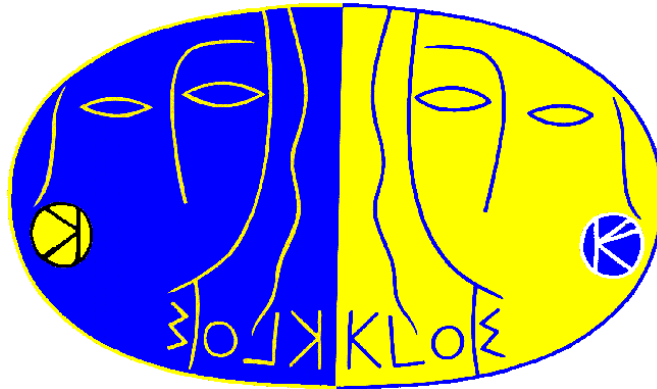


# MEASUREMENT of $e^+e^-$ HADRONIC CROSS SECTION with RADIATIVE RETURN at KLOE



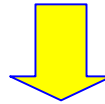
Barva Maura - Università Roma Tre  
On behalf of the KLOE Collaboration  
LNF Spring School - May 2004

# Summary

- ❖ Motivation of  $\sigma_{\text{hadr}}$
- ❖  $\sigma_{\text{hadr}}$  with radiative return
- ❖ Results on  $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  at small angle
- ❖ Conclusions and outlook



# Why the measurement of the cross section is important?



## THE ANOMALOUS MAGNETIC MOMENT OF THE MUON

Magnetic moment  
for pointlike fermion

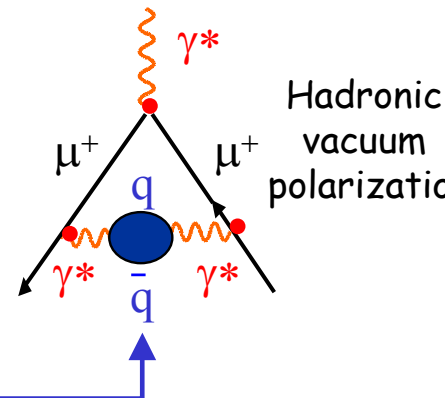
$$\vec{\mu} = g_{\mu} \frac{e}{2m_{\mu}} \vec{s}$$

$$\underbrace{g_{\mu}}_{\text{Dirac}} = 2(1 + a_{\mu})$$

$g \neq 2$  (Dirac prediction) because there are  
quantum correction

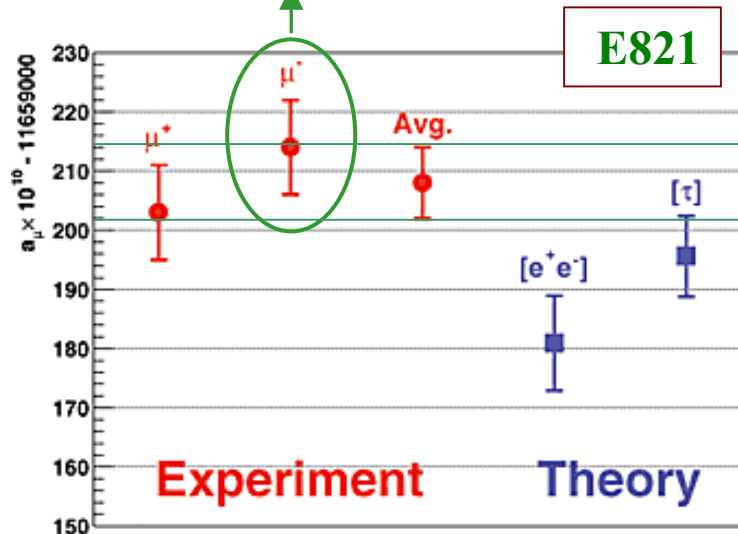


$$a_{\mu}^{SM} = a_{\mu}^{QED} + a_{\mu}^{had} + a_{\mu}^{EW}$$



# Status of $a_\mu$ : Theoretical vs Experimental value

Last result from BNL: 01/04



$\tau$ -data from  
ALEPH, OPAL,  
CLEO  
 $e^+e^-$  dominated  
by CMD-2

$|a_\mu(e^+ e^-) - a_\mu(\text{data})|$ : 2.7  $\sigma$  - Deviation

$|a_\mu(\tau) - a_\mu(\text{data})|$ : 1.4  $\sigma$  - Deviation



**A NEW MEASUREMENT IS VERY IMPORTANT!**



# Hadronic contribution to $a_\mu$

- ❖ The error on  $a_\mu(\text{theo})$  is dominated by the error on  $a_\mu^{\text{had}}$
- ❖ This quantity is **not evaluable in pQCD**, but it can be calculated by  
**DISPERSION INTEGRAL:**

$$a_\mu^{\text{had}} = \frac{\alpha}{3\pi^2} \int_{4m_\pi^2}^{\infty} ds \frac{\mathbf{K}(s)}{s} R(s)$$

$$R(s) = \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

$$\mathbf{K}(s) = \text{KernelFunction} \propto 1/s$$

Input:

- Hadronic electron-positron cross section data
- Hadronic  $\tau$ -decays, which can be used with the help of the CVC-theorem and an isospin rotation (plus isospin breaking corrections)

The factors **1/s** in the dispersion relation makes the low energy region particularly relevant.

The  $e^+e^- \rightarrow \pi^+\pi^-$  channel accounts for ~70% of the contribution both to  $a_\mu^{\text{had}}$



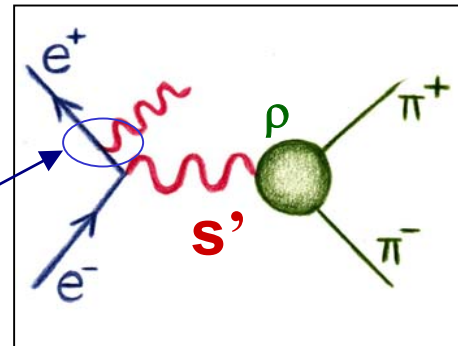
# How to perform this measurement?

traditional way: measuring cross section by varying  $e^\pm$  beams energy  $\rightarrow$  energy scan

BUT

DAΦNE is a  $\phi$  - factory and therefore runs at fixed c.m.s.-energy:  $\sqrt{s} = m_\phi = 1.019 \text{ MeV}$

Complementary approach:  
Take events with  
Initial State Radiation (ISR)



"Radiative Return" to  $\rho$ -resonance:

$$e^+ e^- \rightarrow \rho + \gamma \rightarrow \pi^+ \pi^- + \gamma$$



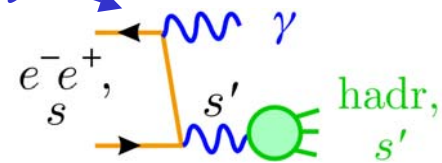
# $\sigma(\text{had})$ through radiative return

The  $\sigma(e^+e^- \rightarrow \pi^+\pi^-\gamma)$  is a function of the 2-Pion invariant mass  $s' = M_{\pi\pi}^2$ . To extract  $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$  with the ISR we

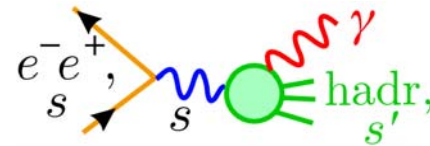
- Need to know the **RADIATOR FUNCTION  $H(s)$**

*$H(s)$  is evaluable  
From MC Phokhara*

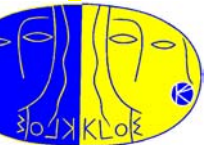
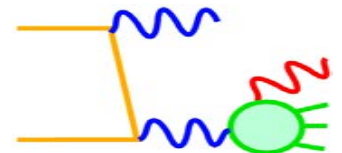
$$M_{\pi\pi}^2 \frac{d\sigma_{\pi\pi\gamma}}{dM_{\pi\pi}^2} = \sigma_{\pi\pi}(s) \cdot H(s)$$



- Have to get rid of "pure" **FSR**:  
which causes events with  $M_{g*} = \sqrt{s}$   
to be assigned to lower  $\sqrt{s'}$  values

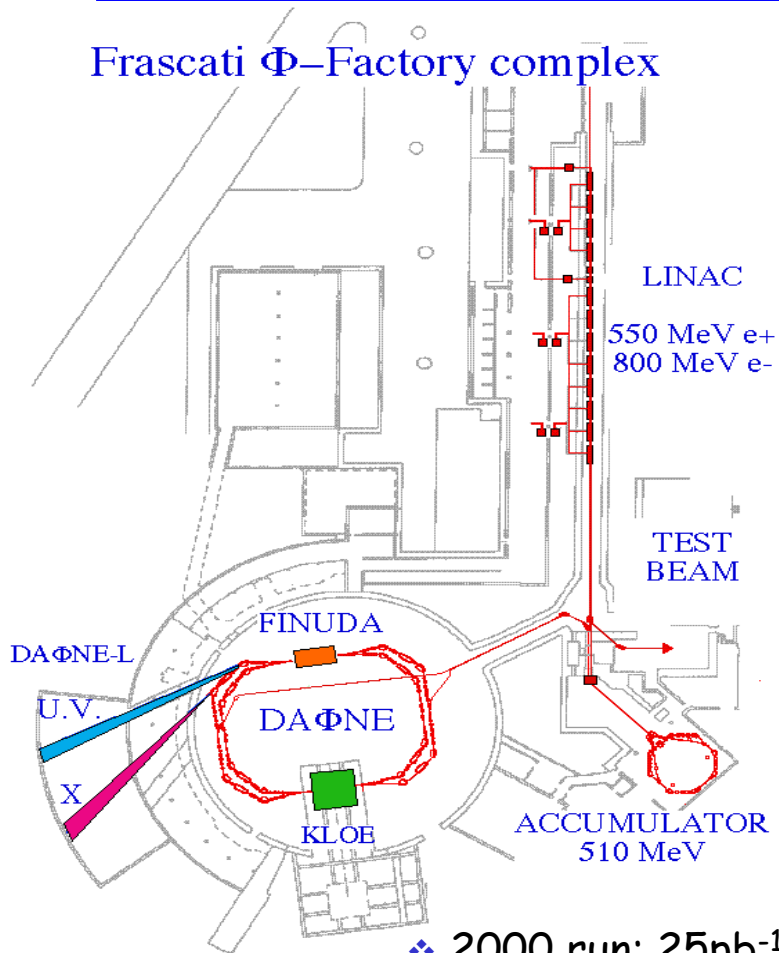


- Have to properly include radiative corrections (including simultaneously emission of ISR and FSR)



# DAΦNE: the Double Annular Φ-factory for Nice Experiments

Frascati Φ-Factory complex



➤  $E_{\text{beams}} \approx 510 \text{ MeV}$

➤ 2 separate rings for  $e^+e^-$  to minimize beam-beam interaction

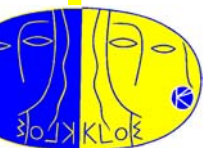
➤ two interaction region: KLOE-DEAR/FINUDA

➤ crossing angle:  $12.5 \text{ mrad}$  ( $p_x(\phi) \approx 13 \text{ MeV}$ )

<i>DAΦNE Parameters</i>	<i>Design</i>
<i>N of bunches</i>	<i>120+120</i>
<i>Lifetime (mins)</i>	<i>120</i>
<i>Bunch current (mA)</i>	<i>40</i>
<i>L<sub>bunch</sub> (cm<sup>-2</sup>s<sup>-1</sup>)</i>	<i><math>4.4 \times 10^{30}</math></i>
<i>L<sub>peak</sub> (cm<sup>-2</sup>s<sup>-1</sup>)</i>	<i><math>5.3 \times 10^{32}</math></i>

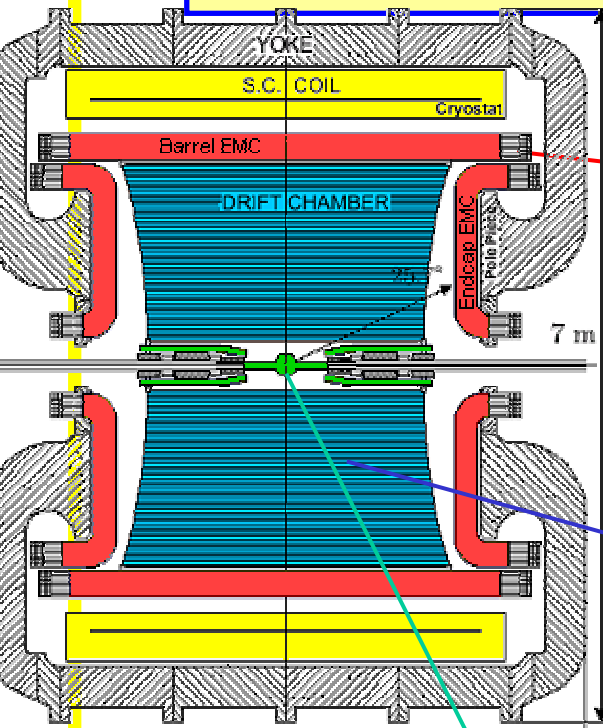
DAΦNE performance:

- ❖ 2000 run:  $25 \text{ pb}^{-1}$ ,  $7.5 \times 10^7 \phi$  decay → first published results
- ❖ 2001 run:  $190 \text{ pb}^{-1}$ ,  $5.7 \times 10^8 \phi$  decay } Analysis in progress
- ❖ 2002 run:  $300 \text{ pb}^{-1}$ ,  $9.0 \times 10^8 \phi$  decay



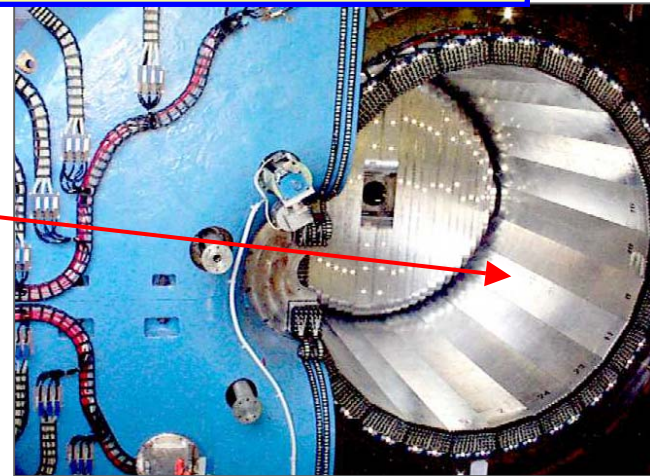


# The KLOE detector: K Long Experiment



## Electromagnetic calorimeter

- lead/scintillating fibers (1 mm  $\varnothing$ ),  $15 X_0$
- 4880 PMT's
- 98% solid angle coverage

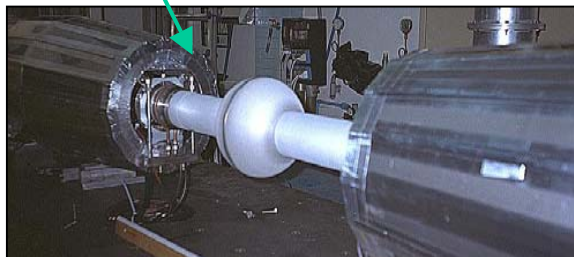


## Drift chamber (4 m $\varnothing \times 3.75$ m, CF frame)

- Gas mixture:  
90% He + 10%  $C_4H_{10}$
- 12582 stereo-stereo sense wires
- almost squared cells



- Beam pipe :  
(spherical, 10 cm  $\varnothing$ , 0.5 mm thick)
- Instrumented permanent magnet quadrupoles  
(32 PMT's)



# Measurement of $\sigma_{\pi\pi\gamma}$ - Analysis scheme

Pion tracks at large angles  
from a vertex close to IP

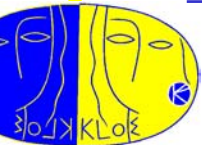
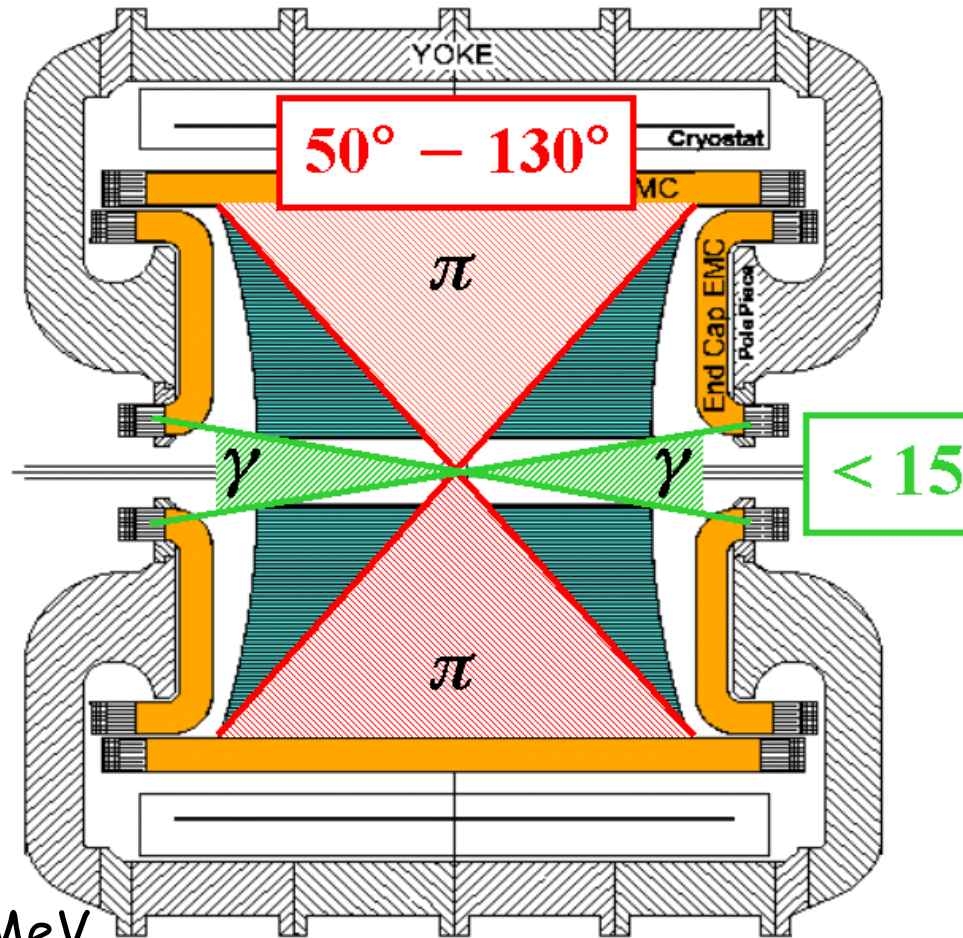
Photons at small angles  
to enhance ISR:  
 $d\sigma_{\text{ISR}}/d\Omega \sim 1/\sin^2\theta$



☺ relative contribution of  
"pure" FSR below the % level  
over entire  $M_{\pi\pi}$  spectrum

☺ reduce background

☹ Lose events with  $M_{\pi\pi} < 600$  MeV



# Summary of syst. errors and background

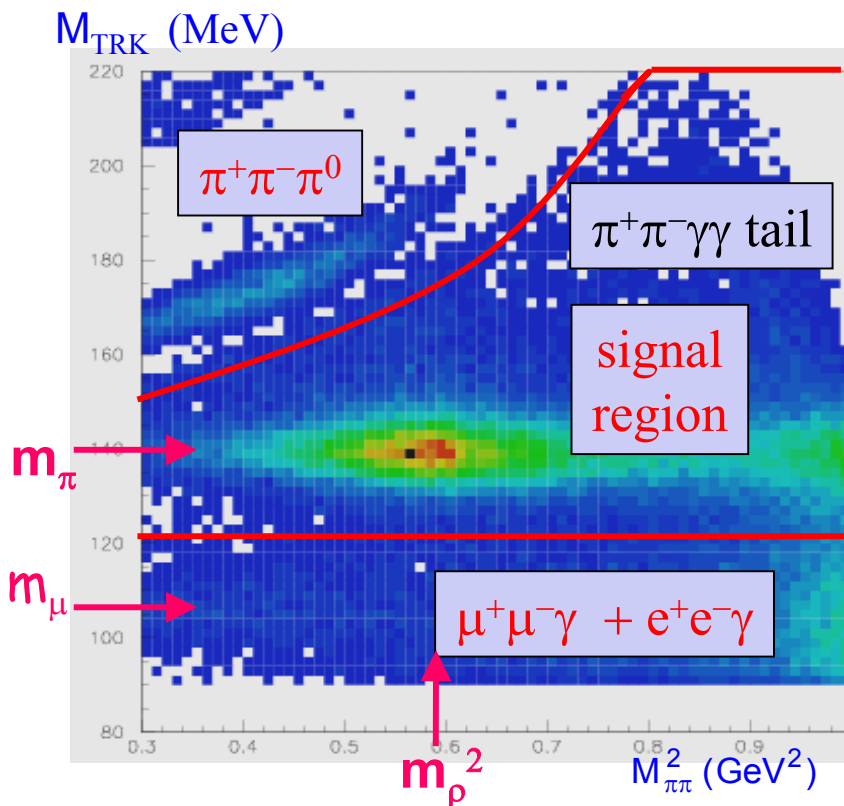
Acceptance	0.3%
Trigger	0.3%
FILFO	0.6%
Tracking	0.3%
Vertex	0.3%
Likelihood	0.1%
Track mass	0.2%
Backg.	
Subtraction	0.5%
Unfolding	0.3%
<b>Total exp</b>	<b>1.0%</b>

Luminosity	0.6%
Vacuum	
Polarization	0.2%
FSR	0.3%
Radiator function	0.5%
<b>Total theory</b>	<b>0.9%</b>

1. Rad. Bhabhas: Pion-Electron-Separation by means of a Particle-ID algorithm

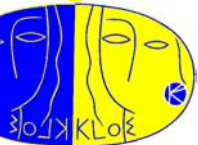
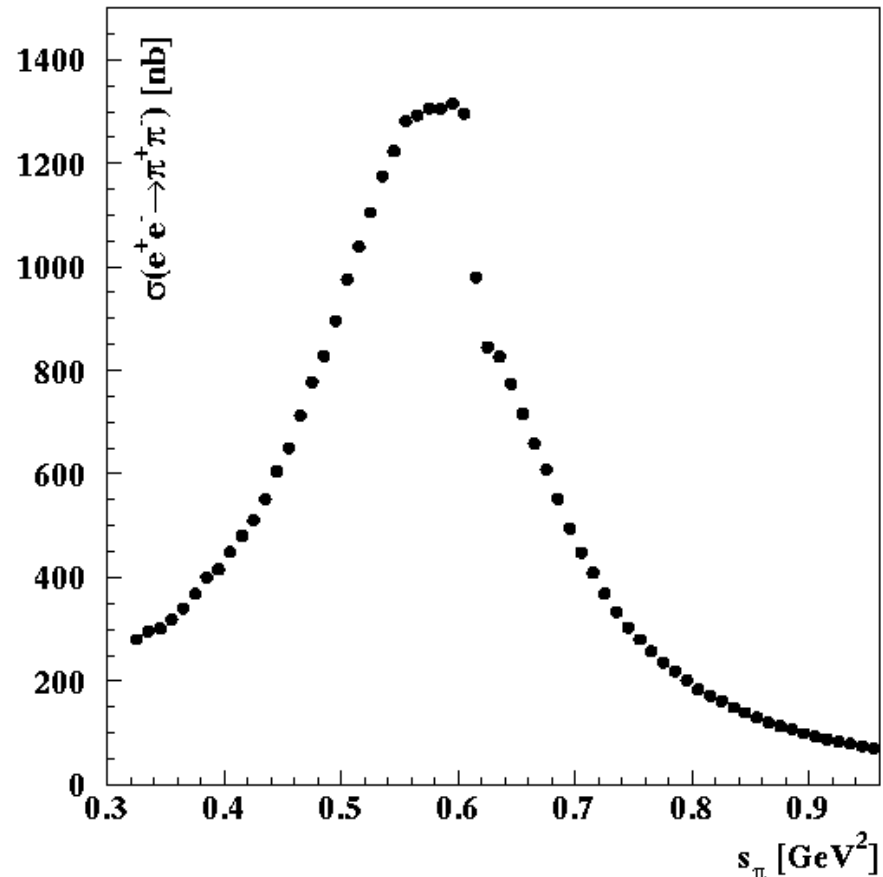
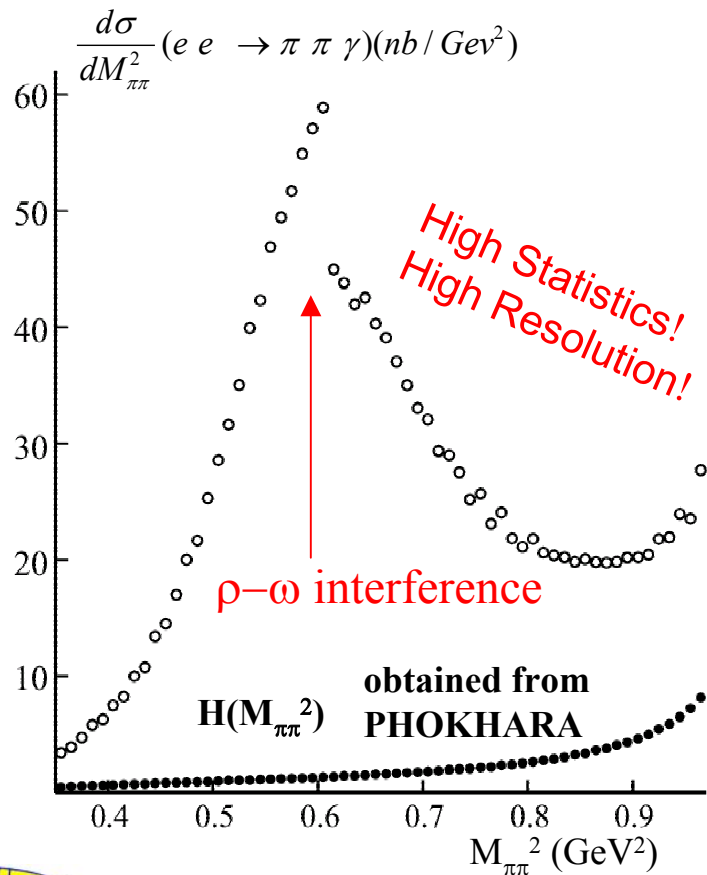
2.  $\phi \rightarrow \pi^+ \pi^- \pi^0$  Kinematic Separation: "Trackmass"

$$e^+e^- \rightarrow \mu^+ \mu^- \gamma: \left( M_\phi - \sqrt{\vec{p}_1^2 + M_{trk}^2} - \sqrt{\vec{p}_2^2 + M_{trk}^2} \right)^2 - (\vec{p}_1 + \vec{p}_2)^2 = q_\gamma^2 = 0$$



# Analysis: $\sigma(e^+e^- \rightarrow \pi^+\pi^-\gamma)$

**Statistics:**  $141\text{pb}^{-1}$  of 2001-Data 1.5 Million Events



# Analysis: Pion Form Factor and $a_\mu^{\text{had}}$

❖ We have evaluated the **dispersions integrals for the 2-Pion-Channel** in the energy range  $0.35 < M_{\pi\pi}^2 < 0.95 \text{ GeV}^2$

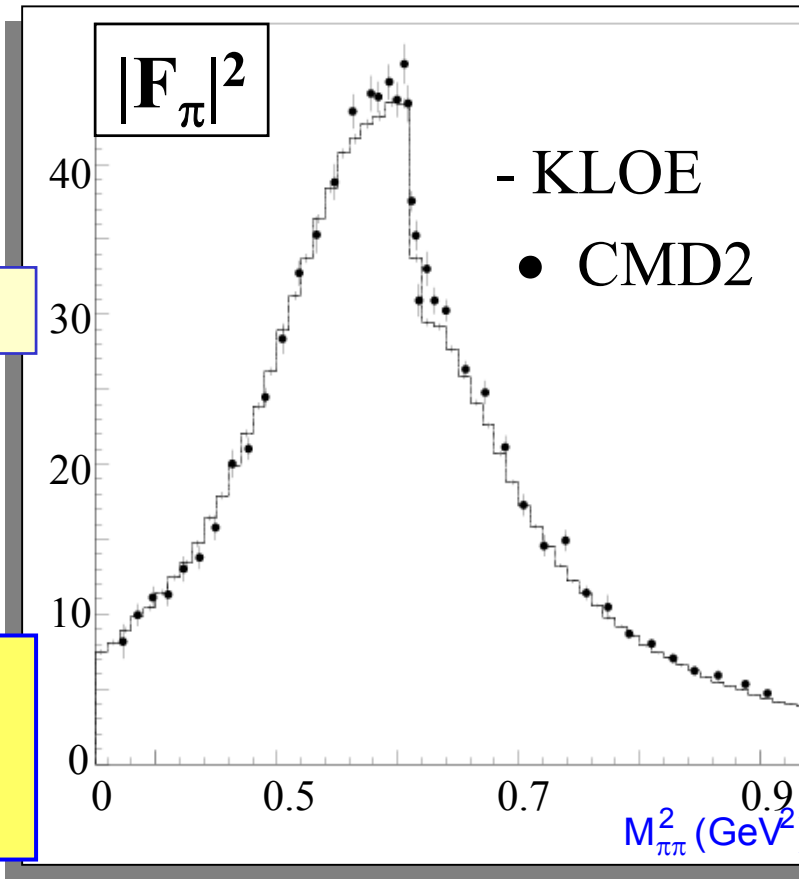
$$a_\mu^{\pi\pi} = (389.2 \pm 0.8_{\text{stat}} \pm 3.9_{\text{syst}} \pm 3.5_{\text{theo}}) 10^{-10}$$

❖ **Comparison with CMD-2** in energy range  $0.37 < M_{\pi\pi}^2 < 0.93 \text{ GeV}^2$

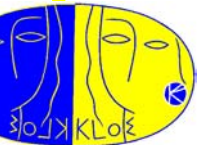
$$\text{KLOE} \quad (376.5 \pm 0.8_{\text{stat}} \pm 5.1_{\text{syst+theo}}) 10^{-10}$$

$$\text{CMD2} \quad (378.6 \pm 2.7_{\text{stat}} \pm 2.3_{\text{syst+theo}}) 10^{-10}$$

The results are in good agreement!



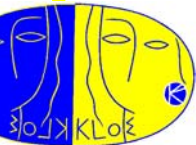
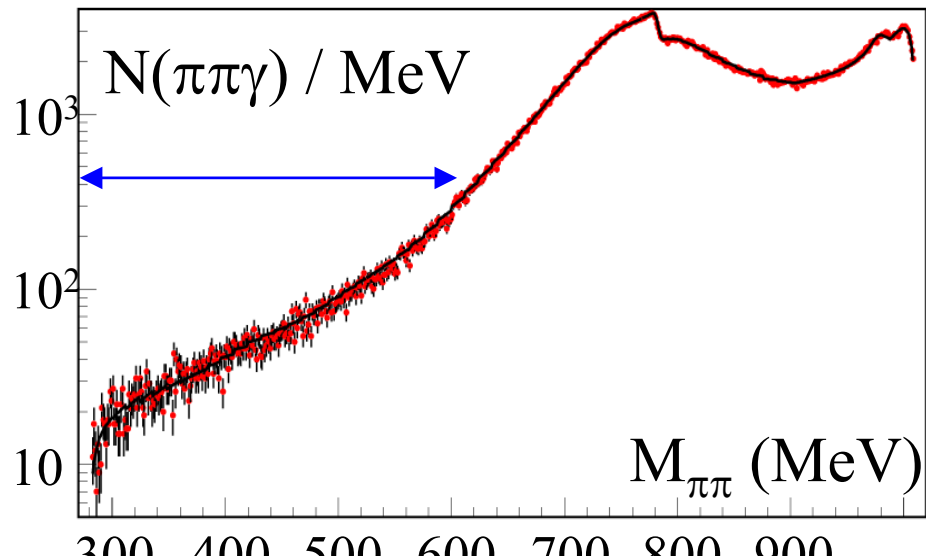
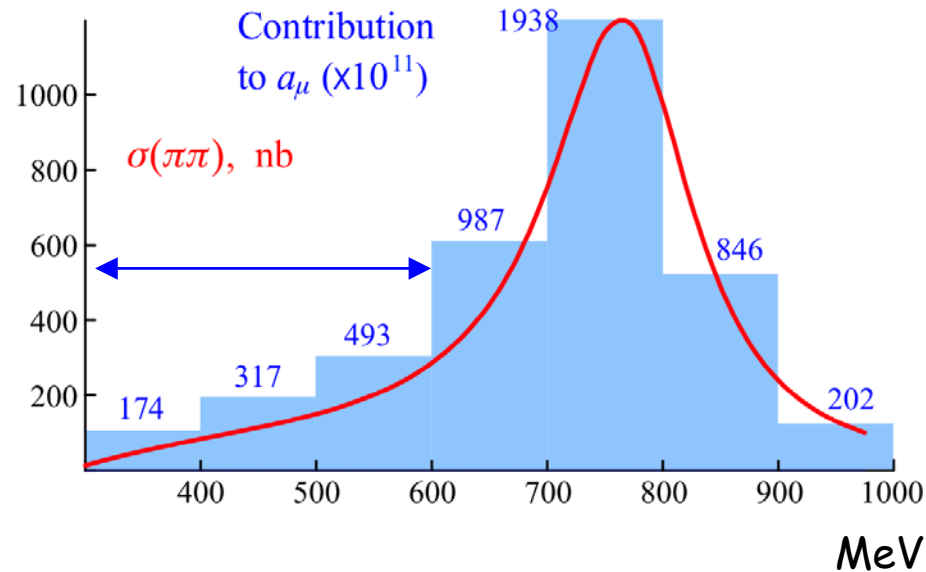
$$\sigma(e^+e^- \rightarrow \pi^+\pi^-) = \frac{\pi\alpha^2}{3M_{\pi\pi}^2} \beta^3 |F_\pi(M_{\pi\pi}^2)|^2$$





# (1) $a_\mu^{\text{had}}$ prospect: Large Angle analysis

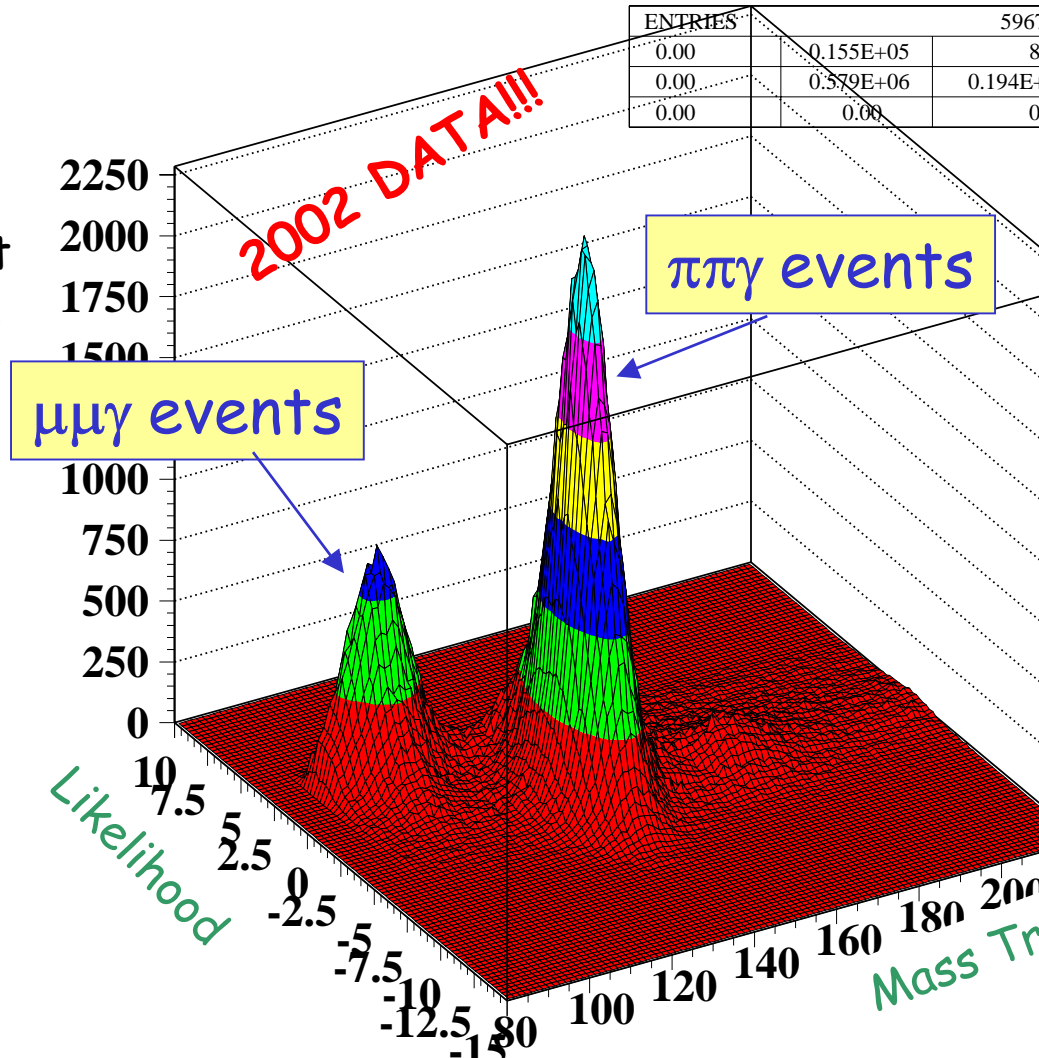
- ✓ The energy region close to threshold,  $M_{\pi\pi} < 600 \text{ MeV}$ , is excluded by our selection cuts
- ✓ This region contributes **~20%** to  $a_\mu^{\text{had}}$
- ✓ We use events at large photon angles to access lower  $M_{\pi\pi}^2$  region. (Photon tagging will be possible in this case)
- ✓ Check **FSR parametrization** (by looking to charge asymmetry)
- ✓ *This analysis is going on...*



## (2) $a_{\mu}^{\text{had}}$ prospect: the direct measurement of $R_{\gamma}$

$$R_{\gamma} = \frac{e^{+}e^{-} \rightarrow \pi^{+}\pi^{-}\gamma}{e^{+}e^{-} \rightarrow \mu^{+}\mu^{-}\gamma}$$

- ✓ We are also studying a direct measurement of  $R$
- ✓ This method is independent from the luminosity estimate
- ✓ We are working on obtaining particle ID combining calorimetric and kinematically variables



# Conclusion:

## Summary:

- ❖ We have presented the first precise measurement of hadronic cross section using radiative return at KLOE
- ❖ Our result is in agreement with CMD2, therefore confirming the existing discrepancy between SM and BNL result on  $(g-2)_\mu$

## Ongoing activities

- ❖ Large angle photon analysis: to study the low  $M_{\pi\pi}^2$  region and measure the asymmetry to check the FSR results
- ❖ The direct measurement of  $R = \sigma(e^+e^- \rightarrow \pi^+\pi^-\gamma) / \sigma(e^+e^- \rightarrow \mu^+\mu^-\gamma)$

