Gluonium content of the η '

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There is the possibility that a pseudoscalar glue ball mixs with a $q\bar{q}$ pair in the η' meson

$$|\eta^{\,\prime}\,
angle = X_{\eta^{\,\prime}} |q\, ar{q}\,
angle + Y_{\eta^{\,\prime}} |s\, ar{s}\,
angle + Z_{\eta^{\,\prime}} G
angle \log \phi_P |q\, ar{q}\,
angle - \sin \phi_P |s\, ar{s}\,
angle = \frac{|uar{u}\,
angle + |dar{d}\,
angle}{\sqrt{2}}$$

If SU(3) were not broken $\phi_p = 45^\circ$

$$X_{\eta'} = \sin\phi_P \cos\phi_G$$

$$Y_{\eta'} = \cos\phi_P \cos\phi_G$$

$$Z_{\eta'} = \sin\phi_G$$

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angle = \frac{|uar{u}
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 $|\eta
angle = \cos\phi_P|q\,ar{q}
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angle}{\sqrt{2}}$

If SU(3) were not broken
$$\phi_p = 45^\circ$$

$$X_{\eta} = \sin \phi_P \cos \phi_G$$

 $Y_{\eta'} = \cos \phi_P \cos \phi_G$
 $Z_{\eta'} = \sin \phi_G$

Pseudoscalar glue balls are predicted by QCD driven models and Lattice

First 3σ hint of η' gluonium content by KLOE

Phys. Lett. B648 (2007) 267

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Good impact on the physics community

11 genuine citations in few months

Very recently, the KLOE Collaboration has reported a new measurement of the ratio $R_{\phi} \equiv B(\phi \to \eta' \gamma)/B(\phi \to \eta \gamma)$ [1]. Combining the value of R_{ϕ} with other constraints, they have estimated the gluonium content of the η' meson as $Z_{\eta'}^2 = 0.14 \pm 0.04$, which points to a significant gluonium fraction in the η' wave function incompatible with zero by more than 3σ . This new result contrasts with the former value $Z_{\eta'}^2 = 0.06_{-0.06}^{+0.09}$, which was compatible with zero within 1σ and consistent with a gluonium fraction below 15% [2].

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Fully compatible within errors!!!

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small amount of gluonium in the η' wave function, in fact compatible with zero within 1σ . Using Eq. (A.6) to calculate $Z_{\eta'}$ from $\phi_{\eta'G}$ gives $|Z_{\eta'}| = 0.2 \pm 0.2$. This is one of the main results of our analysis. Accepting the absence of gluonium for the η meson, the gluonic

content of the η' wave function amounts to $|\phi_{\eta'G}| = (12 \pm 13)^{\circ}$ or $Z_{\eta'}^2 = 0.04 \pm 0.09$.

In other words, our values for ϕ_P and $\phi_{\eta'G}$ (or $Z_{\eta'}$) contrast with those reported by KLOE recently, $\phi_P = (39.7 \pm 0.7)^\circ$ and $|\phi_{\eta'G}| = (22 \pm 3)^\circ$ —or $Z_{\eta'}^2 = 0.14 \pm 0.04$ —[1]. As

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Again problems with comparison within errors

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To understand the objection we need more details.

In order to fit the gluonium we use our measurement of

$$R_{\phi} = \frac{Br(\phi \to \eta' \gamma)}{Br(\phi \to \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\overline{m}} \frac{C_{NS}}{C_S} \cdot \tan \frac{\phi_V}{\sin 2\phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_{\eta}} \right)^3$$

Together with

$$\frac{\Gamma(\eta' \to \gamma \gamma)}{\Gamma(\pi^0 \to \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_{\pi}} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$$

$$\frac{\Gamma(\eta' \to \rho \gamma)}{\Gamma(\omega \to \pi^0 \gamma)} = \frac{C_{NS}}{\cos \phi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_{\rho}^2 m_{\omega}}{m_{\omega}^2 - m_{\pi}^2 m_{\eta'}} \right)^3 X_{\eta'}^2$$

$$\frac{\Gamma(\eta' \to \omega \gamma)}{\Gamma(\omega \to \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_{\omega}^2 m_{\omega}}{m_{\omega}^2 - m_{\pi}^2 m_{\eta'}} \right)^3 \left[C_{NS} X_{\eta'} + 2 \frac{m_s}{\overline{m}} C_s \cdot \tan \phi_V \cdot Y_{\eta'} \right]^2$$

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These parameters multiply the gluonium component

We took them from a fit to the same quantities + further constraints without assuming gluonium content

Because of the discussion we decided to check all the procedure from the beginning Because of the discussion we decided to check all the procedure from the beginning



Redo the fit using different tools and different fitter (myself) in order to check for material errors.

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Redo the Escribano fit in order to check it (Camilla).

The MINUIT fit

(The original fit was made with excel)

The MINUIT fit

(The original fit was made with excel)

Fit result

FCN= 1.420049 FROM MIGRAD STATUS=CONVERGED 30 CALLS 31 TOTAL EDM= 0.46E-08 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT PARAMETER STEP FIRST

NO. NAME VALUE ERROR SIZE DERIVATIVE

1 z2 0.14239 0.33030E-01 0.22096E-04 0.32092E-02

2 PHIP 39.685 0.72252 0.48340E-03 0.10265E-03

EXTERNAL ERROR MATRIX. NDIM= 50 NPAR= 2 ERR DEF= 1.00

0.109E-02-0.113E-01

-0.113E-01 0.522E+00

PARAMETER CORRELATION COEFFICIENTS

NO. GLOBAL 1 2

1 0.47489 1.000-0.475

2 0.47489 -0.475 1.000

	This fit	Paper
Z ²	0.14±0.03	0.14±0.04
ϕ_p	$(39.7 \pm 0.7)^{\circ}$	$(39.7 \pm 0.7)^{\circ}$

The MINUIT fit

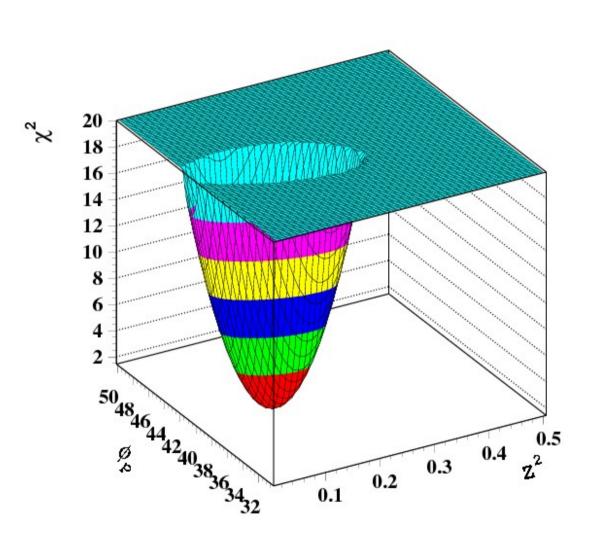
(The original fit was made with excel)

Fit result

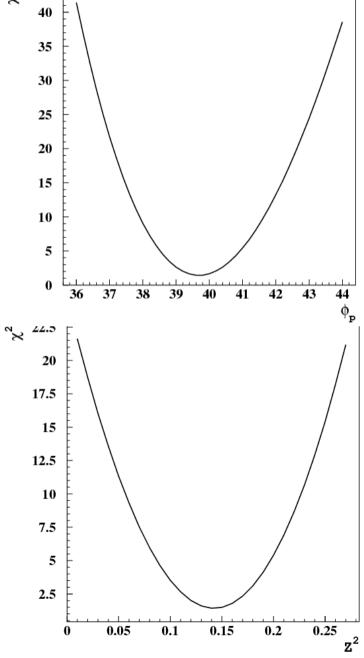
Central value in perfect agreement Error even smaller Gluonium at 4.7σ

	This fit	Paper
Z ²	0.14±0.03	0.14±0.04
$oldsymbol{\phi}_{\mathrm{p}}$	$(39.7 \pm 0.7)^{\circ}$	$(39.7 \pm 0.7)^{\circ}$

Check of the χ^2 behaviour



Only one minimum in the whole parameters' domain.



Check of the Escribano hypothesis

Fit redone using Escribano fit parameters:

$$C_{NS} = 0.86 \pm 0.03 C_{S} = 0.78 \pm 0.05$$

	Fit	Paper	
Z ²	0.12±0.03	0.14 ± 0.04	
ϕ_{p}	$(40.0 \pm 0.7)^{\circ}$	$(39.7 \pm 0.7)^{\circ}$	

The fit is very stable respect to the overlapping parameters

Our fit Escribano

Our fit

Escribano

Only ϕ_{D} and Z^{2} are left free

All theoretical parameters are left free

Our fit

Only ϕ_p and Z^2 are left free

The ratios of Γ 's are used in the fit.

Escribano

All theoretical parameters are left free

The Γ 's are used in the fit.

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4 measured quantities are used in the fit

11 measured quantities are used in the fit

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DATA from PDG '06 + KLOE R_o '07

DATA from PDG '06

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_{\eta} \cos\phi_V + 2\frac{\bar{m}}{m_s} z_s Y_{\eta} \sin\phi_V \right) ,$$

$$g_{\omega\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \cos\phi_V + 2\frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin\phi_V \right) ,$$

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$$z_q = C_{NS}$$

 $z_s = C_s$

Constrain ϕ_p, Z_G

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$$Z_q = C_{NS}$$

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Constrain
 ϕ_p, Z_G

$$\begin{split} g_{\rho^0\pi^0\gamma} &= g_{\rho^+\pi^+\gamma} = \tfrac{1}{3}g \ , \quad g_{\omega\pi\gamma} = g\cos\phi_V \ , \quad g_{\phi\pi\gamma} = g\sin\phi_V \ , \\ g_{K^{*0}K^0\gamma} &= -\tfrac{1}{3}g \, z_K \left(1 + \tfrac{\bar{m}}{m_s}\right) \ , \quad g_{K^{*+}K^+\gamma} = \tfrac{1}{3}g \, z_K \left(2 - \tfrac{\bar{m}}{m_s}\right) \ , \end{split}$$

Fix the parameters $m_s/\overline{m}_i \phi_v$, g

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_{\eta} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta} \sin \phi_V \right) , \quad z_q = C_{NS}$$

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$$z_q = C_{NS}$$

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$$\tan \phi_{V} << 1 \ (\phi_{V} = 3.2^{\circ})$$

$$R_{\phi} = \frac{Br(\phi \to \eta' \gamma)}{Br(\phi \to \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\overline{m}} \frac{C_{NS}}{C_S} \cdot \tan \frac{\phi_V}{\sin 2\phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_{\eta}} \right)^3$$

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_{\eta} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta} \sin \phi_V \right) , \quad Z_{\mathsf{q}} = \mathsf{C}_{\mathsf{NS}} z_s = \mathsf{C}_{\mathsf{s}}$$

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Contains terms up to $tan^2 \phi_v$, but it is not o($tan^2 \phi_v$)

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KLOE fit with full formula

$$R_{\phi} = \frac{Br(\phi \to \eta' \gamma)}{Br(\phi \to \eta \gamma)} = \cot^{2}\phi_{P} \cdot \cos^{2}\phi_{G} \left(1 - \frac{m_{S}}{\overline{m}} \frac{C_{NS}}{C_{S}} \cdot \tan \frac{\phi_{V}}{\sin 2\phi_{P}}\right)^{2} \cdot \left(\frac{p_{\eta'}}{p_{\eta}}\right)^{3} + \left(\frac{C_{NS}}{C_{S}} \frac{m_{S}}{\overline{m}} \tan \phi_{V}\right)^{2} \left(1 + 2\cos^{2}\phi_{P}\right)$$

Fit Paper
$$z^2$$
 0.14±0.03 0.14±0.04 ϕ_p (39.9 ± 0.7)° (39.7 ± 0.7)°

Freeing the overlapping parameters

$$\frac{\Gamma(\eta' \to \gamma \gamma)}{\Gamma(\pi^0 \to \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_{\pi}} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$$

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Not enough constraints to leave free $C_{\rm NS}$ and $C_{\rm S}$

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Not enough constraint to leave free C_{NS} and C_{S}

We add to the fit:

$$\frac{\Gamma(\omega \to \eta \gamma)}{\Gamma(\omega \to \pi^0 \gamma)}, \frac{\Gamma(\rho \to \eta \gamma)}{\Gamma(\omega \to \pi^0 \gamma)}, \frac{\Gamma(\phi \to \eta \gamma)}{\Gamma(\omega \to \pi^0 \gamma)}$$

Fit result

FCN= 1.406759 FROM MINOS STATUS=SUCCESSFUL 187 CALLS 277 TOTAL

EDM= 0.34E-06 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT PARAMETER			PARABOLIC MINOS ERRORS
NO.	NAME	E VALUE	ERROR NEGATIVE POSITIVE
1	z2	0.11720	0.41464E-01 -0.41484E-01 0.41463E-01
2	PHIP	40.056	0.97108 -0.94271 1.0031
3	CNSP	0.86965	0.31043E-01 -0.31096E-01 0.31044E-01
4	CSPA	0.79071	0.47577E-01 -0.44712E-01 0.50965E-01

Fit with free C _{NS} C _S	Paper	Escribano
z ² 0.12±0.04	0.14 ± 0.04	$(0.04 \pm 0.09)^{\circ}$
$\phi_{\rm p}$ (40.1 ± 1.0)°	$(39.7 \pm 0.7)^{\circ}$	$(41.4 \pm 1.3)^{\circ}$
$C_{NS} = 0.87 \pm 0.03$		0.86 ± 0.03
$C_{\rm s} = 0.79 \pm 0.05$		0.78 ± 0.05

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EXT PARAMETER		PARABOL	IC MINO	OS ERRORS	
NO.	NAME	E VALUE	ERROR	NEGATIVE	POSITIVE
1	z 2	0.11720	0.41464E-01 -0	0.41484E-01	0.41463E-01
2	PHIP	40.056	0.97108 -0	.94271 1	.0031
3	CNSP	0.86965	0.31043E-01	0.31096E-	01 0.31044E-01
4	CSPA	0.79071	0.47577E-01	-0.44712E-0	01 0.50965E-01

Fit with free C _{NS} C _S	Paper	Escribano
z ² 0.12±0.04	0.14 ± 0.04	$(0.04 \pm 0.09)^{\circ}$
$\phi_{\rm p} (40.1 \pm 1.0)^{\circ}$	$(39.7 \pm 0.7)^{\circ}$	$(41.4 \pm 1.3)^{\circ}$
$C_{NS} = 0.87 \pm 0.03$		0.86 ± 0.03
$C_{\rm s} = 0.79 \pm 0.05$	Perfect agreement	0.78 ± 0.05

Fit results

Gluonium still at 30

Fit with free C_{NS} C_S

 Z^2 0.12±0.04

 $\phi_{\rm p} = (40.1 \pm 1.0)^{\circ}$

 $C_{NS} = 0.87 \pm 0.03$

 $C_s = 0.79 \pm 0.05$

Paper

 0.14 ± 0.04

 $(39.7 \pm 0.7)^{\circ}$

Perfect agreement

Escribano

 $(0.04 \pm 0.09)^{\circ}$

 $(41.4 \pm 1.3)^{\circ}$

 0.86 ± 0.03

 0.78 ± 0.05

Fit results



Fit w

12±0.04

 $(40.1 \pm 1.0)^{\circ}$

 0.87 ± 0.03

 0.79 ± 0.05

 0.14 ± 0.04

 $(39.7 \pm 0.7)^{\circ}$

Perfect agreement

Escribano

 $(0.04 \pm 0.09)^{\circ}$

 $(41.4 \pm 1.3)^{\circ}$

 0.86 ± 0.03

 0.78 ± 0.05

The $\eta' \rightarrow \gamma \gamma / \pi^0 \rightarrow \gamma \gamma$ constraint

Removing this constraint we obtain:

Fit	with fre	ee C _{NS} C _S
no	$P \rightarrow \gamma \gamma c$	constraint

$$z^2$$
 0.09±0.06

$$\phi_{\rm n} = (40.2 \pm 1.0)^{\circ}$$

$$C_{NS} = 0.86 \pm 0.03$$

$$C_{s} = 0.79 \pm 0.05$$

Fit with free C_{NS} C_S

$$z^2$$
 0.12±0.04

$$\phi_{\rm p} (40.1 \pm 1.0)^{\circ}$$

$$C_{NS} = 0.87 \pm 0.03$$

$$C_{\rm s} = 0.79 \pm 0.05$$

Escribano

$$(0.04 \pm 0.09)^{\circ}$$

$$(41.4 \pm 1.3)^{\circ}$$

$$0.86 \pm 0.03$$

$$0.78 \pm 0.05$$

The $\eta' \rightarrow \gamma \gamma / \pi^0 \rightarrow \gamma \gamma$ constraint

Removing this constraint we obtain:

Fit with free $C_{NS} C_{S}$ no $P \rightarrow \gamma \gamma$ constraint		Fit with free C _{NS} C _S		Escribano
${\bf Z}^2$	0.09±0.06	\mathbf{Z}^2	0.12 ± 0.04	$(0.04 \pm 0.09)^{\circ}$
ϕ_{p}	$(40.2 \pm 1.0)^{\circ}$	ϕ_{p}	$(40.1 \pm 1.0)^{\circ}$	$(41.4 \pm 1.3)^{\circ}$
$\mathbf{C}_{ ext{NS}}$	0.86 ± 0.03	C_{NS}	0.87 ± 0.03	0.86 ± 0.03
C_{s}	0.79 ± 0.05	$\mathbf{C}_{\mathbf{c}}$	0.79 ± 0.05	0.78 ± 0.05

The $P \rightarrow \gamma \gamma$ constraint is important!! It moves the central value and reduce the error (Here someone is cheating..)

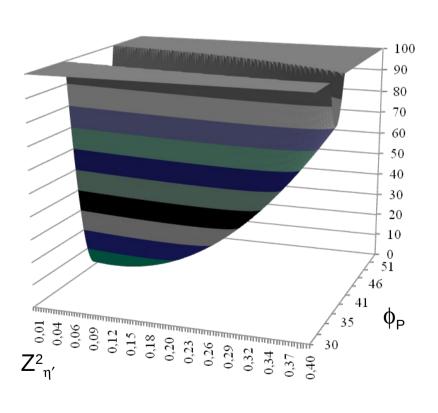
Slide from Camilla

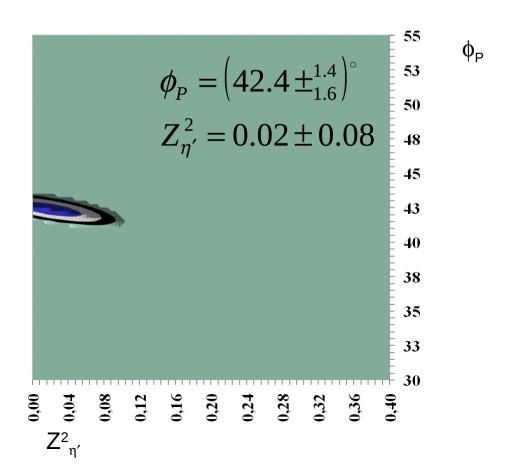
Fitting the Width (using KLOE and last SND results)

We fit as Escribano - constraints from partial width with our method - only $cos\phi_P$, $cos\phi_G$ left free We find the following results to compare with Rafel's ones

Escribano fit

$$\left(\phi_{P}, Z_{\eta'}^{2}\right) = \left(42.6^{\circ}, 0.01\right)$$





Conclusions and outlook

- All the objections to our paper have been rejected by the check performed;
- To complete the study we have to implement 4 further constraints and fit with all free parameters;
- From the preliminary study we can say:
 - The gluonium is at 3σ whatever we use for the overlapping parameters or include them in the fit;
 - The P $\rightarrow \gamma \gamma$ is proved to be an important constraint: increases the gluonium component and reduces the error by 33%
 - The fit to the Γ 's looks promising
- We would like to write a short answer to Escribano and Thomas at the end of the work.