

Latest news and perspectives on the $\phi \rightarrow f_0(980)\gamma$ analysis

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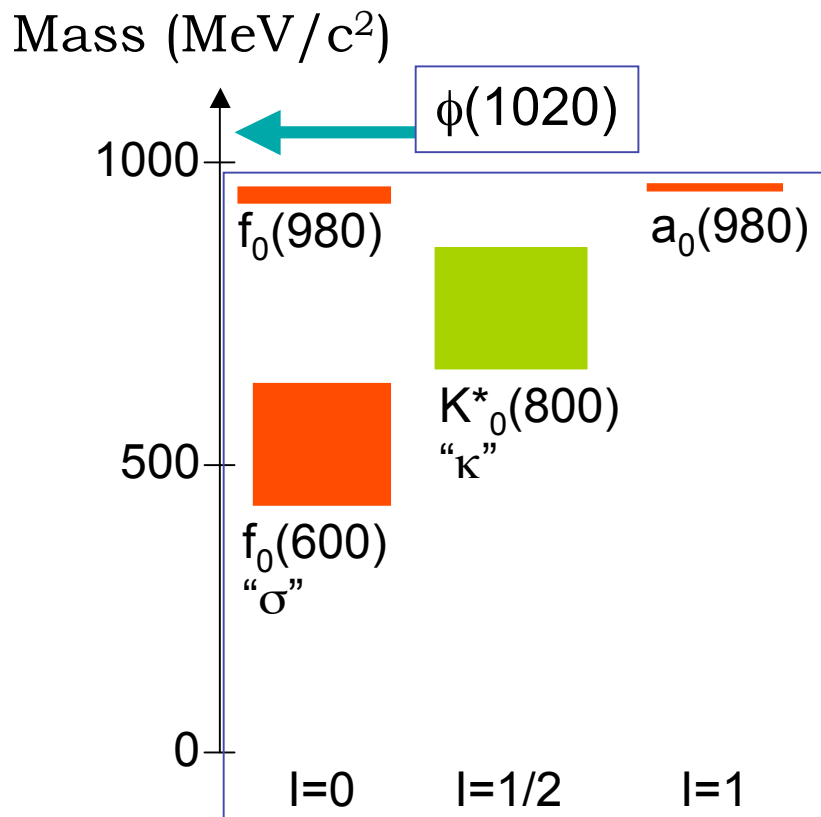
For the scalar phidec wg

- **Short report on $\pi^+\pi^-\gamma$ final results**
- **perspectives on $\pi^+\pi^-\gamma$ final state**
- **situation of the $\pi^0\pi^0\gamma$ final state:**
 - **fits to the \sqrt{s} -dependence of cross sections**
 - **status of KLOE memos ...**
 - **latest results on the Dalitz-plot fit**

KLOE General Meeting
LNF 14-dec-2005

Scalar Mesons at a ϕ - factory

How a ϕ -factory can contribute to the understanding of the scalar mesons



Scalar Mesons Spectroscopy:
 $f_0(980)$, $f_0(600)$ and $a_0(980)$
are accessible (κ not accessible)
through $\phi \rightarrow S\gamma$;

Questions:

1. Is $f_0(600)$ needed to describe the mass spectra ?
2. "couplings" of $f_0(980)$ and $a_0(980)$ to $\phi \cong |ss\rangle$ and to KK , $\pi\pi$ and $\eta\pi$.

→ 4-quark vs. 2-quark states

How to detect these radiative decays

$\phi \rightarrow \mathbf{f_0(980)}\gamma$	$\rightarrow \pi^+\pi^-\gamma$		
	$\rightarrow \pi^0\pi^0\gamma$		
	$\rightarrow K^+K^-\gamma$	[$2m(K) \sim m(f_0) \sim m(\phi)$]	\rightarrow expected BR $\sim 10^{-6}$
	$\rightarrow K^0K^0\gamma$	“	“ $\sim 10^{-8}$
$\phi \rightarrow \mathbf{a_0(980)}\gamma$	$\rightarrow \eta\pi^0\gamma$		
	$\rightarrow K^+K^-\gamma$		\rightarrow expected BR $\sim 10^{-6}$
	$\rightarrow K^0K^0\gamma$		\rightarrow “ $\sim 10^{-8}$
$\phi \rightarrow \mathbf{f_0(600)}\gamma$	$\rightarrow \pi^+\pi^-\gamma$		
	$\rightarrow \pi^0\pi^0\gamma$		

General Comments:

\rightarrow fits of mass spectra needed to extract the **signals**: this requires a *parametrization* for the signal shape;

\rightarrow the unreducible **background** is not fully known: a *parametrization* is required and some parameters have to be determined from the data themselves;

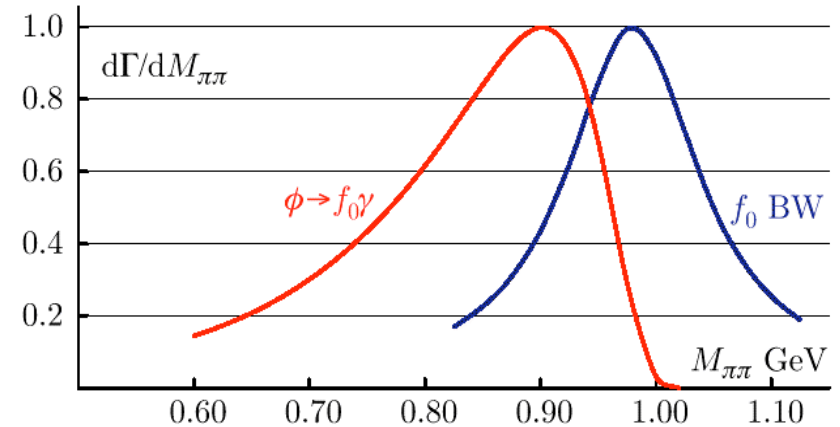
\rightarrow sizeable interferences between **signal** and **background**

How to extract the signal:

1. Electric Dipole Transitions:

$$\rightarrow \Gamma(E1) \propto \mathbf{E}_\gamma^3 \times |\mathbf{M}_{if}(\mathbf{E}_\gamma)|^2$$

2. Distortions due to KK thresholds (Flatte'-like).



Kaon-loop (by N.N.Achasov): for each scalar meson S: ($\mathbf{g}_{S\pi\pi}$, \mathbf{g}_{SKK} , \mathbf{M}_S)

No-Structure (by G.Isidori and L.Maiani): a modified BW + a *polynomial continuum*: ($\mathbf{g}_{\phi S\gamma}$, $\mathbf{g}_{S\pi\pi}$, \mathbf{g}_{SKK} , \mathbf{M}_S + pol. cont. parameter)

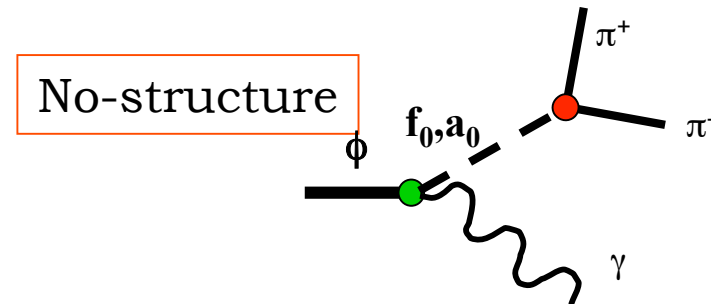
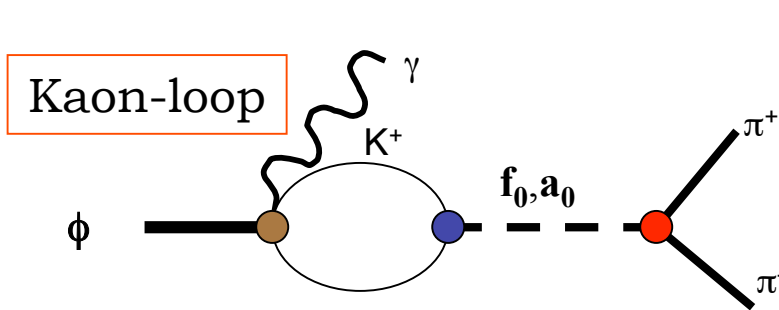
Scattering Amplitudes (by M.E.Boglione and M.R.Pennington)

$$A \propto (a_1 + b_1 m^2 + c_1 m^4) T(\pi\pi \rightarrow \pi\pi) + (a_1 + b_1 m^2 + c_1 m^4) T(\pi\pi \rightarrow KK)$$

\rightarrow pole residual \mathbf{g}_ϕ

Definition of the relevant couplings (S=f₀ or a₀):

S to ϕ	$g_{\phi S \gamma}$	(GeV ⁻¹)
S to kaons	$g_{SKK} = g_{SK^+K^-} = g_{SK^0K^0}$	(GeV)
f ₀ to $\pi\pi$ (I=0)	$g_{f_0\pi\pi} = \sqrt{3/2} g_{f_0\pi^+\pi^-} = \sqrt{3} g_{f_0\pi^0\pi^0}$	(GeV)
a ₀ to $\eta\pi$ (I=1)	$g_{a_0\eta\pi}$	(GeV)
Coupling ratio	$R_{f_0} = (g_{f_0K^+K^-} / g_{f_0\pi^+\pi^-})^2$ $R_{a_0} = (g_{a_0K^+K^-} / g_{a_0\eta\pi})^2$	



$$A_{KL} = g(m^2) e^{i\delta(m)} \frac{g_{f_0K^+K^-} g_{f_0\pi^+\pi^-}}{(s - m^2) D'_{f_0}(m)},$$

$$A_{NS} = \frac{g_{\phi f_0 \gamma} g_{f_0\pi^+\pi^-}}{D_{f_0}(m)} + \frac{a_0}{m_\phi^2} e^{i b_0 p_\pi(m)} + a_1 \frac{m^2 - m_{f_0}^2}{m_\phi^4} e^{i b_1 p_\pi(m)}$$

$$D_{f_0}(m) = m^2 - m_{f_0}^2 + i \left(\frac{g_{f_0\pi\pi}^2}{16\pi} \sqrt{1 - \frac{4m_\pi^2}{m^2}} + \frac{g_{f_0KK}^2}{16\pi} \left(\sqrt{1 - \frac{4m_{K^\pm}^2}{m^2}} + \sqrt{1 - \frac{4m_{K^0}^2}{m^2}} \right) \right)$$

The unreducible backgrounds

$(\pi^+\pi^-)$: *huge* backgrounds:

Initial + Final state radiation (ISR+FSR)

$\phi \rightarrow \rho^\pm \pi^\pm$ with $\rho^\pm \rightarrow \pi^\pm \gamma$

$(\pi^0\pi^0)$: *large* backgrounds:

$e^+e^- \rightarrow \omega\pi^0$ with $\omega \rightarrow \pi^0\gamma$

$\phi \rightarrow \rho^0\pi^0$ with $\rho^0 \rightarrow \pi^0\gamma$

HOWEVER, practically background free for $M_{\pi\pi}$ above 700 MeV

$(\eta\pi^0)$: *small* backgrounds:

$e^+e^- \rightarrow \omega\pi^0$ with $\omega \rightarrow \eta\gamma$

$\phi \rightarrow \rho^0\pi^0$ with $\rho^0 \rightarrow \eta\gamma$

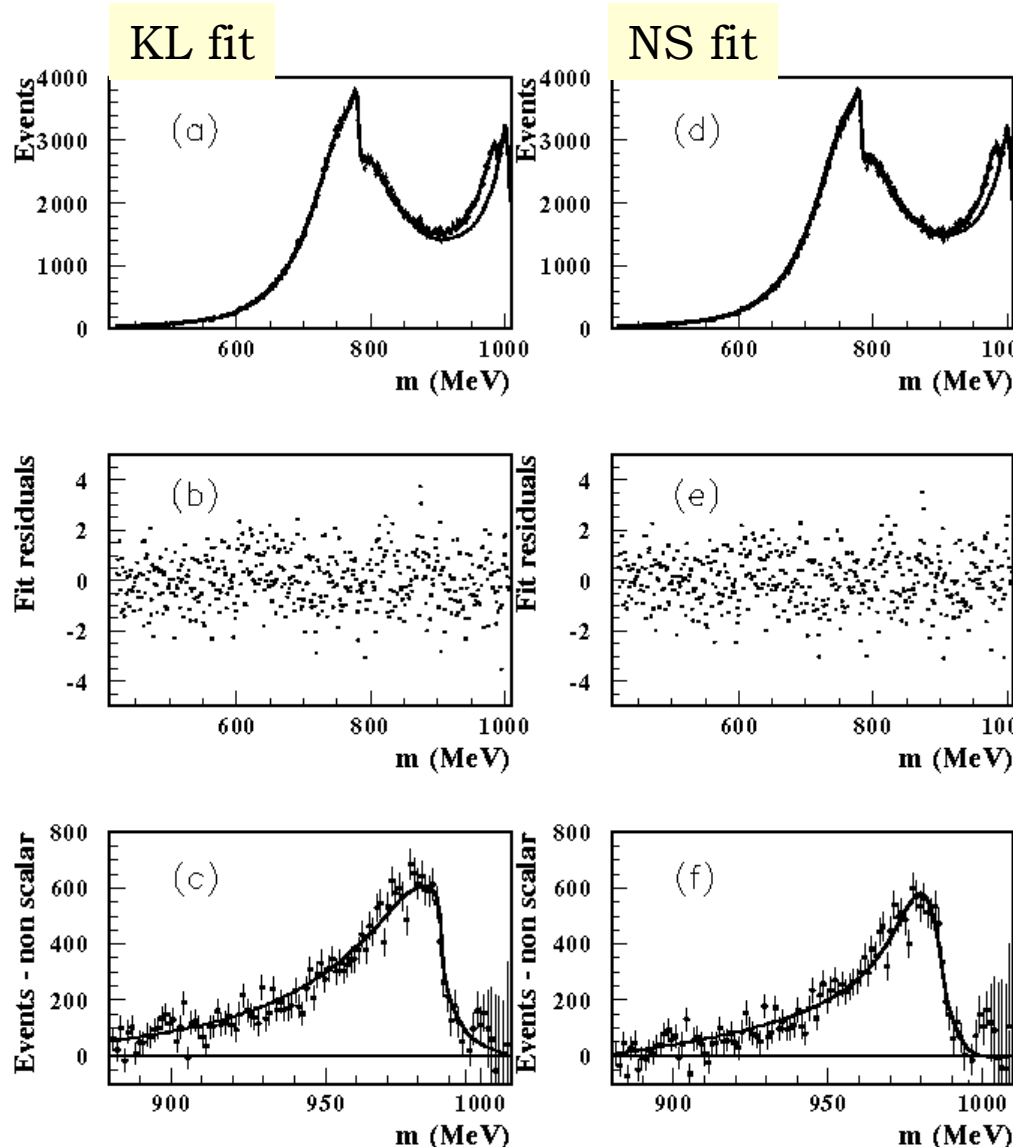
$(\pi^+\pi^-)$ vs. $(\pi^0\pi^0)$: “same amplitude” with different background !

$(\eta\pi^0)$ is the “cleanest” sample:

Not discussed today .. no news since Capri 05

Fit to the $m(\pi^+\pi^-)$ spectrum

$$F = \text{ISR} + \text{FSR} + \rho\pi + \text{scalar} \pm \text{interference}$$



KL and NS fits:

→ Good description in both cases of **signal** and **background** (KS);

→ “negative” interference;

→ $f_0(600)$ doesn't help.

	KL	NS
χ^2 ($p(\chi^2)$)	538/483 (4.2%)	533/479 (4.4%)
m_{f_0} (MeV)	983.0 ± 0.6	977.3 ± 0.9
$g_{\phi f_0 \gamma}$ (GeV^{-1})	—	1.48 ± 0.06
$g_{f_0 K^+ K^-}$ (GeV)	5.89 ± 0.14	1.73 ± 0.12
$g_{f_0 \pi^+ \pi^-}$ (GeV)	(3.6)	0.99 ± 0.02
$R = g_{f_0 K^+ K^-}^2 / g_{f_0 \pi^+ \pi^-}^2$	2.66 ± 0.10	(3.1)
a_0	—	6.00 ± 0.02
a_1	—	4.10 ± 0.04
b_1 (rad/GeV)	—	3.13 ± 0.05
m_{ρ^0} (MeV)	773.1 ± 0.2	773.0 ± 0.1
Γ_{ρ^0} (MeV)	144.0 ± 0.3	145.1 ± 0.1
α ($\times 10^{-3}$)	1.65 ± 0.05	1.64 ± 0.04
β ($\times 10^{-3}$)	-123 ± 1	-137 ± 1
$a_{\rho\pi}$	0.0 ± 0.6	1.5 ± 1.4

Parameter uncertainties are dominated by the systematic errors:

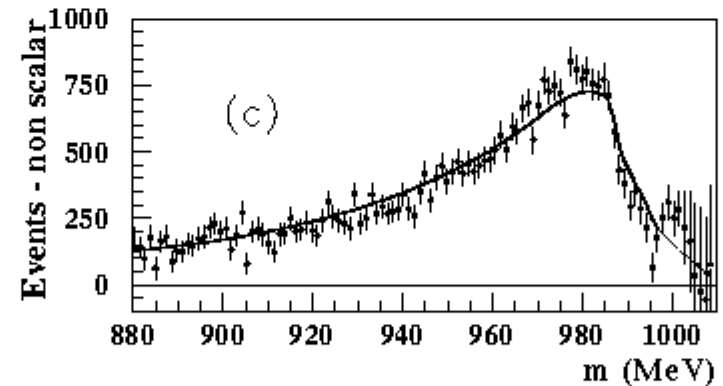
parameter	KL	NS
m_{f_0} (MeV)	980–987	973–981
$g_{f_0 K^+ K^-}$ (GeV)	5.0 – 6.3	1.6– 2.3
$g_{f_0 \pi^+ \pi^-}$ (GeV)	3.0– 4.2	0.9–1.1
$R = g_{f_0 K^+ K^-}^2 / g_{f_0 \pi^+ \pi^-}^2$	2.2– 2.8	2.6– 4.4
$g_{\phi f_0 \gamma}$ (GeV ⁻¹)	–	1.2– 2.0

Comments:

- Mass value OK [PDG 980 ± 10 MeV]
- $R > 1$ in both fits (in agreement with published values $\pi^0 \pi^0 \gamma$)
- KL couplings \gg NS couplings: effect of polynomial continuum
- NS suggests “large” coupling to the ϕ (see following)

Scattering Amplitude Fit

χ^2 (p(χ^2))	577/477 (0.1%)			
a_1	11.9	a_2	-14.7	m_{ρ^0} (MeV) 774.4 ± 0.2
b_1	3.3	b_2	-15.3	Γ_{ρ^0} (MeV) 142.8 ± 0.3
c_1	-15.1	c_2	35.8	α ($\times 10^{-3}$) 1.74 ± 0.05
m_0	0.	λ	-1.63	β ($\times 10^{-3}$) -100 ± 18
			$a_{\rho\pi}$	0 ± 2



$$\Gamma(\phi \rightarrow \gamma f_0(980)) = \frac{\pi^2}{2} g_\phi^2 \frac{m_\phi^2 - m_{f_0}^2}{m_\phi^3}$$

$g_\phi = 6.6 \times 10^{-4} \rightarrow \text{BR}(\phi \rightarrow f_0(980)\gamma) \times \text{BR}(f_0(980) \rightarrow \pi^+\pi^-) \sim 3 \times 10^{-5}$
 [similar conclusion from BP analysis of $\pi^0\pi^0\gamma$ data (KLOE + SND)]

Summarizing:

The peak at ~980 MeV is interpreted in both KL / NS as due to the decay $\phi \rightarrow f_0(980)\gamma$ with a neg. interference with FSR.

The couplings suggest the $f_0(980)$ to be strongly coupled to kaons and to the ϕ . No space for $f_0(600)$.

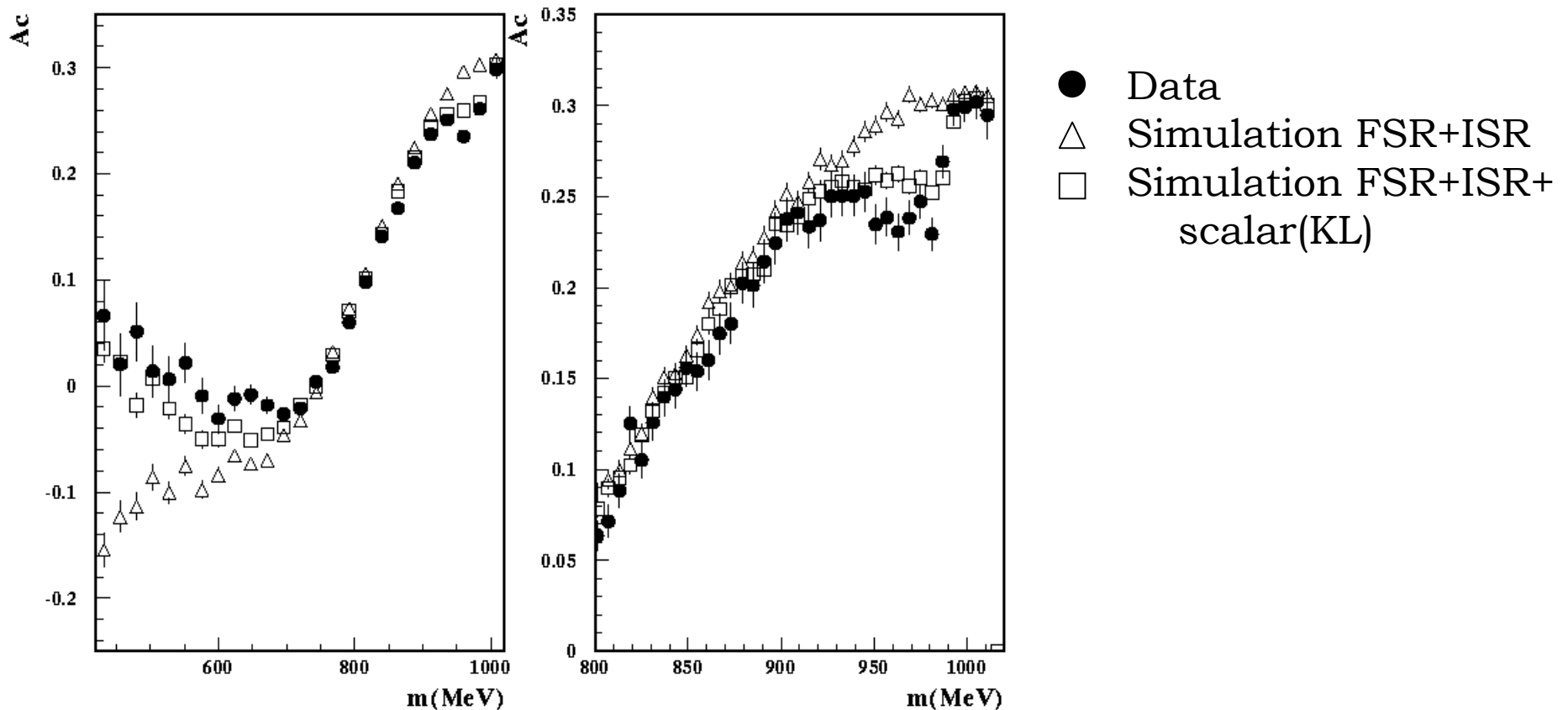
Scattering Amplitude gives a marginal agreement.

Submitted to PLB (HEP-EX 0511031)

FB asymmetry vs. $m(\pi\pi)$:

→ Clear signal ~ 980 MeV

→ Interesting comparison with simulation:



The simulation provides a “qualitative” description of:

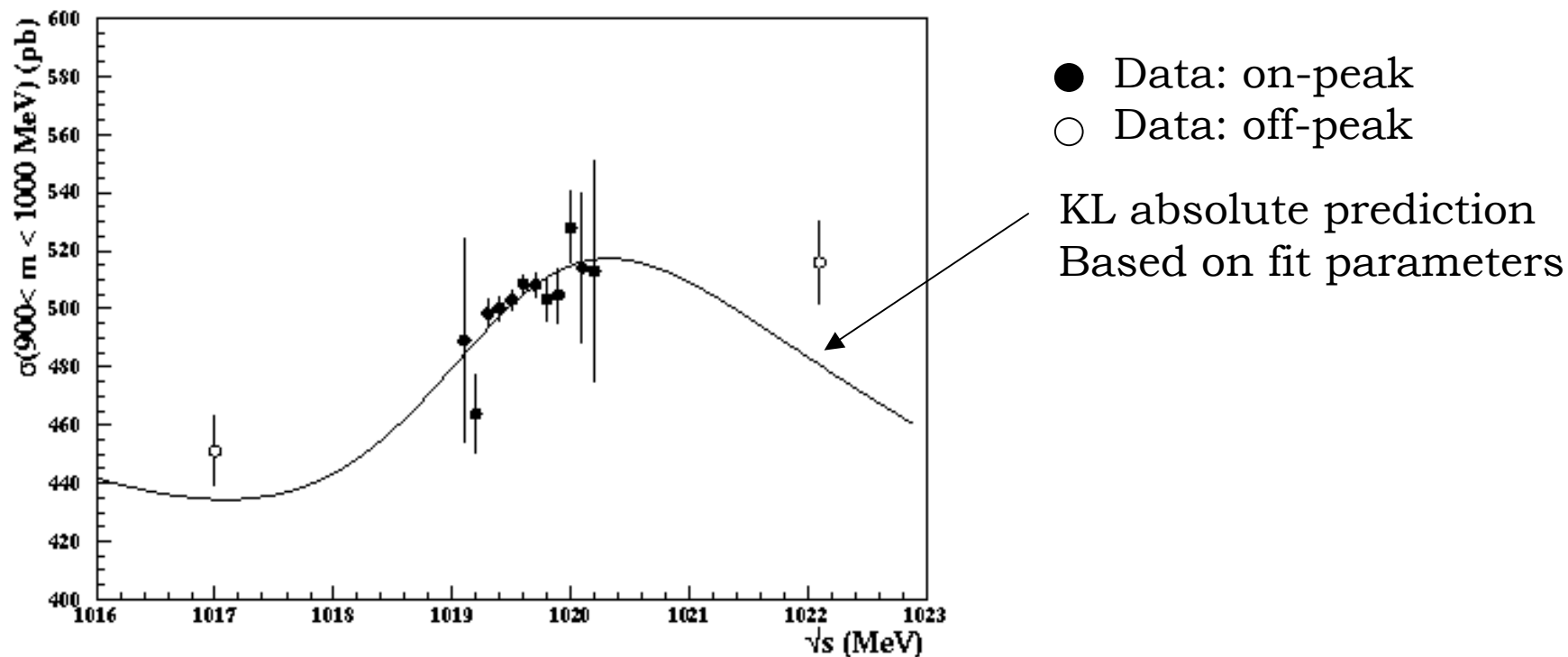
→ $f_0(980)$ region behaviour (the signal is reproduced);

→ Low mass behaviour (low mass tail of the signal).

Remarkable result: not a fit but an **absolute prediction**

Cross section dependence on \sqrt{s} :

Absolute prediction based on KL fit parameters



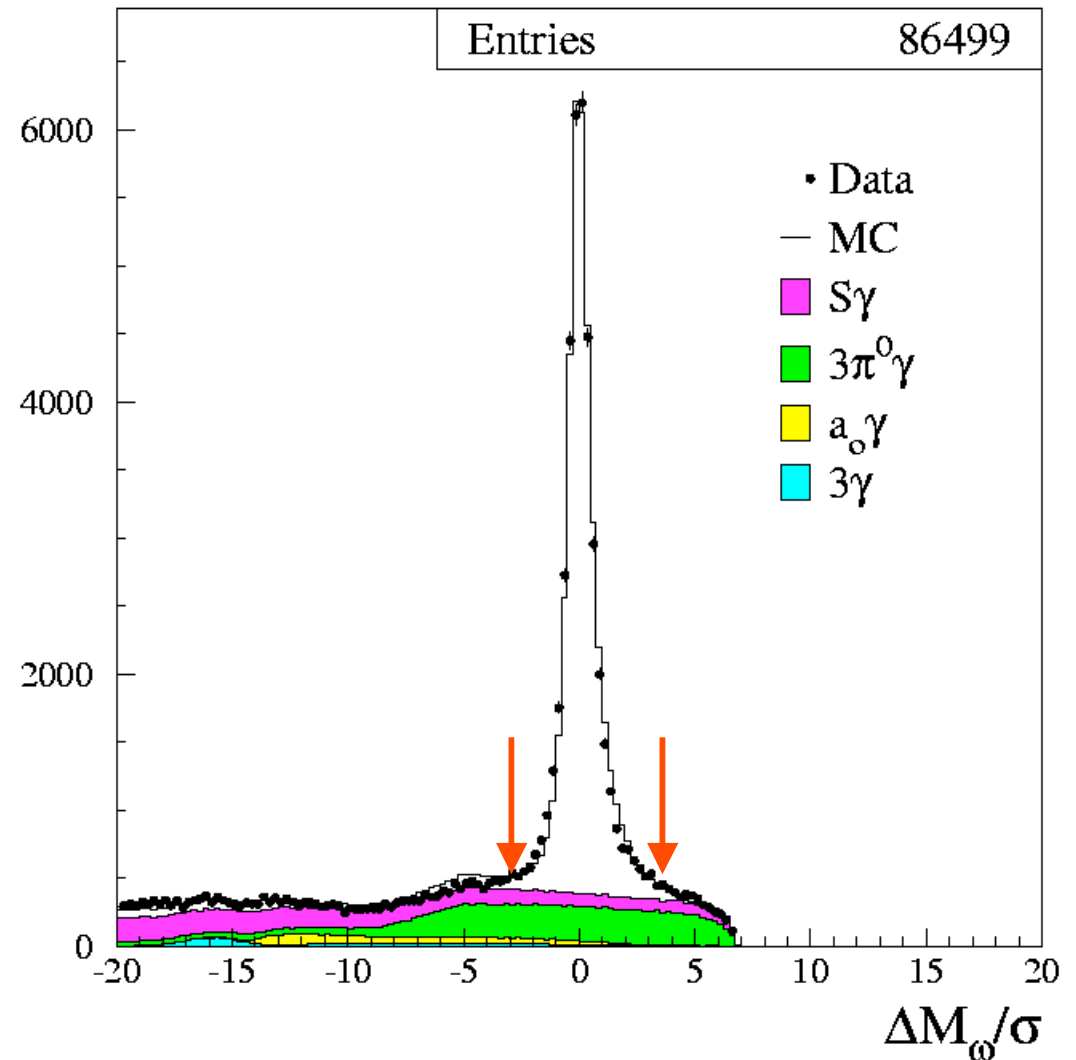
Concluding remark: $\pi^+\pi^-\gamma$ is a powerful tool to test scalar production: mass spectrum, FB asym. and \sqrt{s} dependence
the now collected 2 fb^{-1} at $\phi \rightarrow$ factor 6 more of what already published + the finer energy scan around the ϕ will allow us to test deeply this model

Status of $\pi^0\pi^0\gamma$ final state

- As shown at Capri, we have reached **a stable conclusive result on the data analysis** while we are completing the fit on the dalitz-plot.
- Today we show the results of the fits to the $\pi\pi\gamma$ visible cross section obtained by repeating, **with our new process independent photon pairing procedure**, the analysis “as for 2000 data” i.e. **neglecting any interference between VDM and scalar terms**.
- From these fits we will extract the parameters describing the $e^+e^- \rightarrow \omega\pi^0$ and the $\text{BR}(\phi \rightarrow \pi\pi\gamma)$.
- To understand how well we do all of this (**+ for checking the normalization of our main background**) we have also analyzed a large sample of $\phi \rightarrow \eta\gamma$ decays in 7 photons (prescaling 1/50 while running our 5-photon selection).

$\omega\pi$ vs $S\gamma$ events (Masses)

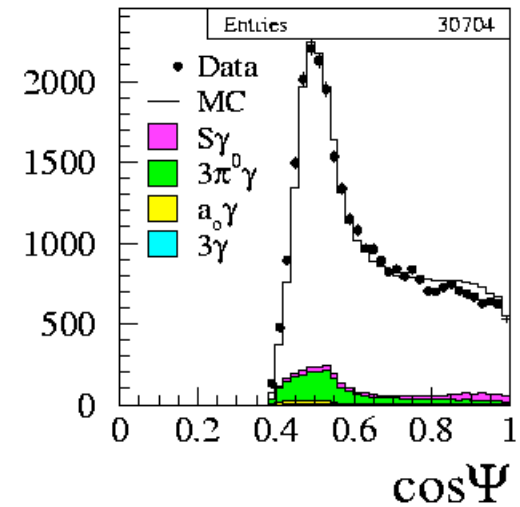
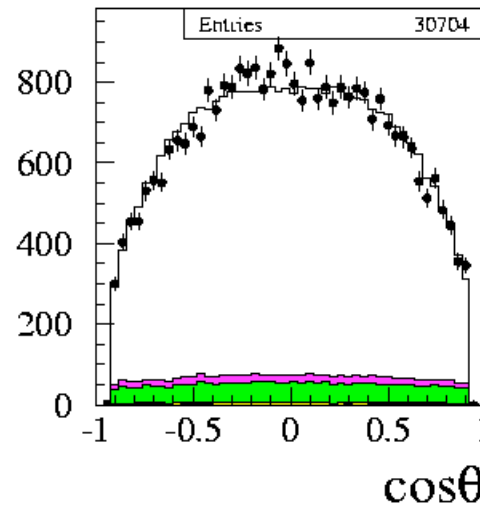
- With our new, process independent, photon pairing procedure, we build the invariant mass $\pi^0\gamma$ and select the one closest to $M\omega$
- As for 2000 data, we then count as :
 - $\omega\pi$ events the ones in within 3 sigma from $M\omega$
 - $S\gamma$ all the others



$\omega\pi$ vs $S\gamma$ events (Angular distributions)

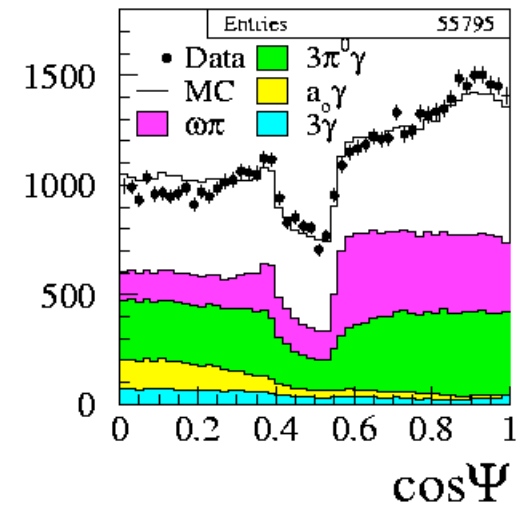
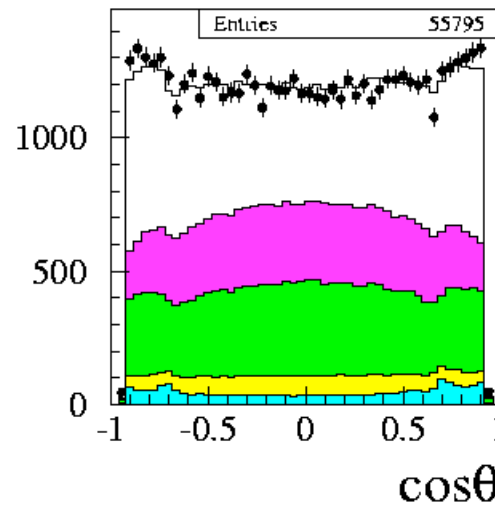
$\omega\pi$ events

Clear $S=1$
angular dependence



$S\gamma$ events

Clear $S=0$
angular dependence



$\omega\pi$: energy dependence of the xsec

$$\sigma^{\omega\pi}(\sqrt{s}) = \sigma_0^{\omega\pi}(\sqrt{s}) \left| 1 - Z \frac{M_\phi \Gamma_\phi}{D_\phi} \right|^2, \quad (11)$$

where $\sigma_0^{\omega\pi}(\sqrt{s})$ represents the nude cross section for the not-resonant process, Z is the complex interference parameter (i.e. the ratio between the ϕ decay amplitude and the not-resonant process), while M_ϕ , Γ_ϕ and $D_\phi = M_\phi^2 - s - i\sqrt{s}\Gamma_\phi$ are respectively the mass, the width and the inverse propagator of the ϕ meson.

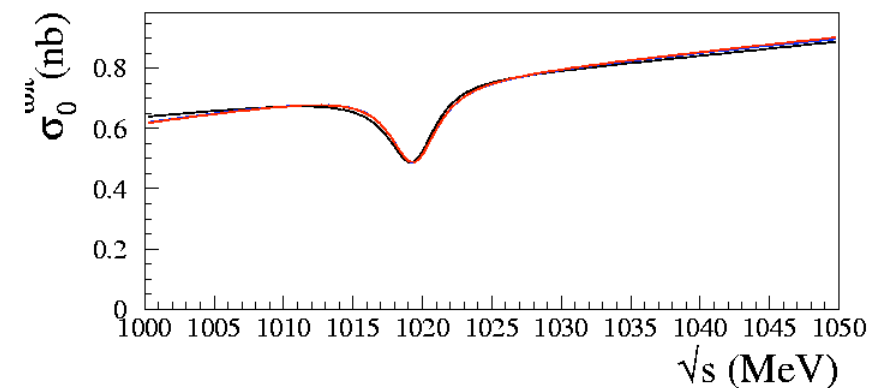
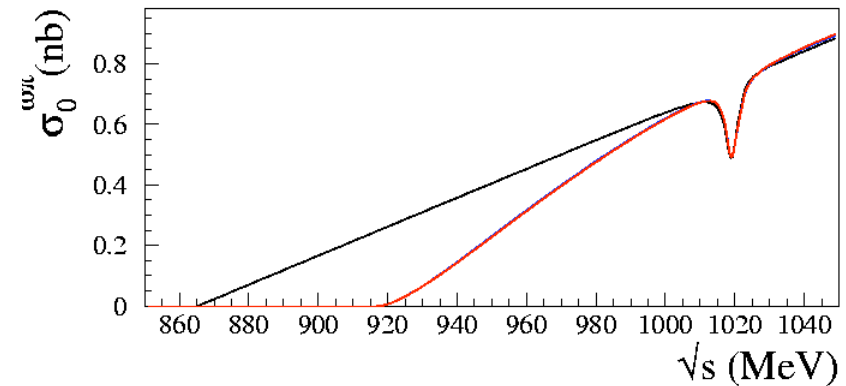
A) Linear dependence

$$- \sigma = \sigma_0 \times (1 + \alpha (\sigma' - M_\phi))$$

B) Model ρ/ρ' mesons

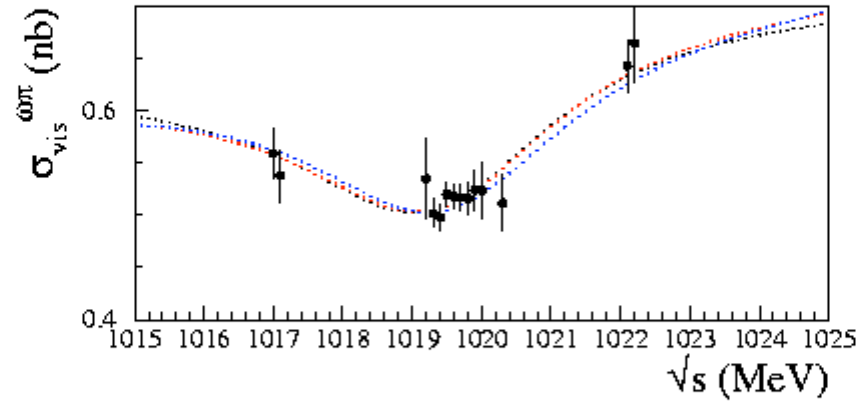
$$\sigma_0^{\omega\pi}(\sqrt{s}) = \frac{K}{s^{3/2}} \left| \frac{M_\rho^2}{D(\rho)} + \frac{A_1 M_{\rho'}^2}{D(\rho')} \right|^2 P_f(\sqrt{s}),$$

2 different parametrizations
of ρ ρ' used

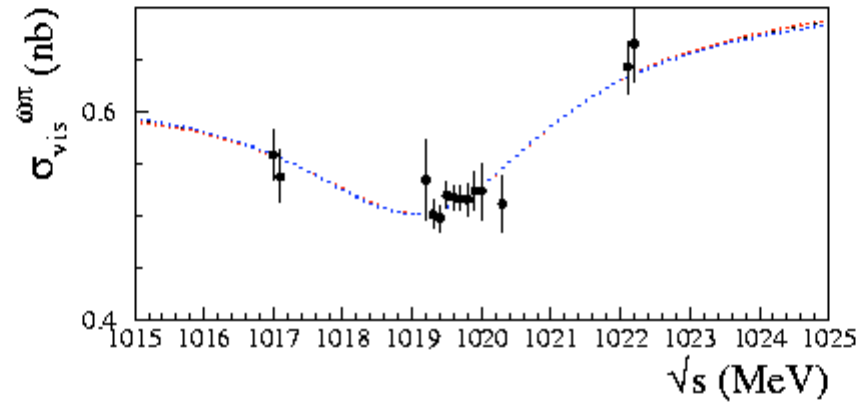


$\omega\pi$: Fit to the visible xsec

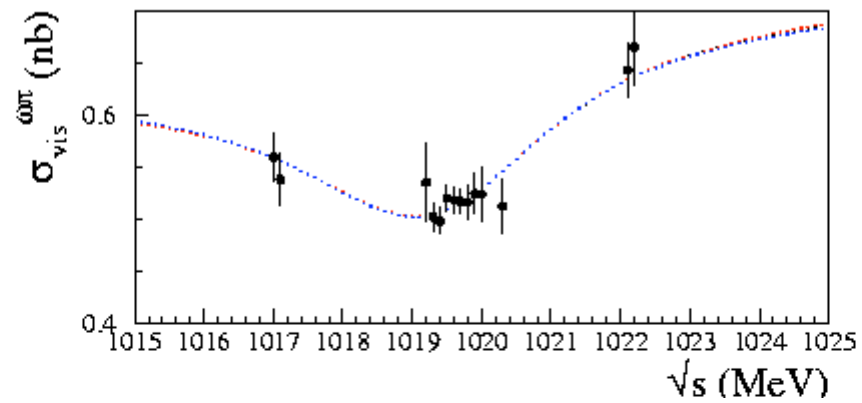
Fit A



Fit B



Fit C



$\varphi \rightarrow \eta\gamma$: energy dependence of the cross sections

$$12\pi \Gamma_{\phi}^{e^+e^-} \Gamma_{\phi}^{\eta\gamma} \left| \frac{e^{i\pi}}{D_{\phi}} + \frac{R_{\rho}}{D_{\rho}} + \frac{R_{\omega}}{D_{\omega}} \right|^2 \left(\frac{M_{\phi}}{\sqrt{s}} \right)^3 \left(\frac{Q_{\eta}(\sqrt{s})}{Q_{\eta}(M_{\phi})} \right)^3 \quad (3)$$

3 Fit parameters :

- α normalization
- M_{ϕ}, Γ_{ϕ}

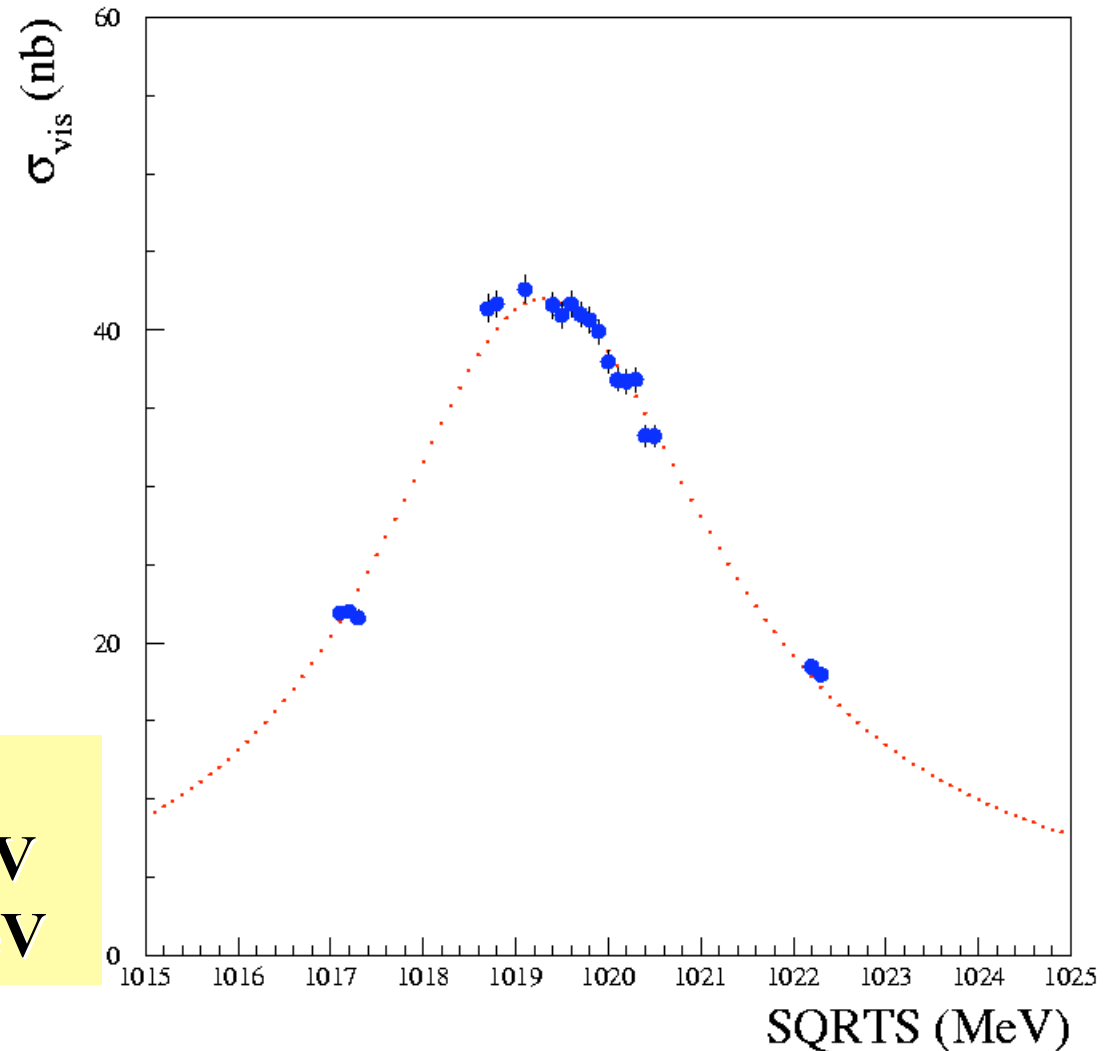
We use $\Gamma_{\phi}^{\text{ll}}(\text{KLOE}) = 1.320 \pm 0.017 \pm 0.015 \text{ keV}$

$$\chi^2 = 16.8/17$$

$$\alpha = 1.014 \pm 0.010$$

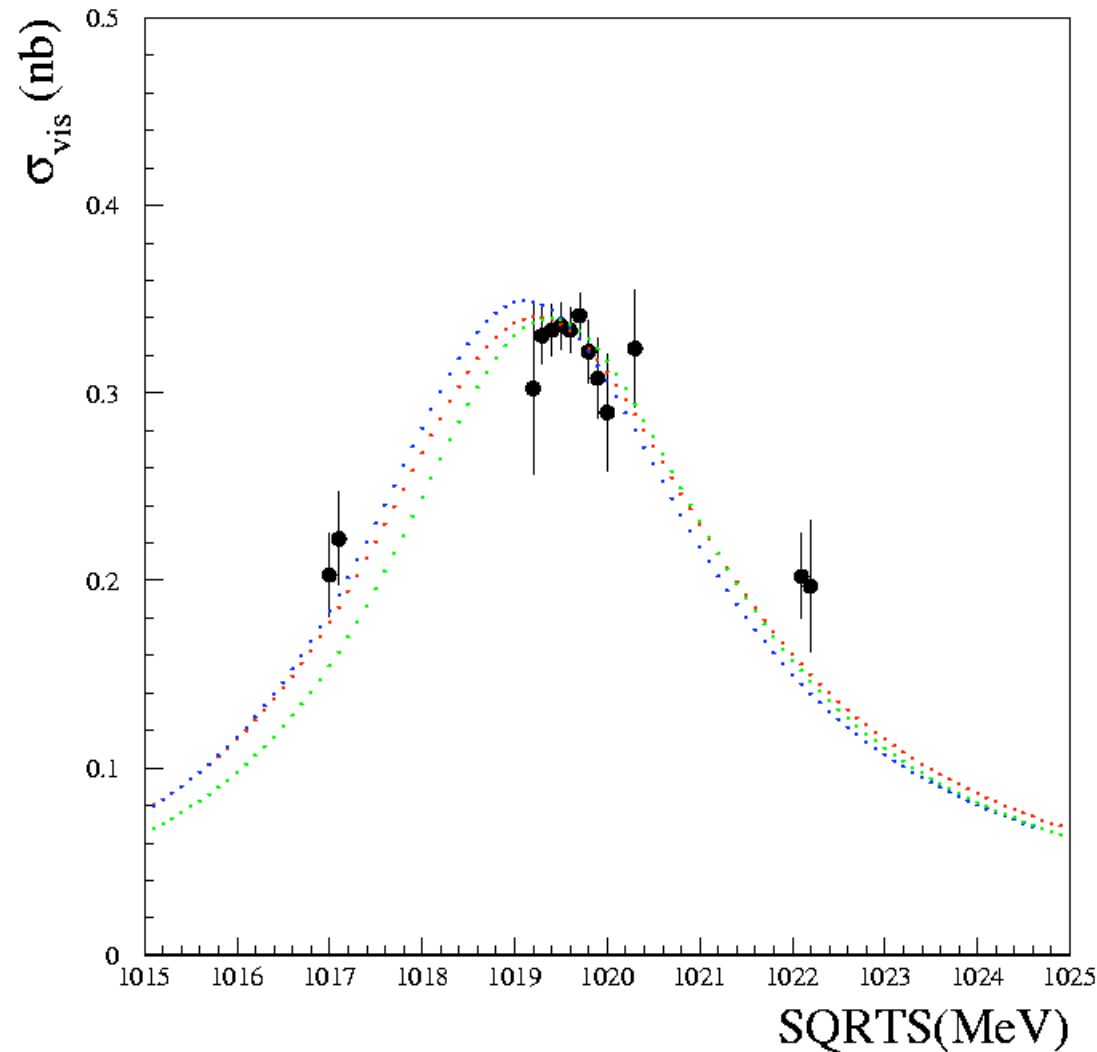
$$M_{\phi} = 1019.40 \pm 0.01 \text{ MeV}$$

$$\Gamma_{\phi} = 4.36 \pm 0.09 \text{ MeV}$$



$\varphi \rightarrow f_0 \gamma$: energy dependence of the xsec

$$\sigma_0^{S\gamma}(s) = 12\pi\Gamma_\phi^{e^+e^-}\Gamma_\phi^{S\gamma} \left| \frac{1}{D_\phi(s)} \right|^2 \left(\frac{M_\phi}{\sqrt{s}} \right)^3 R_\Gamma(s)$$



$f_0\gamma$: Determination of BR ($\phi \rightarrow f_0\gamma \rightarrow \pi^0\pi^0\gamma$)

FIT	α	M_ϕ (MeV)	Γ_ϕ (MeV)	χ^2 / Ndof
(A) All free	1.319 ± 0.012	1019.34 ± 0.01	4.60 ± 0.09	13.9/11
(B) Γ_ϕ fixed	1.285 ± 0.001	1019.21 ± 0.35	4.358	17.2/12
(C) M_ϕ, Γ_ϕ fixed	1.223 ± 0.001	1019.46	4.26	21.8/12

From the values of α we determine the value of $\Gamma(\phi \rightarrow f_0\gamma)$ at M_ϕ which is proportional to $(g_{f_0}^{K^+K^-} - g_{f_0}^{\pi^+\pi^-})^2$. **We get $\Gamma(\phi \rightarrow \pi^0\pi^0\gamma) = (0.498 \pm 0.005 \pm 0.022) \text{ keV}$** . The systematic error is dominated by the variation of the three fits. When dividing by $\Gamma_\phi(M_\phi)$ we determine the $BR(\phi \rightarrow f_0\gamma)$ to be:

$$\mathbf{BR(\phi \rightarrow \pi^0\pi^0\gamma) = (1.057 \pm 0.046_{\text{fit}} \pm 0.017_{\text{norm}}) \cdot 10^{-4}}$$

where the normalization error reflects our knowledge of Γ_ϕ^M . The result is in pretty good agreement with our old measurement.

First conclusions on $\pi^0\pi^0\gamma$ final state

- When neglecting the interference between $\omega\pi$ and $S\gamma$ we are able to distinguish the most relevant features of the $\pi\pi\gamma$ events:
 - There is a clear resonant – not resonant component
 - The not resonant component is dominated by $e^+e^- \rightarrow \omega\pi \rightarrow \pi\pi\gamma$ events with a well defined **spin 1 angular dependence**.
 - The resonant component **is a scalar**
 - If we fit the not-resonant component we find the parameters describing the interference with the ϕ meson to be in reasonable agreement with SND.
 - If we fit the resonant component we find that the two points far away the ϕ peak are not perfectly described by our model.
However **we extract the BR ($\phi \rightarrow \pi\pi\gamma$)**
 - All of this work has been summarized in a KLOE Memo 319

Improved KL parametrization for the $\pi^0\pi^0\gamma$

N.N.Achasov, private communication
NOW PUBLISHED HEP-PH 0512047

- Insertion of a KK phase:

$$\tan \delta_B^{K\bar{K}} = \sqrt{m^2 - 4m_{K^+}^2} f_K(m^2) = \frac{\sqrt{m^2 - 4m_{K^+}^2}}{\Lambda_K} \text{atan} \frac{m_2^2 - m^2}{m_0^2}$$

Beyond to its contribution in the interference term,

**IT CHANGES THE SCALAR TERM AMPLITUDE
IN THE $M_{\pi\pi} < 2M_{K^+}$ REGION**

$$M_{sig} = \sqrt{\frac{1 - f_K(m^2)\sqrt{4m_{K^+}^2 - m^2}}{1 + f_K(m^2)\sqrt{4m_{K^+}^2 - m^2}}} g(m) e^{i\delta_B^{\pi\pi}} \left((\phi\epsilon) - \frac{(\phi q)(\epsilon p)}{(pq)} \right) \sum_{R,R'} g_{RK^+K^-} G_{RR'}^{-1} g_{R'\pi^0\pi^0}$$

- New parametrization of the $\pi\pi$ phase:

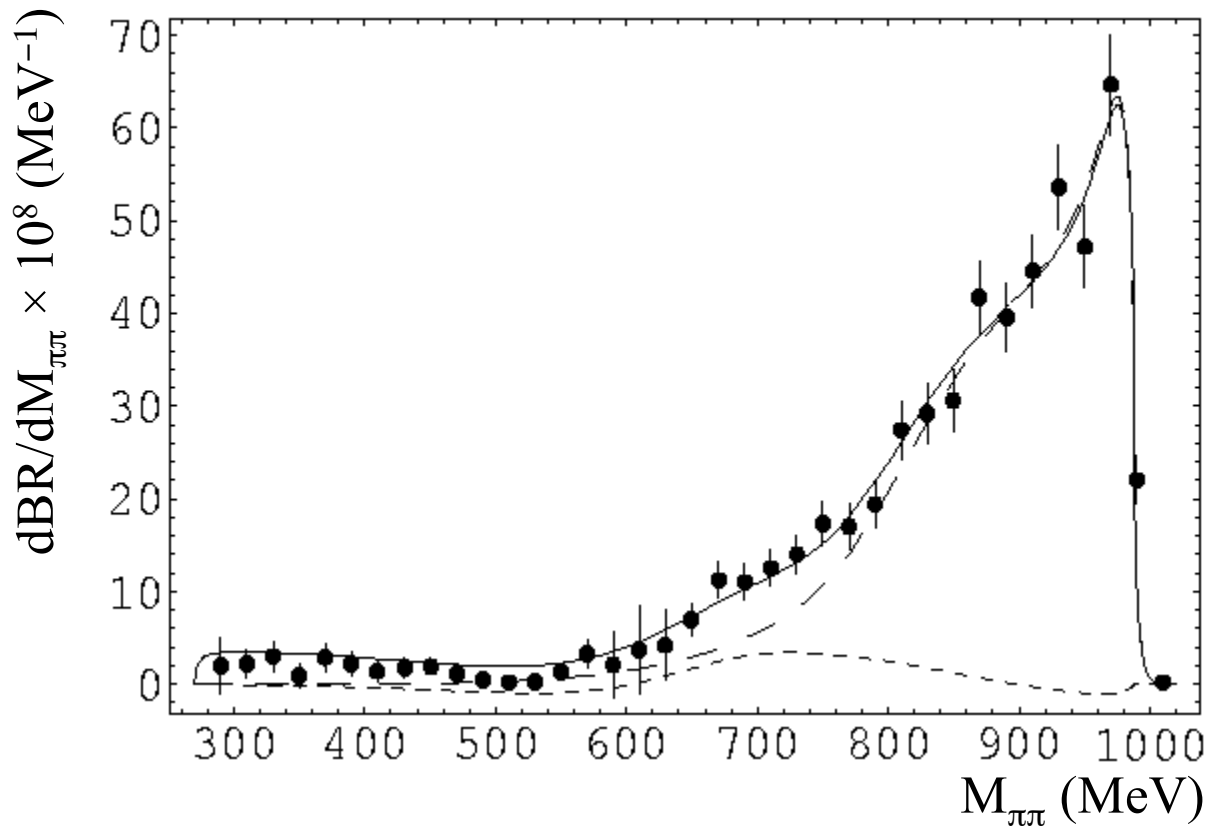
$$\tan(\delta_B^{\pi\pi}) = -\frac{p_\pi}{2m_\pi} \left(b_0 - b_1 \frac{p_\pi^2}{(2m_\pi)^2} + b_2 \frac{p_\pi^4}{(2m_\pi)^4} \right) \frac{1}{1 + p_\pi^2/\Lambda^2}$$

$$p_\pi = \sqrt{m^2 - 4m_{\pi^+}^2}$$

new KL parametrization on old KLOE data (I)

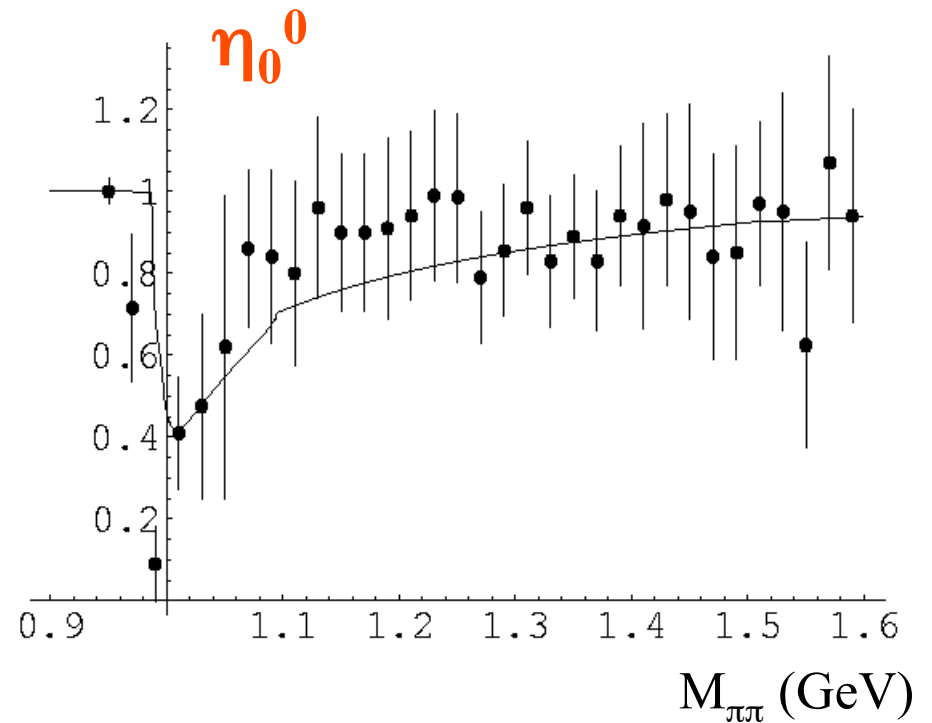
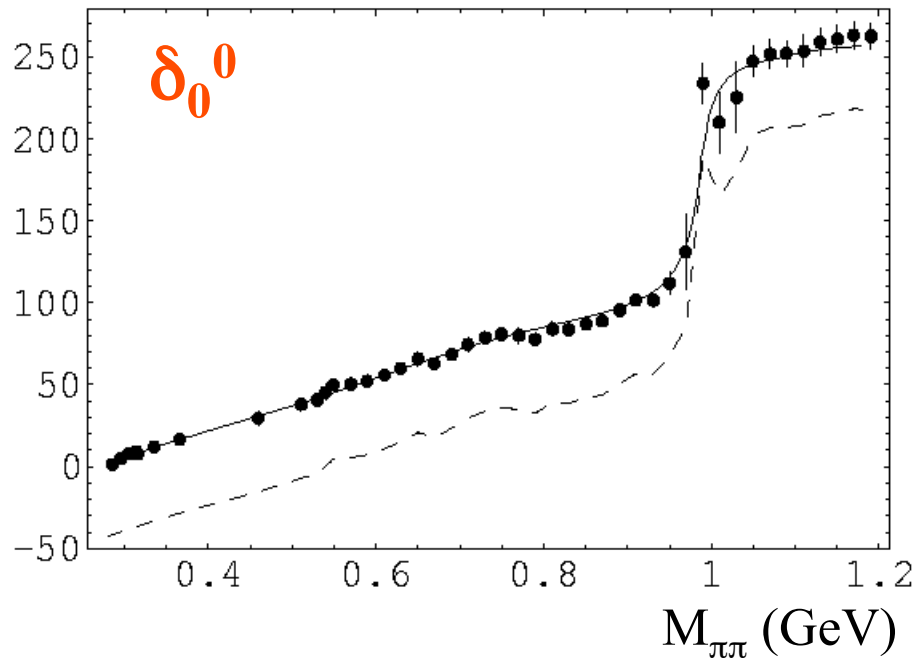
Achasov-Kiselev: combined fit to KLOE 2000 + $\pi\pi$ scattering data

$dBR/dM_{\pi\pi}$ (KLOE 2000 data)



new KL parametrization on old KLOE data (II)

Achasov-Kiselev: combined fit to KLOE 2000 + $\pi\pi$ scattering data



Paper published:
Hep-ph 0512047

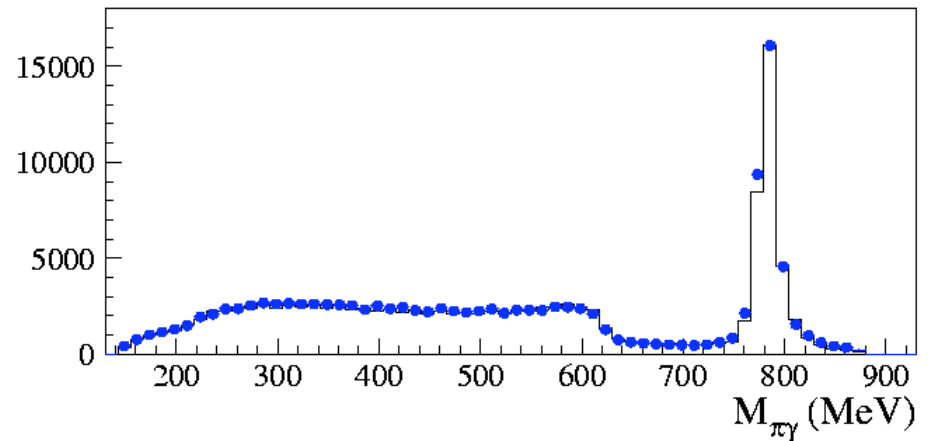
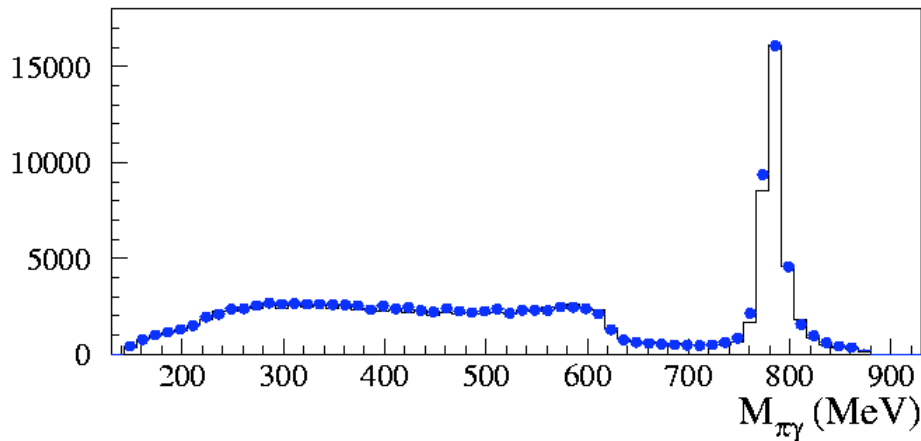
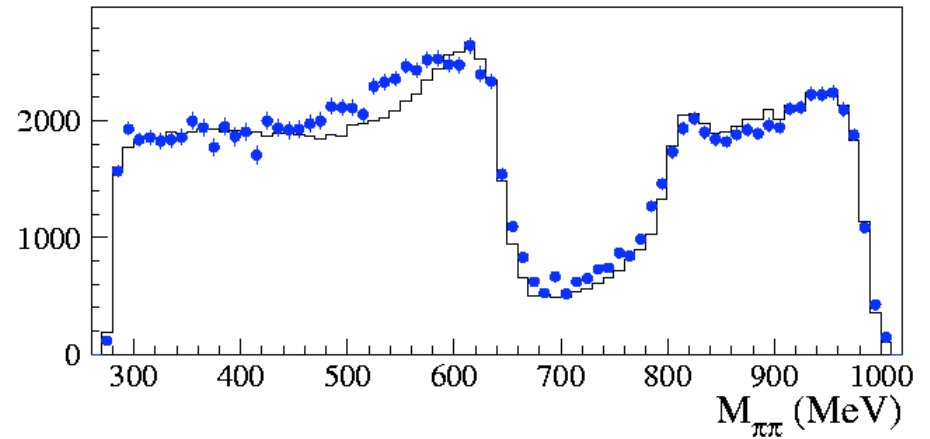
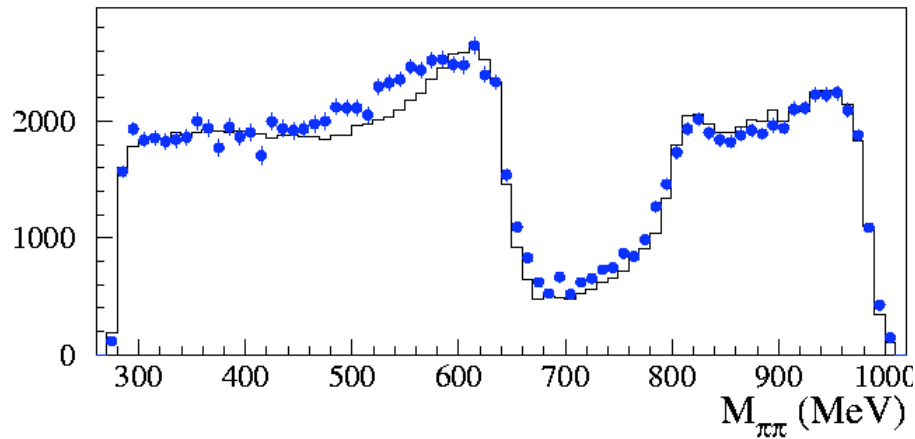
Theory advantages of the new parametrization

- ✓ Able to reproduce Mass-spectrum, δ^0_0 and inelasticity
- ✓ Sum of overlapping resonances with the correct propagator matrix
- ✓ A lot of theory restrictions applied:
 - The $\pi\pi$ scattering length a^0_0 fixed to the recent calculation of Colangelo
 - In the $\pi\pi$ scattering amplitude the “famous?” Adler zero is granted in the region below the threshold ($0 < m^2_{\pi\pi} < 4M^2_\pi$)
 - It needs a $\sigma(600)$ meson to obtain a good fit.

K-loop fit results: $f_0 + \sigma$

- Discussing with Achasov we realized that the parameters of σ and the KK , $\pi\pi$ phases are very much related.
- To let them vary freely we should either fit also the data on δ^0_0 or impose the theory restrictions explained before which are not easy to implement in our fitting function.
- We therefore followed a much more simple approach:
 - (Fit A) we left free only the f_0 parameters + VDM
 - (Fit B) as (Fit A) leaving the sigma mass to vary

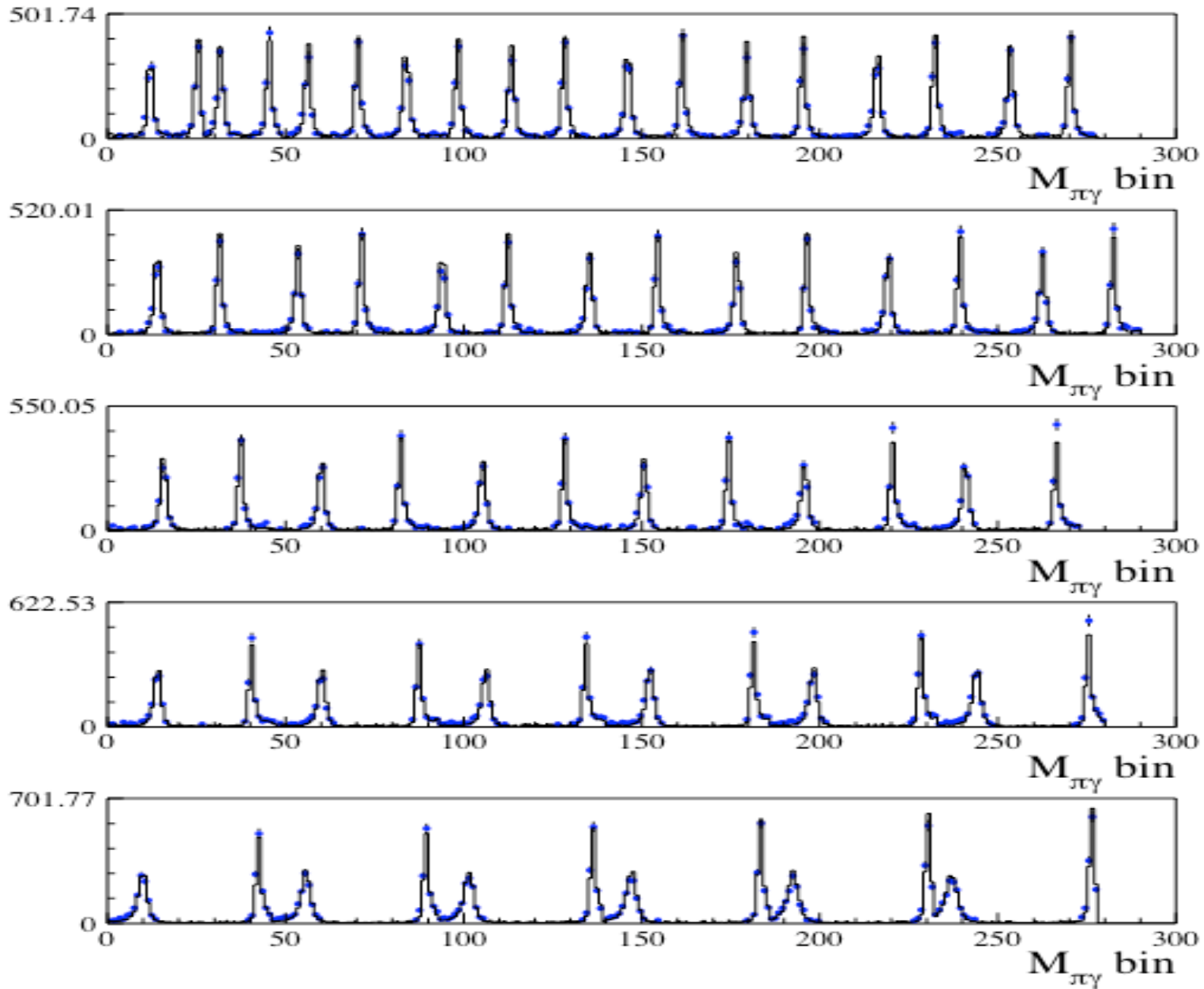
K-loop fit results: $f_0 + \sigma$ (MASSES) $\sqrt{s}=1019.6$ MeV



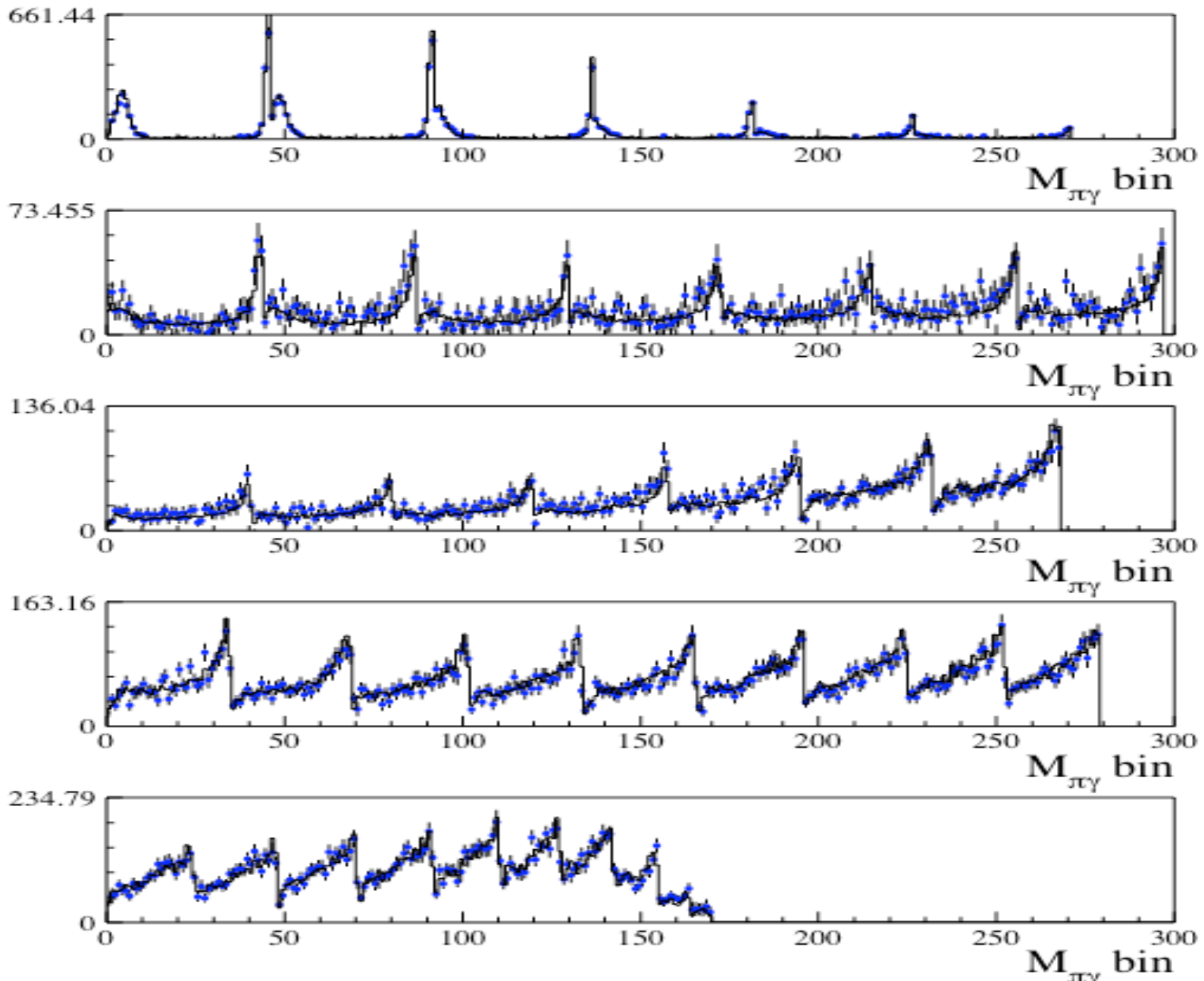
$f_0 + \text{VDM} + M\sigma$ FIXED

$f_0 + \text{VDM} + M\sigma$ Free

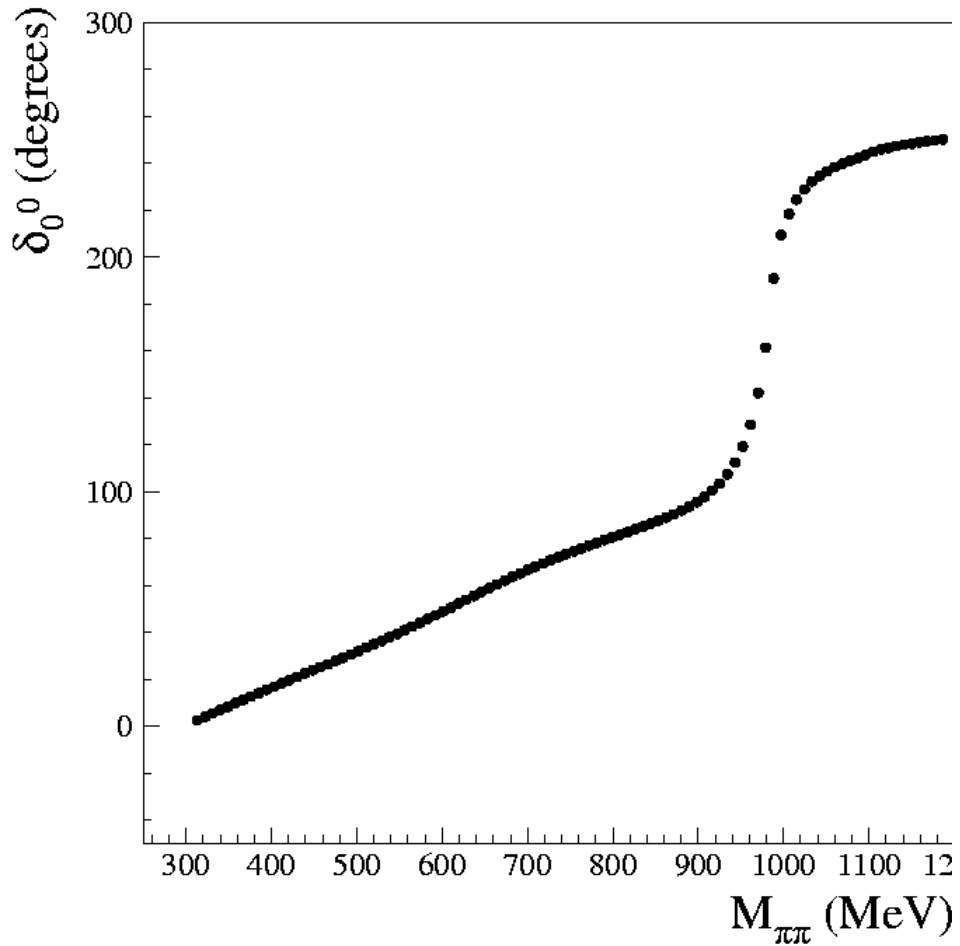
K-loop fit results: $f_0 + \sigma$ (dalitz-slices) $\sqrt{s}=1019.6$ MeV



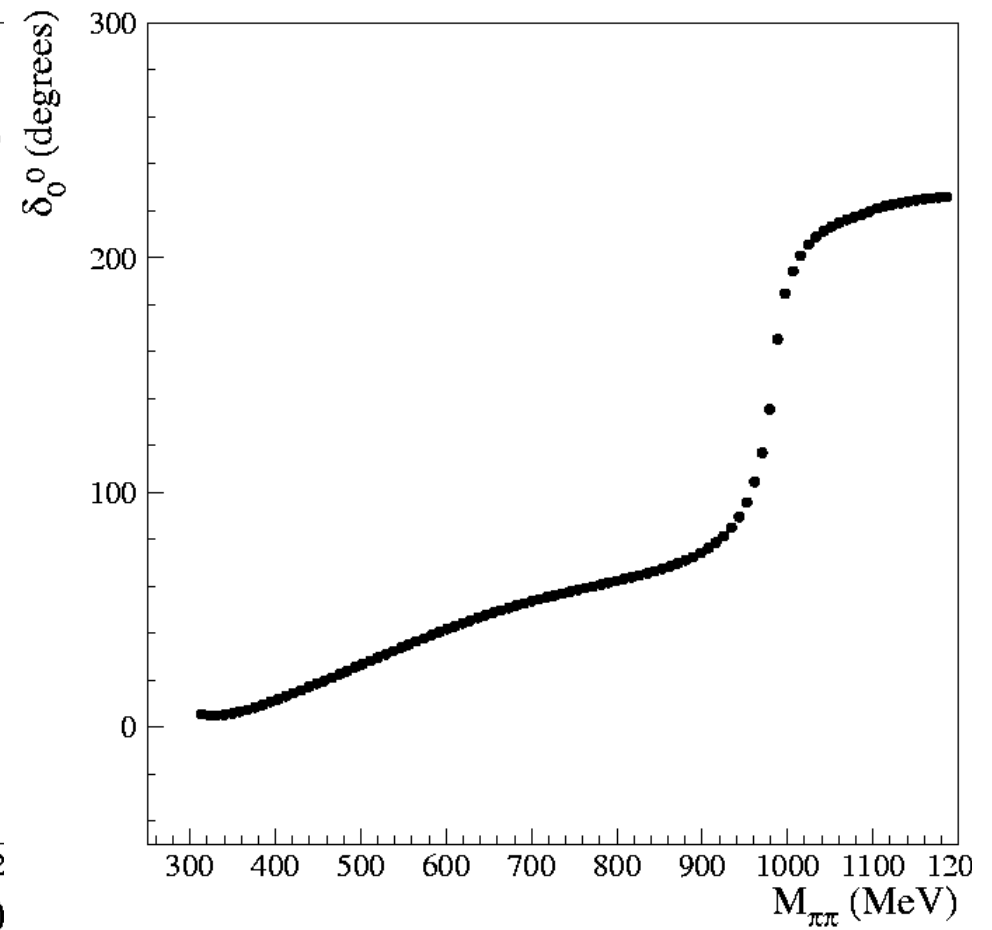
K-loop fit results: $f_0 + \sigma$ (dalitz-slices) $\sqrt{s}=1019.6$ MeV



K-loop fit results: $f_0 + \sigma$ (phases)

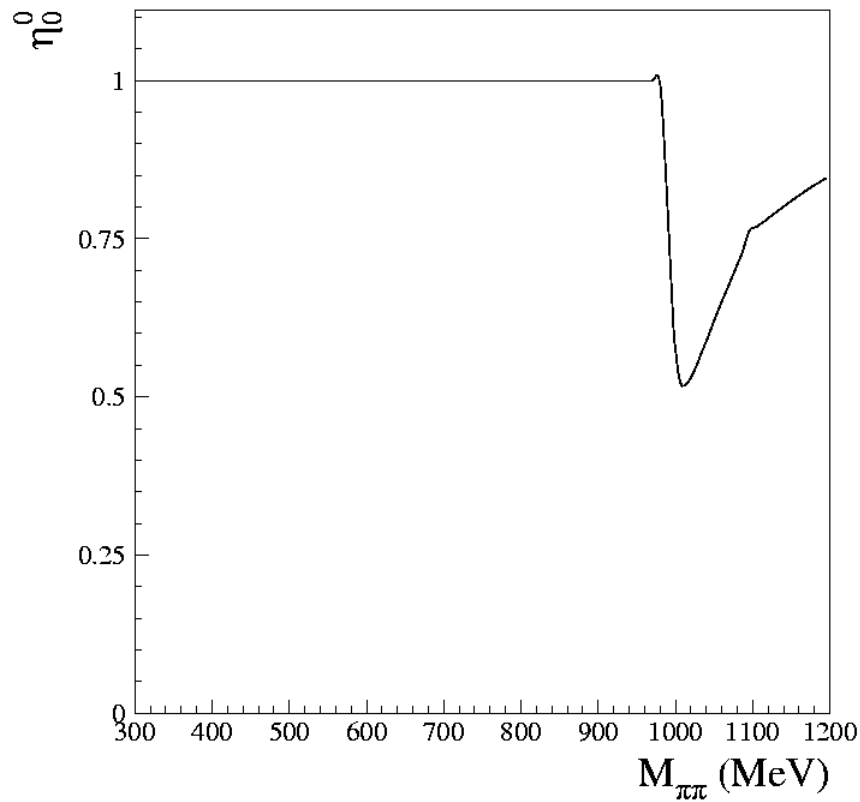


$f_0 + \text{VDM} + M\sigma$ FIXED

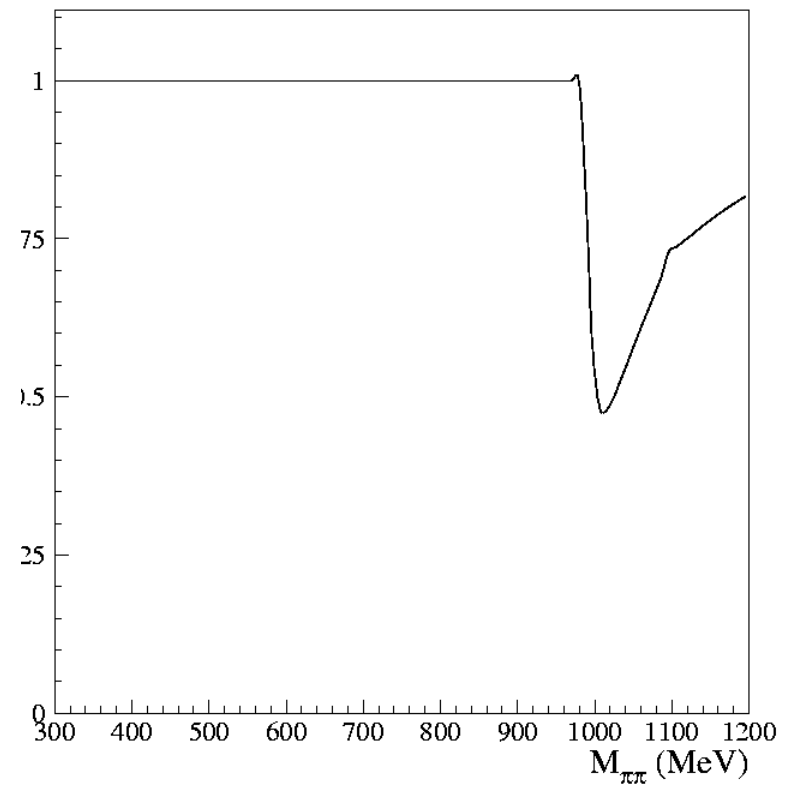


$f_0 + \text{VDM} + M\sigma$ Free

K-loop fit results: $f_0 + \sigma$ (phases)

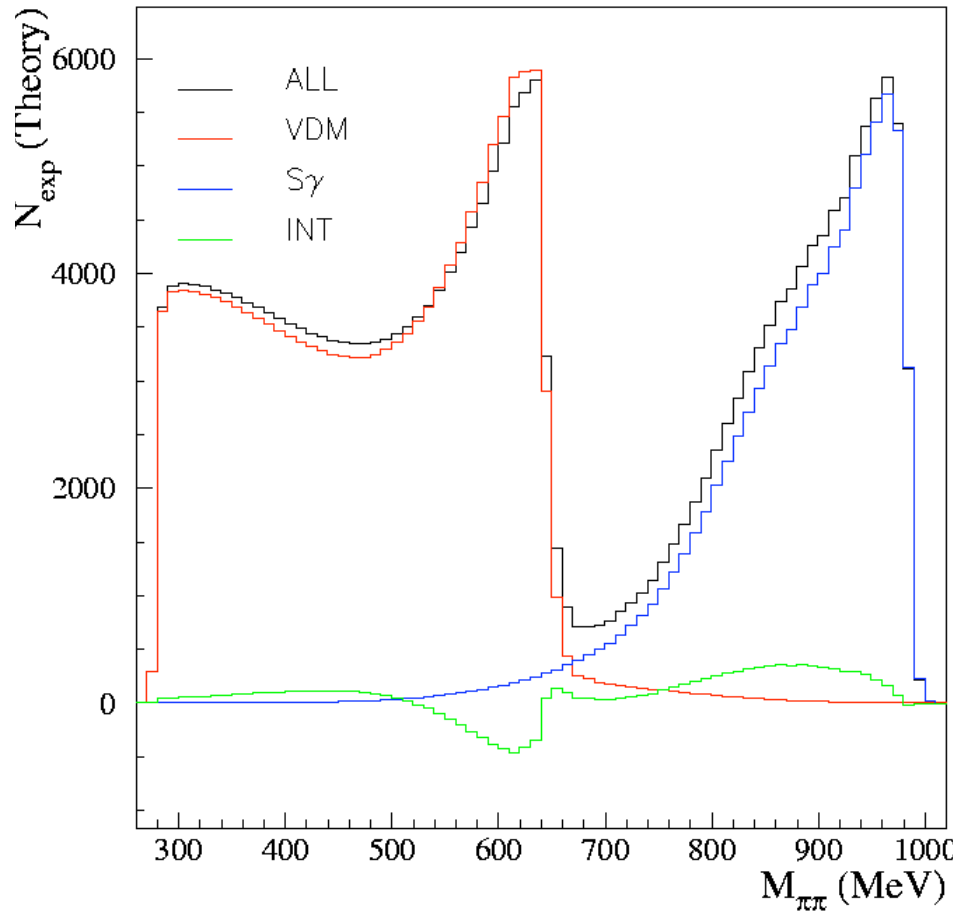


$f_0 + \text{VDM} + M\sigma$ FIXED

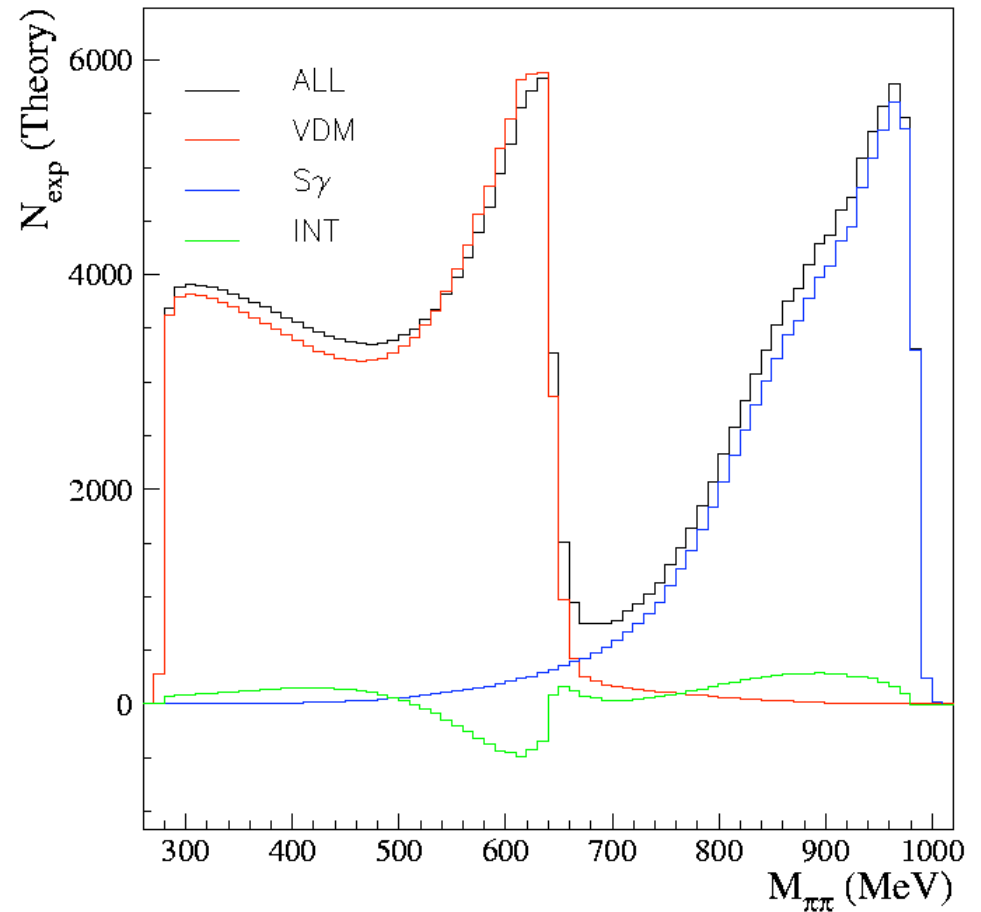


$f_0 + \text{VDM} + M\sigma$ Free

K-loop fit results: $f_0 + \sigma$ (compositions)



$f_0 + \text{VDM} + M\sigma$ FIXED

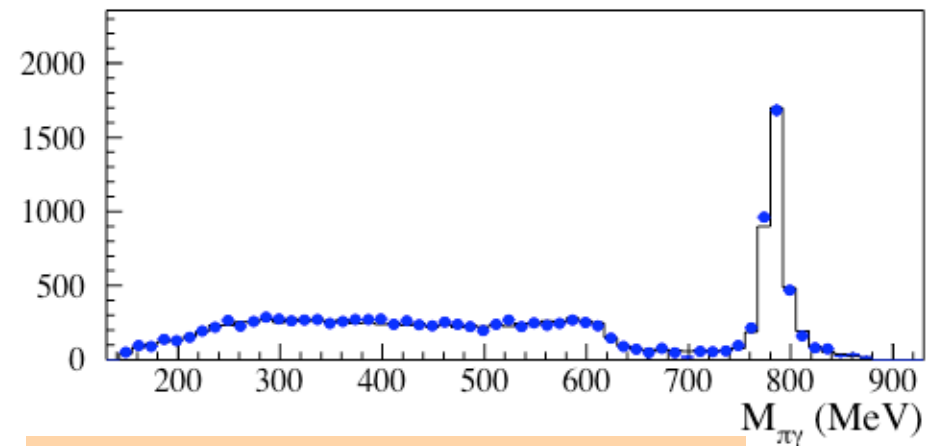
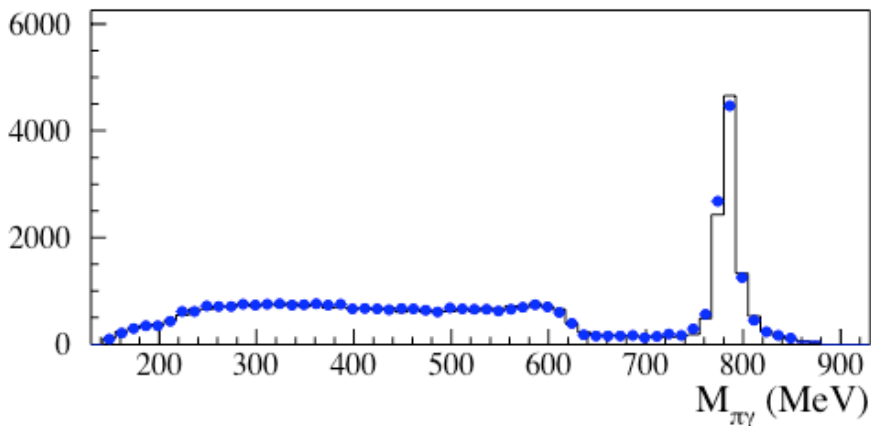
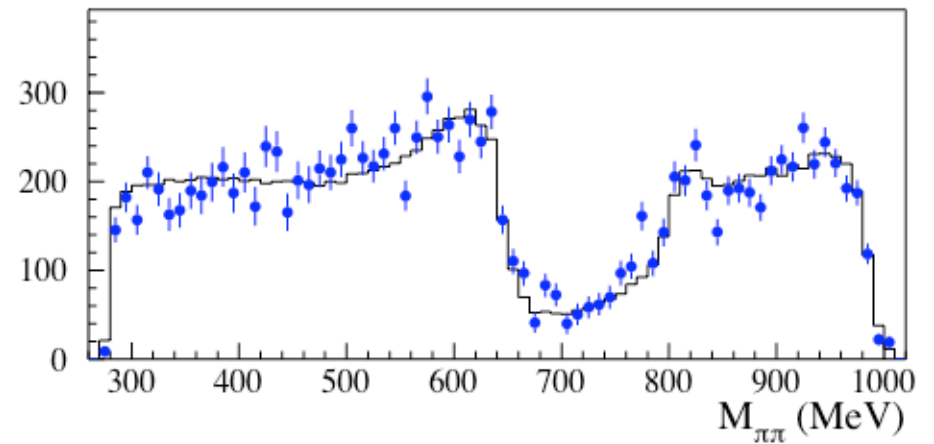
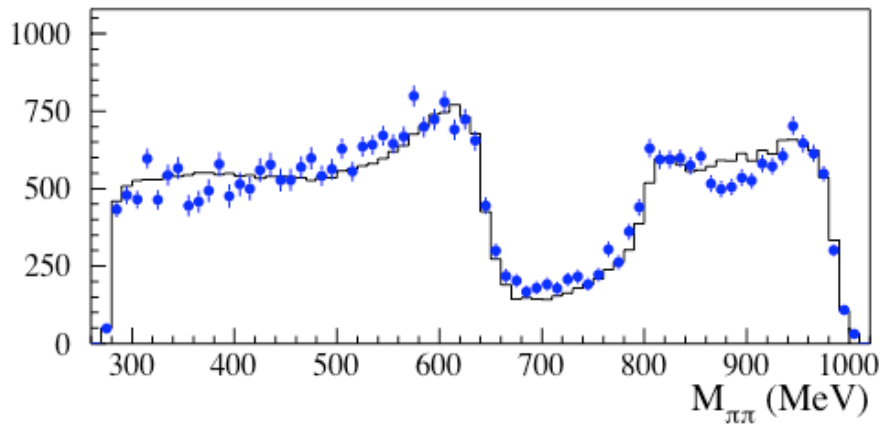


$f_0 + \text{VDM} + M\sigma$ Free

Fit results at $\sqrt{s} = 1019.6 \text{ MeV}$:

	$f_0 + \sigma (M_\sigma \text{ fixed})$	$f_0 + \sigma (M_\sigma \text{ free})$	$f_0 \rightarrow \pi^+\pi^-$
$M_{f_0} \text{ (MeV)}$	987.1 ± 0.1	987.2 ± 0.1	$980 - 987$
$g_{f_0 K^+ K^-} \text{ (GeV)}$	3.53 ± 0.04	3.80 ± 0.07	$3.9 - 6.5$
$g_{f_0 \pi^+ \pi^-} \text{ (GeV)}$	-1.95 ± 0.01	-2.03 ± 0.01	$2.8 - 3.8$
$M_\sigma \text{ (MeV)}$	541	484.6 ± 21.9	
$\alpha_{\rho\pi}(\phi)$	0.76 ± 0.18	0.69 ± 0.05	
$C_{\omega\pi} \text{ (GeV}^{-2}\text{)}$	0.826 ± 0.003	0.827 ± 0.001	
$\phi_{\omega\pi}$	0.21 ± 0.03	0.47 ± 0.05	
$C_{\rho\pi} \text{ (GeV}^{-2}\text{)}$	0.198 ± 0.045	0.62 ± 0.23	
$\phi_{\rho\pi}$	3.14 ± 1.98	3.14 ± 2.45	
$M_\omega \text{ (MeV)}$	782.1 ± 0.3	782.2 ± 0.2	
$\delta_{b\rho} \text{ (degree)}$	7.5 ± 3.2	31.0 ± 4.0	
χ^2/ndf	2862/ 2676	2845 / 2675	
$P(\chi^2)$	0.6 %	1.1 %	

Extrapolating at $\sqrt{s} = 1019.4-1019.8$ MeV:



$\sqrt{s} = 1019.4$ MeV

$\sqrt{s} = 1019.8$ MeV

Not too bad ... by keeping the results of the fit at 1019.6 MeV.
This is an absolute normalization!

No Structure parametrization

G.Isidori, L.Maiani, S.Pacetti, private communication

➤ Flatte-like propagator:
$$\Gamma_{f_0}(s) = (g_{12}^{f_0})^2 \frac{v_\pi(s)}{8\pi s} + (g_{KK}^{f_0})^2 \frac{v_K(s) + v_{K^0}(s)}{8\pi s}$$

Now **we can extract the $g_{S\pi\pi}$, g_{SKK} couplings**
$$v_\alpha(s) = \sqrt{\frac{s}{4} - M_\alpha^2}.$$

➤ New phases related to the particle velocity

➤ Parametrization with the $\sigma(600)$ [M_σ and $g_{\sigma\pi\pi}$ fixed to BES values]

$$F_{\text{Flatté}}^{\text{scal}}(s) = \frac{g_{12}^{f_0} g_{f_0\gamma}^\phi}{s - M_{f_0}^2 + i\sqrt{s}\Gamma_{f_0}(s)} + \frac{a_0 e^{\frac{ib_0 v_\pi(s)}{M_\phi}}}{M_\phi^2} + \frac{a_1 e^{\frac{ib_1 v_\pi(s)}{M_\phi}}}{M_\phi^4} (s - M_{f_0}^2)$$

$$F_S^\sigma(s) = \frac{g_{12}^{f_0} g_{f_0\gamma}^\phi}{s - M_{f_0}^2 + i\Gamma_{f_0}(s)\sqrt{s}} + \frac{a_0 e^{\frac{ib_0 v_\pi(s)}{M_\phi}}}{M_\phi^2} + \frac{g_{12}^\sigma g_{\sigma\gamma}^\phi}{s - M_\sigma^2 + i\Gamma_\sigma(s)\sqrt{s}}$$

b_0 fixed to ensure the proper behaviour of δ_0^0 near the $M_{\pi\pi}$ threshold

Fit results: new No Structure parametrization

	f_0 only	$f_0 + \sigma$	$f_{0 \rightarrow \pi^+\pi^-}$
M_{f_0} (MeV)	987.5 ± 0.4	979.8 ± 0.4	968 – 979
$G_{\phi f\gamma}$ (GeV ⁻¹)	2.83 ± 0.03	2.33 ± 0.02	1.2 – 1.8
$G_{\phi\sigma\gamma}$ (GeV ⁻¹)	—	$(0.0 \pm 0.1) \times 10^{-6}$	
$g_{fK^+K^-}$ (GeV)	0.6 ± 0.1	0.0 ± 5.8	1.2 – 2.8
$g_{f\pi^+\pi^-}$ (GeV)	1.360 ± 0.006	1.209 ± 0.017	0.9 – 1.2
a_0	5.38 ± 0.02	2.81 ± 0.05	6.00 ± 0.02
a_1	2.56 ± 0.02	—	4.10 ± 0.04
b_1 (rad/GeV)	-0.72 ± 0.02	—	3.13 ± 0.05
$\alpha_{\rho\pi}(\phi)$	1.32 ± 0.02	0.92 ± 0.09	
$C_{\omega\pi}$ (GeV ⁻²)	0.952 ± 0.001	0.940 ± 0.007	
$\phi_{\omega\pi}$	0.036 ± 0.009	0.000 ± 0.007	
$C_{\rho\pi}$ (GeV ⁻²)	0.21 ± 0.02	0.29 ± 0.22	
$\phi_{\rho\pi}$	0.65 ± 0.09	2.7 ± 0.3	
M_ω (MeV)	781.70 ± 0.08	782.3 ± 0.2	
δ_{b_ρ} (degree)	87.1 ± 0.5	70 ± 7	
χ^2/ndf	2784.1 / 2672	2981.2 / 2673	
$P(\chi^2)$	6.4%	0.2×10^{-4}	

Summary for the ppg final state

- ❖ **S-dependence of $\pi^0\pi^0\gamma$ x-sec done!**
KLOE memo submitted. For a PLB paper waiting for the new scan data + analysis of $\pi^+\pi^-\pi^0\pi^0$
- ❖ **Fit results to the Dalitz at 1019.6 with new KL parametrization is reasonable !**
+ It has a good $\pi\pi$ phase behaviour and other theoretical advantages.

KLOE memo on the fit to the dalitz-plot in writing.

**PLB paper planned for the KL + NS fit around $M\phi$.
Final blessing expected for Jan 06.**

Summary and Perspectives on $f_0(980)$

1. $f_0(600)$: required in the $\pi^0\pi^0$ channel not in the $\pi^+\pi^-$ one: no clear answer by now ... although the large S/B difference in the spectrum should be considered.

2. Couplings:

with the KL parametrization the $\pi^+\pi^- / \pi^0\pi^0$ final state give results in good agreement:

$$R_{f_0} = (g_{f_0 K^+ K^-} / g_{f_0 \pi^+ \pi^-})^2 = 2 - 4 \quad \text{vs} \quad 3.5 - 3.8$$

$$M_{f_0} = 980 - 987 \text{ MeV} \quad \text{vs} \quad (987.1 \pm 0.1) \text{ MeV}$$

with the NS analysis contradictory results obtained:

$$g_{f_0 K^+ K^-} (\text{GeV}) = 1.6 - 2.3 \quad \text{vs} \quad 0.6$$

$$g_{f_0 \pi^+ \pi^-} (\text{GeV}) = 0.9 - 1.1 \quad \text{vs} \quad 1.36$$

$$g_{\phi f_0 \gamma} (\text{GeV}^{-1}) = 1.2 - 2.0 \quad \text{vs} \quad 2.8$$

$$M_{f_0} (\text{MeV}) = 973 - 981 \quad \text{vs} \quad 987.5$$

suggesting: too much freedom of the parametrization?

KLOE perspectives on scalar mesons

1. Conclude analysis on 2001-2002 data sample for **$f_0(980)$** (neutral final states) and **$a_0(980)$** .
2. With **2000 pb⁻¹ @ ϕ peak**:
 - improvement expected for $f_0 \rightarrow \pi^+\pi^-$
 - combined fit $\pi^+\pi^-$ AND $\pi^0\pi^0$
 - search for $f_0, a_0 \rightarrow KK$
3. With new forthcoming **energy scan data**
 - improved study of the \sqrt{s} -dependence of the cross-section;
 - Off-peak**: “test run” of $\gamma\gamma \rightarrow \pi^0\pi^0$

Fit function: the Achasov parametrization

$$\frac{d\sigma(e^+e^- \rightarrow \pi^0\pi^0\gamma)}{dmdm_{\pi\gamma}} = \frac{\alpha m_{\pi\gamma} m}{3(4\pi)^2 s^3} \left\{ \begin{array}{l} |A_{\text{scalar}}|^2 + \\ \frac{1}{16} F_1(m^2, m_{\pi\gamma}^2) \left| \left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} - C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(m_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(m_{\pi\gamma}^2)} \right|^2 + \\ \frac{1}{16} F_1(m^2, \tilde{m}_{\pi\gamma}^2) \left| \left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} + C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(\tilde{m}_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(\tilde{m}_{\pi\gamma}^2)} \right|^2 + \\ \frac{1}{8} F_2(m^2, m_{\pi\gamma}^2) \text{Re} \left[\left(\left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} + C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(m_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(m_{\pi\gamma}^2)} \right) \times \right. \\ \left. \left(\left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} + C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(\tilde{m}_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(\tilde{m}_{\pi\gamma}^2)} \right)^* \right] \mp \\ \frac{1}{\sqrt{2}} \text{Re} \left[A_{\text{scalar}} \left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} + C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(m_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(m_{\pi\gamma}^2)} \right)^* + \\ F_3(m^2, m_{\pi\gamma}^2) \left(\left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} + C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(m_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(m_{\pi\gamma}^2)} \right)^* + \\ F_3(m^2, \tilde{m}_{\pi\gamma}^2) \left(\left(\frac{e^{i\phi_{\omega\phi}(m_\phi^2)} g_{\phi\gamma} g_{\phi\rho\pi} g_{\rho\pi\gamma}}{D_\phi(s)} + C_{\rho\pi} \right) \frac{e^{i\delta_{b\rho}}}{D_\rho(\tilde{m}_{\pi\gamma}^2)} + \frac{C_{\omega\pi^0}}{D_\omega(\tilde{m}_{\pi\gamma}^2)} \right)^* \right] \right\},
 \end{array} \right.$$

$\alpha_{\rho\pi}(\phi)$ (red arrow pointing to $e^{i\phi_{\omega\phi}(m_\phi^2)}$)
 $f_{0\gamma}$ (blue oval)
 Model dependent term (blue oval)
 $\omega\pi/\rho\pi$ (blue oval)
 Set to +1 (green box)
 $f_{0\gamma}/VP$ interf (blue oval)

[N.N.Achasov, A.V.Kiselev, private communication]

- ✓ VDM free parameters: C_{VP} , $\delta_{b\rho}$, $\alpha_{\rho\pi}(\phi)$, M_ω
- ✓ M_ϕ free or fixed to BES value (541 MeV)

IV - The Forward-Backward asymmetry:

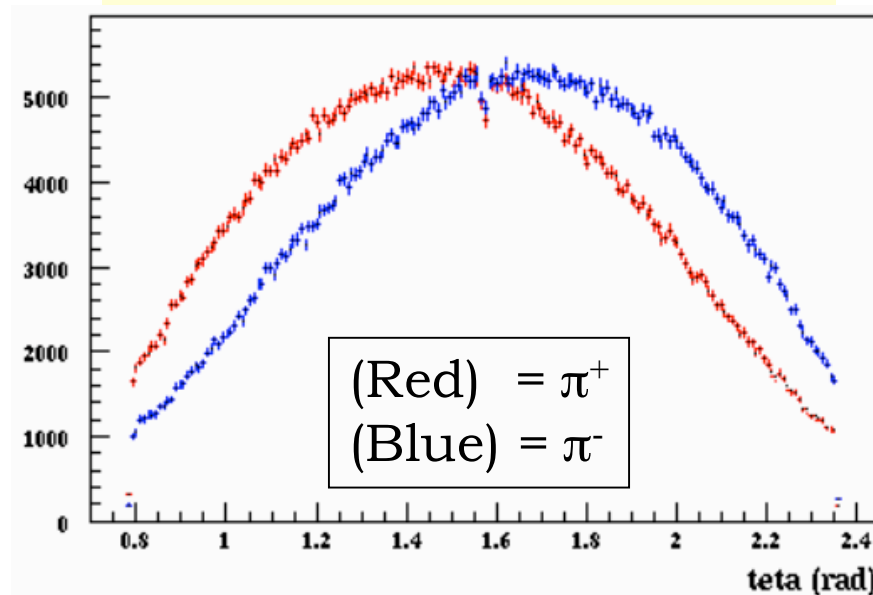
$$\mathbf{A} = (\mathbf{N}(\theta^+ > 90^\circ) - \mathbf{N}(\theta^+ < 90^\circ)) / \text{sum}$$

$\pi^+\pi^-$ system: A(ISR) C-odd

A(FSR) & A(**scalar**) C-even

$$\begin{aligned} \text{Cross-section: } |A(\text{tot})|^2 = & |A(\text{ISR})|^2 + |A(\text{FSR})|^2 + |A(\mathbf{scalar})|^2 \\ & + 2\text{Re}[A(\text{ISR}) A(\text{FSR})] + 2\text{Re}[A(\text{ISR}) A(\mathbf{scalar})] \\ & + 2\text{Re}[A(\text{FSR}) A(\mathbf{scalar})] \end{aligned}$$

Pion polar angle distributions

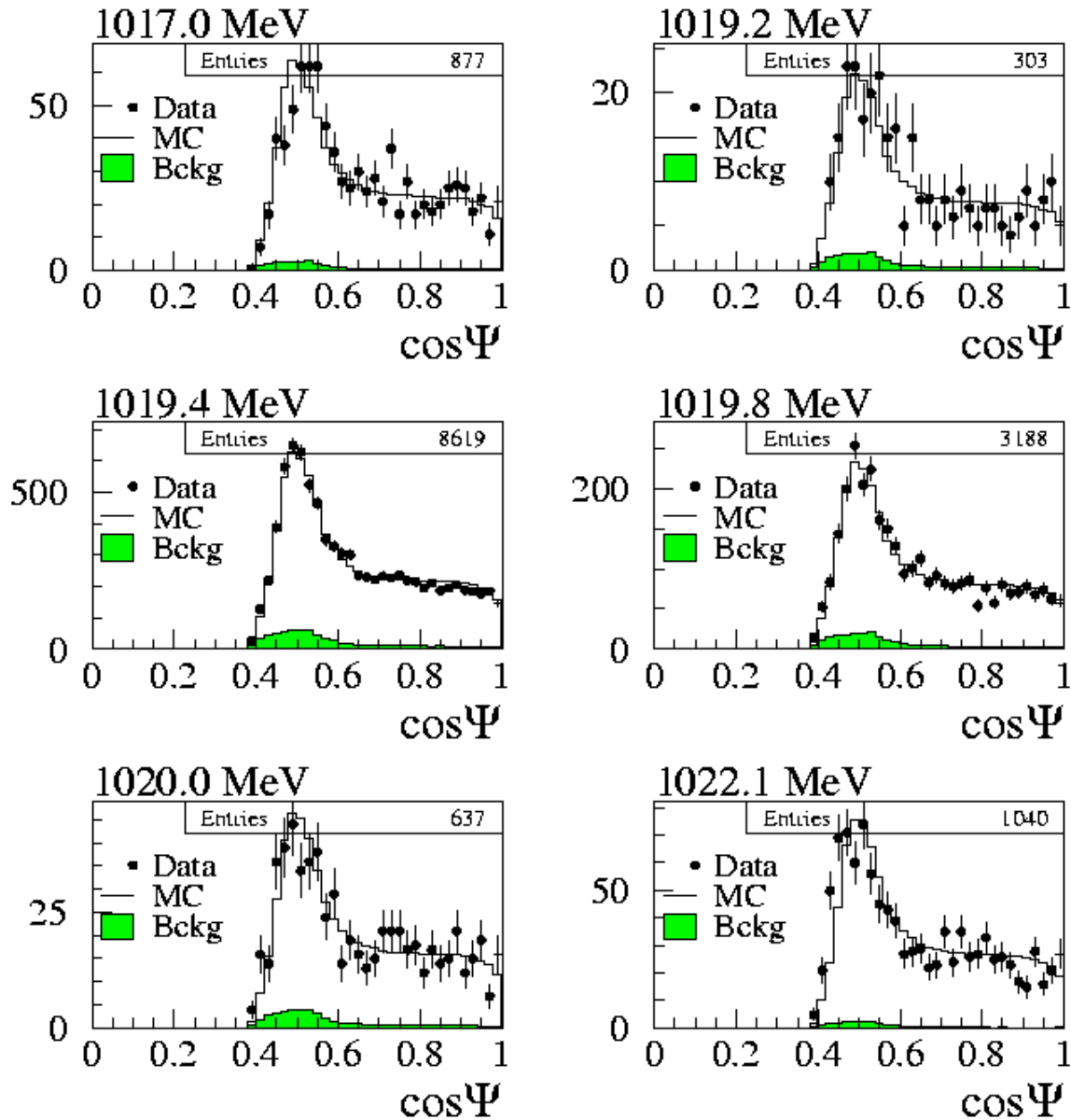


Effect of the scalar amplitude on the FB asymmetry:

Plot of \mathbf{A} in slices of $m(\pi\pi)$;

Comparison with simulation *with* and *without* the scalar amplitude.

$\omega\pi$ events vs \sqrt{s} (angular distributions)



$\omega\pi$: FIT RESULTS to the visible xsec

FIT	σ_0 (nb)	$\Re(Z)$	$\Im(Z)$	σ' (nb/MeV)	χ^2/ Ndof
(A) σ' fixed	0.731 ± 0.035	0.060 ± 0.020	-0.157 ± 0.030	0.0048	5.0/11
(A) σ' fixed	0.748 ± 0.010	0.049 ± 0.016	-0.152 ± 0.007	0.0073	4.8/11
(A) All free	0.756 ± 0.245	0.041 ± 0.040	-0.148 ± 0.124	0.0098 ± 0.0114	4.5/10
FIT	σ_0 (nb)	$\Re(Z)$	$\Im(Z)$	A_1	χ^2/ Ndof
(B) A_1 fixed	0.745 ± 0.014	0.051 ± 0.012	-0.153 ± 0.007	-0.114	5.0/11
(B) A_1 fixed	0.746 ± 0.028	0.050 ± 0.020	-0.153 ± 0.022	-0.150	4.9/11
(B) All free	0.743 ± 0.016	0.054 ± 0.019	-0.154 ± 0.012	-0.005 ± 0.001	5.1/10
FIT	σ_0 (nb)	$\Re(Z)$	$\Im(Z)$	A_1	χ^2/ Ndof
(C) A_1 fixed	0.745 ± 0.011	0.052 ± 0.020	-0.154 ± 0.012	-0.114	5.0/11
(C) A_1 fixed	0.746 ± 0.007	0.051 ± 0.001	-0.154 ± 0.001	-0.150	5.0/11
(C) All free	0.743 ± 0.009	0.055 ± 0.016	-0.154 ± 0.006	-0.012 ± 0.002	5.1/10

$$\sigma_0^{\omega\pi} = (0.75 \pm 0.03_{\text{stat}} \begin{smallmatrix} +0.01 \\ -0.02 \end{smallmatrix}) \text{ nb} \quad (14)$$

$$\Re(Z) = 0.05 \pm 0.02_{\text{stat}} \pm 0.01 \quad (15)$$

$$\Im(Z) = -0.15 \pm 0.02_{\text{stat}} - 0.01 \quad (16)$$

in good agreement and with similar accuracy with respect to SND results [26]: $\sigma_0^{\omega\pi} = (0.74 \pm 0.02_{\text{stat}} \pm 0.04_{\text{syst}}) \text{ nb}$, $\Re(Z) = 0.025 \pm 0.035$, $\Im(Z) = -0.19 \pm 0.05$.