



Updates on the π/μ analysis for pion formfactor

Peter A. Lukin, Graziano Venanzoni
Budker Institute for Nuclear Physics
Laboratori Nazionali di Frascati



Outline

- ✓ Introduction
- ✓ Background subtraction
 - Bhabha spectrum shape from Experimental Data sample (Background I)
 - Bhabha spectrum shape from MC Simulation Data sample (Background II)
- ✓ Data/MC comparison in different Q² slices
- ✓ Simulation crosschecks
- ✓ Conclusion

Introduction

Goal: To measure charged pion formfactor using $N_{\pi\pi}/N_{\mu\mu}$ ratio

Subtask: To perform comparison of DATA/MC for $\mu^+\mu^-\gamma$ events

DATA and MC samples, used in the work:

✓ Experimental Data Runs 23542 - 27079, Luminosity Integral is 241.38 pb⁻¹

✓ $\pi\pi\gamma$ MC Simulation Runs 23587 - 27079, Phokhara Generator, Luminosity Integral is 240.19 pb⁻¹(× 6)

✓ $\mu\mu\gamma$ MC Simulation Runs 23546 - 27079, Phokhara Generator, Luminosity Integral is 240.64 pb⁻¹(× 6)

✓ $e\bar{e}\gamma$ MC Simulation Runs 23546 - 27079, Phokhara Generator, Luminosity Integral is 236.57 pb⁻¹(× 6)

Comparison is performed in integral over all Q^2 as well as in different Q^2 bins

Parameters for comparison are trackmass and polar angles of muons

LikelyHood Cut Definition

Legend: "+" - $\text{LogRL} > 0$, "-" - $\text{LogRL} < 0$

| LikelyHood Cut | First track | Second Track |
|----------------|-------------|--------------|
| OR | + | + |
| | + | - |
| | - | + |
| XOR | + | - |
| | - | + |
| NOR | - | - |

LikelyHood Cut Definition (Cont.d)

OR LikelyHood is used in DATA analysis

NOR LikelyHood is used to determine Bhabha spectrum shape

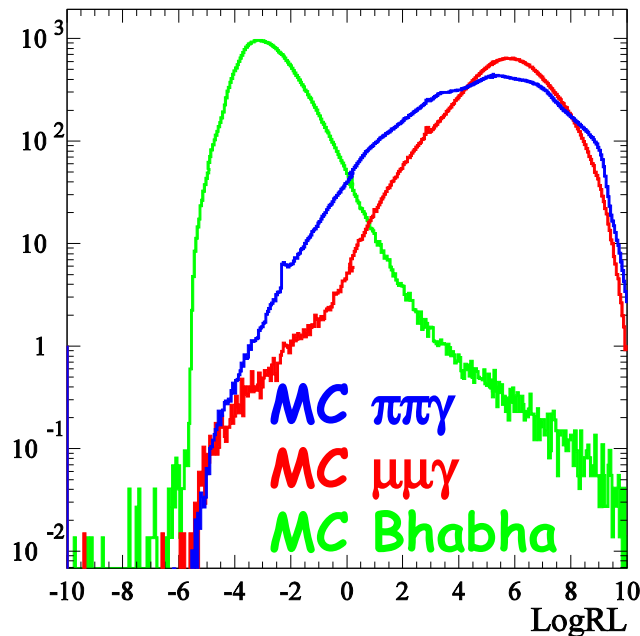
XOR LikelyHood is used to determine scale factor for NOR Bhabha spectrum

$$\text{LogRL} > 0 \Rightarrow \pi, \mu \quad \text{LogRL} < 0 \Rightarrow e$$

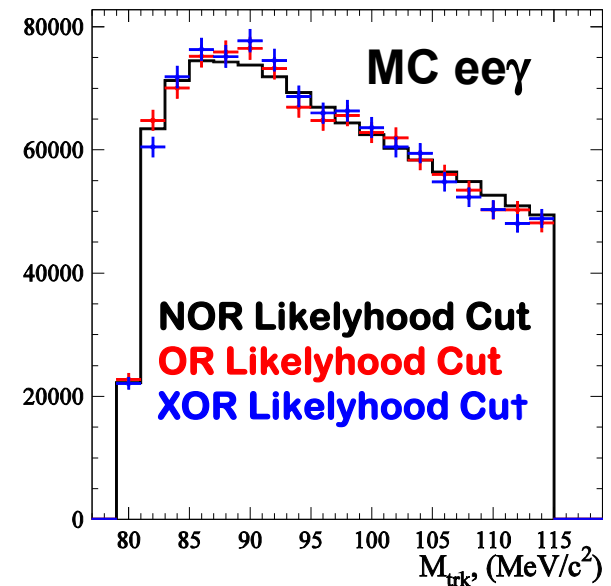
$$I. \varepsilon_e^1 = \varepsilon(\text{LogRL} < 0) \approx 98.5\% \Rightarrow \rho = 1 - \varepsilon_e^1 \approx 1.5\% \Rightarrow \text{NOR} \Leftrightarrow \text{pure } e^+e^-$$

$$II. W_{ee}^{OR} = W_{ee}^{XOR} + W_{ee}^{AND} = W_{ee}^{XOR} \cdot \left(1 + \frac{W_{ee}^{AND}}{W_{ee}^{XOR}} \right) = W_{ee}^{XOR} \cdot \left(1 + \frac{\rho}{2 \cdot \varepsilon_e^1} \right) = W_{ee}^{XOR} \cdot (1 + 0.008)$$

$$W_{ee}^{OR} \cong W_{ee}^{XOR}$$



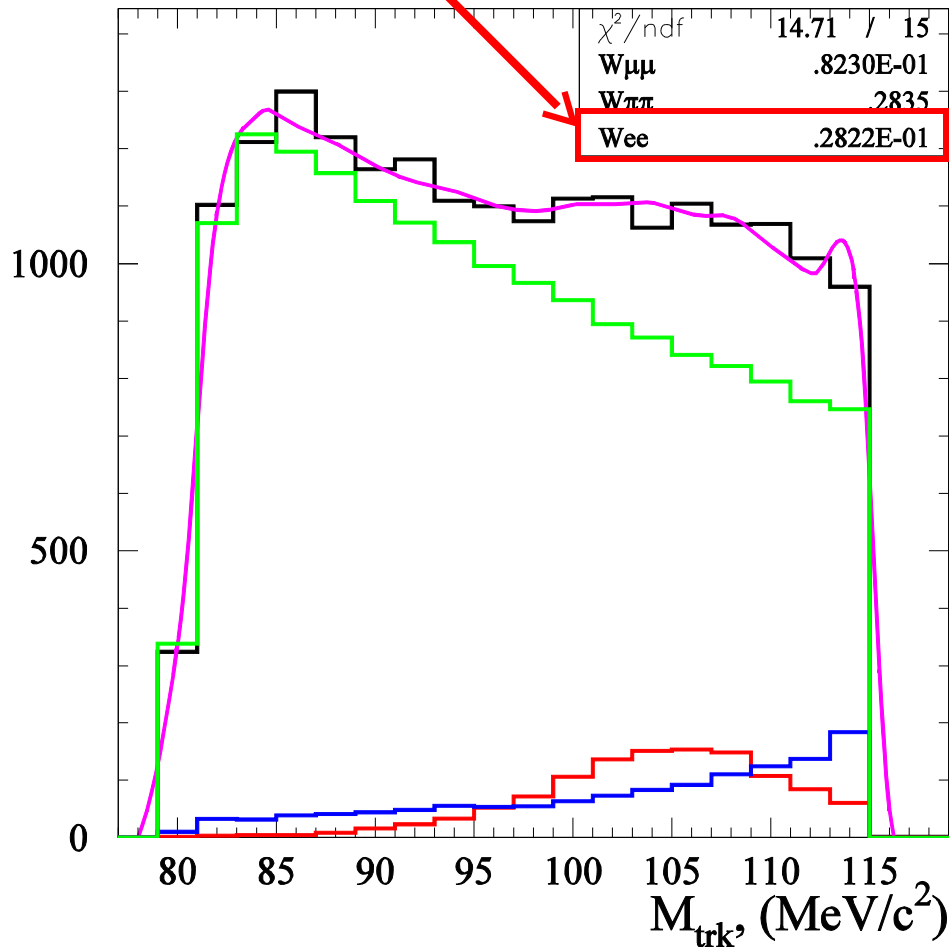
The shape eeg (NOR) is consistent with eeg (OR)



Trackmass

Background subtraction I (scale factor)

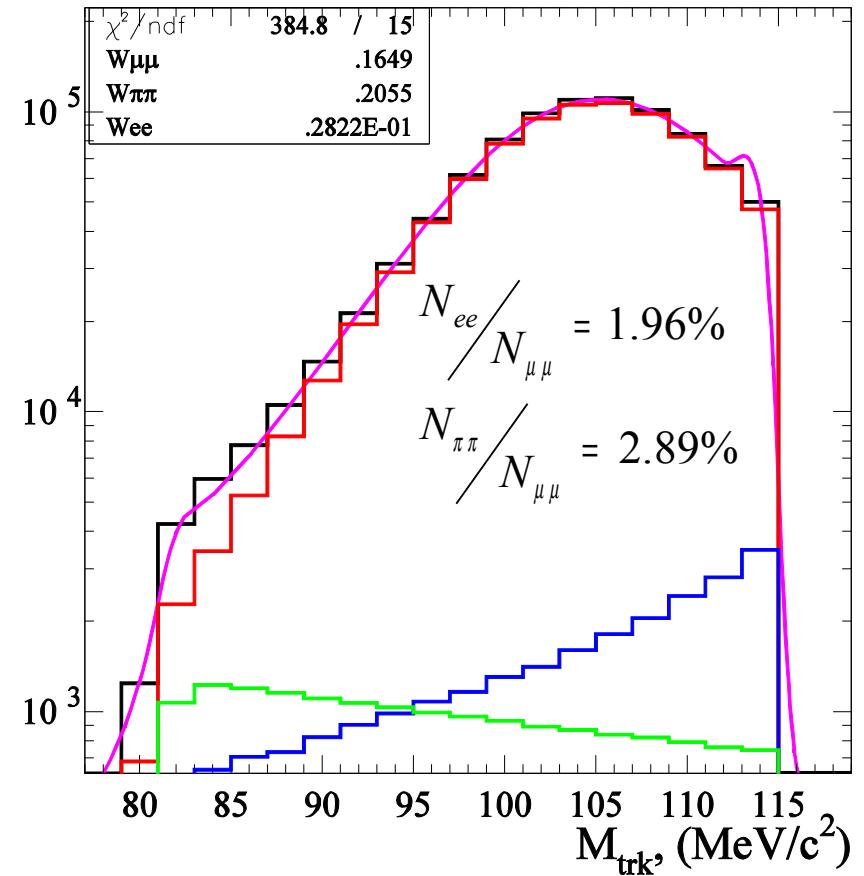
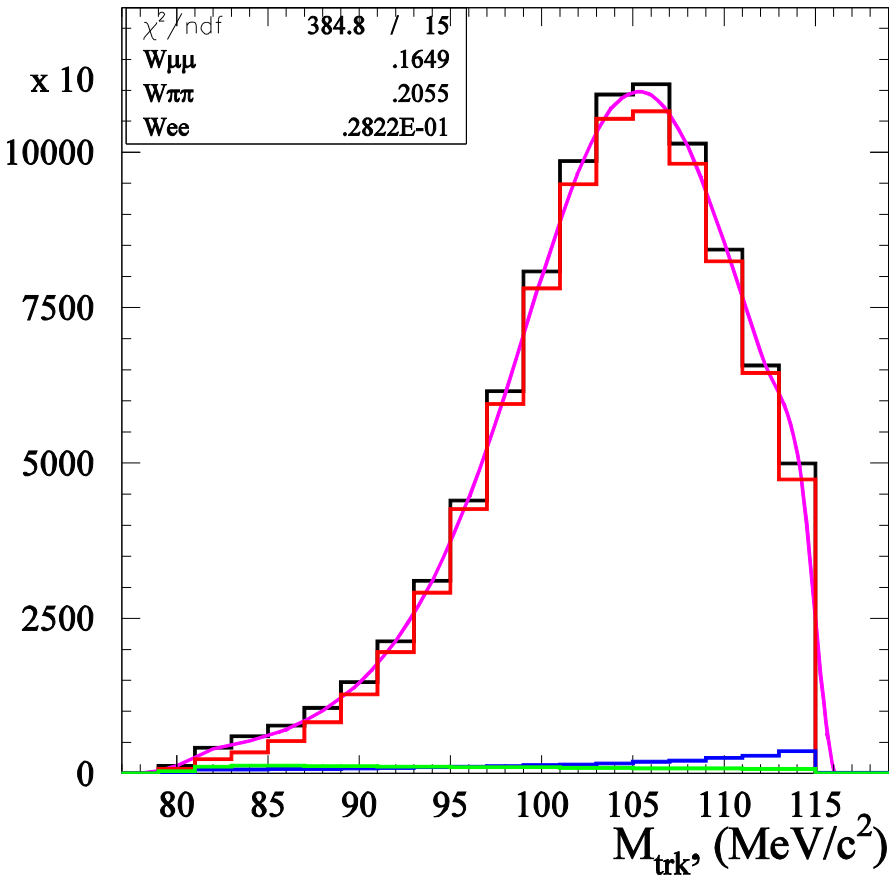
$$F_{DATA}^{XOR}(M) = W_{ee\gamma}^{XOR} \cdot f_{DATA}^{XOR}(M) + W_{\pi\pi\gamma}^{XOR} \cdot f_{MC\pi\pi\gamma}^{XOR}(M) + W_{\mu\mu\gamma}^{XOR} \cdot f_{MC\mu\mu\gamma}^{XOR}(M)$$



$ee\gamma$ is green
 $\pi\pi\gamma$ is blue
 $\mu\mu\gamma$ is red
Fitting function is magenta

Background subtraction I (Fit)

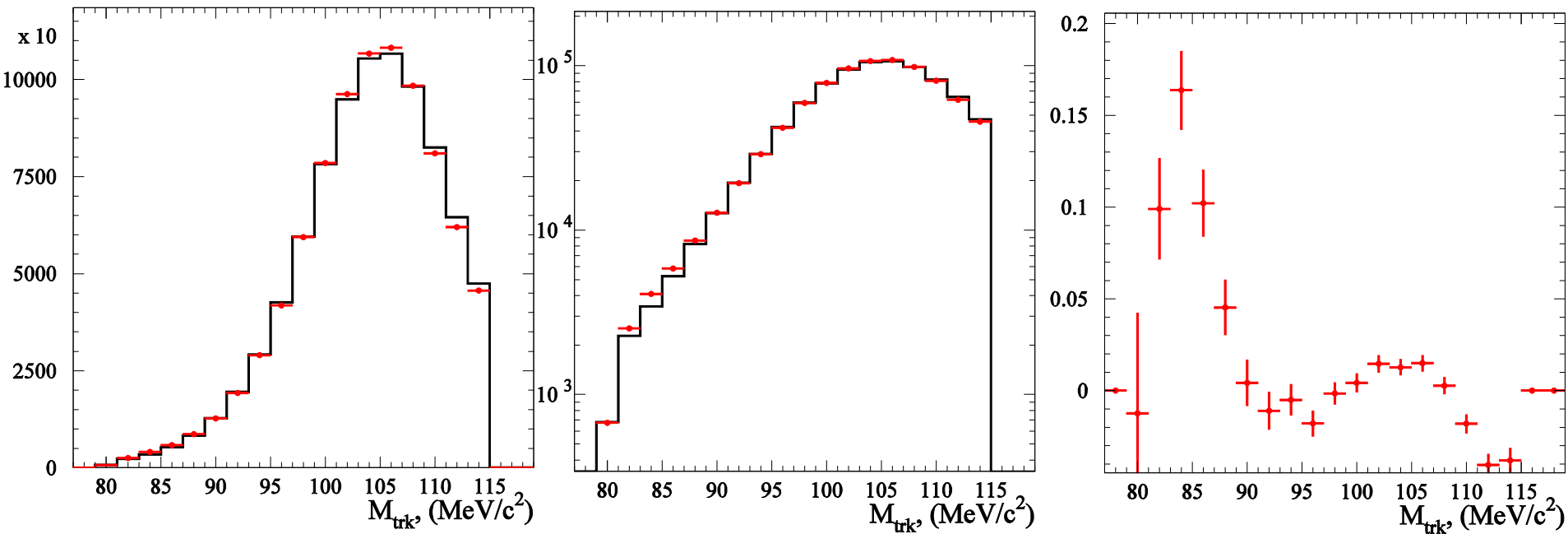
$$F_{DATA}^{OR}(M) = W_{ee\gamma}^{XOR} \cdot f_{DATA}^{NOR}(M) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\pi\pi\gamma}^{OR}(M) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\mu\mu\gamma}^{OR}(M)$$



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction I (Results)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

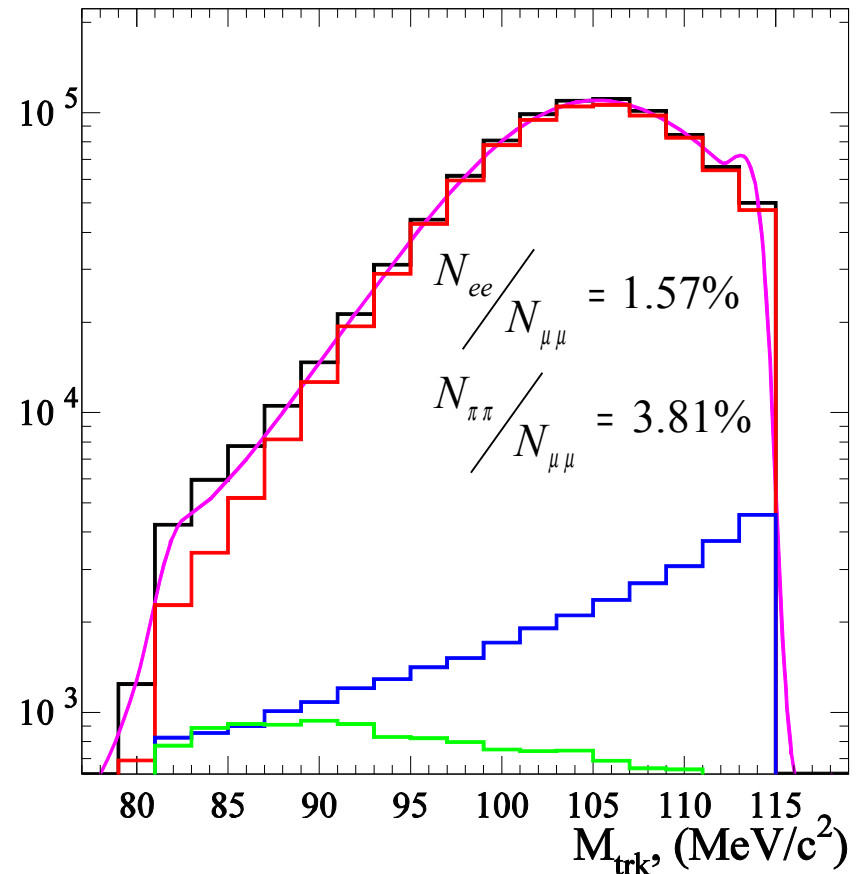
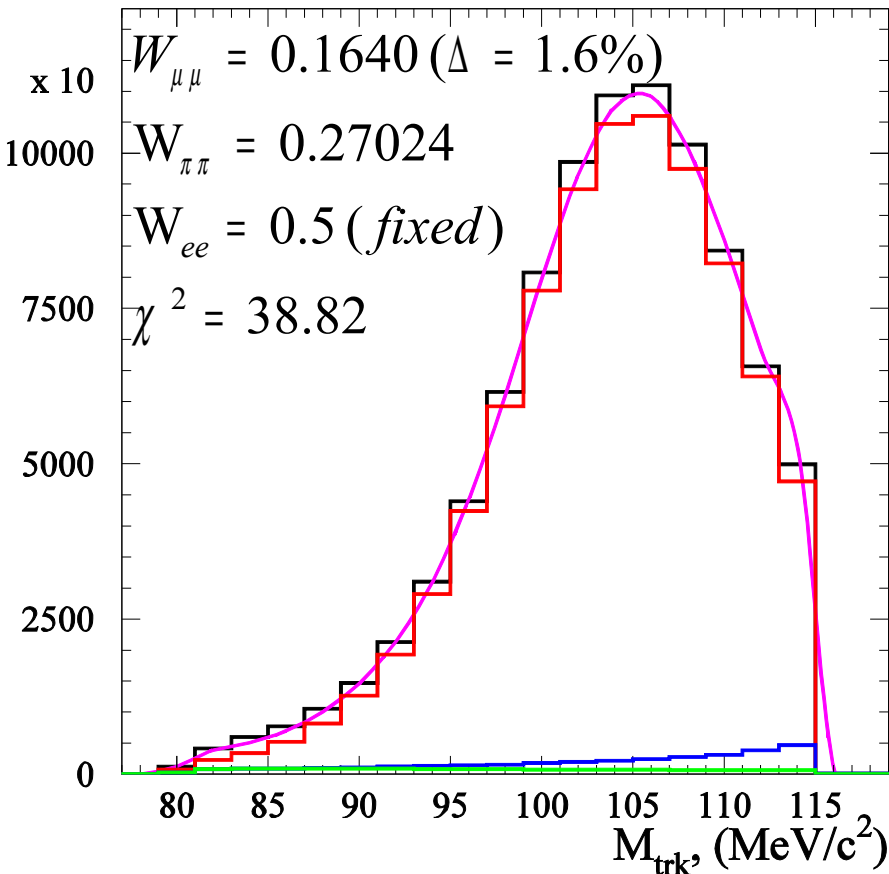


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 1)

$$F_{DATA}^{OR}(M) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(M) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(M) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(M)$$

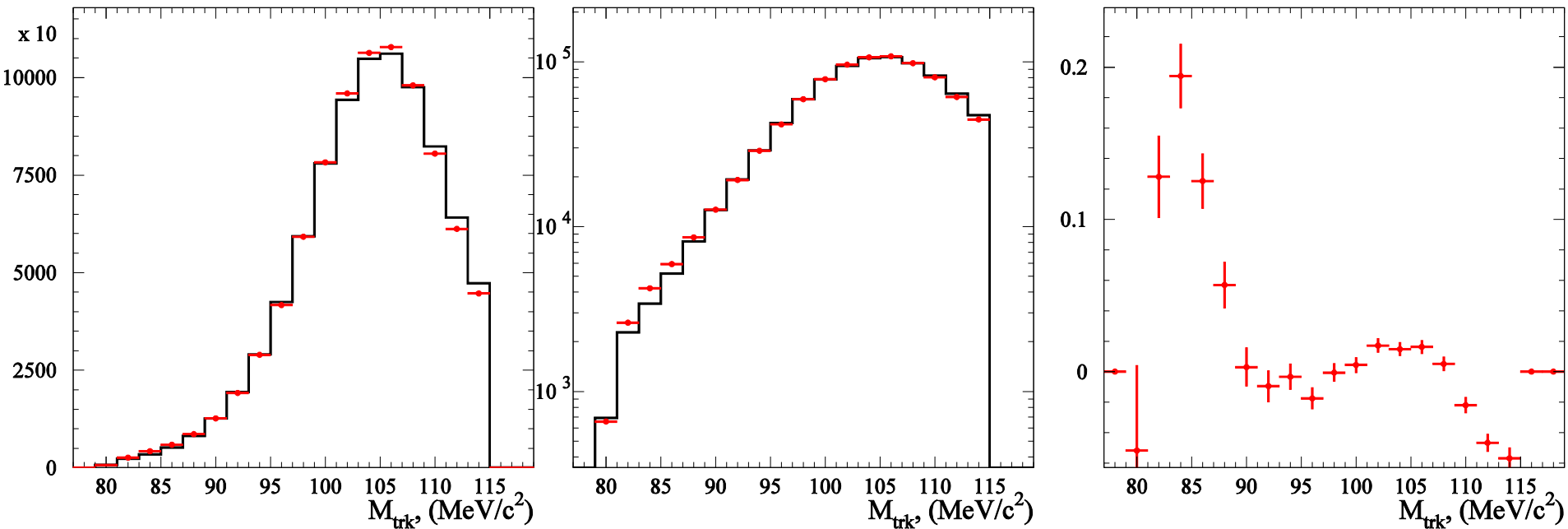
Wee is fixed according to luminosity. $W_{\mu\mu}$, $W_{\pi\pi}$ are free



ee γ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 1)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

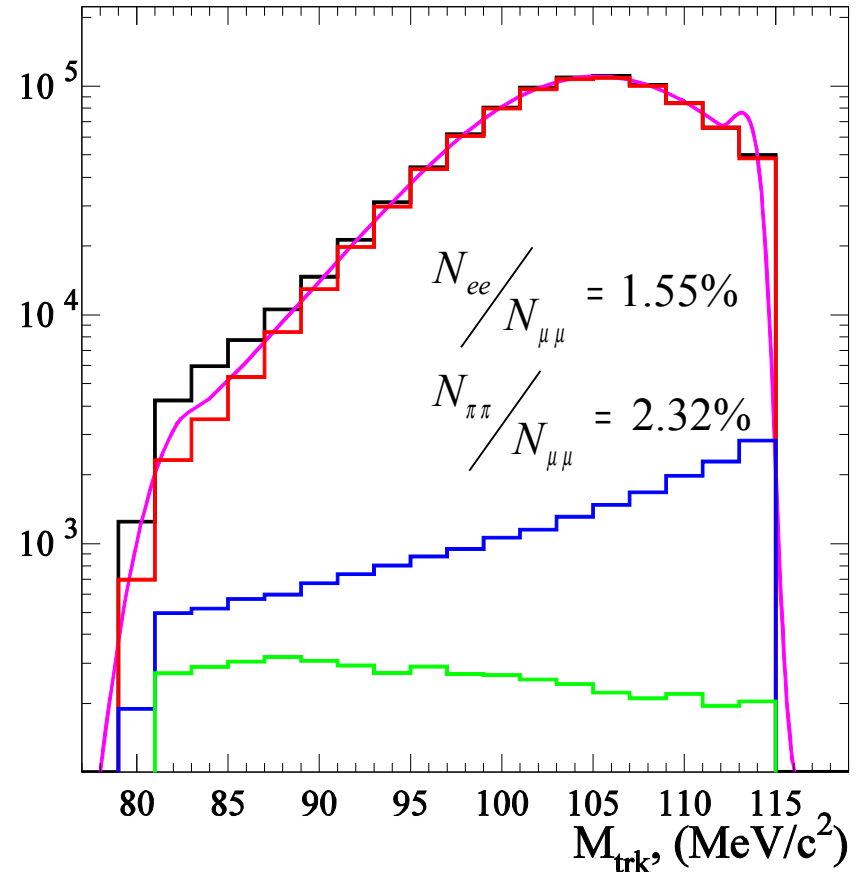
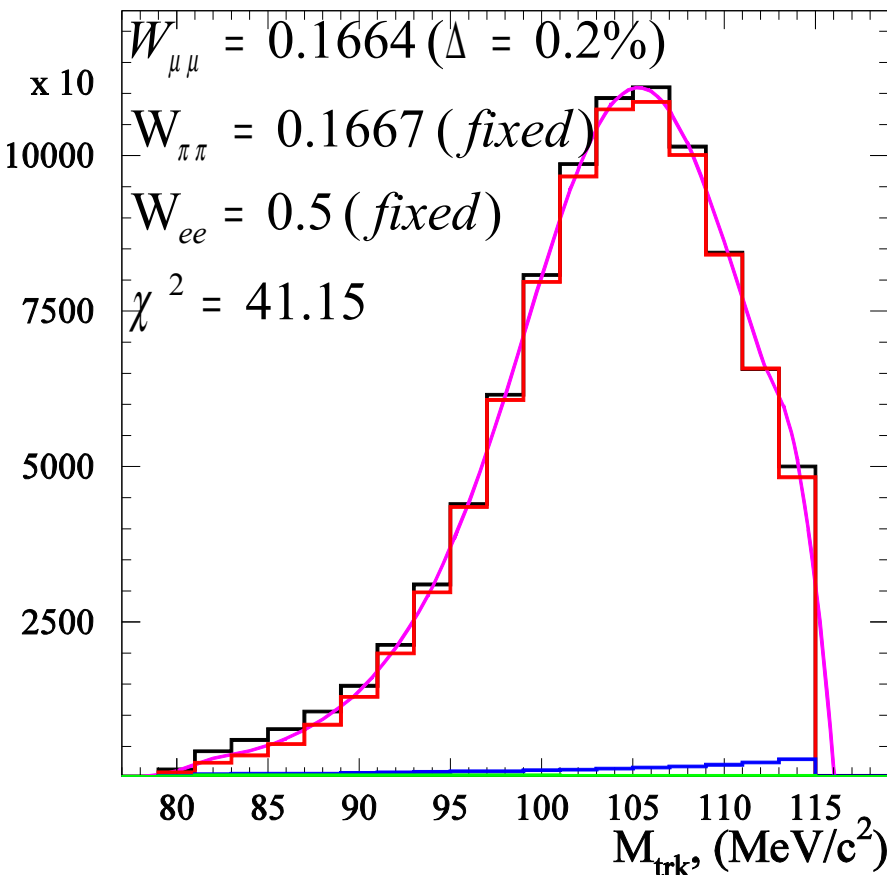


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 2)

$$F_{DATA}^{OR}(M) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(M) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(M) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(M)$$

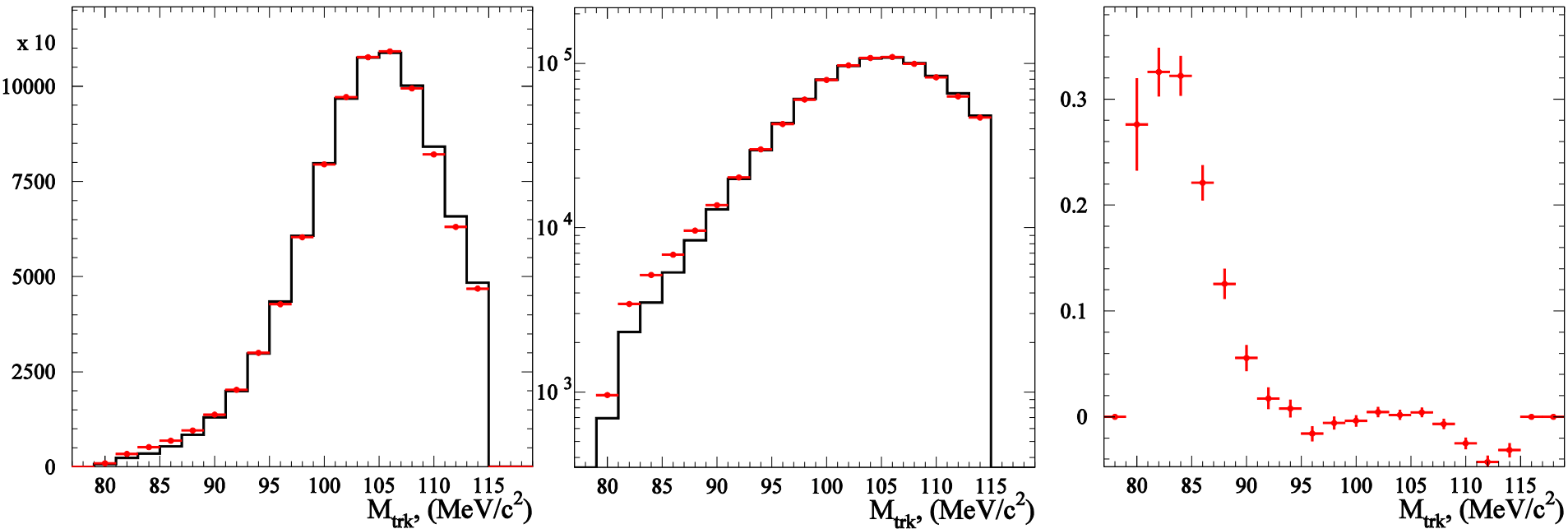
W_{ee} , $W_{\pi\pi}$ are fixed according to luminosity. $W_{\mu\mu}$ is free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 2)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

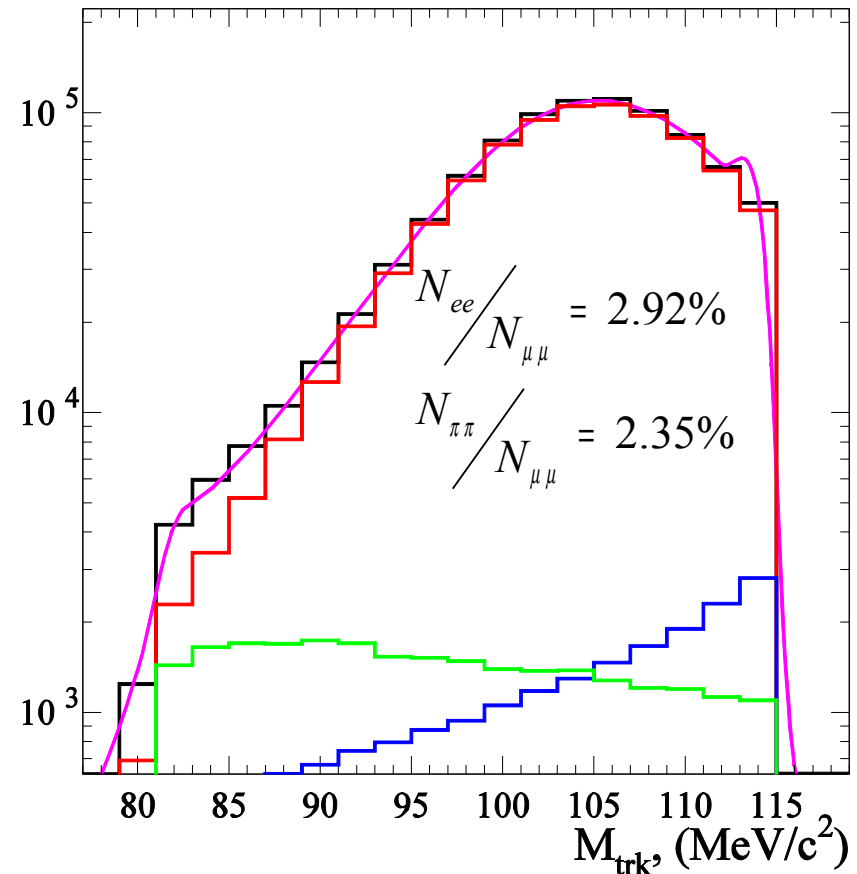
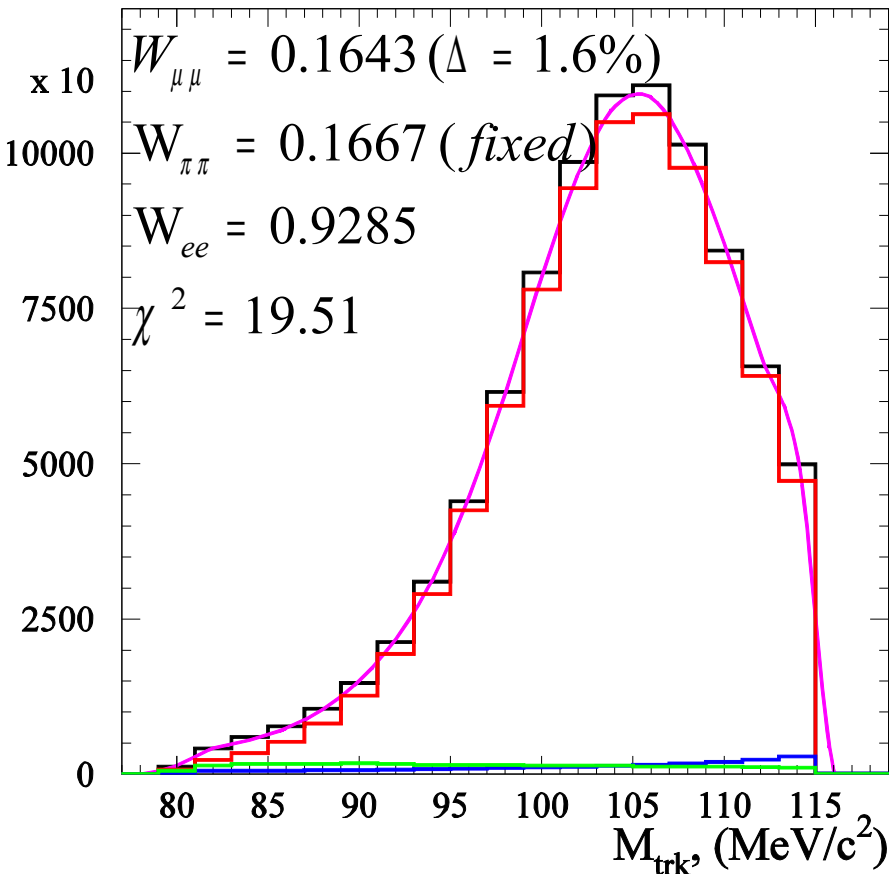


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 3)

$$F_{DATA}^{OR}(M) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(M) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(M) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(M)$$

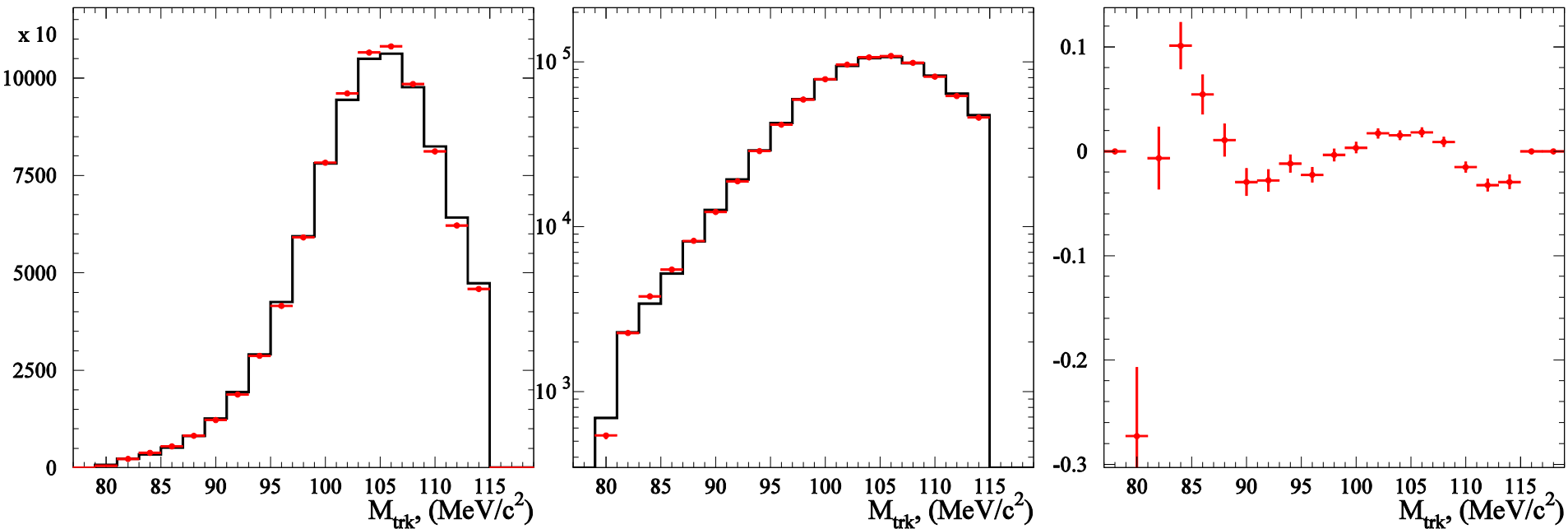
$W_{\pi\pi}$ is fixed according to luminosity. $W_{\mu\mu}, W_{ee}$ are free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 3)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction



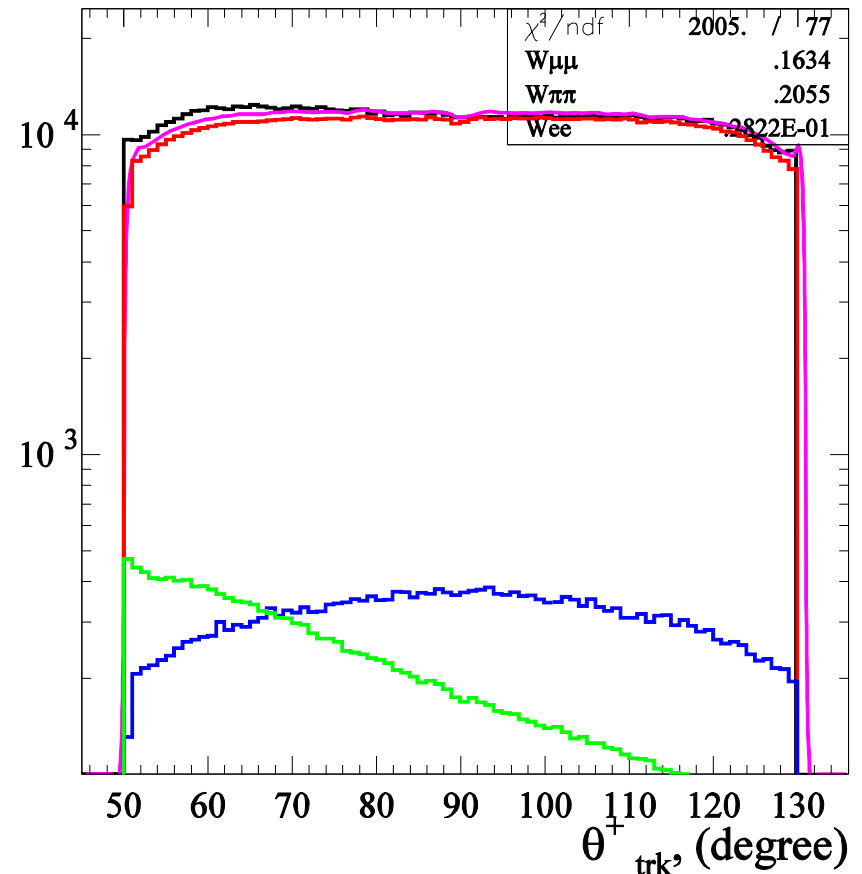
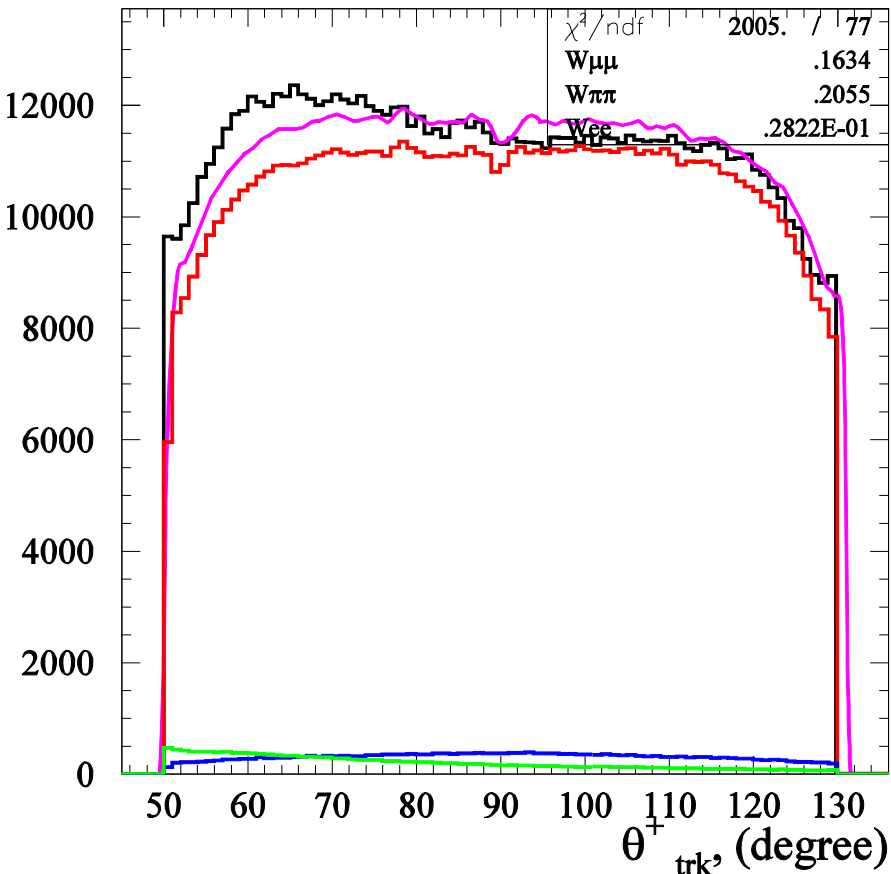
$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Positive muon polar angle

Background subtraction I (Fit)

$$F_{DATA}^{OR}(\theta^+) = W_{ee\gamma}^{XOR} \cdot f_{DATA}^{NOR}(\theta^+) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\pi\pi\gamma}^{OR}(\theta^+) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\mu\mu\gamma}^{OR}(\theta^+)$$

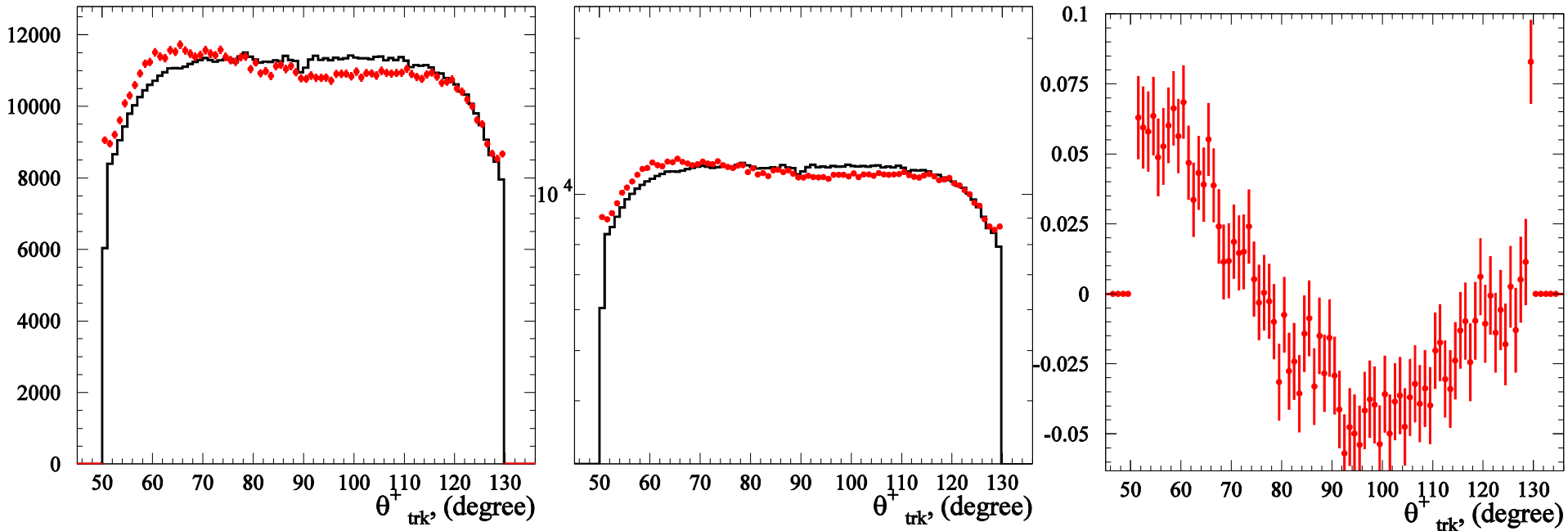
W_{ee} , $W_{\pi\pi}$ are fixed from trackmass, $W_{\mu\mu}$ is free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction I (Results)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

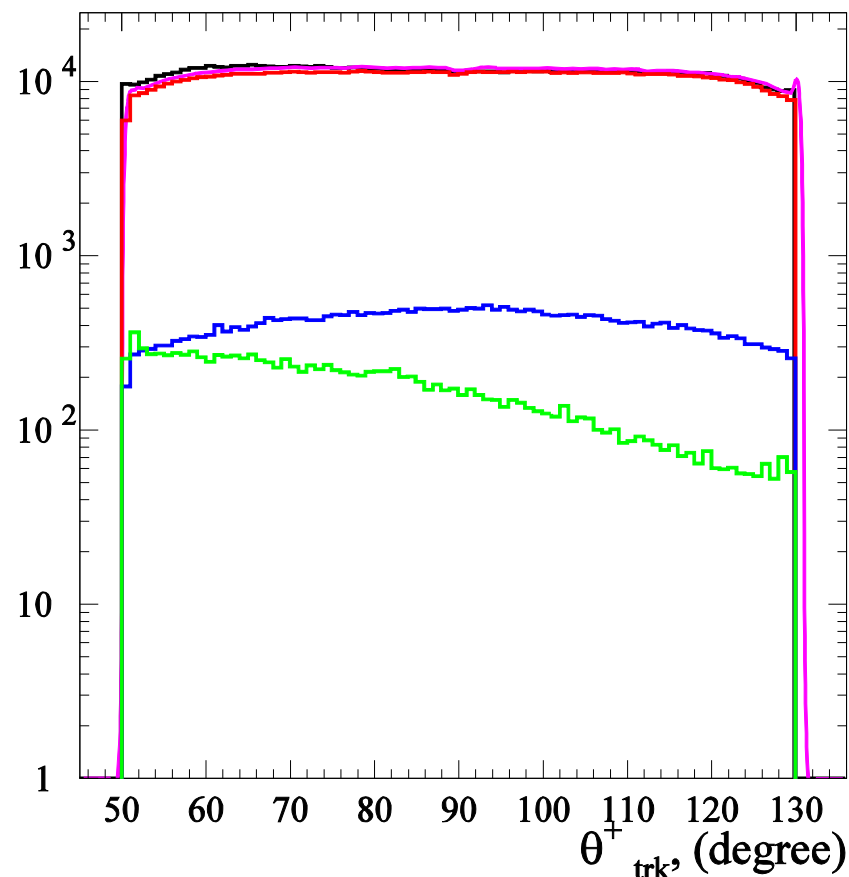
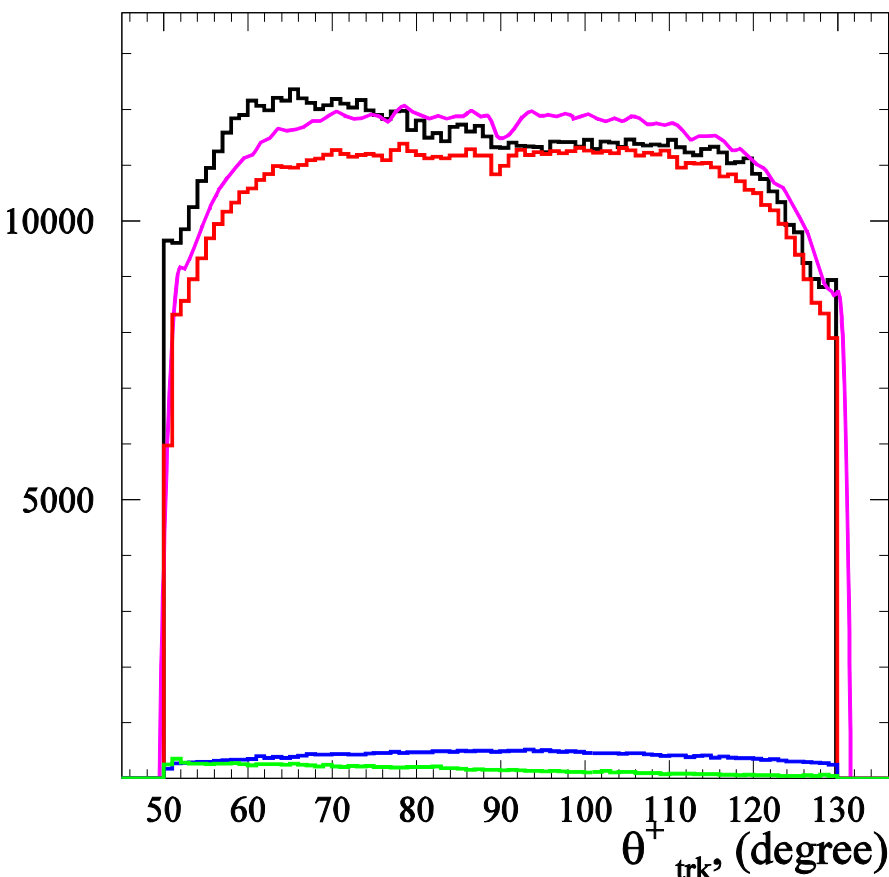


$$\text{Relative difference} = (\text{EXP}-\text{MC})/\text{EXP}$$

Background subtraction II (Fit 1)

$$F_{DATA}^{OR}(\theta^+) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(\theta^+) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(\theta^+) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(\theta^+)$$

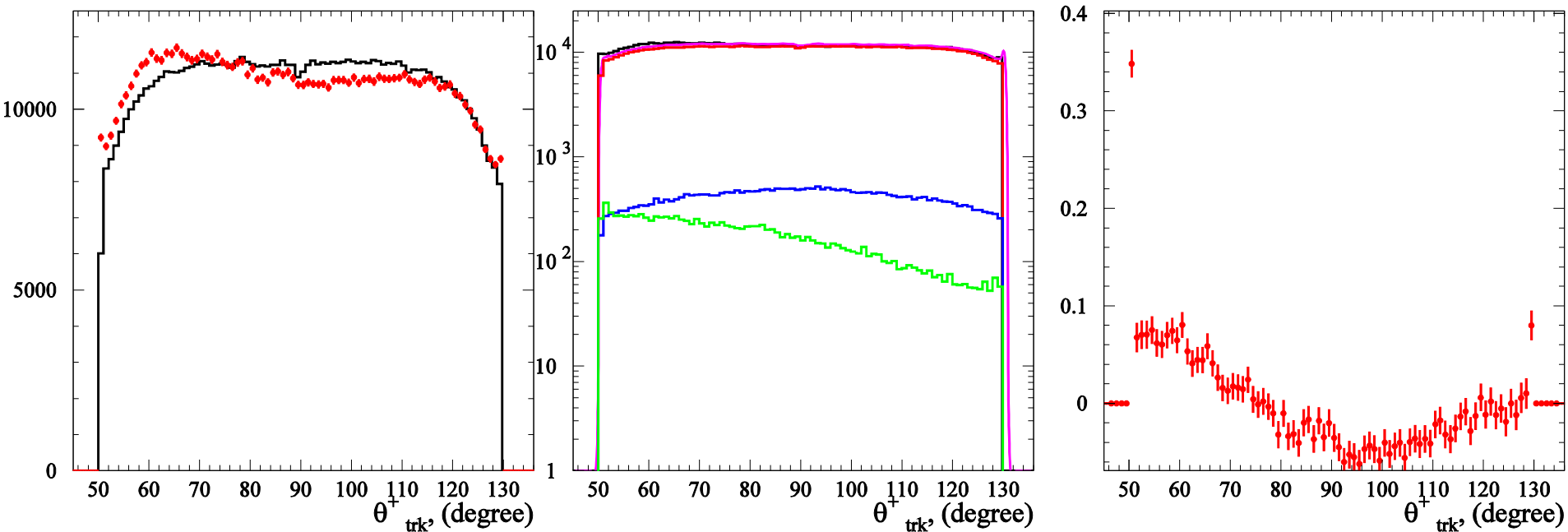
Wee is fixed according to luminosity, $W_{\mu\mu}$, $W_{\pi\pi}$ are free



eeγ is green, ππγ is blue, μμγ is red, fitting function is magenta

Background subtraction II (Results Fit 1)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

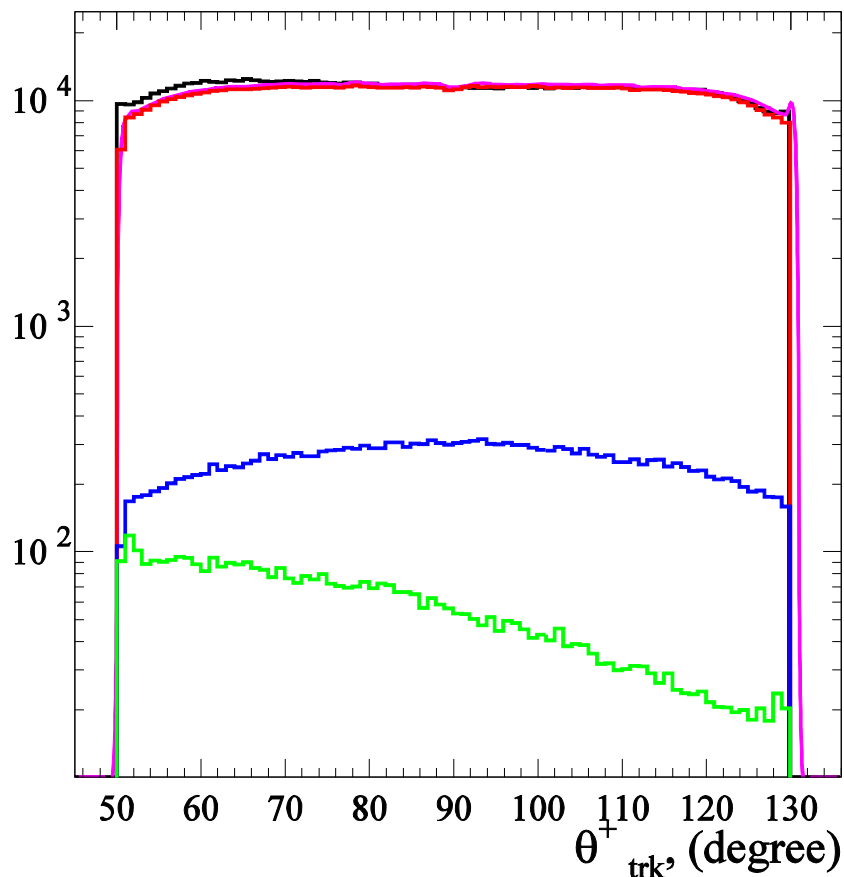
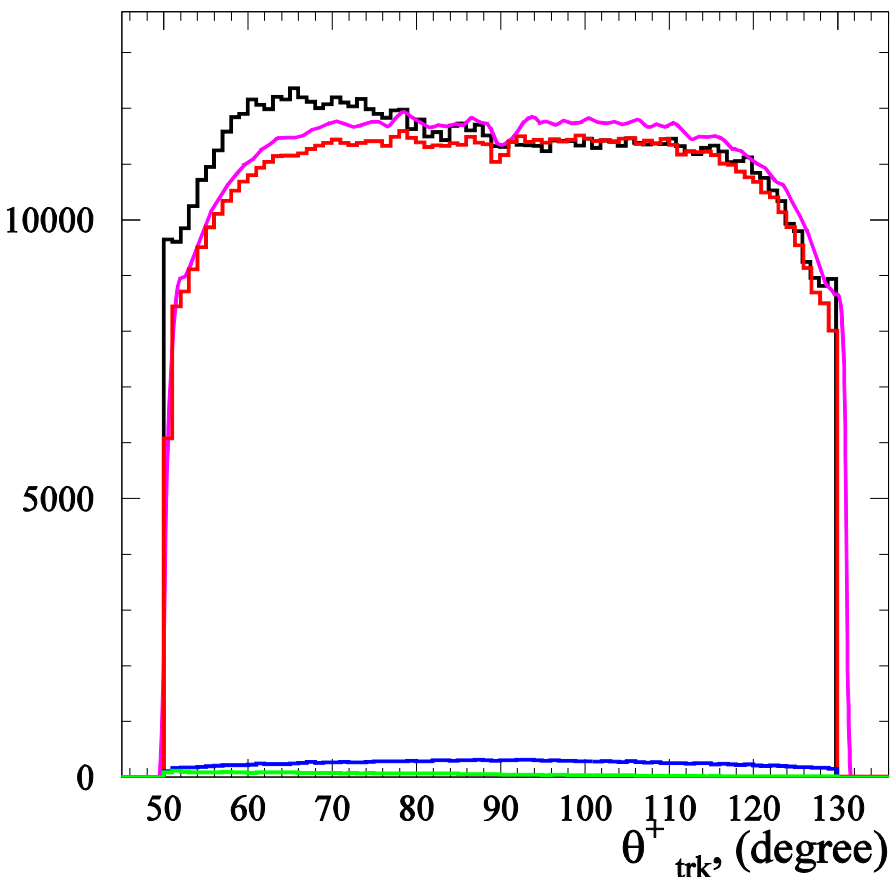


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 2)

$$F_{DATA}^{OR}(\theta^+) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(\theta^+) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(\theta^+) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(\theta^+)$$

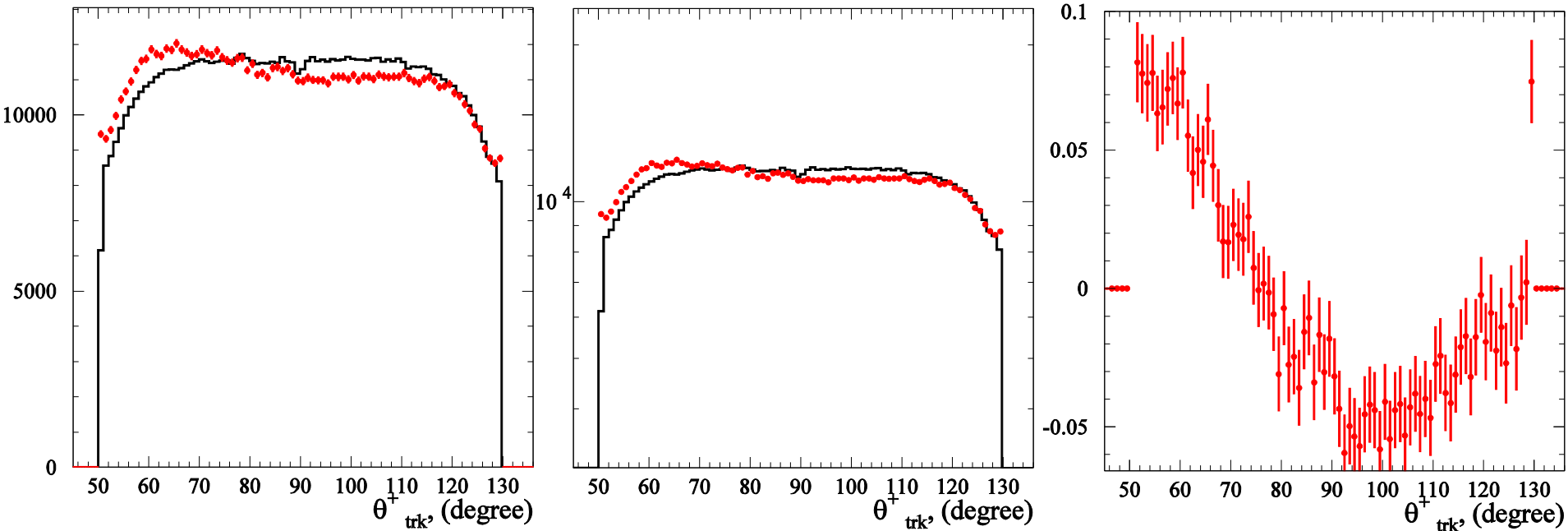
$W_{ee}, W_{\pi\pi}$ are fixed according to luminosity, $W_{\mu\mu}$ is free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 2)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

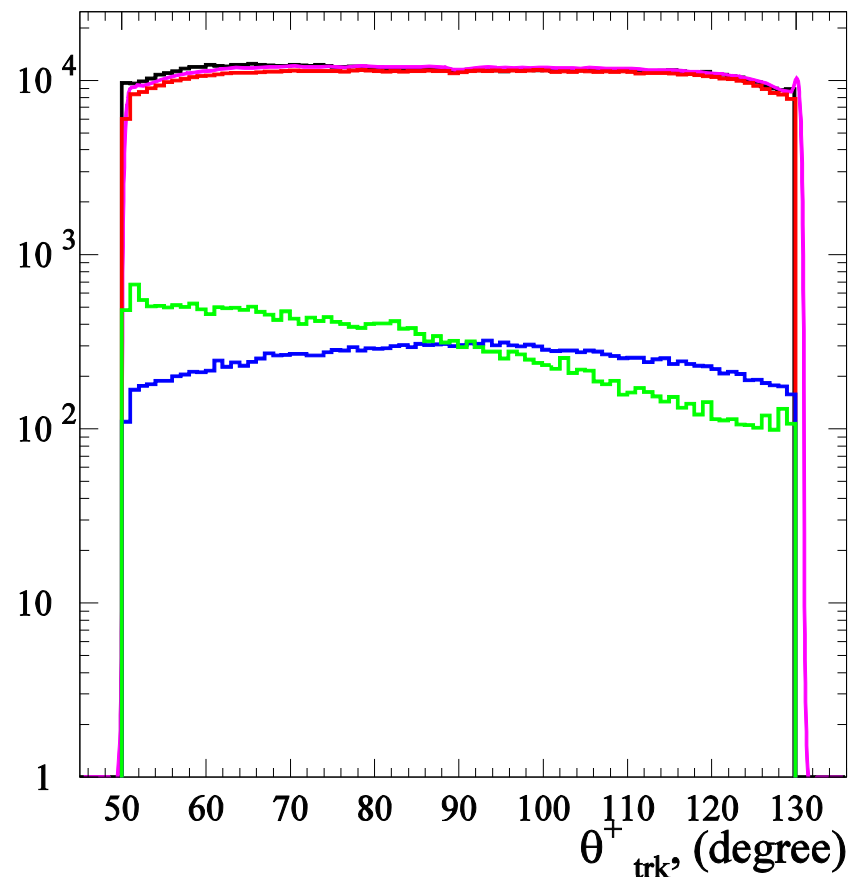
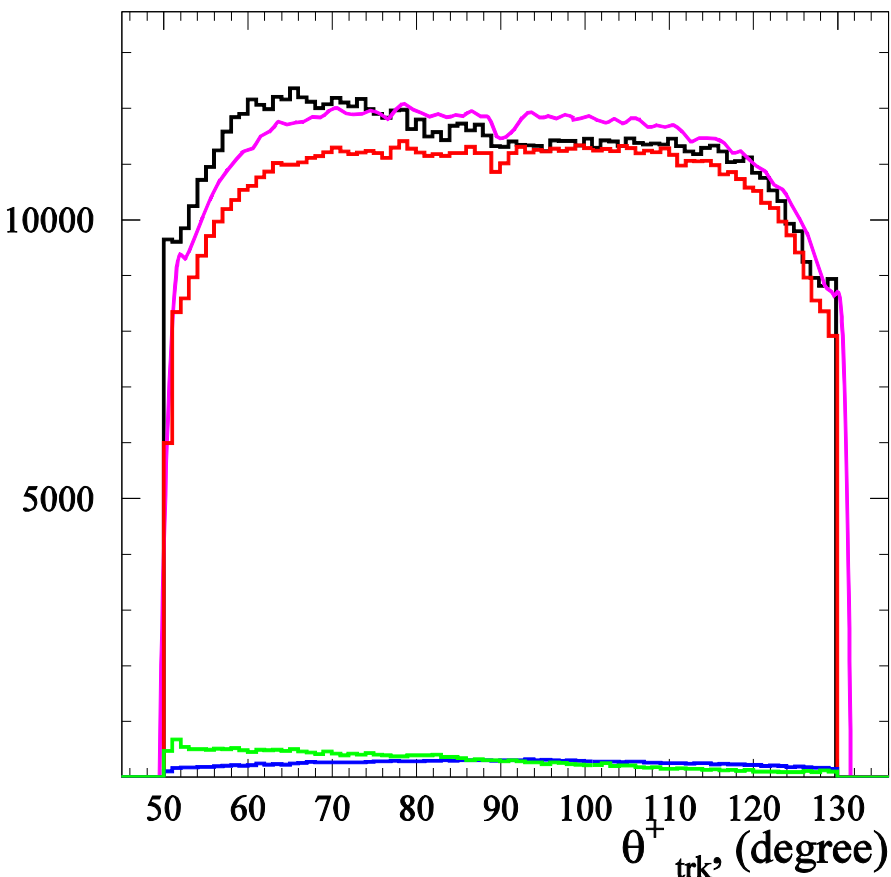


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 3)

$$F_{DATA}^{OR}(\theta^+) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(\theta^+) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(\theta^+) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(\theta^+)$$

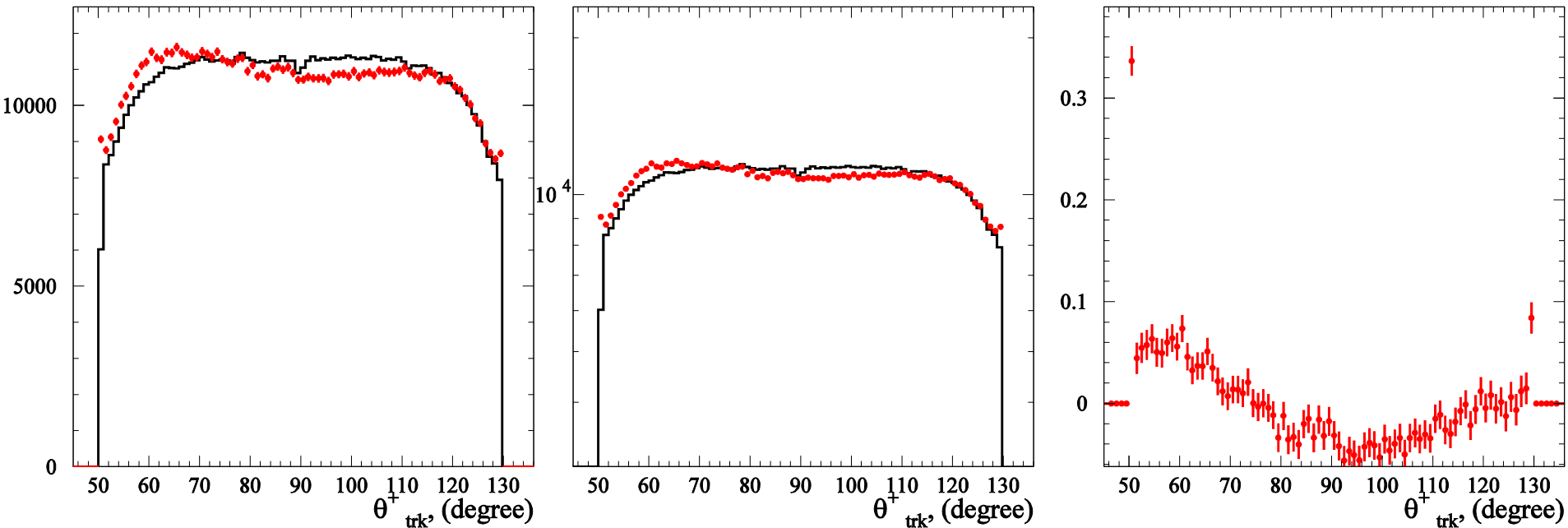
$W_{\pi\pi}$ is fixed according to luminosity, $W_{\mu\mu}$, W_{ee} are free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 3)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction



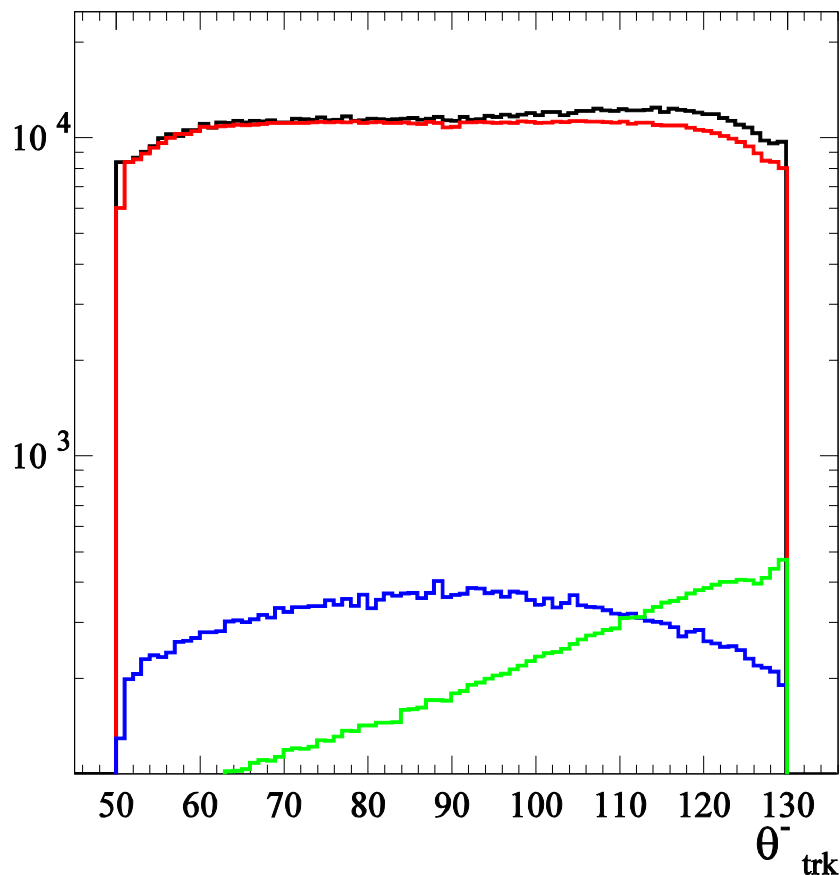
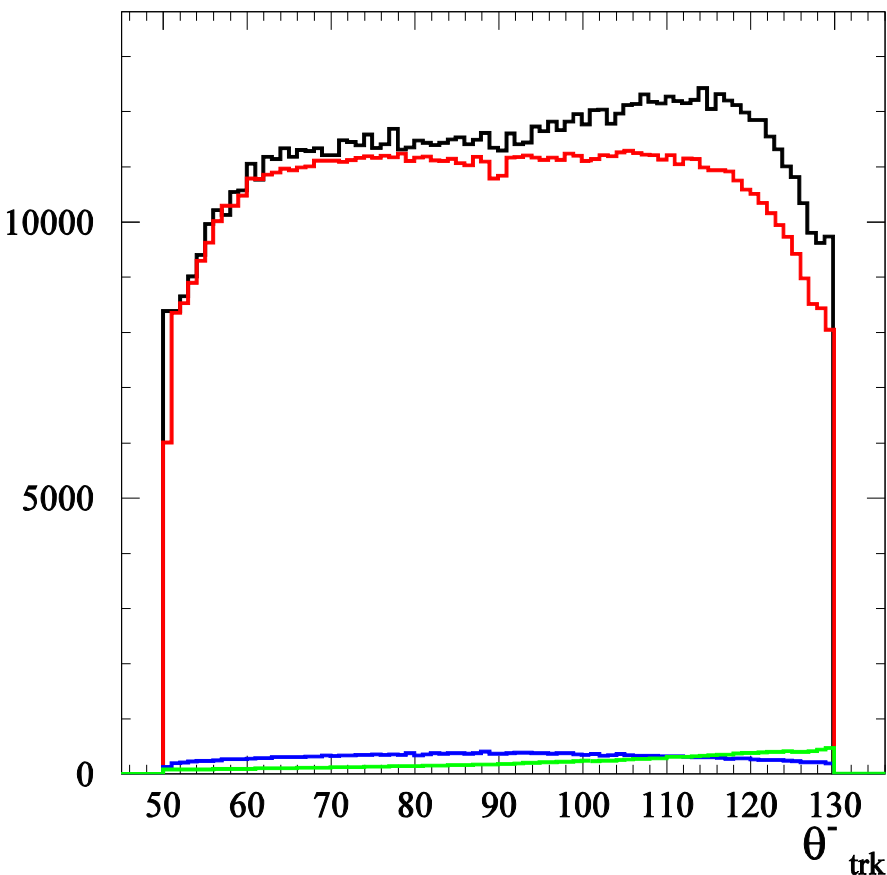
$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Negative muon polar angle

Background subtraction I (Fit)

$$F_{DATA}^{OR}(\theta^-) = W_{ee\gamma}^{XOR} \cdot f_{DATA}^{NOR}(\theta^-) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\pi\pi\gamma}^{OR}(\theta^-) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\mu\mu\gamma}^{OR}(\theta^-)$$

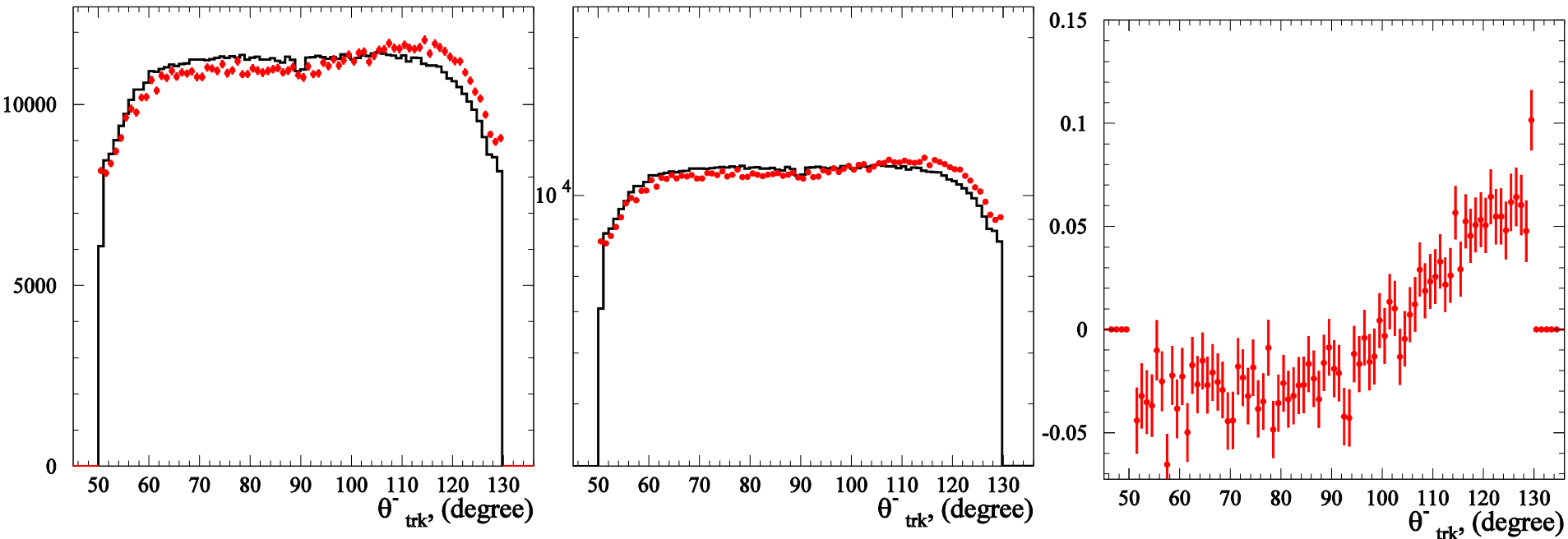
W_{ee} , $W_{\pi\pi}$ are fixed from trackmass, $W_{\mu\mu}$ is free



ee γ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction I (Results)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

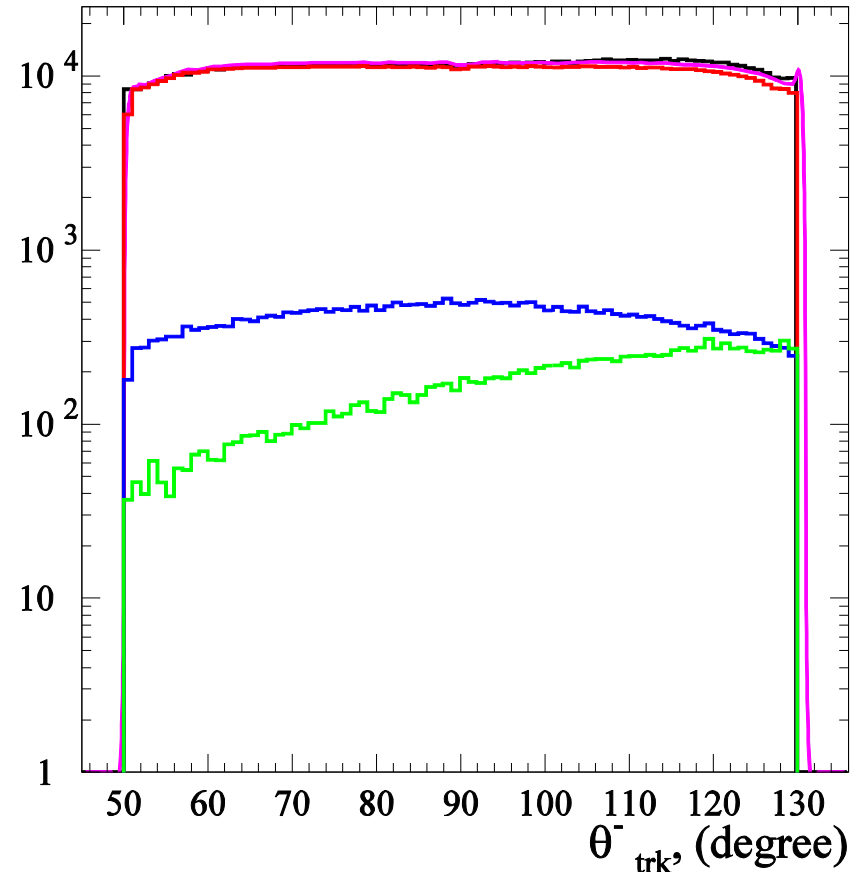
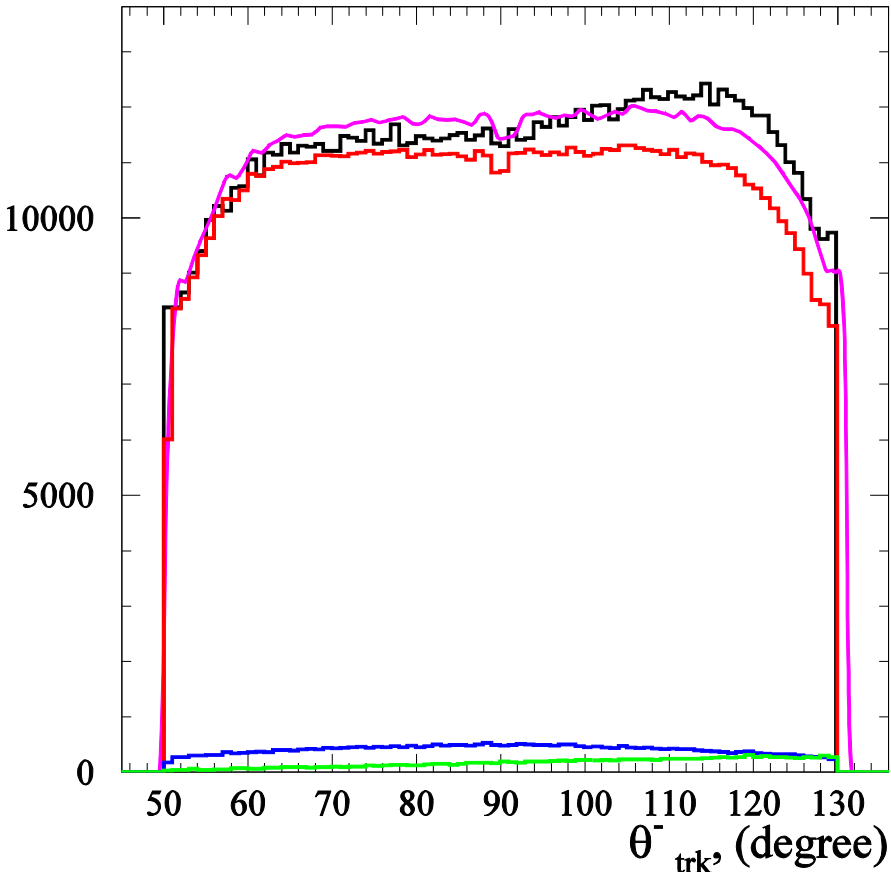


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 1)

$$F_{DATA}^{OR}(\theta^-) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(\theta^-) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(\theta^-) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(\theta^-)$$

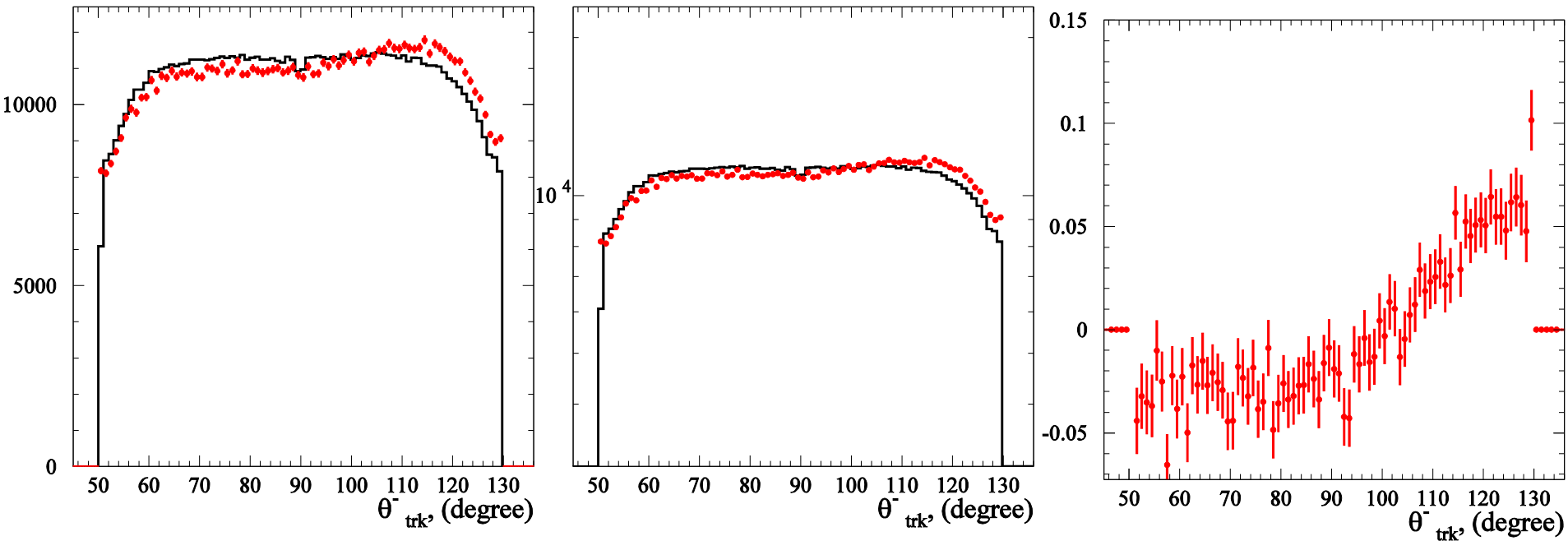
Wee is fixed from trackmass, $W_{\mu\mu}$, $W_{\pi\pi}$ are free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit I)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

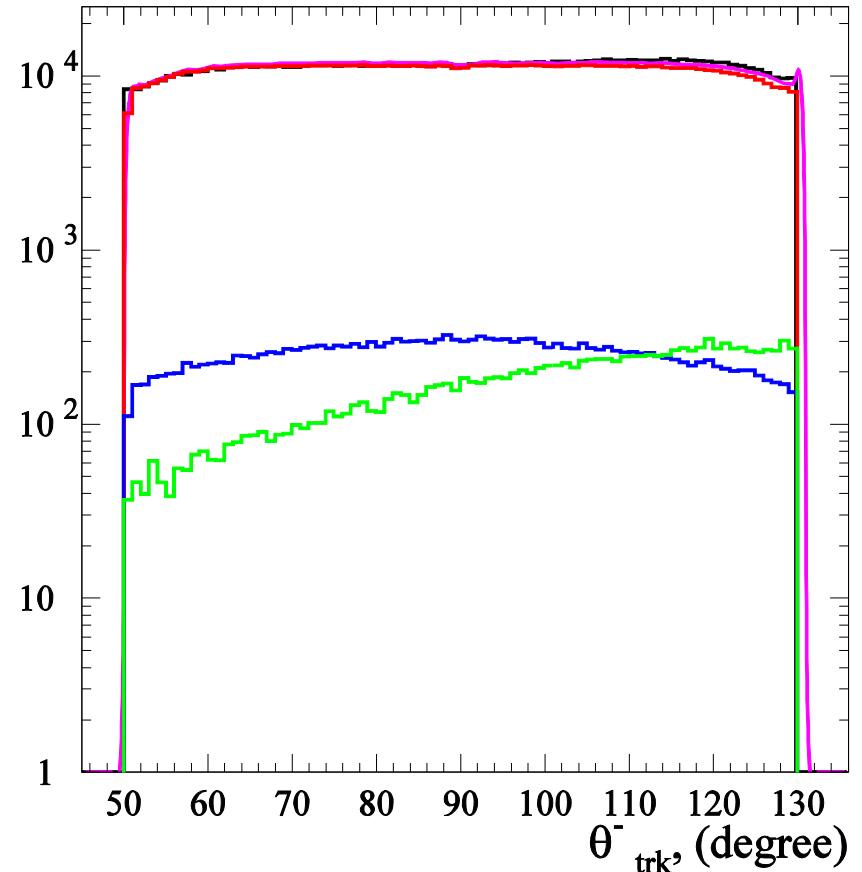
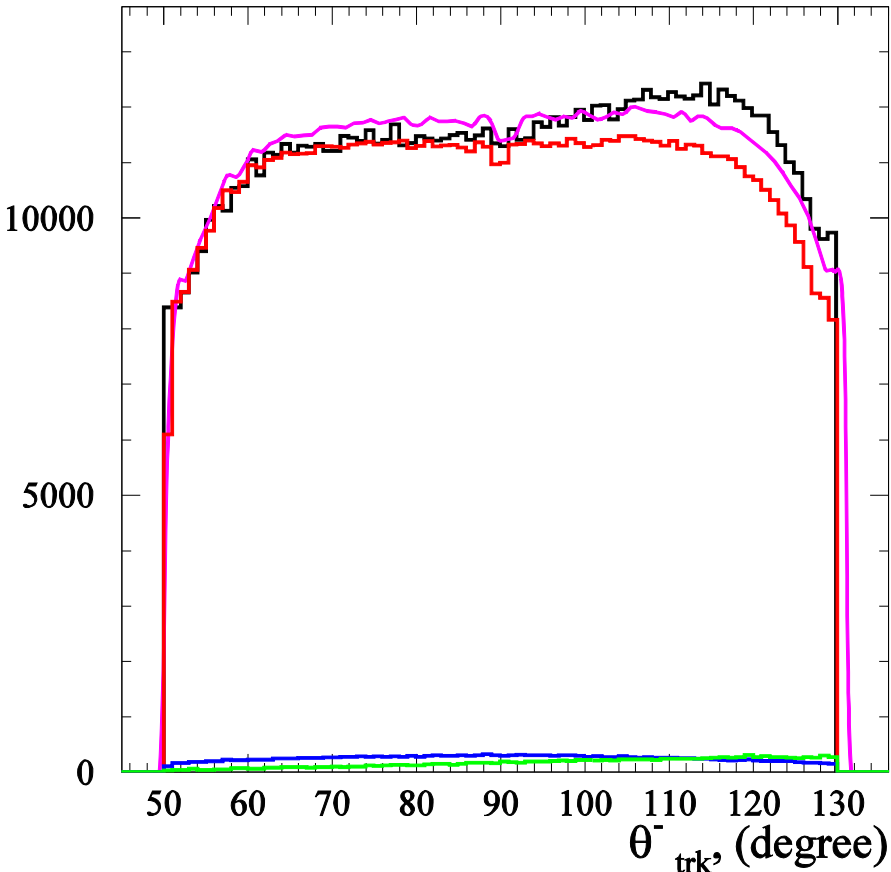


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 2)

$$F_{DATA}^{OR}(\theta^-) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(\theta^-) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(\theta^-) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(\theta^-)$$

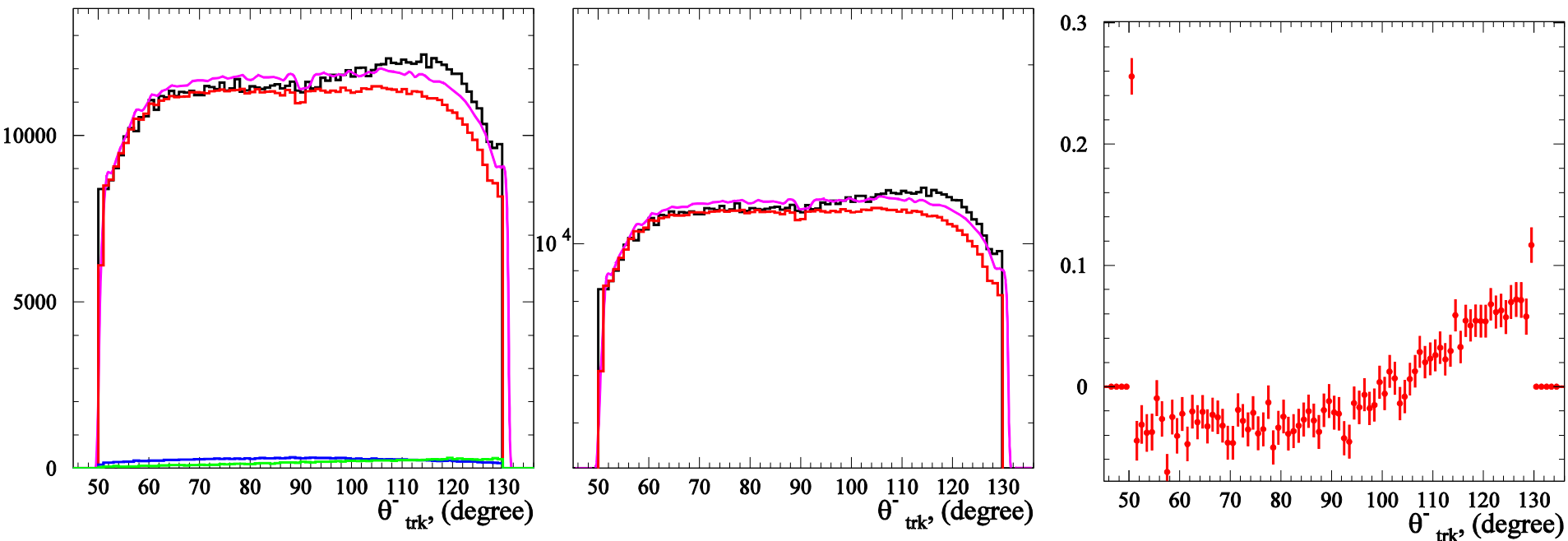
W_{ee} , $W_{\pi\pi}$ are fixed from trackmass, $W_{\mu\mu}$ is free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 2)

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction

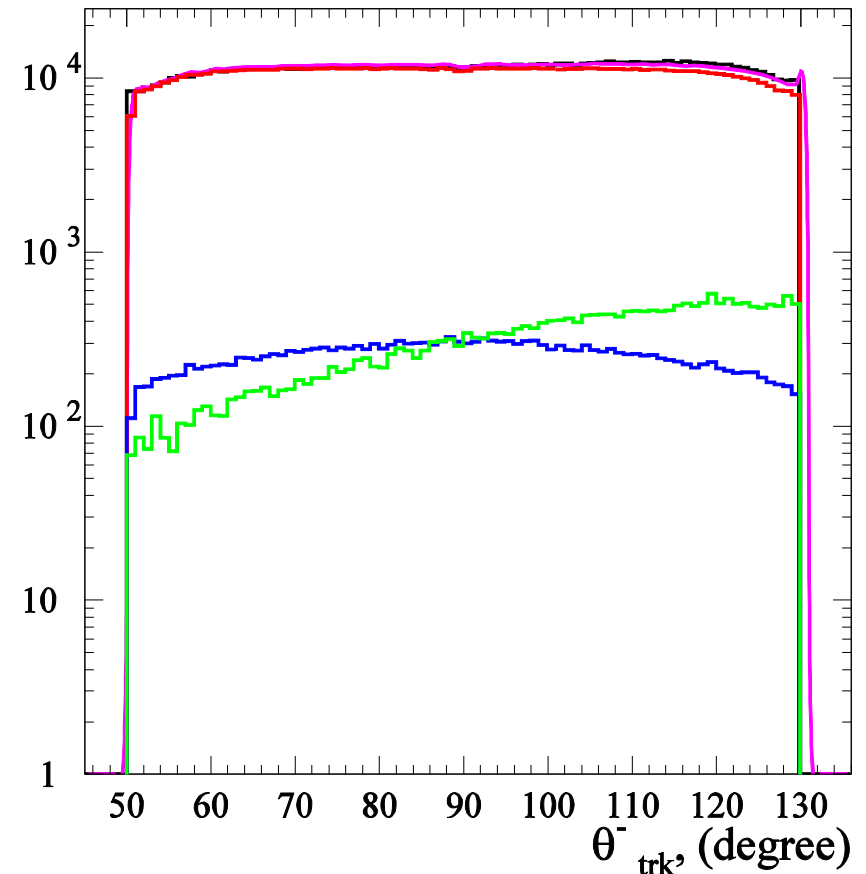
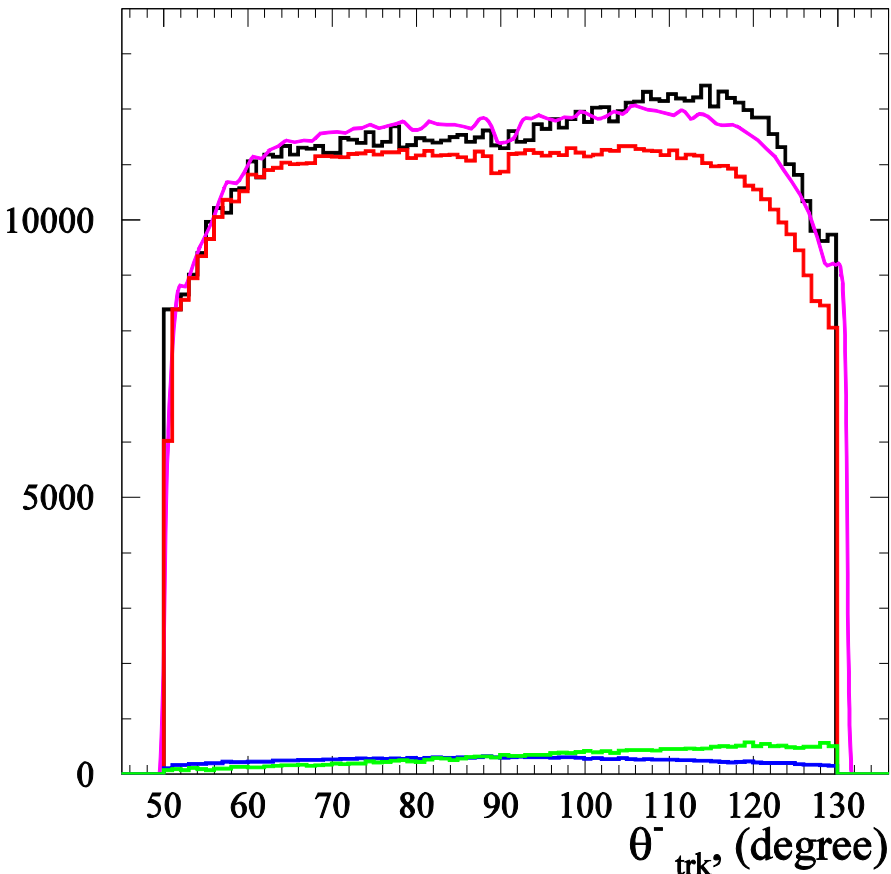


$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Background subtraction II (Fit 3)

$$F_{DATA}^{OR}(\theta^-) = W_{ee\gamma}^{OR} \cdot f_{MC\ ee\gamma}^{OR}(\theta^-) + W_{\pi\pi\gamma}^{OR} \cdot f_{MC\ \pi\pi\gamma}^{OR}(\theta^-) + W_{\mu\mu\gamma}^{OR} \cdot f_{MC\ \mu\mu\gamma}^{OR}(\theta^-)$$

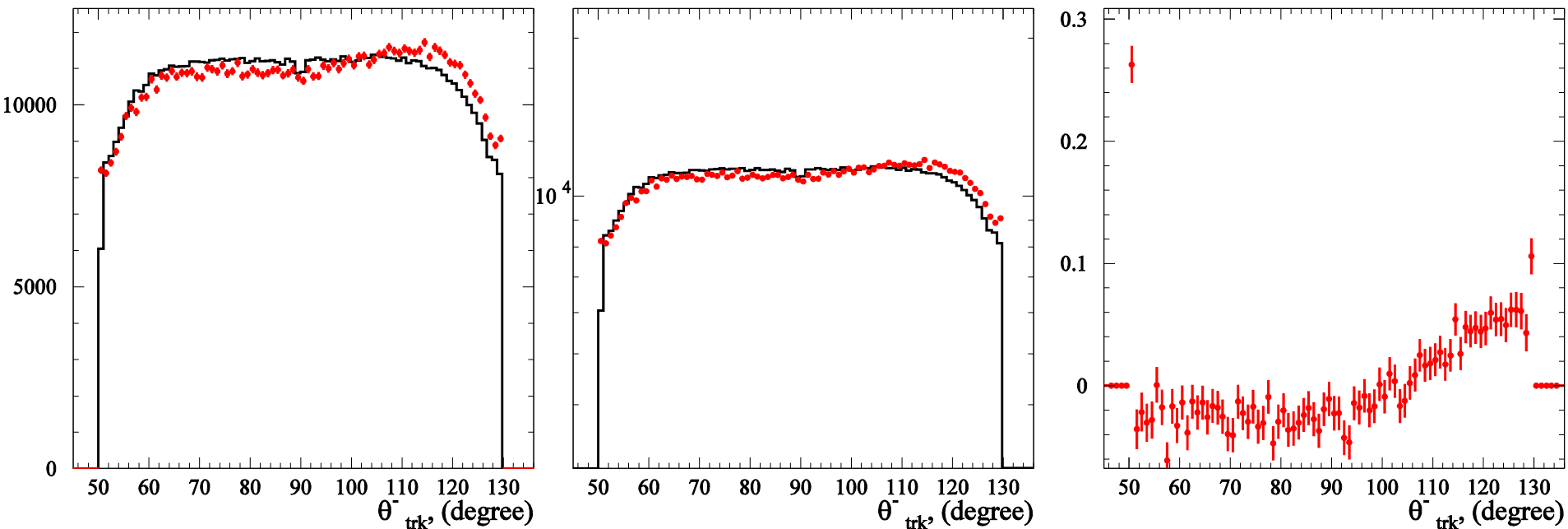
$W_{\pi\pi}$ is fixed from luminosity, $W_{ee}, W_{\mu\mu}$ are free



$ee\gamma$ is green, $\pi\pi\gamma$ is blue, $\mu\mu\gamma$ is red, fitting function is magenta

Background subtraction II (Results Fit 3)

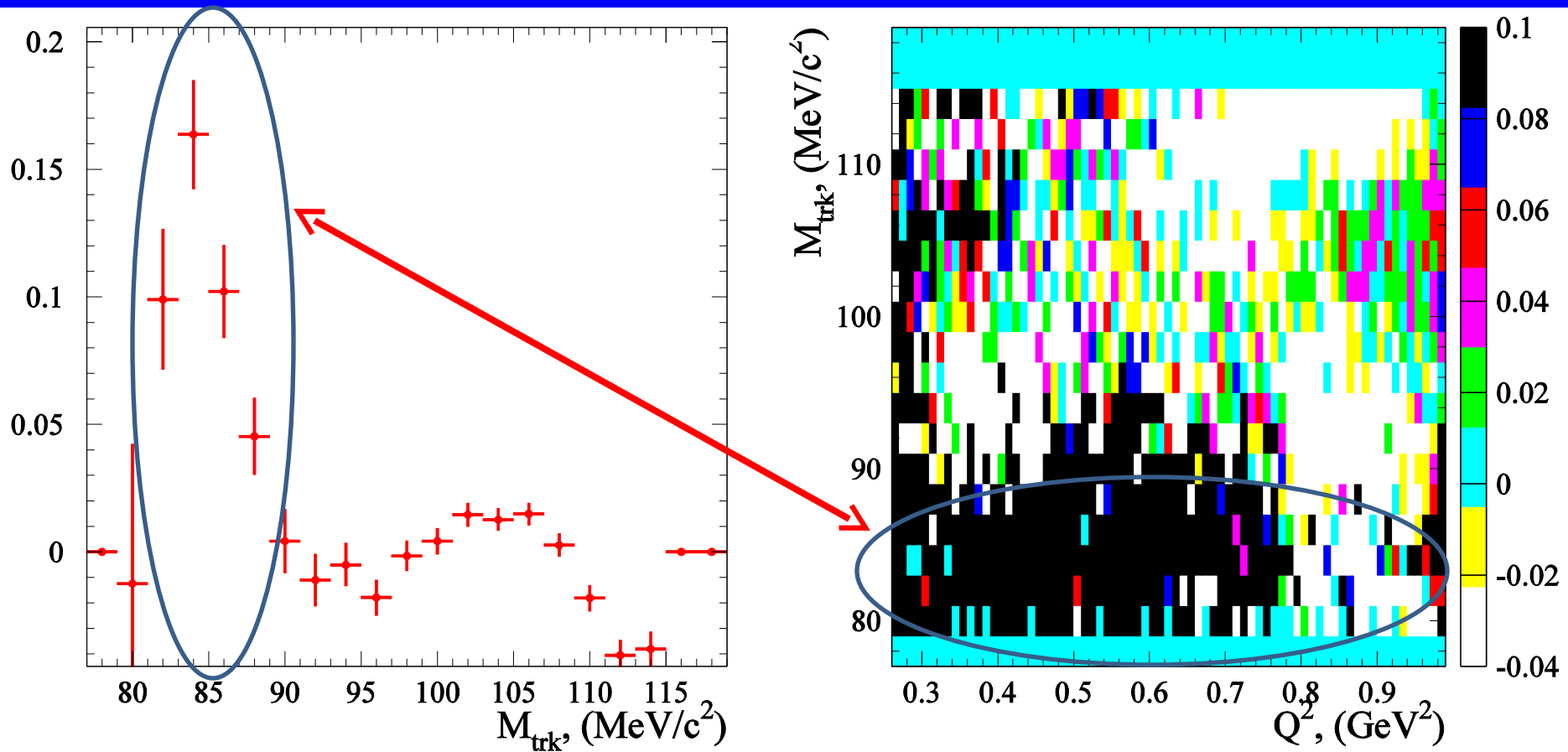
histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction



$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

To the nature of bump at 85 MeV

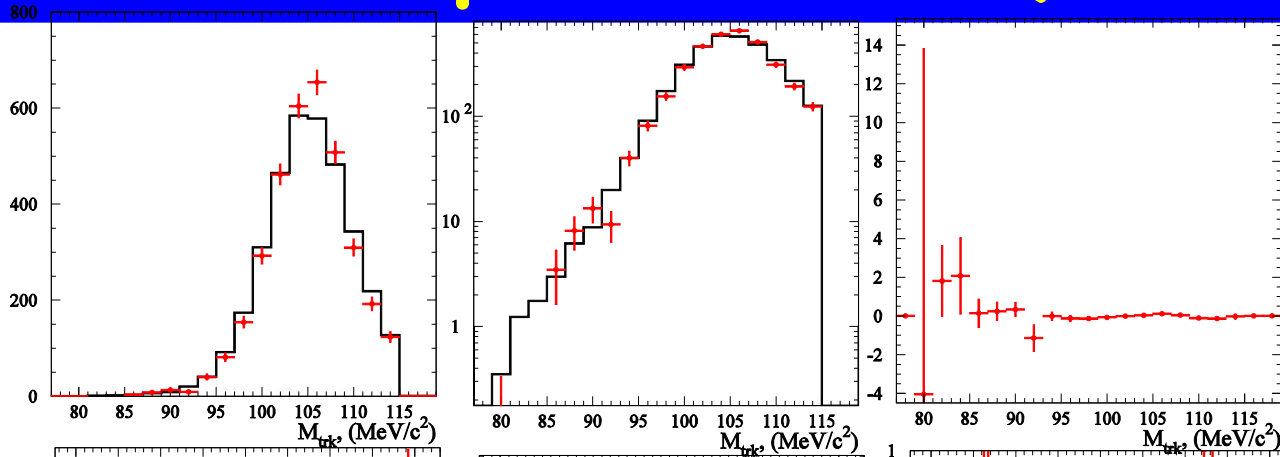
DATA/MC trackmass difference as a function of Q^2



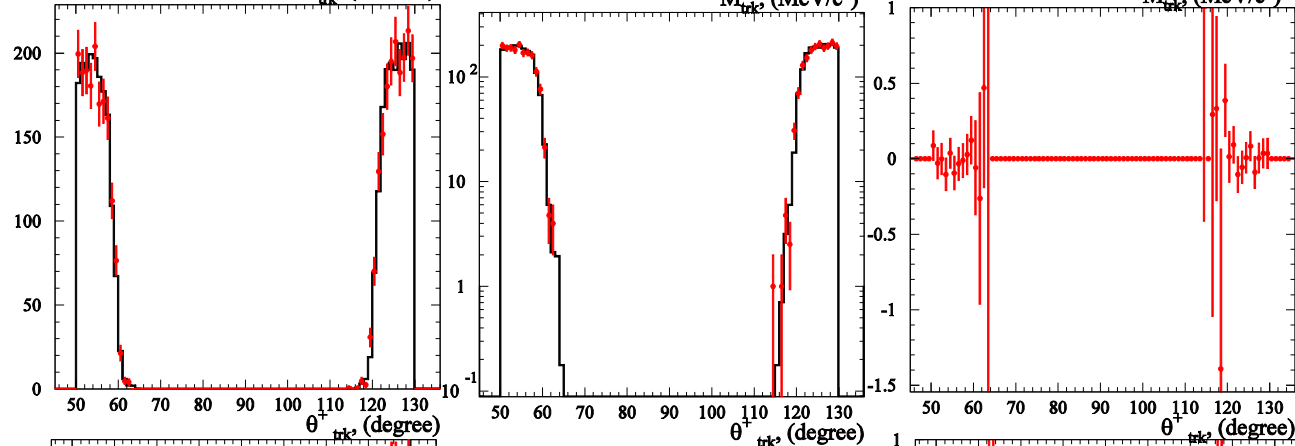
Let's start discussion ?

DATA/MC Comparision in Q^2 slices (I)

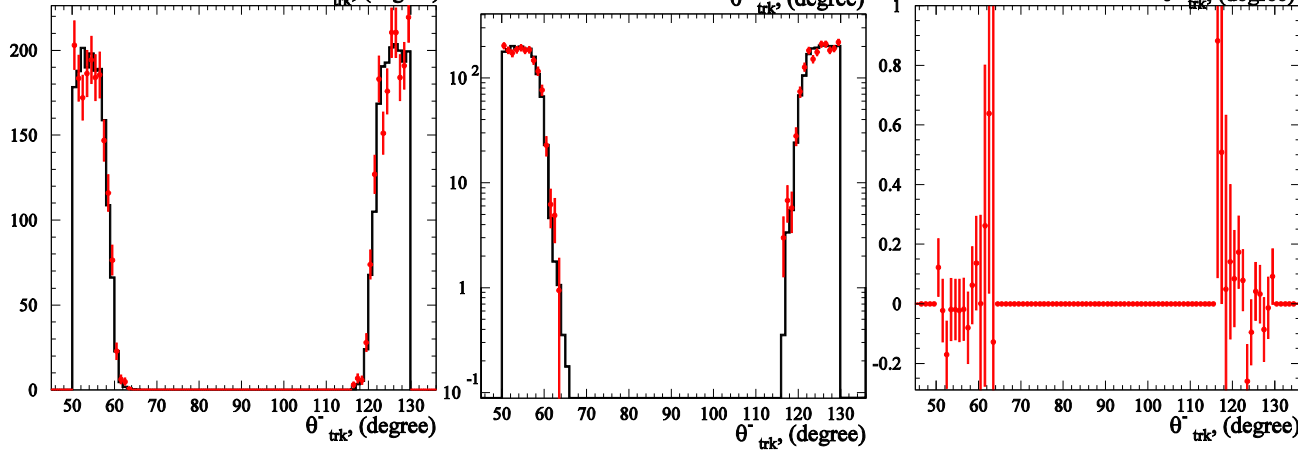
M_{trk}



ϑ_{μ^+}



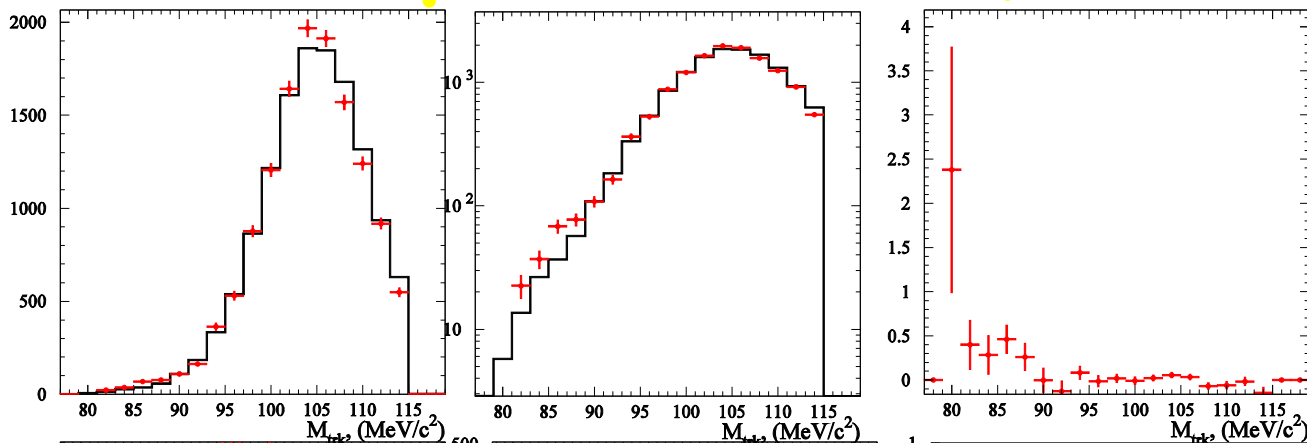
ϑ_{μ^-}



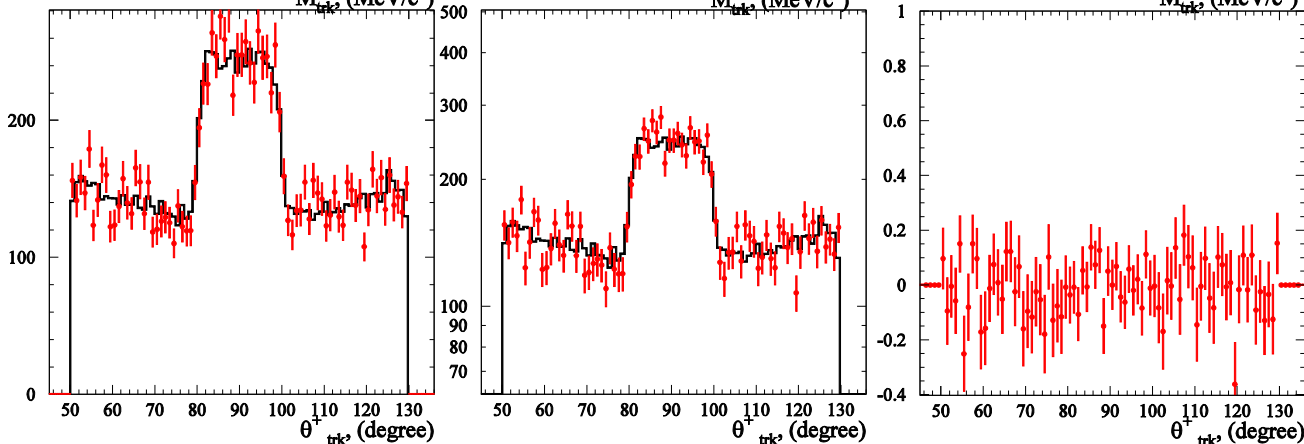
$Q^2 = 0.3 \text{ GeV}^2$

DATA/MC Comparision in Q^2 slices (II)

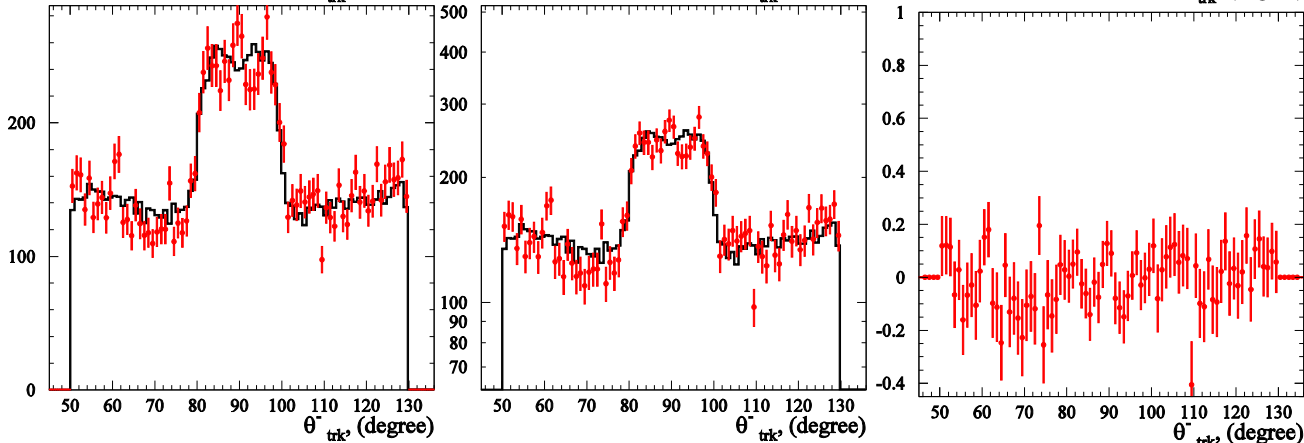
M_{trk}



ϑ_{μ^+}



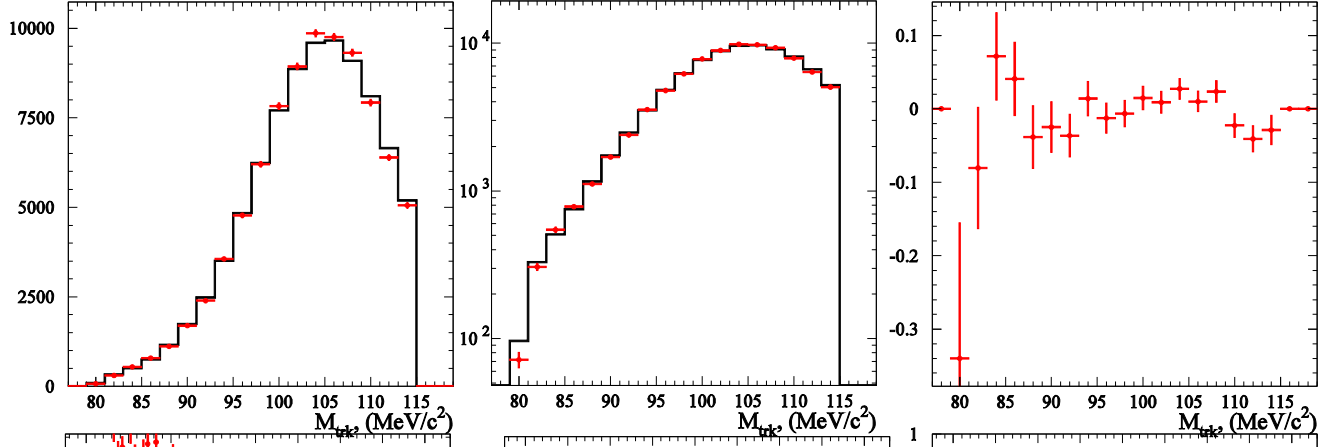
ϑ_{μ^-}



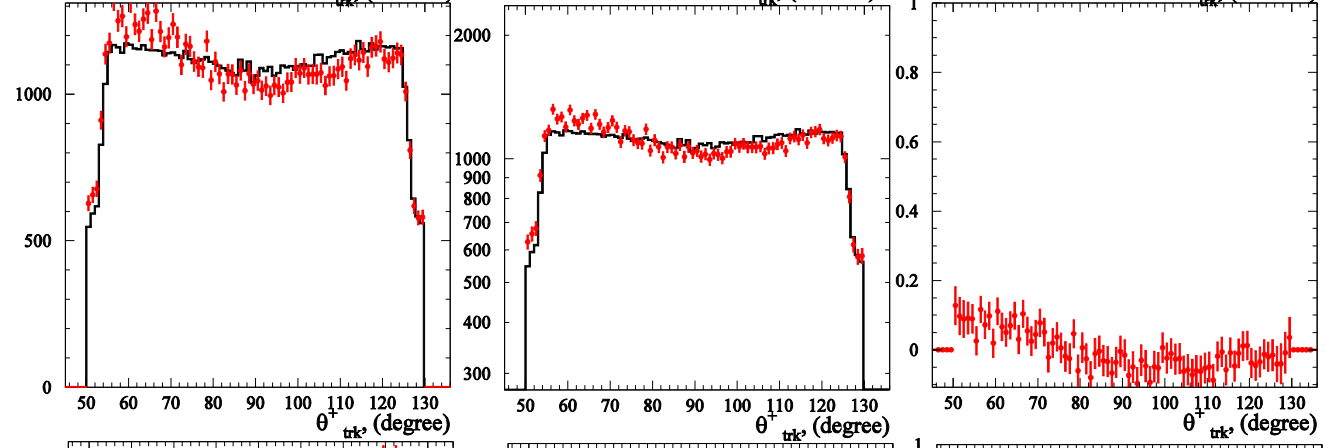
$Q^2 = 0.59 \text{ GeV}^2$

DATA/MC Comparision in Q^2 slices (III)

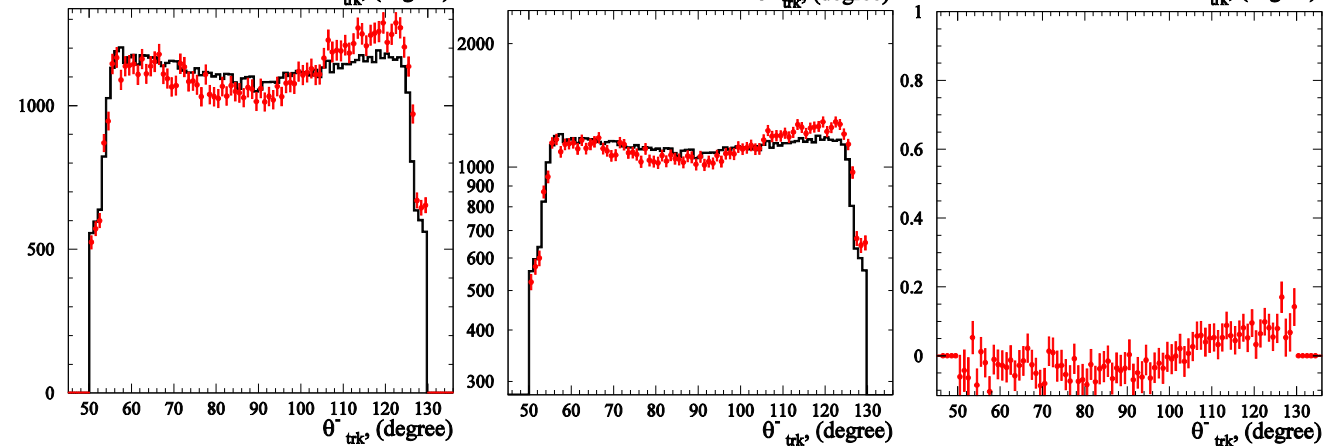
M_{trk}



ϑ_{μ^+}



ϑ_{μ^-}

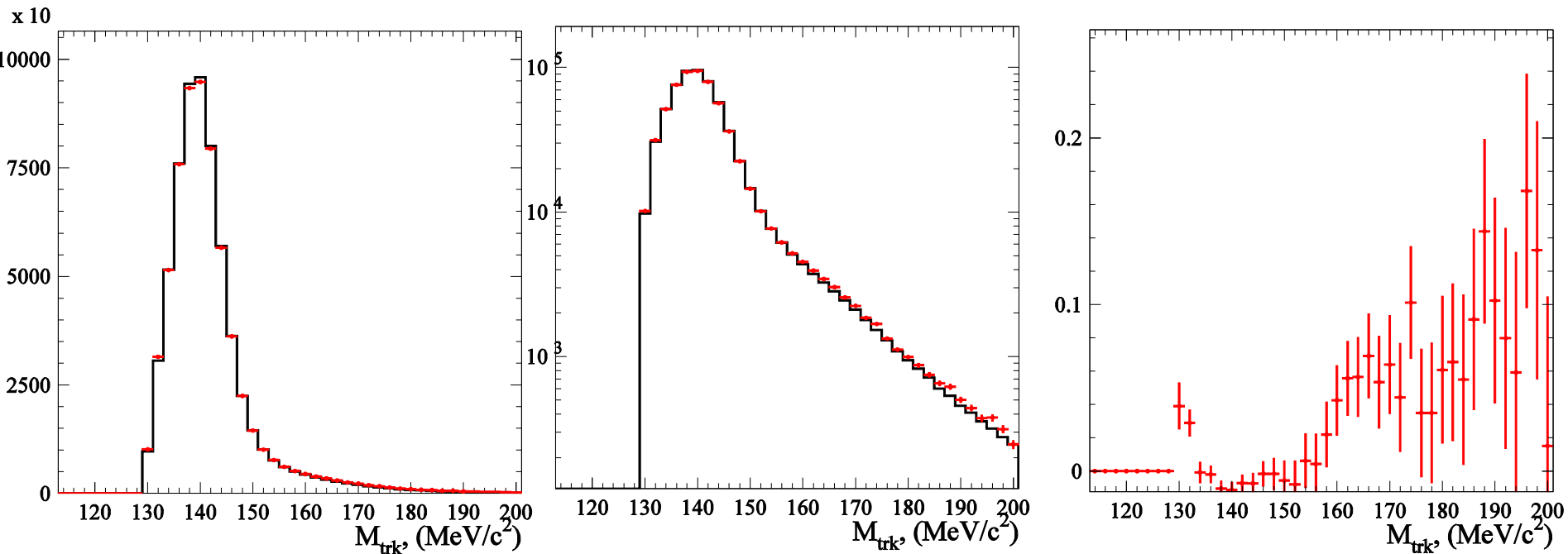


$Q^2 = 0.96 \text{ GeV}^2$

Crosschecks with pions

Pions trackmass

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,
Normalization is to the number of EXP DATA events after background subtraction



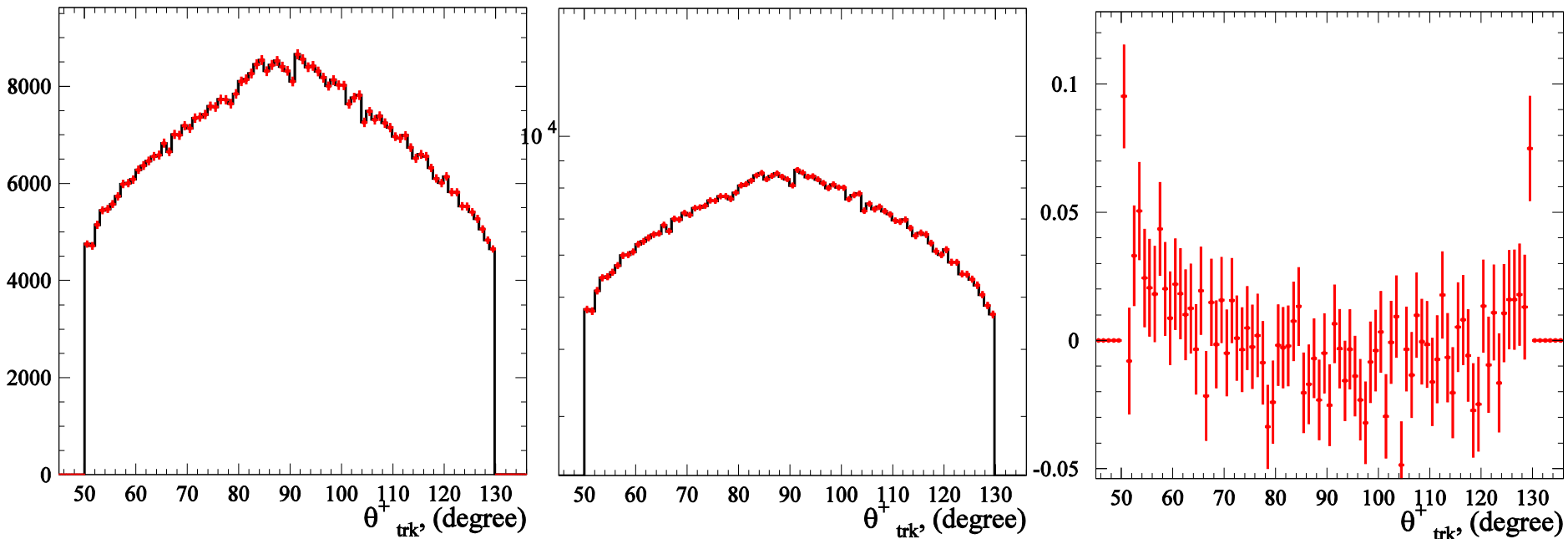
$$\text{Relative difference} = (\text{EXP} - \text{MC}) / \text{EXP}$$

Difference at higher trackmass is due to 3π background was not subtracted

Positive pion polar angle

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,

Normalization is to the number of EXP DATA events after background subtraction



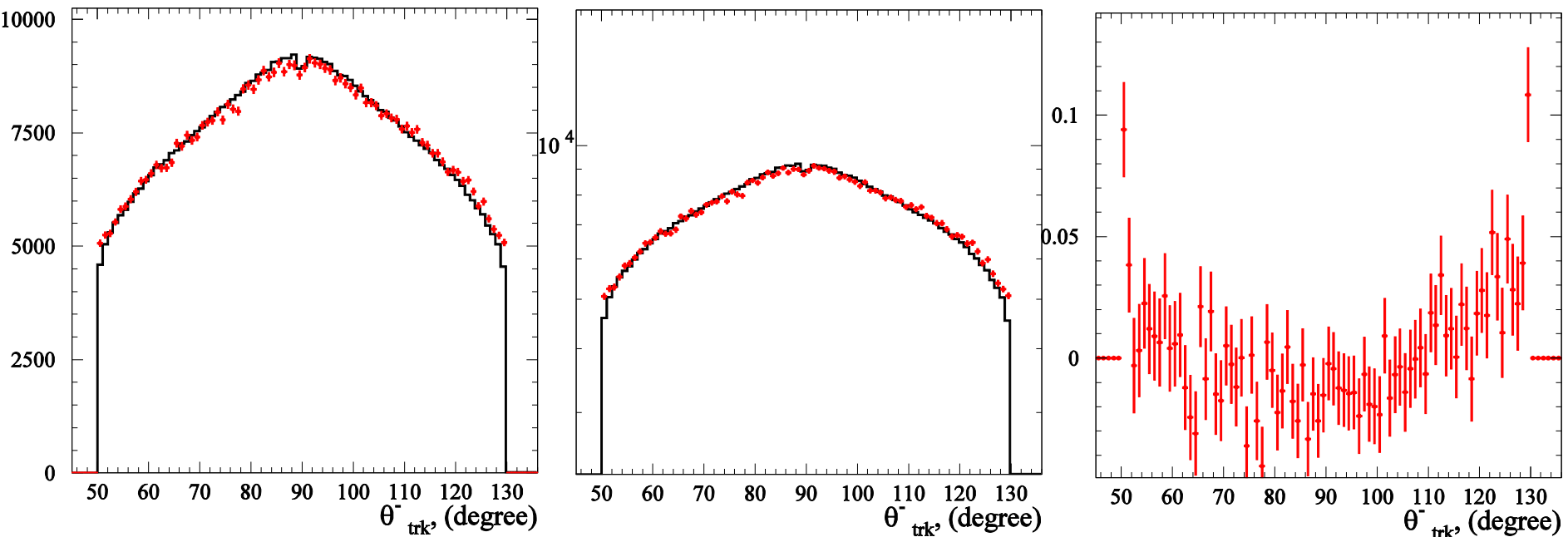
Relative difference = $(\text{EXP} - \text{MC}) / \text{EXP}$

3π background was not studied

Negative pion polar angle

histogram is MC $\mu\mu\gamma$ events, points with errors are EXP DATA,

Normalization is to the number of EXP DATA events after background subtraction



Relative difference = $(\text{EXP}-\text{MC})/\text{EXP}$

3π background was not studied

Cross checks of MC Generators

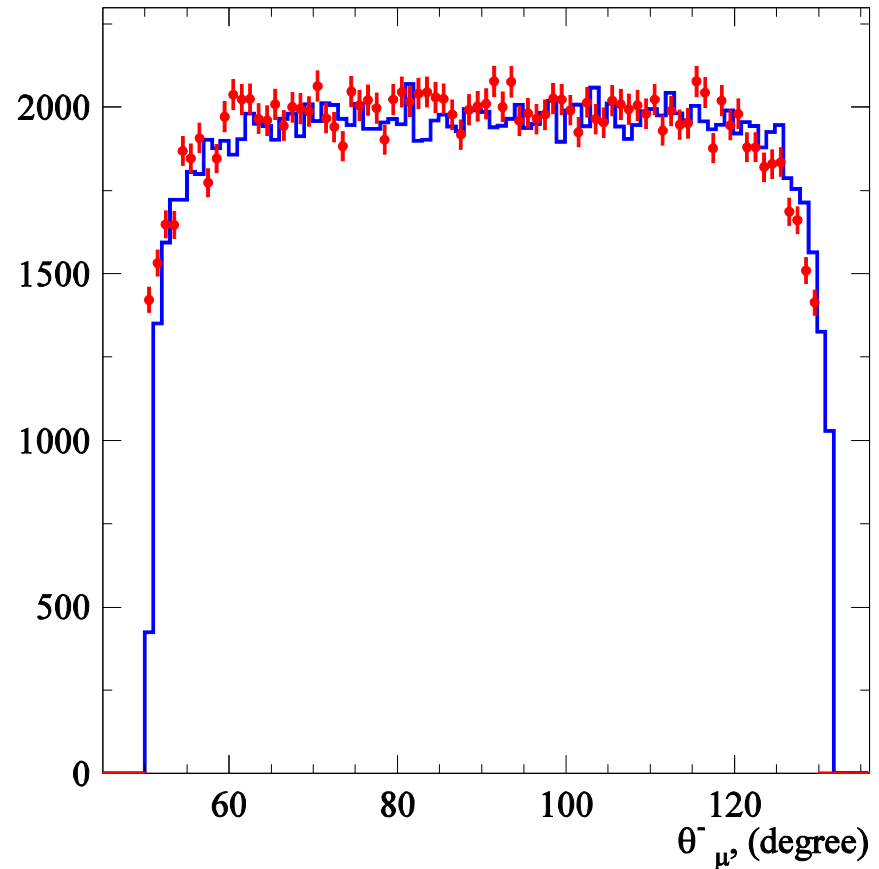
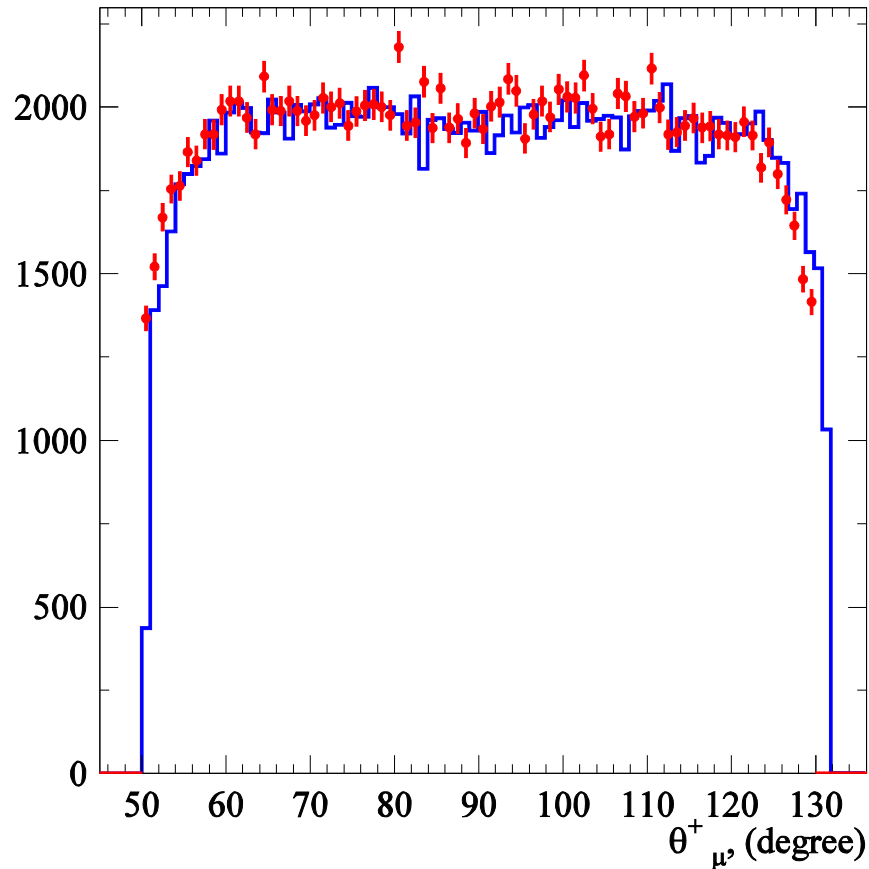
Comparison $\mu^+\mu^-$ MCGPJ & Phokhara 6.0

MCGPJ : $50^\circ < \vartheta_\mu < 130^\circ, |\vartheta_\gamma - 90^\circ| > 75^\circ, \sum E_\gamma > 0.01 \text{ GeV}$

PHOKHARA : $NLO + ISR + FSR + FSNLO$

PHOKHARA is blue histogram

MCGPJ is red points with errors



Quit good agreement in polar angle spectra is observed

Conclusion

- Comparison DATA/MC was performed in both in integral over all Q^2 and in different Q^2 slices.
- The two ways of Bhabha background subtraction were studied, but presence of other background is seen and should be studied yet.
- MC resolution adjustment probably should be performed for muons
- The start of the work is good enough and many things were studied, but a lot of work has to be done for successful completion of whole analysis

Let's continue our fruitful collaboration!

Thank You for Your attention