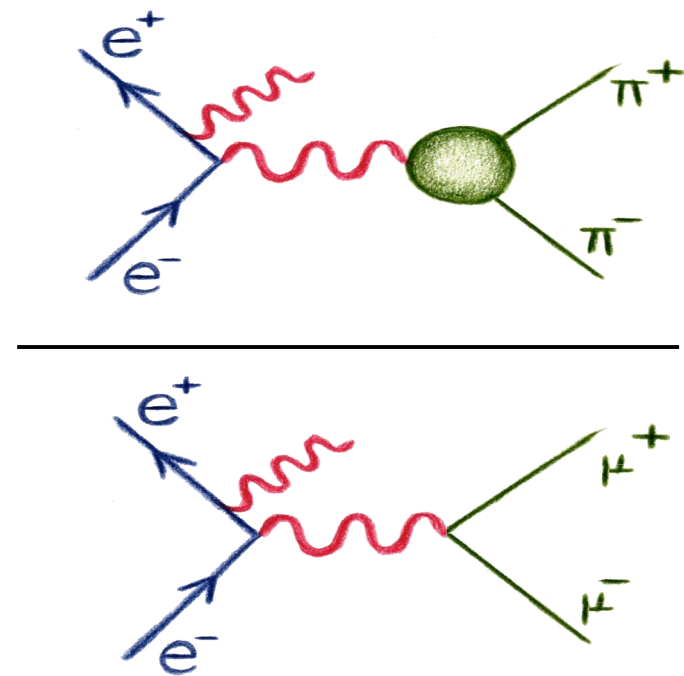


Extraction of $|F_\pi|^2$ from the ratio
of $\pi\pi\gamma$ to $\mu\mu\gamma$ events and
comparison with the absolute
normalization

Federico Nguyen
 Φ Decays 28-02-07



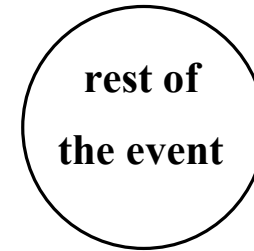
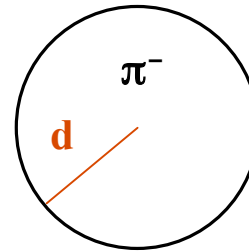
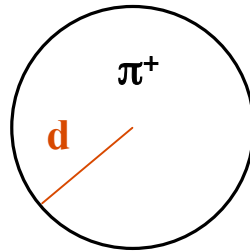


An outline

- 1) Improvements wrt the last *General Meeting* for the trigger
- 2) Estimate of a possible impact on 2001 data
- 3) DC trigger comparison
- 4) Studies and corrections for the formula of the ratio
- 5) Neural networks algorithms for control samples
- 6) Results: comparisons

Single particle method

- classification of all fired sectors according to the cluster position wrt the extrapolated π track:



- then multiplicities are evaluated: e.g. $P_{+,-,r}(0,1,2)$ = probability for the π^+ , π^- or the rest of firing 0,1,2 trigger sectors
- assumption: probabilities are independent no correlation among the categories

$$P(+ = 1, - = 0, r = 0) = P(+ = 1) P(- = 0) P(r = 0)$$

- single conditioned probabilities are built in an unbiased way,
e.g. $P_+(0,1,2)$ is estimated as the probability provided that the rest OR the π^- have fired 2 trigger sectors

above assumptions allow the following formula (M. Incagli, KLOE Memo 278):

$$\epsilon_{\text{trigger}}(M_{\pi\pi}^2) = 1 - P_1^+ \cdot P_0^- \cdot P_0^r - P_0^+ \cdot P_1^- \cdot P_0^r - P_0^+ \cdot P_0^- \cdot P_1^r - P_0^+ \cdot P_0^- \cdot P_0^r$$



Used variables

$$\Delta R = |\vec{x}_{clu} - \vec{x}_{ext}|$$

$$N_{EMC} = \varepsilon_{EMC}^{trg} N_{TOT}$$

$$N_{DC} = \varepsilon_{DC}^{trg} N_{TOT}$$

$$N_{BOTH} = \varepsilon_{EMC}^{trg} \varepsilon_{DC}^{trg} C_T N_{TOT}$$

$$\Delta T = t_{clu} - t_{max}$$

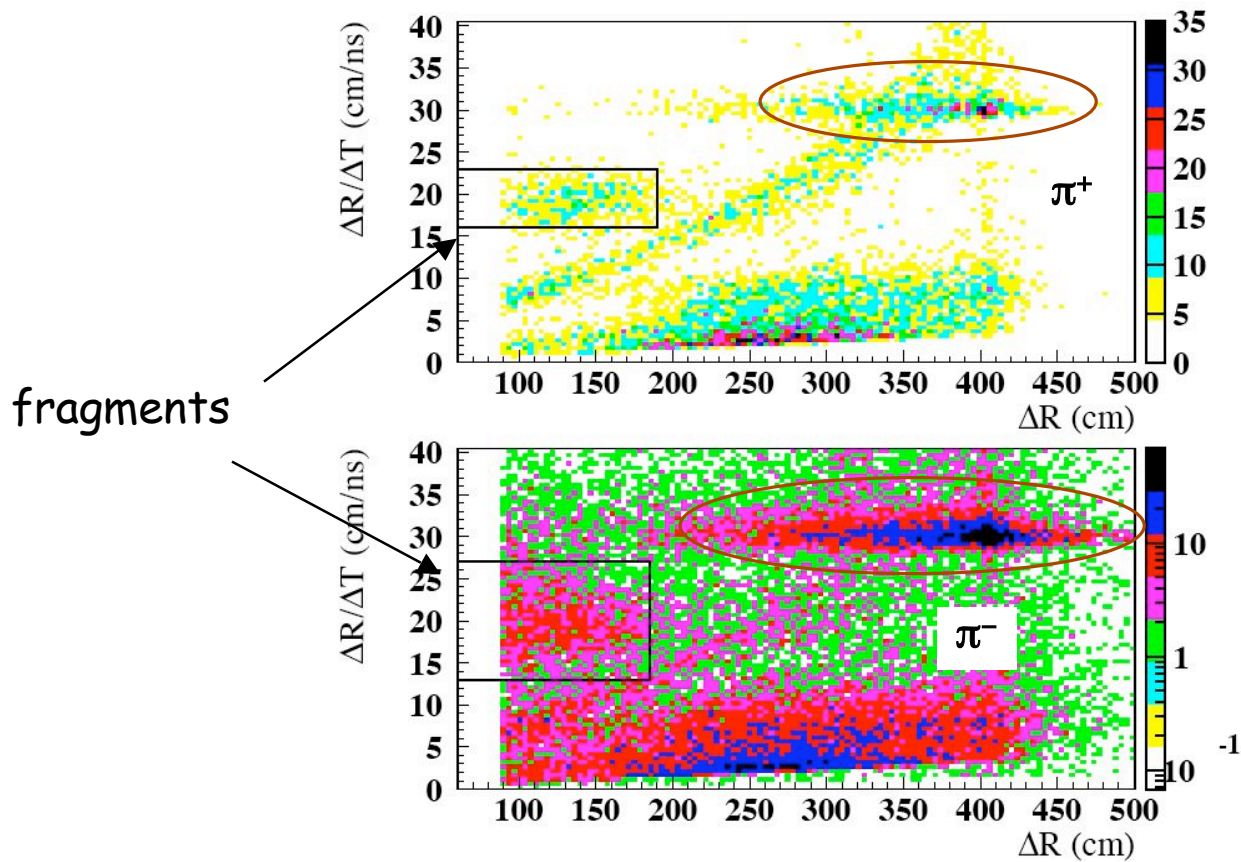
t_{max} = time of the most energetic cluster within 60 cm from the extrapolated point

studying clusters with $E > 30$ MeV was evident that only a topological cut (sphere with $R=60$ cm) cannot account of all clusters correlated with charged pions (moreover MC is different from data)

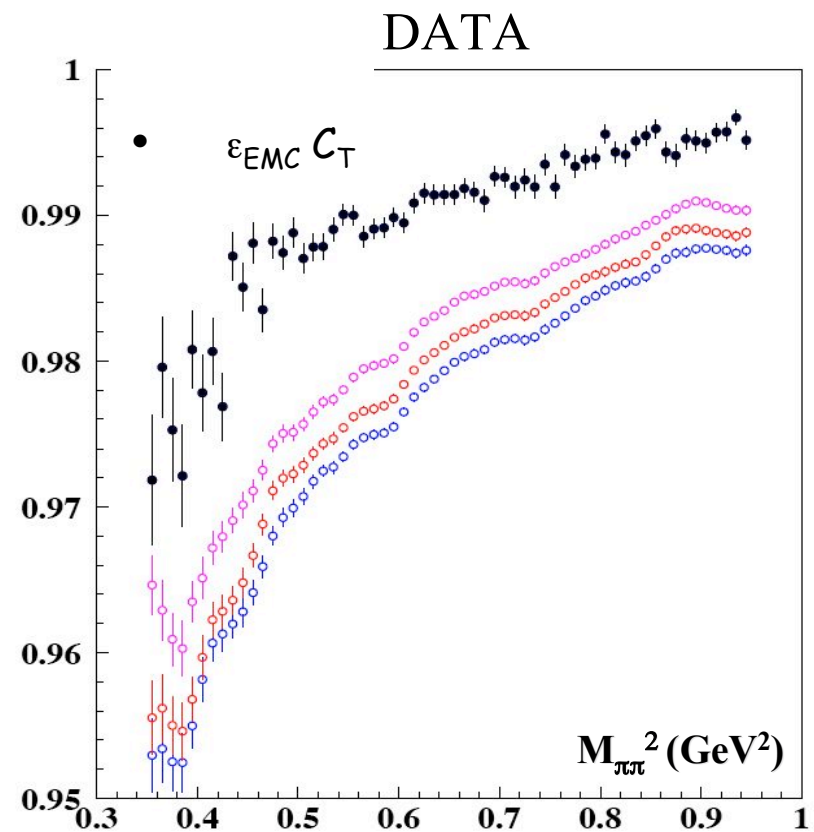
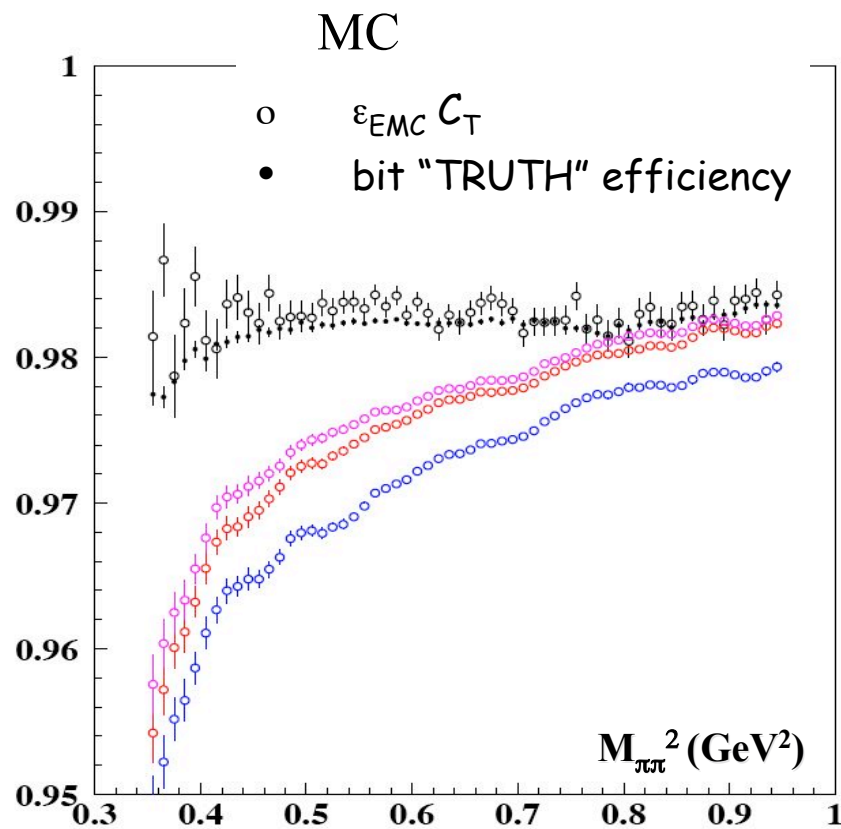
Assessed re-assignment

what's left over out of the 90 cm spheres?

photons (π^0)



From the last KGM



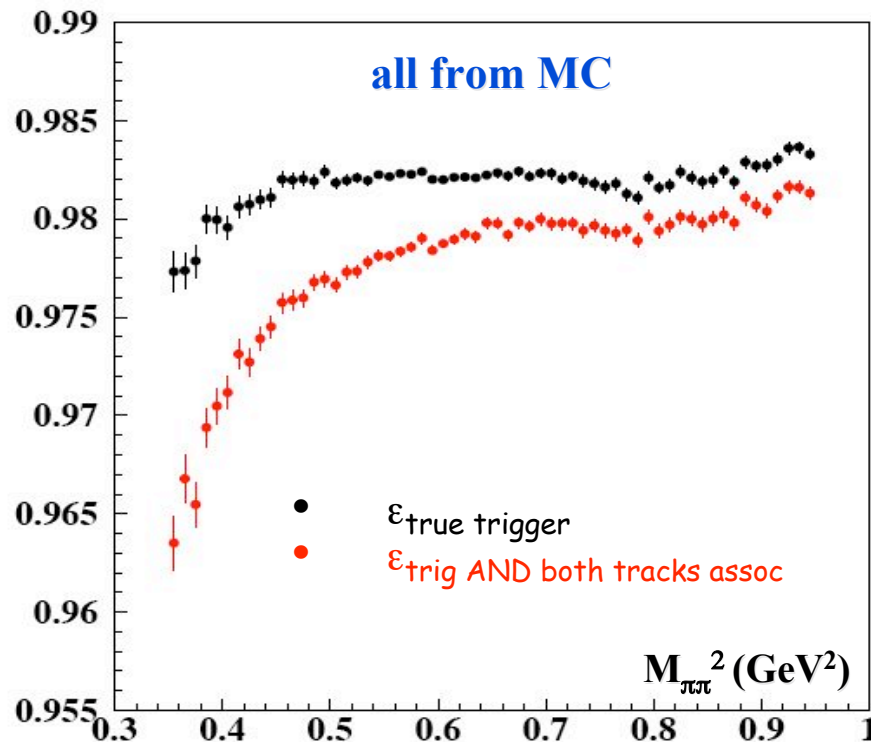
- R=90 cm sphere + photons + "fragments"
- R=90 cm sphere + photons
- R=90 cm sphere

colour plots from single particle method

Checking single particle probabilities

if $P_{+,-,r}(0,1,2)$ =probability for the π^+ , π^- or the rest of firing 0,1,2 trigger sectors,
found a concept bug: probability not conditioned on the presence of the cluster,

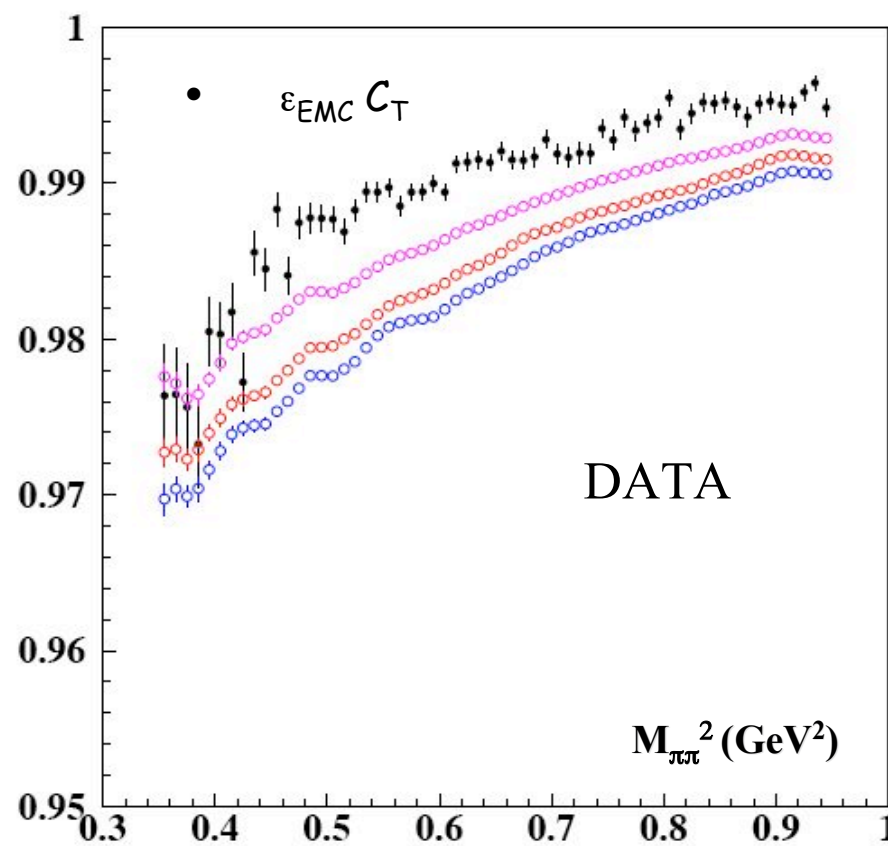
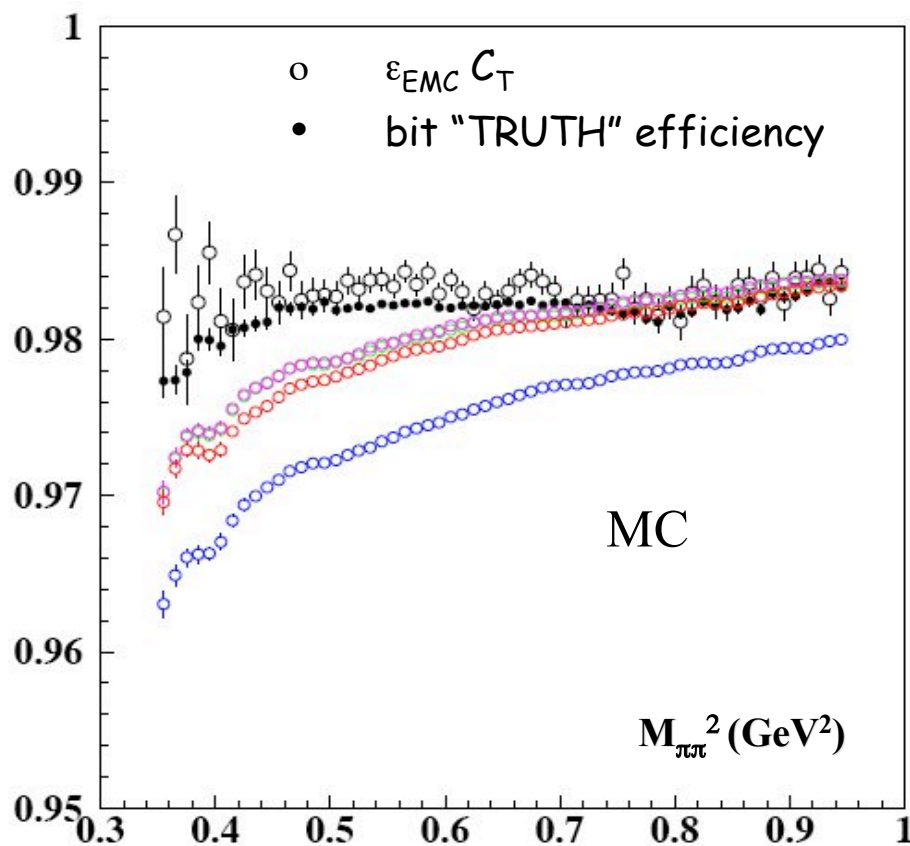
ex.: $P_+(1 \text{ sector} \cap 1 \text{ cluster})$ instead of $P_+(1 \text{ sector} | 1 \text{ cluster})$



I reproduced the slope at low $M_{\pi\pi}$ values requiring the probability to trigger AND both tracks to have a cluster

decrease the trigger efficiency for the probability to reach the calorimeter (lower at lower $M_{\pi\pi}$)

Now it is better...



- R=90 cm sphere + photons + "fragments"
- R=90 cm sphere + photons
- R=90 cm sphere

colour plots from single particle method

Towards an uncertainty estimate

why keep separated DATA and MC for the trigger?

- 1) accidental clusters different by a factor ~ 2 (see Martini-Miscetti studies)
- 2) different $\pi^\pm N \rightarrow \pi^0 X$ cross section in the calorimeter (see my slides @ kgm65)
- 3) ...other than different genuine trigger response

for a systematic error well

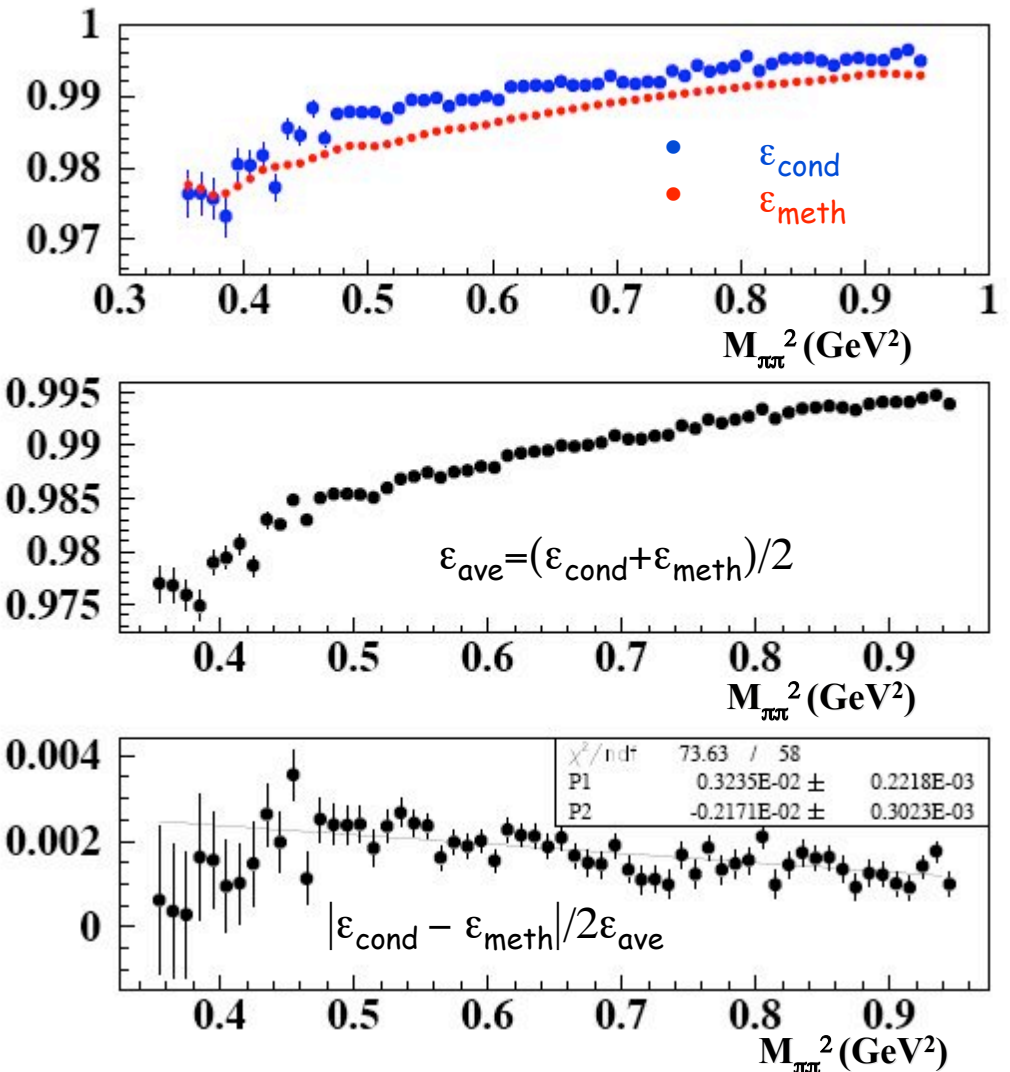
below 1%, 2 independent methods

from data is the preferred way

$$\epsilon_{\text{cond}} = \epsilon_{\text{EMC}}^{\text{trg}} C_T \text{ (DC-EMC corr.)}$$

ϵ_{meth} : photons and "fragments" included

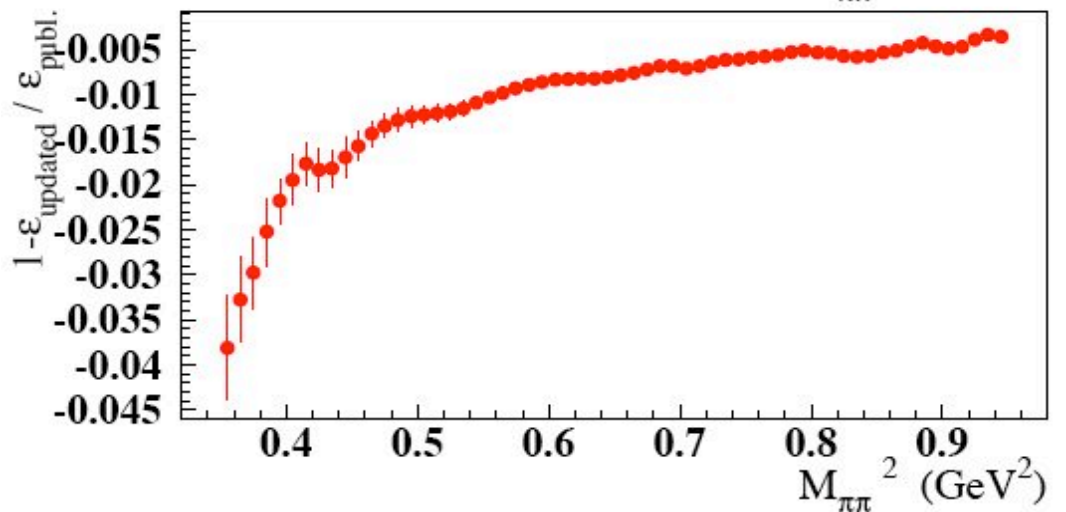
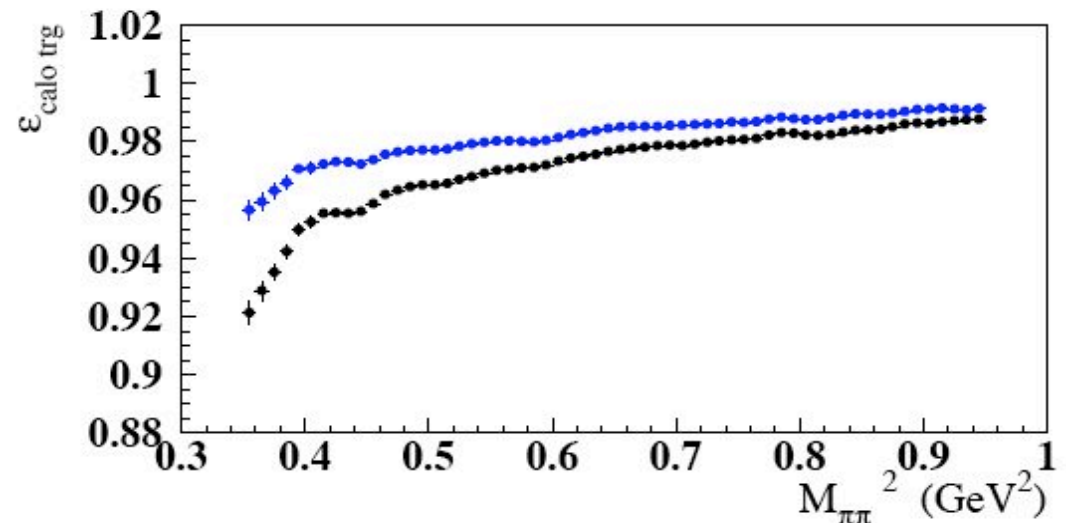
both blue and red curves are from data



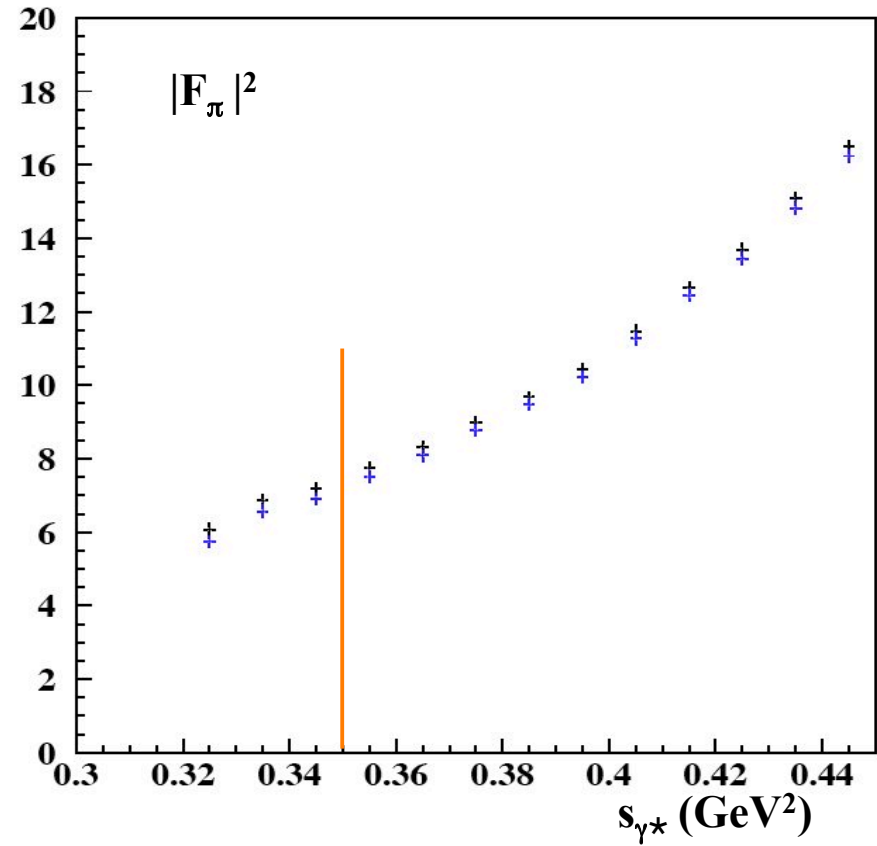
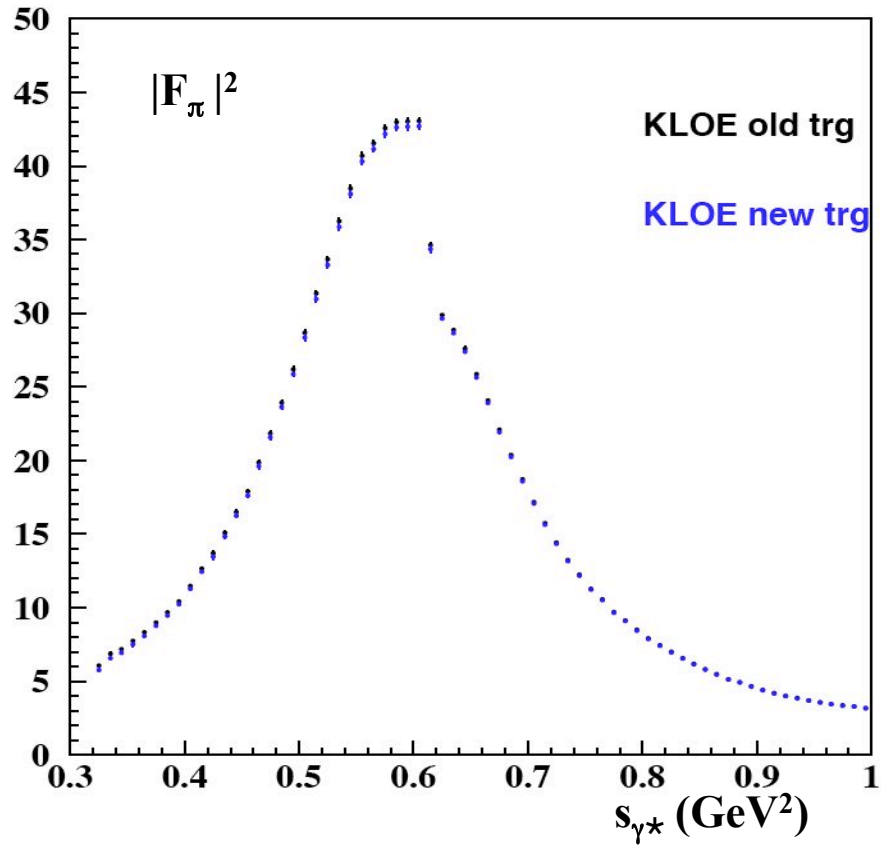
Revising 2001 trigger efficiency

I tried to fix the bug in old 2001 fashioned dst's (old FILFO, old ppntag, Cosmic Veto...) and to estimate an efficiency a` la published way to be compared with that obtained with the same prescription of the previous slides

2001 CALO trigger: black=publ., blue=updated



Possible impact on 2001 F_π



DC trigger studies

define

$$\begin{aligned} \epsilon_{\text{Rel}} &= \frac{N_{DC}}{N_{TRG}} \\ &= \epsilon_{DC} \frac{\cancel{N_{TOT}}}{\cancel{N_{TOT}} (1 - N_{FAIL} / N_{TOT})} \end{aligned}$$

provided 2 tracks to reach the barrel ($50^\circ < \theta < 130^\circ$) and with quite high ($p > 200$ MeV) mom. we assume DC trigger does not care if pions or muons

we expect the overall trigger inefficiency $N_{\text{fail}}/N_{\text{tot}} \sim 1\%-4\%$

$$\frac{\epsilon_{\text{Rel}}^{\pi\pi\gamma}}{\epsilon_{\text{Rel}}^{\mu\mu\gamma}} = \underbrace{\left(\frac{\epsilon_{DC}^{\pi\pi\gamma}}{\epsilon_{DC}^{\mu\mu\gamma}} \left(1 + \frac{N_{FAIL}}{N_{TOT}} \Big|_{\pi\pi\gamma} - \frac{N_{FAIL}}{N_{TOT}} \Big|_{\mu\mu\gamma} + O\left[\left(\frac{N_{FAIL}}{N_{TOT}} \right)^2 \right] \right) \right)}_{\text{assumed 1}}$$

difference from 1 is checked in the following

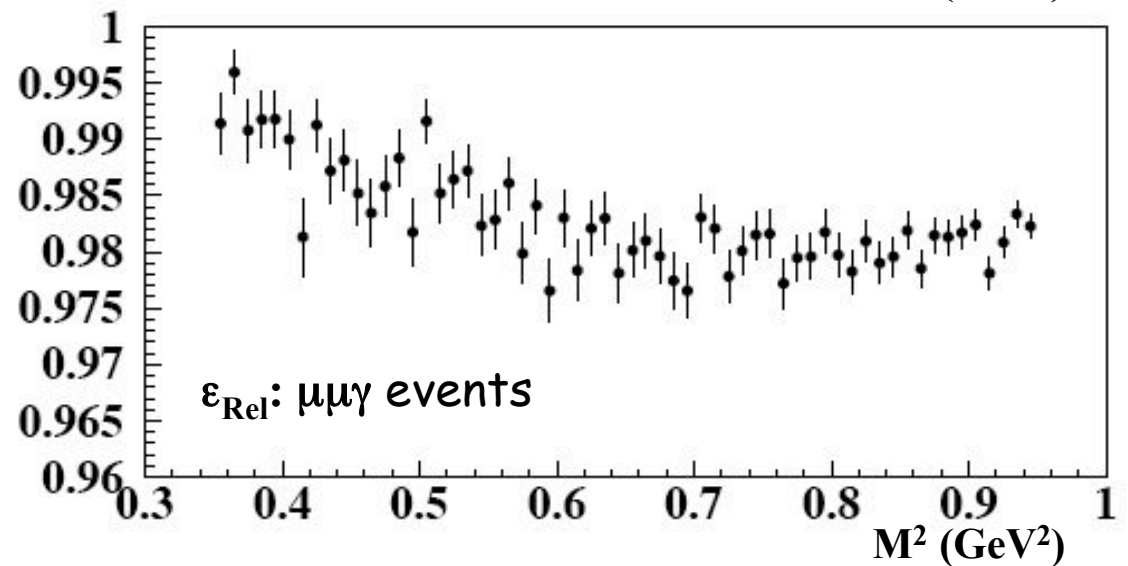
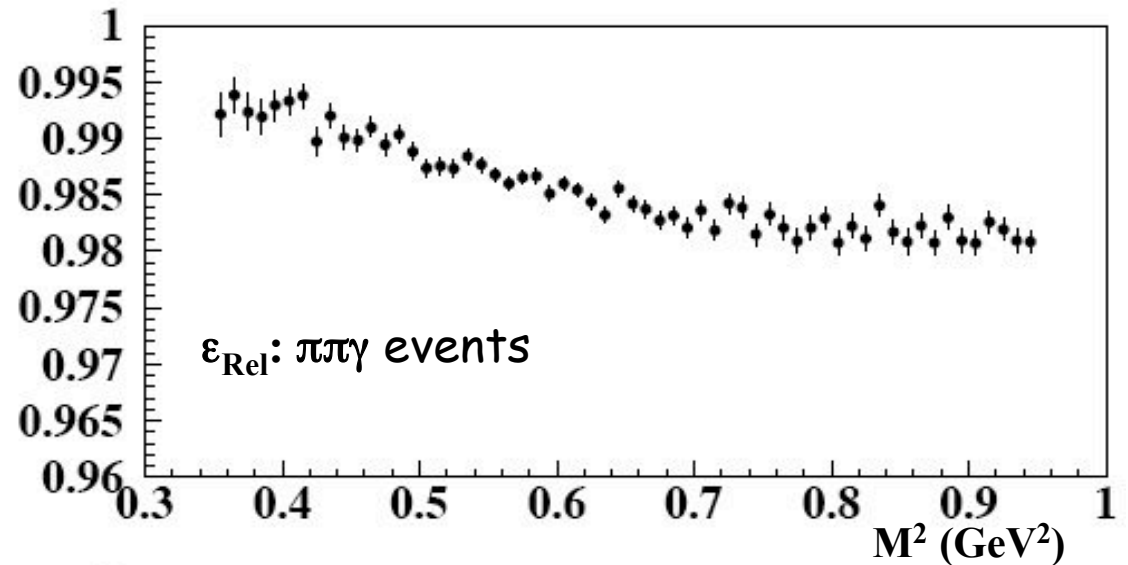
Relative efficiencies from data

idea developed from several discussions with M. Incagli

usual small angle selection from PPG dst's

Low momentum \Rightarrow lower radius \Rightarrow higher n. of hit DC superlayers

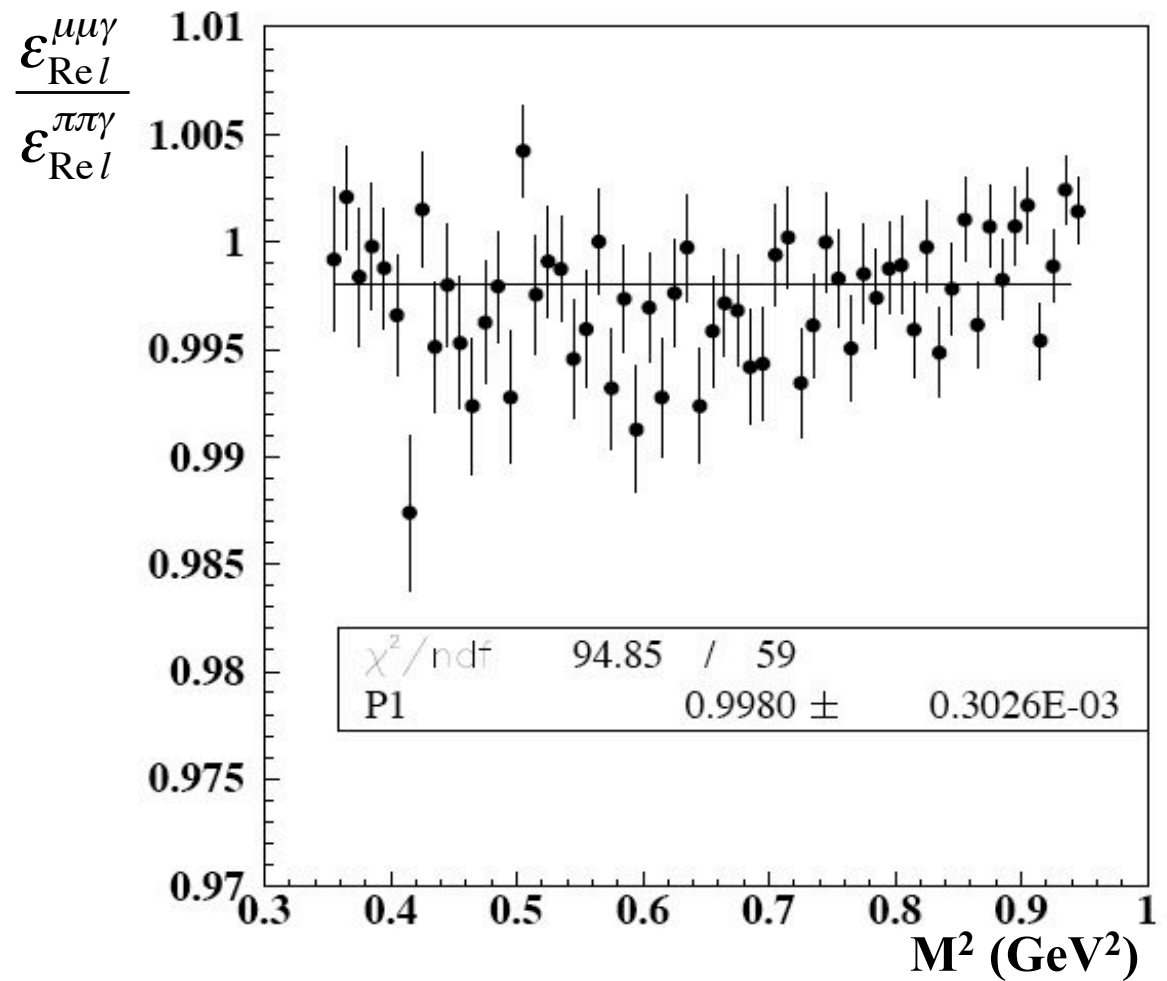
not an absolute scale to compare with CALO trigger!!!



Final correction is nearly 1

$$\frac{\epsilon_{\text{Rel}}^{\pi\pi\gamma}}{\epsilon_{\text{Rel}}^{\mu\mu\gamma}} \approx \frac{\epsilon_{\text{DC}}^{\pi\pi\gamma}}{\epsilon_{\text{DC}}^{\mu\mu\gamma}} \quad \text{within 0.2\%}$$

at the moment we
use it only as in the
following check



A couple of steps further on

if the trigger type is marginally correlated with background
or other reconstruction efficiencies:

$$\frac{N_{\pi\pi\gamma}^{dc} \epsilon_{\mu\mu\gamma}^{dc}}{N_{\mu\mu\gamma}^{dc} \epsilon_{\pi\pi\gamma}^{dc}} \approx \frac{N_{\pi\pi\gamma}^{calo} \epsilon_{\mu\mu\gamma}^{calo}}{N_{\mu\mu\gamma}^{calo} \epsilon_{\pi\pi\gamma}^{calo}}$$

$N_{\pi\pi\gamma}^{calo}$ = $\pi\pi\gamma$ data selected with CALO trg

$N_{\mu\mu\gamma}^{calo}$ = $\mu\mu\gamma$ data selected with CALO trg

$N_{\pi\pi\gamma}^{dc}$ = $\pi\pi\gamma$ data selected with DC trg

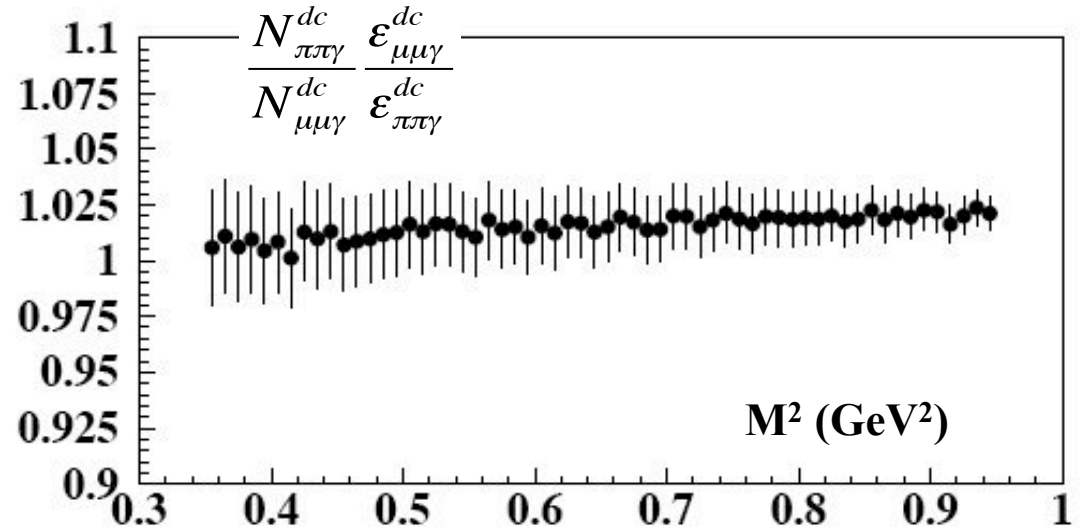
$N_{\mu\mu\gamma}^{dc}$ = $\mu\mu\gamma$ data selected with DC trg

$\epsilon_{\pi\pi\gamma}^{calo}$ = $\pi\pi\gamma$ absolute CALO trg efficiency

$\epsilon_{\mu\mu\gamma}^{calo}$ = $\mu\mu\gamma$ absolute CALO trg efficiency

$\epsilon_{\pi\pi\gamma}^{dc}$ = $\pi\pi\gamma$ relative DC trg efficiency

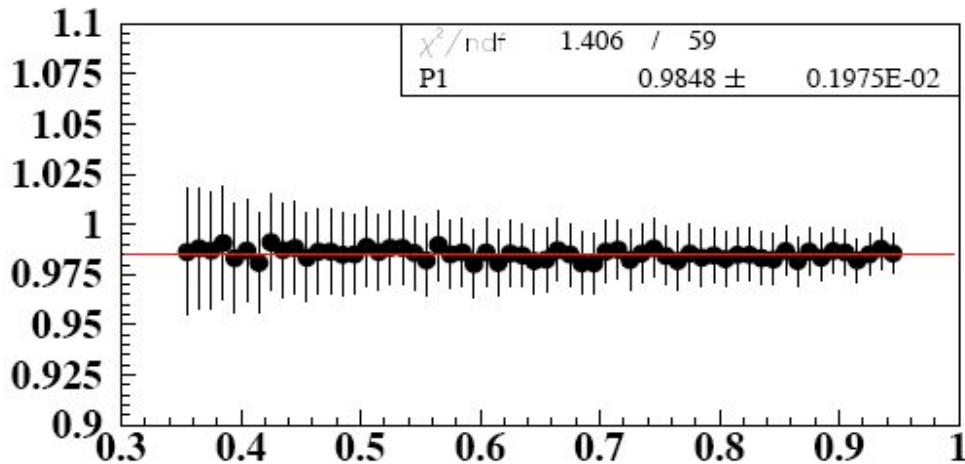
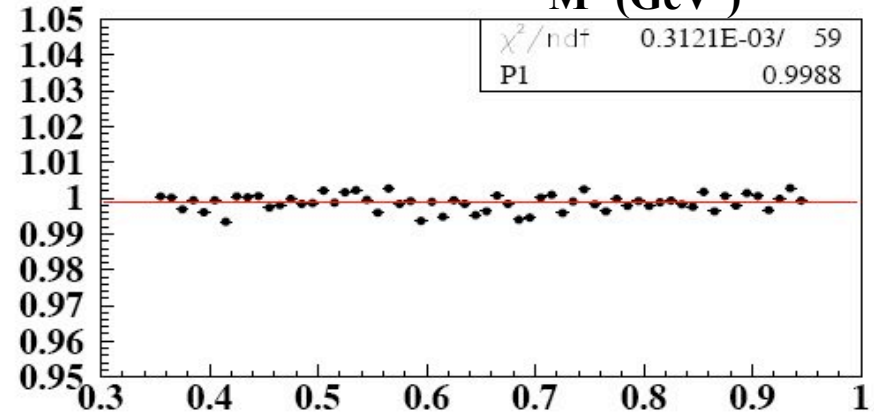
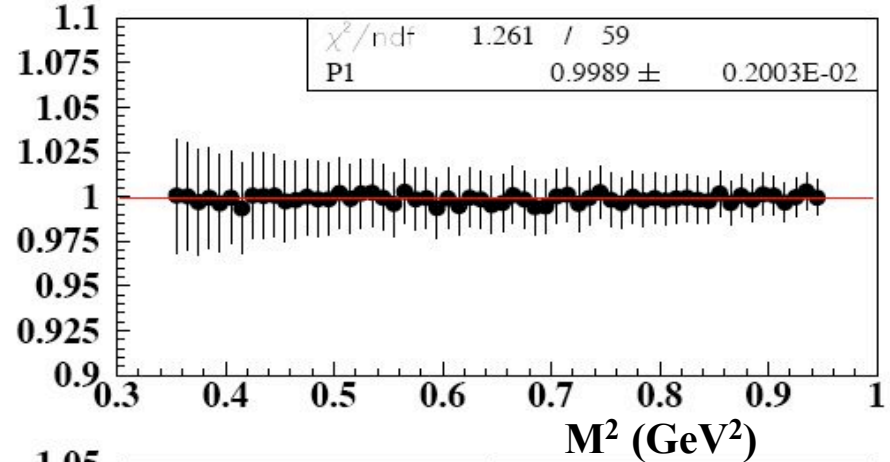
$\epsilon_{\mu\mu\gamma}^{dc}$ = $\mu\mu\gamma$ relative DC trg efficiency



Checks allowed by the ratio

$$\frac{N_{\pi\pi\gamma}^{dc} \epsilon_{\mu\mu\gamma}^{dc}}{N_{\mu\mu\gamma}^{dc} \epsilon_{\pi\pi\gamma}^{dc}} \Bigg/ \frac{N_{\pi\pi\gamma}^{calo} \epsilon_{\mu\mu\gamma}^{calo}}{N_{\mu\mu\gamma}^{calo} \epsilon_{\pi\pi\gamma}^{calo}}$$

to extremely check the alignment,
 below is the same plot, fitted
 without considering the errors,
 what if I took a CALO trigger $\pi\pi\gamma$
 efficiency different by 1.5-2%?





Partial conclusions

- 1) Systematic uncertainties have been assessed for both *CALO* and *DC* trigger issues
- 2) Revision of the 2001 trigger correction is done
- 3) At the moment the accuracy is (conservatively) below 0.5%

Master formula for the ratio

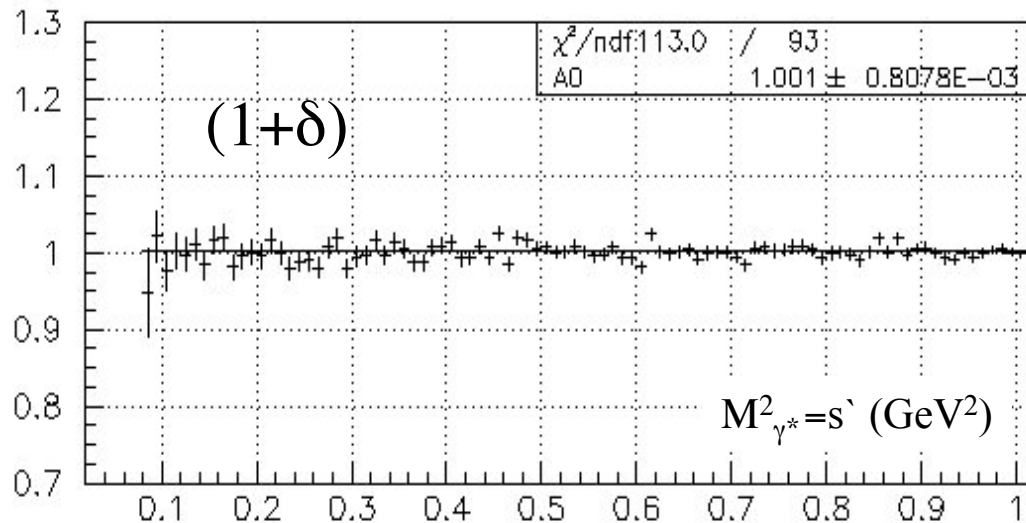
$$\sigma_{\pi\pi}^{Born}(s') \approx \frac{d\sigma_{\pi\pi\gamma}^{obs}/ds'}{d\sigma_{\mu\mu\gamma}^{obs}/ds'} \sigma_{\mu\mu}^{Born}(s')$$

is exact only in the absence of FSR

in fact

$$|F_{\pi}(s')|^2 \cdot \underbrace{(1 + \delta(s'))}_{\text{corr. due to FSR}} = \frac{4(1 + 2m_{\mu}^2/s')\beta_{\mu}}{\beta_{\pi}^3} \cdot \frac{(d\sigma_{\pi\pi\gamma}/ds')}{(d\sigma_{\mu\mu\gamma}/ds')}$$

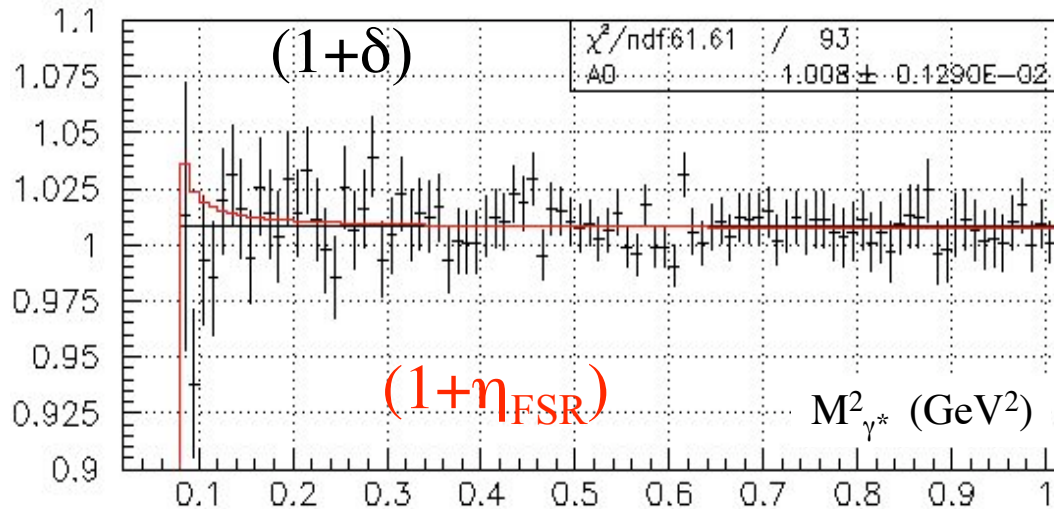
in principle: measured cross sections
for tests: MC generated ones



As expected, $\delta=0$ for ISR only
Radiator function is independent of
final state and cancels out exactly.

Accounting for FSR effects in the ratio

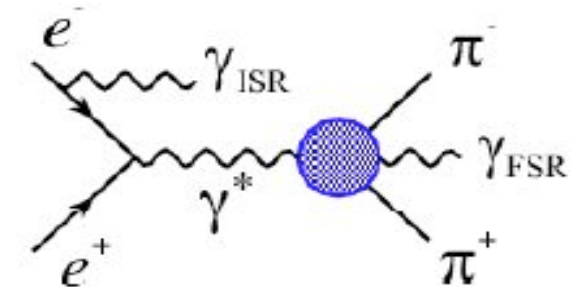
MC: $\pi\pi\gamma$ ISR + FSR nlo („unshifted“) and $\mu\mu\gamma$



Dividing for $(1+\eta_{\text{FSR}})$ and fitting with a constant gives $A_0 = (1.000 \pm 0.128\text{E-}02)$. Also here radiator cancels, leaving only FSR effects.

the idea is to rely on QED FSR corrections for $\mu\mu\gamma$ events and extract F_π inclusive for $\pi\pi\gamma$ FSR

$|F_\pi|^2 \cdot (1+\eta_{\text{FSR}})$ is the quantity to be put in the a_μ^{had} dispersion integral obtained directly from the ratio



$$|F_\pi(s')|^2 \cdot (1 + \eta(s')) = \frac{4(1 + 2m_\mu^2/s')\beta_\mu}{\beta_\pi^3} \cdot \frac{\left(\frac{d\sigma_{\pi\pi\gamma}^{\text{corr}}(\theta^{\pi\pi} < 15^\circ)}{ds'} \right)}{\left(\frac{d\sigma_{\mu\mu\gamma}^{\text{corr}}(\theta^{\mu\mu} < 15^\circ)}{ds'} \right)} \cdot A(\theta^{I+\text{FSR}} / \theta^{\text{ISR}})$$

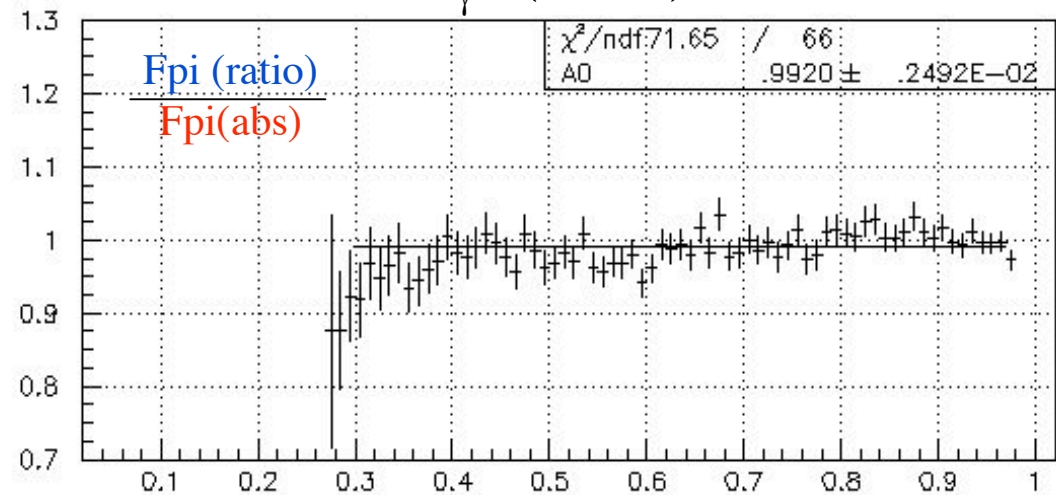
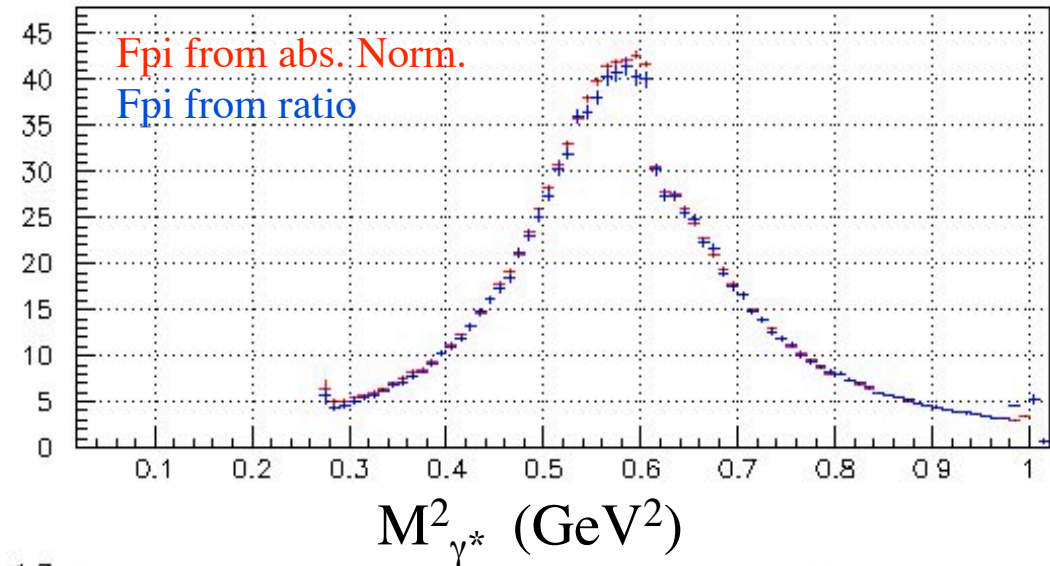
Roadmap

Filfo	from the prescaled events (unbiased control sample) - syst. error is negligible	✓
Background	MC shapes fitted to data - small work on systematics to be done	(✓)
M_{Trk}, E_{Miss}	from MC re-weighted from data - cross check with data Distributions (optimize smearing) - check with UFO	(✓)
Trigger	Solid	✓
Vtx-Track(~ 0.6%)-Like	Up to now from MC, Agreement data-MC < 1%?? Use Neural Net for independent control samples.	
$Q^2_{Rec} \rightarrow Q^2_{Kine}$	From MC. Has to be revisited. Effect in ρ - ω Region.	
Acceptance	$\theta_\pi, p_T, p_z, \theta$. Data-MC comparison?	(✓)
Unshifting ($Q^2_{+-} \rightarrow Q^2_{\gamma^*}$)	PHOKHARA_omega (only for pions!)	(✓)
Luminosity	VLAB. Eff. Cross section for 2002? New BABAYAGA?	(✓)
Radiator	Only for absolute measurement. (Cross check with muons).	✓

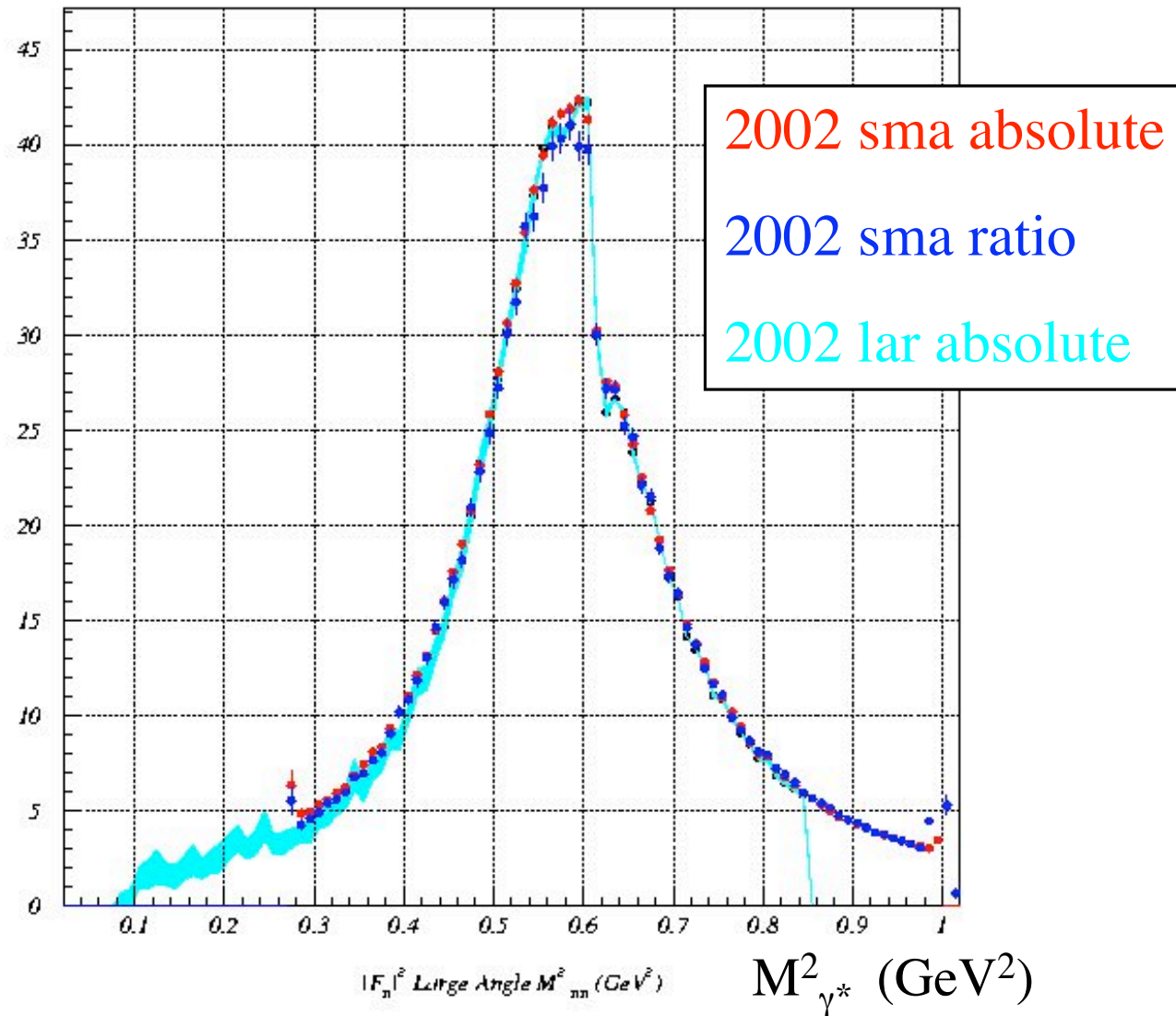
blue = estimated from MC
red = estimated from data

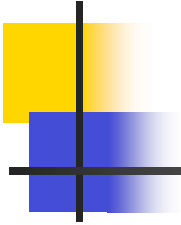
Extracting the form factor in 2 ways

$$|F_{\pi}(s')|^2 \propto \frac{1}{H \cdot VP} (d\sigma_{\pi\pi\gamma} / ds')$$



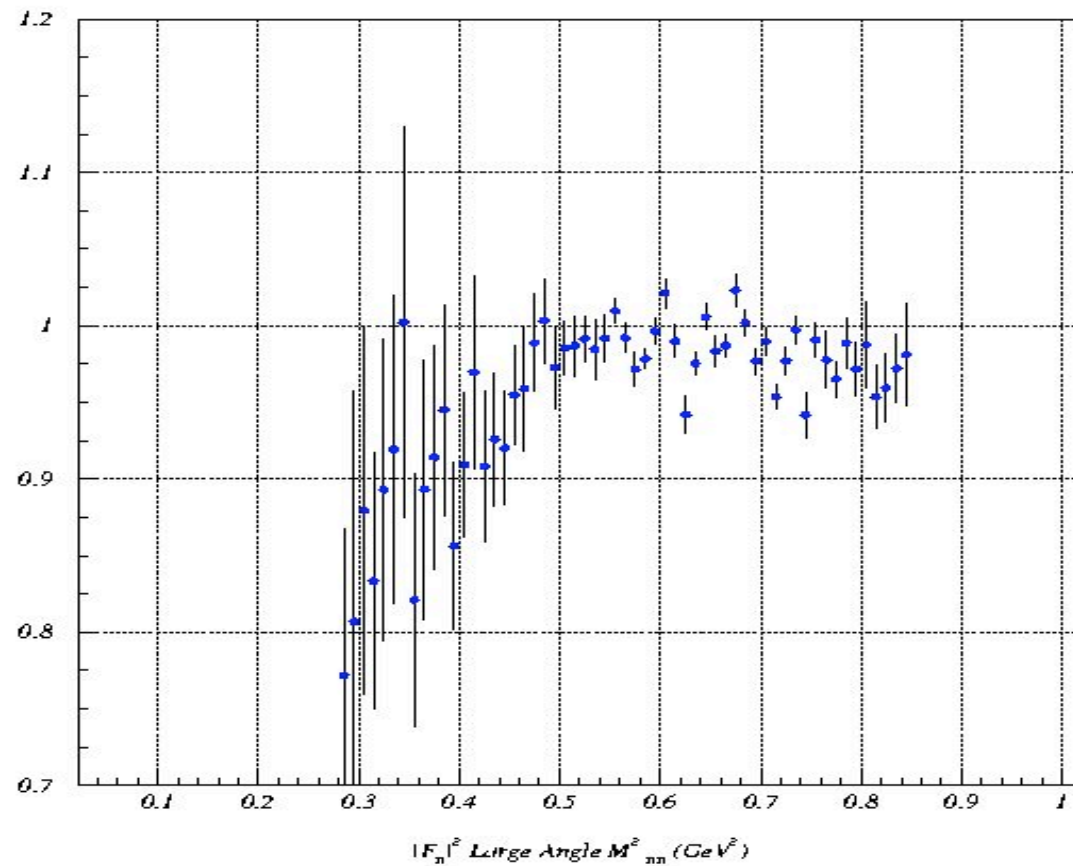
Comparisons of 2002 results

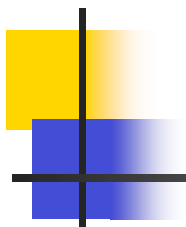




Relative comparison

2002 relative comparison SMA(abs) - LA(abs)





New tool

π/μ discrimination using Neural Network

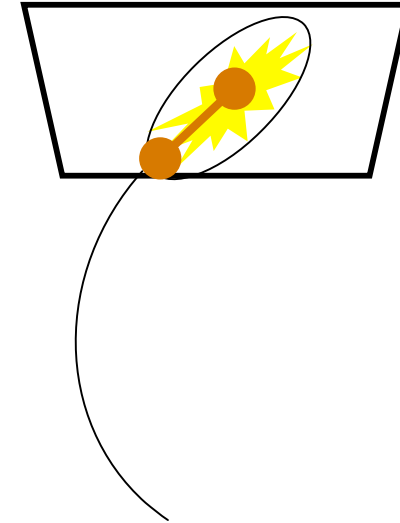
- A clean sample of muons/pions useful for
 - Efficiencies
 - Background
- The idea is to discriminate pions/muons for single track, according to the different interaction with the calorimeter

Discriminant variables

- 4 discriminant variables were selected:

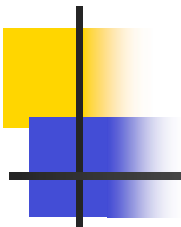
- $V1 = E_{clu}/E_K(m_m)$
- $V2 = |d_{clu} - d_{ext}|$
- $V6 = b = L/cT_{clu}$
- $V11 = dT = T_{CLU} - L_{TRK}E(m_m) / pc$

$$L_{TRK} = L_{F.H.} + L_{D.C.} + L_{extp} + D_{clu}$$



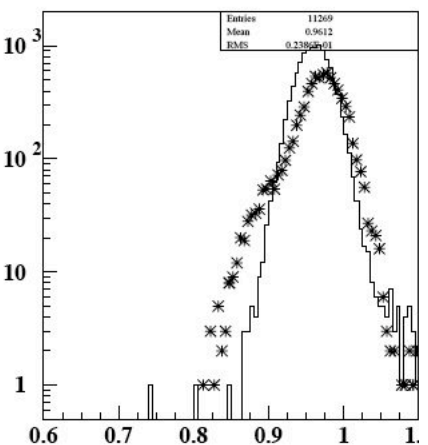
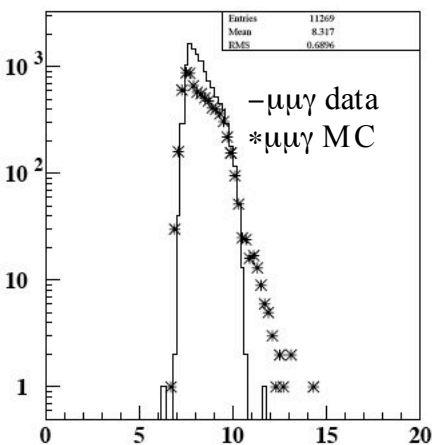
- The cluster is the most energetic associated to the track (within 60cm). Newextratom is used
- The track is required to satisfy the ppg acceptance:
 - $50 < q < 130$, ($PT > 160$ MeV or $|PZ| > 90$ MeV)
 - $r_{FH} < 50$ cm, $\rho P.C.A. < 8$ cm, $|Z_{PCA}| < 7$ cm
- The vtx is not required (information from DTFS)

Condition on
the candidate
trk

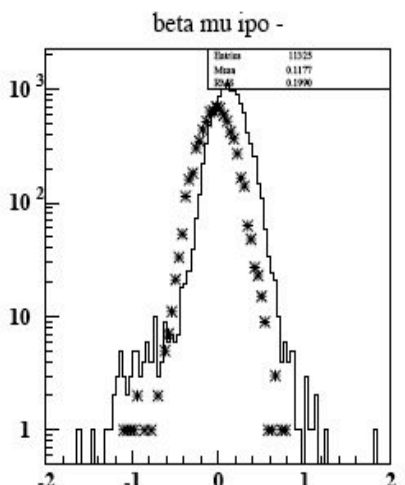
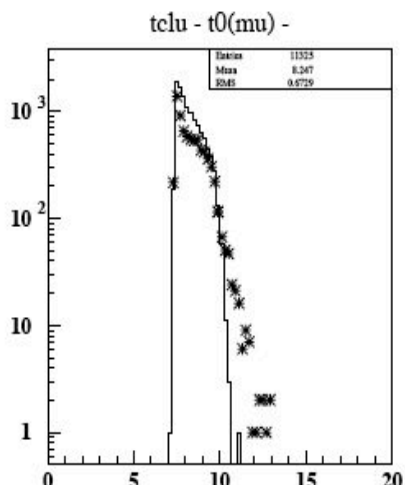
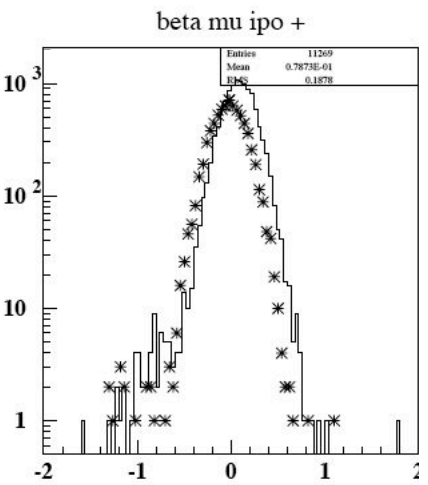
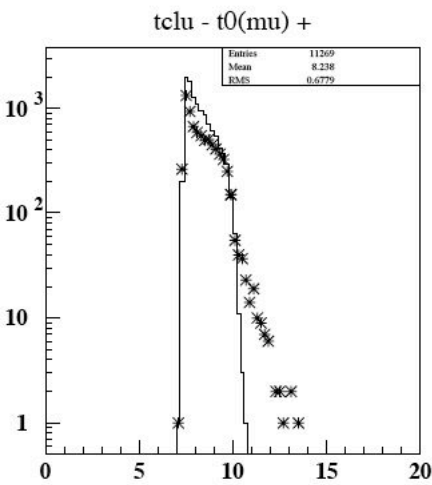
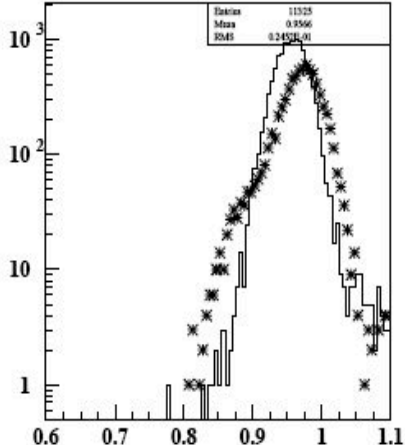
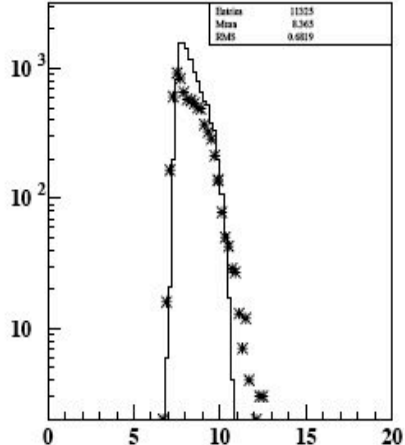


Time distributions: data vs MC

mu+ 2007/01/19



mu- 2007/01/19 14.48



T track mu ipo +

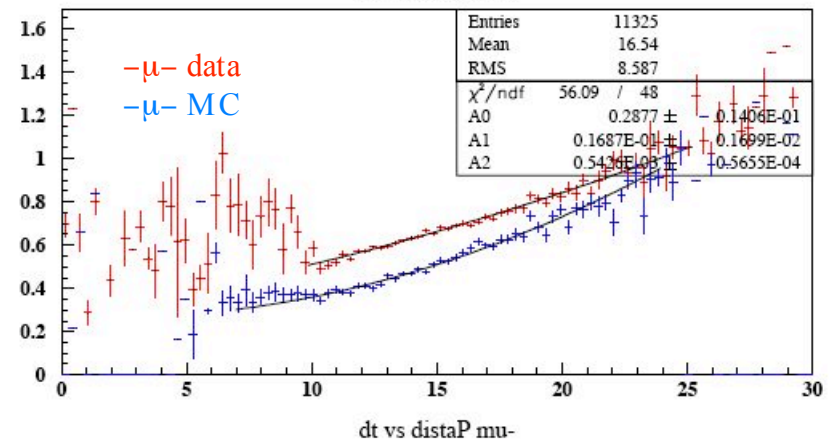
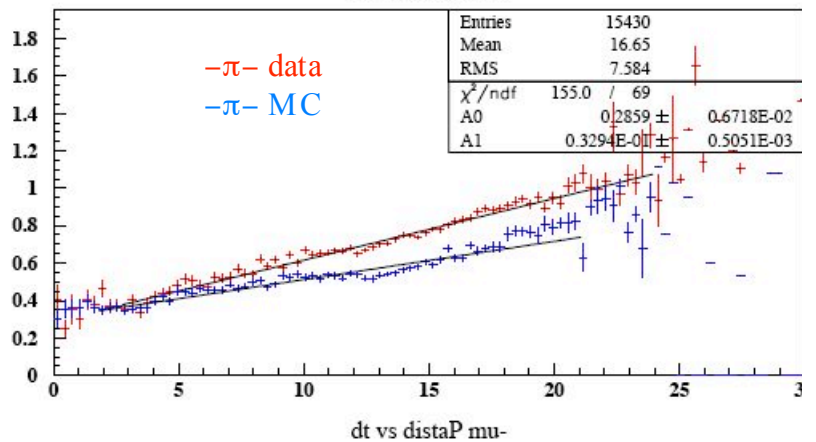
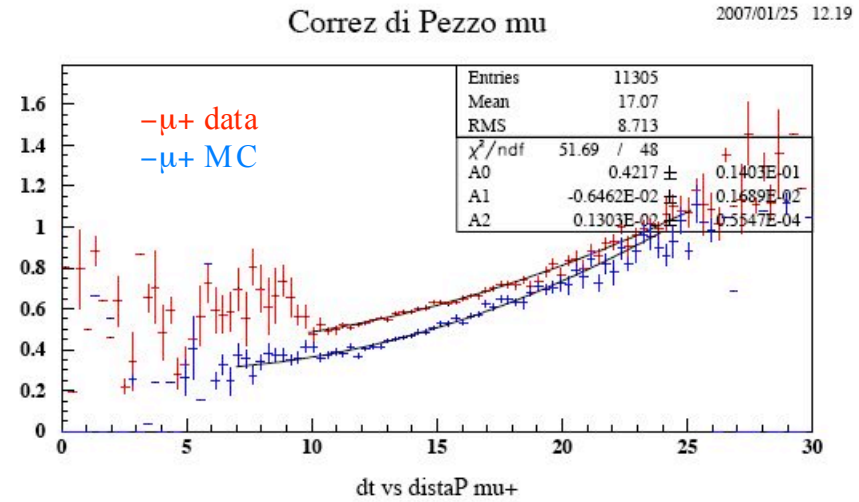
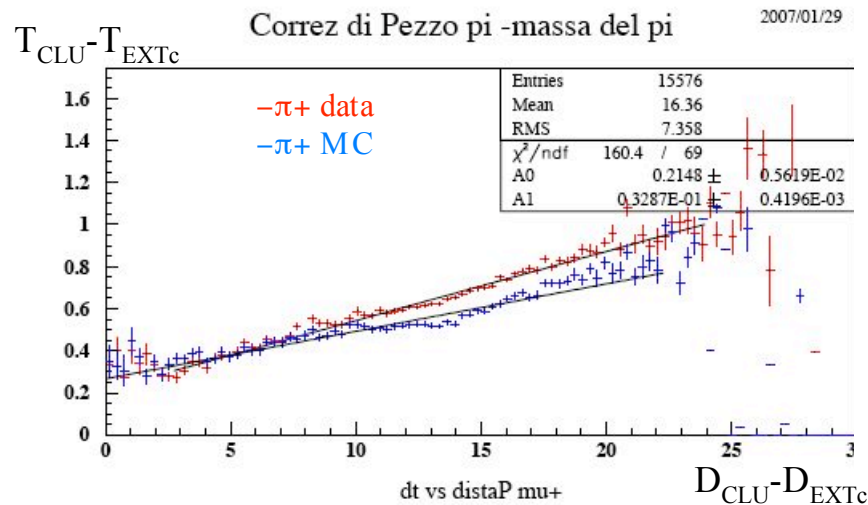
deltat muon mass +

T track mu ipo -

deltat muon mass -

Time (pezzo) corrections

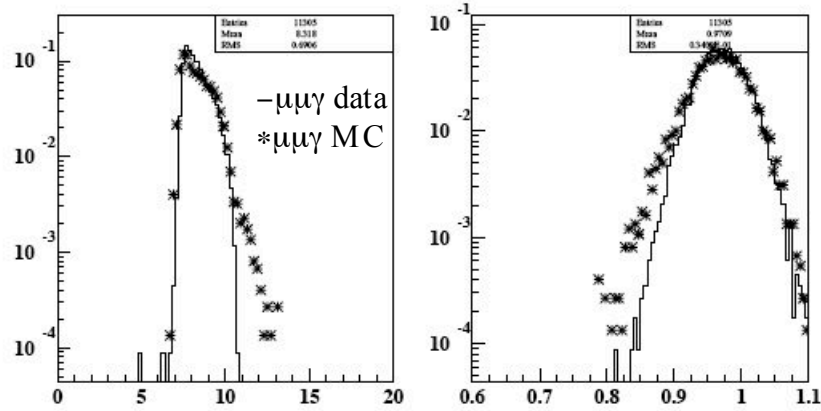
- We look at the time dependence in the EMC vs depth



After corrections

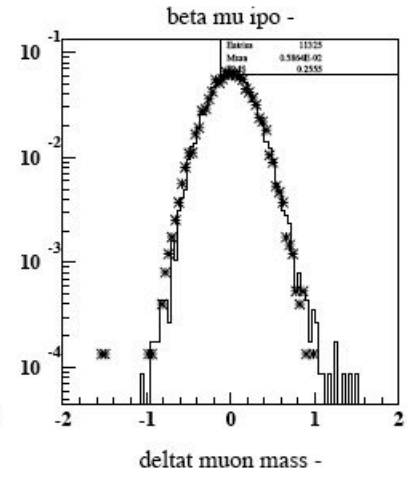
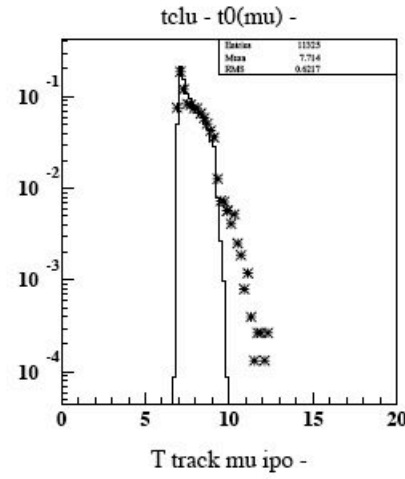
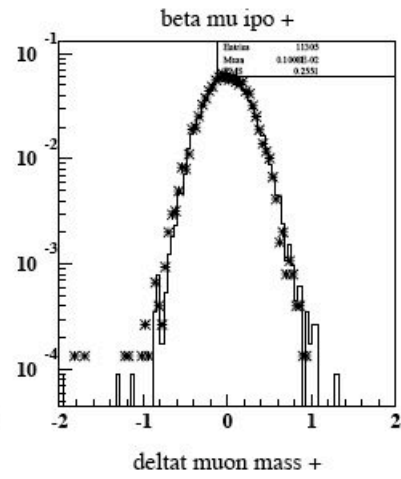
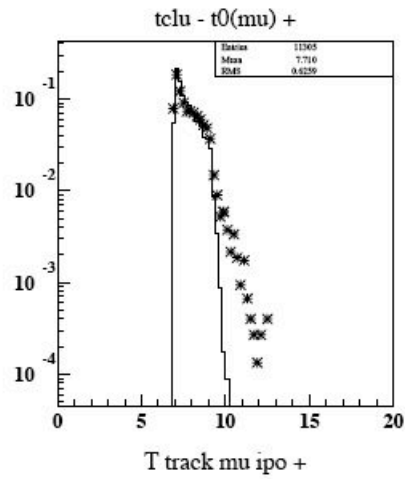
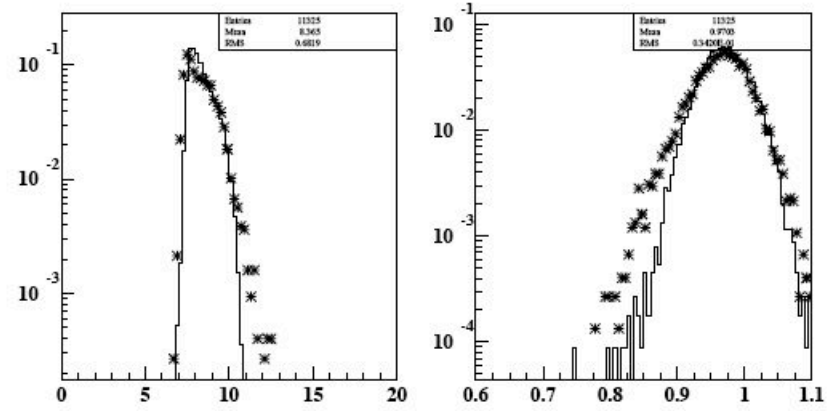
mu+ inclusive in mom

2007/01/29 20.32

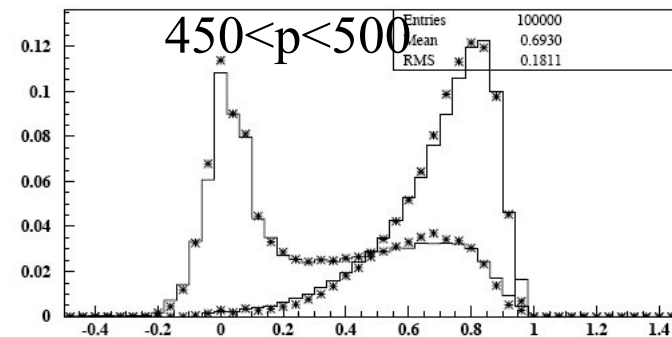
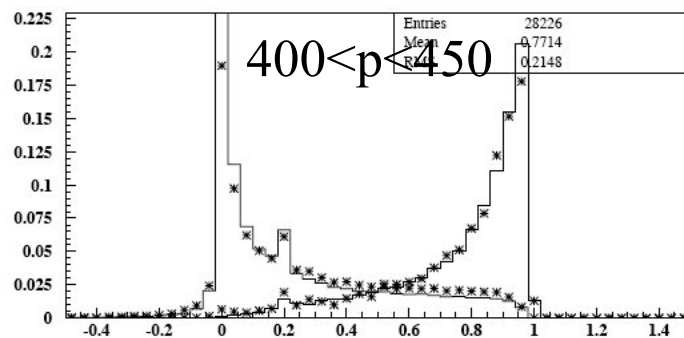
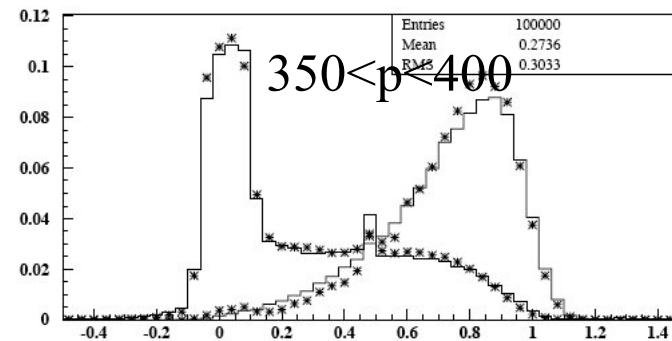
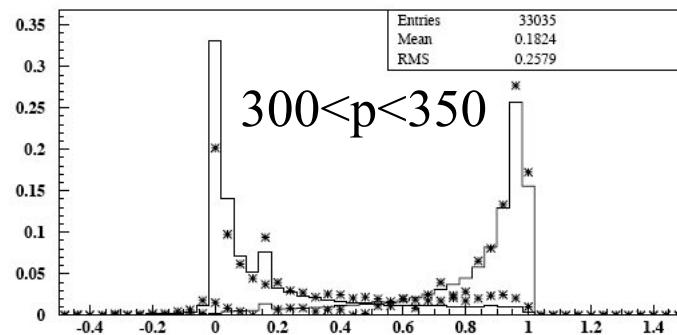
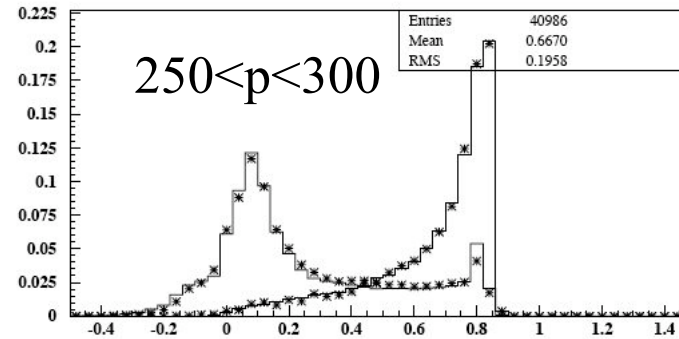
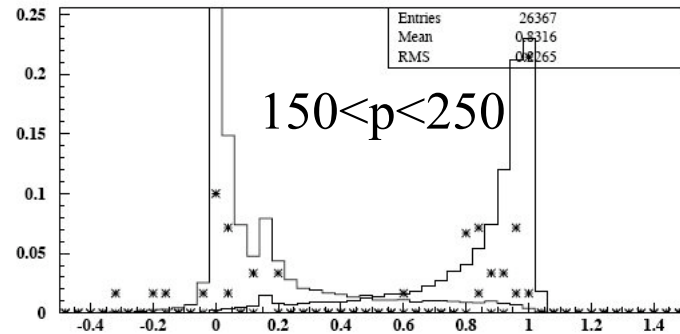


mu+ inclusive in mom

2007/01/29 20.32



NN output: positive track





Conclusions

1) both small angle analyses have reached an important point:

the form factor has been measured both in the absolute normalisation and the ratio.

2) estimate of some systematics are still missing and work is going on in this direction with use of new tools and exchanging ideas with large angle people

3) we expect only small corrections from the missing studies

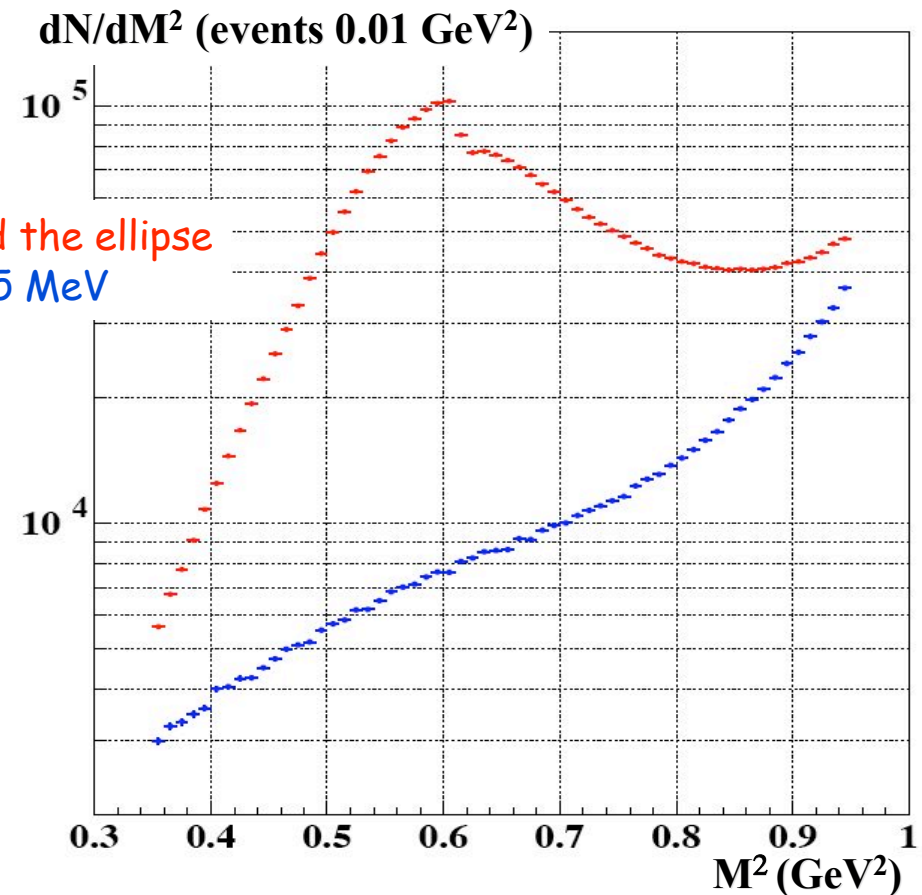
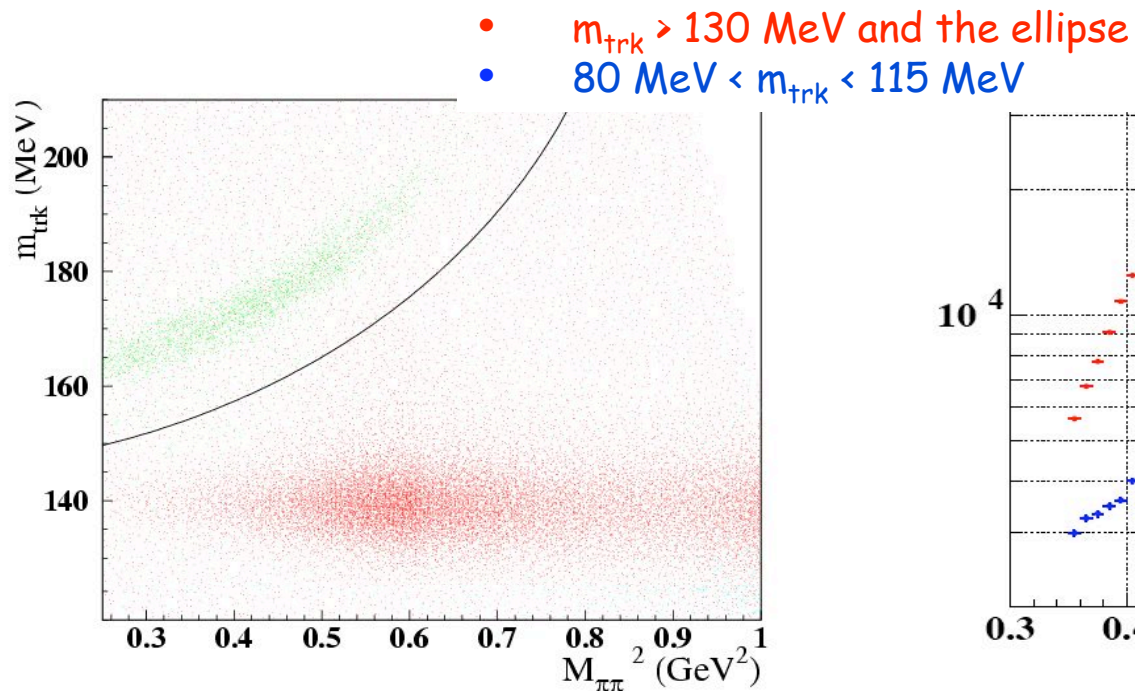
The goal is to have results ready for the summer conferences

Selection steps: a reminder

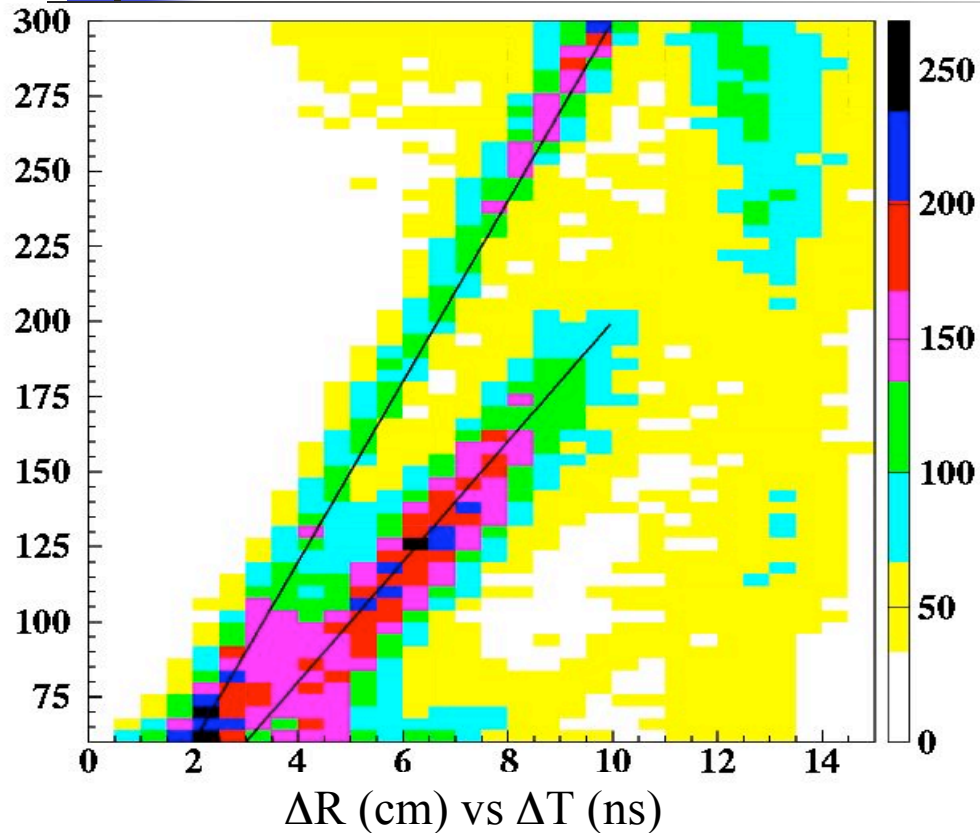
New FILFO
New PPGTAG
No Cosmic VETO

- 1 vertex ($|z| < 7$ cm) connected to 2 and only 2 tracks
- each track with $50^\circ < \theta_{\text{track}} < 130^\circ$
- small angle γ ($\theta_{\pi\pi} < 15^\circ$)
- at least one track with $\log L_\pi/L_e > 0$

2002 data: $L = 242.6$ pb $^{-1}$



$E > 30$ MeV clusters in the rest - MC (1)

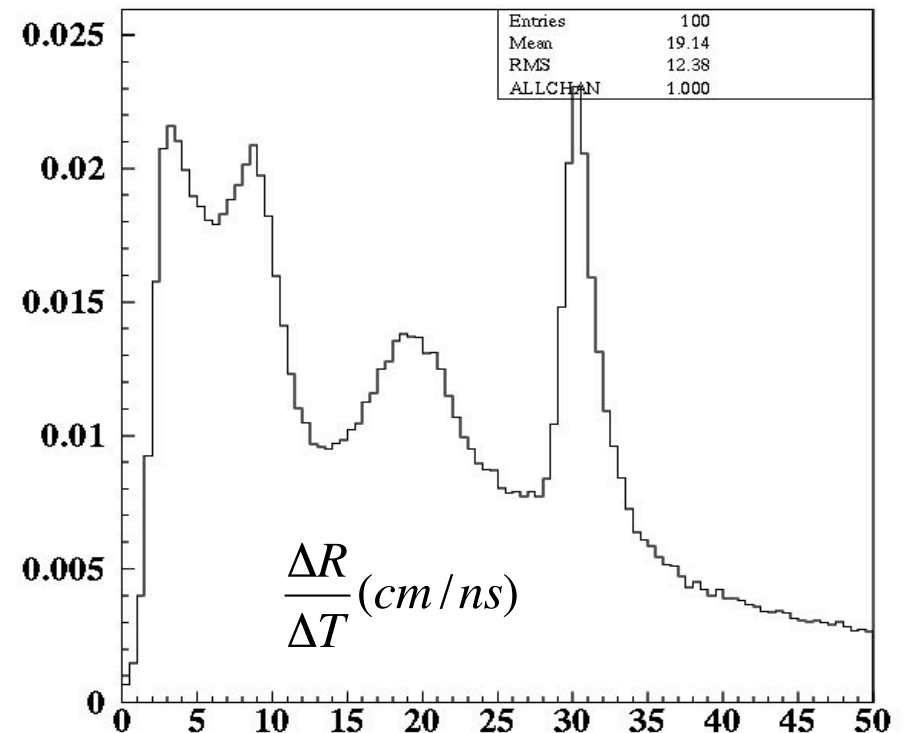


2. the rest is correlated with
both pions

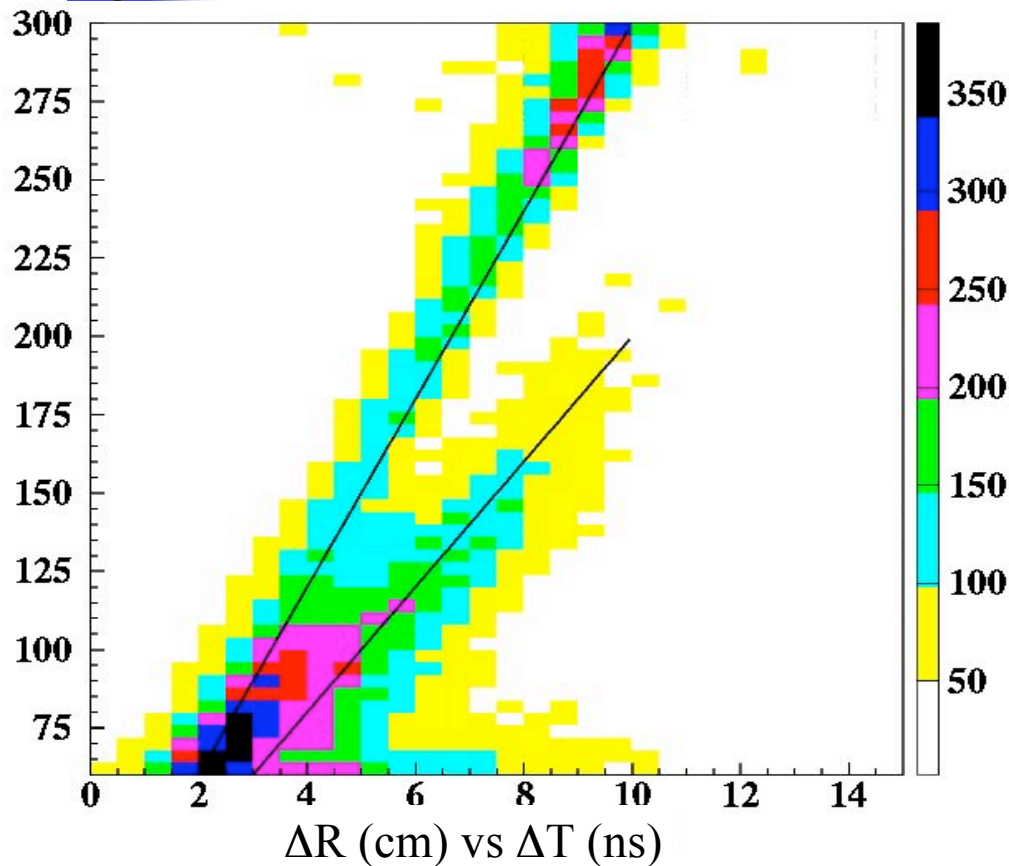
$$\Delta R = |\vec{x}_{clu} - \vec{x}_{ext}|$$

$$\Delta T = t_{clu} - t_{max}$$

t_{max} = time of most energetic
cluster within 60 cm from
extrapolated point



E>30 MeV clusters in the rest - MC (2)

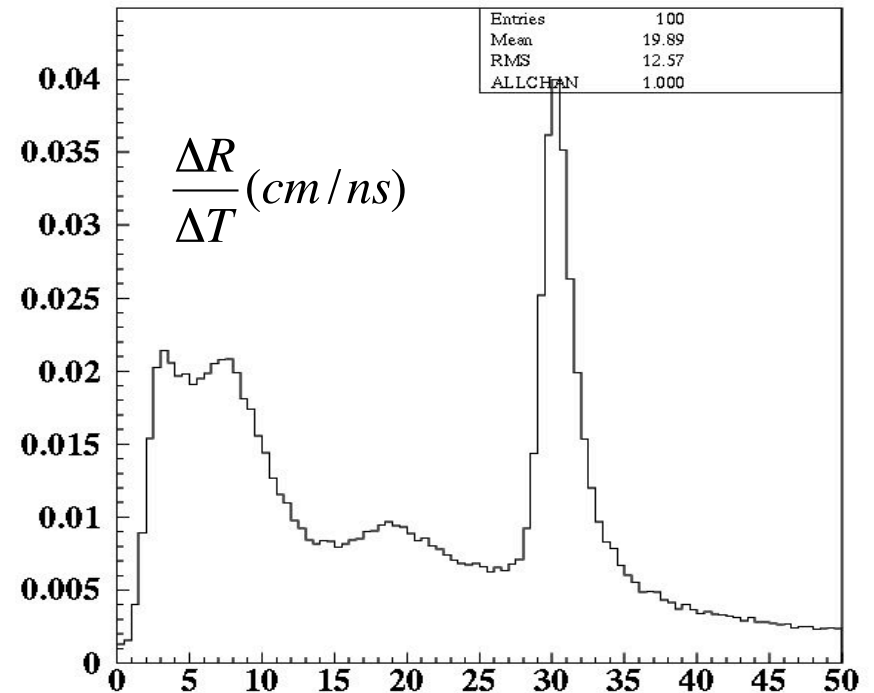


message: association radius
better be increased to 90 cm

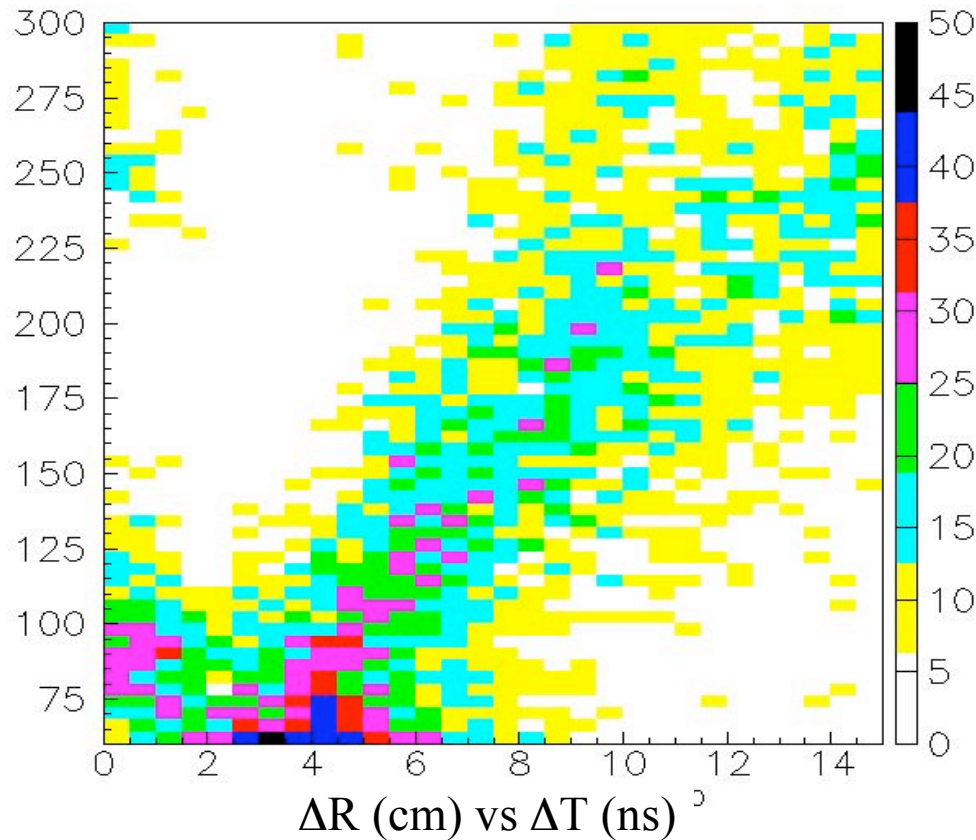
$$\Delta R = |\vec{x}_{clu} - \vec{x}_{ext}|$$

$$\Delta T = t_{clu} - t_{max}$$

t_{max} = time of most energetic
cluster within 60 cm from
extrapolated point



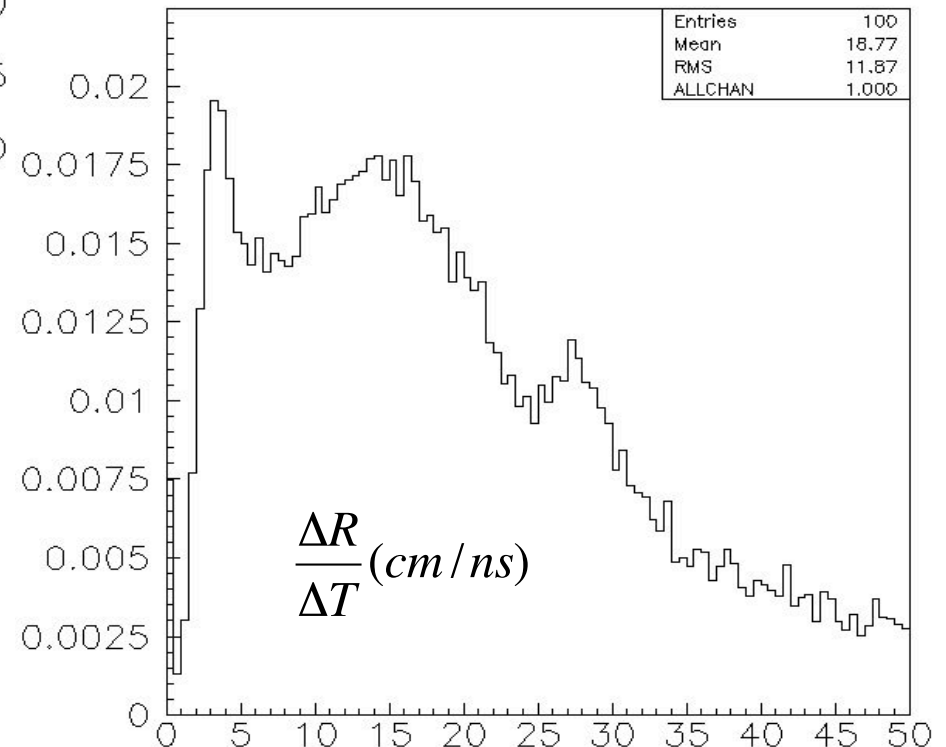
E>30 MeV clusters in the rest - data (1)



$$\Delta R = |\vec{x}_{clu} - \vec{x}_{ext}|$$

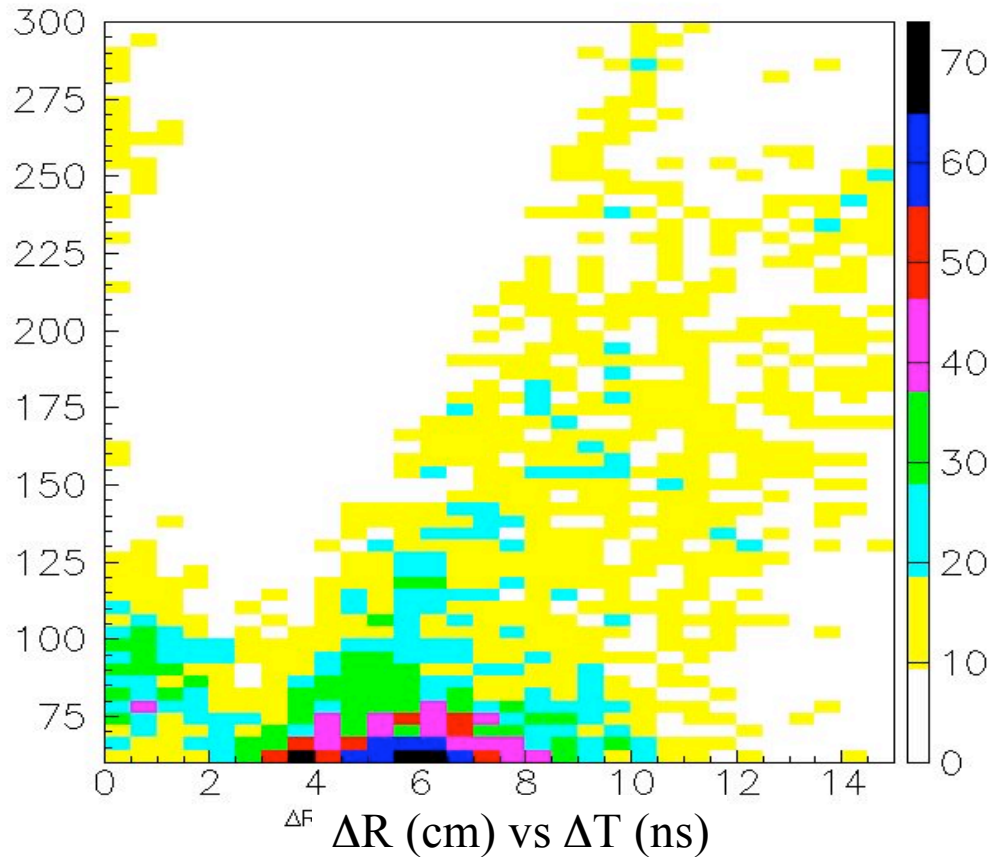
$$\Delta T = t_{clu} - t_{max}$$

t_{max} = time of most energetic cluster within 60 cm from extrapolated point



3. impact from photons much less relevant in real life

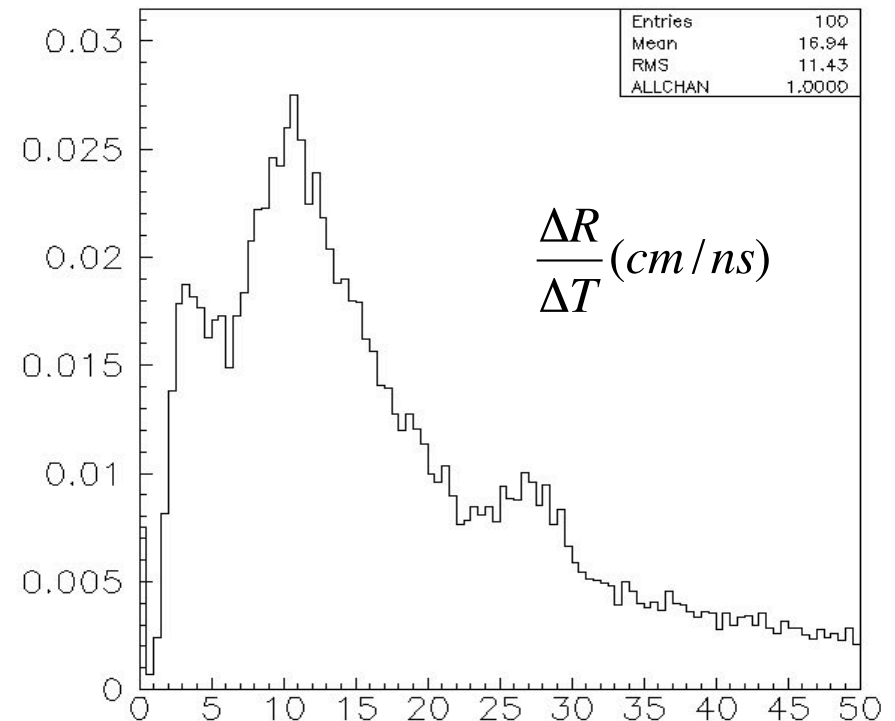
E>30 MeV clusters in the rest - data (2)



$$\Delta R = |\vec{x}_{clu} - \vec{x}_{ext}|$$

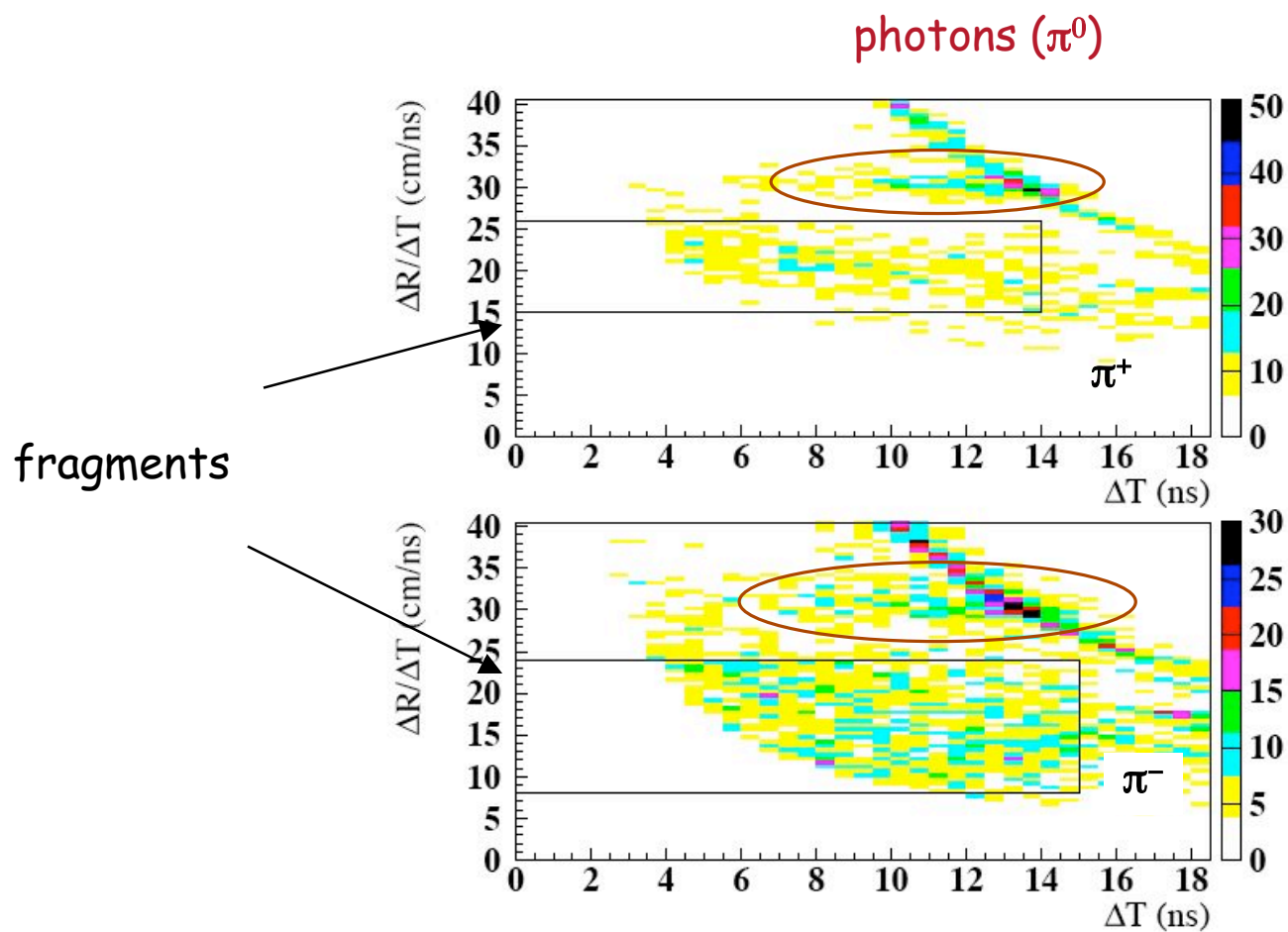
$$\Delta T = t_{clu} - t_{max}$$

t_{max} = time of most energetic cluster within 60 cm from extrapolated point



Assessed re-assignment

what's left over out of the 90 cm spheres?



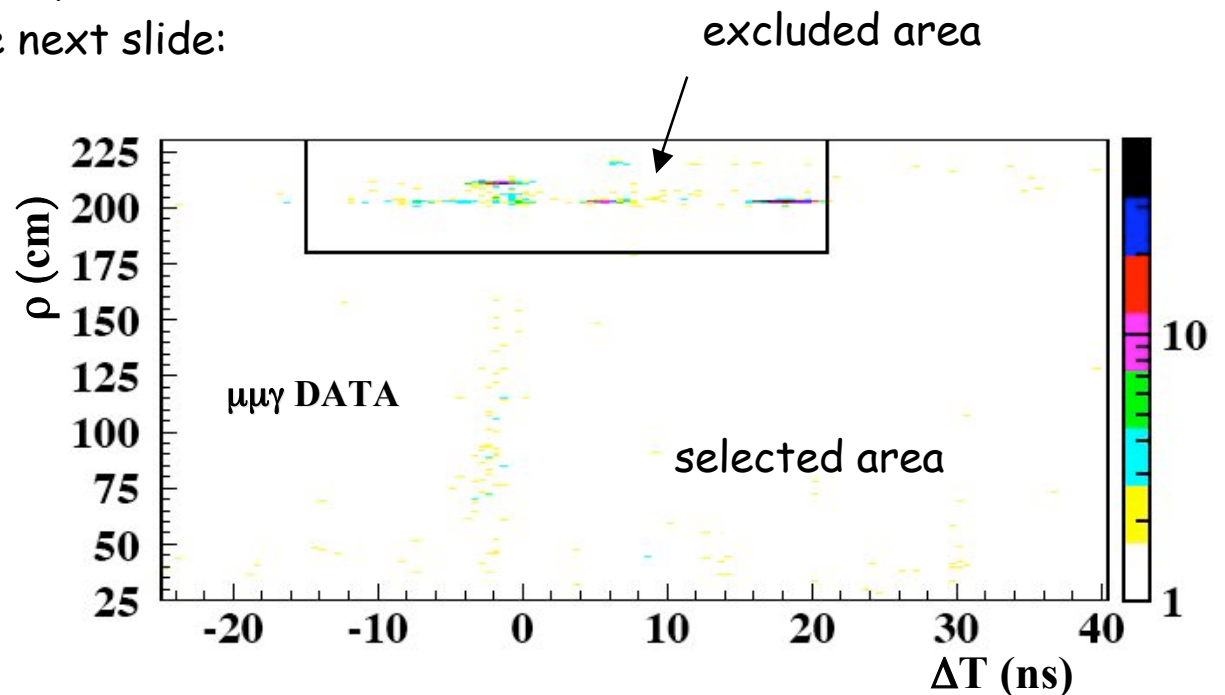
Correct identification of the rest (I)

our analysis: track polar angles must be directed on CALO barrel only, so End Cap clusters are good candidates for the rest of the event, namely accidentals or photons uncorrelated with charged particles

the following requirements to identify clusters of the rest are applied in OR with those in the next slide:

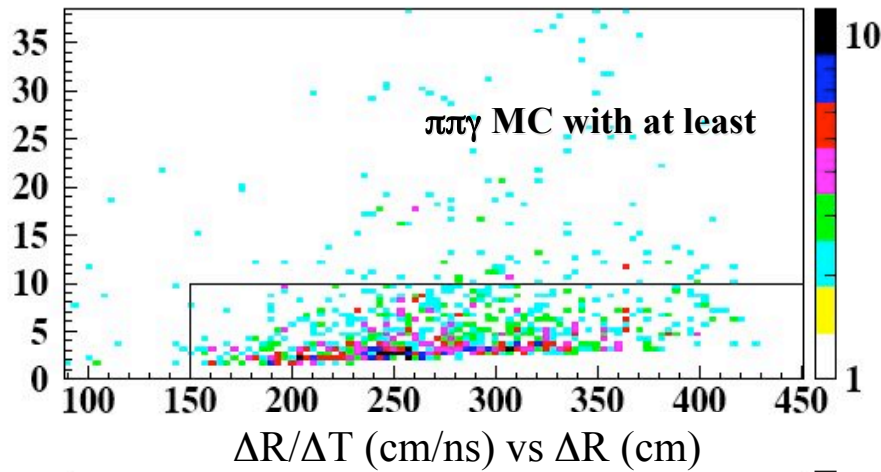
$$\rho = \sqrt{x_{clu}^2 + y_{clu}^2}$$

1. $\rho < 180$ cm, OR
2. $|\Delta T - 2.5 \text{ ns}| > 20$ ns

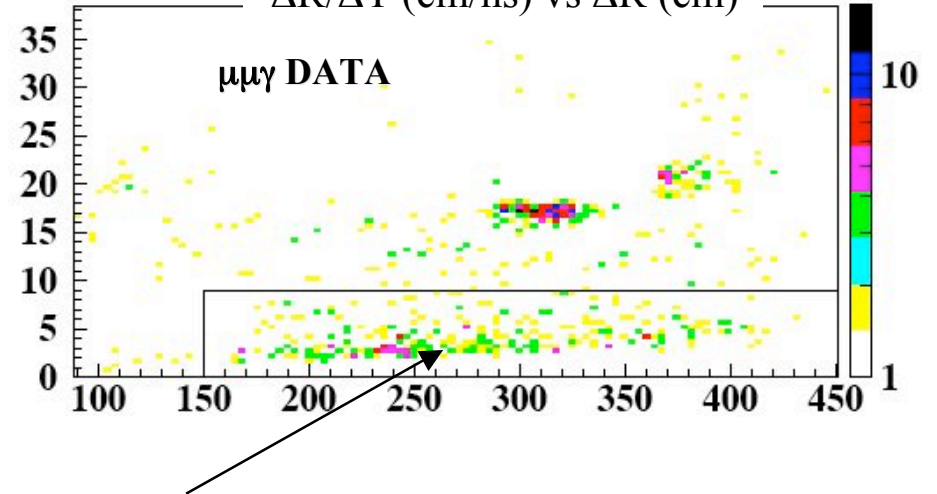
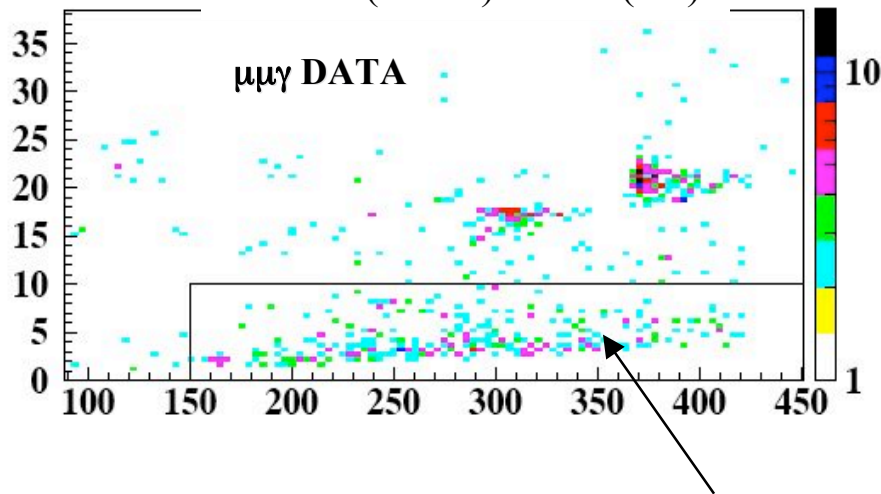
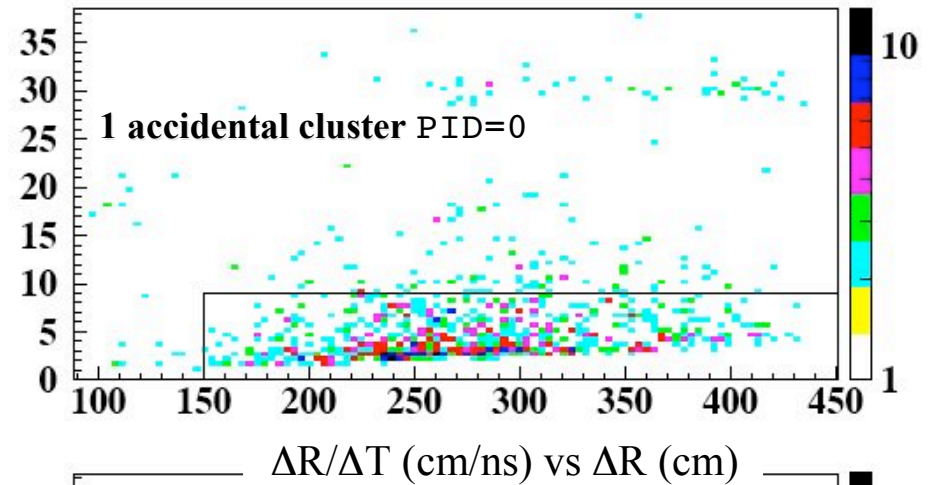


Correct identification of the rest (II)

positive charged track



negative charged track



selected areas