

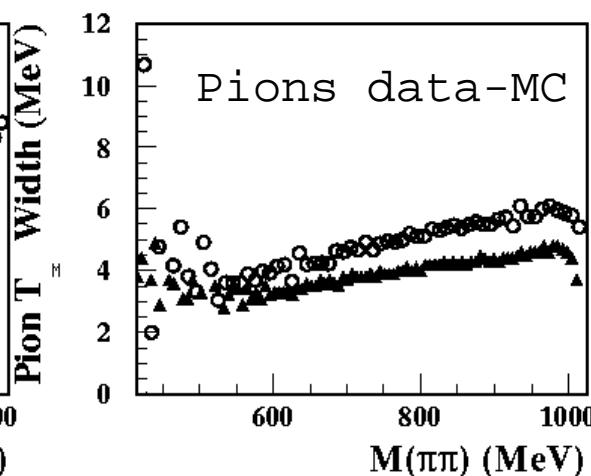
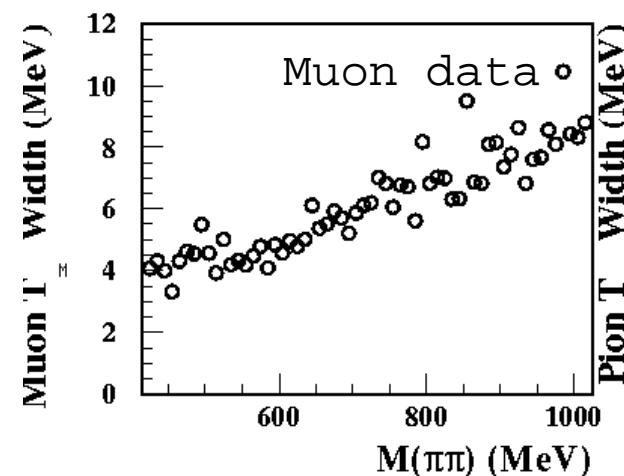
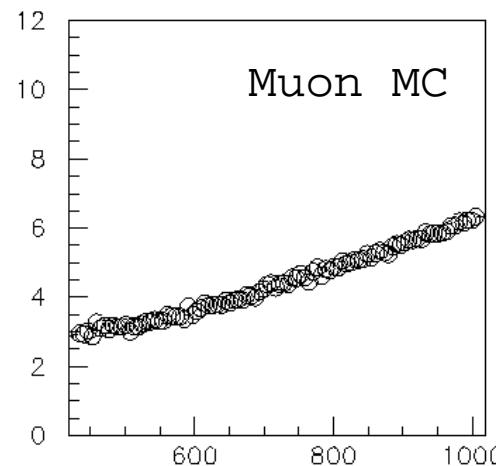
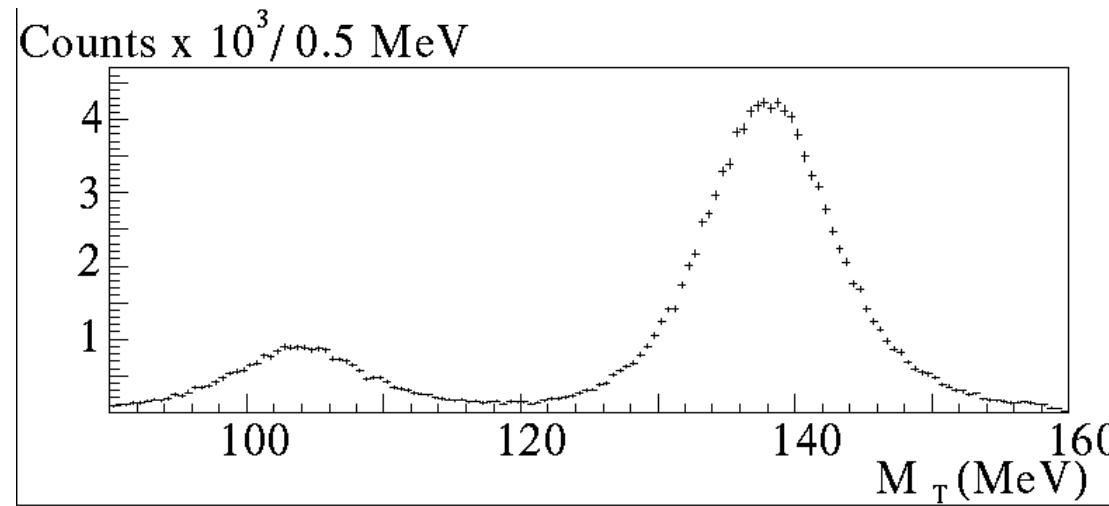
Status of $f_0(980) \rightarrow \pi^+ \pi^-$ analysis

- Study of background sources ($\mu^+ \mu^- \gamma, \pi^+ \pi^- \pi^0, \pi^+ \pi^- \rho^0$)
 ρ^0 line shape and $\rho^0 - \omega$ interference
- Three different fits to the same spectrum
- Charge asymmetry

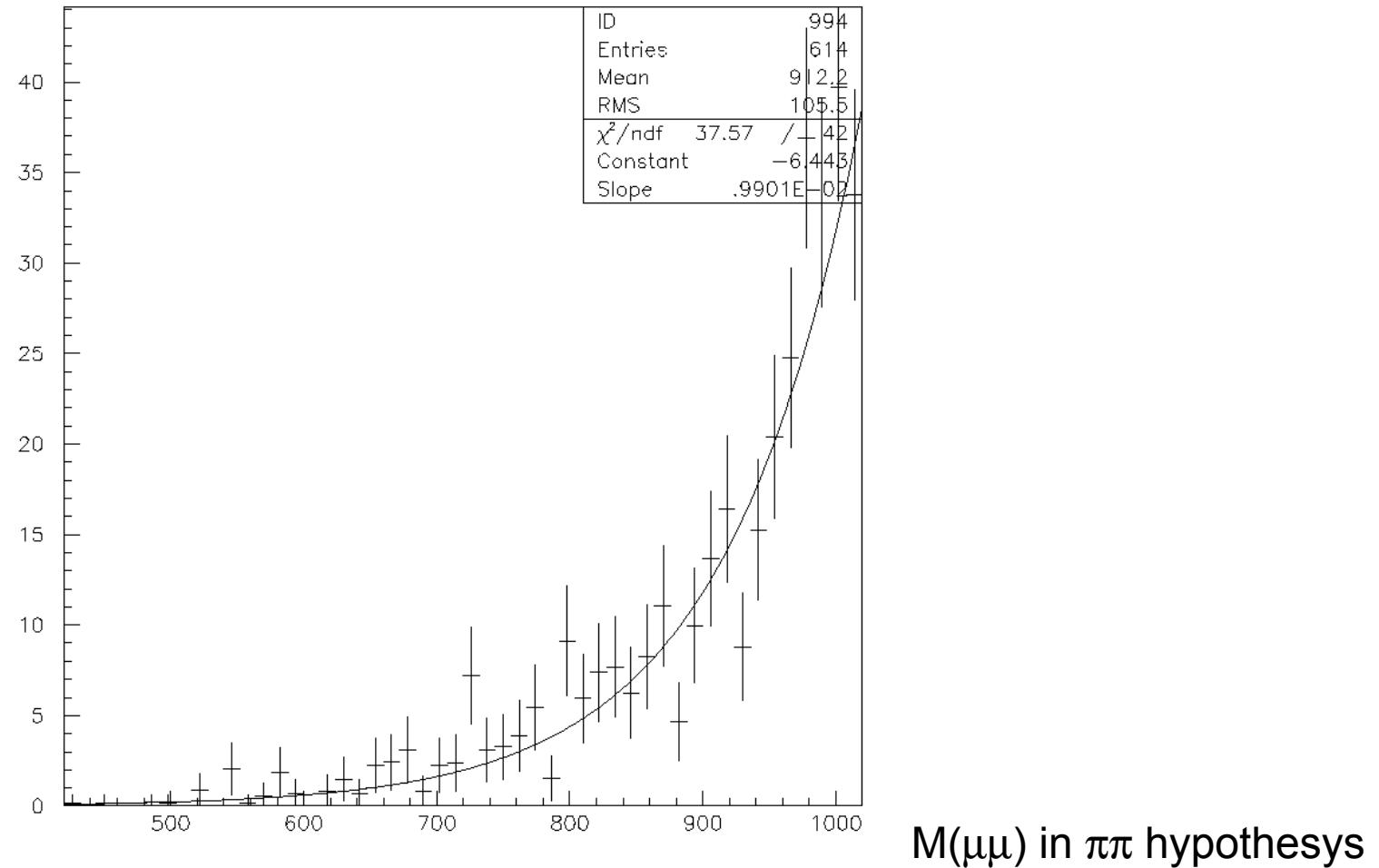
1. Study of background sources

$\mu^+\mu^-\gamma$: new generation based on *phokhara3*

Trackmass: comparison data-MC

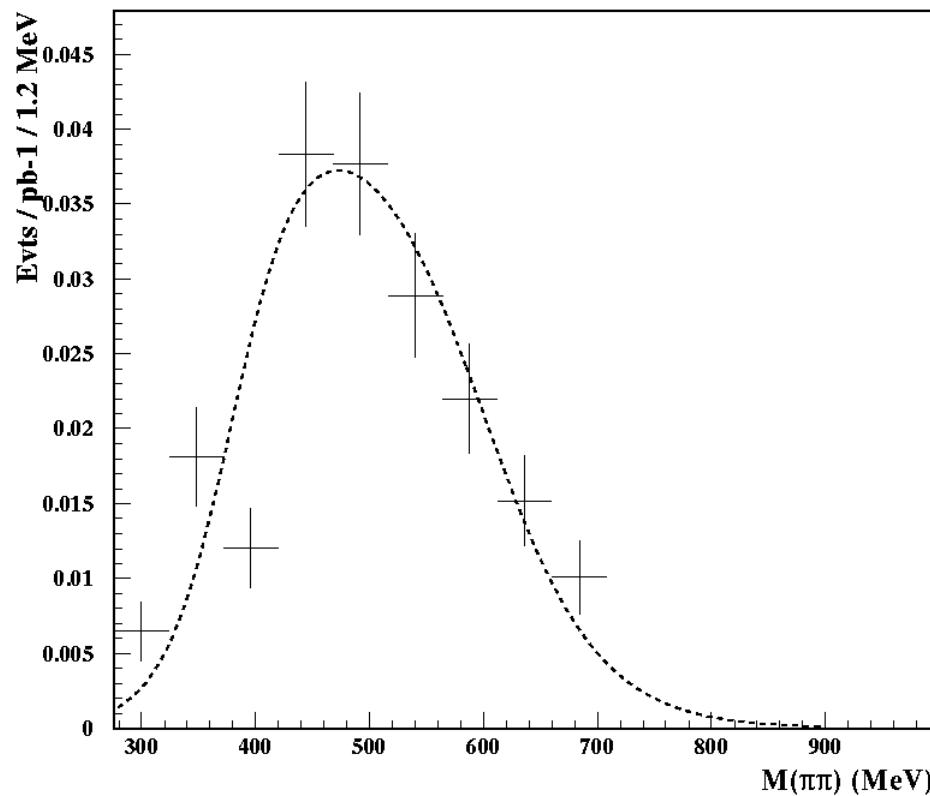


239 pb-1 MC sample → 360 evts surviving
→ 526 evts in the full sample
(6.8×10^5 data sample)



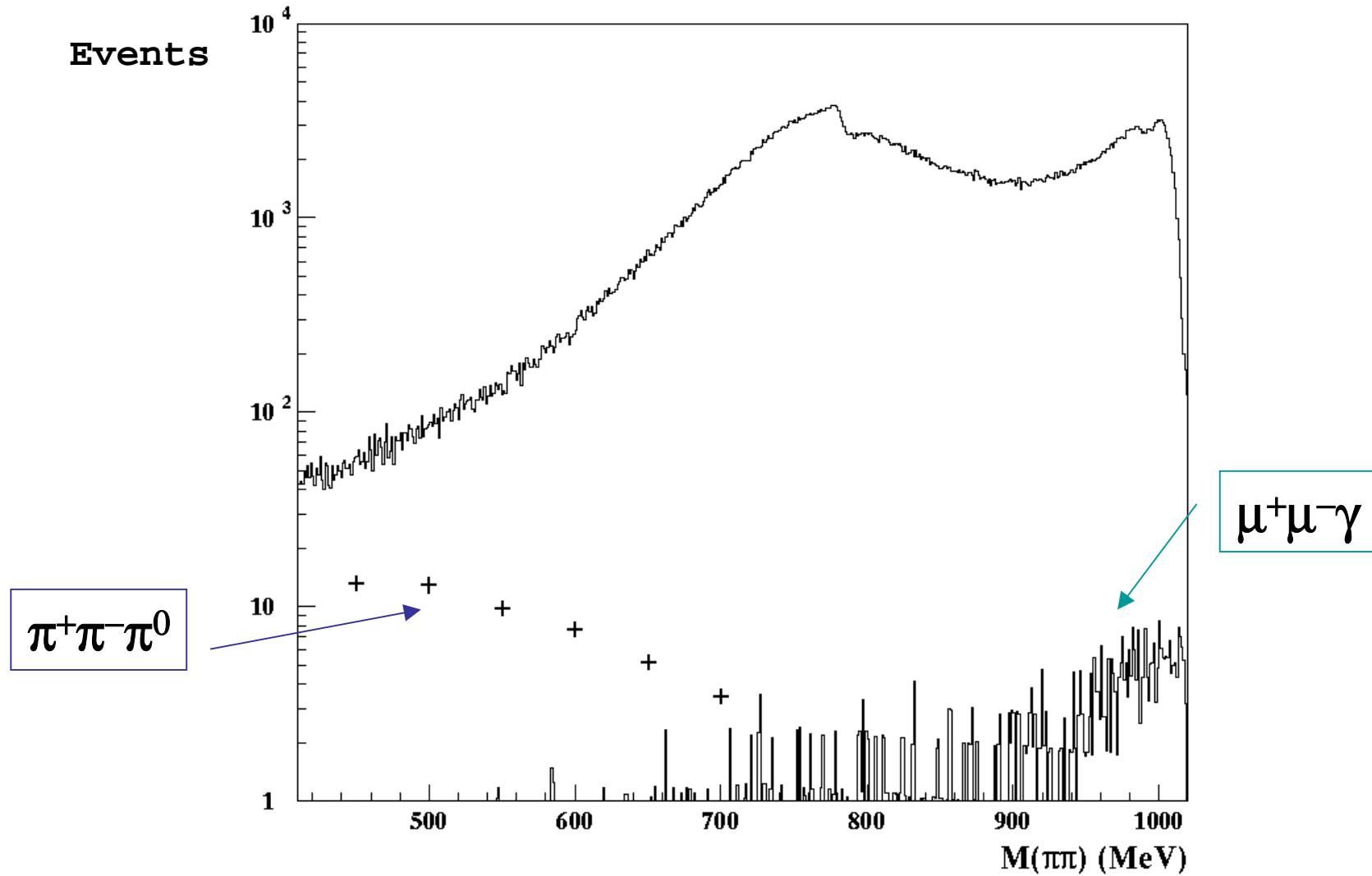
This curve is added to the fit function

$\pi^+\pi^-\pi^0$ higher statistics new generation
→ new function to add in the fit



$\pi^+\pi^-$ new two-body generator done
→ see possible tail on the high mass region

Present estimated backgrounds:



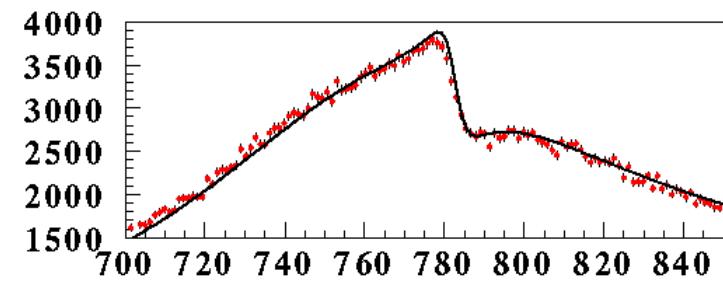
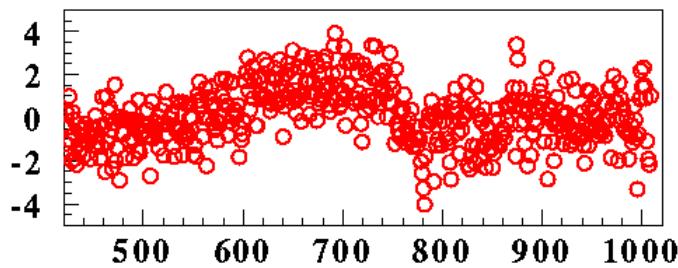
2. ρ^0 line shape and ρ^0 - ω interference

ρ^0 mass and width (773.3 and 144.1 MeV)

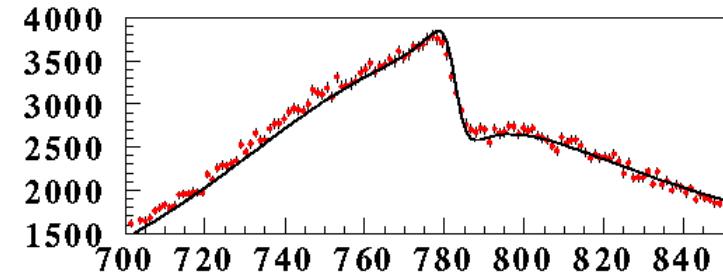
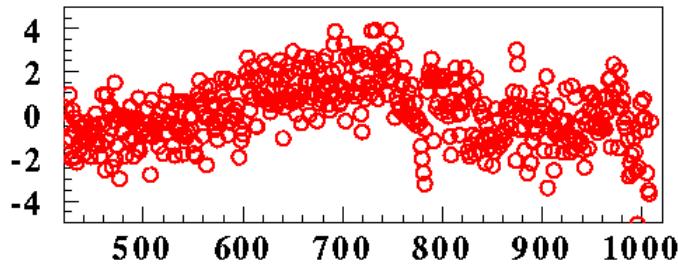
"not consistent" with $\pi^+\pi^-\pi^0$ analysis

(775.9 ± 0.7 and 147.3 ± 1.6 MeV). Try to force

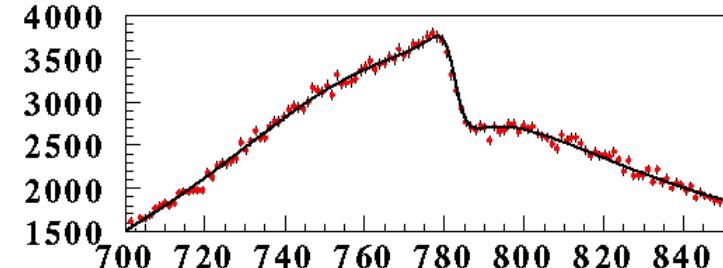
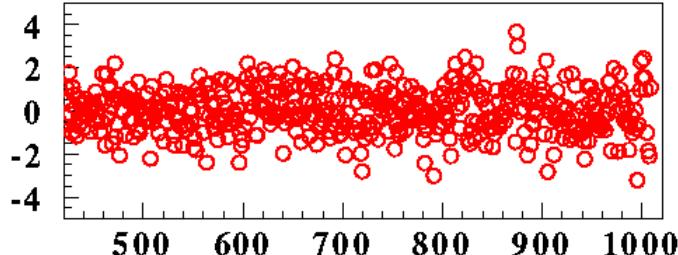
$M(\rho^0)$ and $\Gamma(\rho^0)$
forced



$M(\rho^0)$ forced



$M(\rho^0)$ and $\Gamma(\rho^0)$
Free
(baseline fit)



Are we sensitive to $M(\omega)$ and $\Gamma(\omega)$? Or do they Affect $M(\rho^0)$ and $\Gamma(\rho^0)$ determination ?

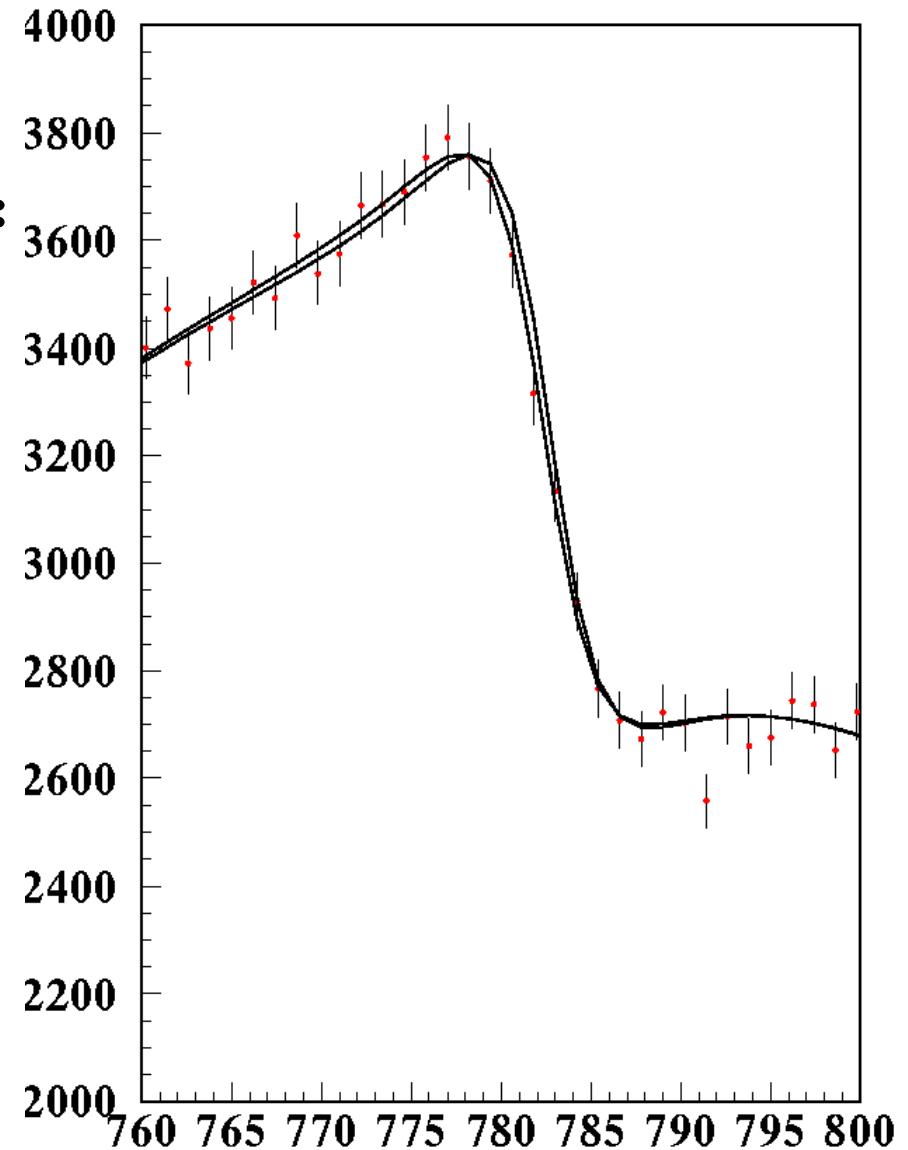
Fit with $M(\omega)$ and $\Gamma(\omega)$ free: ρ^0 parameters do not change: values found:

$M(\omega) = 782.2 \pm 0.6$
(PDG) 782.59 ± 0.11

$\Gamma(\omega) = 8.9 \pm 0.8$
(PDG) 8.49 ± 0.08

Good momentum scale calibration.

No smearing required



3. Three different fits to the same spectrum:

KL = Kaon-loop approach (N.N.Achasov et al)

IM = “no structure” (G.Isidori, L.Maiani)

BP = based on scattering amplitudes
 (M.E.Boglione, M.Pennington)

$$A(\phi \rightarrow S\gamma \rightarrow \pi^+ \pi^- \gamma) = -\frac{esm_\phi^2}{4f_\phi D_\phi(s)(s-m^2)} \{M\}$$

$$M_{KL} = \frac{g_{f\pi\pi} g(m^2) e^{i\delta_m(\theta)}}{D_f(m^2)}$$

$$M_{IM} = (s-m^2) \left[\frac{g_{f\pi\pi} g_{\phi f\gamma}}{D_f(m^2)} + \frac{c_0}{m_\phi^2} + c_1 \frac{m^2 - m_f^2}{m_\phi^4} \right] e^{i\lambda}$$

$$M_{BP} = (m^2 - m_o^2) [(a_1 + b_1 m^2) T(\pi\pi \rightarrow \pi\pi) + (a_2 + b_2 m^2) T(KK \rightarrow \pi\pi)] e^{i\lambda}$$

The fitting function:

$$\frac{d\sigma}{dm} = \left(\frac{d\sigma}{dm} \right)_{ISR} + \left(\frac{d\sigma}{dm} \right)_{FSR} + \left(\frac{d\sigma}{dm} \right)_{\rho\pi} + back(\pi^+\pi^-\pi^0 + \mu^+\mu^-\gamma) \\ + \left(\frac{d\sigma}{dm}(|A|^2) \right)_{Scalar} + \left(\frac{d\sigma}{dm}(A) \right)_{int. Scalar+FSR}$$

Free parameters:

- $a_{\rho\pi}$ (1) for the “background” $m(\rho^0)$ $\Gamma(\rho^0)$ α β
 (2) for the “signal”

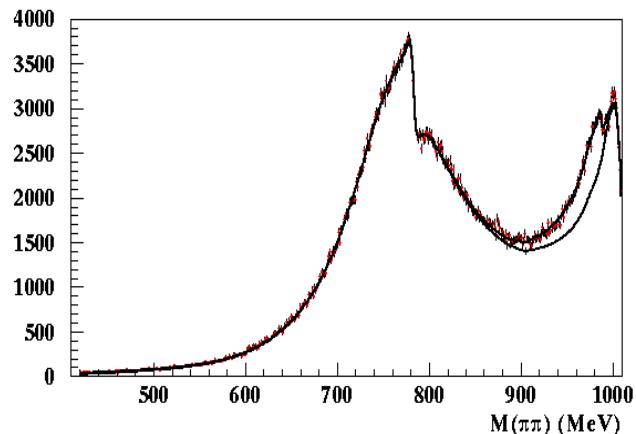
KL (m_f g_{fKK} R)

IM (m_f Γ_f gg c_0 c_1 **fase**)

BP (a_1 b_1 a_2 b_2 s_0 **fase**)

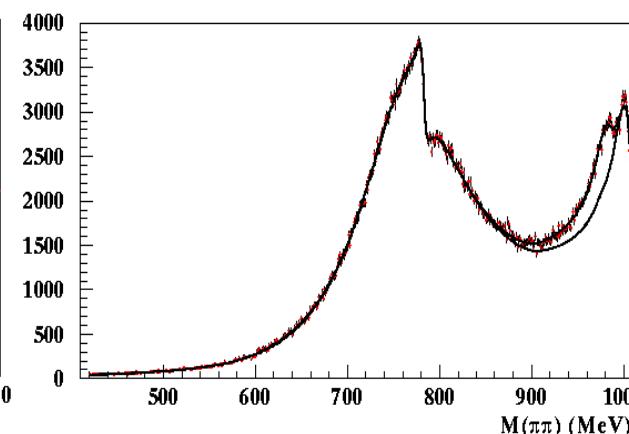
KL fit

$$\chi^2 = 541/481$$
$$P(\chi^2) = 3.0\%$$



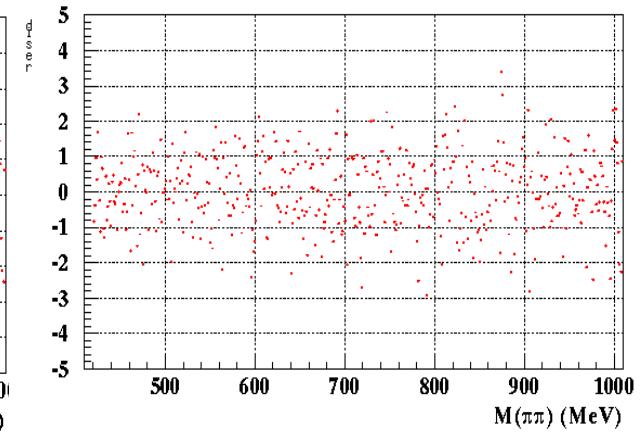
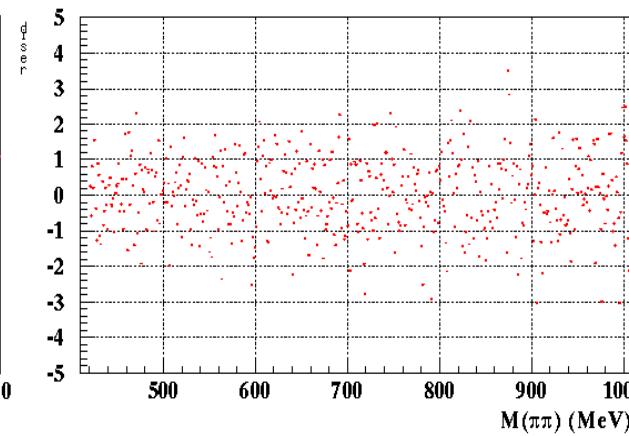
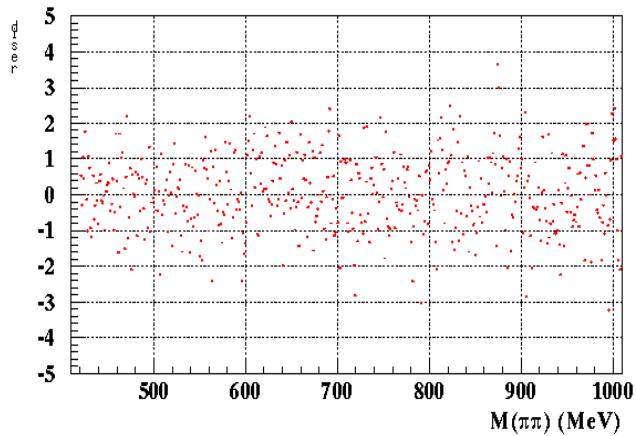
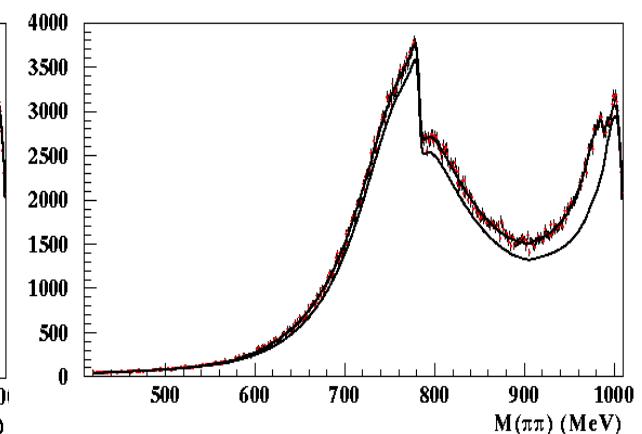
IM fit

$$\chi^2 = 540/478$$
$$P(\chi^2) = 2.6\%$$



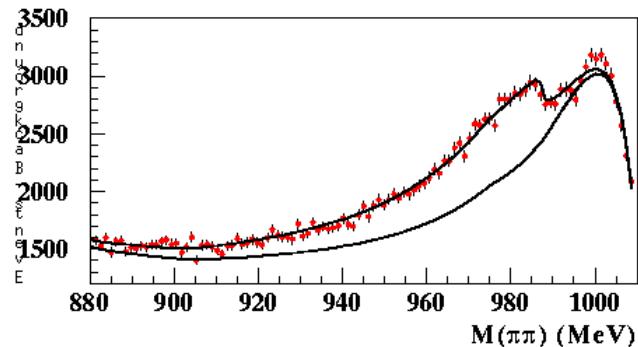
BP fit

$$\chi^2 = 521/478$$
$$P(\chi^2) = 8.4\%$$



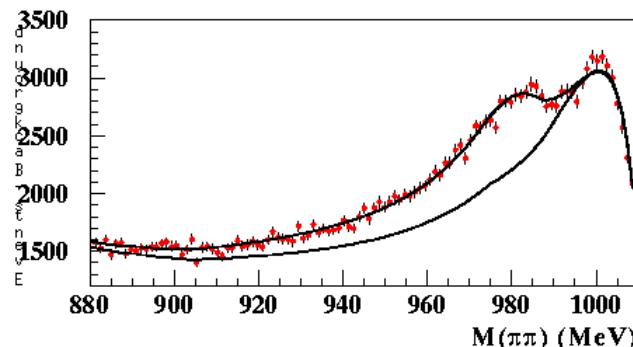
KL fit

$$\chi^2 = 131/100$$



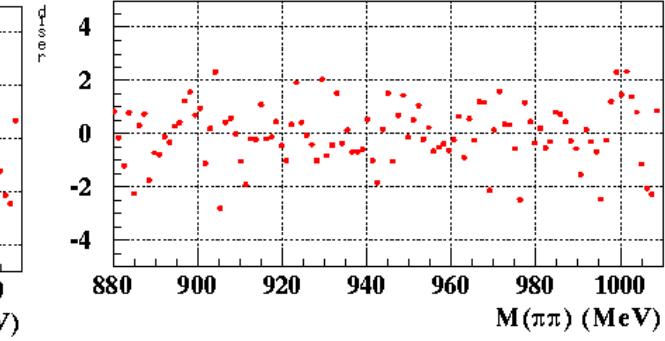
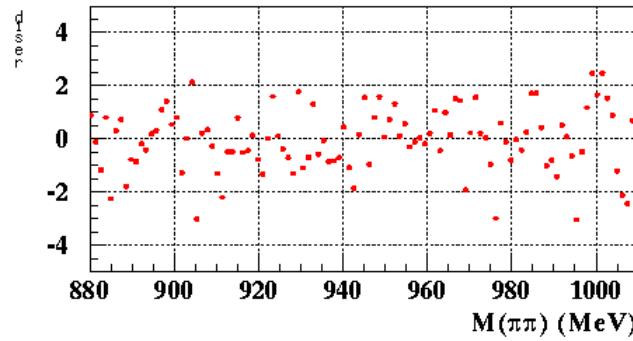
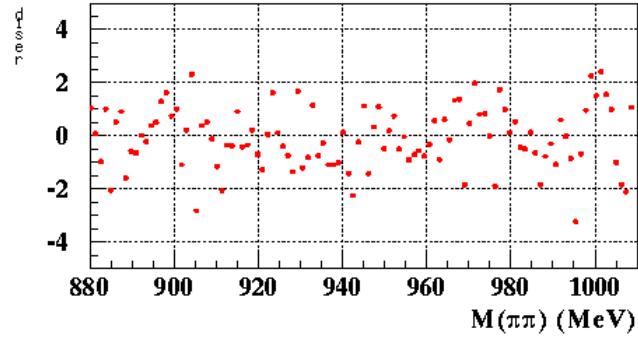
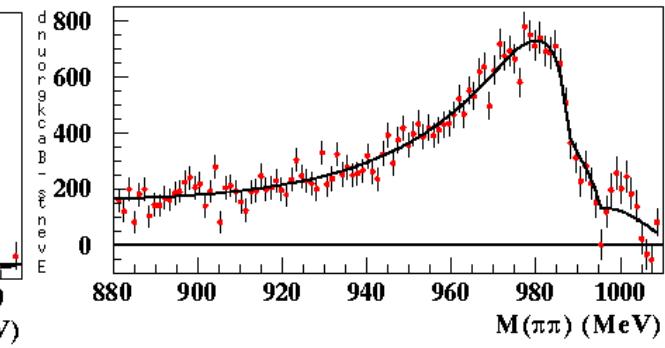
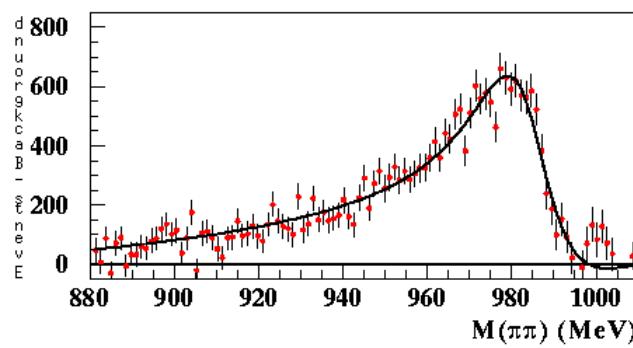
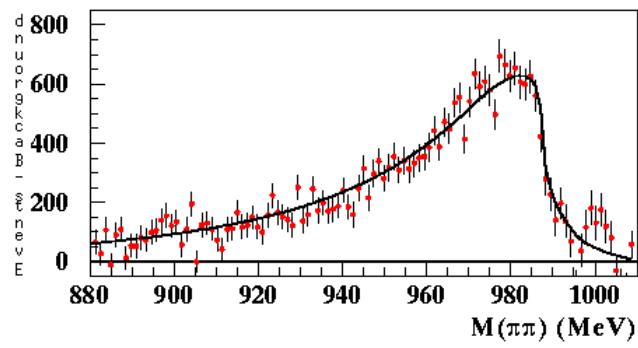
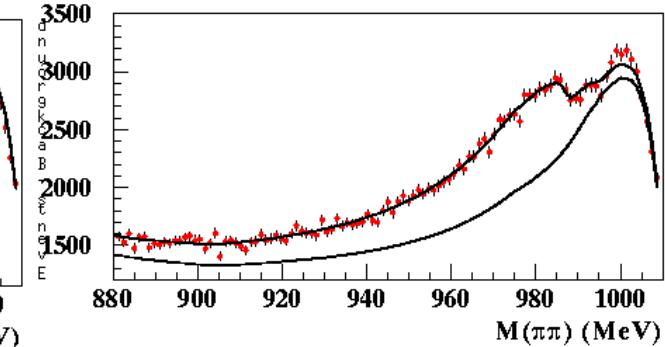
IM fit

$$\chi^2 = 139/100$$



BP fit

$$\chi^2 = 119/100$$



Summary of fit results

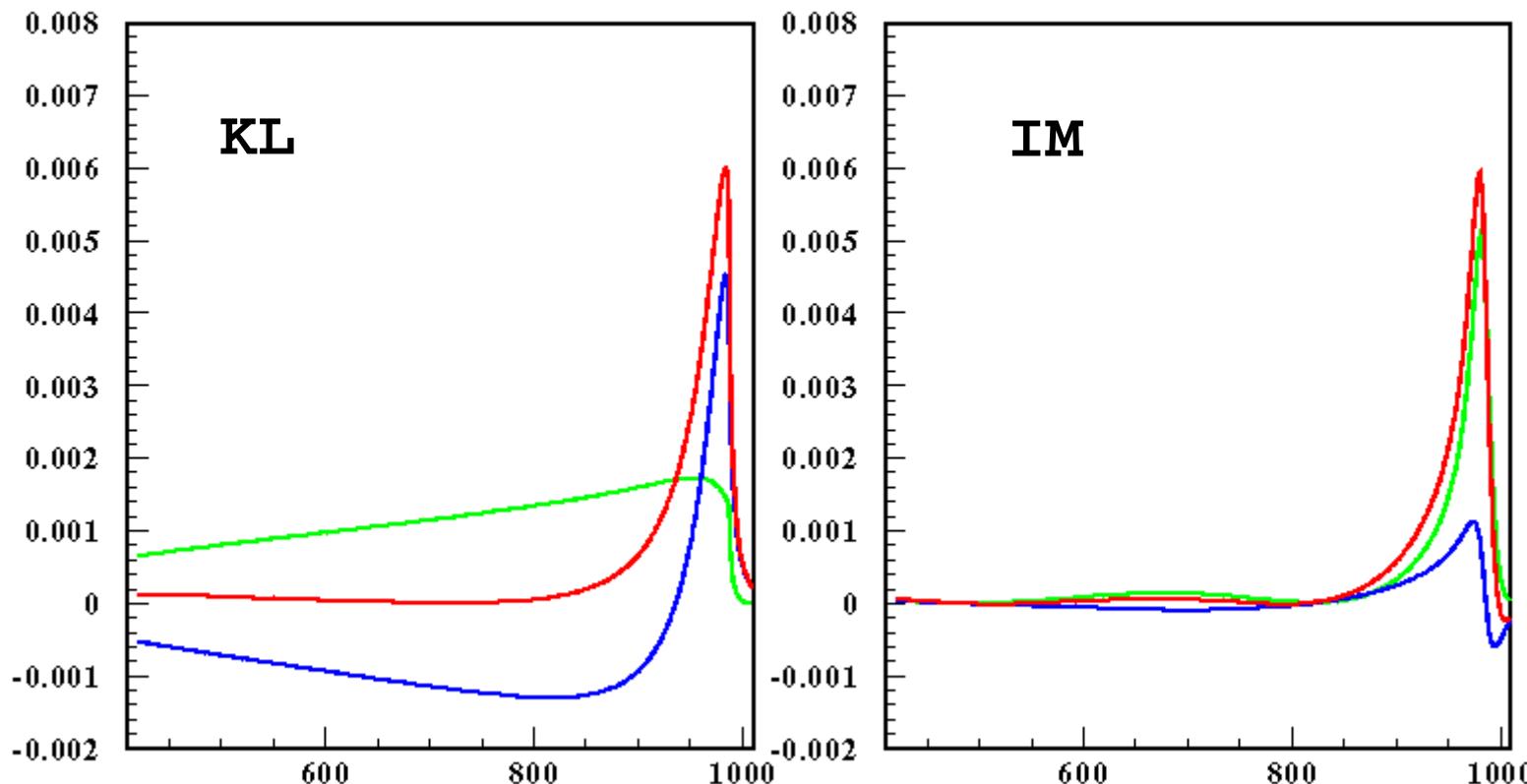
	KL		IM		BP	
χ^2/dof (all)	541 / 481		540 / 478		521 / 478	
χ^2/dof (f0)	131 / 100		139 / 100		119 / 100	
m_f (MeV)	m_f (MeV)	983.7 ± 0.6	m_f (MeV)	984.6 ± 0.5	a_1	-2.57
	$g^2_{f\bar{K}K}/4\pi$ (GeV ²)	3.4 ± 0.6	Γ_f (MeV)	21.3 ± 1.1	b_1	2.56
	R	2.82 ± 0.08	gg	1.58 ± 0.05	a_2	3.73
			C_0	7.8 ± 0.3	b_2	-4.13
			C_1	8.0 ± 0.2	s_0 (GeV ²)	0.21
			fase	0.80 ± 0.32	fase	1.16
$M(\rho^0)$ (MeV)	773.3 ± 0.2		773.7 ± 0.3		772.3 ± 0.1	
$\Gamma(\rho^0)$ (MeV)	144.1 ± 0.3		145.0 ± 0.5		139.9 ± 0.1	
α ($\times 10^{-3}$)	1.68 ± 0.05		1.70 ± 0.05		1.78 ± 0.03	
β ($\times 10^{-3}$)	-122 ± 2		-126 ± 2		-154 ± 1	
$a_{\rho\pi}$	compatibile con 0 e con 1 (atteso)					
BR ($\times 10^{-5}$)	21.4		6.9		22.1	

KL vs IM (1):

red = signal

green = direct

blue = interference

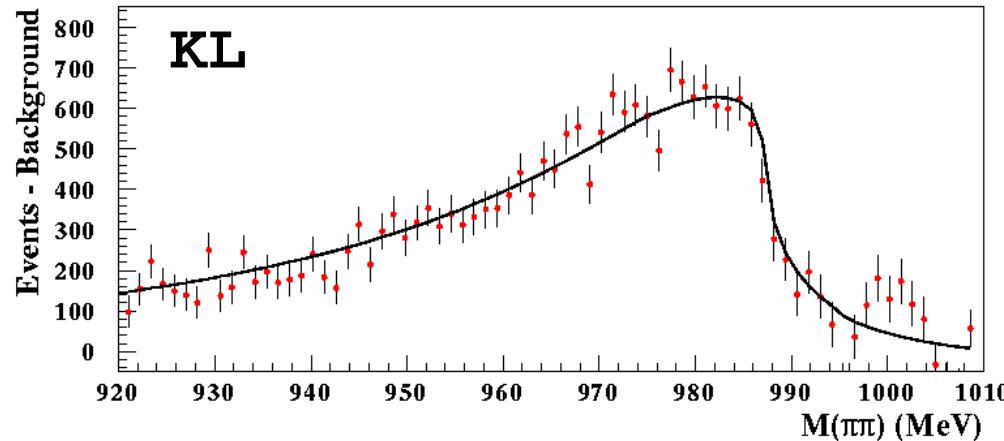


$$\Gamma_f(\text{KL}) \sim 70 \text{ MeV}, \quad \Gamma_f(\text{IM}) \sim 21 \text{ MeV}$$

KL vs IM (2):

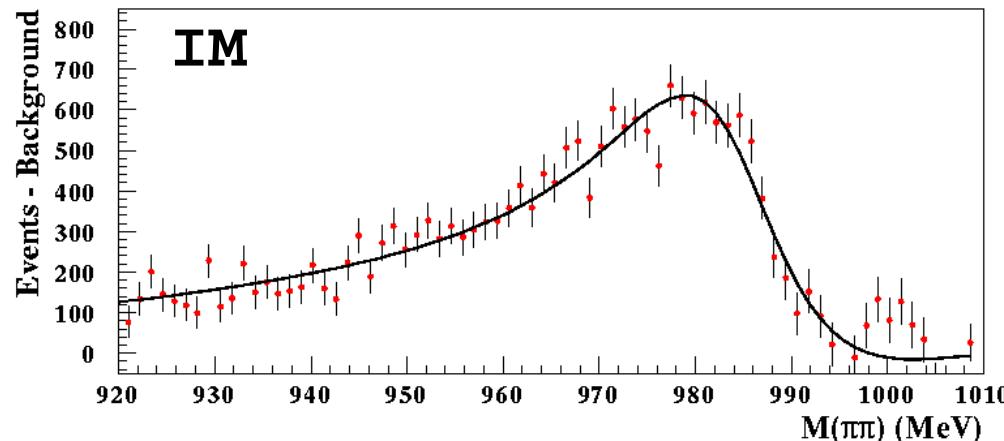
**different “rise” of the signal:
it is due to the different propagator**

$$D_f(m^2) = m^2 - m^2_f + \Re \Pi_f(m^2_f) - \Pi_f(m^2)$$



$$\Pi_f(m^2) = \sum_{ab} \Pi_{ab}(g_{fab}, m^2)$$

**Flatte’- like
 g_{fab} are the parameters**



$$D_f(m^2) = m^2 - m^2_f + im_f \Gamma_f$$

KL vs IM (3):
couplings:

KL:

$$\begin{aligned} g_{f\text{KK}}^2 / 4\pi &= 3.4 \text{ GeV}^2 & \rightarrow g_{f\text{KK}} &= 6.4 \text{ GeV} \\ g_{f\pi\pi}^2 / 4\pi &= 1.2 \text{ GeV}^2 & \rightarrow g_{f\pi\pi} &= 3.9 \text{ GeV} \end{aligned}$$

IM:

$$\begin{aligned} \Gamma_f &= 21 \text{ MeV} & \rightarrow g_{f\pi\pi} &= 1.0 \text{ GeV} (*) \\ g_{\phi f\gamma} g_{f\pi\pi} &= 1.6 & \rightarrow g_{\phi f\gamma} &= 1.6 \text{ GeV}^{-1} \end{aligned}$$

(*) assuming $f \rightarrow \pi^+ \pi^-$ the only contribution to Γ

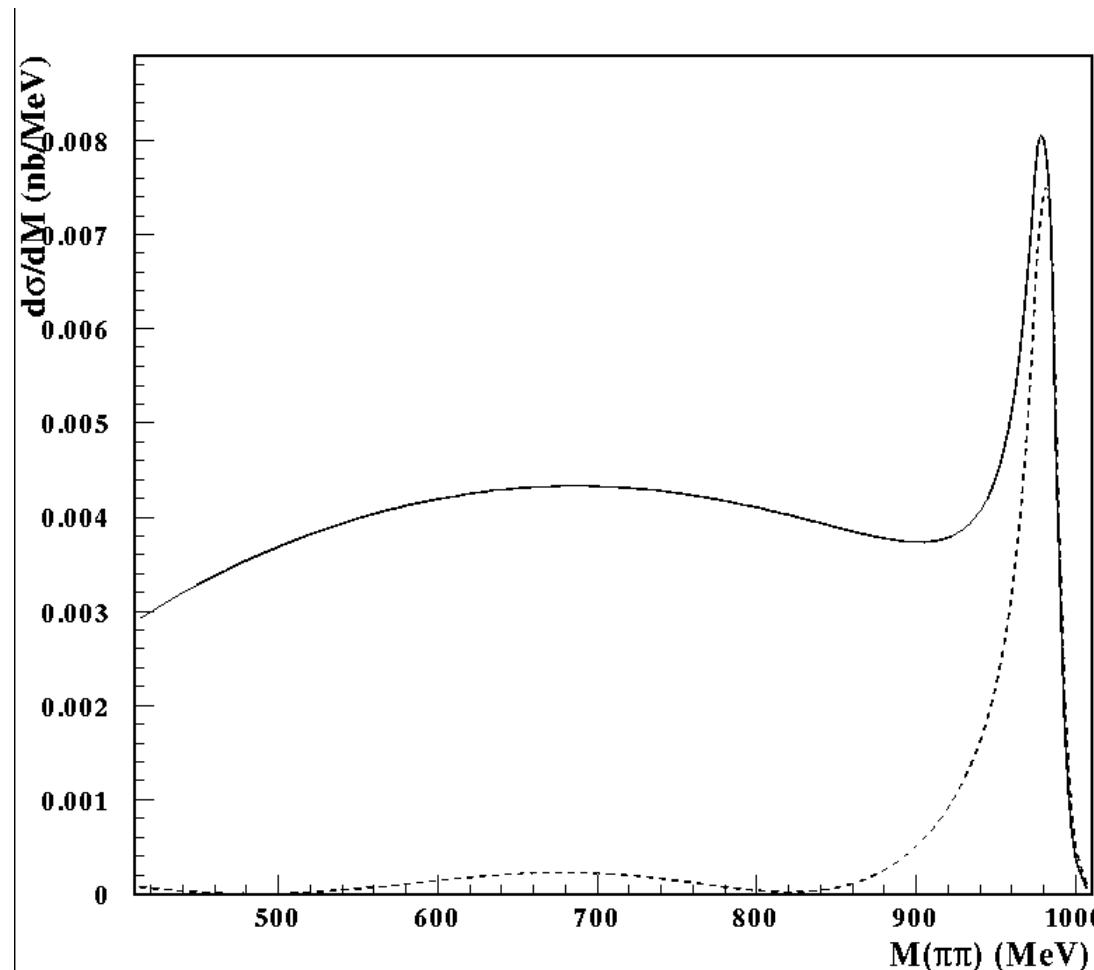
$$\Gamma(f_0 \rightarrow \pi^+ \pi^-) = \frac{g_{f\pi\pi}^2 p_{12}(m_f)}{8\pi m_f^2}$$

IM :

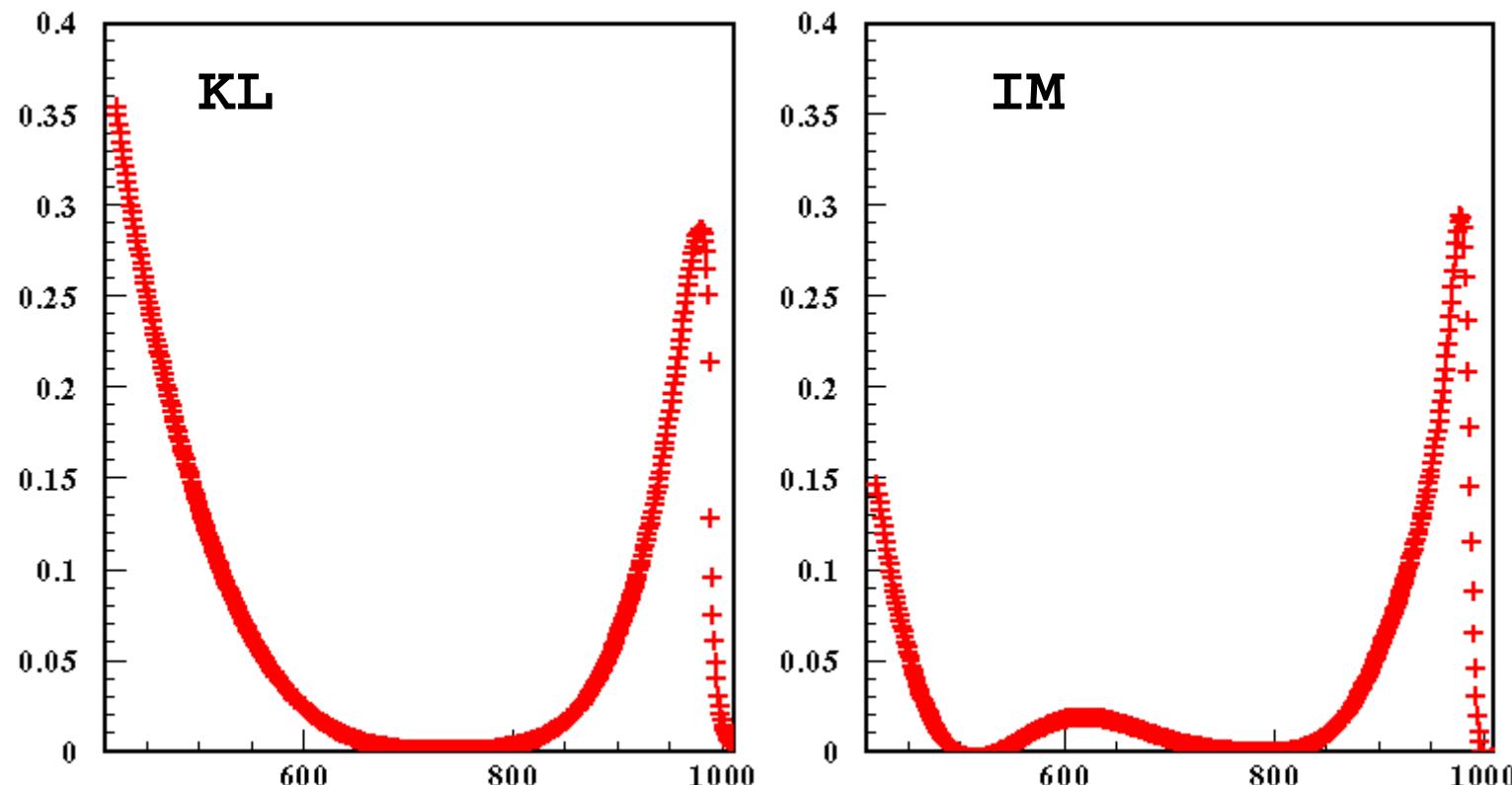
Effect of the c_0 and c_1 "background":

solid: $c_0 = 0$, $c_1 = 0$

dashed: c_0 and c_1 fitted

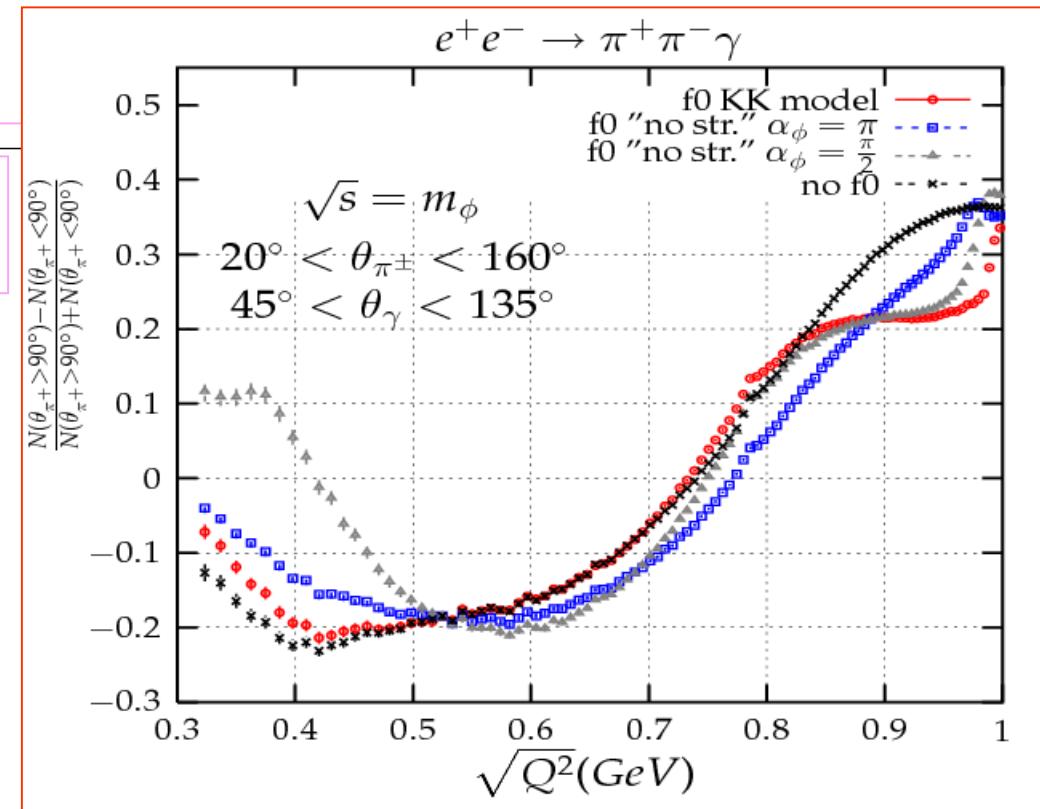
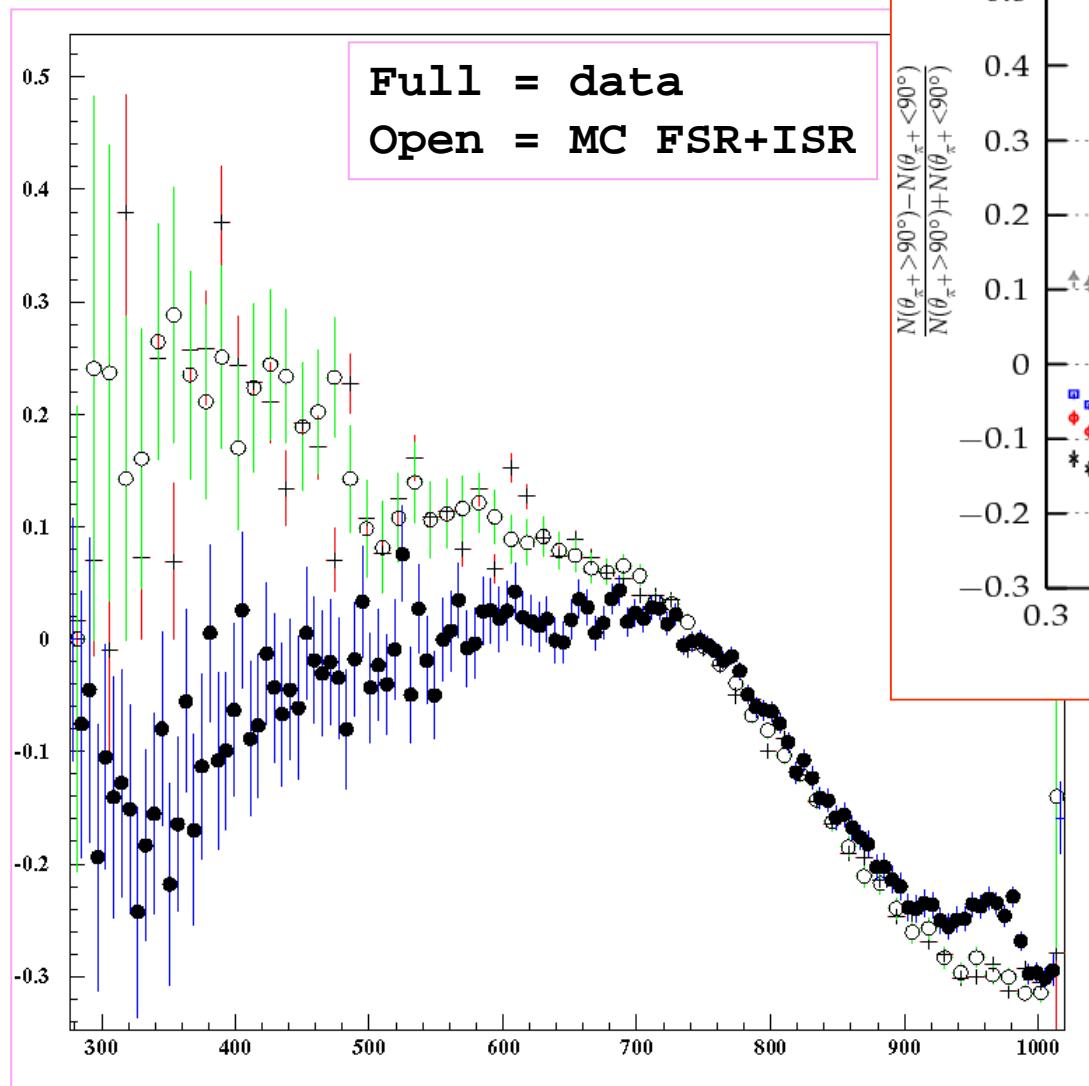


Size of the “scalar” signal respect to ISR:
peak at f_0 mass (size ~ 30%)
rise at low masses



**Any low mass analysis requires knowledge of
the scalar contributions**

4. Charge asymmetry: in hep-ph/0412239 first attempts to predict the $M(\pi\pi)$ behaviour.



Conclusions

- Some more checks on possible backgrounds ($\pi^+\pi^-\pi^0$ and $\pi^+\pi^-$) are needed
- The fit is OK (improve is possible for BP)
- The charge asymmetry is an interesting issue
- A message for hadronic cross-section measurement: take care of scalars even in the low mass region.
- Define a strategy for publications.