

Measurement of the pseudoscalar mixing angle and η' gluonium content extraction.

Blessing meeting
23/04/2009

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I.N.F.N sezione di Roma Tre

Outline

- Model description;
- Refit of all relevant measurements;
- Refit using PDG-2008 and KLOE measurement of $\omega \rightarrow \pi^0 \gamma$;
- Refit using lattice evaluation of f_K/f_π
- The paper

η, η' : mixing and gluonium

The η, η' mesons wave function can be decomposed in the quark mixing base as in the following (J. L. Rosner, Phys. Rev. D 27 (1983) 1101.).

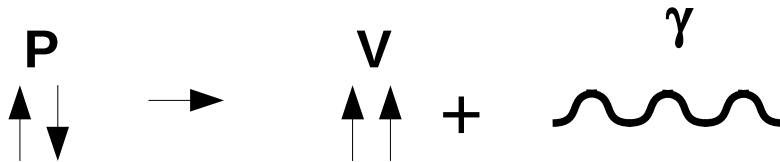
$$|\eta'\rangle = X_{\eta'} |q\bar{q}\rangle + Y_{\eta'} |s\bar{s}\rangle + Z_{\eta'} |G\rangle \quad |\eta\rangle = \cos\varphi_P |q\bar{q}\rangle - \sin\varphi_P |s\bar{s}\rangle \quad |q\bar{q}\rangle = \frac{|u\bar{u}\rangle + |d\bar{d}\rangle}{\sqrt{2}}$$

$$X_{\eta'} = \sin\varphi_P \cos\varphi_G$$

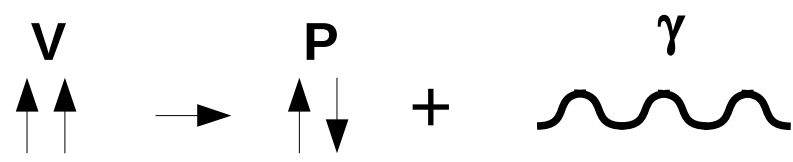
$$Y_{\eta'} = \cos\varphi_P \cos\varphi_G$$

$$Z_{\eta'} = \sin\varphi_G$$

The $\phi \rightarrow \eta, \eta' \gamma$ transition is modelled according a spin flip transition



$$\Gamma(P \rightarrow V \gamma) = \frac{g^2}{4\pi} |p_y|^3$$



$$\Gamma(V \rightarrow P \gamma) = \frac{1}{3} \frac{g^2}{4\pi} |p_y|^3$$

Only quarks participate to the electromagnetic transition, gluonium is spectator.
It appears in the η' decay amplitudes only through the normalisation to 1 ($Y_{\eta'} \sim \cos\varphi_G$)

Magnetic dipole transition

Decay width:

$$\Gamma(V \rightarrow P\gamma) = \frac{2}{3}\alpha\omega^3 \left(\frac{E_P}{m_V}\right) \sum \left| \left\langle V \left| \frac{\mu_q e_q \sigma_q}{e} \right| P \right\rangle \right|^2$$

Quark charge

Pauli matrices

example: Matrix element for $\rho \rightarrow \eta\gamma$ decay

$$|\rho\rangle = \frac{|u\bar{u}\rangle - |d\bar{d}\rangle}{\sqrt{2}}$$

$$\left\langle \rho \left| \frac{\mu_q e_q \sigma_q}{e} \right| \eta \right\rangle = \mu \cos(\varphi_P) \left(\frac{2}{3} \langle u\bar{u}_\rho | u\bar{u}_\eta \rangle + \frac{1}{3} \langle d\bar{d}_\rho | d\bar{d}_\eta \rangle \right) = \mu \cos(\varphi_P) \langle q\bar{q}_\rho | q\bar{q}_\eta \rangle$$

e/m_q (effective quark mass)

wave function overlapping

$$C_q = \langle \eta_q | \omega_q \rangle = \langle \eta_q | \rho \rangle \quad C_s = \langle \eta_s | \phi_s \rangle \quad C_\pi = \langle \pi | \omega_q \rangle = \langle \pi | \rho \rangle$$

In the formulas only the ratios appear: $Z_{NS} = C_q/C_\pi$ $Z_S = C_s/C_\pi$

QCD effects reside in mixing parameters, overlapping parameters and effective quark masses.

V P γ and P $\gamma\gamma$ transitions

KLOE [Phys. Lett. B648 (2007) 267] has fitted:

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos^2 \phi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}$$

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[z_q X_{\eta'} + 2 \frac{m_s}{\bar{m}} z_s \cdot \tan \phi_V \cdot Y_{\eta'} \right]^2$$

together with the measured branching ratio:

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3}$$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\bar{m}} \frac{z_q}{z_s} \cdot \frac{\tan \phi_V}{\sin 2 \phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

and the ratio: $\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_\pi} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$ **E. Kou, Phys. Rev. D 63 (2001) 54027**

V P γ and P $\gamma\gamma$ transitions

KLOE [Phys. Lett. B648 (2007) 267] has fitted:

Were taken from a global fit without gluonium:

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{z_q^2}{\cos \phi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_\rho^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 X_{\eta'}$$

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_\omega^2 m_\omega}{m_\omega^2 - m_\pi^2 m_{\eta'}} \right)^3 \left[z_q^2 X_{\eta'} + 2 \frac{\bar{m}_s}{\bar{m}} z_s \tan \phi_V X_{\eta'} \right]^2$$

A. Bramon, R. Escribano,
M.D. Scadron
Phys. Lett. B503 (2001) 271

together with the measured branching ratio:

$$R_\phi = (4.77 \pm 0.09 \pm 0.19) \times 10^{-3}$$

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Escribano couplings

$$g_{\rho^0\pi^0\gamma} = g_{\rho^+\pi^+\gamma} = \frac{1}{3}g , \quad g_{\omega\pi\gamma} = g \cos \phi_V , \quad g_{\phi\pi\gamma} = g \sin \phi_V ,$$

$$g_{K^{*0}K^0\gamma} = -\frac{1}{3}g z_K \left(1 + \frac{\bar{m}}{m_s}\right) , \quad g_{K^{*+}K^+\gamma} = \frac{1}{3}g z_K \left(2 - \frac{\bar{m}}{m_s}\right) ,$$

$$g_{\rho\eta\gamma} = g z_q X_\eta , \quad g_{\rho\eta'\gamma} = g z_q X_{\eta'}$$

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \cos \phi_V + 2\frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right) ,$$

$$g_{\omega\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \cos \phi_V + 2\frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right) ,$$

All couplings are proportional to g

$$g_{\phi\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \sin \phi_V - 2\frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right) ,$$

$$g_{\phi\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \sin \phi_V - 2\frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right) ,$$

Fit redone leaving free all parameters

- 1) Leave the z's parameter free;
- 2) Add more constraints (needed to perform the fit with larger number of parameters);
- 3) Check the contribution from $\eta' \rightarrow \gamma\gamma$ / $\pi^0 \rightarrow \gamma\gamma$

Deacy width ratio evaluated from Escribano couplings.

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[Z_q \cos(\phi_p) - 2 \frac{\bar{m}}{m_s} Z_s \tan(\phi_v) \sin(\phi_p) \right]^2 \left(\frac{m_\omega^2 - m_\eta^2}{m_\omega^2 - m_{\pi^0}^2} \right)^3$$

$$\frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = Z_q^2 \frac{\cos^2(\phi_p)}{\cos^2(\phi_v)} \left(\frac{m_\rho^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\rho} \right)^3$$

$$\frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[Z_q \tan(\phi_v) \cos(\phi_p) + 2 \frac{\bar{m}}{m_s} Z_s \sin(\phi_p) \right]^2 \left(\frac{m_\phi^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\phi} \right)^3$$

$$\frac{\Gamma(\phi \rightarrow \pi^0 \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \tan^2 \phi_v \cdot \left(\frac{m_\phi^2 - m_{\pi^0}^2}{m_\omega^2 - m_{\pi^0}^2} \cdot \frac{m_\omega}{m_\phi} \right)^3, \quad \frac{\Gamma(K^{*+} \rightarrow K^+ \gamma)}{\Gamma(K^{*0} \rightarrow K^0 \gamma)} = \left(\frac{2 \frac{m_s}{\bar{m}} - 1}{1 + \frac{m_s}{\bar{m}}} \right)^2 \cdot \left(\frac{m_{K^{*+}}^2 - m_{K^{*0}}^2}{m_{K^{*0}}^2 - m_{K^0}^2} \cdot \frac{m_{K^{*0}}}{m_{K^{*+}}} \right)^3$$

Fit procedure.

C. Di Donato,
Kloe memo n. 327

The χ^2 is defined as follows:

$$\chi^2 = \sum_{i,j=1,3} (y_i - y_i^{th}) \times V_{ij}^{-1} (y_j - y_j^{th})$$

V_{ij} is the error matrix which is a function of theoretical uncertainties, as well as the experimental

$$V_{ij} = [B_{ij} + (A_{ik} \times C_{kl} \times A_{lj}^T)]$$

Experimental
covariance matrix

Theoretical parameters
covariance matrix

B_{ij} Full covariance matrix
(correlation comes
from the constrained
fit to η' Br)

$$; A_{ik} = \begin{pmatrix} \frac{\partial y_1^{th}}{\partial f_s} & \frac{\partial y_1^{th}}{\partial f_q} & \frac{\partial y_1^{th}}{\partial C_{NS}} & \frac{\partial y_1^{th}}{\partial C_S} & \frac{\partial y_1^{th}}{\partial \frac{m_s}{\bar{m}}} \\ \frac{\partial y_2^{th}}{\partial f_s} & \frac{\partial y_2^{th}}{\partial f_q} & \frac{\partial y_2^{th}}{\partial C_{NS}} & \frac{\partial y_2^{th}}{\partial C_S} & \frac{\partial y_2^{th}}{\partial \frac{m_s}{\bar{m}}} \\ \frac{\partial y_3^{th}}{\partial f_s} & \frac{\partial y_3^{th}}{\partial f_q} & \frac{\partial y_3^{th}}{\partial C_{NS}} & \frac{\partial y_3^{th}}{\partial C_S} & \frac{\partial y_3^{th}}{\partial \frac{m_s}{\bar{m}}} \end{pmatrix}$$

$$C_{kl} = \begin{pmatrix} \sigma_{f_q}^2 & 0 \\ 0 & \sigma_{f_s}^2 \end{pmatrix}$$

Re-evaluated at
each minimization
step

The experimental covariance matrix B contains correlation among common used quantities in the fitted relations:

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} \longrightarrow \text{Introduces a correlation in the fitted quantities}$$

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{Br(\eta' \rightarrow \gamma \gamma) \Gamma_{\eta'}}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} \quad \frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{Br(\eta' \rightarrow \rho \gamma) \Gamma_{\eta'}}{\Gamma(\omega \rightarrow \pi^0 \gamma)}$$

x_2	-34					
x_3	-78	-29				
x_4	-35	-24	32			
x_5	-26	-12	26	8		
x_6	-28	-11	35	11	9	
Γ	32	-2	-24	-5	-88	-8
	x_1	x_2	x_3	x_4	x_5	x_6

Br and Γ strongly correlated
(above all $\Gamma(\eta' \rightarrow \gamma \gamma)$)

the Γ is measured using:

$$e^+e^- \rightarrow \eta' e^+e^-$$

An independent measurement of the η' total width is welcome.

	Mode	Rate (MeV)	Scale factor
Γ_1	$\pi^+ \pi^- \eta$	0.090 $\pm$ 0.008	1.2
Γ_2	$\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$)	0.060 $\pm$ 0.005	1.2
Γ_3	$\pi^0 \pi^0 \eta$	0.042 $\pm$ 0.004	1.6
Γ_4	$\omega \gamma$	0.0062 $\pm$ 0.0008	1.2
Γ_5	$\gamma \gamma$	0.00430 $\pm$ 0.00015	1.1
Γ_6	$3\pi^0$	(3.2 $\pm$ 0.6) $\times 10^{-4}$	1.1

Fit results without $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$

$$\Gamma(P \rightarrow V \gamma) = \frac{g^2}{4\pi} |p_\gamma|^3$$

very similar results

Fit redone a la Escribano

(using couplings and not taking into account correlations)

	Fit with width ratios	Escribano <i>et al.</i> , JHEP 0705:006 (2007)	Fit with couplings
$\chi^2/n.d.f(Prob)$	1.8/2 (41 %)	4.2/4 (38 %)	4.7/4 (32 %)
Z_G^2	0.03 ± 0.06	0.04 ± 0.09	0.04 ± 0.07
φ_G	$(10 \pm 10)^\circ$	$(12 \pm 13)^\circ$	$(11 \pm 11)^\circ$
φ_P	$(41.6 \pm 0.8)^\circ$	$(41.4 \pm 1.3)^\circ$	$(41.5 \pm 1.1)^\circ$
Z_{NS}	0.85 ± 0.03	0.86 ± 0.03	0.86 ± 0.03
Z_S	0.78 ± 0.05	0.79 ± 0.05	0.78 ± 0.05
φ_V	$(3.16 \pm 0.10)^\circ$	$(3.2 \pm 0.1)^\circ$	$(3.18 \pm 0.10)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07	1.24 ± 0.07
Z_K		0.89 ± 0.03	0.89 ± 0.03
g		0.72 ± 0.01	0.72 ± 0.01

disappear
in the ratio

Table 3: Comparison among the fit results without the $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$ measurement and the Escribano *et al.* results.

Adding the $\eta' \rightarrow \gamma\gamma$ / $\pi^0 \rightarrow \gamma\gamma$ constraint

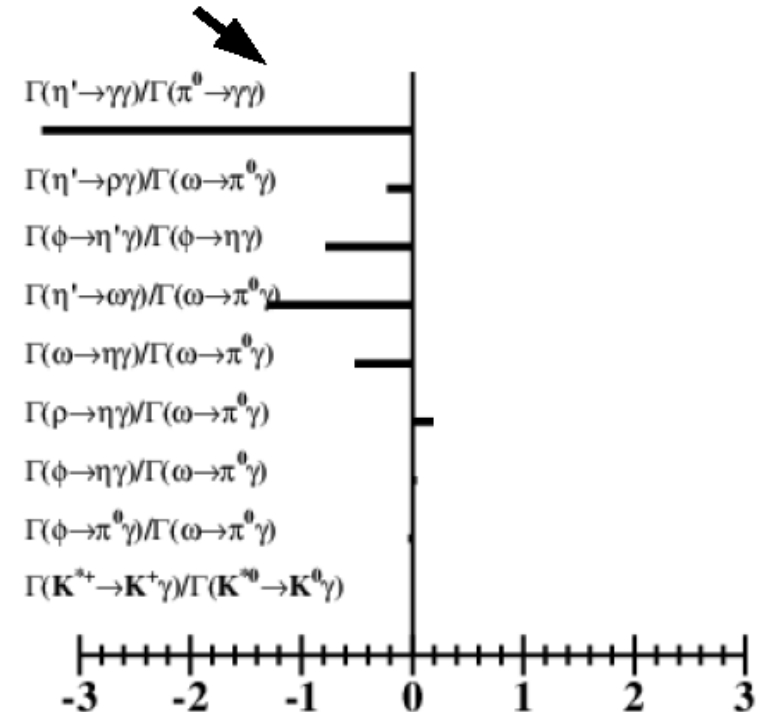
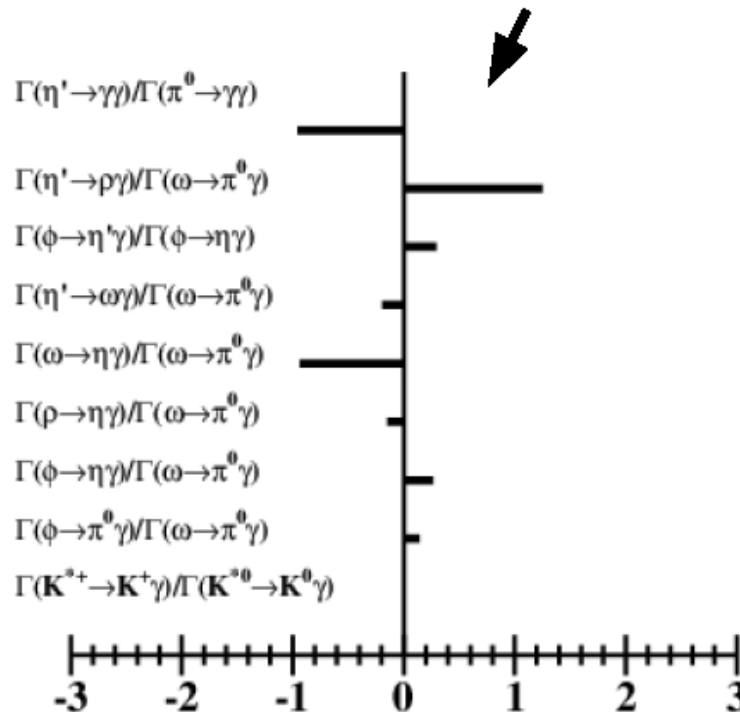
	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	5/3 (17.5 %)	13/4 (1.1 %)
Z_G^2	0.105 ± 0.037	0 fixed
φ_P	$(40.7 \pm 0.7)^\circ$	$(41.6 \pm 0.5)^\circ$
Z_{NS}	0.866 ± 0.025	0.863 ± 0.024
Z_S	0.79 ± 0.05	0.78 ± 0.05
φ_V	$(3.15 \pm 0.10)^\circ$	$(3.17 \pm 0.10)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07

KLOE
(Phys. Lett. B648 (2007) 267)

$$\phi_P = (39.7 \pm 0.7_{\text{tot}})^\circ$$

$$|\phi_G| = (22 \pm 3)^\circ$$

$$\sin^2 \phi_G = Z^2 = 0.14 \pm 0.04$$



Fit to the couplings with $\eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma$

$P \rightarrow \gamma\gamma$ measurement included as:

$$\frac{\Gamma(\eta' \rightarrow \gamma\gamma)}{\Gamma(\pi^0 \rightarrow \gamma\gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_{\pi}} \right)^3 \left(5 \sin(\phi_P) \cos(\phi_G) + \sqrt{2} \frac{f_q}{f_s} \cos(\phi_P) \cos(\phi_G) \right)^2$$

without glue

with glue

$$\chi^2/\text{ndf} = 13/5 \text{ (2.3\%)} \quad \chi^2/\text{ndf} = 7.2/4$$

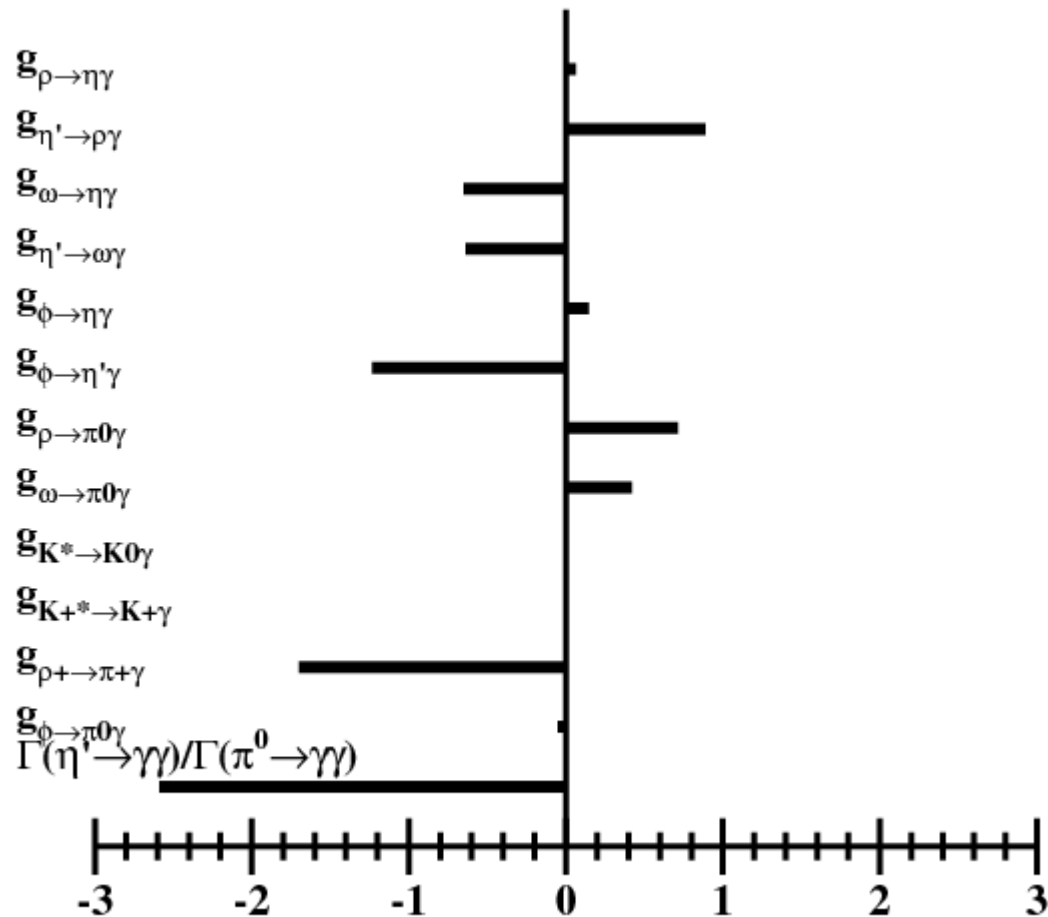
ϕ_G	fixed at 0	$(20 \pm 4)^\circ$
ϕ_P	$(40.1 \pm 0.9)^\circ$	$(41.2 \pm 1.1)^\circ$
Z_q	0.85 ± 0.024	0.88 ± 0.03
Z_s	0.80 ± 0.05	0.79 ± 0.05
ϕ_V	$(3.2 \pm 0.1)^\circ$	$(3.18 \pm 0.10)^\circ$
$\frac{m_s}{\bar{m}}$	1.24 ± 0.07	1.24 ± 0.07
Z_K	0.89 ± 0.03	0.89 ± 0.03
g	0.72 ± 0.01	0.719 ± 0.010

The gluonium appears also in the fit with couplings.

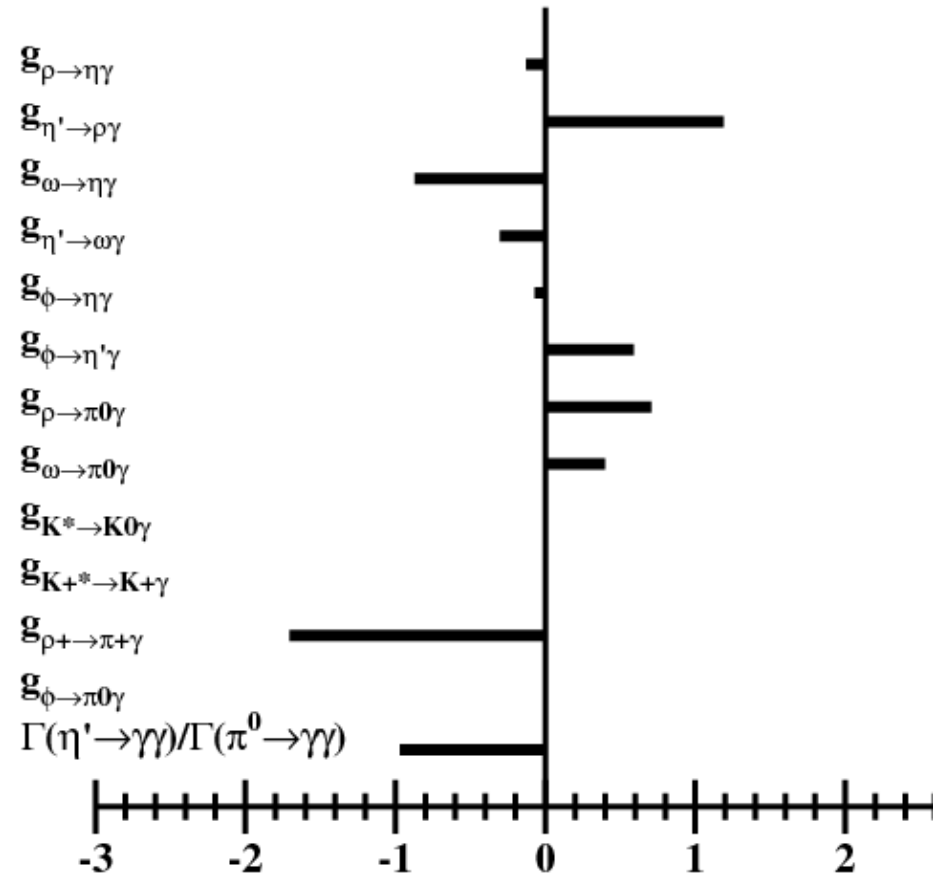
$$Z_{\eta'}^2 = 0.11 \pm 0.05$$

Pulls comparison

without glue



with glue



Update using PDG2008 results

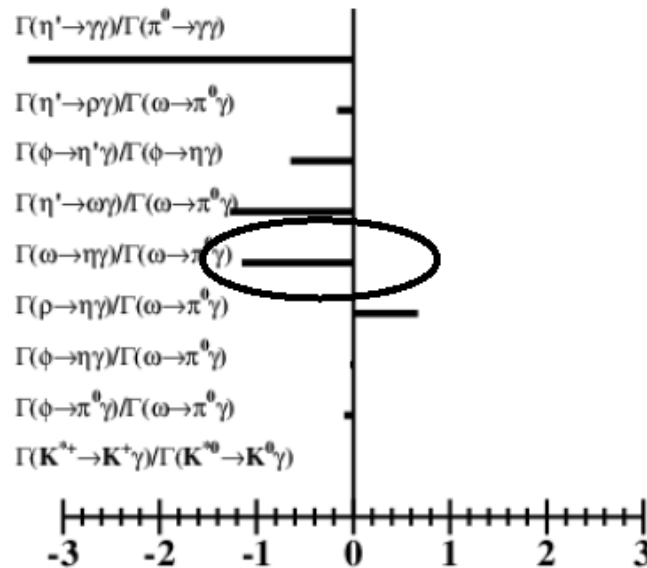
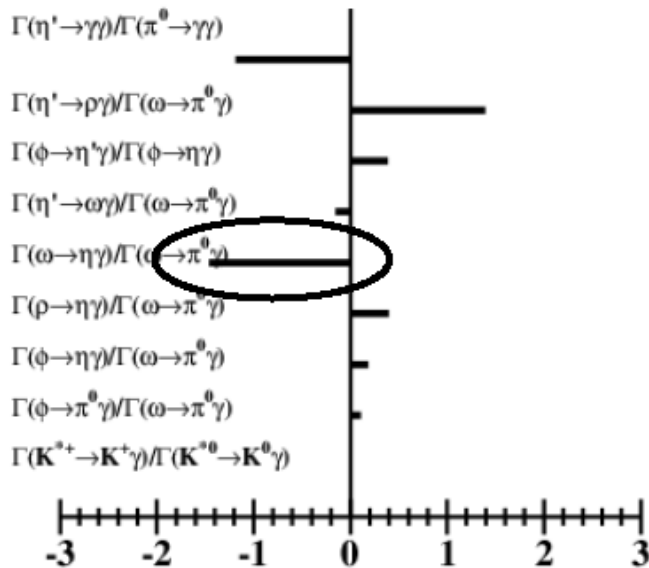
	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	7.9/3 (5 %)	15/4 (5×10^{-3})
Z_G^2	0.097 ± 0.037	0 fixed
φ_P	$(41.0 \pm 0.7)^\circ$	$(41.7 \pm 0.5)^\circ$
Z_{NS}	0.86 ± 0.02	0.858 ± 0.021
Z_S	0.79 ± 0.05	0.78 ± 0.05
φ_V	$(3.17 \pm 0.09)^\circ$	$(3.19 \pm 0.09)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07

PDG08

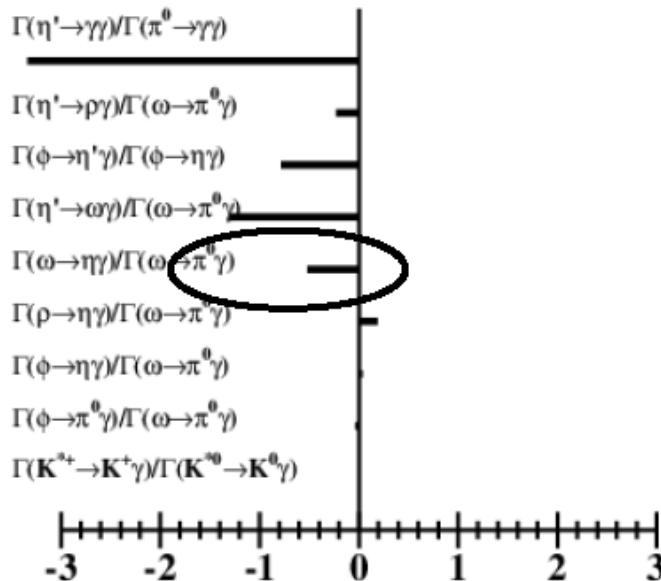
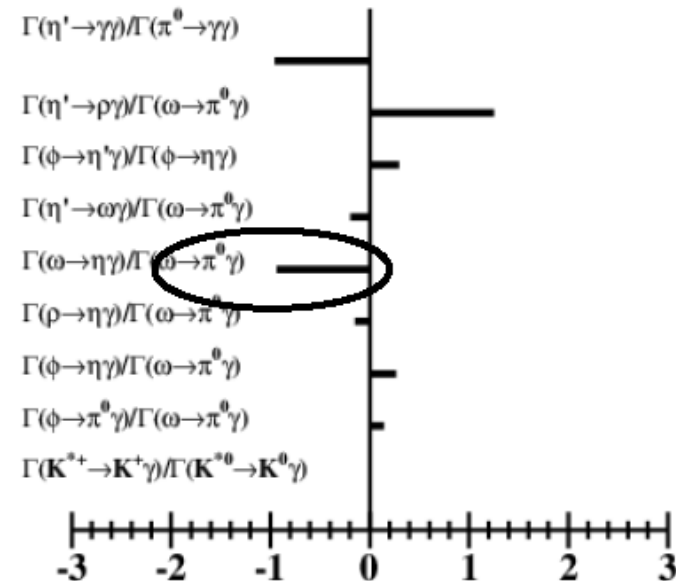
The same gluonium content but unsatisfying fit quality.

	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	5/3 (17.5 %)	13/4 (1.1 %)
Z_G^2	0.105 ± 0.037	0 fixed
φ_P	$(40.7 \pm 0.7)^\circ$	$(41.6 \pm 0.5)^\circ$
Z_{NS}	0.866 ± 0.025	0.863 ± 0.024
Z_S	0.79 ± 0.05	0.78 ± 0.05
φ_V	$(3.15 \pm 0.10)^\circ$	$(3.17 \pm 0.10)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07

PDG06



$\omega \rightarrow \eta \gamma$ pull has increased in both gluonium hypothesis

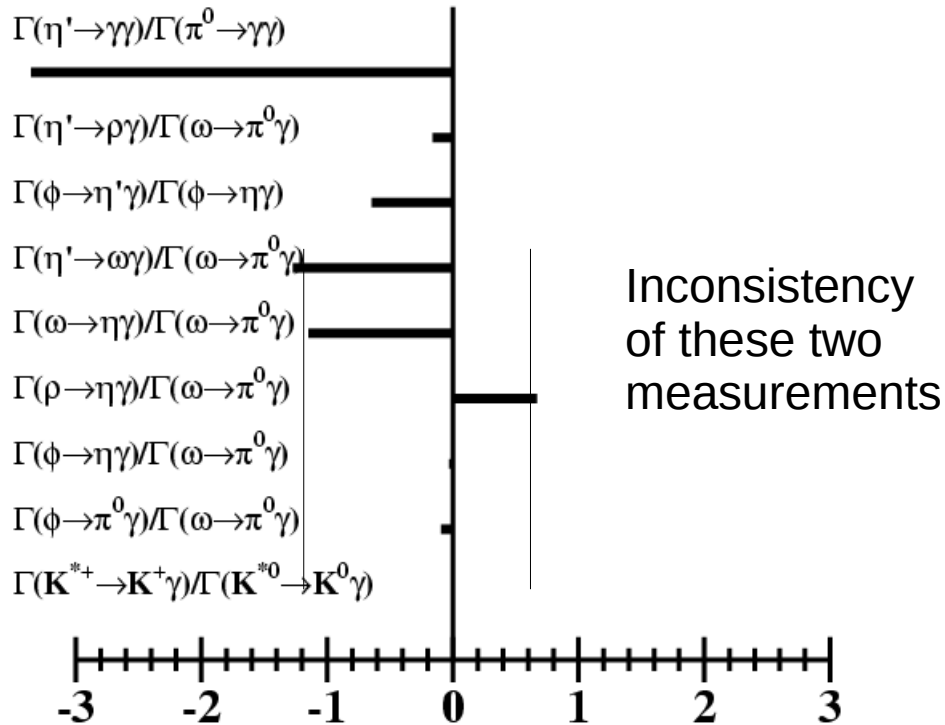


Check if the $\eta' \rightarrow \gamma\gamma$ / $\pi^0 \rightarrow \gamma\gamma$ introduces any distortion

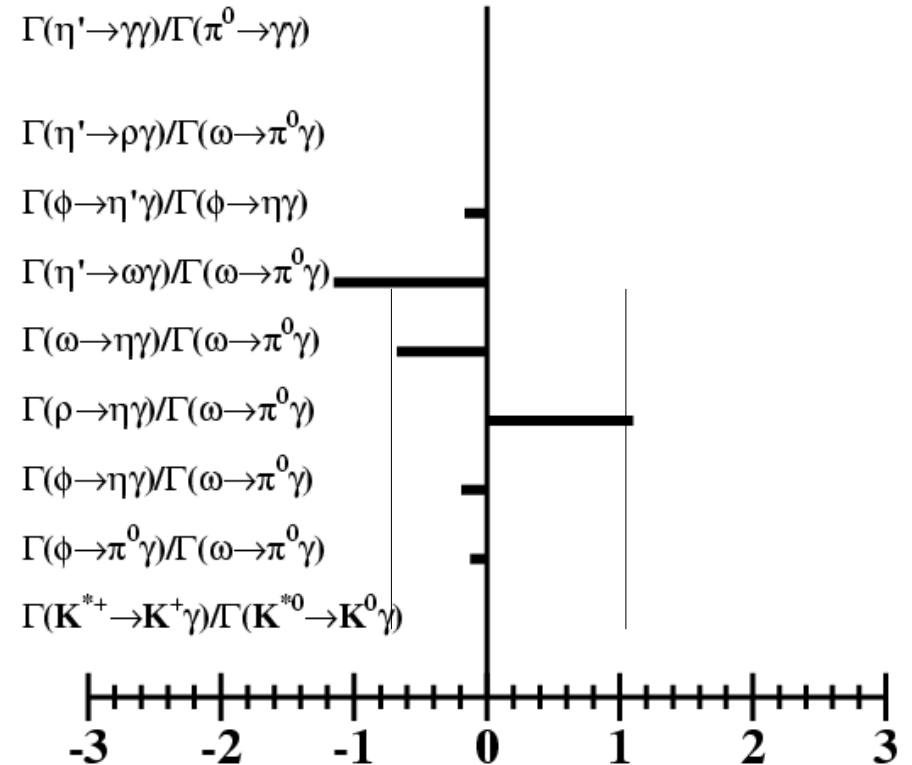
$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{9} \left[Z_q \cos(\phi_p) - 2 \frac{\bar{m}}{m_s} Z_s \tan(\phi_V) \sin(\phi_p) \right]^2 \left(\frac{m_\omega^2 - m_\eta^2}{m_\omega^2 - m_{\pi^0}^2} \right)^3$$

$$\frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = Z_q^2 \frac{\cos^2(\phi_p)}{\cos^2(\phi_V)} \left(\frac{m_\rho^2 - m_\eta^2}{m_\omega^2 - m_\pi^2} \frac{m_\omega}{m_\rho} \right)^3$$

with $\eta' \rightarrow \gamma\gamma$ / $\pi^0 \rightarrow \gamma\gamma$



without $\eta' \rightarrow \gamma\gamma$ / $\pi^0 \rightarrow \gamma\gamma$



The $\omega \rightarrow \eta\gamma$ partial width changed from

$$(4.9 \pm 0.5) \times 10^{-4} \text{ to } (4.6 \pm 0.4) \times 10^{-4}$$

This value is determined by the global PDG fit, and it is mainly determined by:

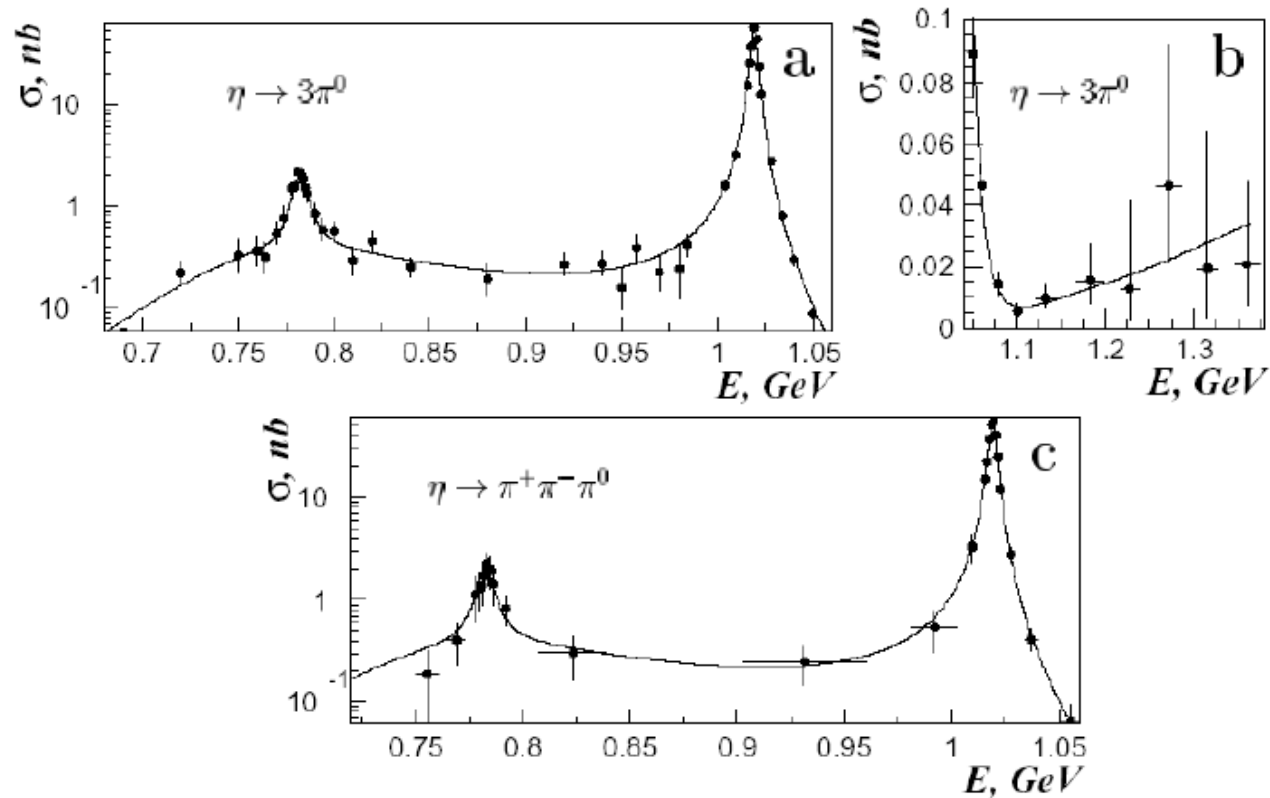
$\Gamma(e^+e^-) \times \Gamma(\eta\gamma)/\Gamma_{\text{total}}^2$					$\Gamma_9\Gamma_5/\Gamma^2$
VALUE (units 10^{-8})	EVTS	DOCUMENT ID	TECN	COMMENT	
3.31±0.28 OUR FIT Error includes scale factor of 1.1.					
3.18±0.28 OUR AVERAGE					
$3.10\pm0.31\pm0.11$	33k	²⁴ ACHASOV	07B	SND	0.6–1.38 $e^+e^- \rightarrow \eta\gamma$
$3.17^{+1.85}_{-1.31}\pm0.21$	17.4k	²⁵ AKHMETSHIN	05	CMD2	0.60-1.38 $e^+e^- \rightarrow \eta\gamma$
$3.41\pm0.52\pm0.21$	23k	^{26,27} AKHMETSHIN	01B	CMD2	$e^+e^- \rightarrow \eta\gamma$



ACHASOV 07B: Phys. Rev. D76 (2007) 077101

$\omega \rightarrow \eta\gamma$ branching ratio measurement from SND

The branching ratio is extracted with a global fit to the $e^+e^- \rightarrow \eta\gamma$ with a VMD model with $\rho, \omega, \phi, \rho'$ included (ρ' parameters varied to compute systematics and constrained from $e^+e^- \rightarrow \eta\rho$).



ω contribution overwhelmed by the $\rho \rightarrow \eta\gamma$ contribution
no correlation matrix is given in the paper

The fit is dominated by the SND measurement

$\Gamma(\eta\gamma)/\Gamma_{\text{total}}$		<i>EVTS</i>	<i>DOCUMENT ID</i>	<i>TECN</i>	<i>COMMENT</i>
VALUE (units 10^{-4})					
4.6 $\pm$ 0.4	OUR FIT	Error includes scale factor of 1.1.			
6.3 $\pm$ 1.3	OUR AVERAGE	Error includes scale factor of 1.2.			
6.6 $\pm$ 1.7		53	ABELE	97E CBAR	0.0 $\bar{p}p \rightarrow 5\gamma$
8.3 $\pm$ 2.1			ALDE	93 GAM2	38 $\pi^- p \rightarrow \omega n$
3.0 $^{+2.5}_{-1.8}$		54	ANDREWS	77 CNTR	6.7–10 γCu

1.2 σ

In Crystal Barrel the channel $p\bar{p} \rightarrow \eta \omega$ is used that is 6 times larger than $p\bar{p} \rightarrow \eta \rho$, the $\omega \rightarrow \eta \gamma$ Br was normalized to the $\omega \rightarrow \pi^0 \gamma$ Br

Using $\omega \rightarrow \eta \gamma$ from PDG average

Giorgio request

	Gluonium allowed	Gluonium at zero	Gluonium allowed (no $P \rightarrow \gamma\gamma$ constraint)
$\chi^2/n.d.f(Prob)$	3.9/3 (27.5 %)	13/4 (1.1 %)	2.07 /2 (35 %)
Z_G^2	0.111 $\pm$ 0.036	0 fixed	0.06 $\pm$ 0.05
φ_P	(40.6 $\pm$ 0.7) $^\circ$	(41.5 $\pm$ 0.5) $^\circ$	(41.2 $\pm$ 0.8) $^\circ$
Z_{NS}	0.890 $\pm$ 0.025	0.882 $\pm$ 0.023	0.88 $\pm$ 0.03
Z_S	0.79 $\pm$ 0.05	0.78 $\pm$ 0.05	0.78 $\pm$ 0.05
φ_V	(3.15 $\pm$ 0.10) $^\circ$	(3.18 $\pm$ 0.09) $^\circ$	(3.17 $\pm$ 0.09) $^\circ$
$m_s/\bar{m}$	1.24 $\pm$ 0.07	1.24 $\pm$ 0.07	1.24 $\pm$ 0.07

Results using KLOE $\text{Br}(\omega \rightarrow \pi^0 \gamma)$

$$\text{KLOE } \text{Br}(\omega \rightarrow \pi^0 \gamma) = 8.09 \pm 0.14 \%$$

3σ away

$$\text{PDG08} = 8.92 \pm 0.24 \%$$

$\omega \rightarrow \eta \gamma$ from PDG average

	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	4.16/3 (25 %)	13/4 (1.1 %)
Z_G^2	0.109 ± 0.036	0 fixed
φ_P	$(40.5 \pm 0.7)^\circ$	$(41.4 \pm 0.5)^\circ$
Z_{NS}	0.935 ± 0.025	0.926 ± 0.023
Z_S	0.83 ± 0.05	0.82 ± 0.05
φ_V	$(3.3 \pm 0.09)^\circ$	$(3.3 \pm 0.09)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07

No big effect on Z_G but important contribution to $Z_{S,NS}$ and ω - ϕ mixing angle

Referee request: try to find a more robust estimate of f_q and f_s

Estimates used in our previous paper

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_{\pi}} \right)^3 \left(\frac{f_{\pi}}{f_q} 5 \sin(\phi_P) \cos(\phi_G) + \sqrt{2} \frac{f_{\pi}}{f_s} \cos(\phi_P) \cos(\phi_G) \right)^2$$

T. Feldmann, Int. J. Mod. Phys. A 15 (2000) 159

source	f_q/f_{π}	f_s/f_{π}	ϕ_q	ϕ_s
Mass matrix and radiative decays ^{16,17}	[1.0]	[1.4]	44°	
$U(1)_A$ anomaly & meson masses ¹⁸	1.0	1.4	[42°]	
Phenomenology ^{2,19,20,21}	[1.1 – 1.2]	[1.1 – 1.3]	[28°-34°]	[35°-41°]
NJL quark model & phenom. ²²	[1.07]	[1.36]	[44.1°]	[40.6°]
Current mixing model & phenom. ⁴³	[0.98]	[0.66]	[35.9°]	[26.2°]
Phenomenology ²³	[1.00]	[1.45]	39.2°	
GMO mass formula ⁴²	[1.13]	[1.16]	[31.2°]	[35.4°]
χ PT & $1/N_C$ expansion & phenom. ²⁴	[1.08]	[1.43]	[44.8°]	[40.5°]
FKS scheme & theory ²⁶	1.00	1.41	42.4°	
FKS scheme & phenom. ²⁶	1.07	1.34	39.3°	
Vector meson dominance & phenom. ⁴⁴	[1.09]	[1.55]	[47.5°]	[42.1°]
Energy dependent scheme & phenom. ⁴⁵	[1.10]	[1.46]	[38.9°]	[41.0°]

Better to avoid
phenomenological
calculations.

Value used up to now, 1% error assumed.
Reasonable if compared to $U(1)_A$ anomaly and meson
masses.

Alternative approach

E. Kou, Phys. Rev. D 63 (2001) 54027

Isospin conservation implies:

$$if_q p^\mu = \langle 0 | \bar{\psi} \gamma^\mu \gamma^5 \psi \left| \frac{u\bar{u} + d\bar{d}}{\sqrt{2}} \right\rangle \quad \longleftrightarrow \quad if_\pi p^\mu = \langle 0 | \bar{\psi} \gamma^\mu \gamma^5 \psi \left| \frac{u\bar{u} - d\bar{d}}{\sqrt{2}} \right\rangle$$
$$f_q = f_\pi; \quad f_s = \sqrt{f_K^2 - f_\pi^2}$$

$$f_q/f_\pi = 1 \quad \text{with no error} \quad \frac{f_s}{f_\pi} = \sqrt{2 \frac{f_K^2}{f_\pi^2} - 1}$$

$$f_K/f_\pi = 1.189(7)$$

Lattice-UKQCD:

Follana et al., Phys. Rev. Lett.
100 (2008) 062002

$$\frac{f_s}{f_\pi} = 1.352 \pm 0.007$$

**0.5% error
but 4% difference
with our previous
value.**

Fit with new values for f_q and f_s

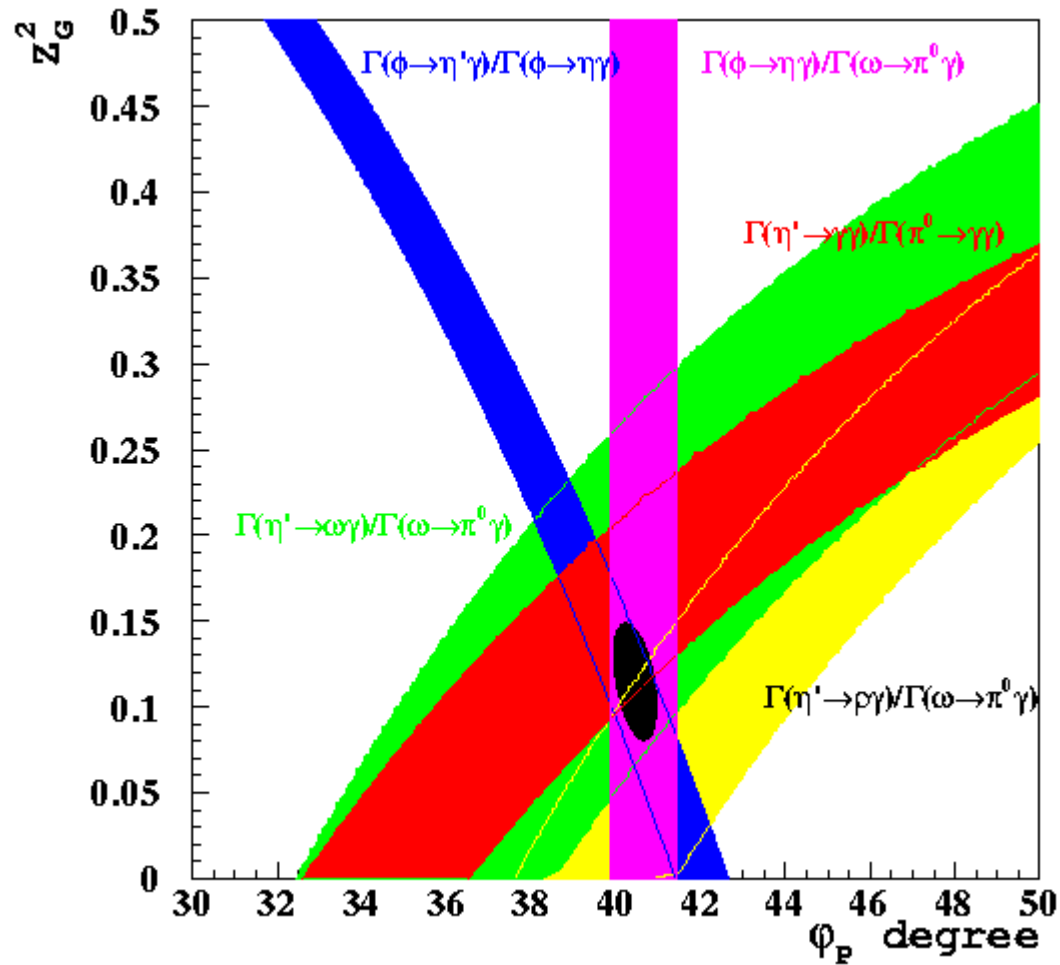
	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	4.6/3 (20.5 %)	14.7/4 (.5 %)
Z_G^2	0.115 ± 0.036	0 fixed
φ_P	$(40.4 \pm 0.6)^\circ$	$(41.4 \pm 0.5)^\circ$
Z_{NS}	0.936 ± 0.025	0.927 ± 0.023
Z_S	0.83 ± 0.05	0.82 ± 0.05
φ_V	$(3.32 \pm 0.09)^\circ$	$(3.34 \pm 0.09)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07

5% difference in
the gluonium
content

Fit with old values for f_q and f_s

	Gluonium allowed	Gluonium at zero
$\chi^2/n.d.f(Prob)$	4.16/3 (25 %)	13/4 (1.1 %))
Z_G^2	0.109 ± 0.036	0 fixed
φ_P	$(40.5 \pm 0.7)^\circ$	$(41.4 \pm 0.5)^\circ$
Z_{NS}	0.935 ± 0.025	0.926 ± 0.023
Z_S	0.83 ± 0.05	0.82 ± 0.05
φ_V	$(3.3 \pm 0.09)^\circ$	$(3.3 \pm 0.09)^\circ$
$m_s/\bar{m}$	1.24 ± 0.07	1.24 ± 0.07

Measurements contributions



What to put in the paper?

In order to use the same experimental informations, but using our way we normalise all quantities to $\Gamma(\omega \rightarrow \pi^0 \gamma)$.

In this way the fit is independent from the coupling g .

Discrepancy between our definition of $\Gamma(\eta' \rightarrow \rho \gamma)/\Gamma(\omega \rightarrow \pi^0 \gamma)$ and Escribano definition of g 's

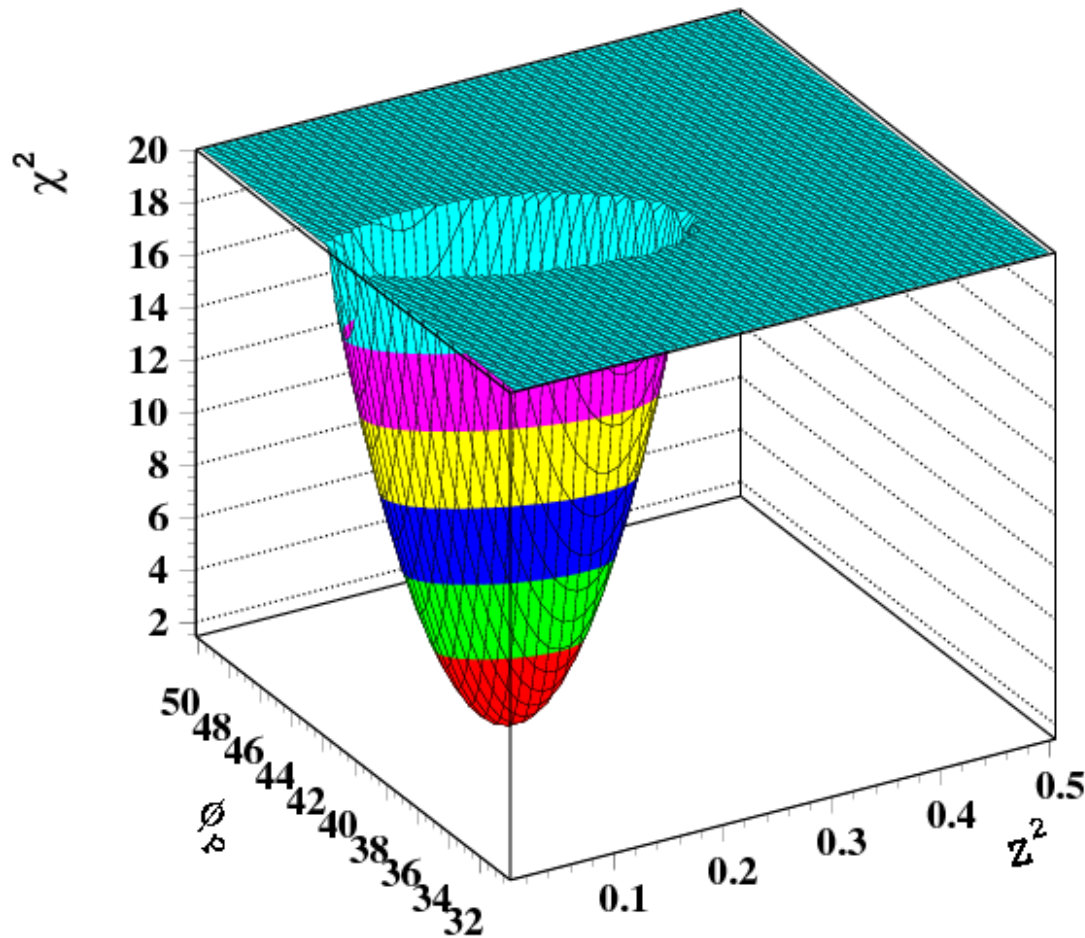
$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{\frac{g_{\eta' \rightarrow \rho \gamma}^2}{4\pi} |p_{\gamma}^{\eta'}|^3}{\frac{g_{\omega \rightarrow \pi^0 \gamma}^2}{12\pi} |p_{\gamma}^{\omega}|^3} = 3 \frac{|p_{\gamma}^{\eta'}|^3}{|p_{\gamma}^{\omega}|^3} \frac{g^2 Z_q^2 X_{\eta'}^2}{g^2 \cos^2 \phi_V} = 3 \frac{|p_{\gamma}^{\eta'}|^3}{|p_{\gamma}^{\omega}|^3} \frac{Z_q^2}{\cos^2 \phi_V} \sin^2 \phi_P \cos^2 \phi_G$$

$$\Gamma(\eta' \rightarrow \rho \gamma)/\Gamma(\omega \rightarrow \pi^0 \gamma)$$

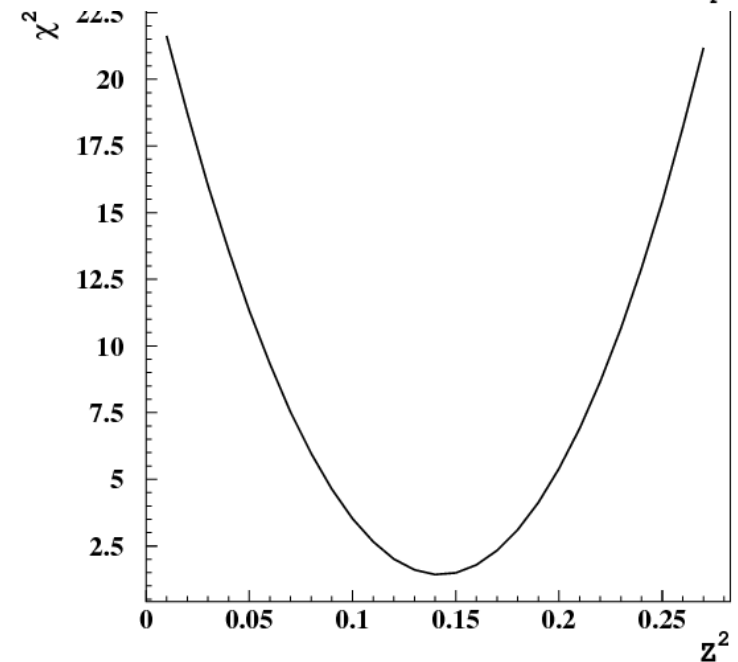
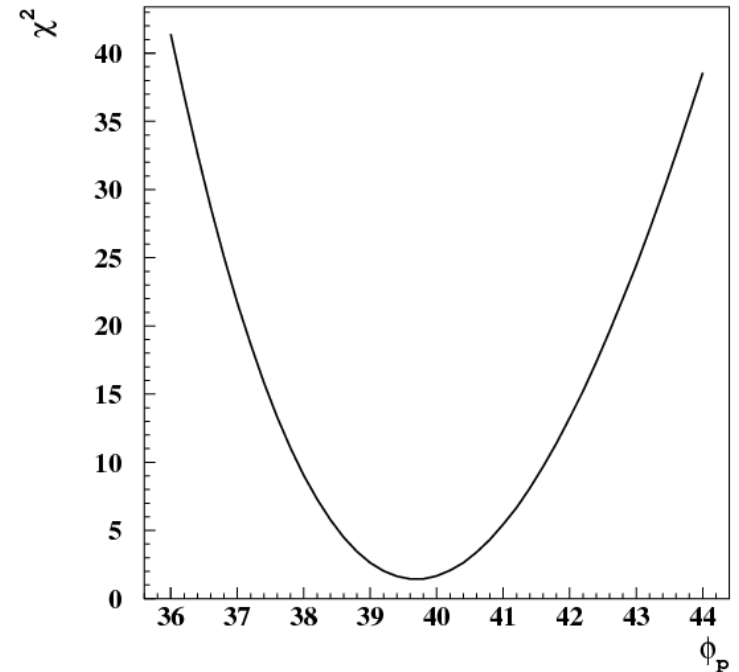
while in our paper:

$$= \frac{C_{NS}}{\cos \phi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_{\rho}^2}{m_{\omega}^2 - m_{\pi}^2} \frac{m_{\omega}}{m_{\eta'}} \right)^3 \cos^2 \phi_G \sin^2 \phi_P$$

Check of the χ^2 behaviour



Only one minimum in the whole parameters' domain.



Check of the Escribano hypothesis

Fit redone using Escribano fit parameters:

$$C_{\text{NS}} = 0.86 \pm 0.03 \quad C_{\text{S}} = 0.78 \pm 0.05$$

	Fit	Paper
$\mathbf{z}^2$	0.12 ± 0.03	0.14 ± 0.04
ϕ_{p}	$(40.0 \pm 0.7)^\circ$	$(39.7 \pm 0.7)^\circ$

The fit is very stable respect to the overlapping parameters

Differences between Escribano and our fit

Our fit

Escribano

Differences between Escribano and our fit

Our fit

Only ϕ_p and Z^2 are left free

Escribano

All theoretical parameters
are left free

Differences between Escribano and our fit

Our fit

Only ϕ_p and Z^2 are left free

The ratios of Γ 's are used in the fit.

Escribano

All theoretical parameters are left free

The Γ 's are used in the fit.

Differences between Escribano and our fit

Our fit

Only ϕ_p and Z^2 are left free

The ratios of Γ 's are used in the fit.

4 measured quantities are used in the fit

Escribano

All theoretical parameters are left free

The Γ 's are used in the fit.

11 measured quantities are used in the fit

Differences between Escribano and our fit

Our fit

Only ϕ_p and Z^2 are left free

The ratios of Γ 's are used in the fit.

4 measured quantities are used in the fit

DATA from PDG '06 +
KLOE R_ϕ '07

Escribano

All theoretical parameters are left free

The Γ 's are used in the fit.

11 measured quantities are used in the fit

DATA from PDG '06

Escribano amplitudes

$$\begin{aligned}
 g_{\omega\eta\gamma} &= \frac{1}{3}g \left(z_q X_\eta \cos \phi_V + 2\frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right) , \\
 g_{\omega\eta'\gamma} &= \frac{1}{3}g \left(z_q X_{\eta'} \cos \phi_V + 2\frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right) , \\
 g_{\phi\eta\gamma} &= \frac{1}{3}g \left(z_q X_\eta \sin \phi_V - 2\frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right) , \\
 g_{\phi\eta'\gamma} &= \frac{1}{3}g \left(z_q X_{\eta'} \sin \phi_V - 2\frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right) ,
 \end{aligned}
 \left| \begin{array}{l}
 z_q = C_{NS} \\
 z_s = C_s \\
 \textbf{Constrain} \\
 \phi_p, \mathbf{Z}_G
 \end{array} \right.$$

Escribano amplitudes

$$\begin{aligned}
 g_{\omega\eta\gamma} &= \frac{1}{3}g \left(z_q X_\eta \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right) , \\
 g_{\omega\eta'\gamma} &= \frac{1}{3}g \left(z_q X_{\eta'} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right) , \\
 g_{\phi\eta\gamma} &= \frac{1}{3}g \left(z_q X_\eta \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right) , \\
 g_{\phi\eta'\gamma} &= \frac{1}{3}g \left(z_q X_{\eta'} \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right) ,
 \end{aligned}
 \left| \begin{array}{l}
 z_q = C_{NS} \\
 z_s = C_s \\
 \text{Constrain} \\
 \phi_p, Z_G
 \end{array} \right.$$

$$\begin{aligned}
 g_{\rho^0\pi^0\gamma} &= g_{\rho^+\pi^+\gamma} = \frac{1}{3}g , & g_{\omega\pi\gamma} &= g \cos \phi_V , & g_{\phi\pi\gamma} &= g \sin \phi_V , \\
 g_{K^{*0}K^0\gamma} &= -\frac{1}{3}g z_K \left(1 + \frac{\bar{m}}{m_s} \right) , & g_{K^{*+}K^+\gamma} &= \frac{1}{3}g z_K \left(2 - \frac{\bar{m}}{m_s} \right) ,
 \end{aligned}$$

Fix the parameters $m_s/\bar{m}, \phi_V, g$

Escribano amplitudes

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right) ,$$

$$z_q = C_{NS}$$

$$z_s = C_s$$

$$g_{\omega\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right) ,$$

Constrain

ϕ_p, Z_G

$$g_{\phi\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right) ,$$

$$g_{\phi\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right) ,$$

$\tan \phi_V \ll 1 \quad (\phi_V = 3.2^\circ)$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\bar{m}} \frac{C_{NS}}{C_s} \cdot \tan \frac{\phi_V}{\sin 2\phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

Escribano amplitudes

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right) ,$$

$$z_q = C_{NS}$$

$$z_s = C_s$$

$$g_{\omega\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right) ,$$

Constrain

ϕ_p, Z_G

$$g_{\phi\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right) ,$$

$$g_{\phi\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right) ,$$

$$\tan \phi_V \ll 1 \quad (\phi_V = 3.2^\circ)$$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\bar{m}} \frac{C_{NS}}{C_s} \cdot \tan \frac{\phi_V}{\sin 2\phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

Contains terms up to $\tan^2 \phi_V$, but it is not $\mathcal{O}(\tan^2 \phi_V)$

Escribano amplitudes

$$g_{\omega\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_\eta \sin \phi_V \right) ,$$

$$g_{\omega\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \cos \phi_V + 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \sin \phi_V \right) ,$$

$$g_{\phi\eta\gamma} = \frac{1}{3}g \left(z_q X_\eta \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_\eta \cos \phi_V \right) ,$$

$$g_{\phi\eta'\gamma} = \frac{1}{3}g \left(z_q X_{\eta'} \sin \phi_V - 2 \frac{\bar{m}}{m_s} z_s Y_{\eta'} \cos \phi_V \right) ,$$

$$z_q = C_{NS}$$

$$z_s = C_s$$

Constrain

ϕ_p, Z_G

$\tan \phi_V \ll 1 \quad (\phi_V = 3.2^\circ)$

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\bar{m}} \frac{C_{NS}}{C_s} \cdot \tan \frac{\phi_V}{\sin 2\phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3$$

$$+ \left(\frac{C_{NS}}{C_s} \frac{m_s}{\bar{m}} \tan \phi_V \right)^2 (1 + 2 \cos^2 \phi_P) \left(\frac{p_{\eta'}}{p_\eta} \right)^3 + o(\tan^2 \phi_V)$$

KLOE fit with full formula

$$R_\phi = \frac{Br(\phi \rightarrow \eta' \gamma)}{Br(\phi \rightarrow \eta \gamma)} = \cot^2 \phi_P \cdot \cos^2 \phi_G \left(1 - \frac{m_s}{\bar{m}} \frac{C_{NS}}{C_S} \cdot \tan \frac{\phi_V}{\sin 2\phi_P} \right)^2 \cdot \left(\frac{p_{\eta'}}{p_\eta} \right)^3 + \left(\frac{C_{NS}}{C_S} \frac{m_s}{\bar{m}} \tan \phi_V \right)^2 (1 + 2\cos^2 \phi_P)$$

	Fit	Paper
z^2	0.14 ± 0.03	0.14 ± 0.04
ϕ_p	$(39.9 \pm 0.7)^\circ$	$(39.7 \pm 0.7)^\circ$

Freeing the overlapping parameters

$$\frac{\Gamma(\eta' \rightarrow \gamma \gamma)}{\Gamma(\pi^0 \rightarrow \gamma \gamma)} = \frac{1}{9} \left(\frac{m_{\eta'}}{m_{\pi}} \right)^3 \left(5X_{\eta'} + \sqrt{2} \frac{f_q}{f_s} Y_{\eta'} \right)^2$$

$$\frac{\Gamma(\eta' \rightarrow \rho \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{C_{NS}}{\cos \phi_V} \cdot 3 \left(\frac{m_{\eta'}^2 - m_{\rho}^2 m_{\omega}}{m_{\omega}^2 - m_{\pi}^2 m_{\eta'}} \right)^3 X_{\eta'}^2$$

$$\frac{\Gamma(\eta' \rightarrow \omega \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)} = \frac{1}{3} \left(\frac{m_{\eta'}^2 - m_{\omega}^2 m_{\omega}}{m_{\omega}^2 - m_{\pi}^2 m_{\eta'}} \right)^3 \left[C_{NS} X_{\eta'} + 2 \frac{m_s}{\bar{m}} C_s \cdot \tan \phi_V \cdot Y_{\eta'} \right]^2$$

Not enough
constraint to
leave free
 C_{NS} and C_s

We add to the fit:

$$\frac{\Gamma(\omega \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\rho \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}, \frac{\Gamma(\phi \rightarrow \eta \gamma)}{\Gamma(\omega \rightarrow \pi^0 \gamma)}$$

Fit result

FCN= 1.406759 FROM MINOS STATUS=SUCCESSFUL 187 CALLS 277
TOTAL

EDM= 0.34E-06 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT	PARAMETER	PARABOLIC	MINOS ERRORS	
NO.	NAME	VALUE	ERROR	NEGATIVE POSITIVE
1	z2	0.11720	0.41464E-01	-0.41484E-01 0.41463E-01
2	PHIP	40.056	0.97108	-0.94271 1.0031
3	CNSP	0.86965	0.31043E-01	-0.31096E-01 0.31044E-01
4	CSPA	0.79071	0.47577E-01	-0.44712E-01 0.50965E-01

Fit with free C_{NS} C_S

Paper

Escribano

z^2 0.12±0.04

0.14±0.04

$(0.04 \pm 0.09)^\circ$

ϕ_p $(40.1 \pm 1.0)^\circ$

$(39.7 \pm 0.7)^\circ$

$(41.4 \pm 1.3)^\circ$

C_{NS} 0.87±0.03

0.86±0.03

C_S 0.79 ± 0.05

0.78±0.05

Fit result

FCN= 1.406759 FROM MINOS STATUS=SUCCESSFUL 187 CALLS 277
TOTAL

EDM= 0.34E-06 STRATEGY= 1 ERROR MATRIX ACCURATE

EXT	PARAMETER	PARABOLIC	MINOS ERRORS	
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2	PHIP	40.056	0.97108	-0.94271 1.0031
3	CNSP	0.86965	0.31043E-01	-0.31096E-01 0.31044E-01
4	CSPA	0.79071	0.47577E-01	-0.44712E-01 0.50965E-01

Fit with free C_{NS} C_S

Paper

Escribano

z^2 0.12±0.04

0.14±0.04

$(0.04 \pm 0.09)^\circ$

ϕ_p $(40.1 \pm 1.0)^\circ$

$(39.7 \pm 0.7)^\circ$

$(41.4 \pm 1.3)^\circ$

C_{NS} 0.87±0.03

0.86±0.03

C_S 0.79 ± 0.05

0.78±0.05



Perfect agreement

Fit results

Glueonium still at 3σ

Fit with free C_{NS} C_S

z^2	0.12 ± 0.04
-------	-----------------

$$\phi_p \quad (40.1 \pm 1.0)^\circ$$

$$C_{NS} \quad 0.87 \pm 0.03$$

$$C_S \quad 0.79 \pm 0.05$$

Paper

$$0.14 \pm 0.04$$

$$(39.7 \pm 0.7)^\circ$$

Escribano

$$(0.04 \pm 0.09)^\circ$$

$$(41.4 \pm 1.3)^\circ$$

$$0.86 \pm 0.03$$

$$0.78 \pm 0.05$$



Perfect agreement

Fit results

TO BE CONTINUED

Fit with

at 3σ

Paper

Escribano

z^2 0.12 ± 0.04

0.14 ± 0.04

$(0.04 \pm 0.09)^\circ$

ϕ_p $(40.1 \pm 1.0)^\circ$

$(39.7 \pm 0.7)^\circ$

$(41.4 \pm 1.3)^\circ$

C_{NS} 0.87 ± 0.03

0.86 ± 0.03

C_s 0.79 ± 0.05

Perfect agreement

0.78 ± 0.05

The $\eta' \rightarrow \gamma\gamma/\pi^0 \rightarrow \gamma\gamma$ constraint

Removing this constraint we obtain:

Fit with free $C_{NS} C_S$
no $P \rightarrow \gamma\gamma$ constraint

z^2	0.09 ± 0.06
ϕ_p	$(40.2 \pm 1.0)^\circ$
C_{NS}	0.86 ± 0.03
C_S	0.79 ± 0.05

Fit with free $C_{NS} C_S$

z^2	0.12 ± 0.04
ϕ_p	$(40.1 \pm 1.0)^\circ$
C_{NS}	0.87 ± 0.03
C_S	0.79 ± 0.05

Escribano

$(0.04 \pm 0.09)^\circ$
$(41.4 \pm 1.3)^\circ$
0.86 ± 0.03
0.78 ± 0.05

The $\eta' \rightarrow \gamma\gamma/\pi^0 \rightarrow \gamma\gamma$ constraint

Removing this constraint we obtain:

Fit with free C_{NS} C_S
no $P \rightarrow \gamma\gamma$ constraint

z^2	0.09 ± 0.06
ϕ_p	$(40.2 \pm 1.0)^\circ$
C_{NS}	0.86 ± 0.03
C_S	0.79 ± 0.05

Fit with free C_{NS} C_S

z^2	0.12 ± 0.04
ϕ_p	$(40.1 \pm 1.0)^\circ$
C_{NS}	0.87 ± 0.03
C_S	0.79 ± 0.05

Escribano

$(0.04 \pm 0.09)^\circ$
$(41.4 \pm 1.3)^\circ$
0.86 ± 0.03
0.78 ± 0.05

The $P \rightarrow \gamma\gamma$ constraint is important!! It moves the central value and reduce the error (Here someone is cheating..)

Fitting the Width (using KLOE and last SND results)

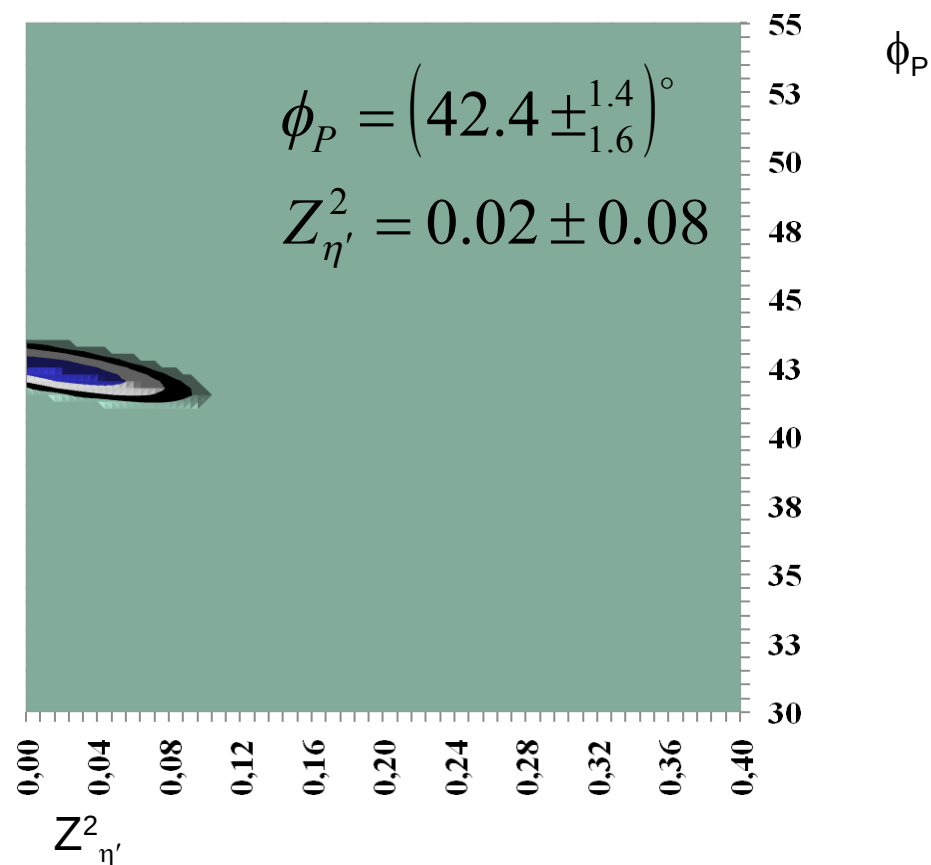
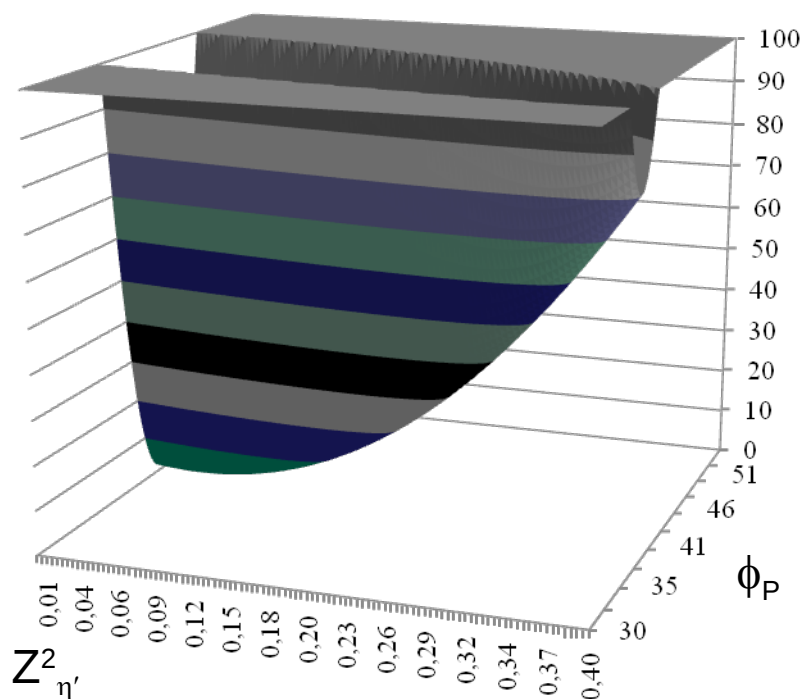
Slide from Camilla

We fit as Escribano - constraints from partial width
with our method - only $\cos\phi_P$, $\cos\phi_G$ left free

We find the following results to compare with Rafael's ones

Escribano fit

$$(\phi_P, Z_{\eta'}^2) = (42.6^\circ, 0.01)$$



Conclusions and outlook

- All the objections to our paper have been rejected by the check performed;
- To complete the study we have to implement 4 further constraints and fit with all free parameters;
- From the preliminary study we can say:
 - The gluonium is at 3σ whatever we use for the overlapping parameters or include them in the fit;
 - The $P \rightarrow \gamma\gamma$ is proved to be an important constraint: increases the gluonium component and reduces the error by 33%
 - The fit to the Γ 's looks promising
- We would like to write a short answer to Escribano and Thomas at the end of the work.

