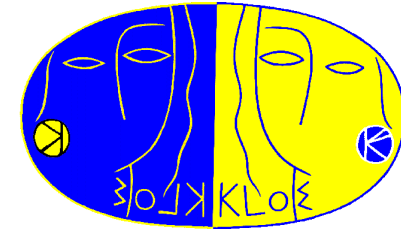
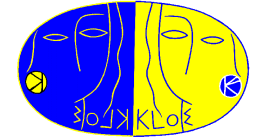


*A preliminary measurement  
of  $\text{BR}(K_L \rightarrow \pi^+ \pi^-)$  using a  
double-tag method*



**M. Antonelli, M. Dreucci, M. Moulson, T. Spadaro**  
KLOE Physics Workshop, Isola d'Elba, 24 May 2001



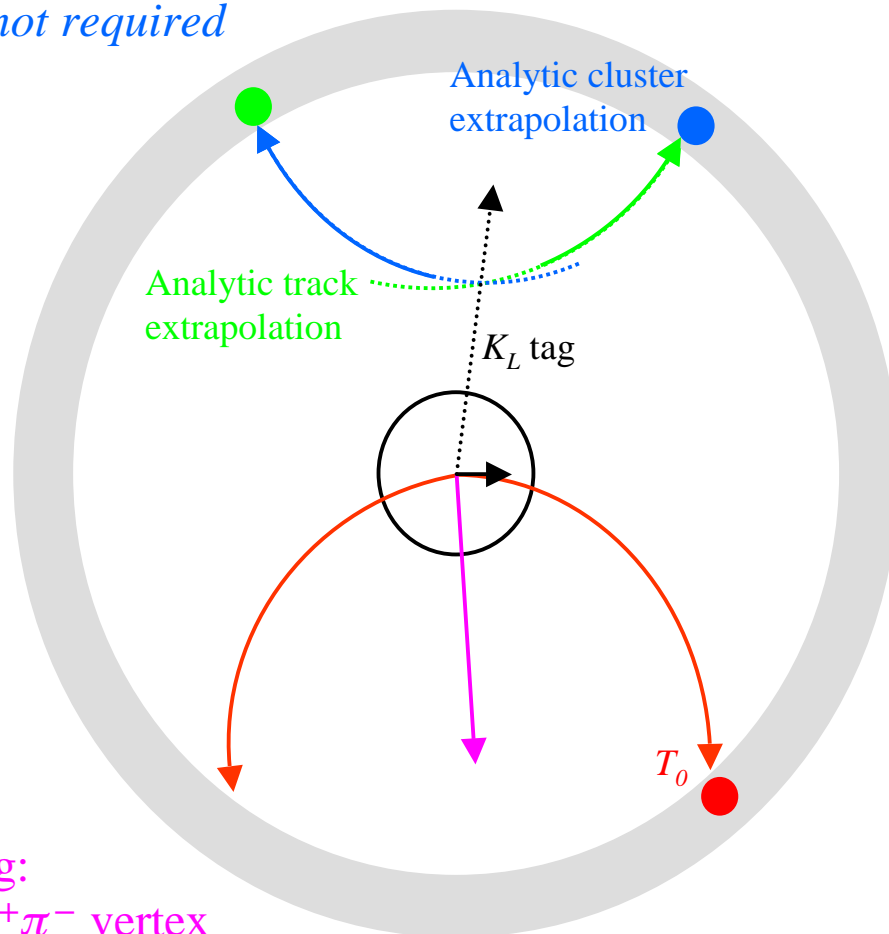


# The double-tag method

Decay tag:

1 track + cluster opposite

*Vertex not required*



Event tag:

$K_S \rightarrow \pi^+ \pi^-$  vertex

**Tag cuts:**

- Track residual
- Cluster residual
- $p^*$  (CM frame of KL tag)

$$N_1 = 2\varepsilon_1 S + B_1$$

$$N_2 = \varepsilon_1^2(1-\rho)S + B_2$$

$$S = 4(1-\rho)N_1^2/N_2$$

$$\varepsilon = 2N_2/[N_1(1-\rho)]$$

**Input from MC:**

Background ( $B_1, B_2$ )

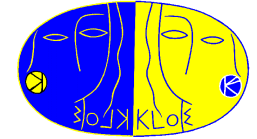
Dominantly from  $K_{\mu 3}$

Shape from MC

Sideband/fit normalization

Tagging correlation ( $1 - \rho$ ):

$$(1 - \rho) = \varepsilon_2^{\text{MC}}/(\varepsilon_1^{\text{MC}})^2$$



# Data and MC samples

---

## Data:

All **ks2p** Ntuples as of 18 May 2001

Runs 13732-14678: July/Aug 2000 (4.1 pb<sup>-1</sup>)

Runs 16211-17186: Nov 2000 (13.3 pb<sup>-1</sup>)

7441626 total  $K_L$  tags found

## MC Signal:

Y2K **cpv\_cksh**, Runs 5-16

$K_S \rightarrow \pi^+\pi^-$ ,  $K_L \rightarrow \pi^+\pi^-$  ( $K_L \rightarrow \pi^0\pi^0$  removed)

81755 total  $K_L$  tags in FV (208 pb<sup>-1</sup> assuming  $\sigma_\phi = 3.1 \mu\text{b}$ )

## MC Background:

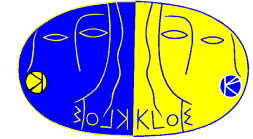
Y2K **neu\_kaon**, Runs 26-225

$K_S \rightarrow \pi^+\pi^-$ ,  $K_L \rightarrow$  all ( $K_S \rightarrow \pi^0\pi^0$ ,  $K_L \rightarrow \pi^+\pi^-$  removed)

3302226  $K_L$  tags (4.6 pb<sup>-1</sup> assuming  $\sigma_\phi = 3.1 \mu\text{b}$ )

---

# $K_L$ tag



1 vertex, zero net charge

$$r_{xy} < 5 \text{ cm}, -20 \text{ cm} < z < 20 \text{ cm}$$

$$M - M_K < 20 \text{ MeV}$$

Tree/vertex extension

1 track (or daughter of recognized kink)  
analytically extrapolates to cluster

$$d < 30 \text{ cm}, E > 50 \text{ MeV}$$

Primary decay position from extrapolation  
of  $p_{KS}$  to beam line

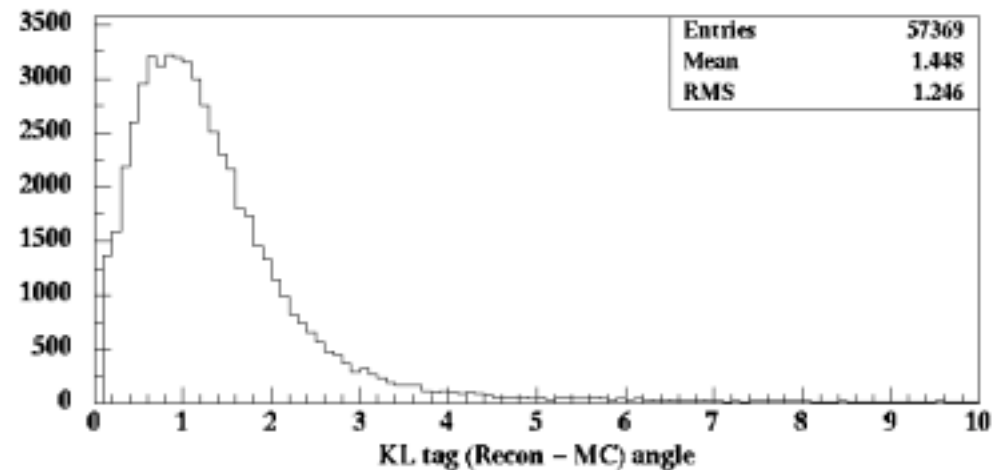
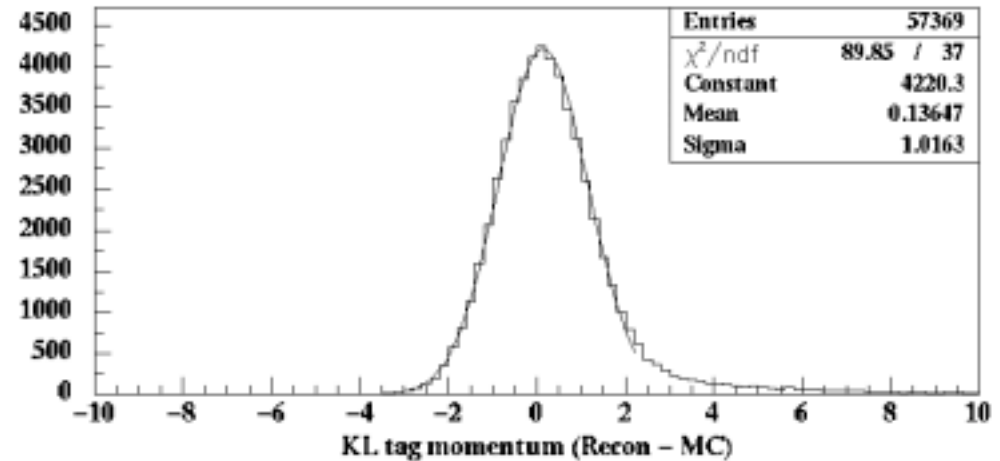
$K_S$  momentum from boost

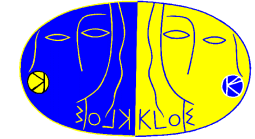
$\sqrt{s}$ , boost components run-by-run

$\sigma(K_L \text{ tag})$ :

428 nb, using  $L_{\text{datarec}}$

477 nb, using  $\sigma_\phi = 3.1 \mu\text{b}, \varepsilon_{\text{KLtag}}(\text{MC})$





# $K_L$ tag efficiency

$K_L$  tag efficiencies from MC:

$K_L \rightarrow$  all, everywhere:  $0.6631 \pm 0.0003$

$K_L \rightarrow \pi^+\pi^-$  in FV:  $0.7017 \pm 0.0016$

Tag bias:

$$f = \mathbf{0.945 \pm 0.002}$$

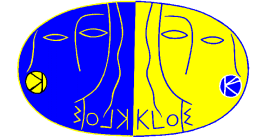
*Assume 50% systematic error on this correction*

$$BR = \frac{N_{\text{decay}} / \epsilon_{\text{tag}}^{\text{decay}}}{N_{\text{tag}} / \epsilon_{\text{tag}}}$$

$$f = \epsilon_{\text{tag}} / \epsilon_{\text{tag}}^{\text{decay}}$$

MC $K_S \rightarrow \pi^+\pi^-$ and:	81755 evts $K_L \rightarrow \pi^+\pi^-$ in FV		3302226 evts $K_L \rightarrow$ all	
Trigger	77753	0.951	2860194	0.866
FILFO	81643	0.999	3218969	0.975
ECL $K_L$ tag	62277	0.762	2562475	0.775
Our $K_L$ tag selection	59354	0.726	2430574	0.736
<b>Overall</b>	57369	<b>0.702</b>	2189761	<b>0.663</b>

# Decay tag



Tree extend excluding  $K_S$  tracks

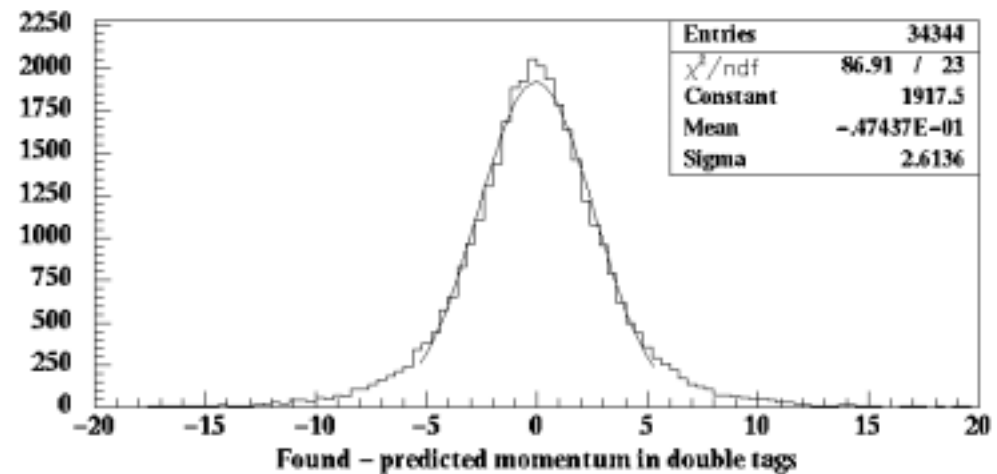
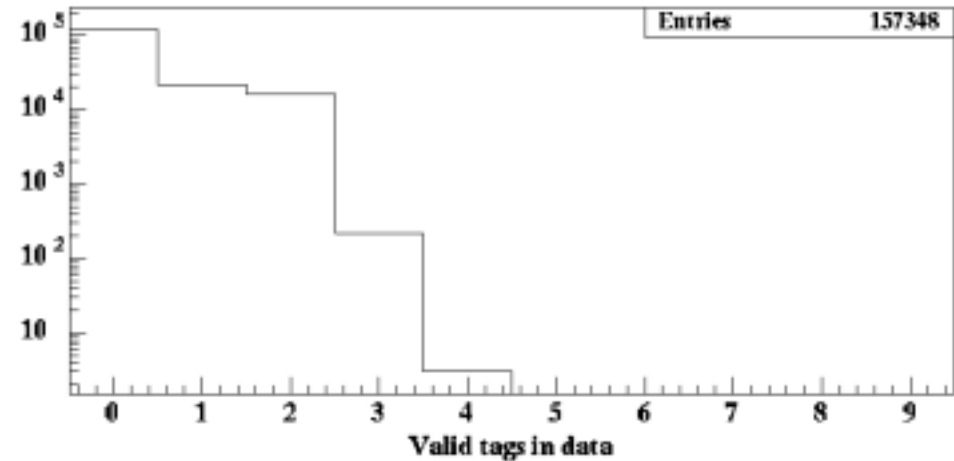
Select branch of each tree with smallest track residual

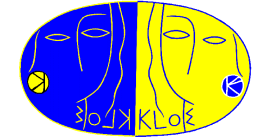
Construct  $p_{\text{miss}}$  from  $p, p_{KL}$

Analytically extrapolate to EmC

Apply track, cluster distance cuts

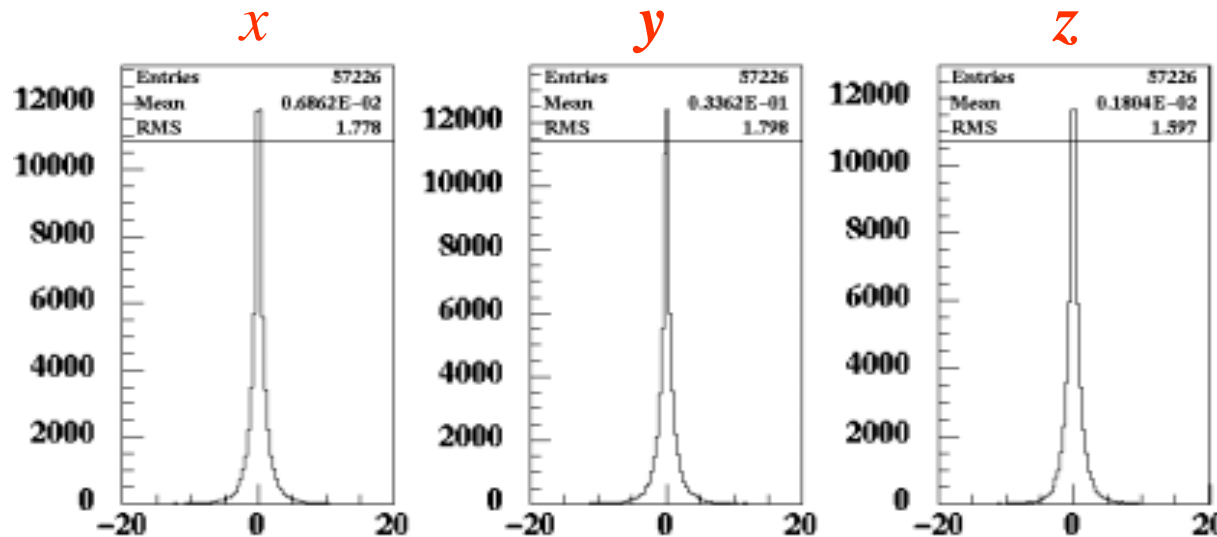
Retain  $+/-$  track with best  $p^*$





# Fiducial volume

Single tags



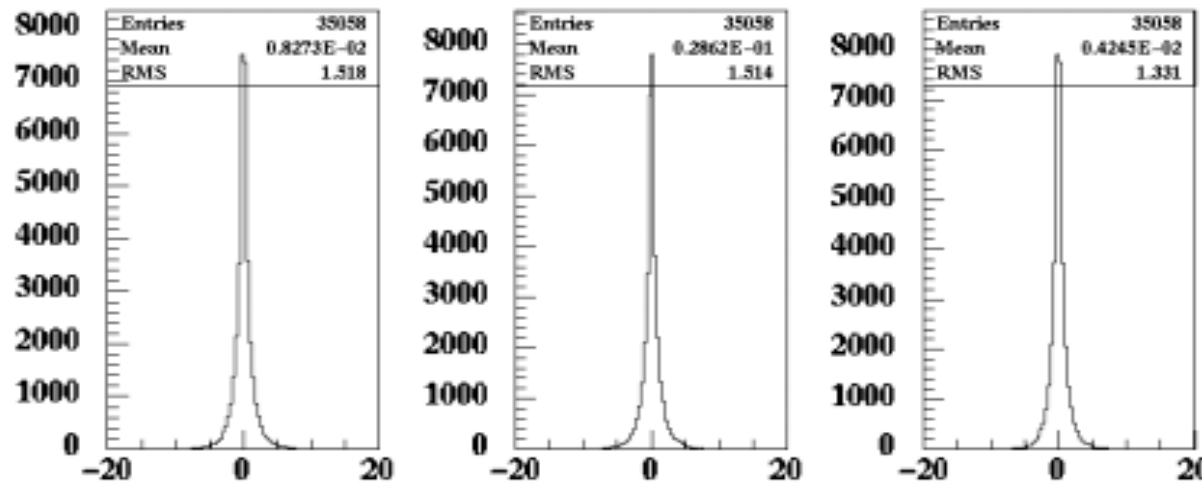
Fiducial volume:

$$35 \text{ cm} < r_{xy} < 150 \text{ cm}$$
$$-100 \text{ cm} < z < 100 \text{ cm}$$

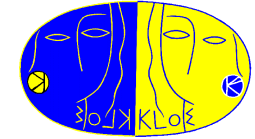
$\epsilon_{\text{FV}}$  from MC:

$$0.2653 \pm 0.0009$$

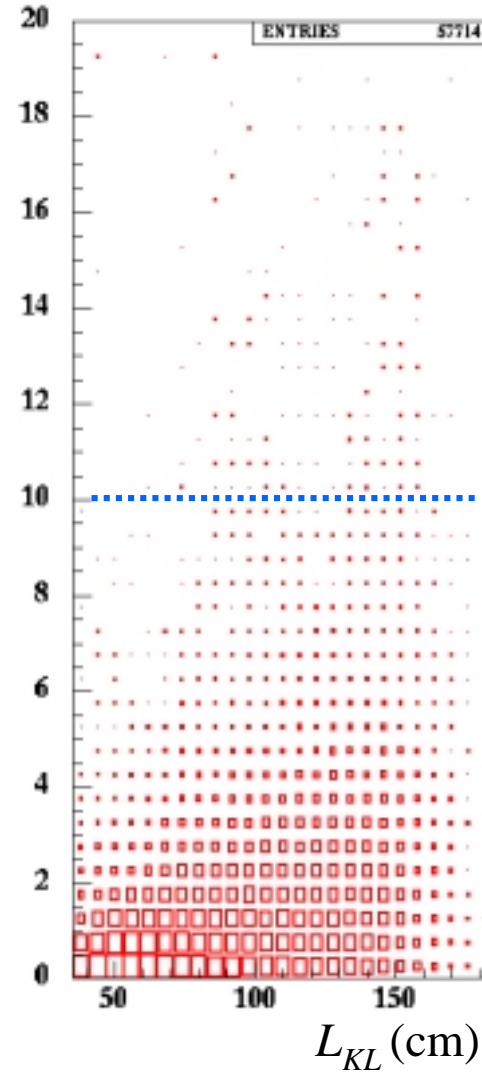
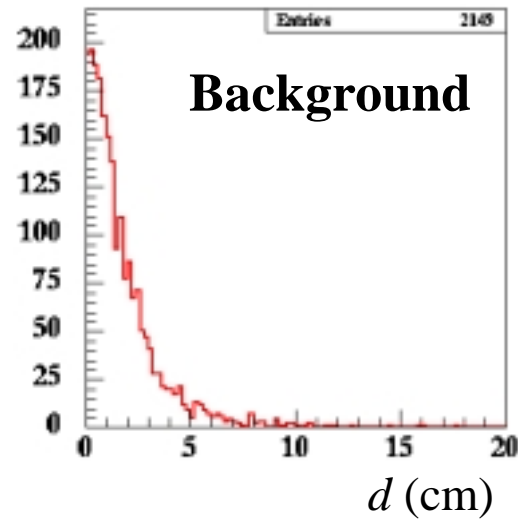
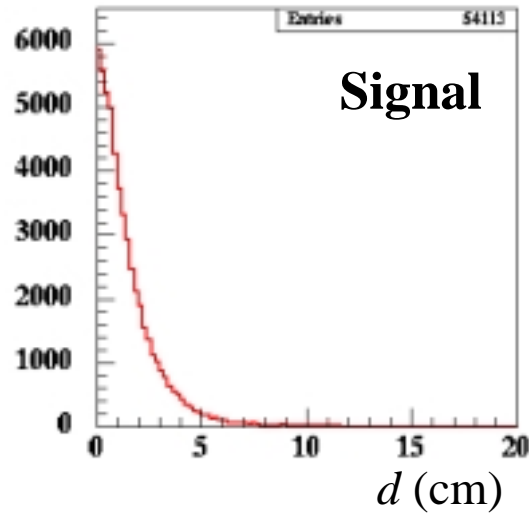
Double tags



Not explicitly in  
expression for BR  
Enters via  $(1-\rho)$



# Track residual cut

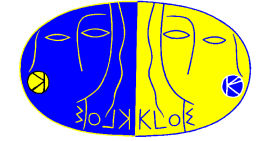


Important for cleaning events

No background rejection

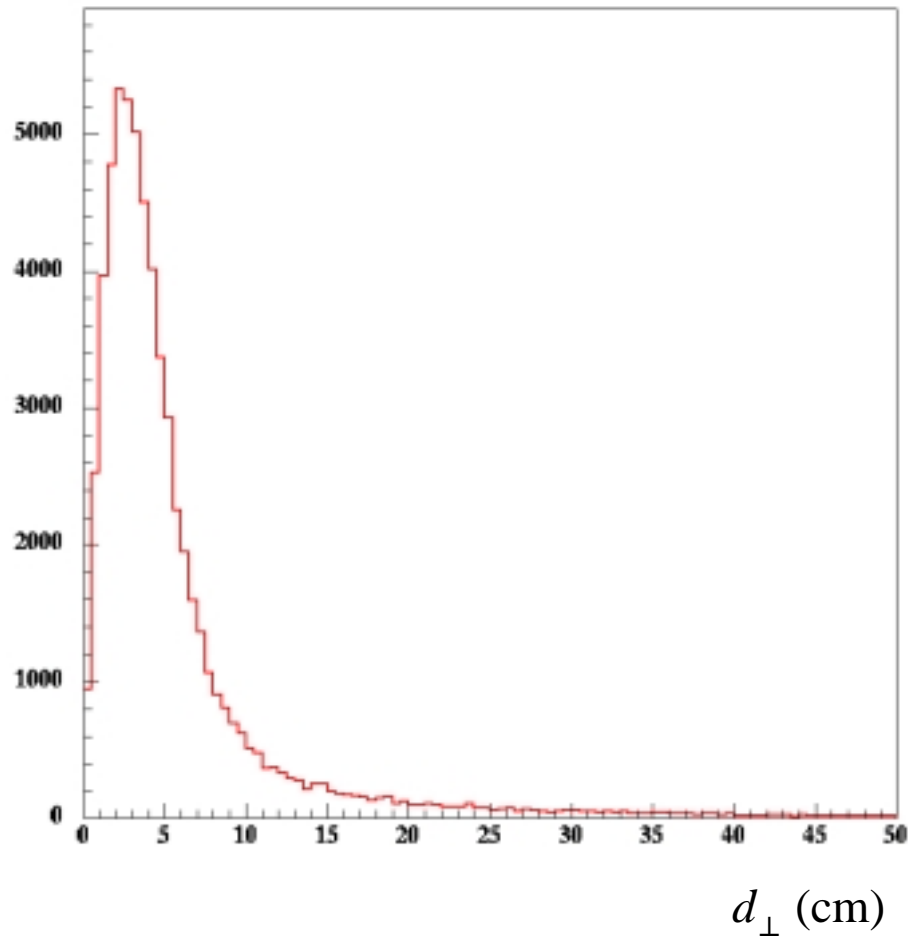
Cut placed at 10 cm



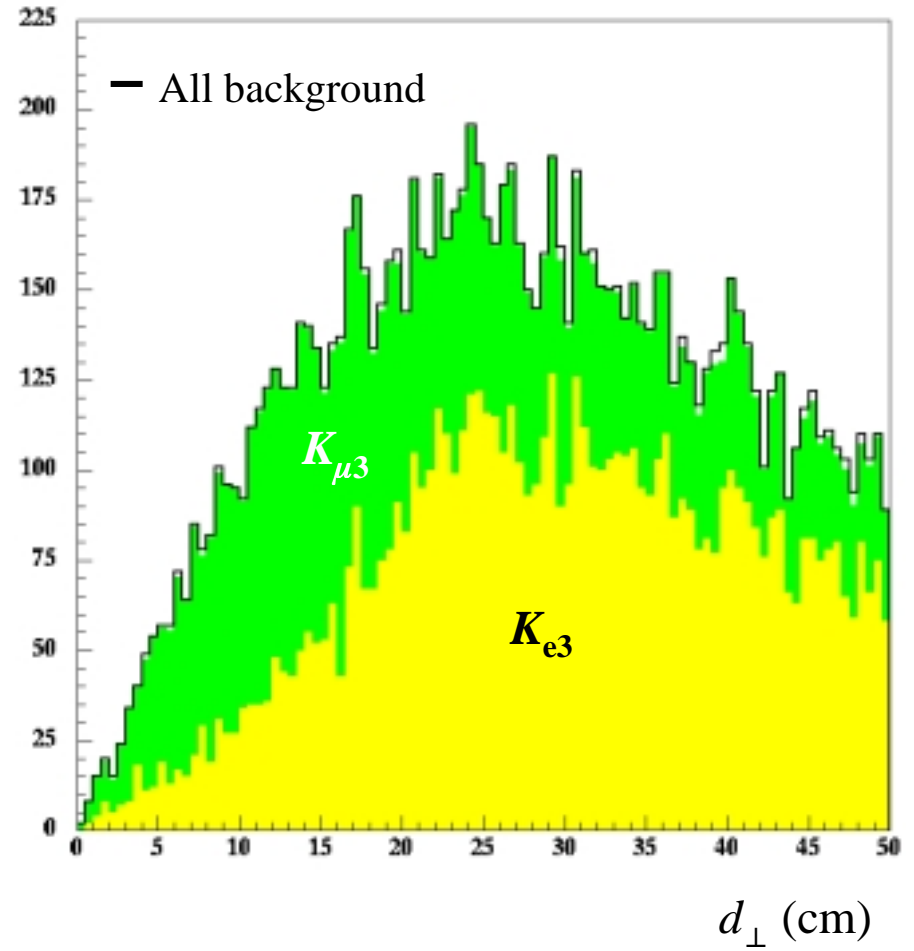


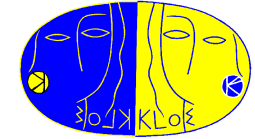
# Cluster residual cut

## Signal



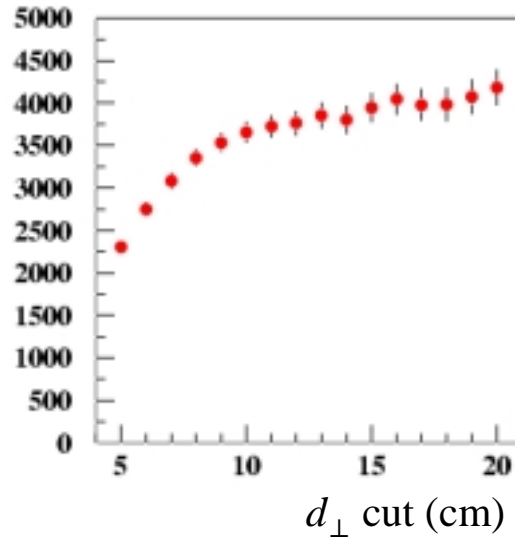
## Background



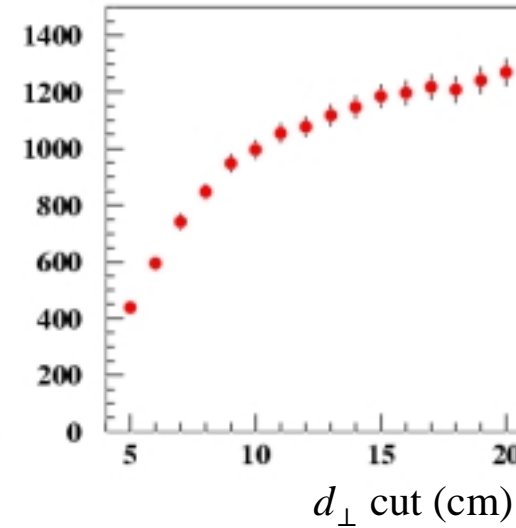


# Optimization of cluster residual cut

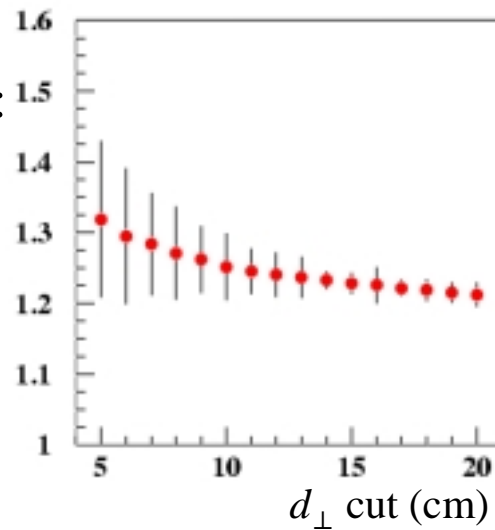
Single tags  
from fit with  
error from  $S/B$



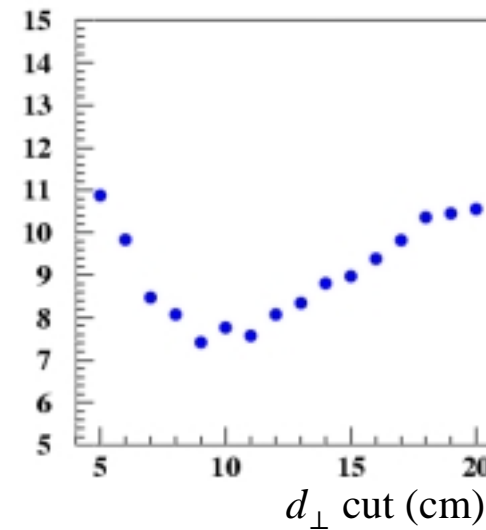
Double tags  
from fit

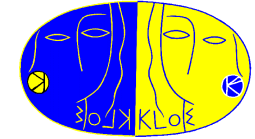


Correlation  $(1-\rho)$ :  
Error includes  
systematic as  
estimated from  
 $\varepsilon_1(\text{MC}) \Leftrightarrow \varepsilon_1(\text{tag})$



**Overall error on  
signal counts**





# Time of flight

$\Delta\text{TOF} =$

$$T_{\text{cl}} - \frac{L_{\text{KL}}}{c\beta(p_{\text{KLtag}})} - \frac{L_{\text{proj}}}{c\beta(p_{\text{proj}})} - 0.42 \text{ ns}$$

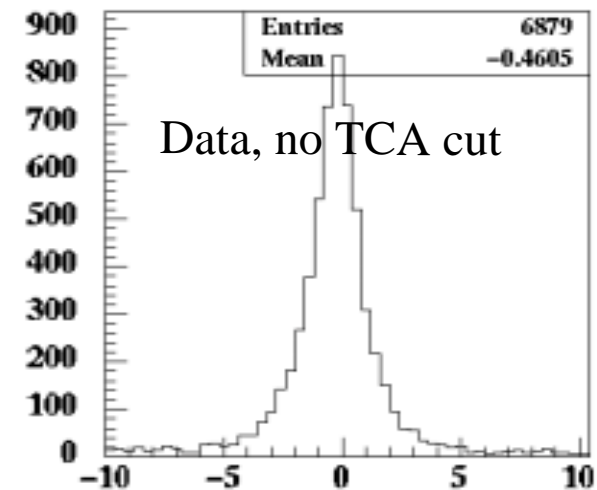
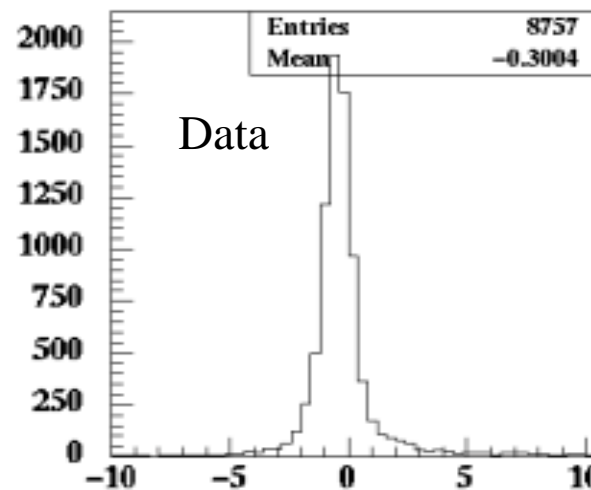
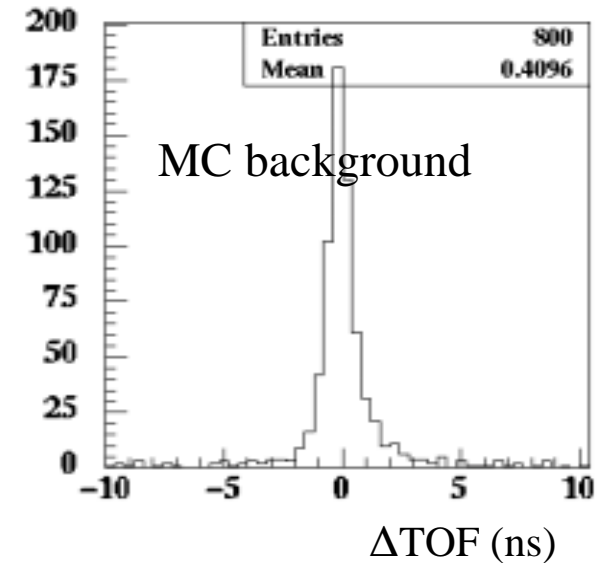
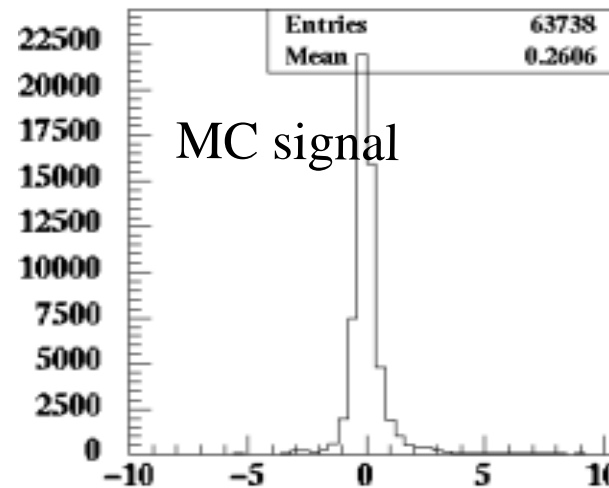
No rejection power beyond cluster distance cut

Loose cut applied at 2.5 ns  
Slewing correction undone, but not in these plots

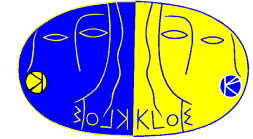
$E/p$  also explored, no help

Can only eliminate background from  $e$  (not  $\mu$ ,  $\pi$ )

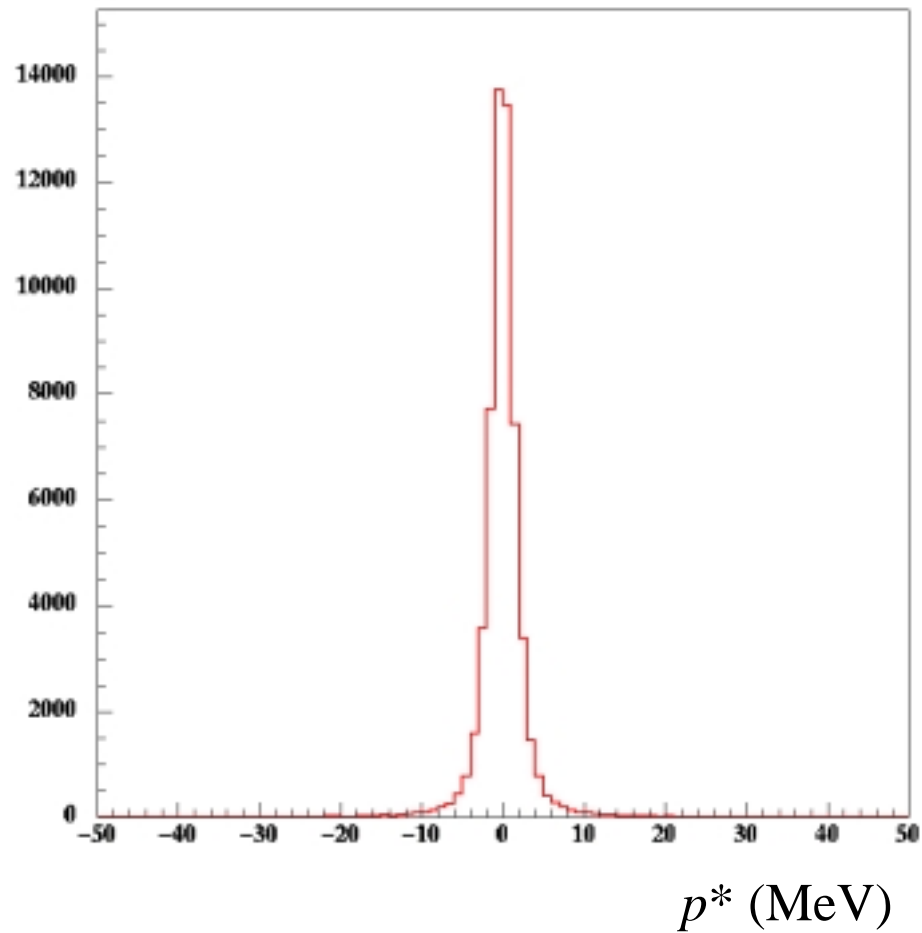
$K_{e3}$  less than 50% of background



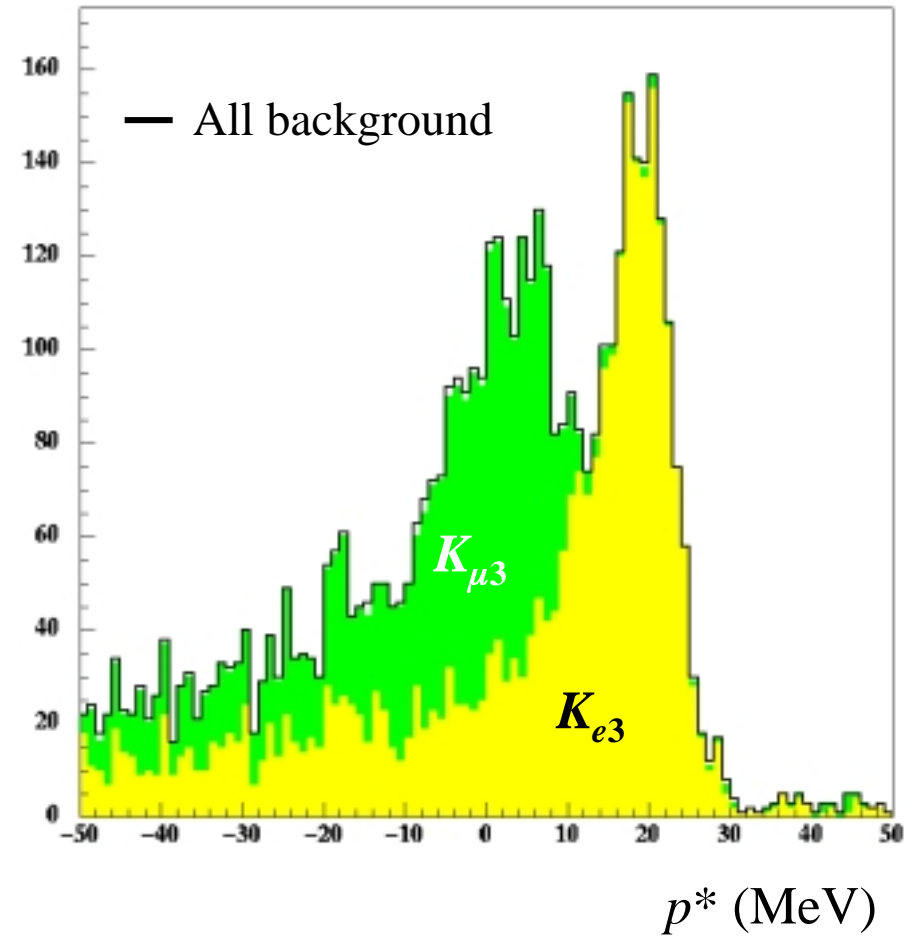
# Single tag $p^*$ spectra



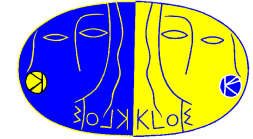
Signal ( $\sim 210 \text{ pb}^{-1}$ )



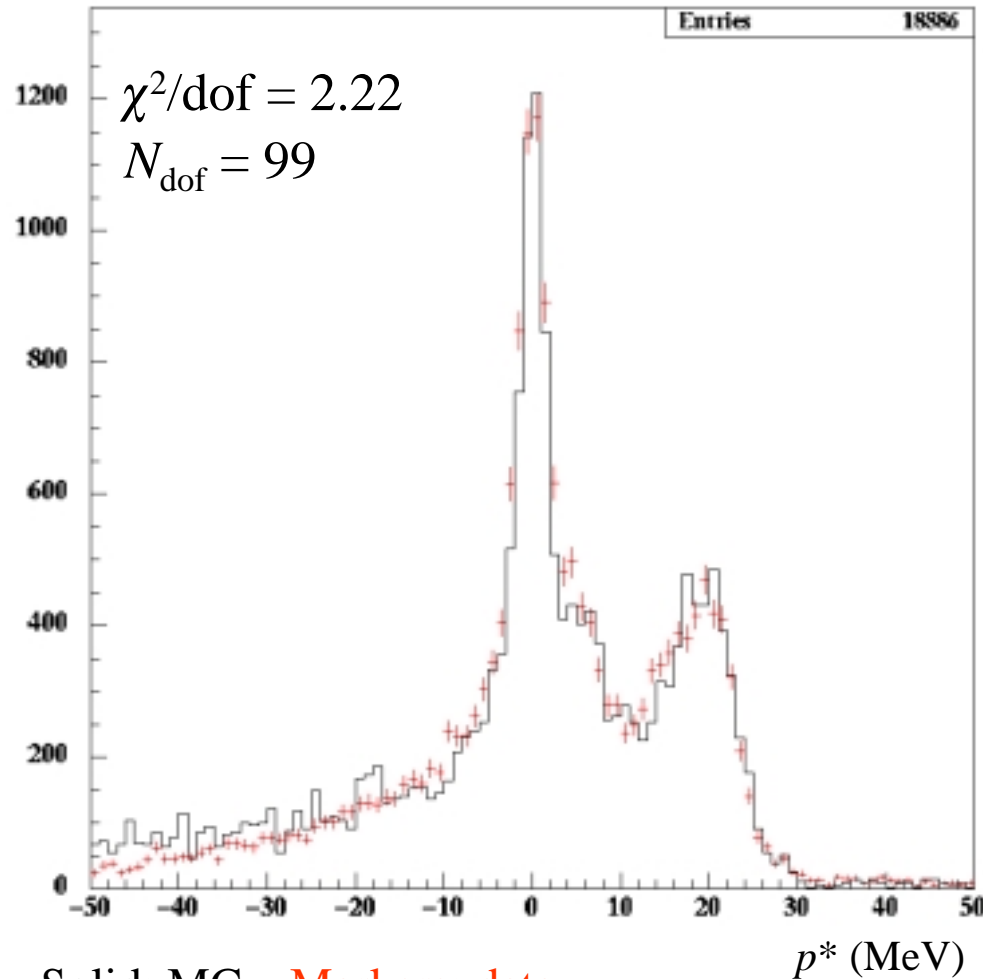
Background ( $\sim 4.6 \text{ pb}^{-1}$ )



# Analysis of single-tag $p^*$ spectrum



MC signal + background, norm  $|p^*| < 50$  MeV



Solid: MC    Markers: data

MC roughly reproduces  $p^*$  spectrum  
Resolution underestimated  
Background overestimated at low  $p^*$

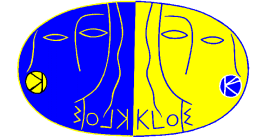
Signal extraction by HMCMLL fit to  
MC signal  
MC background  
 $S$ ,  $B$  fit parameters  
Optional Gaussian convolution

Statistical error includes MC statistics

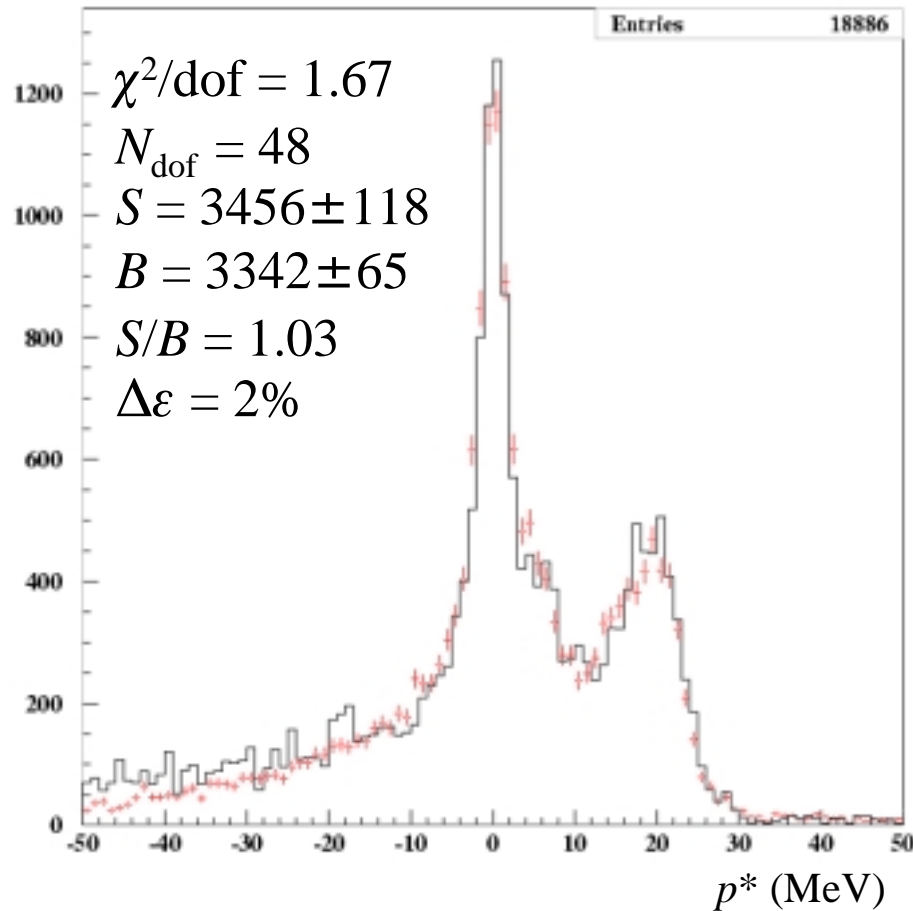
Fit region:  $|p^*| < 25$  MeV

Signal region:  $|p^*| < 5$  MeV

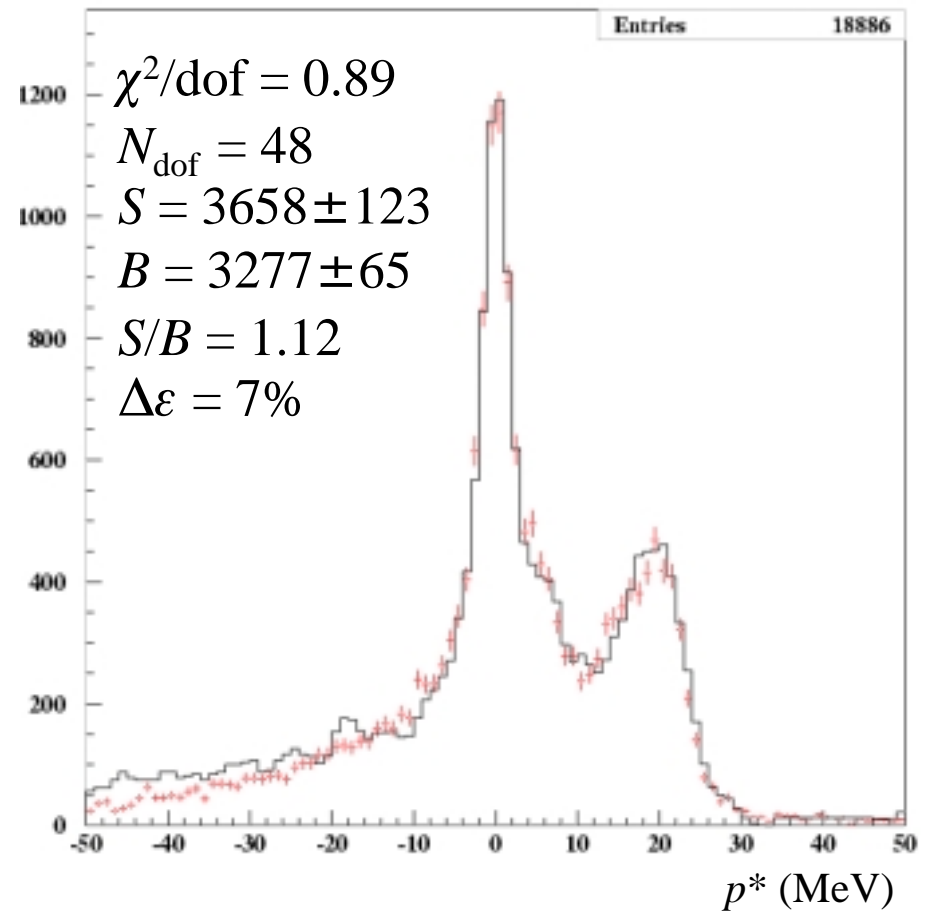
# Effect of smearing MC distributions



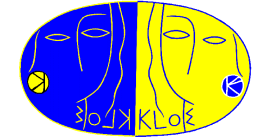
## No convolution



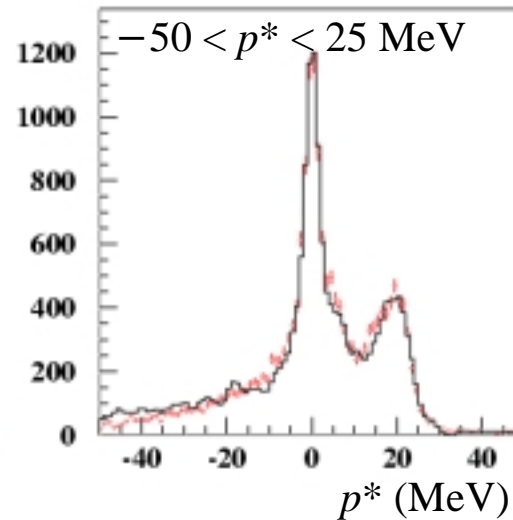
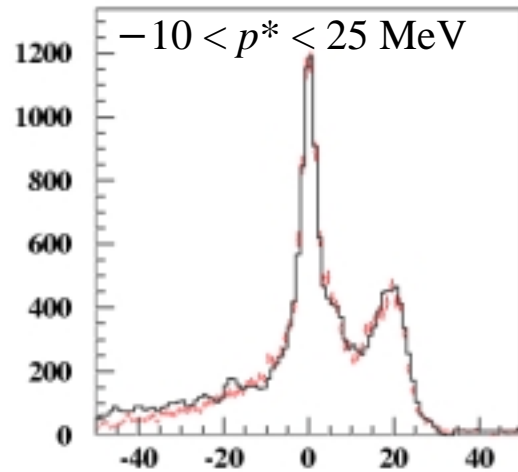
## Convolution, $\sigma = 0.7$ MeV



Solid: fit    Markers: data    Fit interval:  $|p^*| < 25$  MeV    Signal region:  $|p^*| < 5$  MeV



# Single tag fit systematics



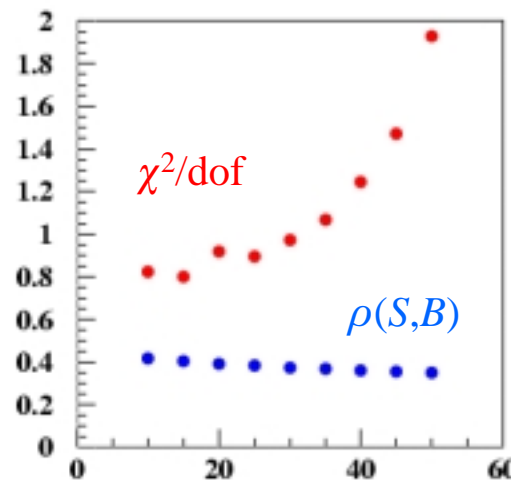
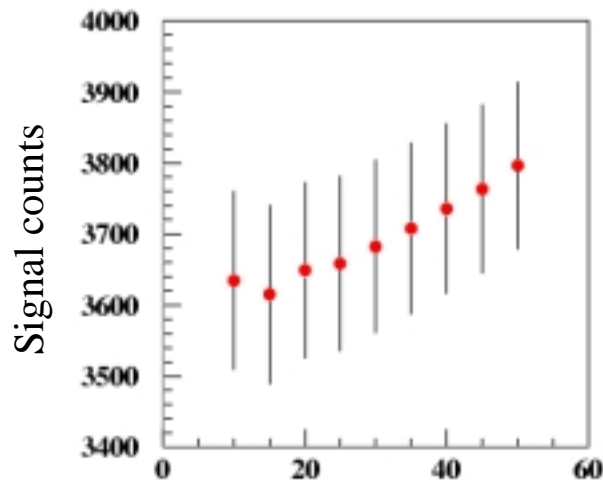
## Fit interval:

Upper bound  $p^* = 25$  MeV

Lower bound  $-10 \rightarrow -35$  MeV

**2.0% effect on  $S$**

$\chi^2/\text{dof}$  blows up for broader range



## Shape agreement:

Explored effect of varying  $\sigma$

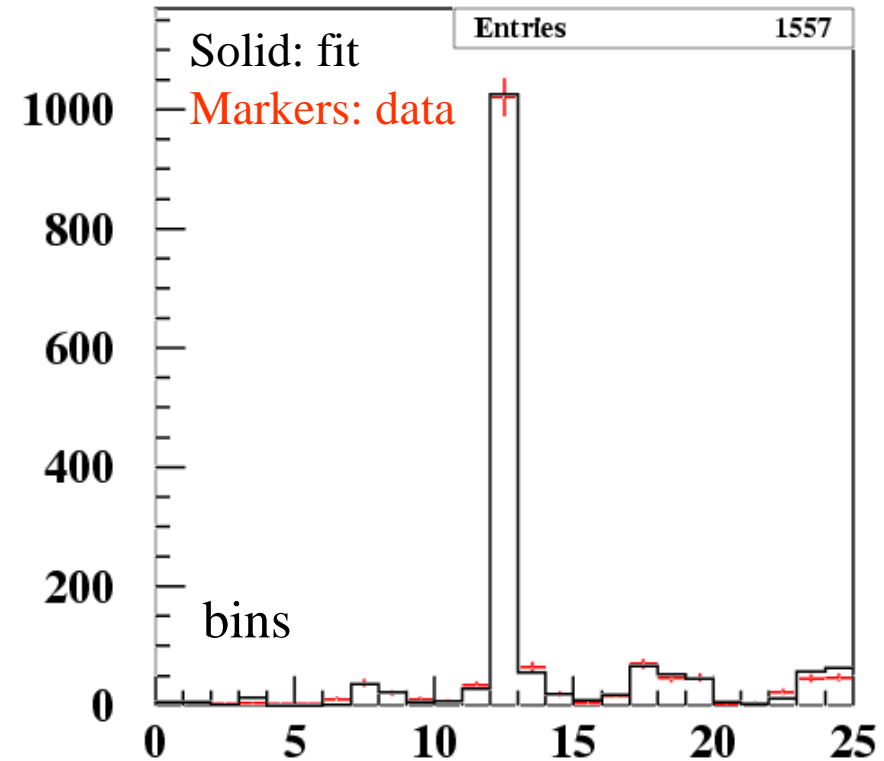
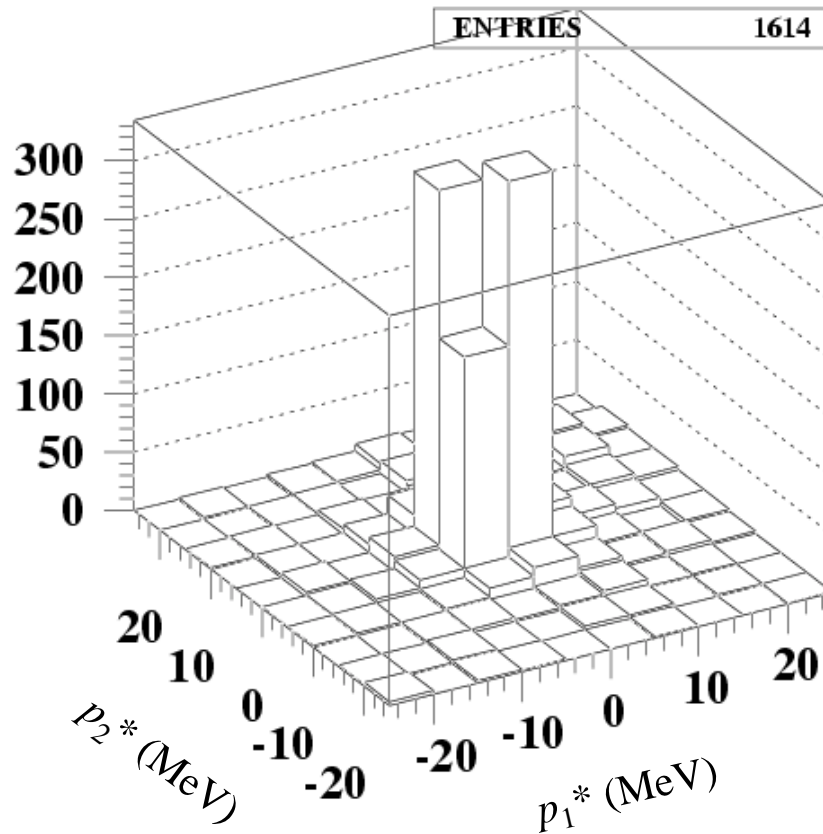
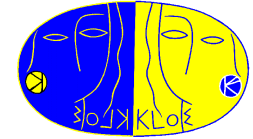
With  $\sigma$  a free parameter

Some probs. with convergence

$\sigma \rightarrow 0.94$  MeV, **3.0% effect on  $S$**

fit lower bound (upper bound  $p^* = 25$  MeV)

# Analysis of double-tag $p^*$ spectrum



Fit analogous to single-tag fit  
No convolution performed

$$S = 996 \pm 34$$

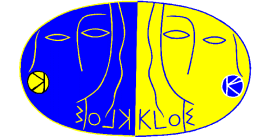
$$B = 29 \pm 3$$

$$S/B = 34.7$$

$$\chi^2/\text{dof} = 0.49$$

$$N_{\text{dof}} = 23$$





# MC efficiencies and correlation

---

## MC signal sample:

57369  $K_L \rightarrow \pi^+\pi^-$  decays in FV

**53729 single tags**

**15839 double tags**

## Tagging efficiency:

$$\begin{aligned}\varepsilon_1 &= N_1/2N_{\text{KLFV}} \\ &= 0.468 \pm 0.002\end{aligned}$$

$$\begin{aligned}\varepsilon_2 &= N_2/N_{\text{KLFV}} \\ &= 0.276 \pm 0.002\end{aligned}$$

## Correlation:

$$\begin{aligned}1-\rho &= \varepsilon_2/\varepsilon_1^2 \\ &= \mathbf{1.259 \pm 0.012}\end{aligned}$$

## Cross checks:

Tagging efficiency from “data”

$$\varepsilon_1 = 2N_2/N_1(1-\rho)$$

$$0.433 \pm 0.019$$

Conditional tag efficiency:

$$R_{21} = 2N_2/N_1 = \varepsilon_1(1-\rho)$$

$$0.590 \pm 0.003 \quad \text{MC}$$

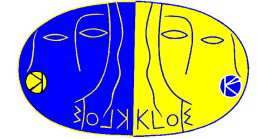
$$0.545 \pm 0.006 \quad \text{Data}$$

**Safe systematic error on  $(1-\rho)$ :**

50% of difference in  $R_{21}$  (3.8%)

---

# Preliminary estimate of $\text{BR}(K_L \rightarrow \pi^+ \pi^-)$



*Summary (stat. error only):*

$$N_1 = 3658 \pm 123 \quad (210 \text{ datarec pb})$$

$$N_2 = 996 \pm 34 \quad (57 \text{ datarec pb})$$

$$1 - \rho = 1.259 \pm 0.012$$

$$\varepsilon_{\text{tag}} = 2N_2/N_1(1 - \rho) = 0.433 \pm 0.019$$

$$N_{\pi^+\pi^-} = N_1/2\varepsilon_{\text{tag}} = 4226 \pm 287$$

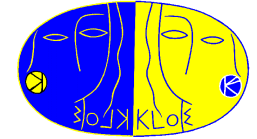
$$N_{KS} = 7441626$$

$$\varepsilon_{\text{FV}} = 0.2653 \pm 0.0009$$

$$f = 0.945 \pm 0.002$$

Single tag	6.7%
Double tag	3.4%
Sample correlation	-3.4%
Tag correlation	0.9%
Fiducial volume*	0.3%
<b>Statistical error</b>	<b>6.8%</b>
Conditional track efficiency	3.8%
Tag bias	2.8%
Fit interval	2.0%
Resolution MC/data	3.0%
<b>Systematic error</b>	<b>5.9%</b>
<b>Total error</b>	<b>9.1%</b>

$$\text{BR}(K_L \rightarrow \pi^+ \pi^-) = fN_{\pi^+\pi^-}/N_{KS}\varepsilon_{\text{FV}} = (2.02 \pm 0.19) \times 10^{-3}$$



# Conclusions

---

$\text{BR}(K_L \rightarrow \pi^+\pi^-)$	$(2.02 \pm 0.19) \times 10^{-3}$	<b>KLOE preliminary?</b>
	$(2.056 \pm 0.033) \times 10^{-3}$	<b>PDG 2000</b>

## Prospects for reducing systematic errors:

Fit-related problems tractable

More MC statistics, background from data, work on fit technique

Errors on  $1-\rho, f$  are more difficult but have been conservatively estimated

## Statistical error considerations:

Error scales as  $2\sqrt{(S+2B)} \approx 4\sqrt{S}$

100 pb<sup>-1</sup> = 21000 single tags = 2.8% statistical error

Compare vertex method with kinematic fit, assume error simply  $\sqrt{S}$

17.4 pb<sup>-1</sup> = 2260 events = 2.1% statistical error

100 pb<sup>-1</sup> = 13000 events = 0.9% statistical error

## Recommendation: pursue vertex method without abandoning this approach

Valuable checkpoint

Mature structure for tracking efficiency estimates

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