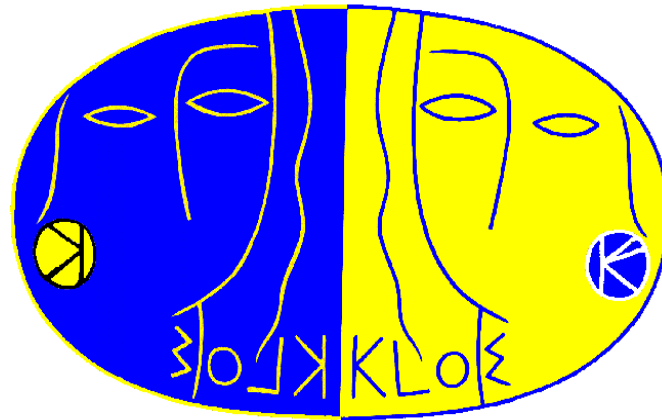




Tests of Chiral Perturbation theory with KLOE



E. De Lucia
INFN Rome

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Chiral Perturbation Theory



Chiral Perturbation Theory (ChPT) is the low-energy effective field theory of strong interactions.

For process involving the s quark \rightarrow SU(3) version of ChPT

Assumptions

- ◆ spontaneous breaking of $SU(3)_L \times SU(3)_R$ symmetry of \mathcal{L}_{QCD} in the chiral limit \Rightarrow $q\bar{q}$ condensate
- ◆ Goldstone modes \Rightarrow octet of pseudoscalar mesons (π, K, η)

Chiral Perturbation Theory



SU(3) version of ChPT

- ✓ write the Chiral Lagrangian in terms of the Goldstone boson fields
- ✓ add the soft breakings terms induced by the quark masses

Lagrangian not renormalizable + infinite number of arbitrary constants

low energy limit

expansion up to a given order in powers of pseudoscalar momenta and quark masses

finite number of constants to be determined experimentally

Testing ChPT with kaons



Since their discovery K mesons have represented one of the most powerful sources of information on fundamental interactions.

In the framework of ChPT kaon decays play a twofold role:

- **semileptonic decays** allow us to investigate the strong sector of the chiral Lagrangian

low energy coupling constants are known



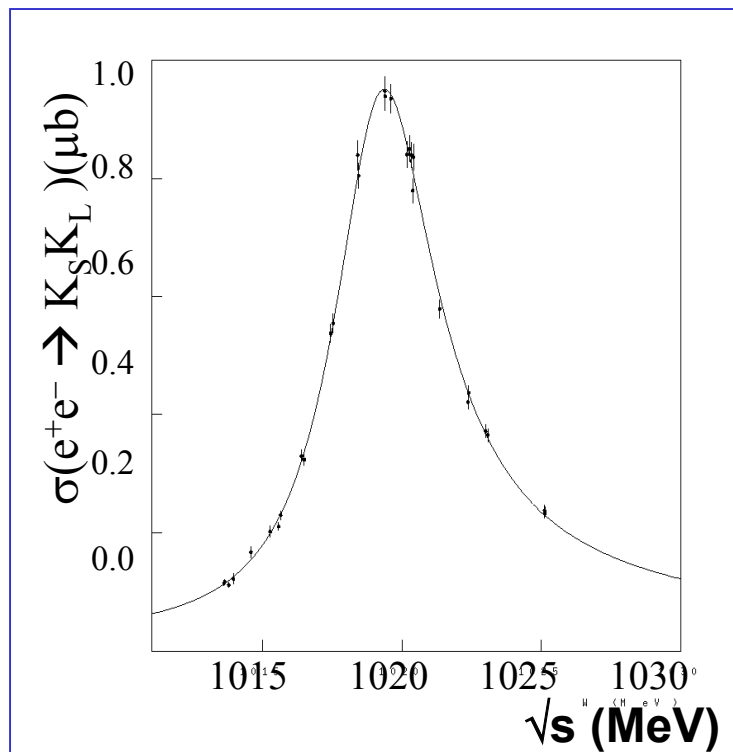
precise & interesting tests of the theory

- **non-leptonic and radiative non-leptonic decays** allow us to investigate the chiral realization of the four-quark effective hamiltonian for weak interactions

Kaon Physics at the ϕ - factory DAΦNE



$$e^+e^- \rightarrow \phi(1020)$$



ϕ decays:

$$BR(\phi \rightarrow K^+K^-) = 49.2\%$$

$$BR(\phi \rightarrow K^0\bar{K}^0) = 33.8\%$$

$$BR(\phi \rightarrow \rho\pi) = 15.4\%$$

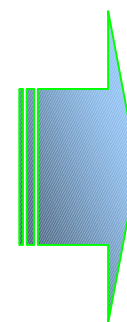
$$BR(\phi \rightarrow \eta\gamma) = 1.3\%$$

$$\vec{P}_\Phi = \vec{P}_K + \vec{P}_{\bar{K}}$$

$$P_{K0} \approx 110 \text{ MeV}/c$$

$$P_{K\pm} \approx 125 \text{ MeV}/c$$

- ♦ very clean environment
- ♦ pure $K_S K_L$ and $K^+ K^-$ beams
almost monochromatic ($P_\phi \approx 13 \text{ MeV}/c$)
- ♦ kaon momentum precisely known
thanks to kinematics enclosure of the event

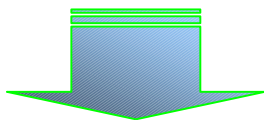


tagging

The tagging

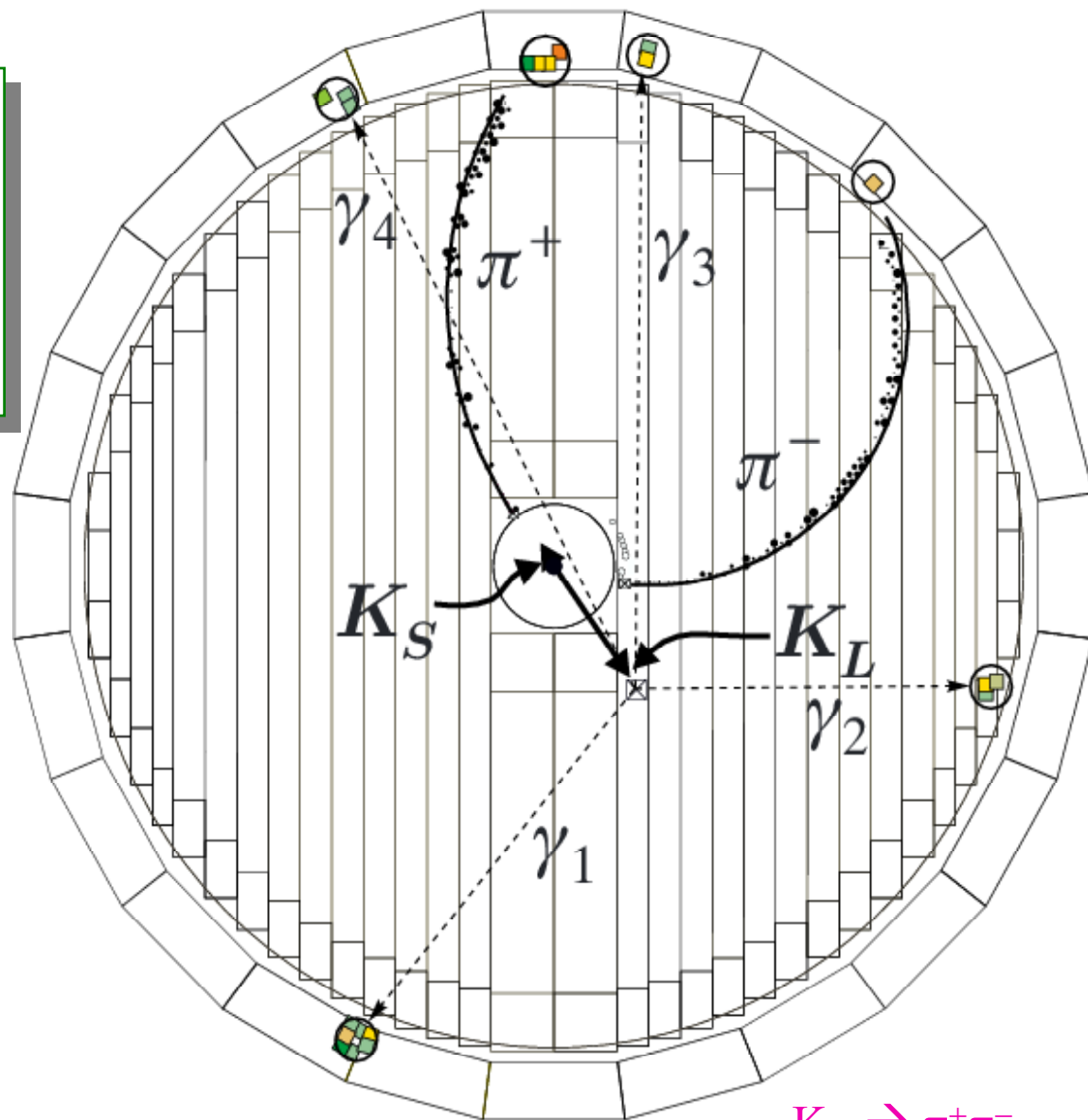


Neutral kaons are produced in a pure quantum state ($J^{PC}=1^{--}$):



detection of a K_S (K_L) guarantees the presence of a K_L (K_S) with known momentum and direction

and the same stands for $K^+ K^-$



$$K_S \rightarrow \pi^+ \pi^-$$

$$K_L \rightarrow \pi^0 \pi^0$$

The KLOE detector



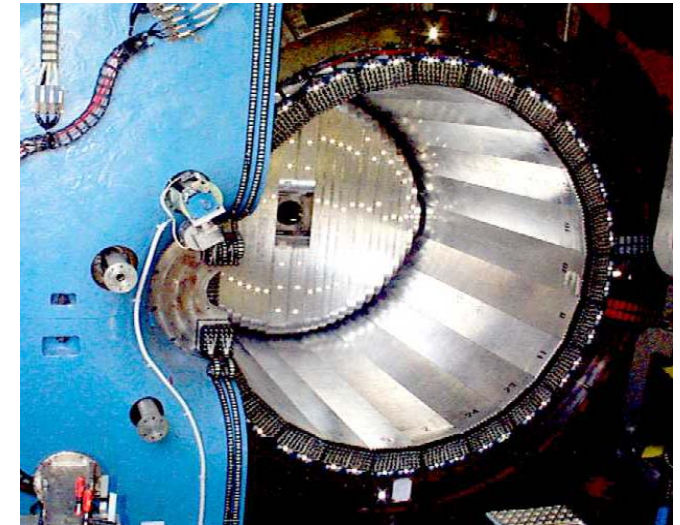
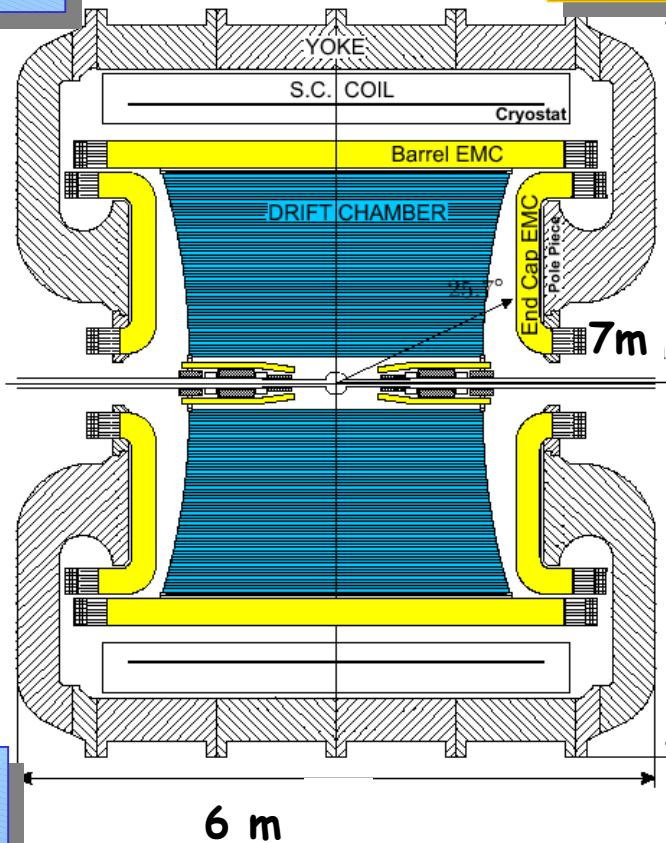
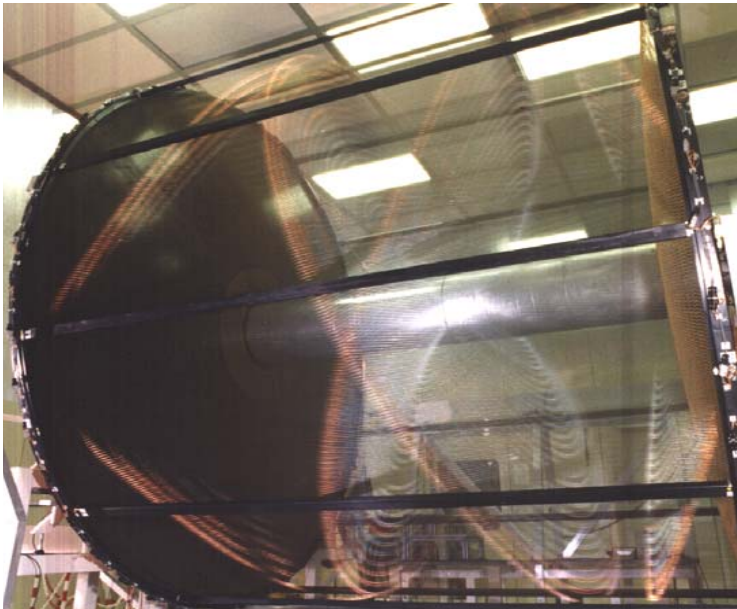
Drift Chamber

- 4 m diameter × 3.3 m length
- 90% helium, 10% isobutane
- 12582/52140 sense/tot wires
- All-stereo geometry

$$\begin{aligned}\lambda_S &= 0.6 \text{ cm} \\ \lambda_L &= 340 \text{ cm} \\ \lambda_{\pm} &= 95 \text{ cm}\end{aligned}$$

Electromagnetic Calorimeter

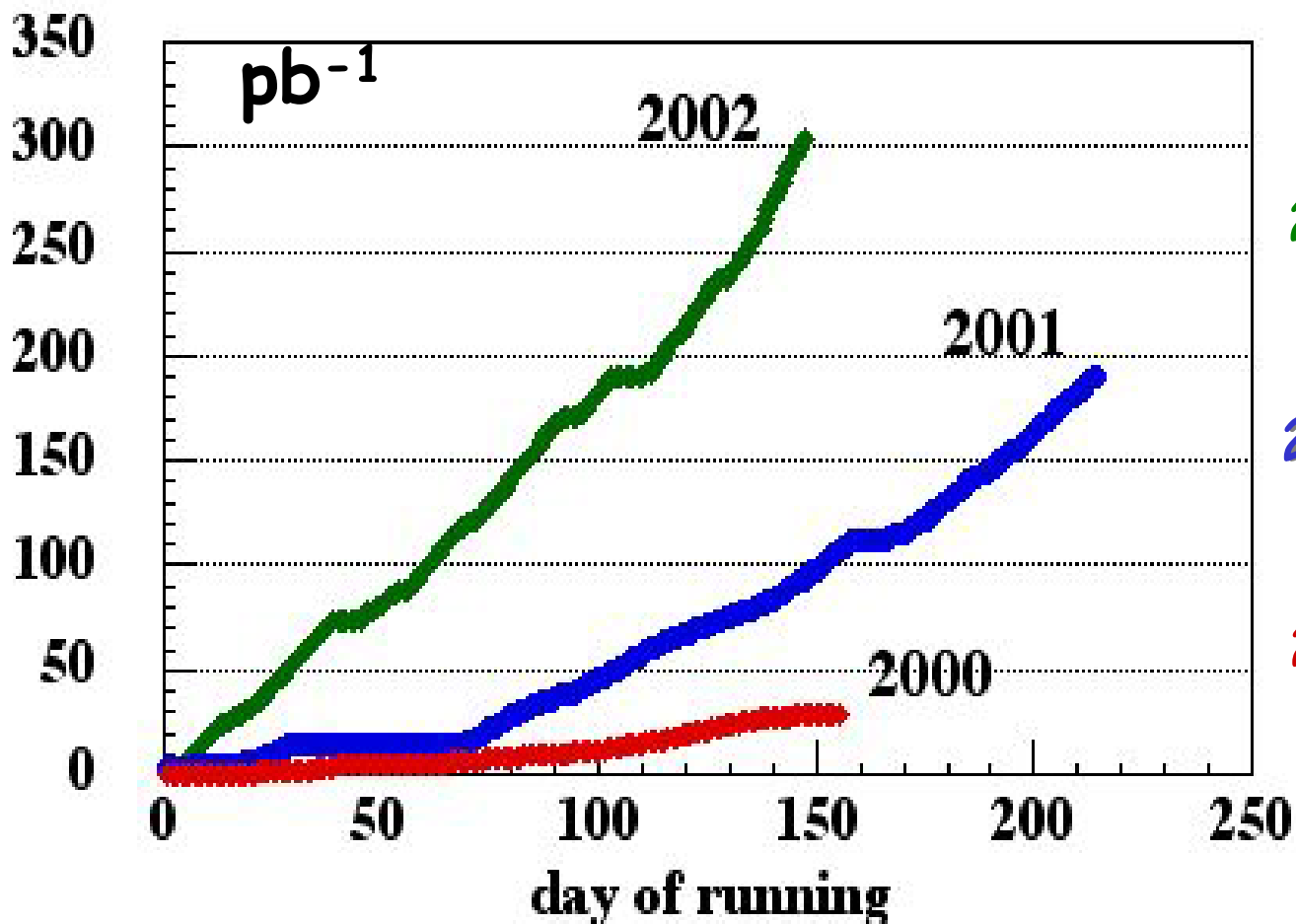
- Lead/scintillating fiber
- 98% coverage of solid angle
- 88 modules (barrel + end-caps)
- 4880 PMTs (two side read-out)



$$\begin{aligned}\sigma_{r\phi} &= 150 \text{ mm} & \sigma_z &= 2 \text{ mm} \\ \sigma_V &= 3 \text{ mm} & \sigma_p/p &= 0.4 \%\end{aligned}$$

$$\begin{aligned}\sigma_E/E &= 5.4\% / \sqrt{E(\text{GeV})} \\ \sigma_T &= 54 \text{ ps} / \sqrt{E(\text{GeV})} \\ &\oplus 50 \text{ ps(cal)}\end{aligned}$$

KLOE Integrated Luminosity



2002 (300 pb⁻¹ → 9 × 10⁸ φ)
analysis in progress

2001 (190 pb⁻¹ → 5.7 × 10⁸ φ)
analysis in progress

2000 (20 pb⁻¹ → 7.5 × 10⁷ φ)
published results

1.5 × 10⁶ K⁺K⁻/pb⁻¹

10⁶ K_LK_S/pb⁻¹

The KLOE physics program



2000 statistics:

K_S physics :

$$\text{BR}(K_S \rightarrow \pi^+\pi^-(\gamma))/\text{BR}(K_S \rightarrow \pi^0\pi^0)$$

$$\text{BR}(K_S \rightarrow \pi e \nu)$$

ϕ radiative decays

$$\phi \rightarrow f_0\gamma, a_0\gamma$$

$$\phi \rightarrow \eta'\gamma, \eta\gamma$$

$O(20 \text{ pb}^{-1})$
✓ first publications

2001+2002 statistics:

- rare $K \rightarrow \gamma\gamma$
- K^\pm decays
- $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ via ISR
- η decays

$O(500 \text{ pb}^{-1})$

on tape analysis progress

- ε'/ε via double ratio
- Semileptonic asymmetry (CPT test)
- $K_L K_S$ Interferometry



Outline



Among the various tests of ChPT accessible at KLOE
I will focus on:

1) $\Gamma(K_S \rightarrow \pi^+\pi^- (\gamma))/\Gamma(K_S \rightarrow \pi^0\pi^0)$

Isospin (I=0 and 2) amplitudes and the $\pi\pi$ phase-shifts

2) $\text{Br}(K_L \rightarrow \gamma\gamma) / \text{Br}(K_L \rightarrow 3\pi^0)$

high order corrections in ChPT and theoretical prediction of $K_L \rightarrow \mu^+\mu^-$

3) K_{I3} decays

BR's , kaon form factors and V_{us} for charged and neutral kaons

4) K_{I4} decays

phase shift of the $\pi\pi$ elastic scattering and strength of the condensate

5) $\eta \rightarrow \pi^0\gamma\gamma$

high order corrections in ChPT

$q\bar{q}$



$$1) \Gamma(K_S \rightarrow \pi^+ \pi^- (\gamma)) / \Gamma(K_S \rightarrow \pi^0 \pi^0)$$

K_S analysis at KLOE

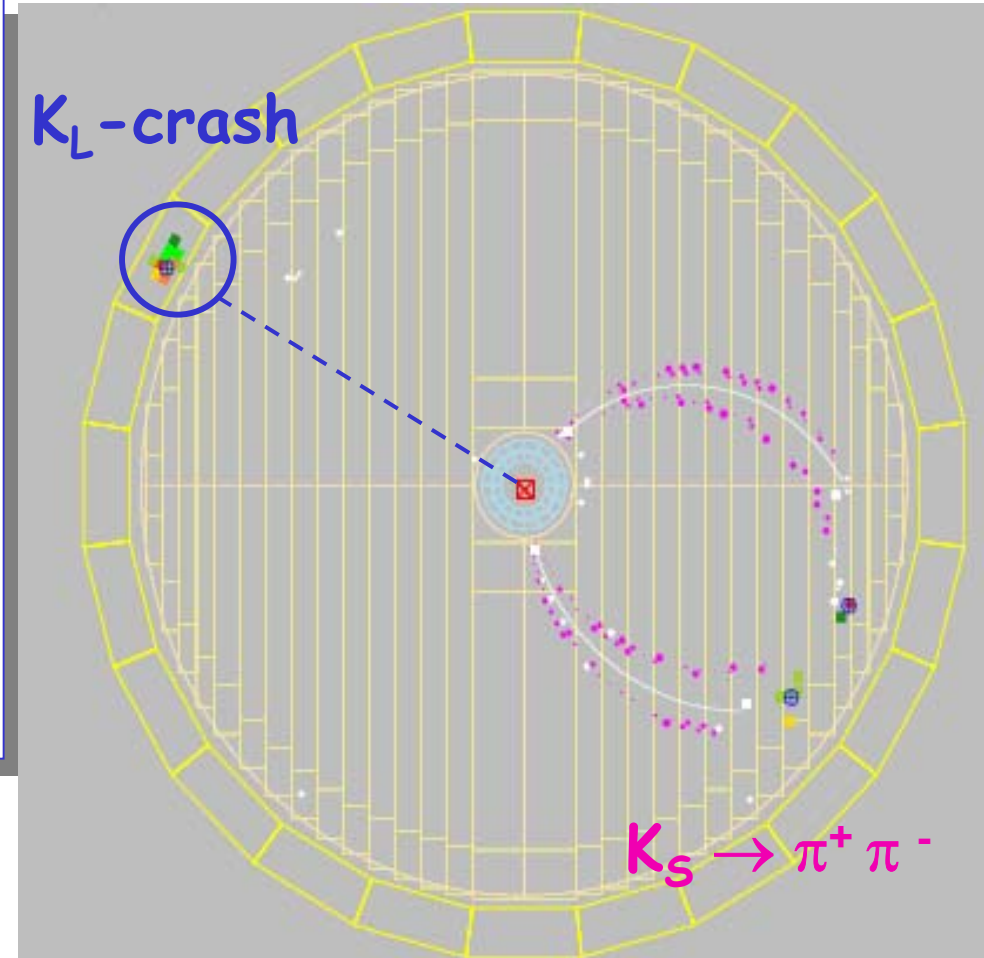


K_S tagging

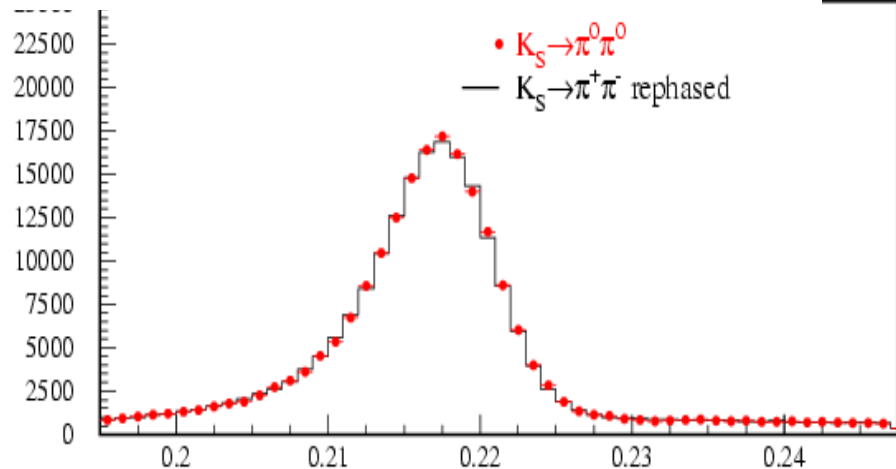
- time of flight identification of K_L interacting in the EmC (“ K_L -crash”)
- selected as a calorimeter cluster with:
 - $E_{CLU} > 200 \text{ MeV}$
 - $|\cos(\theta_{CLU})| < 0.7$
 - $0.195 \leq \beta^* \leq 0.2475$

(β^* = K_L velocity in the ϕ rest frame)

K_L -crash



β^* distribution of “ K_L -crash”



- ❖ K_S momentum from K_L cluster position
- ❖ Tagging efficiency $\epsilon_{\text{tag, total}} \sim 30\%$



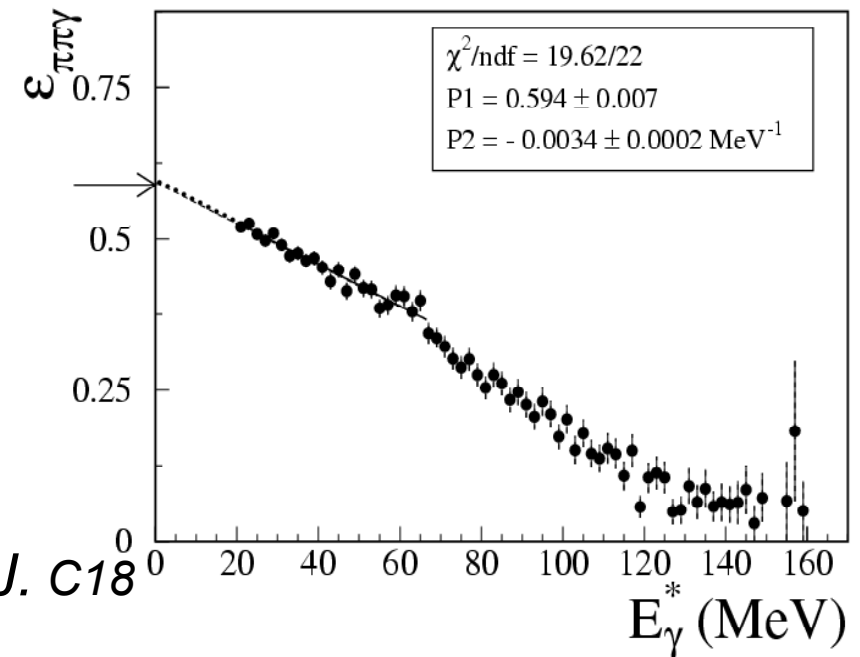
$$\Gamma(K_S \rightarrow \pi^+ \pi^- (\gamma)) / \Gamma(K_S \rightarrow \pi^0 \pi^0)$$

Motivations

first step towards $\text{Re}(\varepsilon'/\varepsilon)$ and extraction of Isospin 0 and 2 amplitudes and phases from consistent treatment of soft γ in $K_S \rightarrow \pi^+ \pi^- (\gamma)$

$K_S \rightarrow \pi^+ \pi^- (\gamma)$ selection

- ◆ K_L -crash
- ◆ 2 tracks from IP reaching EMC(*) and acceptance cuts
- ◆ no γ required in EMC
 \Rightarrow **fully inclusive measurement**
- ◆ $\varepsilon_{\pi\pi(\gamma)}(E_\gamma^*)$ from MC folded to theoretical γ spectrum from *Cirigliano et al., Eur. Phys. J. C18*



$K_S \rightarrow \pi^0 \pi^0$ selection

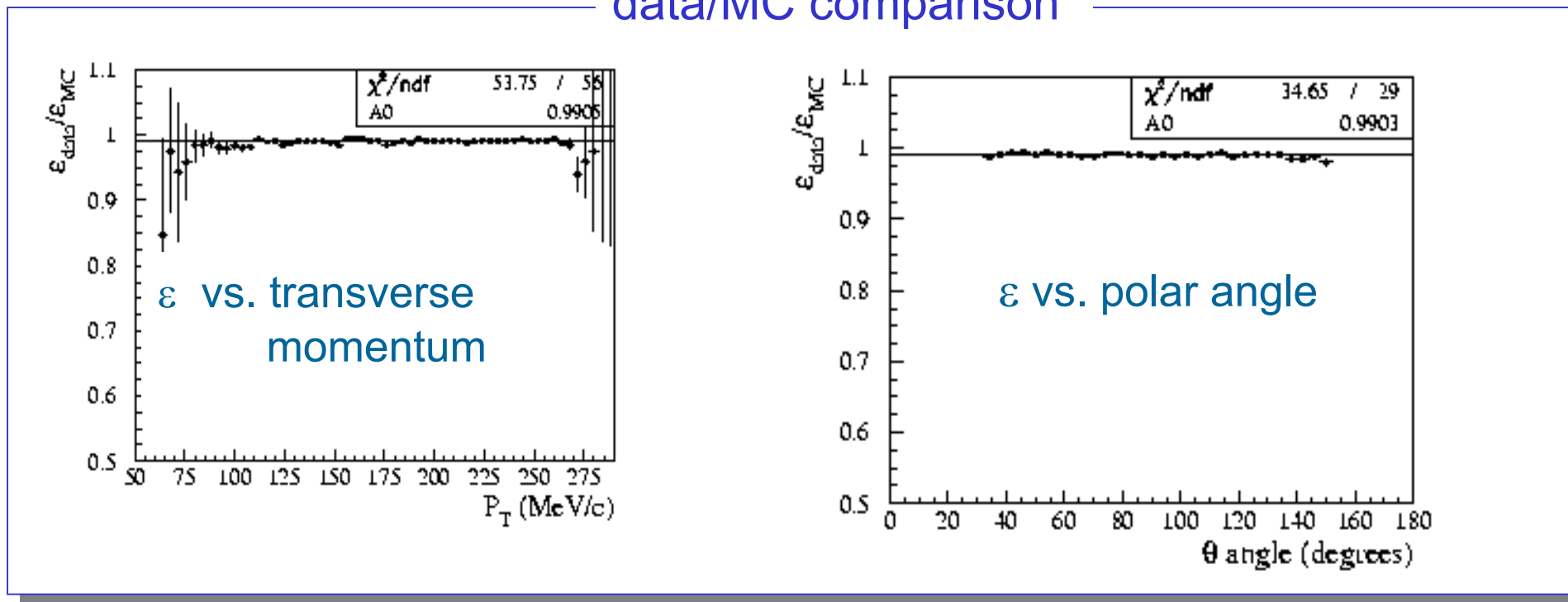
K_L -crash .and. ≥ 3 neutral “prompt” clusters: $|t-R/c| < 5\sigma_+$.and. $E_\gamma > 20 \text{ MeV}$

Efficiency evaluation : $K_S \rightarrow \pi^+ \pi^- (\gamma)$



- **single-track reconstruction efficiency** from $K_S \rightarrow \pi^+ \pi^-$ data, used to scale MC

data/MC comparison



$$\epsilon_{+-} (\text{sel and rec}) = (57.6 \pm 0.2) \%$$

- **single-particle t_0 and trigger efficiencies** from data, plugged into MC

$$\epsilon_{+-} (t_0 \text{ and trig}) = (97.9 \pm 0.03) \%$$

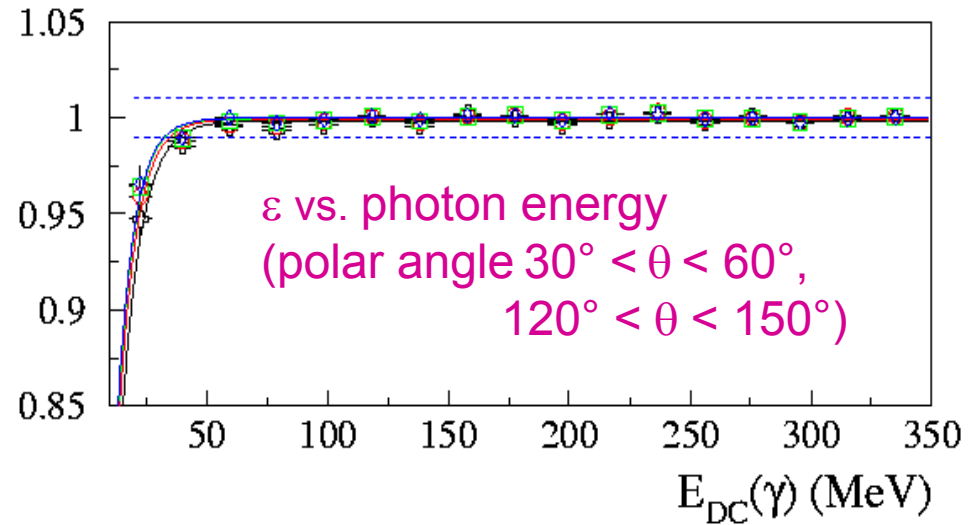
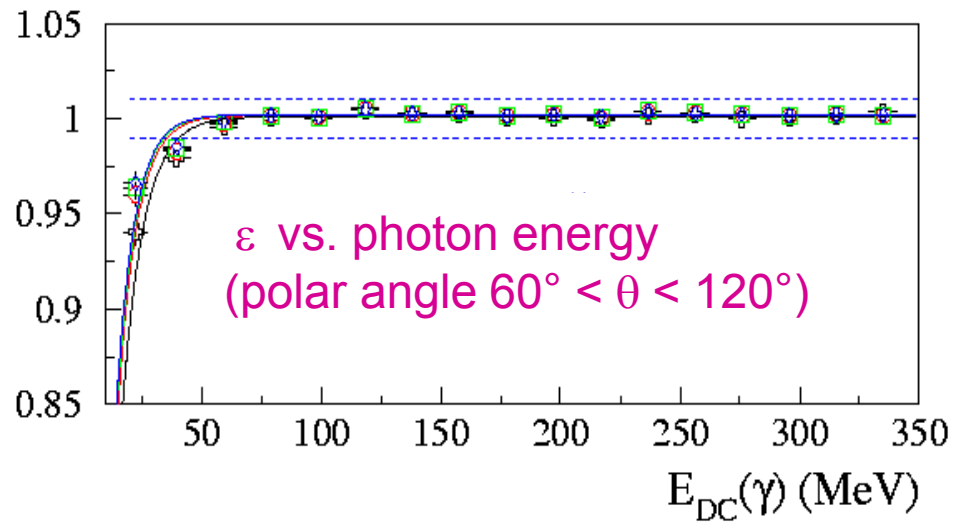
$K_S \rightarrow \pi^+ \pi^-$ from $K_L \rightarrow \pi^+ \pi^- \pi^0$ -tagged sample and $\phi \rightarrow \pi^+ \pi^- \pi^0$

Efficiency evaluation : $K_S \rightarrow \pi^0 \pi^0$



➤ **photon detection efficiency** from data using $\phi \rightarrow \pi^+ \pi^- \pi^0$ events.

data/MC comparison



$$\epsilon_{00}(\text{sel}) = (90.1 \pm 0.2)\%$$

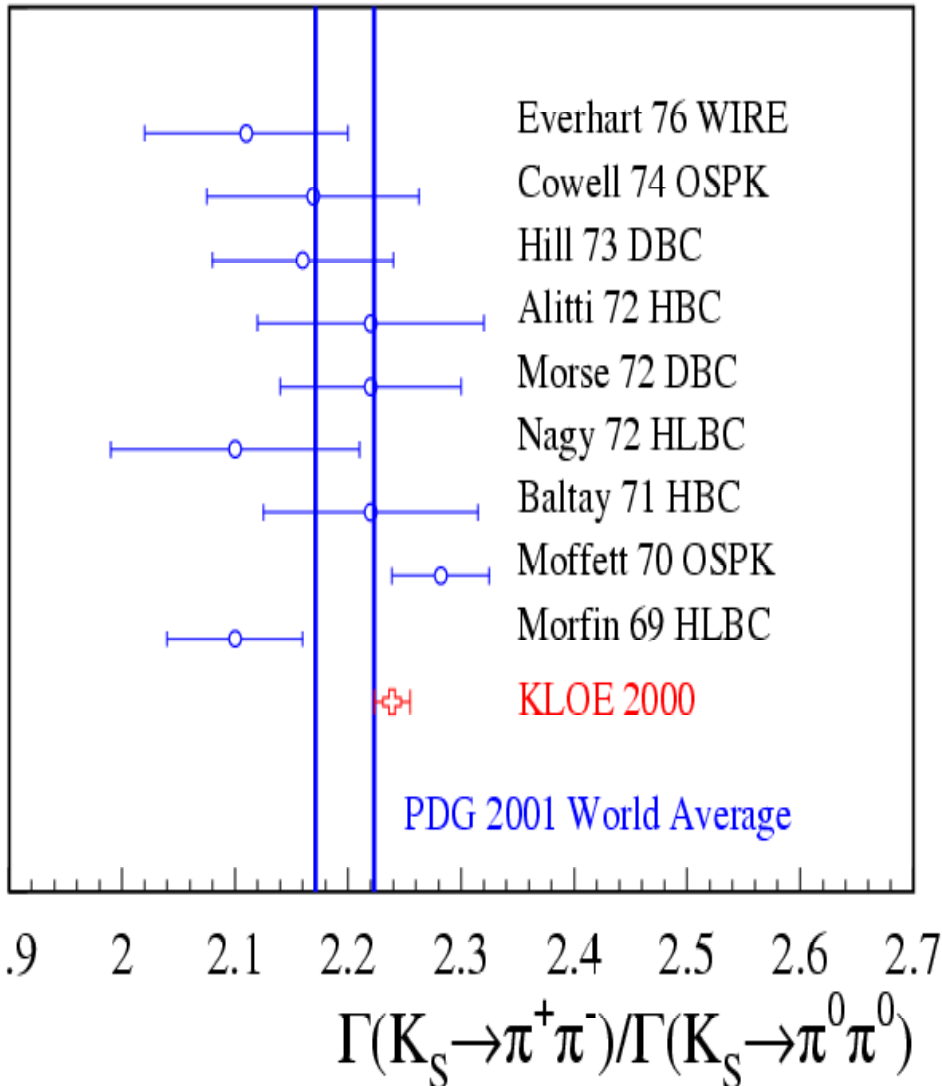
➤ **single-particle t_0 and trigger efficiencies** from data, plugged into MC

$$\epsilon_{00}(t_0 \text{ and trig}) = (99.86 \pm 0.04)\%$$

$K_S \rightarrow \pi^0 \pi^0$ from $K_L \rightarrow \pi^+ \pi^- \pi^0$ -tagged sample



$R = \Gamma(K_S \rightarrow \pi^+ \pi^- (\gamma)) / \Gamma(K_S \rightarrow \pi^0 \pi^0)$ result



KLOE 2000 data *Phys. Lett. B 538 (2002), 21*

$$R = 2.239 \pm 0.003_{\text{stat}} \pm 0.015_{\text{syst}}$$

PDG 2000 average

$$R = 2.197 \pm 0.026$$

(without clear indication of E_γ^*)

Near future goals

- reach 0.1% systematic uncertainty on R
[< 2·10⁻⁴ on Re(ε'/ε)]
- measure absolute branching ratios
- E_γ^* spectrum



$\Gamma(K_S \rightarrow \pi^+ \pi^- (\gamma)) / \Gamma(K_S \rightarrow \pi^0 \pi^0)$ theory

Both the isospin ($I=0$ and 2) amplitudes and the pp phase-shifts can be estimated from the measured $K \rightarrow \pi\pi$ branching ratios:

Transition amplitudes

$$A(K_1 \rightarrow \pi^+ \pi^-) = \sqrt{\frac{2}{3}} A_0 e^{i\delta_0} + \sqrt{\frac{1}{3}} A_2 e^{i\delta_2}$$

$$A(K_1 \rightarrow \pi^0 \pi^0) = \sqrt{\frac{1}{3}} A_0 e^{i\delta_0} - \sqrt{\frac{2}{3}} A_2 e^{i\delta_2}$$

$$A(K^+ \rightarrow \pi^+ \pi^0) = \sqrt{\frac{3}{4}} A_2 e^{i\delta_2}$$

Decay rates

$$\Gamma(\pi^+ \pi^-) = \frac{2}{3} A_0^2 + \frac{1}{3} A_2^2 + \frac{2\sqrt{2}}{3} A_0 A_2 \cos(\delta_0 - \delta_2)$$

$$\Gamma(\pi^0 \pi^0) = \frac{1}{3} A_0^2 + \frac{2}{3} A_2^2 - \frac{2\sqrt{2}}{3} A_0 A_2 \cos(\delta_0 - \delta_2)$$

$$\Gamma(\pi^+ \pi^0) = \frac{3}{2} A_2^2$$

$$K_1 = \frac{|K^0\rangle + |\bar{K}^0\rangle}{\sqrt{2}} \cong K_S$$

$$\left(\frac{A_0}{A_2}\right)^2 = \frac{3\Gamma_S}{4\Gamma^+} - 1 = \frac{3}{4} \frac{1}{\tau_S} \frac{\tau^+}{\text{BR}(K^+ \rightarrow 2\pi)} - 1 = (22.2 \pm 0.07)^2$$

$$R = \frac{\Gamma(K_1 \rightarrow \pi^+ \pi^-)}{\Gamma(K_1 \rightarrow \pi^0 \pi^0)} = \frac{\rho_{\pm}}{\rho_{00}} \left[2 + 6\sqrt{2} \frac{A_2}{A_0} \cos(\delta_0 - \delta_2) \right]$$



$\delta_0 - \delta_2$ situation

1) $O(p^2)$ ChPT prediction

$$\delta_0 - \delta_2 = (45 \pm 6)^\circ$$

2) $\pi\pi$ scattering

$$\delta_0 - \delta_2 = (45.2 \pm 1.3 \pm 1.5)^\circ$$

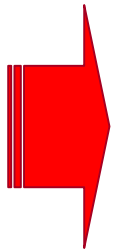
3) BR's from PDG

$$\delta_0 - \delta_2 = (56.7 \pm 3.8)^\circ$$

4) KLOE measurement
of $\Gamma(\mathbf{K}_S \rightarrow \pi^+\pi^-) / \Gamma(\mathbf{K}_S \rightarrow \pi^0\pi^0)$

$$\delta_0 - \delta_2 = (48 \pm 3)^\circ$$

← *inconsistent
with 1) and 2)*



*Using the KLOE measurement the estimate of $\delta_0 - \delta_2$
from $K \rightarrow \pi\pi$ BR's is consistent with 1) and 2)*



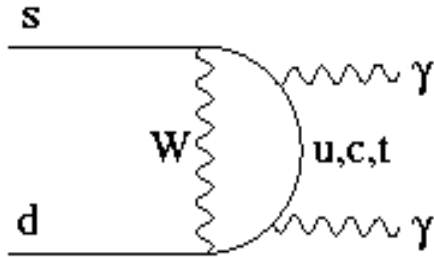
$$2) \quad Br(K_L \rightarrow \gamma\gamma) / Br(K_L \rightarrow 3\pi^0)$$



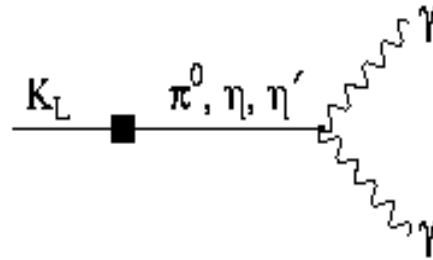
$$K_L \rightarrow \gamma\gamma$$

ChPT

❖ $O(p^6)$ amplitude and long-distance contribution are dominant



Short-distance contribution



Long-distance contribution

very sensitive to chiral corrections, in particular η - η' mixing

❖ prediction of $BR(K_L \rightarrow \mu^+\mu^-)$

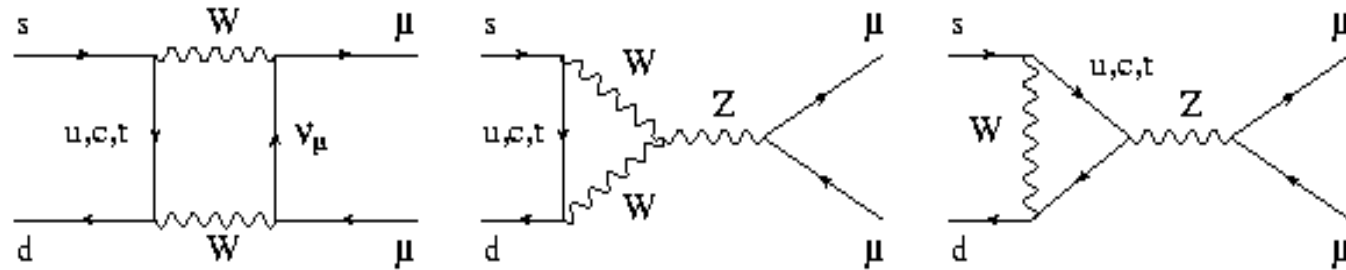
$$BR = |\Im A|^2 + |\Re A|^2$$

$\propto BR(K_L \rightarrow \gamma\gamma)$
model independent

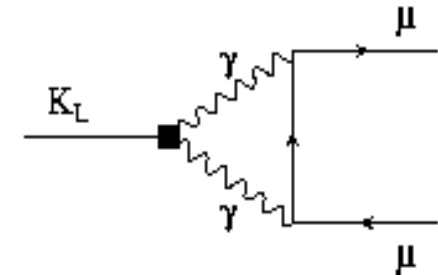
$\propto BR(K_L \rightarrow \gamma\gamma)$
model dependent

$$\Re A_{LONG} + \Re A_{SHORT}$$

dominated by t quark
 \Rightarrow extraction V_{td}



Short-distance contribution



Long-distance contribution

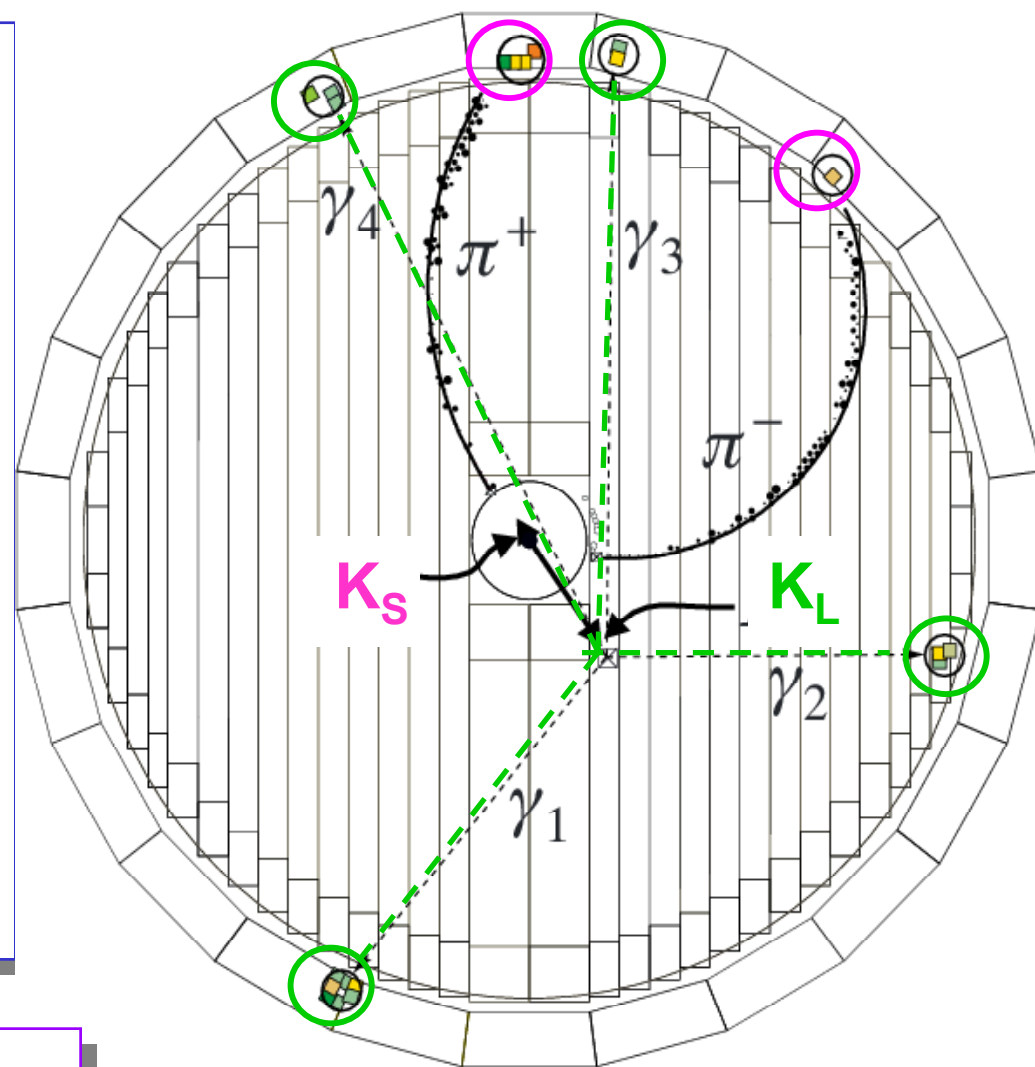
K_L tagging at KLOE



K_L tagging

- ❖ identification of $K_S \rightarrow \pi^+\pi^-$ events
- ❖ single vertex in K_S fiducial volume
 $r_T < 4$ cm and $|z| < 8$ cm
- ❖ two and only two tracks of opposite charge connected to the vertex
- ❖ $50 < p_{K_S} < 170$ MeV/c in ϕ ref. frame
- ❖ $400 < M_{K_S} < 600$ MeV/c²

- ❖ K_L momentum from K_S and ϕ momenta
- ❖ Tagging efficiency $\epsilon_{\text{tag,total}} \sim 75\%$



$$K_L \rightarrow \pi^0 \pi^0$$

$$K_S \rightarrow \pi^+ \pi^-$$

$K_L \rightarrow \gamma\gamma$

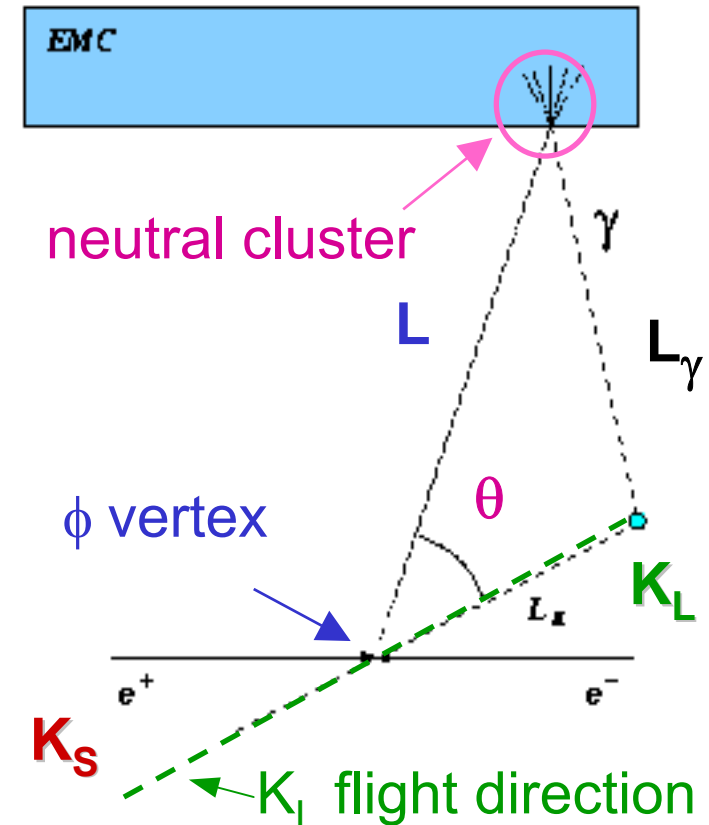


Strateg

- ♦ $BR(K_L \rightarrow \gamma\gamma)$ from $\Gamma(K_L \rightarrow \gamma\gamma) / \Gamma(K_L \rightarrow 3\pi^0)$ ($\Delta BR(K_L \rightarrow 3\pi^0) / BR \sim 1.3\%$)
- ♦ K_L tagging from $K_S \rightarrow \pi^+\pi^-$ events
- ♦ neutral vertex in: $30 < r_T < 170$ cm and $|z| < 140$ cm
- ♦ selection for $K_L \rightarrow \gamma\gamma$ and $K_L \rightarrow 3\pi^0$ events

Neutral vertices reconstructed applying the time of flight triangle to cluster not attached to tracks:

$$\left. \begin{aligned} L^2 + L_K^2 - 2LL_K \cos \theta &= L_\gamma^2 \\ L_K / \beta_K + L_\gamma &= ct_\gamma \end{aligned} \right\} L_K = \frac{\sum_{i=1}^{NCLU} \mathbf{E}_i \cdot \mathbf{l}_{Ki}}{\sum_{i=1}^{NCLU} \mathbf{E}_i}$$



$K_L \rightarrow \gamma\gamma$ selection



- look for a neutral vertex with 2 γ 's attached
- pre-selection to reject the most dangerous background from $K_L \rightarrow 3\pi^0$ events (BR~21%)

$$E_\gamma > 100 \text{ MeV}$$

$$E_{\text{tot}} > 350 \text{ MeV}$$

$$\psi > 160^\circ \quad (2 \gamma\text{'s angle in plane } \perp \text{ to } p_{K_L})$$

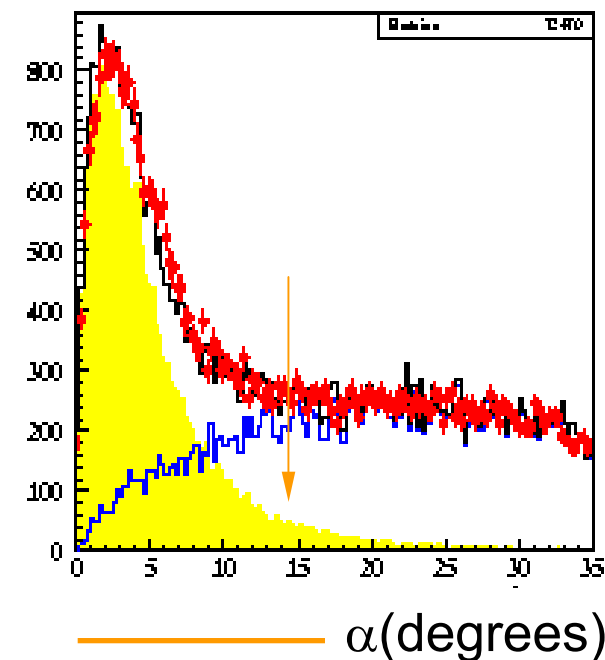
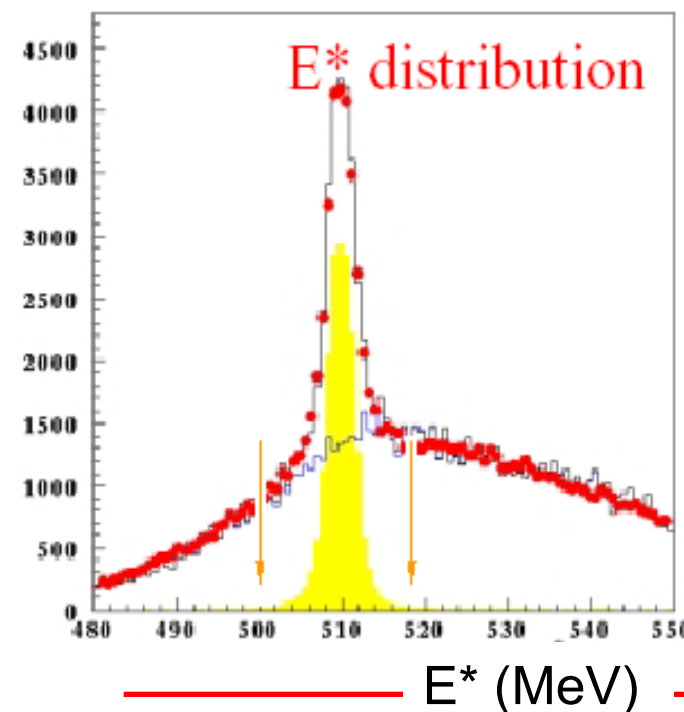
- selection cuts on:

a) E^* the total energy of the 2 γ 's:

$$(E^* - 510) < 5 \sigma^*$$

b) α the angle between the K_L momentum reconstructed from 2 γ 's and the K_L momentum from K_S and ϕ

$$\alpha < 15^\circ$$



$K_L \rightarrow 3\pi^0$ selection



- neutral vertex with > 3 γ 's attached
- cluster energy $E_\gamma > 20$ MeV .and. at least one cluster with $E_\gamma > 80$ MeV (*)
- distance from any another cluster > 40 cm

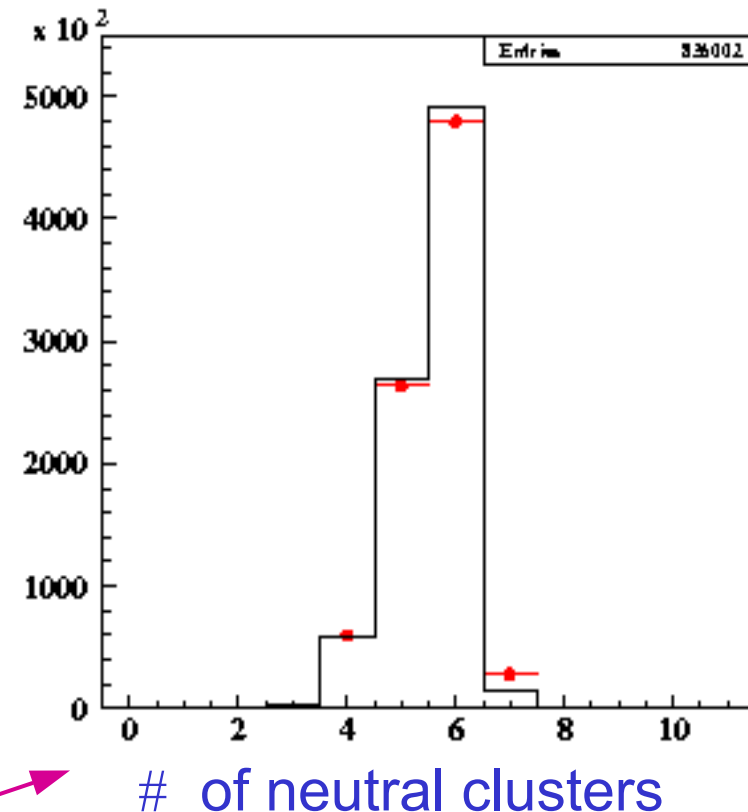
Background comes from:

- $K_L \rightarrow \pi^0\pi^+\pi^-$ and no track-to-cluster association
- $K_L \rightarrow 2\pi^0$
- machine background (*)

Main sources of inefficiencies are:

- geometrical acceptance
- merging with other clusters or splitting
- accidental association to a charged track

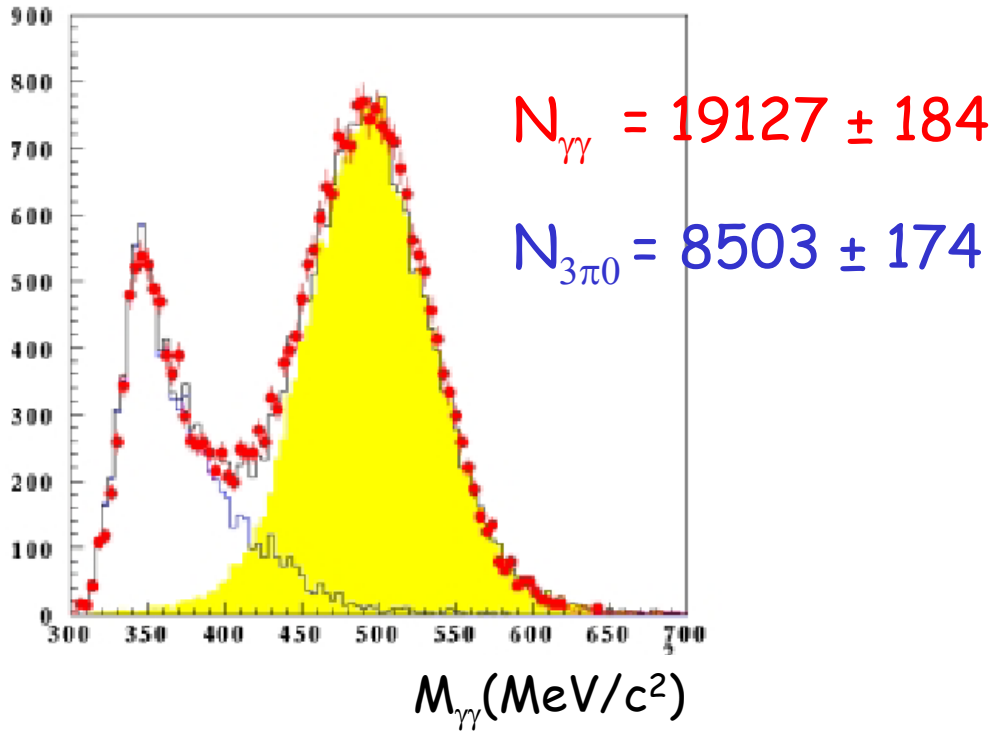
changes the weight of the relative population in



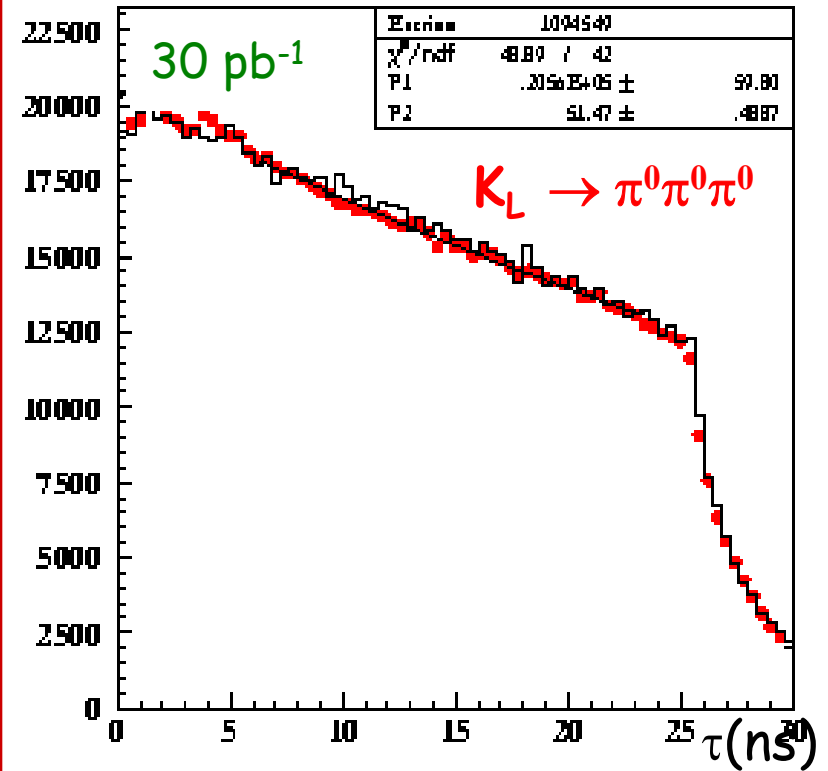


$$R = \Gamma(K_L \rightarrow \gamma\gamma) / \Gamma(K_L \rightarrow \pi^0\pi^0\pi^0)$$

- 312 pb⁻¹ analyzed (2001+2002 data)
- efficiencies estimated mainly from data



K_L lifetime



KLOE $\tau_L = 51.5 \pm 0.5$ ns
PDG $\tau_L = 51.7 \pm 0.4$ ns

Results

KLOE: $R = (2.797 \pm 0.028_{\text{stat}} \pm 0.025_{\text{syst}}) \times 10^{-3}$
NA48: $R = (2.81 \pm 0.01_{\text{stat}} \pm 0.02_{\text{syst}}) \times 10^{-3}$
PDG: $R = (2.77 \pm 0.08) \times 10^{-3}$

$$K_S \rightarrow \gamma\gamma$$




Significant test of ChPT:

- ❖ its branching ratio is unambiguously predicted at $O(p^4)$ order:

$$BR^{(4)}(K_S \rightarrow \gamma\gamma) = 2.1 \times 10^{-6}$$

- ❖ higher order effects are predicted to be $\sim 20\%$ of $O(p^4)$ value

$BR^{\text{EXP}}(K_S \rightarrow \gamma\gamma)$ vs $BR^{(4)}(K_S \rightarrow \gamma\gamma)$  $O(p^6)$ loop contribution estimation

Experimental situation

$$BR^{\text{EXP}}(K_S \rightarrow \gamma\gamma) = (2.78 \pm 0.06_{\text{stat}} \pm 0.04_{\text{syst}}) \times 10^{-6}$$

NA48 from

$$\Gamma(K_S \rightarrow \gamma\gamma) / \Gamma(K_S \rightarrow 2\pi^0)$$

- significantly higher than $BR^{(4)}(K_S \rightarrow \gamma\gamma)$
- higher order corrections increase the decay rate by $\sim 30\%$

To subtract the background coming from $K_L \rightarrow \gamma\gamma$ NA48 has to evaluate it from the measurement of the ratio $R = \Gamma(K_L \rightarrow \gamma\gamma) / \Gamma(K_L \rightarrow \pi^0\pi^0\pi^0)$

$K_S \rightarrow \gamma\gamma$ with KLOE



• Pre-selection to reject the most dangerous background $K_S \rightarrow 2\pi^0$ (BR~31%)

- K_L -crash
- 2 “prompt” clusters $|t-R/c| < 5\sigma_t$
- $E_\gamma > 220$ MeV

• Selection

- $M_{\gamma\gamma} > 400$ MeV/c² invariant mass on the 2 γ 's
- $\cos\theta < -0.9$ and $-0.95 < \cos\theta_{12} < -0.85$
 - $\cos\theta$ angle between K_S direction from K_L -crash and K_S direction from 2 γ 's
 - $\cos\theta_{12}$ angle between the 2 γ 's

$\epsilon_{\text{tot}} \approx 20\%$

$N_{\gamma\gamma} \sim 70$ expected with 500 pb^{-1} but $S/B=1/4 \Rightarrow$ *More statistics is needed*

Thanks to the tagging we will have systematic uncertainties totally different from those of NA48



3) K_{l3} decays

V_{us} from K_{l3} decays



$$\underbrace{\Gamma(K_{e3})}_{\text{measuring}} = \frac{G_F^2 m_K^5}{192 \pi^3} C_K^2 \underbrace{|V_{us}|^2}_{\text{provided by the theory}} \underbrace{|f_+^{K\pi}(0)|^2}_{\text{measuring } q^2 \text{ evolution of the form factor:}} I_K(m_K^2, m_\pi^2, m_\ell^2, \tilde{f}_+^{K\pi}(q^2))$$

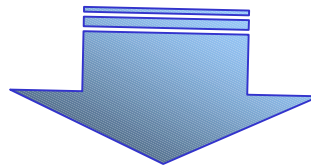
measuring

$$BR(K_{l3})/\tau_K$$

provided by
the theory

measuring q^2 evolution
of the form factor:

$$f_+^{K\pi}(q^2) = f_+^{K\pi}(0) \cdot \left(1 + \frac{\lambda_+^{K\pi}}{m_\pi^2} q^2 \right)$$



The observable is: $|V_{us}| |f_+(0)|$

V_{us} from K_{l3} decays

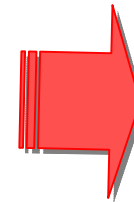


Ignoring phase space and form factor differences:

$$\Gamma(K_L \rightarrow \pi e \nu) = \Gamma(K_S \rightarrow \pi e \nu) = 2 \Gamma(K^\pm \rightarrow \pi^0 e^\pm \nu)$$

But:

$$2 \times (2\Gamma^+ - \Gamma^0) / (2\Gamma^+ + \Gamma^0) = (3.66 \pm 0.06)\%$$



**SU(2) (and SU(3)_F)
symmetry breaking
effect**

To extract V_{us} from the experimental observable we need:

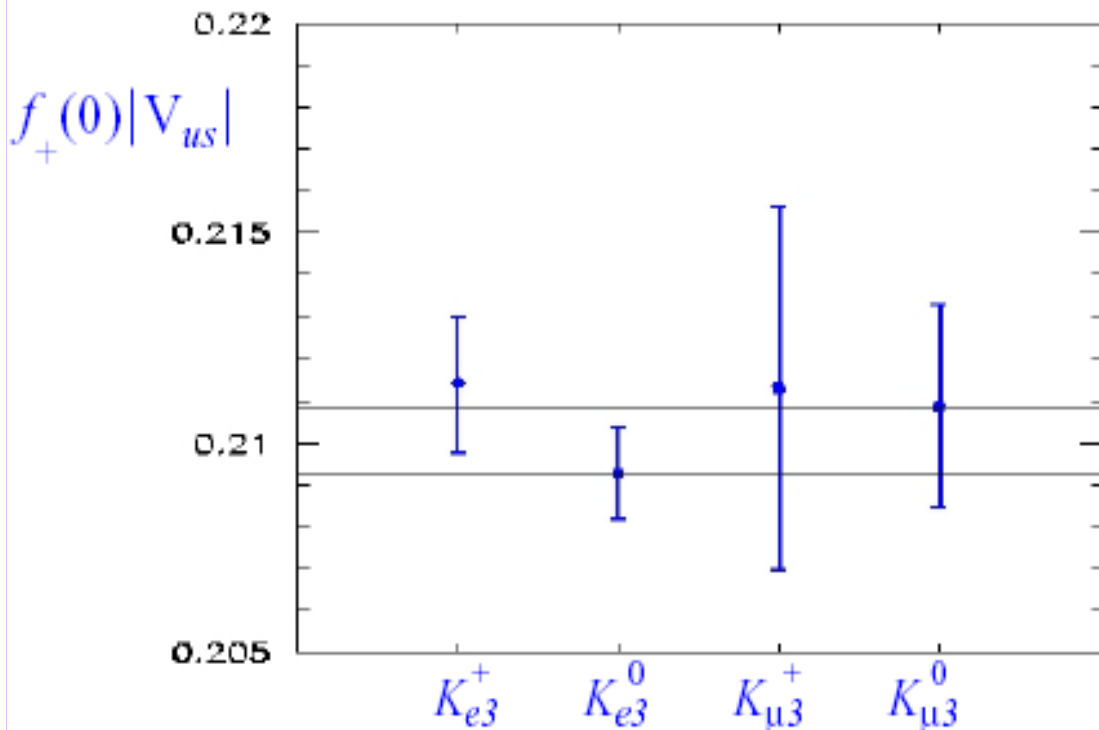
- ✧ SU(2) and SU(3)_F symmetry breaking corrections
- ✧ radiative corrections

$$\mathbf{V_{us} = 0.2196 \pm 0.0026 (PDG '02) \quad \Delta V_{us}/V_{us} = 1.18\%}$$

Status of K_{l3} decays: theoretical corrections



Applying previous corrections to all the K_{l3} modes we have:



$$\diamond \quad |V_{us}|_{K_{l3}} = 0.2187 \pm 0.0020$$

Calderon-Lopez Castro

Phys Rev D65 (2002)

\diamond Large spread after IB corrections
 γ inclusive measurement ???

\diamond Clear prescription for radiative corrections from *Cirigliano et al.*,
Eur. Phys. J. C 23 (2002)

\diamond Applied to K_{e3}^+ gives the result: $|V_{us}|_{K_{e3}^+} = 0.2207 \pm 0.0024$

Status of K_{l3} decays: experimental situation



$\frac{\Delta BR}{BR} (\%)$	$\frac{\Delta \tau}{\tau} (\%)$	$\frac{\Delta \Gamma}{\Gamma} (\%)$	$\frac{\Delta \lambda_{\pm}}{\lambda_{\pm}} (\%)$	$\frac{\Delta \lambda_0}{\lambda_0} (\%)$
K_{e3}^+				
1.2	0.2	1.22	4.5	-
$K_{\mu 3}^+$				
2.5	0.2	2.5	12.2	19.7
K_{e3}^0				
0.7	0.8	1.06	4.7	-
$K_{\mu 3}^0$				
0.9	0.8	1.20	14.7	24.0

Contributions to the relative accuracy on V_{us}

$$\frac{\Delta |V_{us}|}{|V_{us}|} = 0.5 \underbrace{\left(\frac{\Delta BR_{K_{e3}}}{BR_{K_{e3}}} + \frac{\Delta \tau}{\tau} \right)}_{0.59\%} + 0.05 \underbrace{\frac{\Delta \lambda_{\pm}}{\lambda_{\pm}}}_{0.22\%} + \underbrace{\frac{\Delta f_{+}(0)}{f_{+}(0)}}_{0.86\%}$$

K_{e3}^{\pm}

► $\Gamma(K_{l3})$ inclusive measurement with both K^{\pm} and K^0

Measuring $\Gamma(e3)$ at KLOE



Traditional method

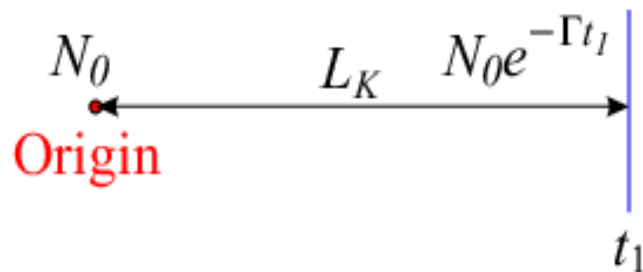
- ◆ measurement of $\Gamma = 1/\tau$
- ◆ measurement of **BR(e3)**



$$\Gamma(e3) = \text{BR}(e3) \times \Gamma$$

$$\frac{\delta \Gamma(e3)}{\Gamma(e3)} = \sqrt{\left(\frac{\delta \tau}{\tau}\right)^2 + \left(\frac{\delta(\text{BR}(e3))}{\text{BR}(e3)}\right)^2}$$

KLOE method



Decay
region

$$\Gamma(e3) = (\Delta N_{e3} / \Delta t) / N_{KL}$$

- ◆ by the tag count the number of K produced, N_{KL}
- ◆ count the number N_{e3} of semileptonic decays in the decay region

Γ is a correction & $\delta\tau/\tau$ dependence reduced by a factor ≈ 5

Measuring V_{us} at KLOE



$$\frac{\Delta|V_{us}|}{|V_{us}|} = \underbrace{0.5 \left(\frac{\Delta BR_{K_{e3}}}{BR_{K_{e3}}} + \frac{\Delta \tau}{\tau} \right)}_{\text{from experiments}} + \underbrace{0.05 \frac{\Delta \lambda_+}{\lambda_+} + \frac{\Delta f_+(0)}{f_+(0)}}_{\text{from theory}}$$

KLOE with the **same detector** and using **both charged and neutral kaons**

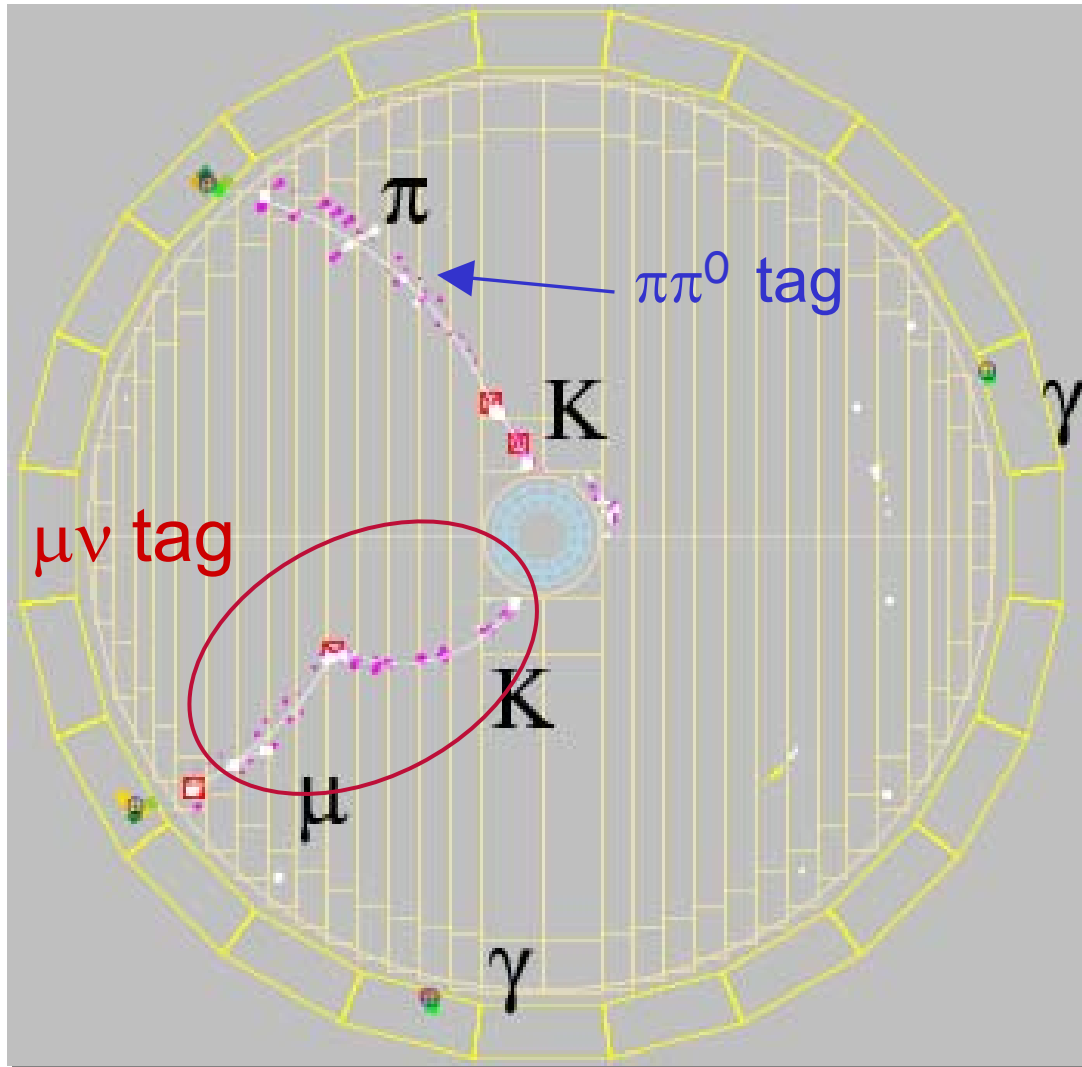
can **improve the experimental contribution to V_{us} accuracy** measuring:

- ❖ absolute branching ratios or directly the partial decay width
- ❖ form factor slopes λ_+ and λ_0

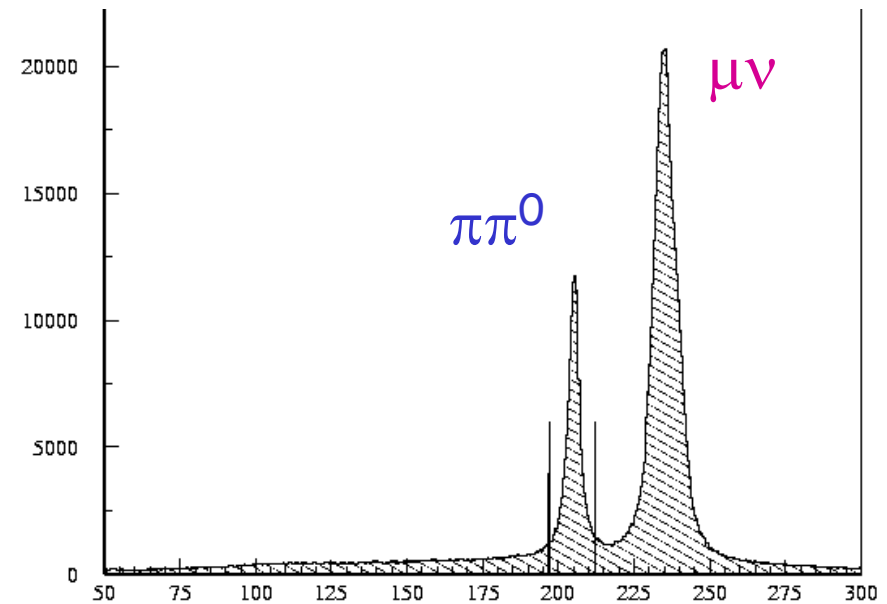
K_{l3} decays from charged kaons



Tag is provided by $K \rightarrow \mu\nu$, $K \rightarrow \pi\pi^0$ (BR~85%) selected using only DC information:



- ◆ K from IP ($70 < p_K < 130$ MeV/c)
- ◆ decay in fiducial volume
- ◆ “right” $p_K - p_{\text{daughter}}$ at vertex
- ◆ p_{track} in K ref. frame



P_{track} (MeV/c)

$\epsilon_{\pi\pi^0}^{\text{TAG}} \approx \epsilon_{\mu\nu}^{\text{TAG}}$ from data using only EMC information

K_{e3}^{\pm} signal selection

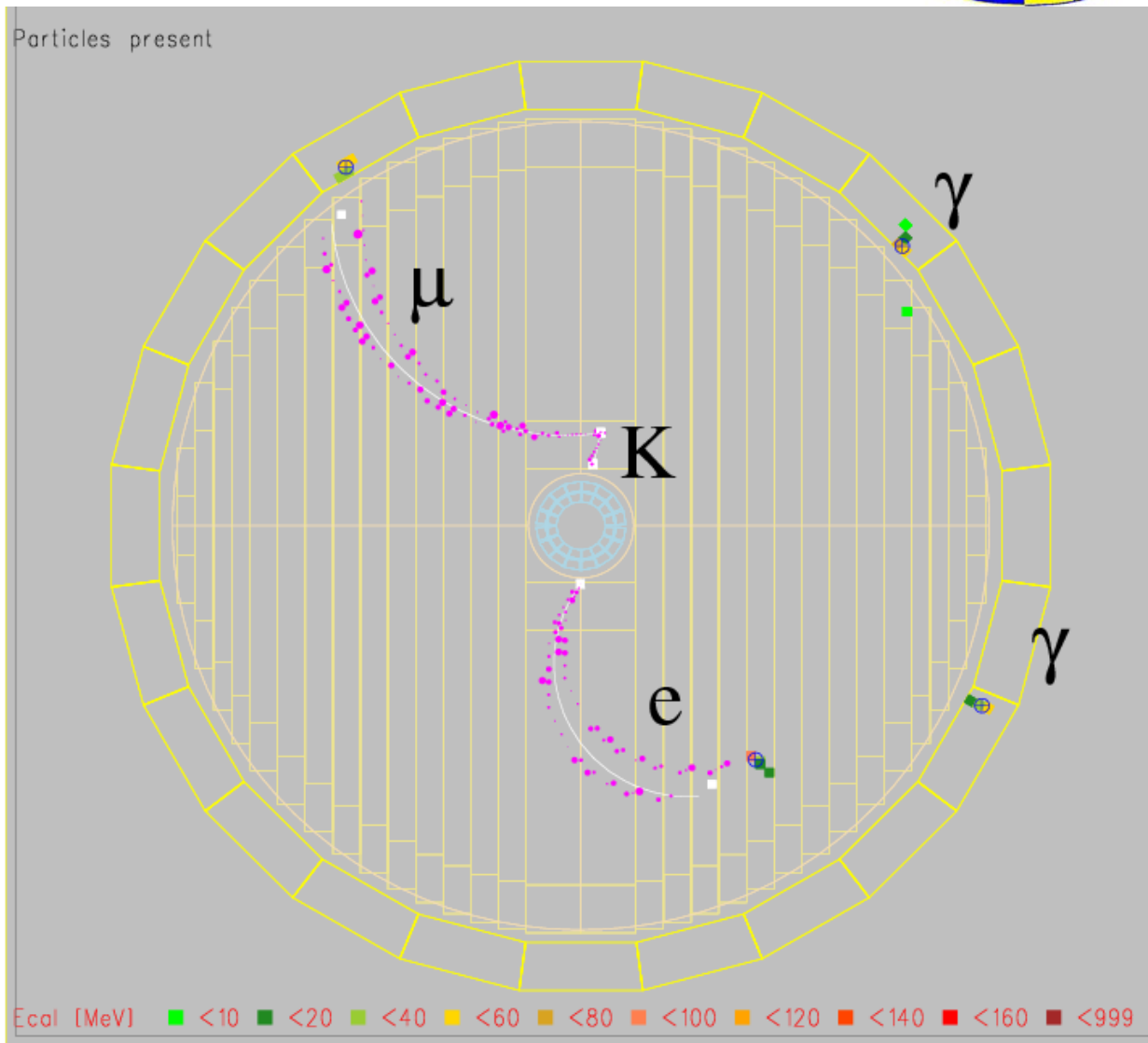


- ✓ Tag on one side
- ✓ Vertex in DC
- ✓ ToF selection
- ✓ π^0 in EMC

17 pb⁻¹

	K_{e3}^{\pm} (yield)	$\epsilon_{sele}(K_{e3}^{\pm})(\%)$
$K_{\mu}^{\pm} TAC$	21 662	34.4 ± 0.6
$K_{\pi\pi^0}^{\pm} TAC$	3 872	32.7 ± 1.3

Preliminary



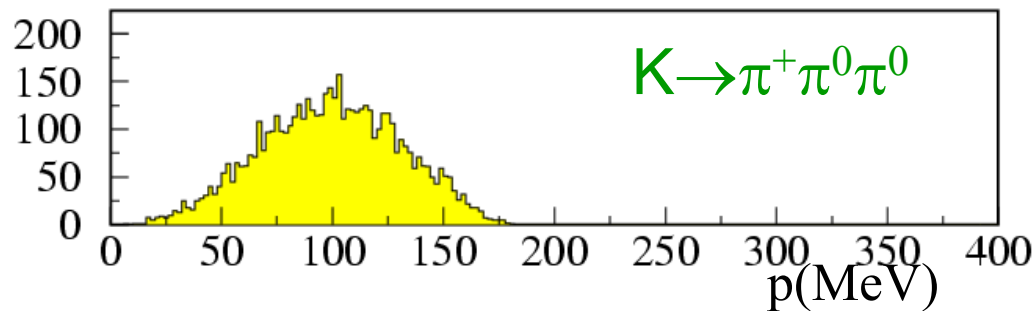
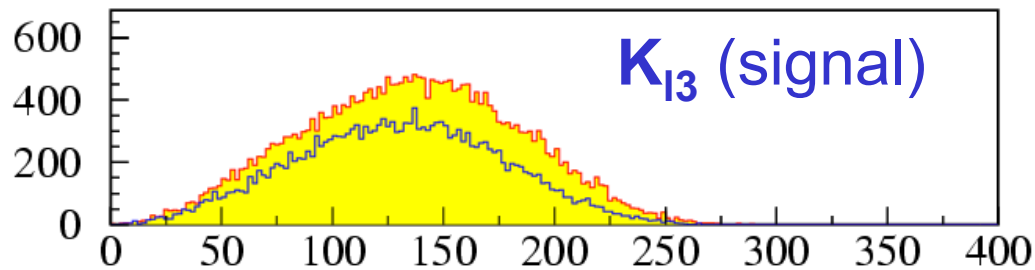
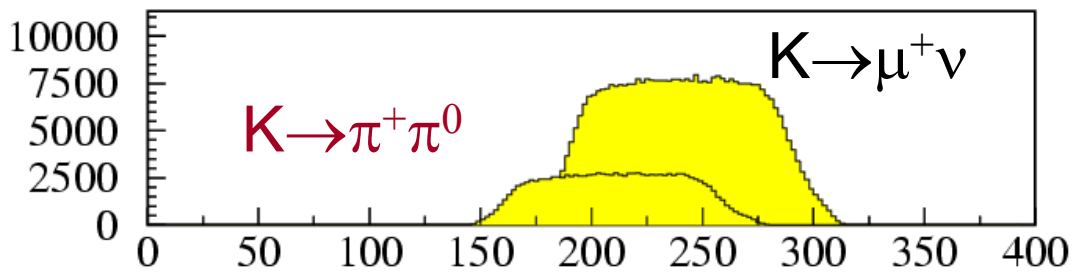
$$N_{K_{e3}^{\pm}} \approx 2000/\text{pb}^{-1} \Rightarrow \underbrace{0.4 \times 10^6}_{200 \text{ pb}^{-1} \text{ (2001 run)}} + \underbrace{0.6 \times 10^6}_{\approx 300 \text{ pb}^{-1} \text{ (2002 run)}}$$

K_{e3}^{\pm} signal efficiency

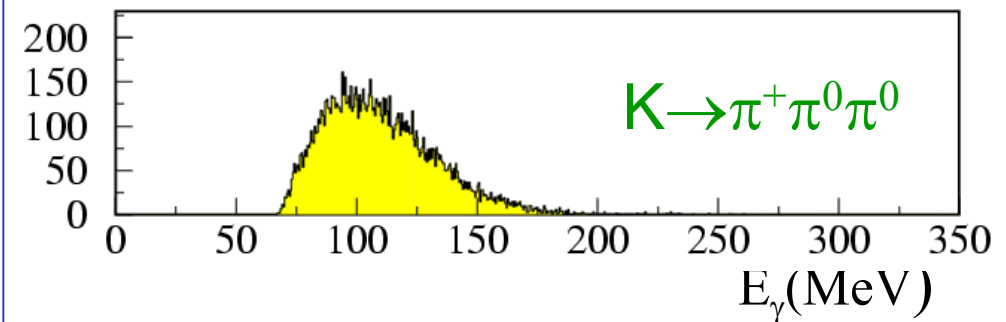
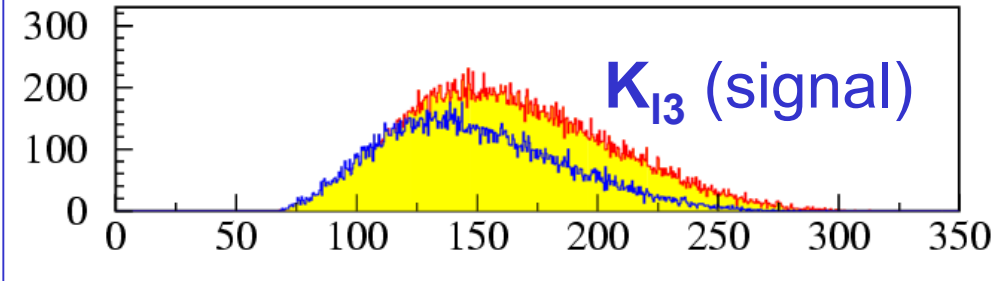
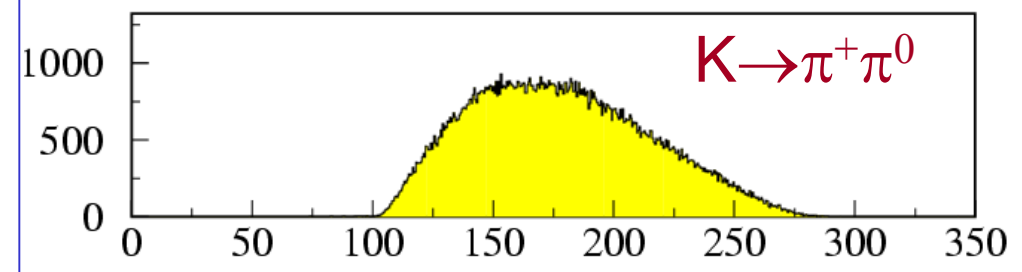


Most of the efficiencies can be evaluated directly from data using control samples \Rightarrow method used for $\Gamma(K_S \rightarrow \pi^+\pi^-(\gamma))/\Gamma(K_S \rightarrow \pi^0\pi^0)$

Track + Vertex fit



π^0 cluster



K_{l3} decays from neutral kaons



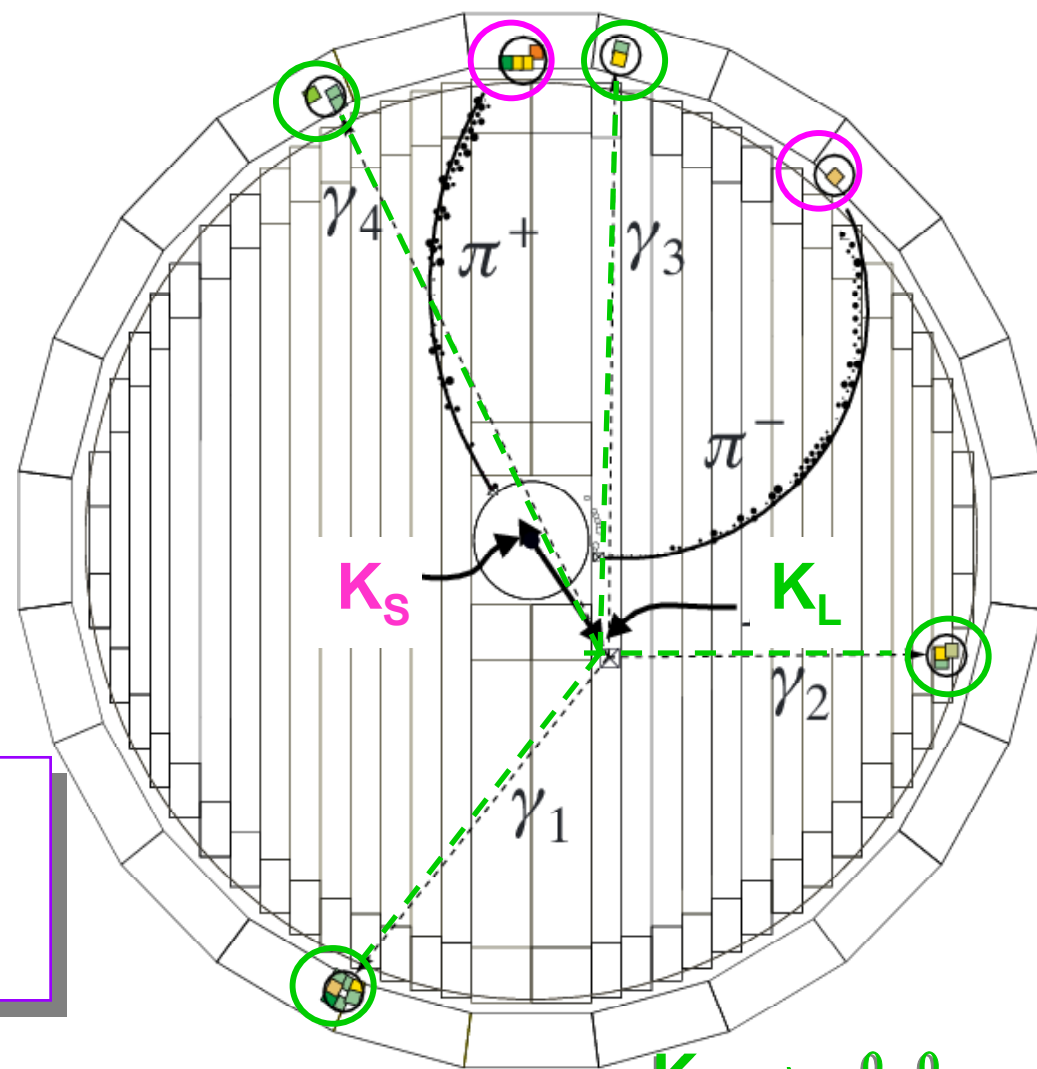
Tag is provided by $K_S \rightarrow \pi^+ \pi^-$ decays selected using only DC information:

- ❖ single vertex in K_S fiducial volume
 $r_T < 4$ cm and $|z| < 8$ cm
- ❖ two and only two tracks of opposite charge connected to the vertex
- ❖ $50 < p_{K_S} < 170$ MeV/c in ϕ ref. frame
- ❖ $400 < M_{K_S} < 600$ MeV/c²

❖ K_L momentum from K_S and ϕ momenta

❖ Tagging efficiency $\varepsilon_{\text{tag,total}} \sim 75\%$

$\varepsilon_{\text{tag,total}}$ can be estimated from data using a sample with “ K_L – crash” and two tracks



$K_L \rightarrow \pi^0 \pi^0$

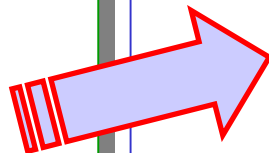
$K_S \rightarrow \pi^+ \pi^-$

K^0_{e3} signal selection

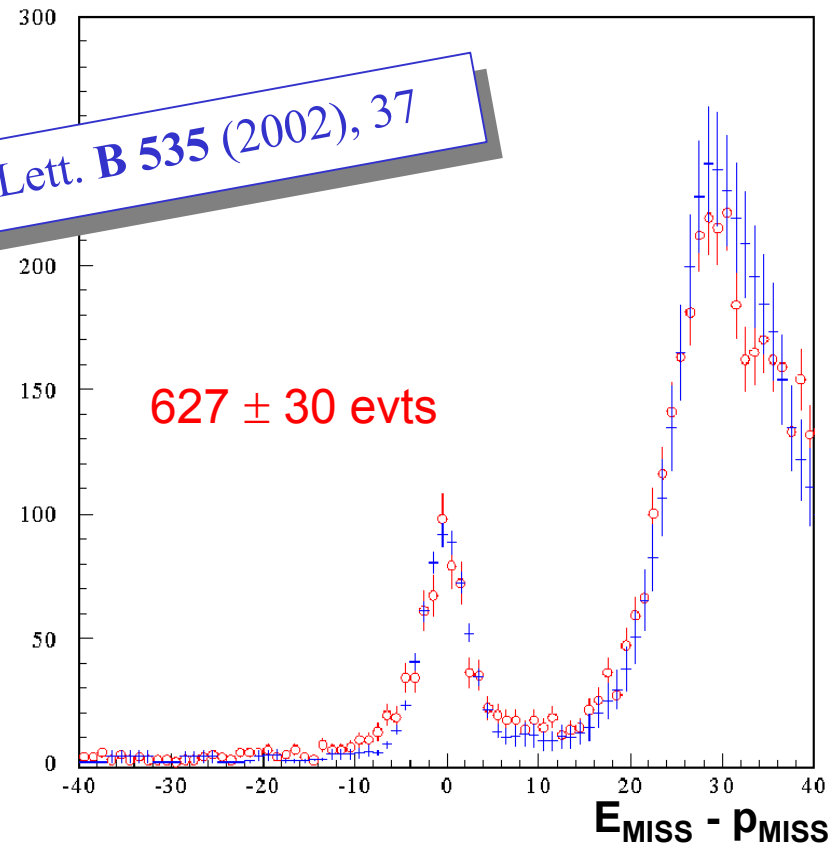


- ✓ Tag on one side
- ✓ Vertex in DC fiducial volume
- ✓ Invariant mass cut
- ✓ ToF selection

➤ Procedure already used for $K_S \rightarrow \pi^\pm e^\pm \nu$:



Phys. Lett. B 535 (2002), 37

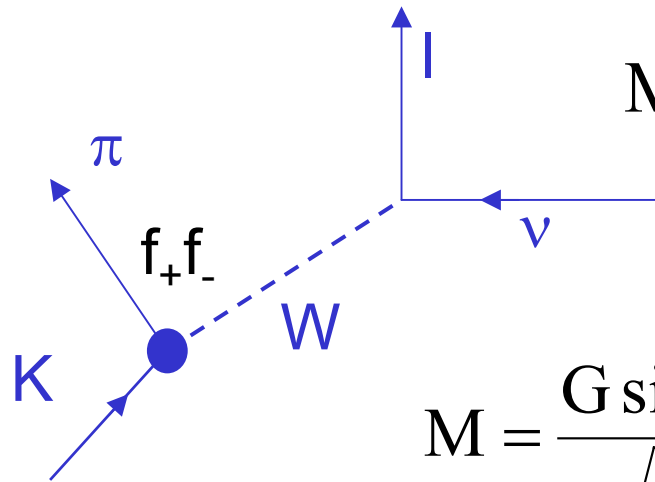


KLOE 2000 data:

$$\text{BR}(K_S \rightarrow \pi^\pm e^\pm \nu) = (6.79 \pm 0.33_{\text{stat}} \pm 0.16_{\text{syst}}) \times 10^{-4}$$

$$N_{K^0_{e3}} \approx 3 \times 10^4 / \text{pb}^{-1} \Rightarrow \underbrace{6 \times 10^6}_{200 \text{ pb}^{-1} \text{ (2001 run)}} + \underbrace{9 \times 10^6}_{\approx 300 \text{ pb}^{-1} \text{ (2002 run)}} (\sim 1.5 \times 10^4 K_S \rightarrow \pi^\pm e^\pm \nu)$$

K_{l3} the form factors



$$M = \frac{G \sin \theta}{\sqrt{2}} \underbrace{\langle \pi | J_\mu^{\text{had}} | K \rangle}_{f_+(t)P_\mu + f_-(t)q_\mu} u_1 \gamma^\mu (1 - \gamma_5) u_\nu$$

$$t = q^2 = (P^K - P^\pi)^2$$

$$P_\mu = P_\mu^K + P_\mu^\pi$$

$$q_\mu = P_\mu^K - P_\mu^\pi$$

$$M = \frac{G \sin \theta}{\sqrt{2}} \left\{ f_+(t) P_\mu \bar{u}_\nu \gamma^\mu (1 - \gamma_5) u_1 + \underline{m_1} f_-(t) u_1 (1 - \gamma_5) u_\nu \right\}$$

event density: $\rho(E_\mu, E_\pi) = \frac{d^2 \Gamma}{dE_\pi dE_\mu} = \frac{|M|^2}{8M(2\pi)^3} \propto A f_+^2(t) + B f_+(t) f(t) + C f^2(t)$

$$f(t) = f_+(t) + \frac{t}{M_K^2 - m_\pi^2} f_-(t)$$

linear expansion of the $f_i(t)$:

$$f_+(t) = f_+(0) \left(1 + \lambda_+ t / m_\pi^2 \right)$$

$$f(t) = f(0) \left(1 + \lambda_0 t / m_\pi^2 \right) \Rightarrow \rho(E_\mu, E_\pi, \lambda_+, \lambda_0)$$

λ_+ and λ_0 can be measured from fit of the Dalitz plot distribution

Measuring λ_+



$$\lambda_+^{K^0_{e3}} = 0.0245 \pm 0.0012_{stat} \pm 0.0022_{syst} \text{ (CPLEAR)} \quad 3.6 \times 10^5 \text{ events}$$

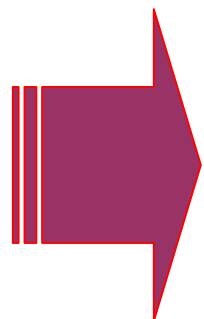
6×10^6

@KLOE (200 pb⁻¹)
 $\sigma_{stat} \approx O(10^{-4})$

$$\lambda_+^{K^\pm_{e3}} = 0.0293 \pm 0.0015_{stat} \pm 0.002_{syst} \text{ (ISTRA+)} \quad 1.3 \times 10^5 \text{ events}$$
$$\lambda_+^{K^\pm_{e3}} = 0.0278 \pm 0.0017_{stat} \pm 0.0015_{syst} \text{ (KEK-E246)} \quad 10^5 \text{ events}$$

4×10^5

@KLOE (200 pb⁻¹)
 $\sigma_{stat} \approx O(10^{-3})$



KLOE can improve the actual measurements of λ_+ using both K^0_{e3} and K^\pm_{e3} decays

Measuring λ_0



$\mathbf{K^0_{\mu 3}}$
 $\lambda_0 = 0.019 \pm 0.004$ (Donaldson et al.) 1.6×10^6 events

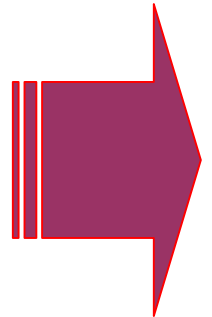
6×10^6

@KLOE (200 pb⁻¹)
 $\sigma_{stat} \approx O(10^{-4})$

$\mathbf{K^{\pm}_{\mu 3}}$
 $\lambda_0 = 0.0209 \pm 0.004_{stat} \pm 0.002_{syst}$ (ISTRA+) 1.1×10^5 events
 $\lambda_0 = 0.022 \pm 0.005_{stat} \pm 0.004_{syst}$ (KEK-E246) 4.1×10^4 events

4×10^5

@KLOE (200 pb⁻¹)
 $\sigma_{stat} \approx O(10^{-3})$



KLOE can improve the actual measurements of λ_0 using both $\mathbf{K^0_{\mu 3}}$ and $\mathbf{K^{\pm}_{\mu 3}}$ decays



4) *Kl4 decays*

K_{e4} decays



The $\pi\pi$ scattering at low energy is the simplest possible hadronic interaction

- promising ground for studying the strength of the $q\bar{q}$ condensate
- test the hypothesis that the quark condensate is the leading order parameter of the spontaneous broken chiral symmetry

❖ $\pi N \rightarrow \pi\pi N$

High statistics available but extraction of $\pi\pi$ amplitude is **model dependent**

❖ $Ke4$ decays

no additional strongly interacting particles in the final state

- **very precise predictions from ChPT** (*but* $BR(K_{e4}) = 3.91 \times 10^{-5}$)

K_{e4} decays



$$d\Gamma = G_F^2 |V_{us}|^2 N(s_\pi, s_e) J_5(s_\pi, s_e, \vartheta_\pi, \vartheta_e, \phi) ds_\pi ds_e d\cos\vartheta_\pi d\cos\vartheta_e d\phi$$

- J_5 is a simple function of $\vartheta_e \phi$ and of 9 intensities $I_i(s_\pi, s_e, \vartheta_\pi, F, G, H, R)$

full kinematics described by 5 variables

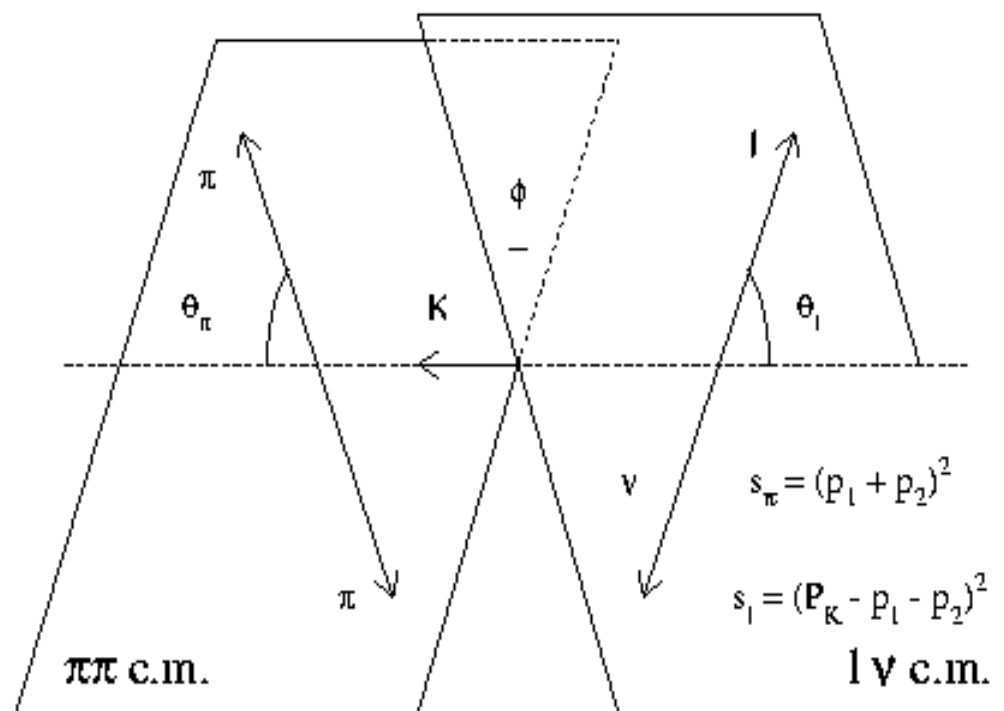
- performing the partial wave expansion of the form factors F, G, H, R in the variable ϑ_π :

$$\vartheta_\pi$$

the amplitudes are functions of s_π, s_e

the phases coincide with the phase shift of the $\pi\pi$ elastic scattering and are functions of

$$\delta_l^I(s_\pi)$$





The observable is the phase difference:

$$\delta(s_\pi) = \delta_0^0(s_\pi) - \delta_1^1(s_\pi) \quad 4M_\pi^2 < s_\pi < M_K^2$$

To extract it from data we can use the **Pais-Treiman method**:

- $d^2\Gamma/d\cos\theta_e d\phi$ event distribution in s_π bins
- fit the event distribution with the 9 intensities I_i
- neglecting all the waves higher than S and P we have:

$$\tan(\delta_0^0 - \delta_1^1) = \frac{1}{2} \frac{\int_{-1}^1 I_7 d\cos\theta_\pi}{\int_{-1}^1 I_4 d\cos\theta_\pi}$$

K_{e4} decays theoretical predictions

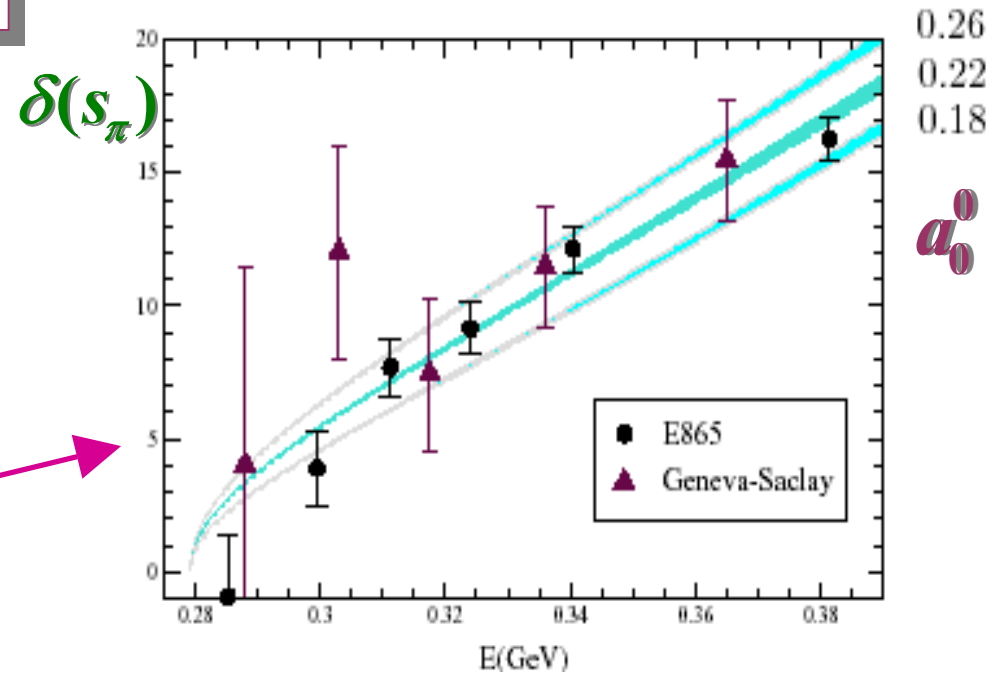


Predictions are made on the S-wave scattering length a_0^0 (dominant wrt a_0^2)

ChPT prediction $a_0^0 = 0.220 \pm 0.005$

Need to relate δ to a_0^0 :

- ❖ expansion by Basdevant et al. but introduces new parameters
- ❖ Roy equations phenomenological description



Experimental situation (from K_{e4}^\pm)

Rosselet et al. $a_0^0 = 0.26 \pm 0.05$ $\sim 3 \times 10^4$ events (1977)

E865 Coll. $a_0^0 = 0.228 \pm 0.012$ $\sim 3 \times 10^5$ events (2000)

K_{e4} decays at KLOE

- ✓ Tag on one side using $K \rightarrow \mu \nu$ decays
simpler reconstruction of the 4 tracks
- ✓ Vertex in DC fiducial volume
- ✓ 4 tracks attached to the vertex
 $p_T < 200 \text{ MeV}/c \Rightarrow$ spiralling tracks
- ✓ ToF selection
- ✓ main background $K^+ \rightarrow \pi^+ \pi^- \pi^+$

Need optimization of:

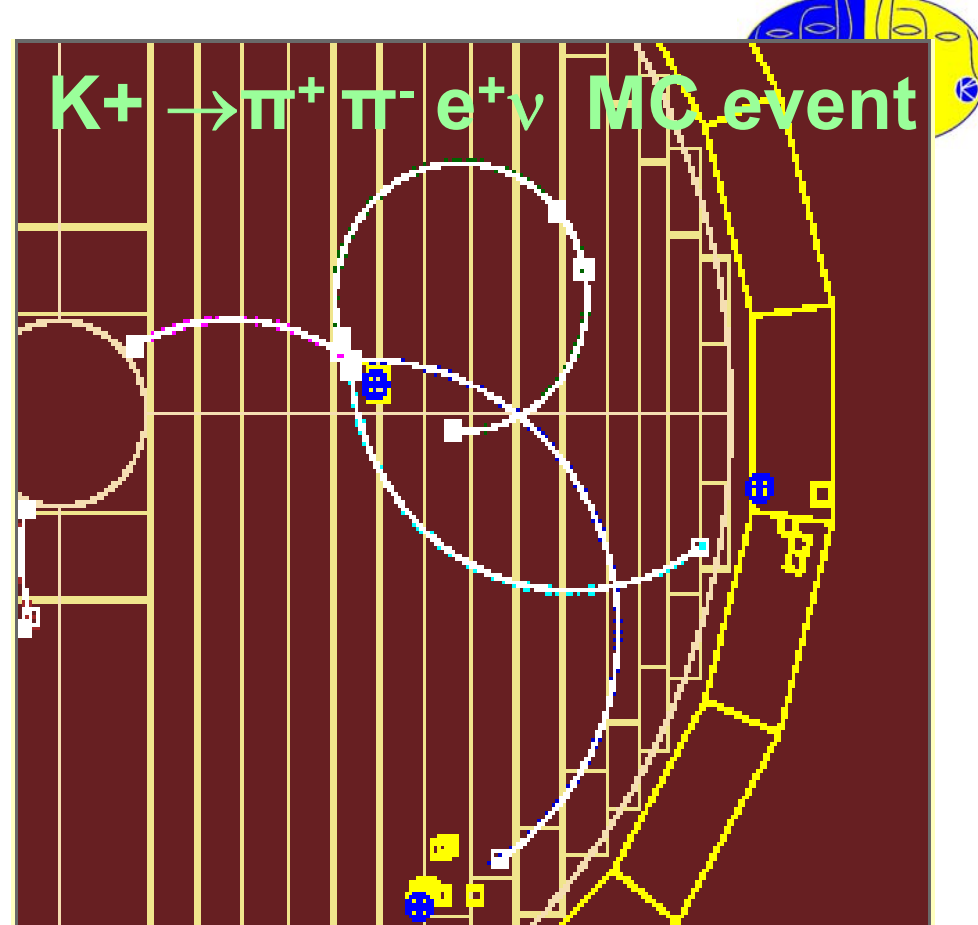
- pattern recognition and track fit procedure for very low momenta
- Vertex fit with 4 tracks

(everything optimized for CP events)

$$N_{K_{\pm e4}}^{\text{tag}} \approx 1.5 \times 10^4 \text{ but}$$

more statistics is needed to enter into the game!!

***Totally different systematic uncertainties at KLOE
thanks to the unique feature of the tagging***





$$5) \quad \eta \rightarrow \pi^0 \gamma \gamma$$

$\eta \rightarrow \pi^0 \gamma\gamma$: theory



This decay is a window on rather high order corrections in ChPT

- ❑ Leading term $O(p^2)$ is absent
- ❑ tree-level amplitude $O(p^4)$ is also zero
- ❑ loop contributions $O(p^4)$ plays a very minor role:

❑ chiral expansion starts from $O(p^6)$ $\Rightarrow \Gamma^{(4)}(\eta \rightarrow \pi^0 \gamma\gamma) = 4 \div 7 \times 10^{-3} \text{ eV}$

Theoretical predictions of $\Gamma(\eta \rightarrow \pi^0 \gamma\gamma)$

❖ VDM	0.30 ± 0.16	(Ng-Peters)
❖ V+A resonance	0.47 ± 0.20	(Ko)
❖ q-box diagram	$0.70 \div 0.92$	(Ng-Peters, Nemoto et al.)
❖ ChPT	0.42 ± 0.20	(Ametller et al.)
❖ ChPT	0.58 ± 0.30	(Bellucci-Bruno)

$\eta \rightarrow \pi^0 \gamma\gamma$: experiments



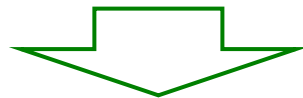
Experimental situation

GAMS-2000 (1981)	$6 \times 10^5 \eta$	38 events	$BR(\eta \rightarrow \pi^0 \gamma\gamma) = (9.5 \pm 2.3) \times 10^{-4}$
GAMS-2000 (1984) reanalysis			$BR(\eta \rightarrow \pi^0 \gamma\gamma) = (7.1 \pm 1.4) \times 10^{-4}$
SND(2001)	$2.6 \times 10^5 \eta$	170 events (7 signal + 163 bckg)	$BR(\eta \rightarrow \pi^0 \gamma\gamma) = (2.1^{+3.8}_{-1.9}) \times 10^{-4}$
Crystal Ball (2001) preliminary	$2 \times 10^7 \eta$	500 events	$BR(\eta \rightarrow \pi^0 \gamma\gamma) = (3.2 \pm 0.9) \times 10^{-4}$

$\Gamma(\eta \rightarrow \pi^0 \gamma\gamma) = 0.84 \pm 0.18 \text{ eV}$

$\Gamma(\eta \rightarrow \pi^0 \gamma\gamma) = 0.38 \pm 0.11 \text{ eV}$

No agreement between **GAMS-2000** and **Crystal Ball**



measures of E_γ and of $\gamma\gamma$ invariant mass spectra are needed
 \Rightarrow different shapes for different models

$\eta \rightarrow \pi^0 \gamma \gamma$ with KLOE



- Tag η decays from $\phi \rightarrow \eta \gamma$ asking for a photon with $E_\gamma = 363$ MeV available statistics:

$$N_{\eta}^{\text{tag}} \approx 2 \times 10^7 \text{ same as Crystal Ball}$$

- the selection looks for 5 “prompt” γ in the final state:
- photon pairing and kinematic fit with mass constraint in the hypothesis:

- $\pi^0 \pi^0 \gamma$ ($f_0 \rightarrow \pi^0 \pi^0$)
- $\eta \pi^0 \gamma$ ($a^0 \rightarrow \eta \pi^0$)
- $\omega \pi^0 \rightarrow \pi^0 \pi^0 \gamma$ ($M(\pi^0 \gamma) = M(\omega)$)
- $\eta \gamma \rightarrow 3 \gamma$
- $\eta \gamma \rightarrow \pi^0 \gamma \gamma \gamma$

$\eta \rightarrow \pi^0 \gamma \gamma$ with KLOE

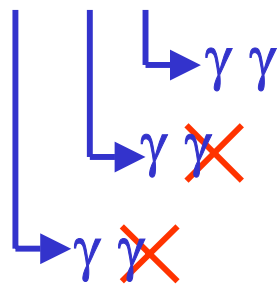


After $\pi^0 \pi^0 \gamma$ and $\eta \pi^0 \gamma$ rejection:

- (1) Signal (MC)
- (2) Residual $\pi^0 \pi^0 \gamma$ (MC)
- (3) $\eta \gamma \rightarrow \pi^0 \pi^0 \pi^0 \gamma$ (MC)
- (4) Data

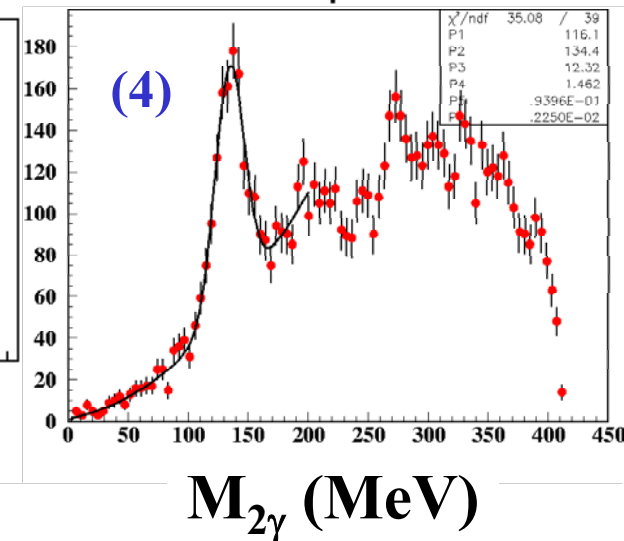
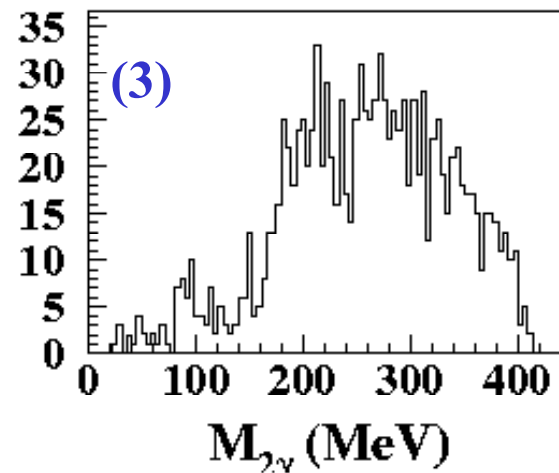
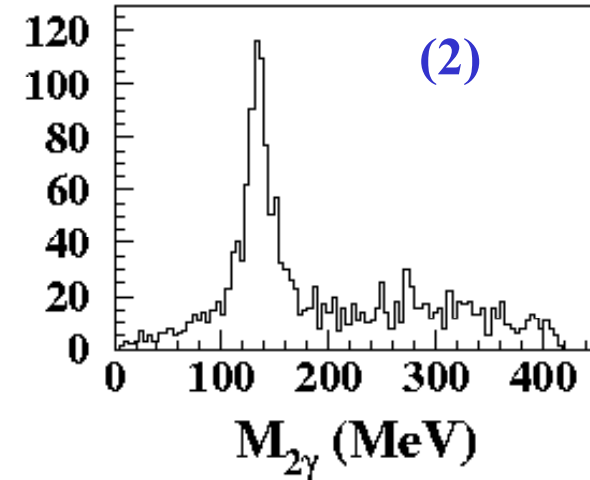
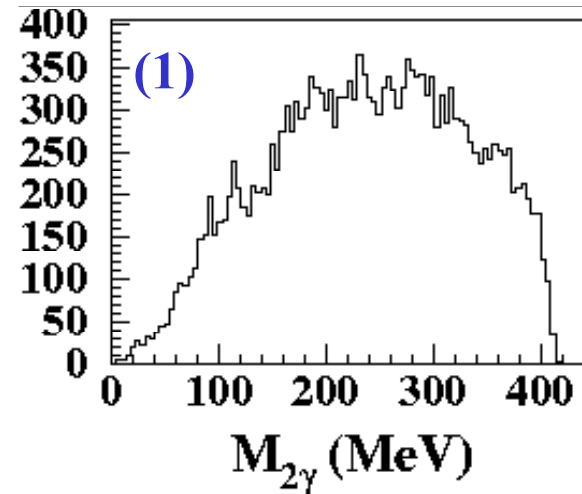
Cutting the π^0 peak does not help with (3)

$\phi \rightarrow \eta \gamma \rightarrow \pi^0 \pi^0 \pi^0 \gamma$



\Rightarrow only one π^0 is reconstructed

$M_{2\gamma} \gamma \gamma$ invariant mass spectra



Still no clear signal of $\eta \rightarrow \pi^0 \gamma \gamma$ crucial to improve $\phi \rightarrow \eta \gamma \rightarrow \pi^0 \pi^0 \pi^0 \gamma$ rejection both using QCAL (γ lost) and shower shape variables (merging)

Conclusions



KLOE can perform many tests of Chiral Perturbation Theory

- ❖ Totally different systematic uncertainties wrt other experiments thanks to the unique feature of the tagging
- ❖ First results from:
 - $\delta_0 - \delta_2$ measurement using $K \rightarrow \pi\pi$
 - $\Gamma(K_L \rightarrow \gamma\gamma) / \Gamma(K_L \rightarrow \pi^0\pi^0\pi^0)$ measurement
- ❖ With the available statistics relevant contribution to:
 - K_{l3} decays for the measurement of V_{us}
 - $\eta \rightarrow \pi^0\gamma\gamma$
- ❖ With more luminosity the following items will be accessible:
 - Ke4 decays
 - $K_S \rightarrow \gamma\gamma$

DAΦNE parameters

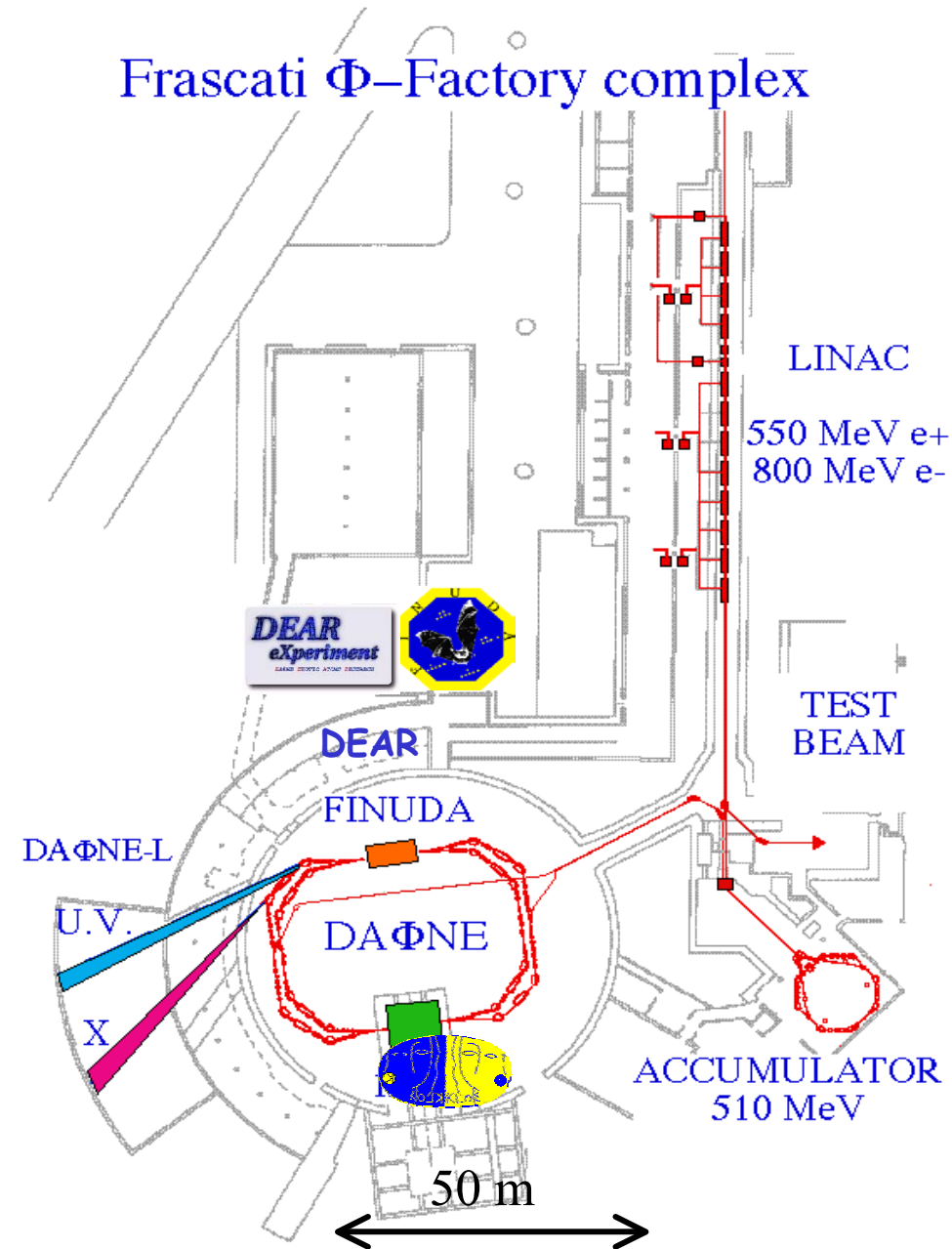


Design parameters

- Beam energy : 510 MeV
- Max number of bunches : 120
- Bunch spacing : 2.7 ns
- Bunch current : 40 mA
- Single bunch luminosity : $4 \cdot 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$



$$L = 5 \cdot 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$$





BR($K_S \rightarrow \pi^\pm e^\pm \nu$)

Motivations

- if (CPT).and.(ΔS .eq. ΔQ) then

$$BR(K_S \rightarrow \pi^\pm e^\pm \nu) = BR(K_L \rightarrow \pi^\pm e^\pm \nu) \times \Gamma_L / \Gamma_S$$

from PDG values = $(6.704 \pm 0.071) \times 10^{-4}$

only one measurement (CMD-2 1999): $(7.2 \pm 1.4) \times 10^{-4}$

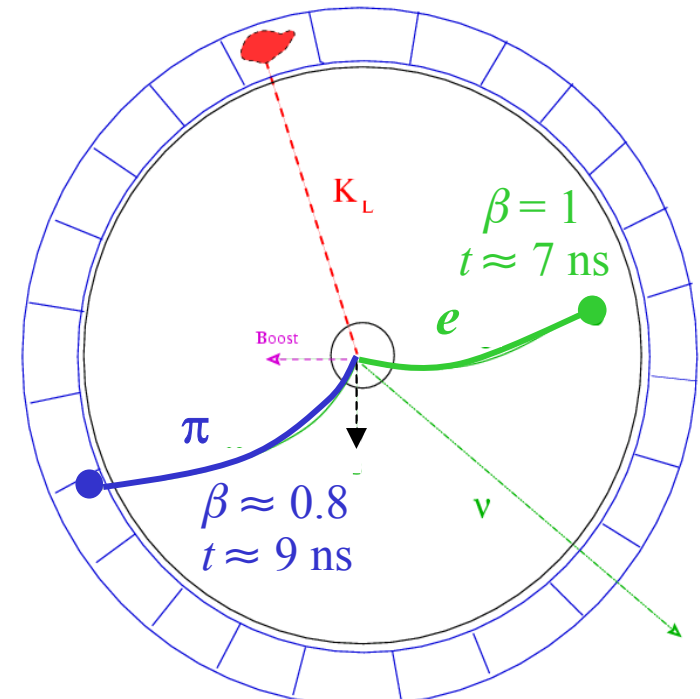
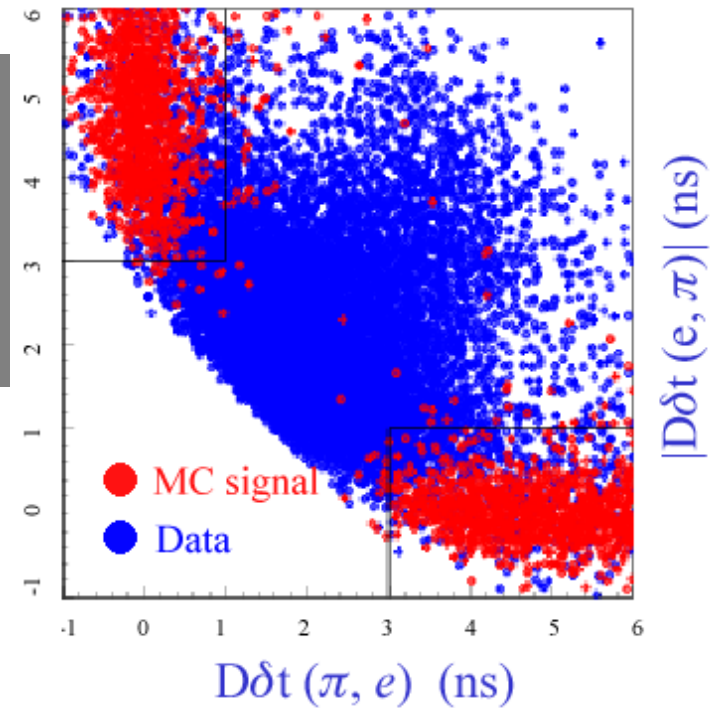
Selectio

- ❖ K_L -crash.and.charged vertex at IP ($r < 8\text{cm}$, $|z| < 10\text{cm}$)
- .and.2 tracks with associated EmC clusters
- ❖ invariant mass of the tracks in π hp $M_{\pi\pi} < 490 \text{ MeV}/c^2$
(against background from $K_S \rightarrow \pi^+\pi^-$)
- ❖ π/e identification using time-of-flight
- ❖ $E_{\text{miss}} - |p_{\text{miss}}|$

π/e identification using time-of-flight

$$D\delta t(\pi, e) = [t_1^{\text{CLU}} - t_2^{\text{CLU}}] - [L_1 / c \beta(\pi) - L_2 / c \beta(e)]$$

- ❖ $|D\delta t(\pi, \pi)| > 1.5 \text{ ns}$ to reject $K_S \rightarrow \pi^+\pi^-$
- ❖ Cuts on $D\delta t(\pi, e)$ and $D\delta t(e, \pi)$



Efficiency evaluation



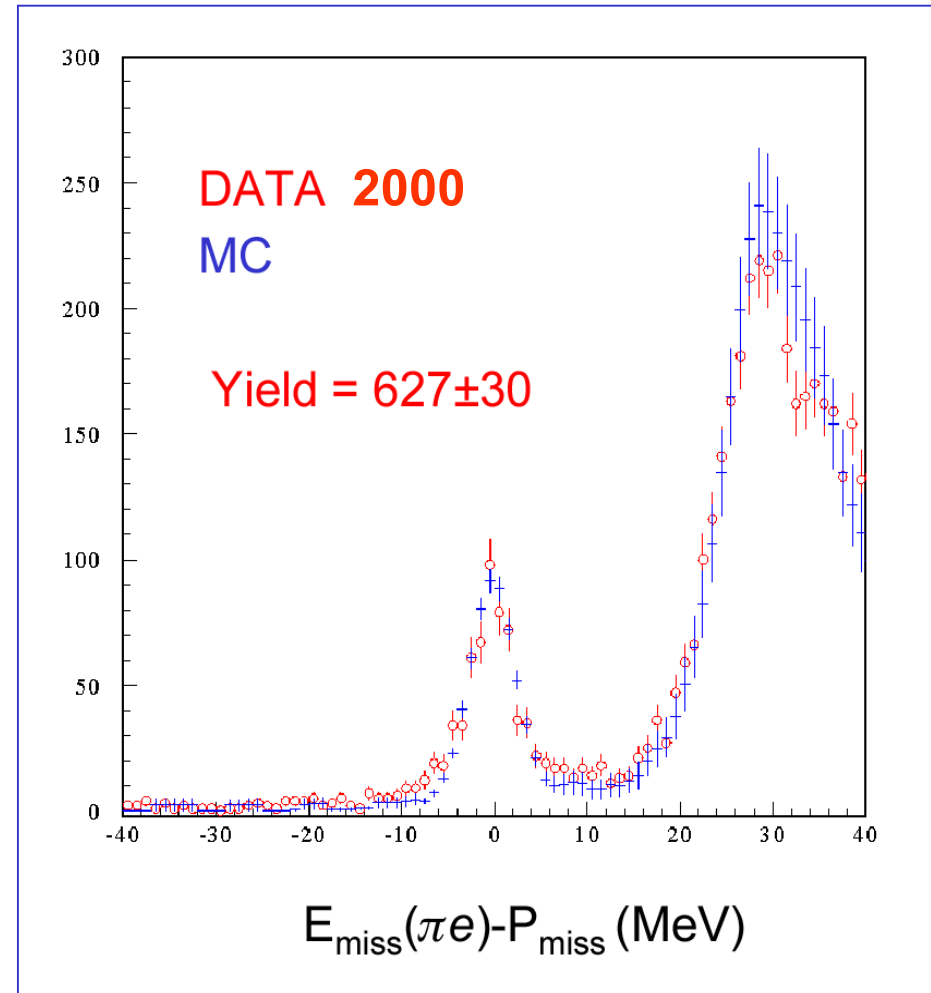
✓ **Vertex reconstruction, fiducial cuts and $M_{\pi\pi}$ efficiency** from MC but also from data $K_L \rightarrow \pi e \nu$ near I.P. (high-purity sample ($> 99.7\%$), by kinematic cuts) and $K_S \rightarrow \pi^0 \pi^0$ to scale MC
Tracking efficiency for MC and data from $K_S \rightarrow \pi^+ \pi^-$

✓ **Single-particle t_0 , track-cluster, and trigger efficiencies from data** using $K_L \rightarrow \pi e \nu$ near origin and $K_S \rightarrow \pi^+ \pi^-$ but also $\phi \rightarrow \pi^+ \pi^- \pi^0$. MC efficiency scaled accordingly

✓ **Time of flight ID efficiency** from $K_L \rightarrow \pi e \nu$ decays near origin and $K_S \rightarrow \pi^+ \pi^-$

Overall selection efficiency:

$(20.8 \pm 0.4)\%$



Fit to $E_{\text{miss}}-P_{\text{miss}}$ spectrum using MC spectra for signal and $\pi^+ \pi^-$ background

Normalization to $K_S \rightarrow \pi^+ \pi^-$ decays



$BR(K_S \rightarrow \pi^\pm e^\pm \nu)$

CPT and $\Delta S = \Delta Q$ predicts: $\Gamma(K_S \rightarrow \pi^\pm e^\pm \nu) = \Gamma(K_L \rightarrow \pi^\pm e^\pm \nu)$

and then: $BR(K_S \rightarrow \pi^\pm e^\pm \nu) = BR(K_L \rightarrow \pi^\pm e^\pm \nu) \times (\Gamma_L / \Gamma_S)$

Using PDG:

$$BR(K_S \rightarrow \pi^\pm e^\pm \nu) = (6.704 \pm 0.071) \times 10^{-4}$$

Result

KLOE 2000 data, $(6.79 \pm 0.33_{\text{stat}} \pm 0.16_{\text{syst}}) \times 10^{-4}$ 627 \pm 30 evts

CMD-2 1999, $(7.2 \pm 1.4) \times 10^{-4}$ 75 \pm 13 evts

Main contributions to the total error	%
Statistics	4.9
Tracking + vertex efficiency	2.0
Cluster, t_0 , trigger	0.9
TOF selection eff	0.8
Tag eff	0.6
Total	5.9

lower with the 2001 data !!