



Update on the momentum resolution by MCS with the angle method

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❁ **Improved estimate of $\Delta P/P$**

❁ **$\Delta P/P$ parameterisation as a function of the
number of cells and P**

Reference: Opera note OPLAPP 1812-01



How to define the resolution?

Momentum measurement \Rightarrow determination of $\Delta P/P$

8 GeV muons

Previous estimate : RMS or σ of gaussian fit

not satisfactory : asymmetric with long tails

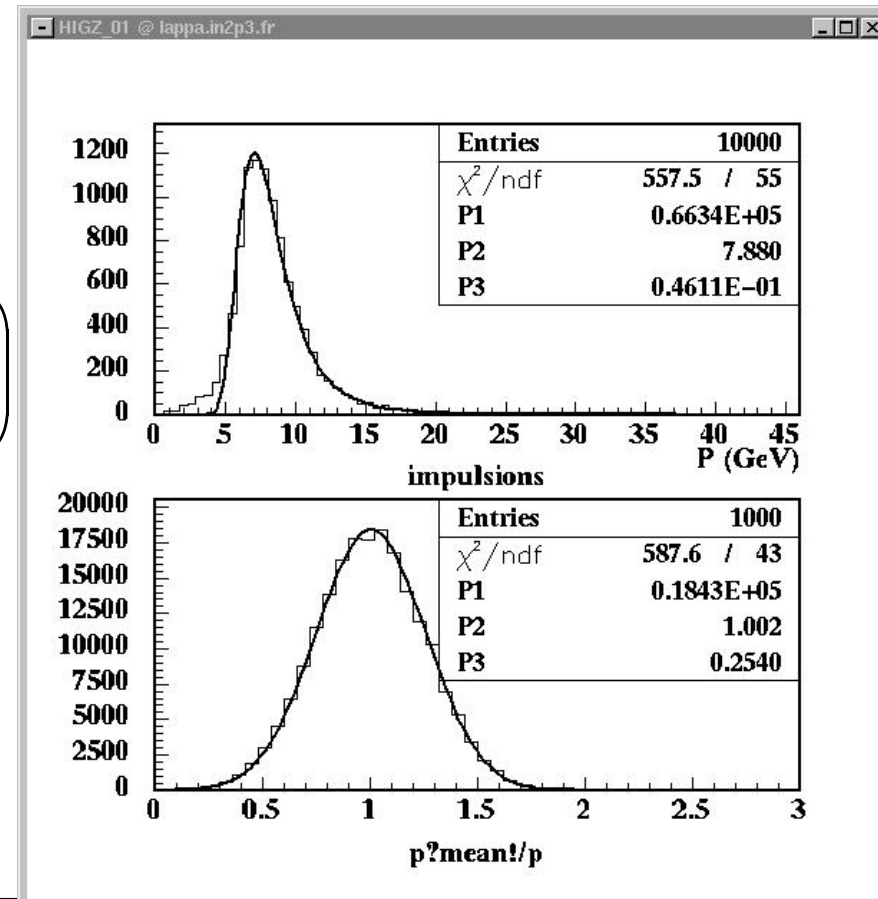
fitted function = «expected» function

$$f(p) = \frac{1}{p^2} \text{par}(1) \exp\left(\frac{-(1/p - 1/\text{par}(2))^2}{\text{par}(3)^2}\right)$$

express f as a function of $1/p \Rightarrow g(1/p)$

$g(1/p)$ is gaussian

- $\Delta P/P = \Delta(1/P)/(1/P)$





Momentum resolution results

muons measured with 56 films (1 brick)

Old estimate was really underestimating the resolution : RMS was not a good choice.

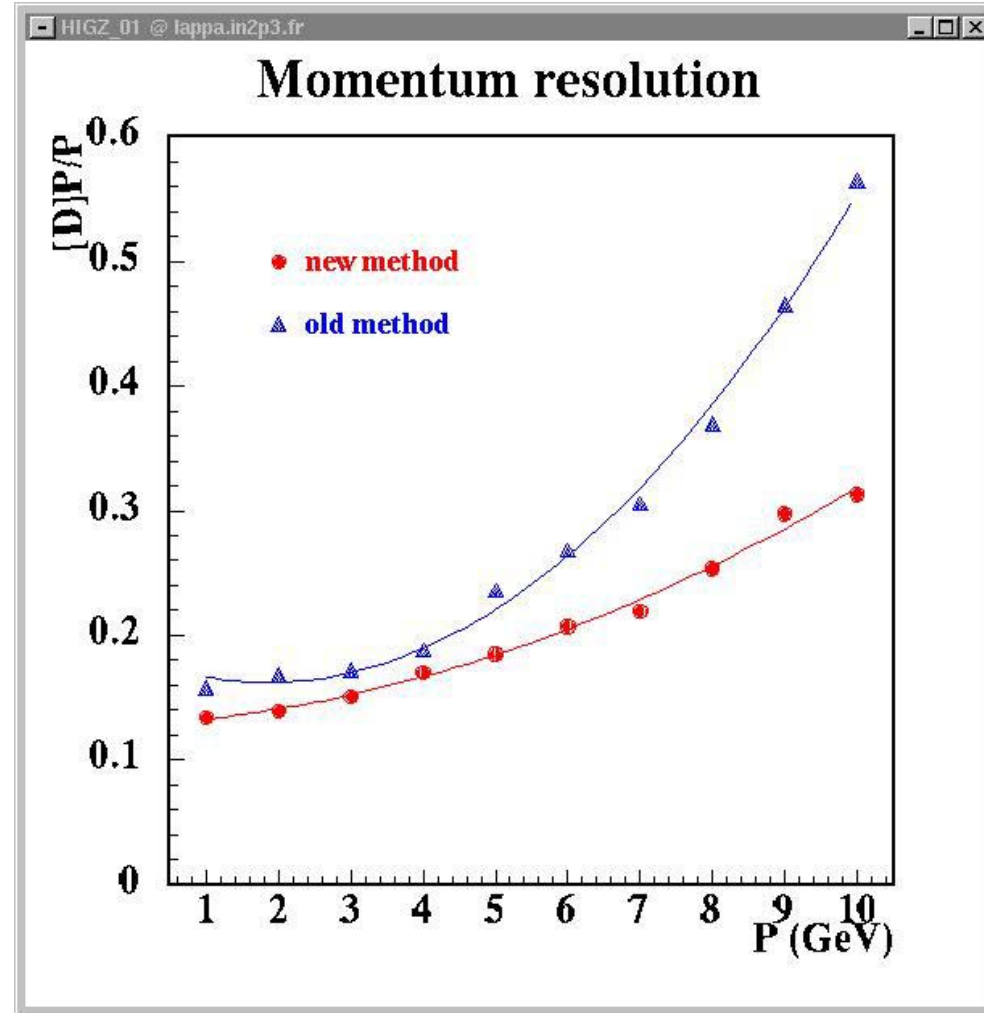
old parameterisation

$$\Delta P/P = 0.16 + 1.1 \times 10^{-2} p + 4.8 \times 10^{-3} p^2$$

new parameterisation

$$\Delta P/P = 0.13 + 4.3 \times 10^{-3} p + 1.6 \times 10^{-3} p^2$$

$\Delta P/P < 20\%$ for $p < 7$ GeV





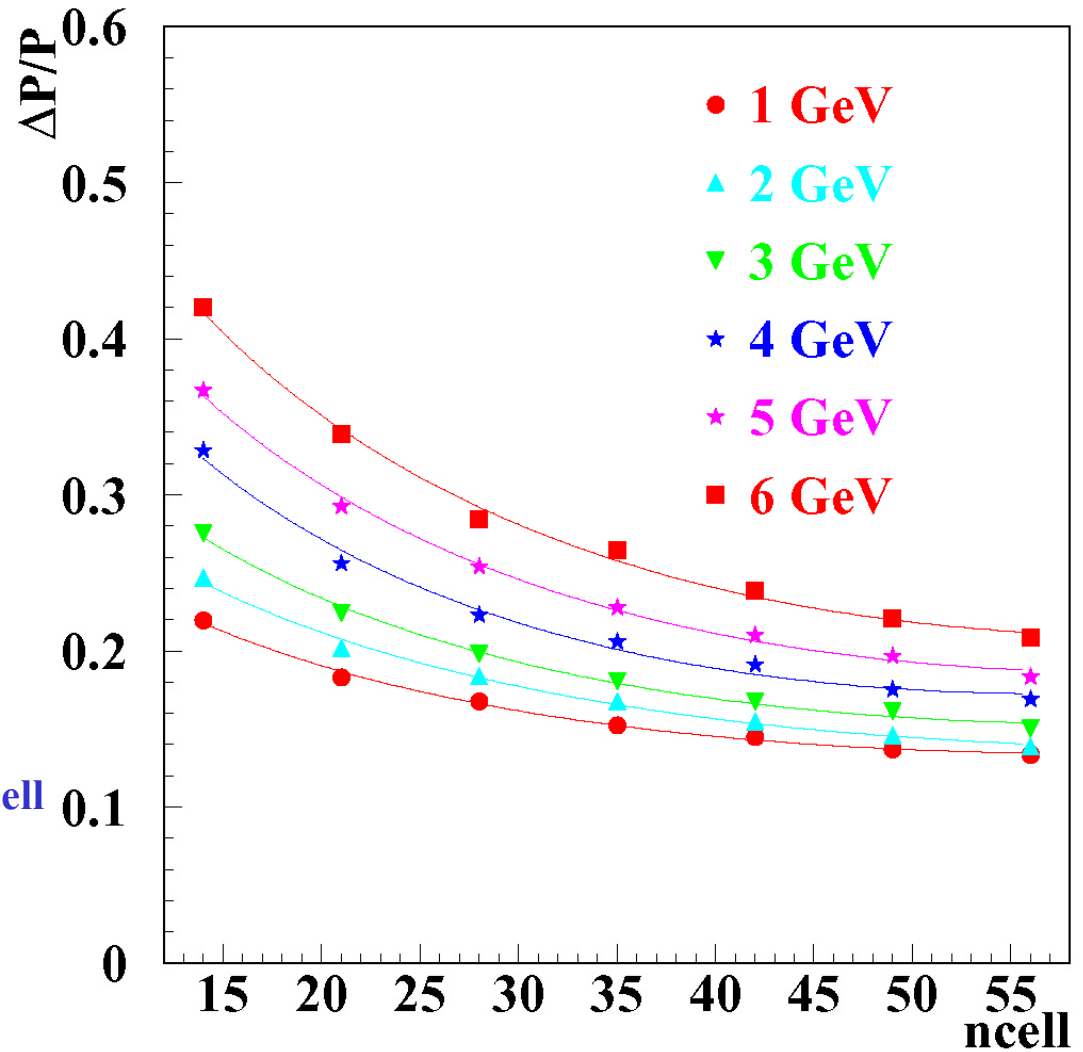
Momentum resolution as a function of the number of cells

$$\delta\theta = 2\text{mrad}$$

- Resolution $\Delta P/P$ has been estimated with 14, 21, 28, 42 and 56 cells for a fixed momentum

for a given p

$$\Delta P/P = c + d \times n_{\text{cell}}^{0.5} + e \times n_{\text{cell}}$$

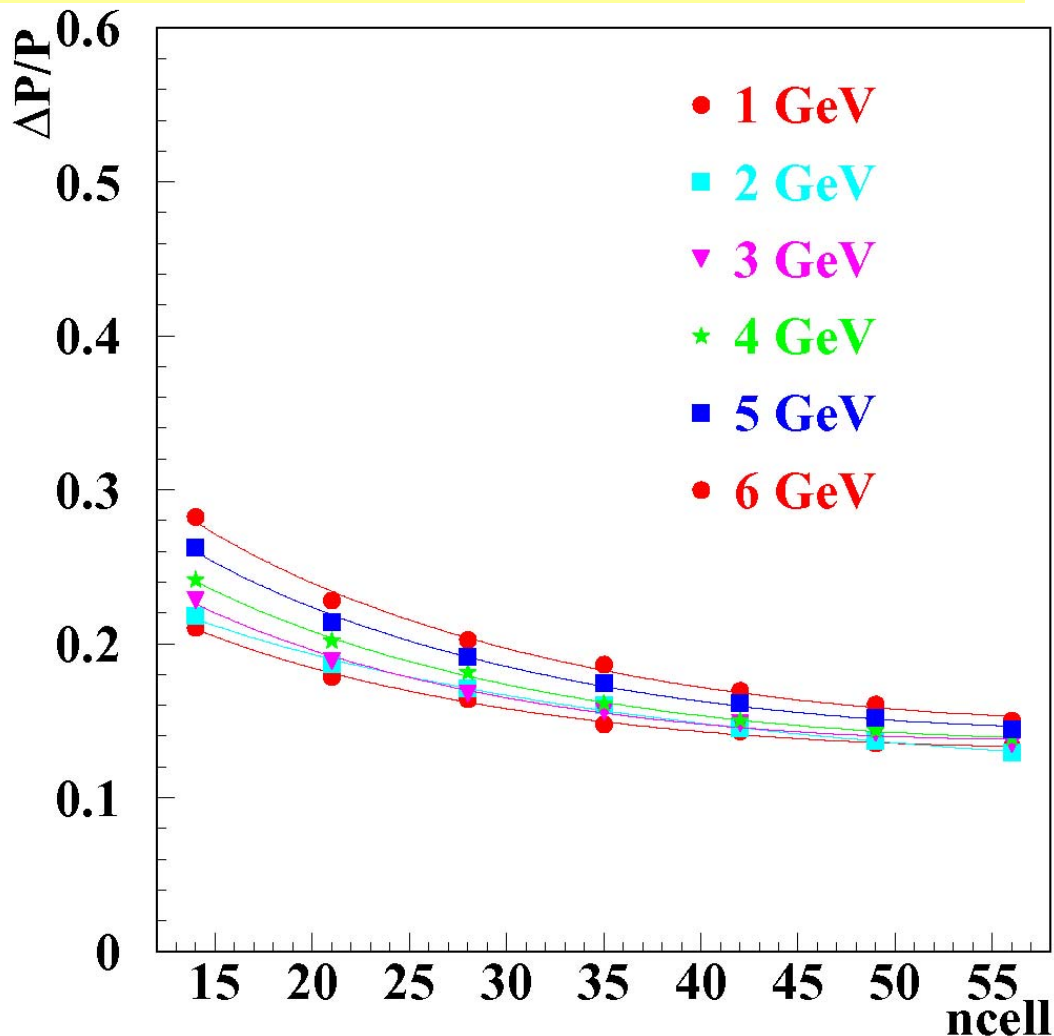




$\delta\theta=1\text{ mrad}$

- Resolution $\Delta P/P$ has been estimated with 14, 21, 28, 42 and 56 cells for a fixed momentum

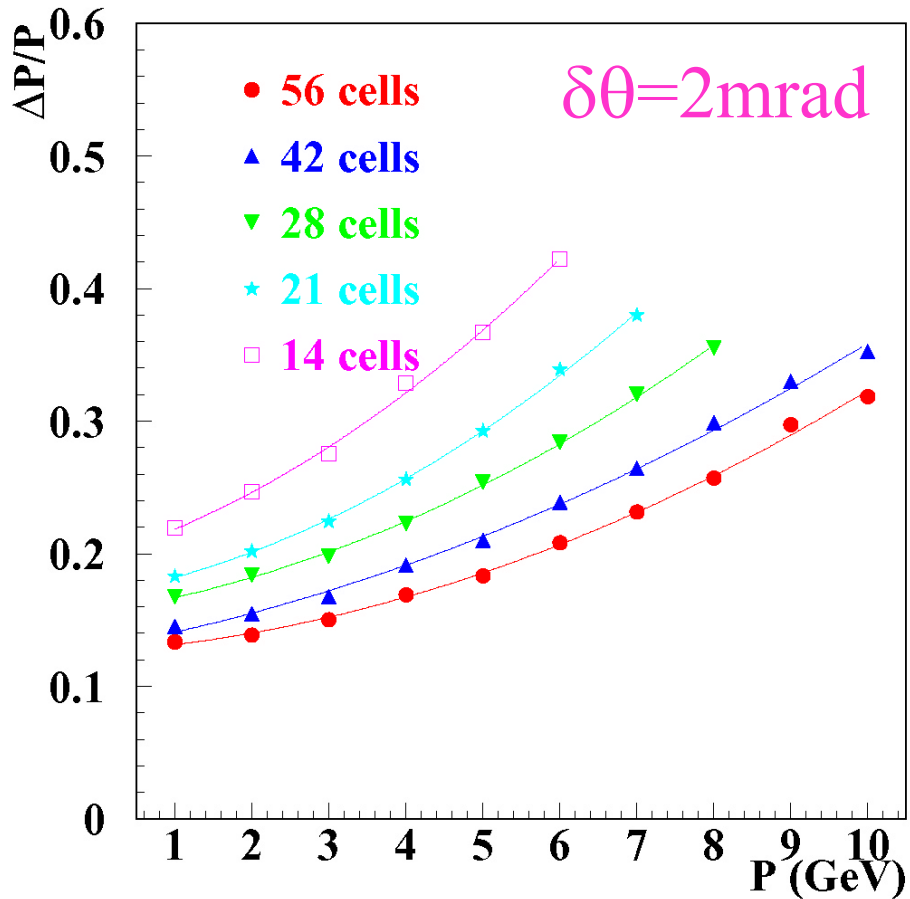
Momentum resolution as a function of the number of cells



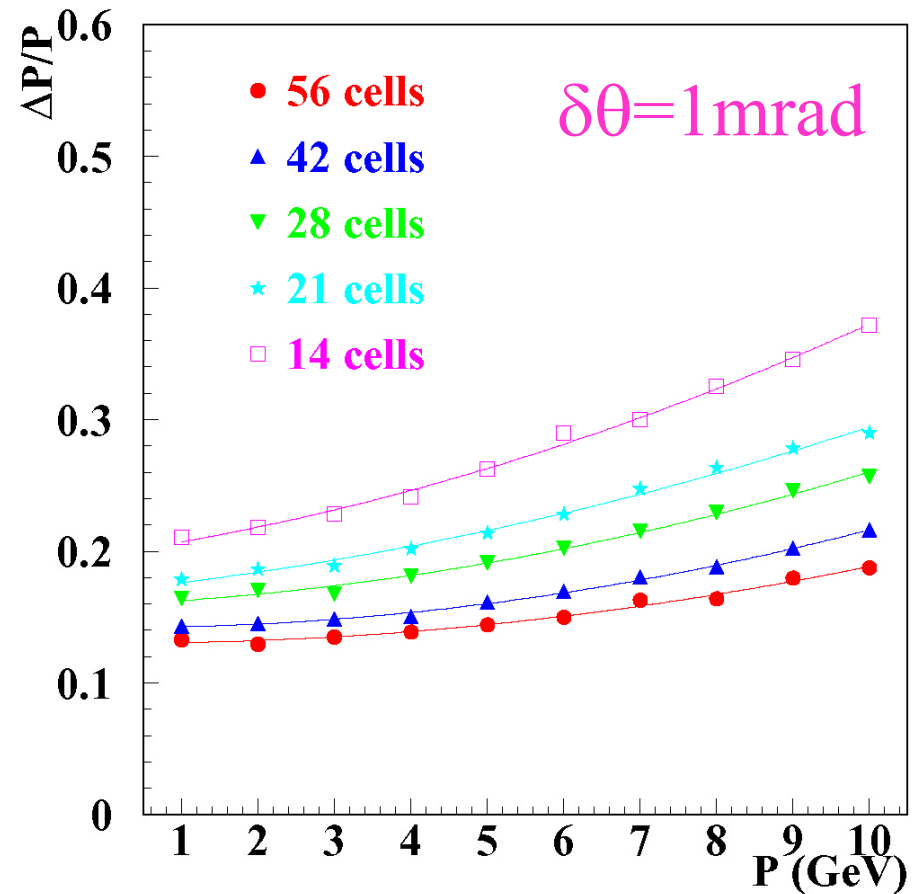
Results

$$\Delta P/P = a + b \times p + c \times p^2$$

Momentum resolution

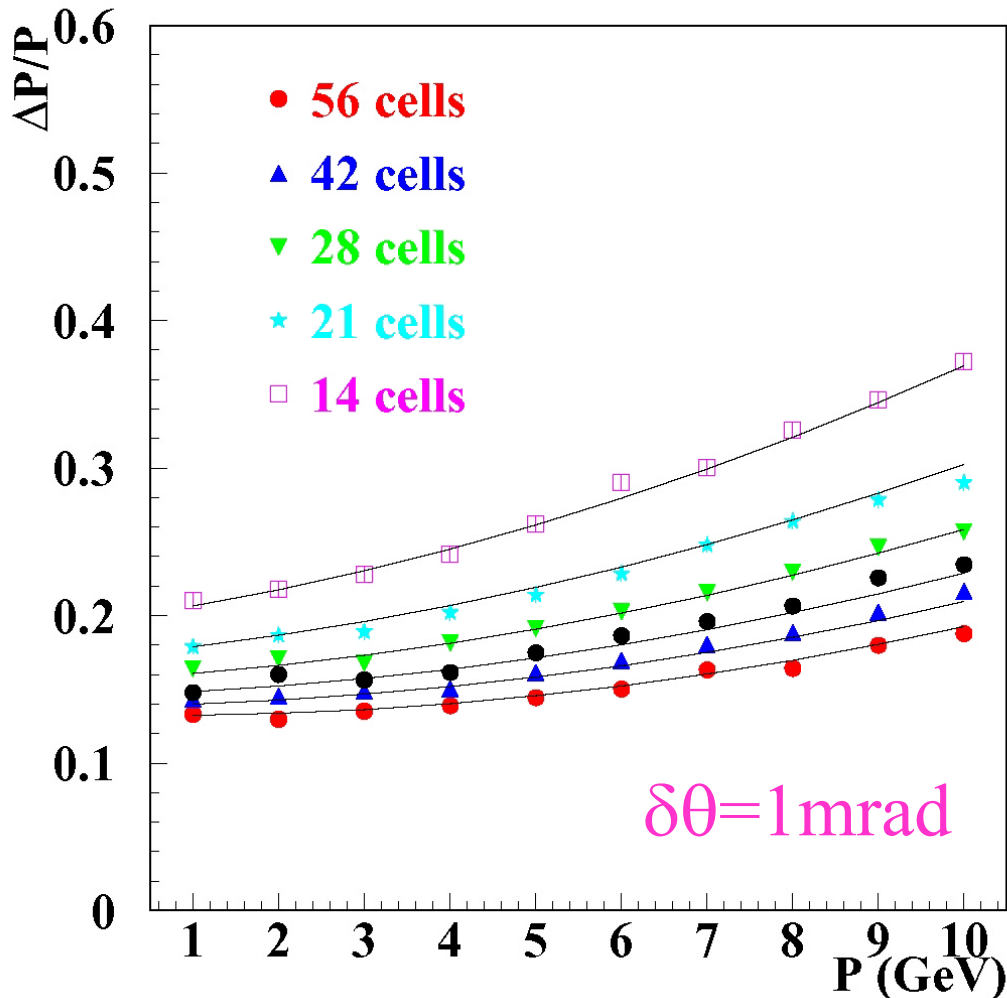


Momentum resolution



Global parametrisation with n_{cell} and p

$$\begin{aligned} \Delta P/P = & (0.37 + 0.028 \times p + 0.0020 \times p^2) \\ & - (0.062 + 0.0067 \times p + 0.00042 \times p^2) \times n_{\text{cell}}^{0.5} \\ & + (0.0040 + 0.00037 \times p + 0.000034 \times p^2) \times n_{\text{cell}} \end{aligned}$$

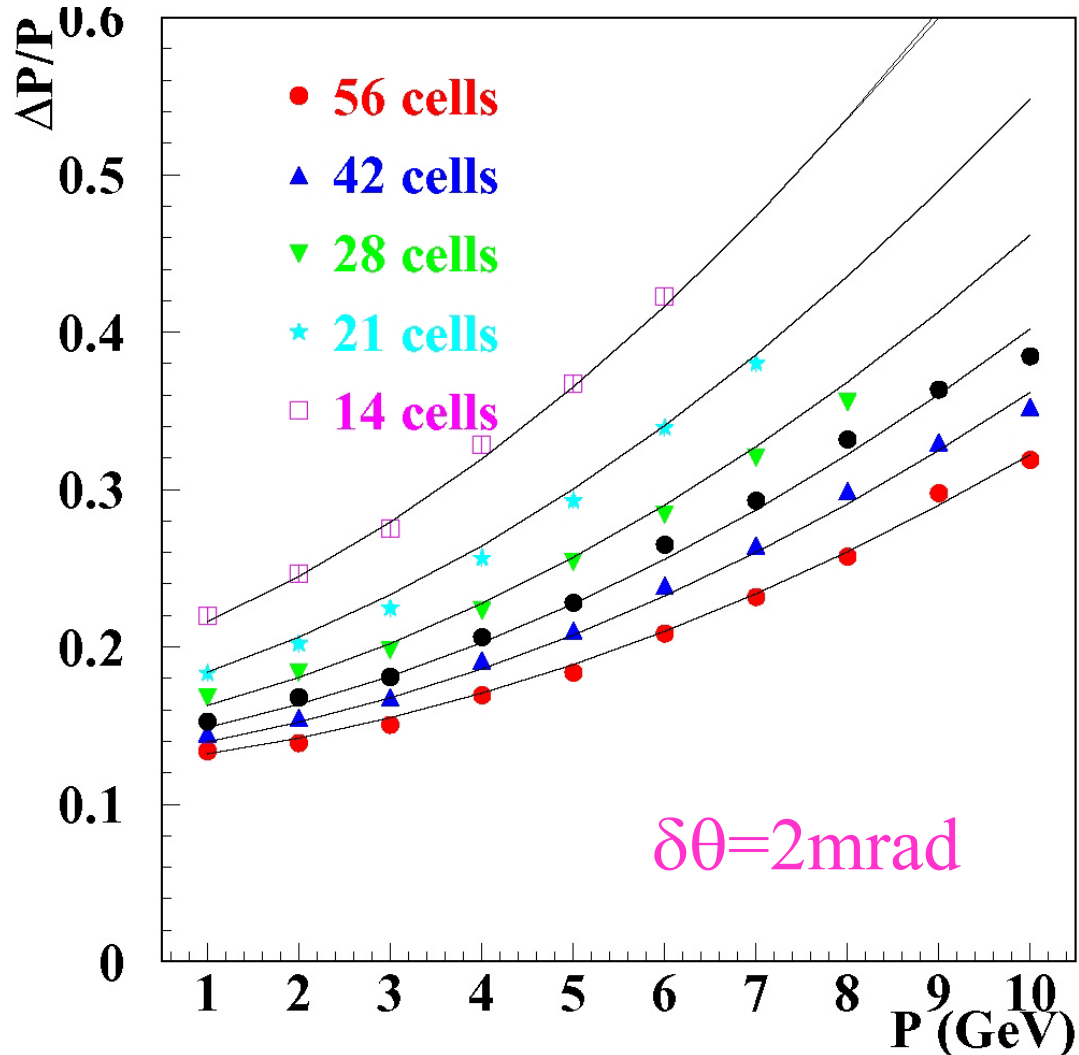


Global parametrisation with n_{cell} and p

$$\Delta P/P = (0.39 + 0.056 \times p + 0.0066 \times p^2)$$

$$- (0.070 + 0.012 \times p + 0.0013 \times p^2) \times n_{\text{cell}}^{0.5}$$

$$+ (0.0046 + 0.00074 \times p + 0.000083 \times p^2) \times n_{\text{cell}}$$





Conclusion

- An estimation of the momentum resolution is now possible for each momentum and each number of cells for 1 and 2 mrad resolution
- An update of the previous note is being written