A critical analysis of deeply bound kaonic states in nuclei. A critical analysis of the FINUDA experiment on deeply bound kaonic states in the pp system

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Unitarized Chiral Perturbation Theory

Skillful combination of the information of the Chiral Lagrangians and unitarity in coupled channels.

• Pioneering work of *Kaiser, Siegel, Waas, Weise 95-97* using Lipmann-Schwinger eq. and input from Chiral Lagrangians as potential.

Subsequent work

- Inverse Amplitude Method (IAM)
$$\rightarrow \begin{cases} Truong \\ Dobado, Peláez '97 \\ Oller, E.O., Peláez '98 \end{cases}$$

- (N/D) method
$$\rightarrow$$

Oller, E.O. '99
Oller, Meissner '01

- Bethe-Salpeter eq.
$$\rightarrow$$

Nieves, Ruiz-Arriola '00

(Ollar E.O. 107

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Meson-Baryon interaction



General scheme Oller, Meissner PL '01 (meson baryon as exemple)

• Unitarity in coupled channels $\bar{K}N$, $\pi\Sigma$, $\pi\Lambda$, $\eta\Sigma$, $\eta\Lambda$, $K\Xi$, in S = -1

- Dispersion relation

$$T_{ij}^{-1} = -\delta_{ij} \left\{ \hat{a}_i(s_0) + \frac{s - s_0}{\pi} \int_{s_i}^{\infty} ds' \frac{\sigma(s')_i}{(s - s')(s' - s_0)} \right\} + V_{ij}^{-1} \equiv -g(s)_i \delta_{ij} + V_{ij}^{-1}$$

g(s) accounts for the right hand cut



V accounts for local terms, pole terms and crossed dynamics. V is determined by matching the general result to the χPT expressions (usually at one loop level)

$$g(s) = \frac{2M_i}{16\pi^2} \left\{ a_i(\mu) + \log \frac{m_i^2}{\mu^2} + \frac{M_i^2 - m_i^2 + s}{2s} \log \frac{M_i^2}{m_i^2} + \frac{q_i}{\sqrt{s}} \log \frac{m_i^2 + M_i^2 - s - 2q_i\sqrt{s}}{m_i^2 + M_i^2 - s + 2q_i\sqrt{s}} \right\}$$

 μ regularization mass a_i subtraction constant

Inverting T^{-1} :

$$T = [\mathbf{1} - Vg]^{-1}V$$

Example 1: Take $V \equiv$ lowest order chiral amplitude

In meson-baryon S-wave

$$[1 - Vg]T = V \rightarrow T = V + VgT$$

Bethe Salpeter eqn. with kernel V

This is the method of E. O., Ramos '98 using cut off to regularize the loops

Oller, Meissner show equivalence of methods with

$$a_i(\mu) \simeq -2\ln\left[1 - \sqrt{1 + \frac{m_i^2}{\mu^2}}\right];$$

$$\mu \text{ cut off}$$
$$a_i \simeq -2 \rightarrow \mu \simeq 630 \text{ MeV in } \bar{K}N$$

If higher order Lagrangians not well determined then fit a_i to the data





Evidence for the two pole structure of the $\Lambda(1405)$

One does many body corrections in the KN amplitude tis) -> Z(q,p) KT TN $\Rightarrow \Pi_{\bar{\kappa}} (q^{\circ}, q, p) = 2 \int \frac{d^{3}p}{(2\pi)^{3}} n(\vec{p}) \left[\tilde{t}_{\bar{\kappa}p}(q, p) + \tilde{t}_{\bar{\kappa}n}(q, p) \right]$ $\frac{1}{p^{\circ}-\varepsilon_{1}p^{\circ}+i\varepsilon} + \frac{n_{1}p^{\circ}}{p^{\circ}-\varepsilon_{1}p^{\circ}-\varepsilon_{2}p^{\circ}-i\varepsilon} \qquad Pauli blocking Koch 94$ Pauli blocking Waas, weize 97Shifts the A(1405) at higher energiesLutz 98 KSelfconsistentLutz 98SelfconsistentLutz 98SelfconsistentBrings backSelfconsistentUse of K selfenergyTPBin the loopsTPB the free position Ramos, E.O. Sefcons. K V V V NPA (2000) + π selfenergy + mean field Opens new baryon potential decay channed PB Vier for different Baryons and widens spectral function

Medium decay channels $\vec{\mathbf{x}} \Rightarrow (\vec{\mathbf{z}} \mathbf{h}) \pi , (\mathbf{h}) \pi$ Koch Waas Weise $\bar{\kappa} \rightarrow (\Xi h)(ph)\pi (\Lambda h)(ph)\pi$ Lutz K→ (Eh)(ph), (1h)(ph) Ramos T. extra (Eh)(ph) n, (Ah)(ph) n addition we have p-wave K selfenergy from the existation N () = * (1385) Couplings related to SU(3) well. D. F. of original chival Lagrangian

FIG. 7. Real (top) and imaginary (bottom) parts of the K^- optical potential as a function of density obtained from the *In-medium pions and kaons* approximation. Results are shown for three different K^- energies: $\omega = m_K - 45$ MeV (dotted lines), $\omega = m_K$ (solid lines) and $\omega = m_K + 20$ MeV (dashed lines).

Similar results in Schaffner-Bielich, Koch, Effenberg Cieply, Friedman, Gal, Mares NPA 2000

Claims for deeply bound Kaon atoms

Theoretical claim of deep potential, Y. Akaishi and T. Yamazaki, Phys. Rev. C 65 (2002) 044005. Quoting the authors textually,

"we construct phenomenologically a quantitative $\bar{K}N$ interaction model that is as simple as possible using free $\bar{K}N$ scattering data, the KpX data of kaonic hydrogen and the binding energy and width of $\Lambda(1405)$, which can be regarded as an isospin I=0 bound state of $\bar{K} + N$ ".

They use as input $v_{\bar{K}N,\bar{K}N}$, $v_{\bar{K}N,\pi\Sigma}$, $v_{\bar{K}N,\pi\Lambda}$, which are fitted to data, and set $v_{\pi\Sigma,\pi\Sigma}$, $v_{\pi\Lambda,\pi\Lambda}$ equal zero "to simply reduce the number of parameters".

The last condition implies that they miss the second pole of the $\Lambda(1405)$

The chiral Lagrangian gives

 $v_{\pi\Sigma,\pi\Sigma} = \frac{4}{3} v_{\bar{K}N,\bar{K}N}$

Theoretical claims

The claim of the $\Lambda(1405)$ as a bound state of KN is not supported by the chiral theory. This assumption leads to a I=0 $\overline{K}N$ amplitude below threshold twice as big as a standard chiral amplitude.

AY take into account Pauli Blocking of intermediate states to get \bar{K} nucleus potential.

For the A=3 and 4 systems leads to binding energies of the kaon of the order of 70 MeV with widths around 75 MeV, (from $K^-N \rightarrow \pi \Sigma$).

Next, the nucleus is allowed to shrink to densities $\rho = 10\rho_0$

Then, K^- bound in ${}^{3}He$ by 108 MeV and in ${}^{4}He$ by 86 MeV

 $\Gamma = 20 - 24 \text{ MeV from } K^- p \rightarrow \pi \Lambda$

Extra defficiencies in the K^- potential

No selfconsistency in the calculation: Overestimate

No many body decay channels, $K^-NN \rightarrow \Lambda N, \Sigma N$

Rough estimate made of these channels, $\Gamma = 12 M eV$

More realistic is 22 MeV at $\rho = \rho_0$

But if $\rho = 10\rho_0$, $\Gamma = 2000 MeV$, or at least 200 MeV if ρ_{av} is used.

Experimentalist "find" a possible deeply bound K^- state. Suzuki et al. PLB597 (2004)

 $K^{-4}He \rightarrow Sp$, S(3115) Strange tribaryon. But I=1, and if K^{-} state, B=195 MeV

Contradiction with AY with I=0 and 108 MeV!!

The saga continues

AY strike back:

Introduce relativistic corrections (use Klein Gordon equation) (The chiral theories always did)

some spin orbit corrections

Increase ad hoc the $\bar{K}N$ interaction

B=195 comes out then

At this point the K^- potential in the center of the nucleus has become 618 MeV!!!

Experimental reconversion: Sato in BadHonnef, PANIC05... claim the state seen is indeed a K^- bound state.

Discussion of the KEK experiment, Suzuki et al.

- Kaons at rest absorbed: $K^{-4}He \rightarrow S p$, They see a peak in the p spectrum around 500 MeV/c.
- Auger emission of the p. Binding energy taken by K^- .
- Alternative explanation

.. Many possible conventional mechanisms studied and discarded

- The one passing all tests
- $K^-NN \to \Lambda N$ $p_N = 562 MeV/c$
- $K^-NN \rightarrow \Sigma N$ $p_N = 488 MeV/c$ The other nucleons left as spectators
- exp. peak seen at $p_p = 475 MeV/c$ (some energy loss in thick target) But what about a peak at $p_p = 562 MeV/c$ from K^- mp

But what about a peak at $p_p = 562 MeV/c$ from $K^-pp \rightarrow \Lambda p$?

Suzuki et al NEK

Further tests of K^- absorption mechanism

- Peak at 545 MeV/c seen in experiment !!
- Further tests
- $K^- pp \to \Lambda p$ $\Lambda \to \pi N \quad p_\pi = [61 - 146] MeV/c$
- $K^- pp \to \Sigma p$ $\Sigma \to \pi N \quad p_\pi = [162 - 217] MeV/c$
- A cut in the pion momenta could help Test partially done: cut done that accepts 90 % of 255 MeV/c ("fast pions") and complementary
- Peak from $K^-pp \rightarrow \Sigma p$ seen in boths cuts
- Peak from $K^-pp \to \Lambda p$ seen in basically only the non "fast pions"

Further considerations

- Why more strength in Σp peak than in Λp peak?
- Katz et al. PRD 1 (70) $K^{-4}He \rightarrow$

- 2.3 % for Σ^0 and 9.4 % for Λ , using isospin symmetry
- Another estimate

$$\frac{Y\left(\Sigma^{0}NN\right)}{Y\left(\Lambda NN\right)} = \frac{\sigma(K^{-}p \to \pi^{0}\Sigma^{0})}{\sigma(K^{-}p \to \pi^{0}\Lambda)} \tag{1}$$

This ratio is about 1 experimentally

- Using these estimates: ratio of Σp to Λp about [1.2-2.5]
- Rates of K^- absorption around 1%, in agreement with strength of peak estimated by Suzuki.

Further tests

- These peaks should be seen in other nuclei!!, what can we predict?
- In K⁻ absorption two protons are removed. Binding energy smaller than 28 MeV of ⁴He breakup. Hence, bigger energy of emitted p in heavier nuclei.
- Estimates

502 MeV/cfor Σp 574 MeV/cfor Λp

- FINUDA sees peaks in ⁷Li (and other nuclei) at 505 MeV/c and 570 MeV/c
- Peaks should get narrower in heavier nuclei, because of smaller recoil energy of the nucleus
- Signals should gradually disappear for heavier nuclei because of p distortion These are indeed features of the FINUDA experiment

FINUDA experiment, M. Agnello et al. PRL 94 (2005)

- K⁻ absorption at rest from ⁶Li,⁷Li,¹²C.... They look for events back to back. Find two peaks in Λp invariant mass: a narrow one at higher energies and a broad one at lower energies. The latter is identified with a bound K⁻ state.
- Cuts: $p_{\Lambda} > 300 MeV/c$ to eliminate $K^-p \rightarrow \Lambda \pi$ $|cos(\theta)| > 0.8$
- Narrow peak identified as K⁻pp → Λp removing binding energy Broad one at lower energies: "bound K⁻ state in pp " with B=115 MeV.
- Questions:

where does the binding energy of the kaon go? Where is the strength if $K^-pp \rightarrow \Lambda p$ exciting the nucleus (largest part)?

i) Invariant-mass distribution of a proton and a π^- for all the events in which these two particles are observed, ssian together with a linear background in the invariant-mass range of 1100–1130 MeV/ c^2 . (b) Opening angle A and a proton: solid line, ⁶Li, ⁷Li, and ¹²C; dashed line, ²⁷Al and ⁵¹V. The shaded area ($\cos\theta^{Lab} < -0.8$) is select the event.

FIG. 3. Invariant mass of a Λ and a proton in back-to-back correlation ($\cos\theta^{\text{Lab}} < -0.8$) from light targets before the acceptance correction. The inset shows the result after the acceptance correction for the events which have states before the acceptance correction for the events which have states and between 2.22 and

Our description of the peaks

- We run a computer simulation code for K^- absorption in nuclei by pp and pn pairs:
- $|\Psi(r)|^2$ distribution for K^- peaked around surface of nucleus
- *K*⁻ absorbed by pp or pn, with momenta randomly chosen from local Fermi sea.
- energy and momentum conservation including nuclear potential
- Λp , Λn emitted according to phase space
- p, n have further collisions

 pN -> p' N
 np -> pn
 (fast n to fast p)
 done according to *σρ* probability per unit length and
 experimental angular distributions (*σ*_Λ = ²/₃*σ_N*)
- Λp invariant mass reconstructed from final events.

Analysis of first peak: g.s. formation of residual nucleus

- Analogy to α decay: p and Λ survival probability without collisisions times formation probability.
- Survival probability P= $exp(-\int \sigma \rho dl)$ Calculated by MC simulation, P ~ 0.4
- Formation probability:

 $|<\Phi(r,A-2,final)|\Phi(r,A-2,initial)>|^2, \ |\sim 0.3-0.7|^2$

- Rate of g.s. formation $\sim 0.4 * 0.25 \sim 0.1$
- THE LARGEST PART OF THE K⁻ ABSORPTION EVENTS GO INTO NUCLEAR EXCITATION, MOSTLY TO THE CONTINUUM where is this strength in the experiment?

PVIO VP 1P x-t: -> PP SH g.s Schematic exitation little overlag with 5H breakup channels Giessen, Bonn A critical analysis of deeply bound kaonic states in nuclei - p.30/4

MC simulation of K^- absorption: inclusive

- The MC simulation is done as described before This has been applied with success to other physical problems: (e,e') inclusive reactions
 - (π,π') inclusive reactions
 - (p,p') inclusive reactions
- In all tese processes a distinct peak appears which collects most of the strength: the quasielastic peak The QSE peak comes mostly from one collision of the particles exciting the nucleus to the continuum
- In the present case this QSE peak comes from the collision of the p (or Λ) after $K^-NN \rightarrow \Lambda N$
- THE QSE PEAK ACCOUNTS FOR THE SECOND PEAK OF THE FINUDA EXPERIMENT

 ^{12}C Results imposing the experimental angle cut for back to back events, $\cos\Theta_{ec{p}_\Lambdaec{p}_p} <$

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-0.8, and up to three collisions. 3d orbit.

⁶*Li*. K^- absorption from 2p orbit.

⁷*Li*. K^- absorption from 2p orbit.

 $^{27}Al. K^{-}$ absorption from 3p orbit.

⁵¹*V*. K^- absorption from 4f orbit.

Other channels studied

- $K^-pp \rightarrow \Sigma^+n$, $\rightarrow \Sigma^0 p$ followed by, $\Sigma^+n \rightarrow \Lambda p$, $\Sigma^0 p \rightarrow \Lambda p$ this peaks around the third experimental peak and has smaller strength than $K^-pp \rightarrow \Lambda p$
- $K^-pp \rightarrow \Sigma^0 p$ $\Sigma^0 \rightarrow \Lambda \gamma$, $\sqrt{s} = 2240 - 2300 MeV$ hence, (Λp) invariant mass in QES peak and all events back to back strength smaller, $\sim 10 - 30$ percent of $K^-pp \rightarrow \Lambda p$ events.

Conclusions

- The K⁻ optical potential on which predictions of narrow deeply bound K⁻ states was done is overly exagerated and incomplete in the decay channels.
- The KEK and FINUDA experiment do not have any support for the interpretation of the data as bound kaons except the "theoretical predictions" of the mentioned work.
- We have shown that all the peaks can be interpreted in terms of K⁻ absorption on pairs of nucleons, in KEK with remnant nucleus as spectator in FINUDA, first peak with remnant nucleus as spectator second peak with nuclear excitation to the continuum
- These mechanisms passed all tests for which there were available data.

Pole positions of the *T* matrix in the complex *W* plane. The triangles, diamonds, squares and circles correspond to the "WT", "c", "*s*" and "*u*" approach, respectively. The dashed lines represent the K^-p and \bar{K}^0n cuts, respectively. Right: Pole positions of the *T* matrix in the complex *W* plane. The circles, triangles and squares correspond to the fits "1", "2" and "3", respectively.

Summary of DHD06 Workshop, Kyoto Feb 2006

- Akaishi strikes back, confusion of cut off in fi eld theory and range of interaction.
 No selfconsistency yet, still 10ρ₀ density.
- Yamazaki strikes back, makes wrong assumption on fi nal state in $K^{-4}He$ absorption going to $p\Sigma nn$ instead of $p\Sigma d$ (small recoil energy of d, 10 MeV for 200 MeV/c of Fermi motion). Misses the experimental fact of the narrow signal in FINUDA for K^{-} absorption without extra fi nal state interaction. Disguised offer of compromise, peaks partly from K^{-} absorption and partly from production of tribaryon. Compromise rejected: too much coincidence that the peaks appear in all nuclei at the K^{-} absorption kinematics.
- No help from any body else of the japanese community.
- No claims in the experimental talks about deeply bound kaon atoms. Back to tribaryon claim.
- Iwasaki pledge "please understand all this is still preliminary, we are working to understand what happens"
- The paper of 2003 with claims for deeply bound K from the $K^-(at \ rest)$ absorption in 4He , (K^-, n) has been withdrawn.

Summary of DHD06 Workshop, Kyoto Feb 2006

- Y. Yamagata presents calculations of (K⁻, p) in flight and concludes that even if there are deeply bound kaon states the signal would be too weak to be seen in present experiments.
- S. Okada (Hayano exp.) presents results for 3d → 2p X-rays of Kaonic Helium. 2p shift: Old experiments 40 eV, chiral unitary model 0.2 eV, Akaishi potential 11 eV.
 New experiment compatible with zero with 3-4 eV precision.