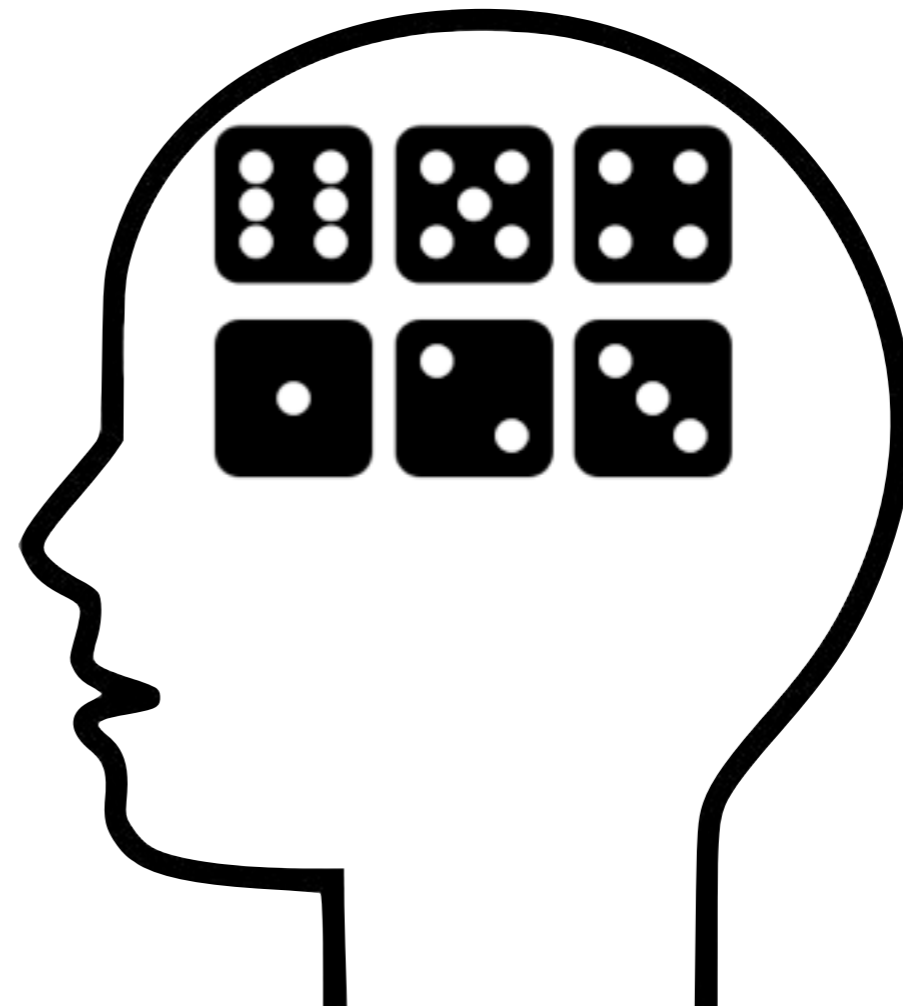


Why Monte Carlo generators? Theory point of view

A. Bacchetta
“TMD Monte Carlo”
Frascati, 7 Nov 2011



Two types of generators

Two types of generators

- Full event generators (Pythia, Lepto...)
All final-state particles are generated

Two types of generators

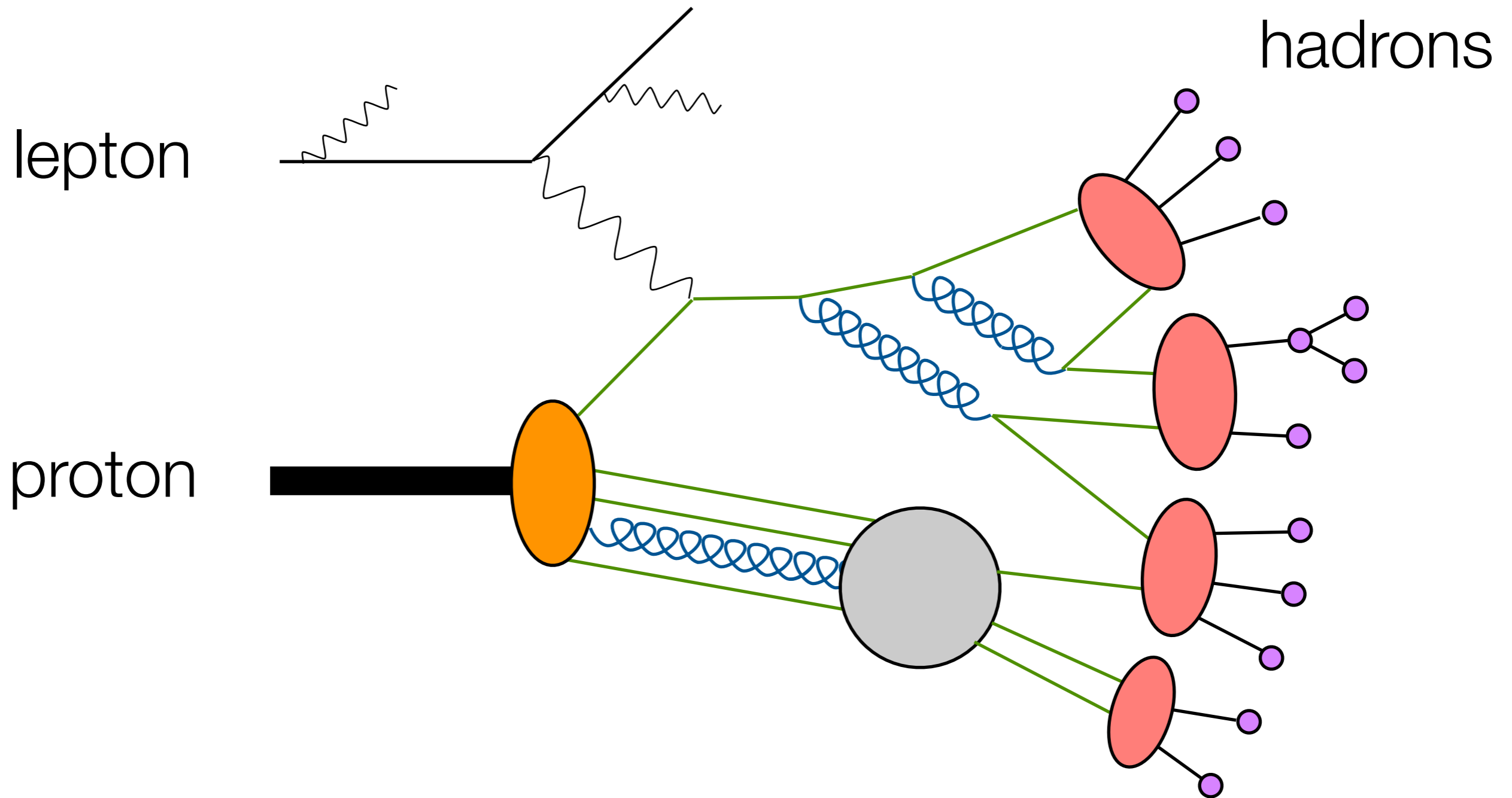
- Full event generators (Pythia, Lepto...)
All final-state particles are generated

Two types of generators

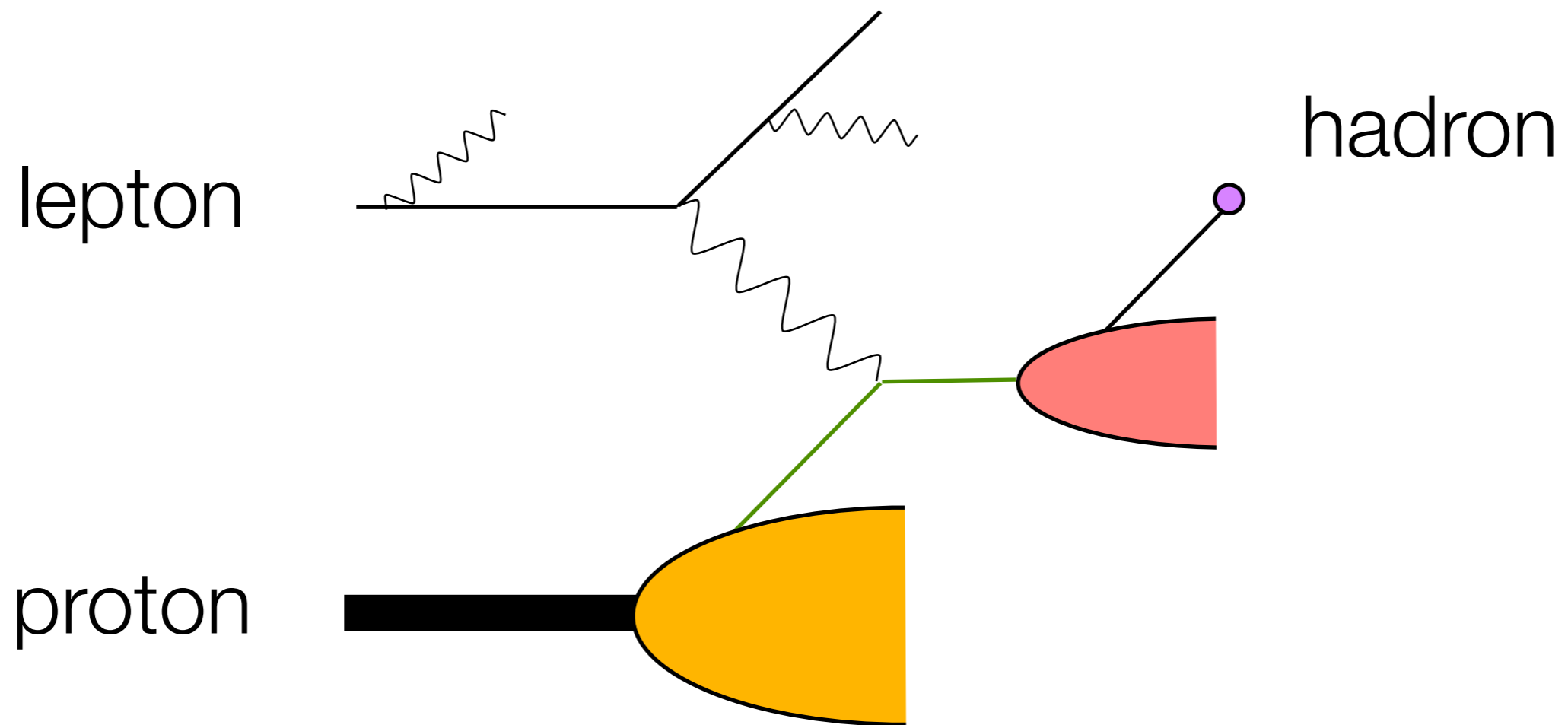
- Full event generators (Pythia, Lepto...)
All final-state particles are generated

- Generators for single-particle (or two-particle) inclusive DIS (gmc_trans, TMDgen, ResBos...)
Only one or two final-state particles are generated

Full event generator

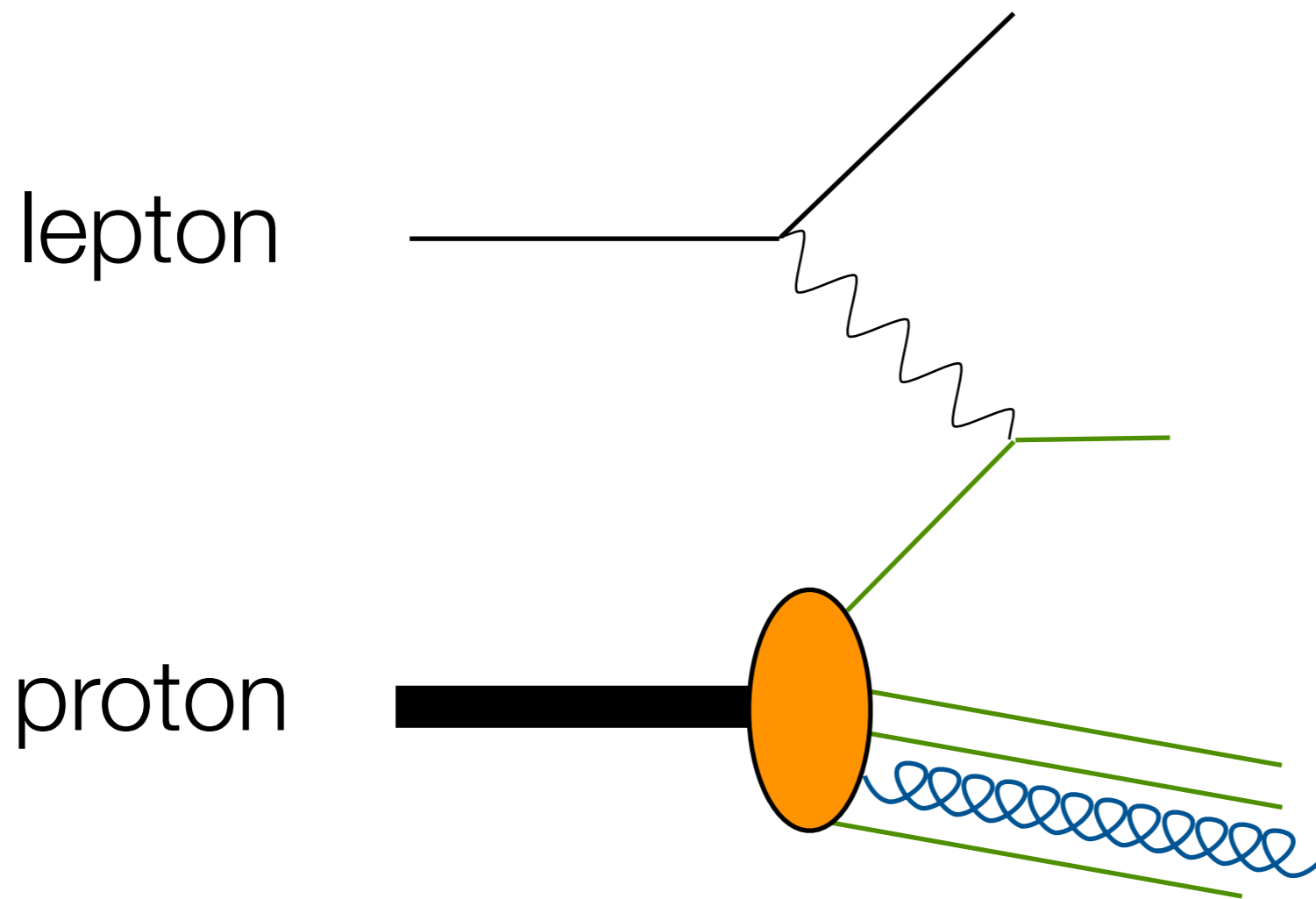


Single-particle DIS generator

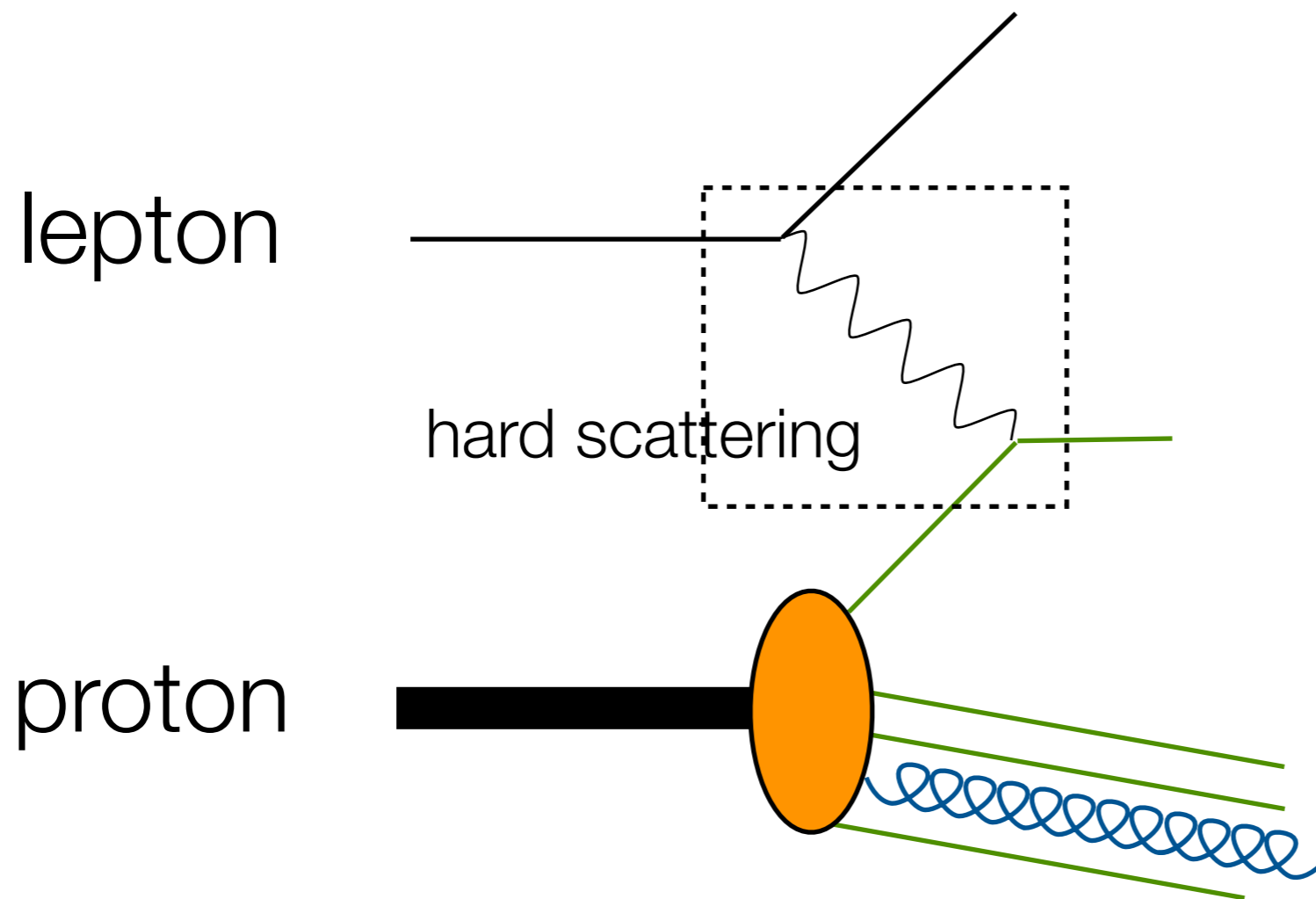


Something about full event generators

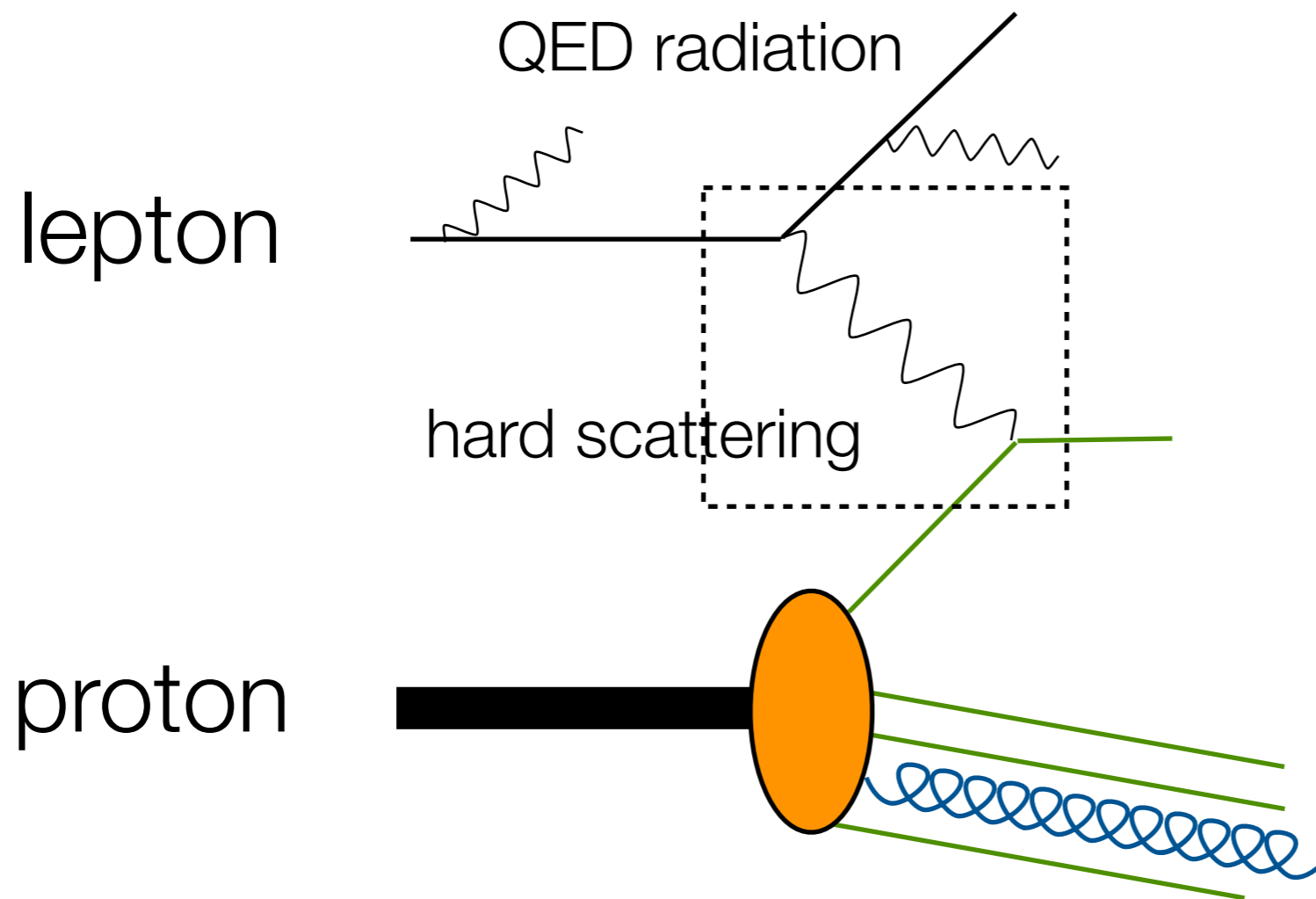
Full event generator



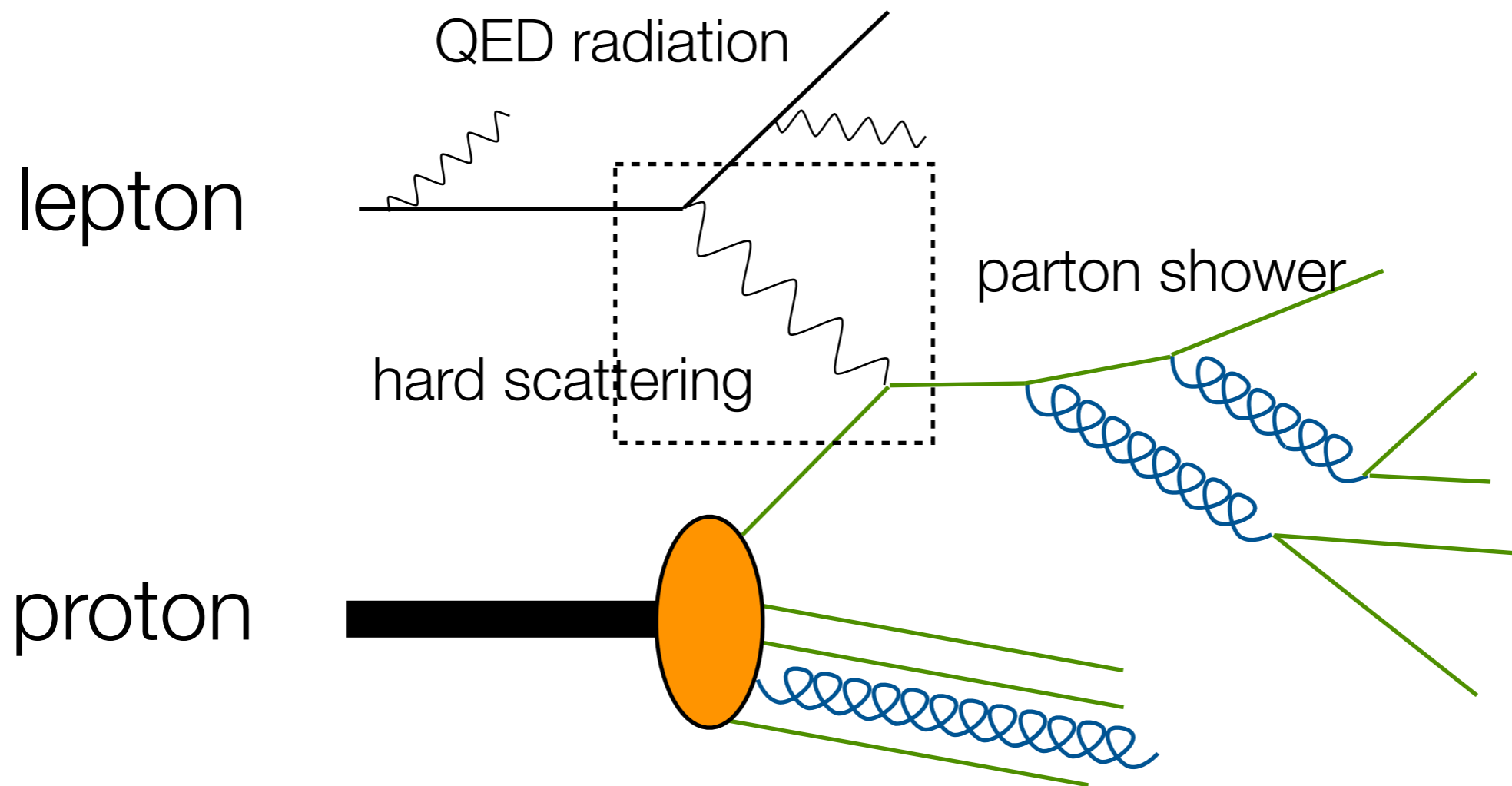
Full event generator



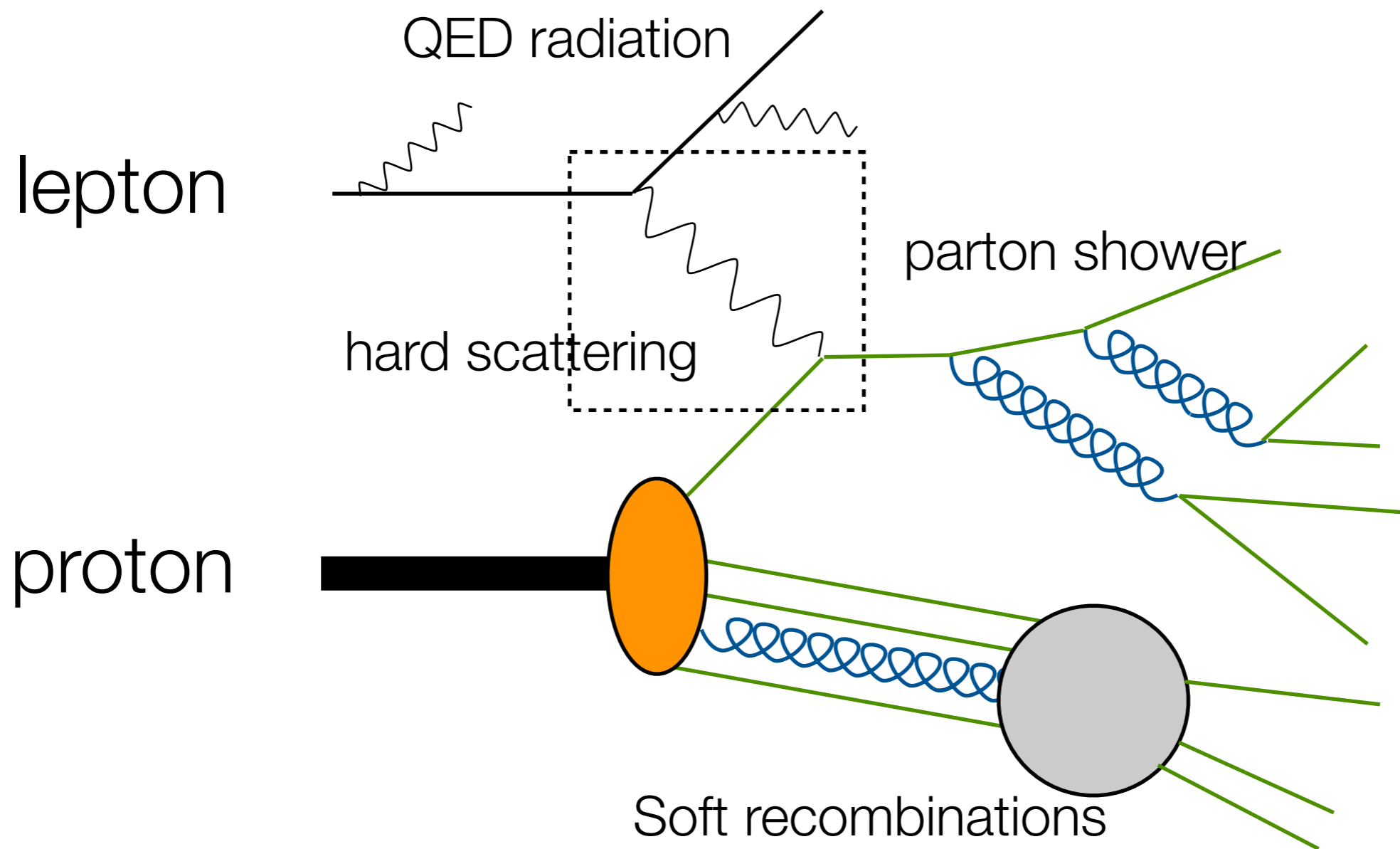
Full event generator



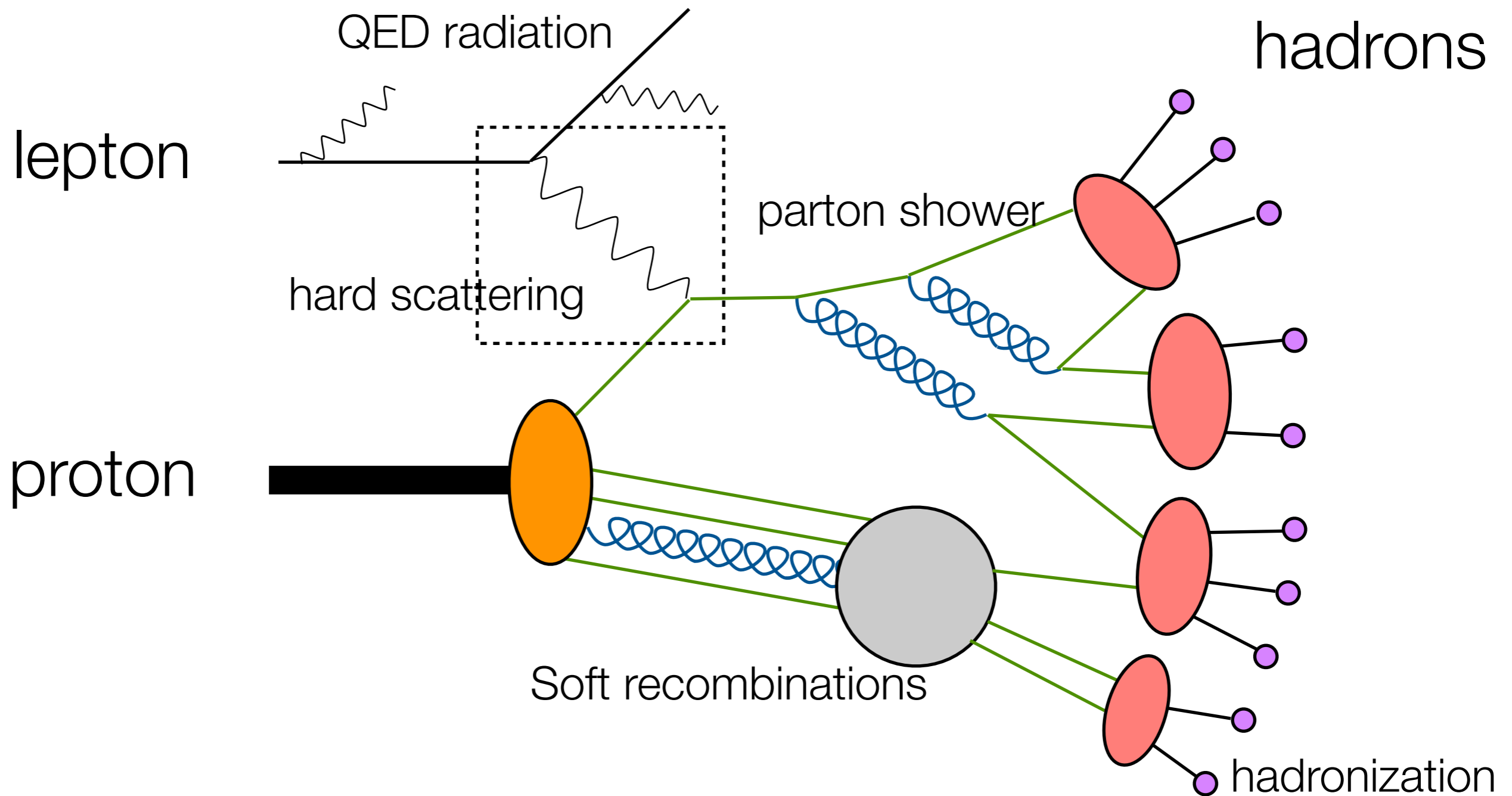
Full event generator



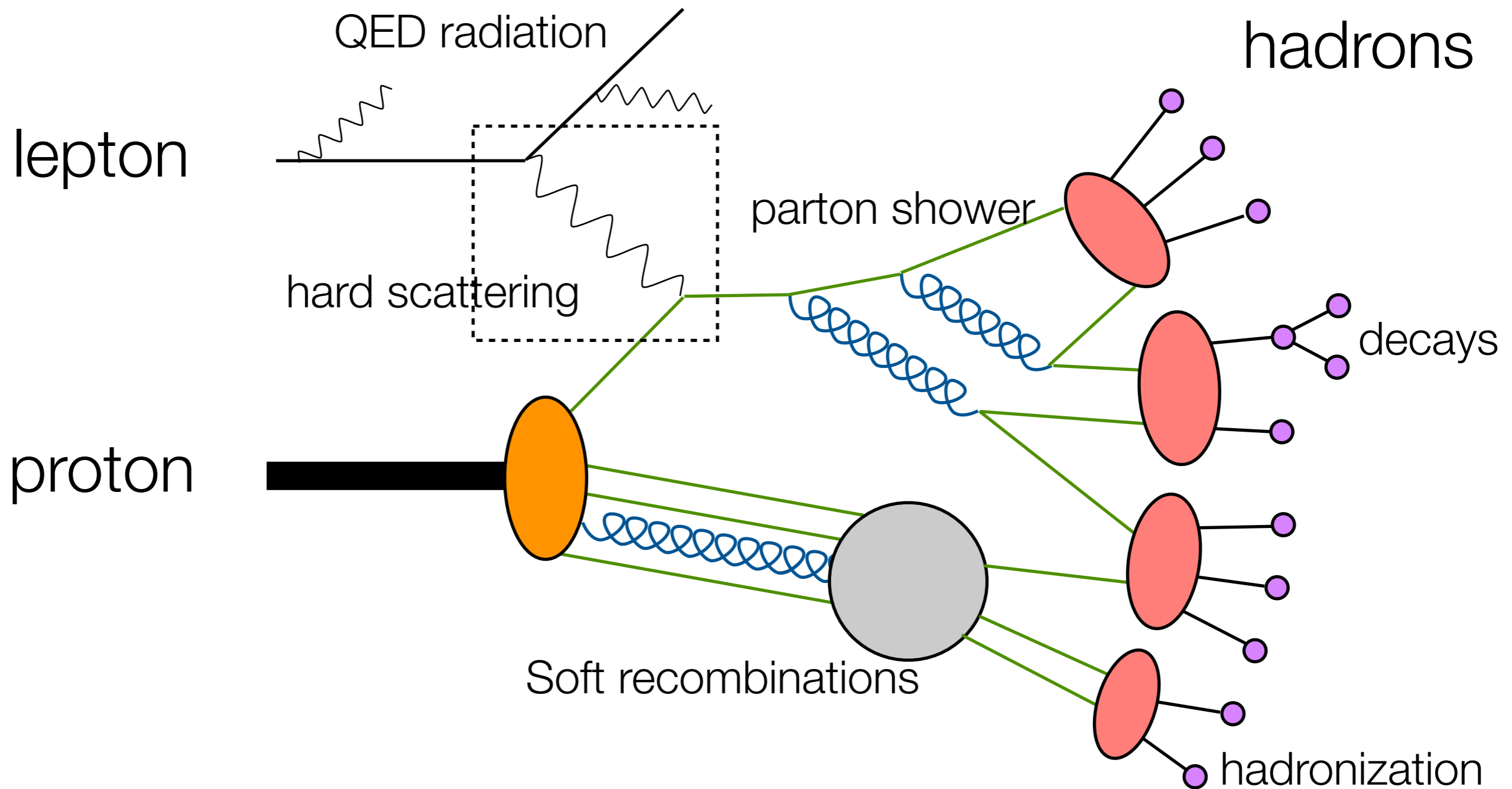
Full event generator



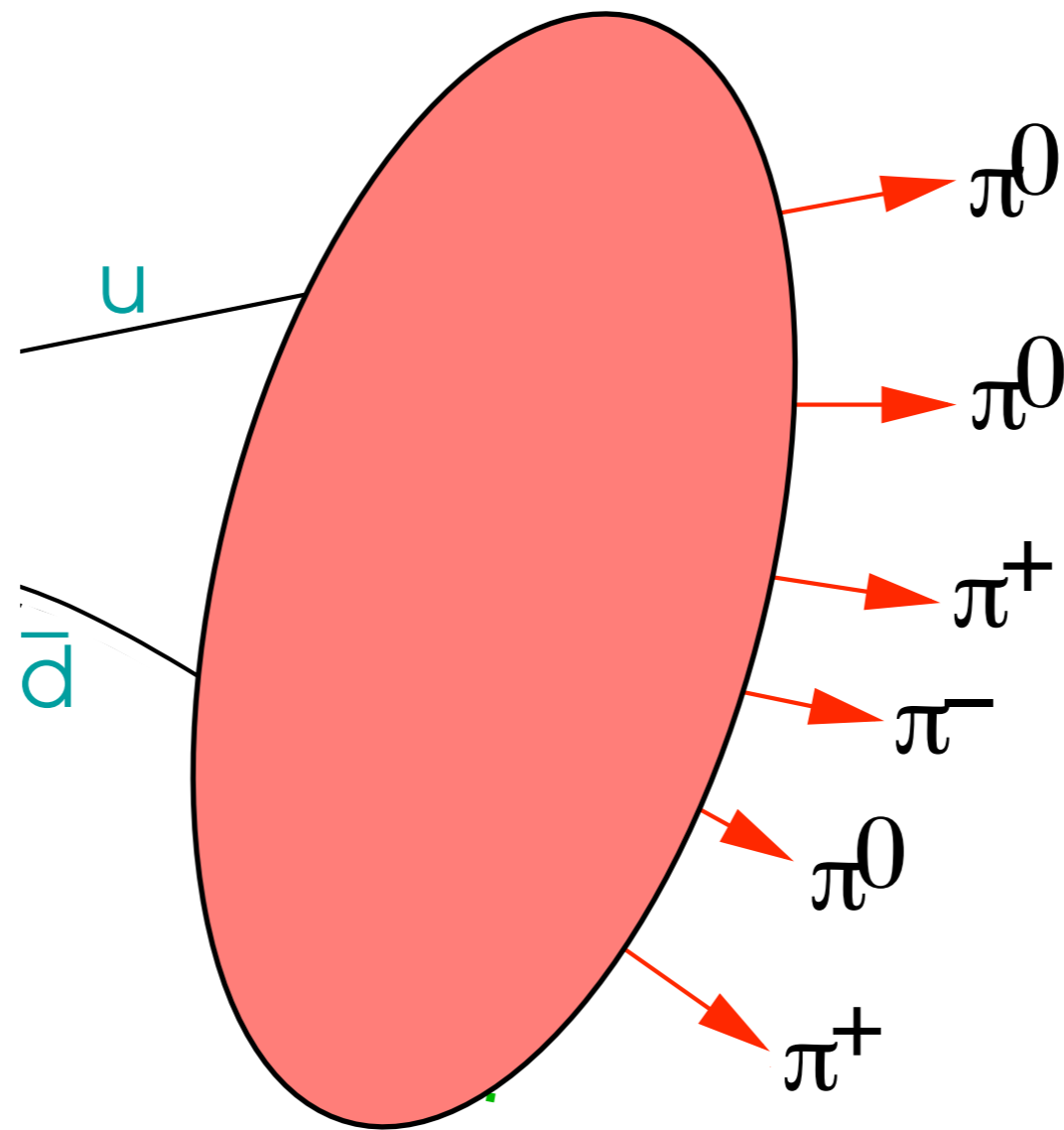
Full event generator



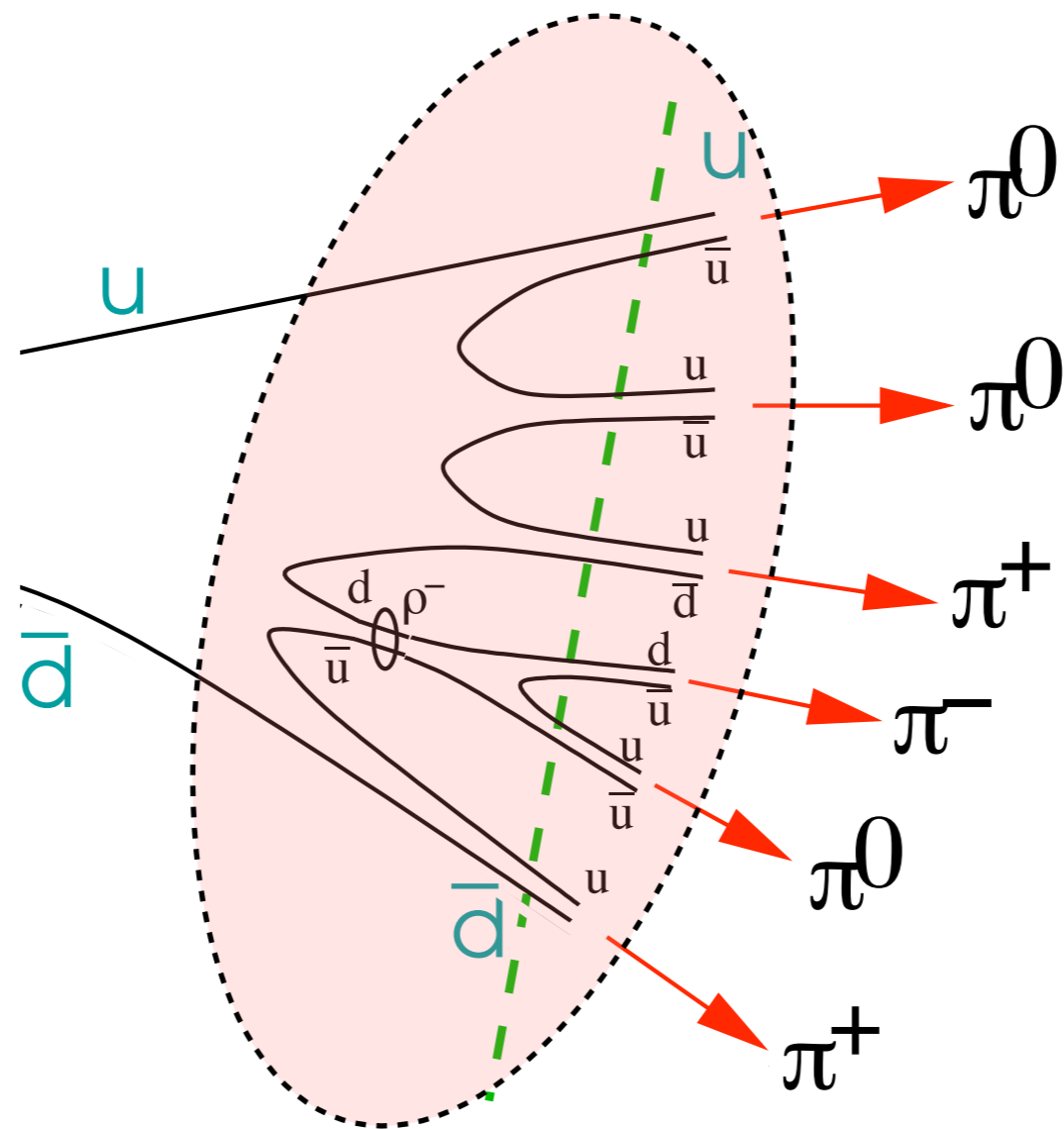
Full event generator



Example of fragmentation model



Example of fragmentation model



What are they used for?

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- Predictions of unmeasured cross sections

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- Search for new physics

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- Predictions of unmeasured cross sections
- Systematic studies
- Search for new physics
- Access to quantities that are not directly measurable (i.e., W -boson mass)

Strong points of event generators

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- Gives a full description of the final state, in all kinematic regions

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- Very sophisticated implementations, containing many ingredients

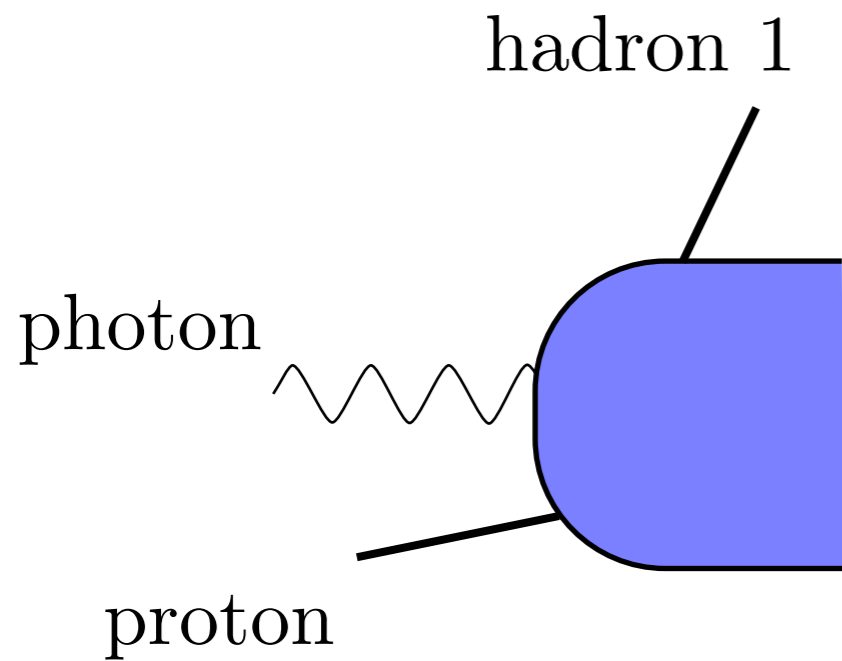
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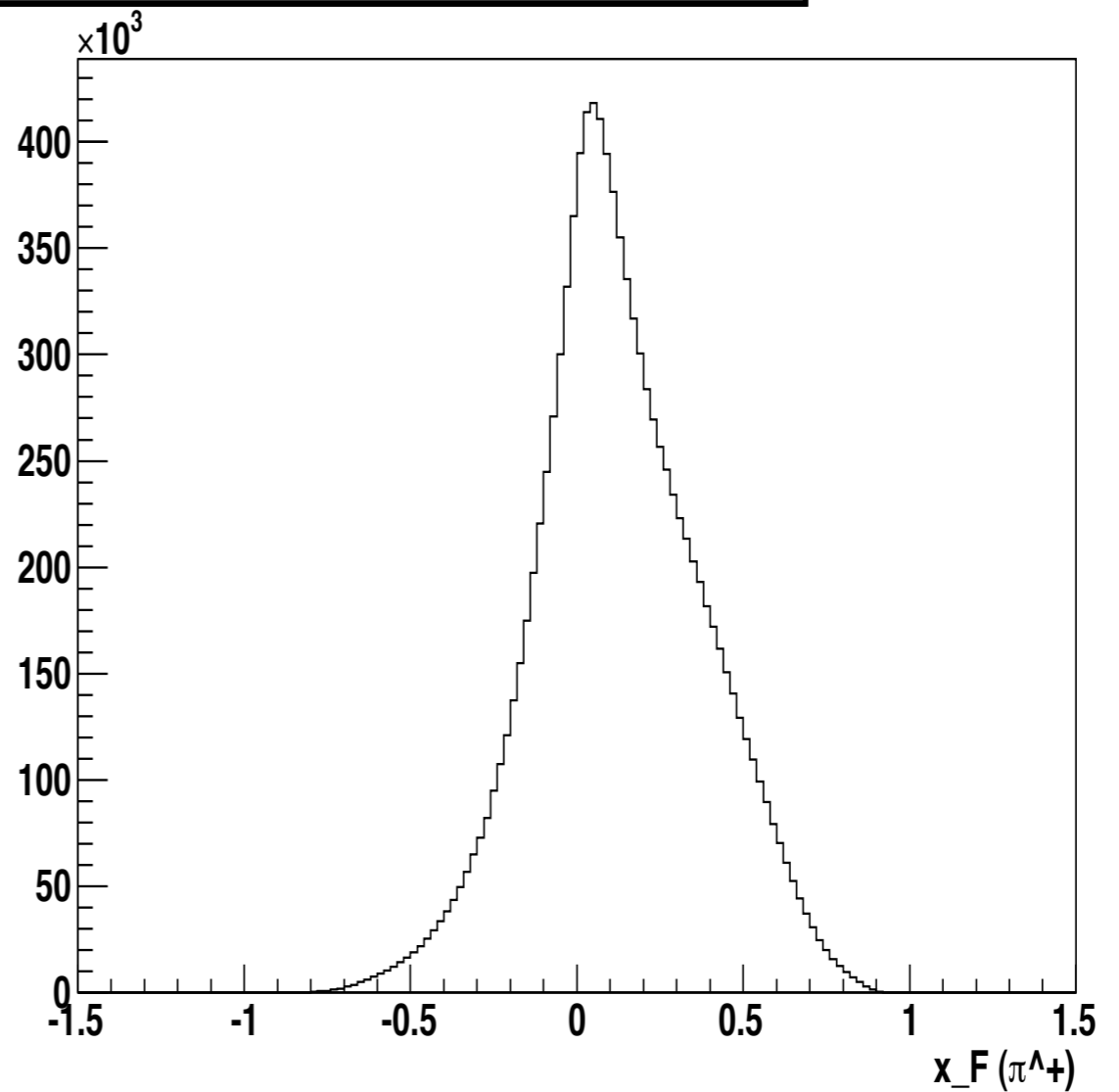
Strong points of event generators

- Gives a full description of the final state, in all kinematic regions
- Very sophisticated implementations, containing many ingredients
- Parameters well tuned
- Excellent coding, based on years of experience

Full description of the final state

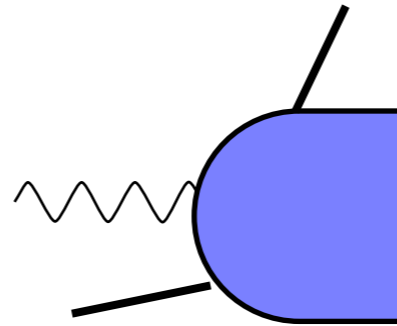


Distribution of x_F for the π^+ in the $\pi^+\pi^-$ channel

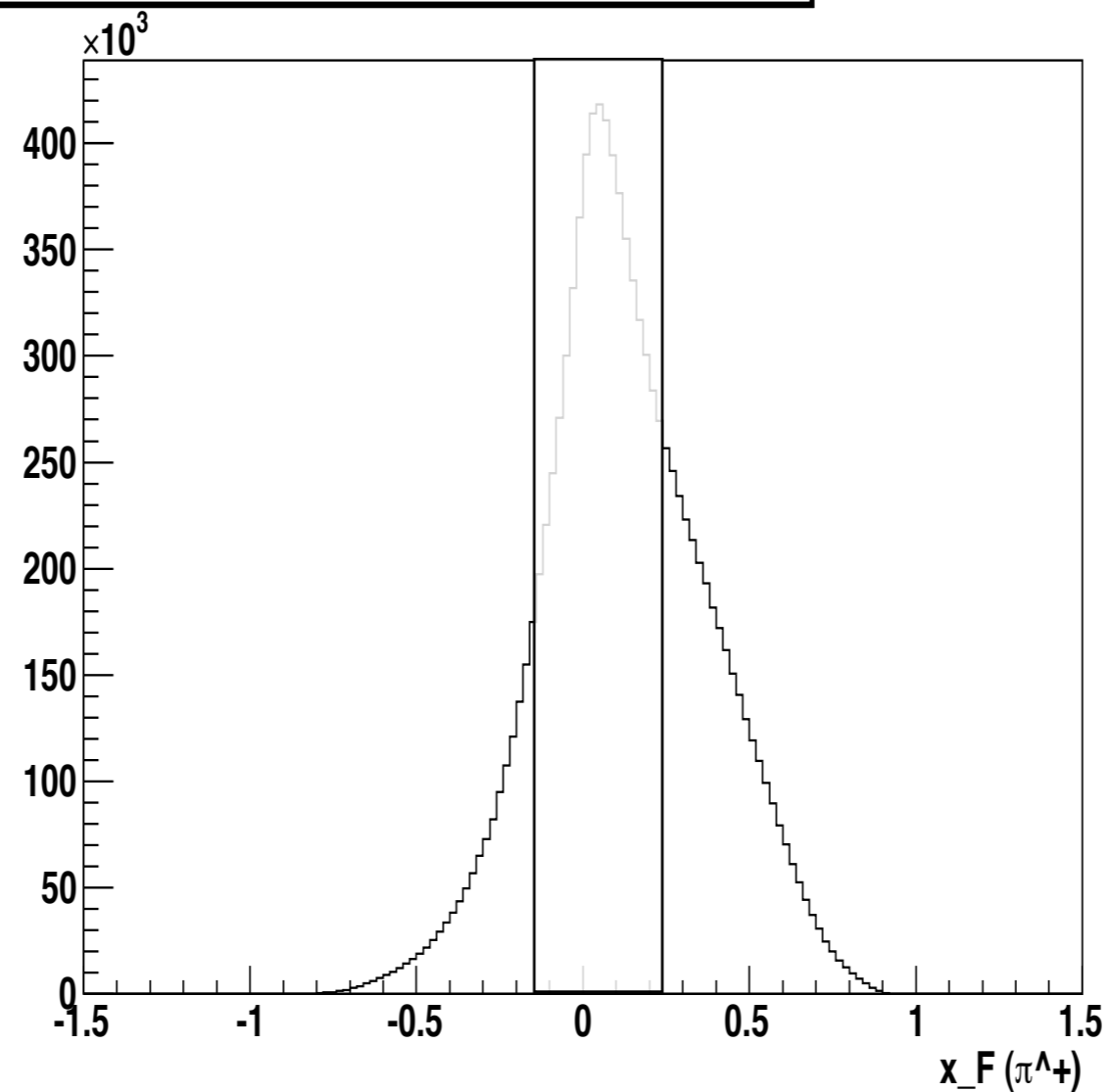


simulation for CLAS12

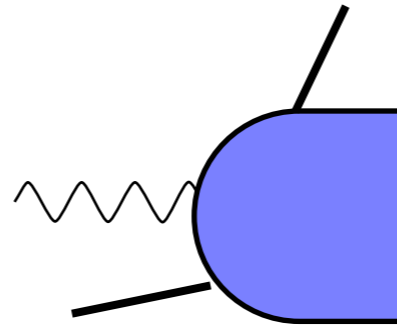
Comparison with SIDIS generators



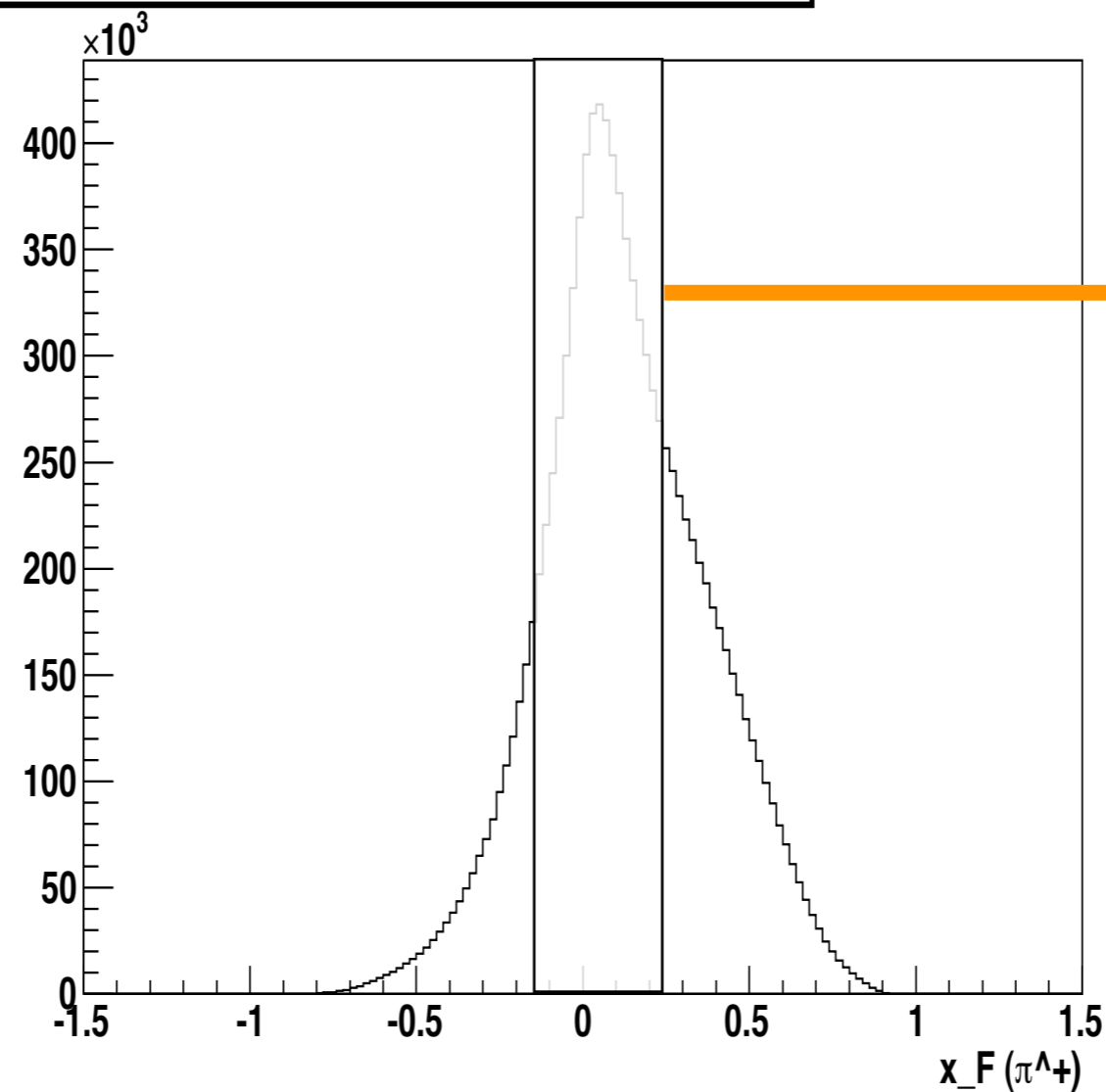
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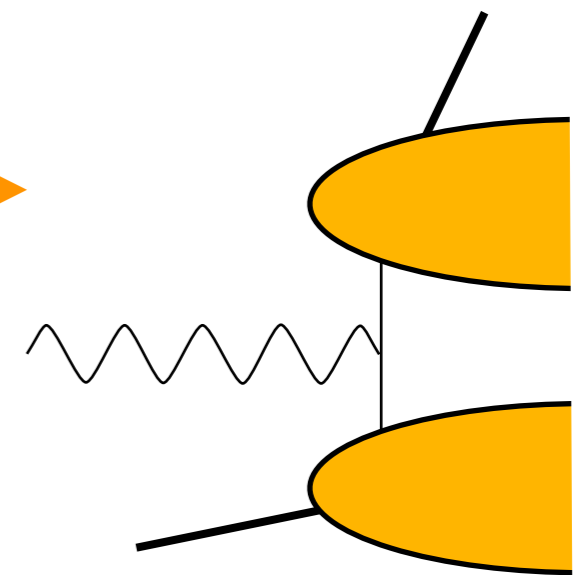
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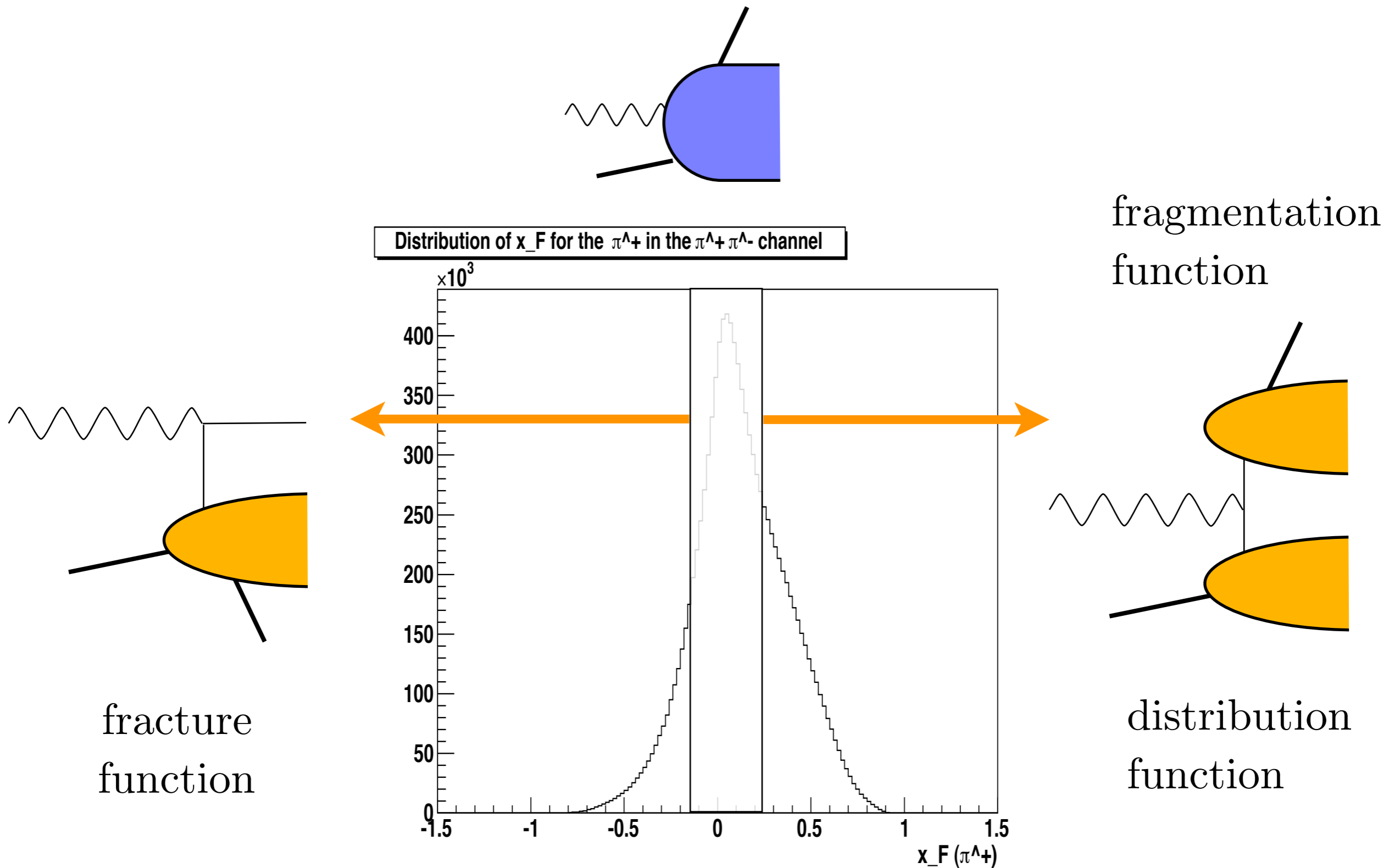


fragmentation function



distribution function

Comparison with SIDIS generators



Example of results

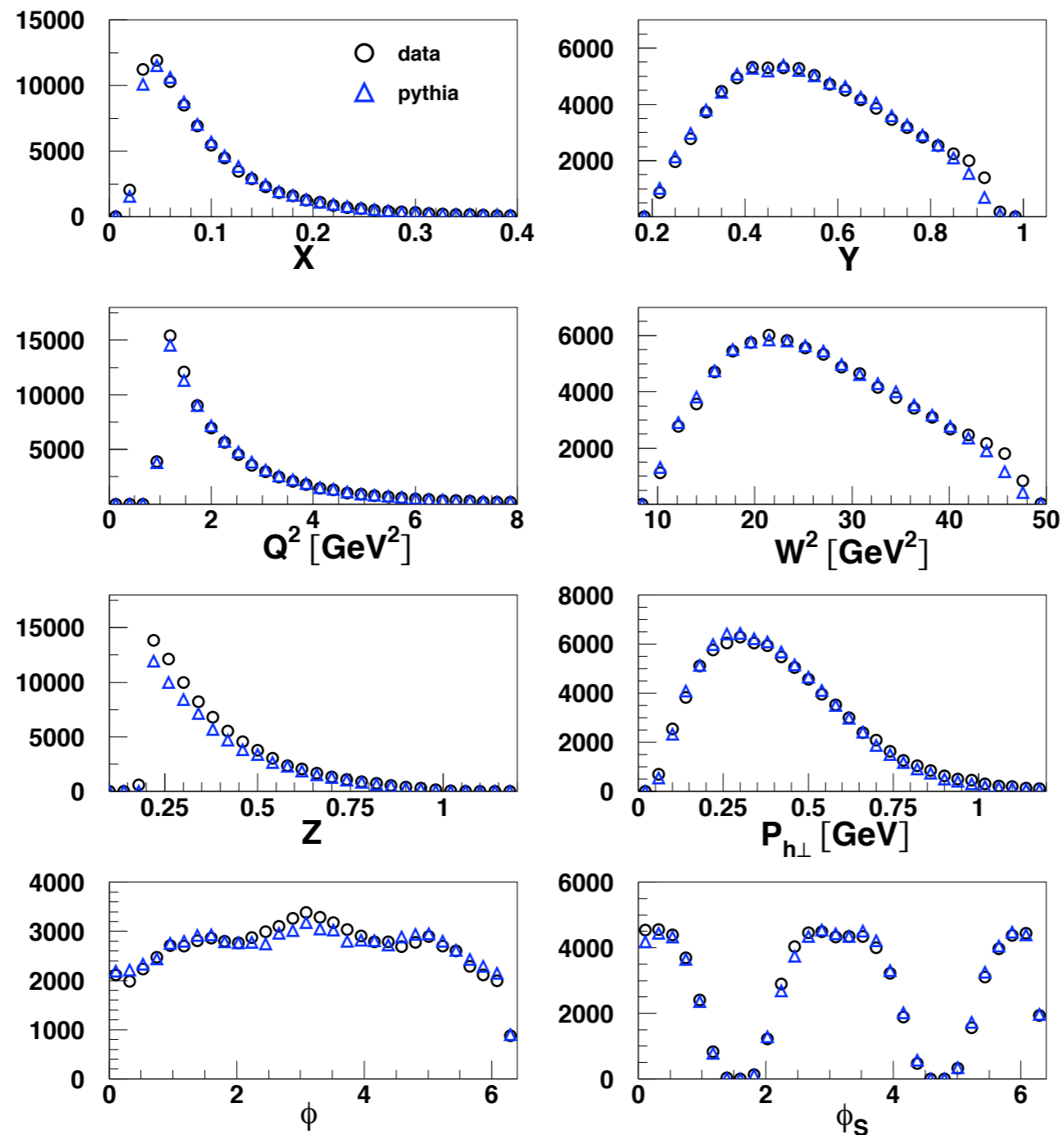


Figure 6.1: Comparison between the distributions of selected DIS and SIDIS kinematic variables obtained from real events and from events generated by PYTHIA.

Some limitations of full event generators

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Possible developments

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Artru, arXiv:1001.1061; Bianconi, arXiv:1109.0688, Kotzinian, hep-ph/0510359

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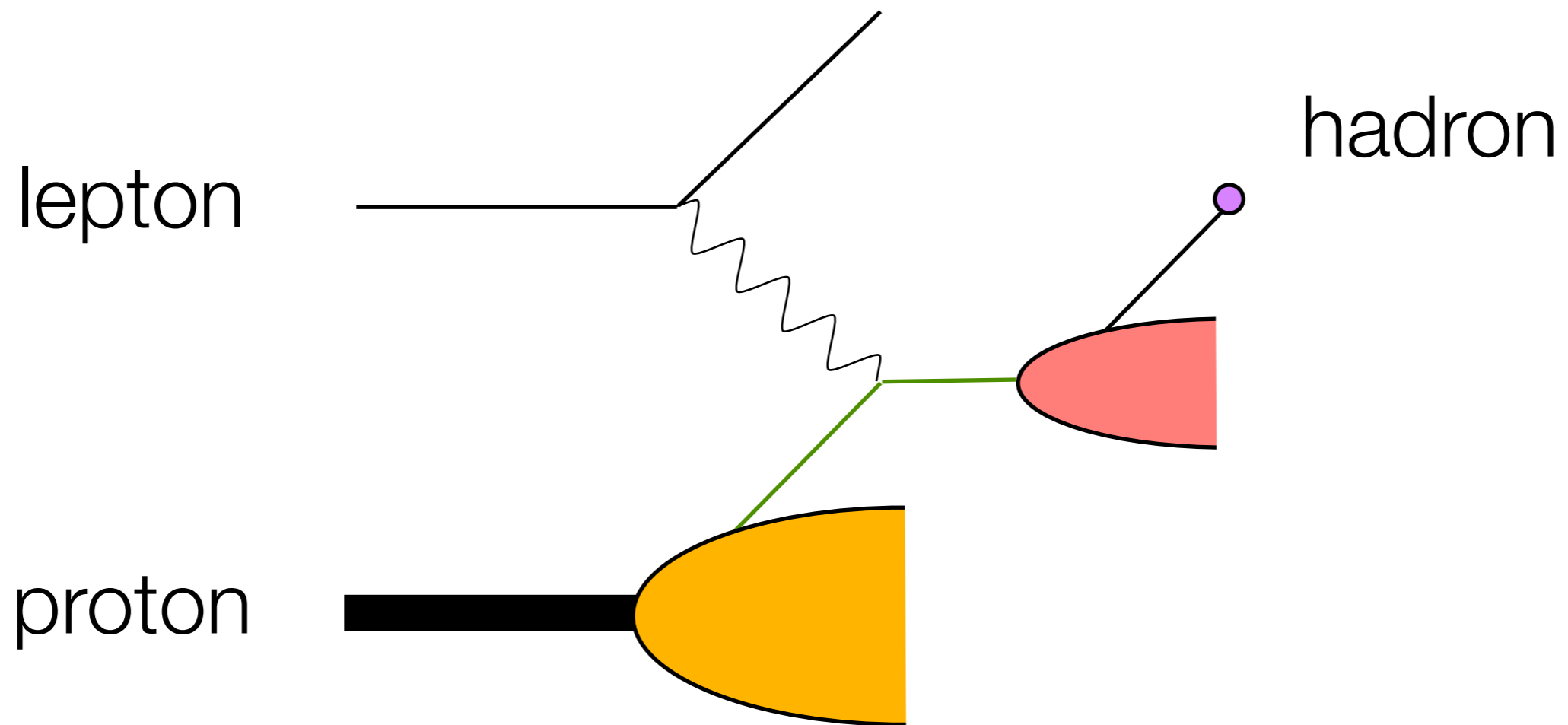
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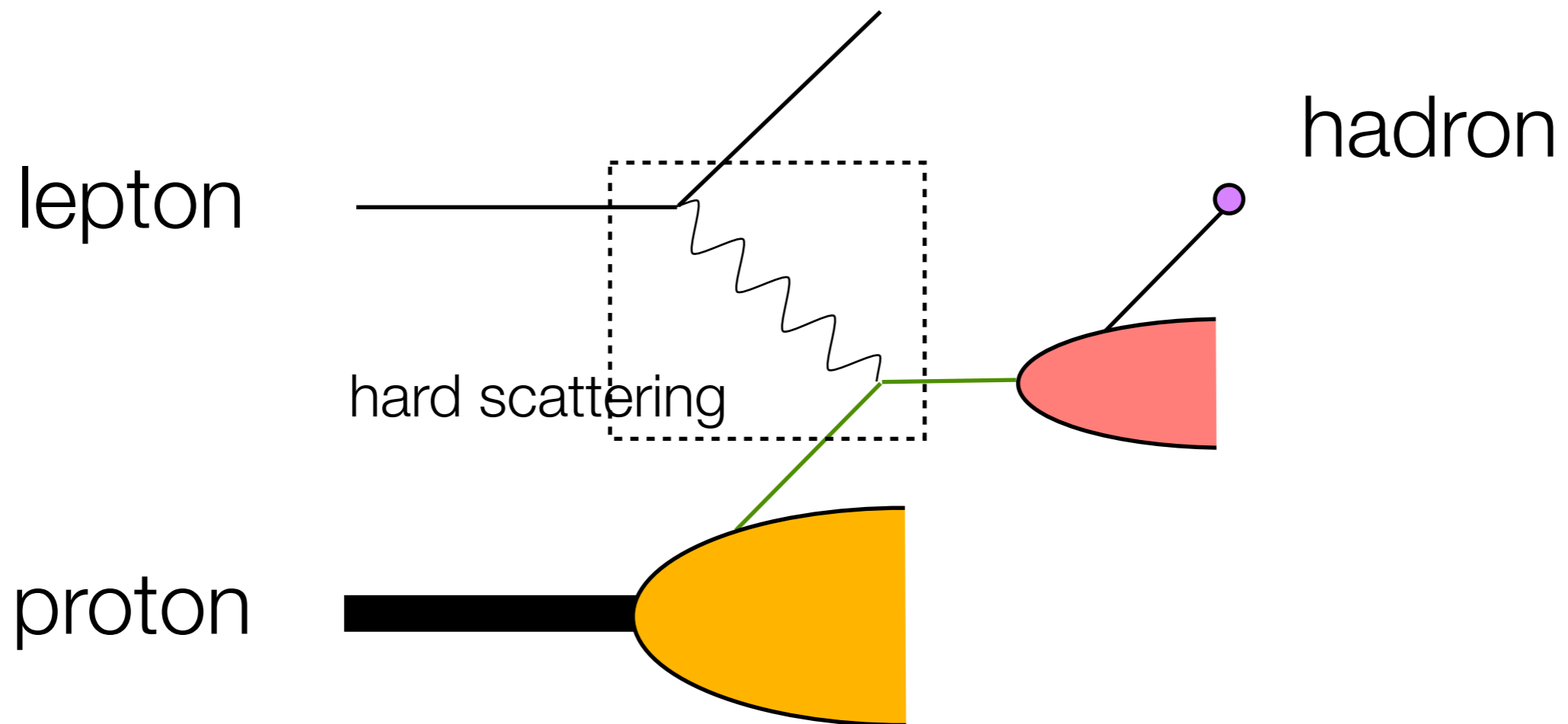
- Artificial modulation of the final cross section based on polarized cross-section (reweighting). Often used by experimental collaborations. No publication?

Something about SIDIS generators

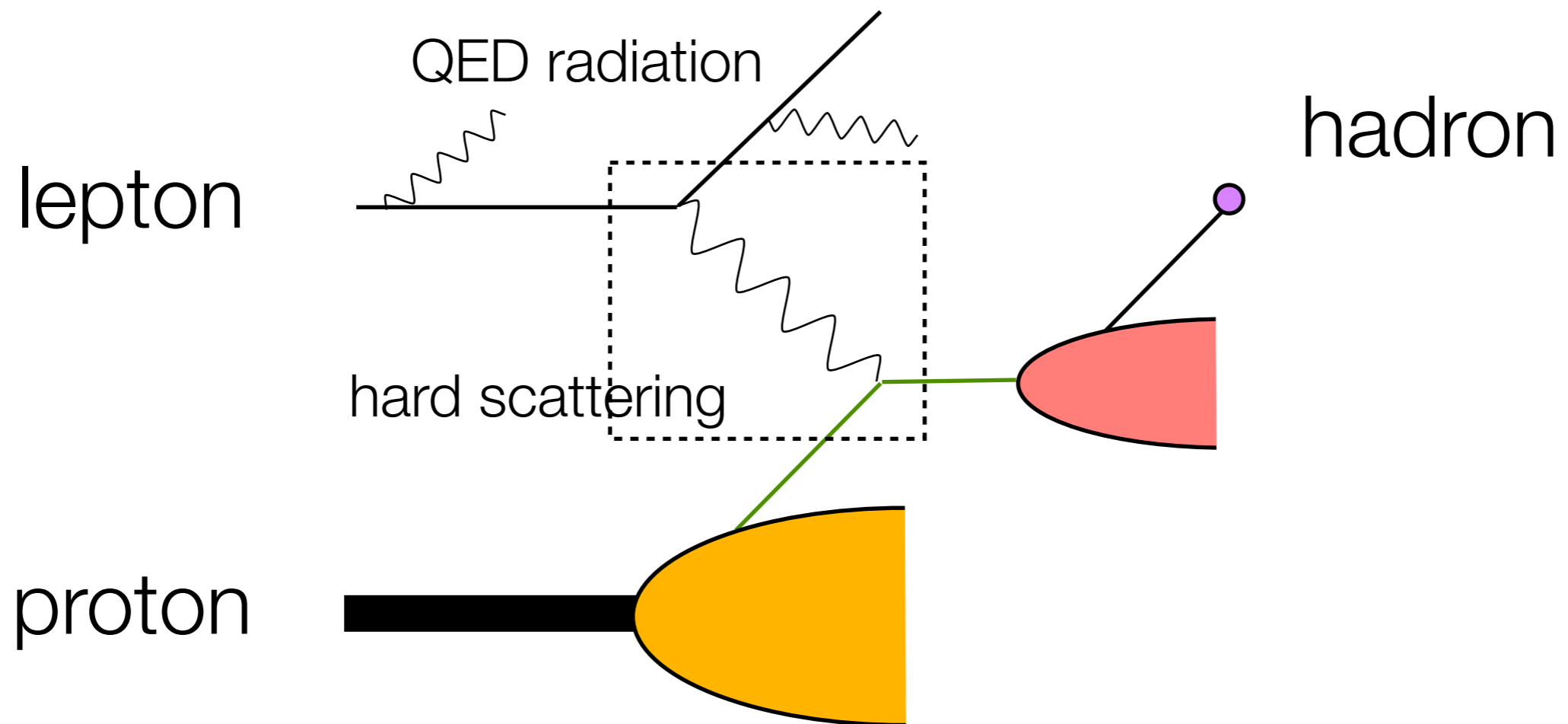
Single-particle DIS generator



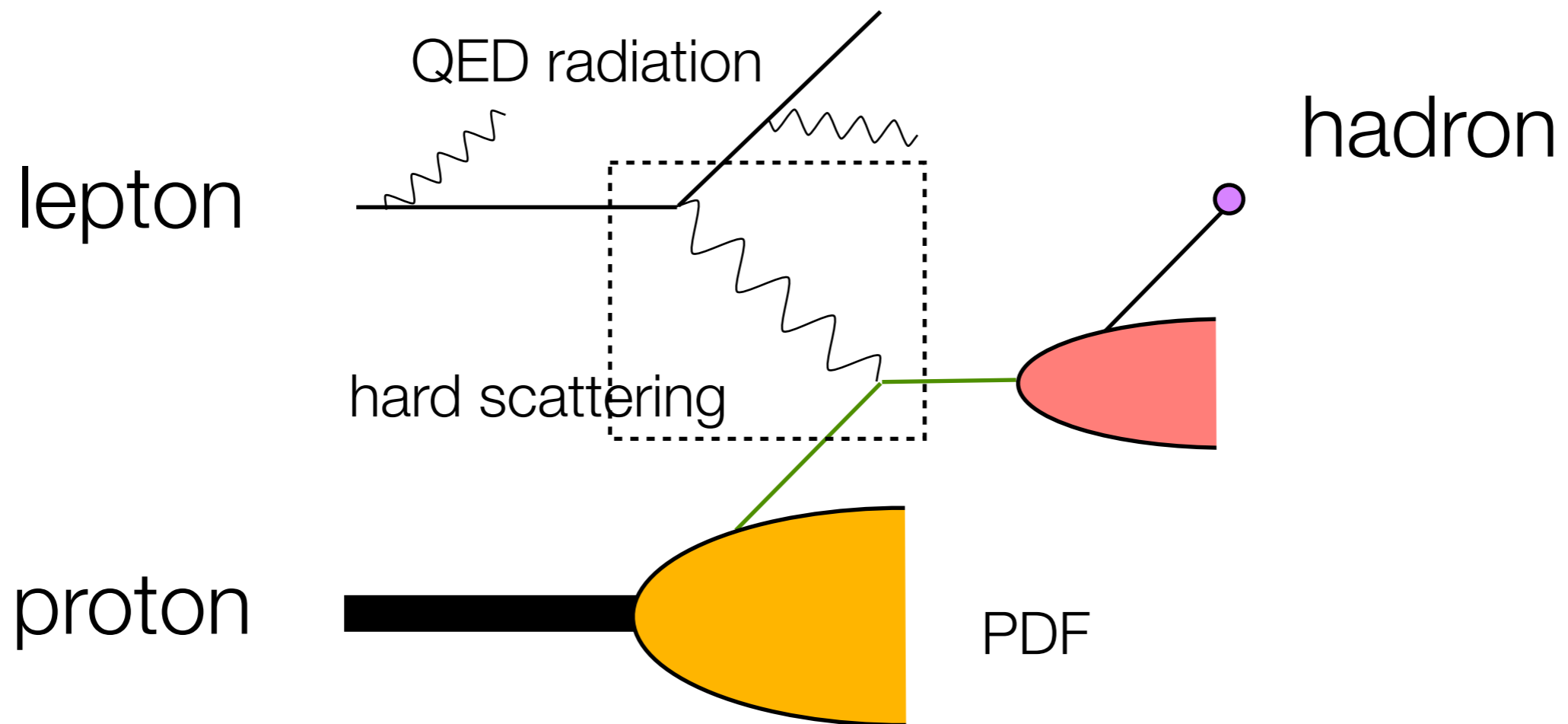
Single-particle DIS generator



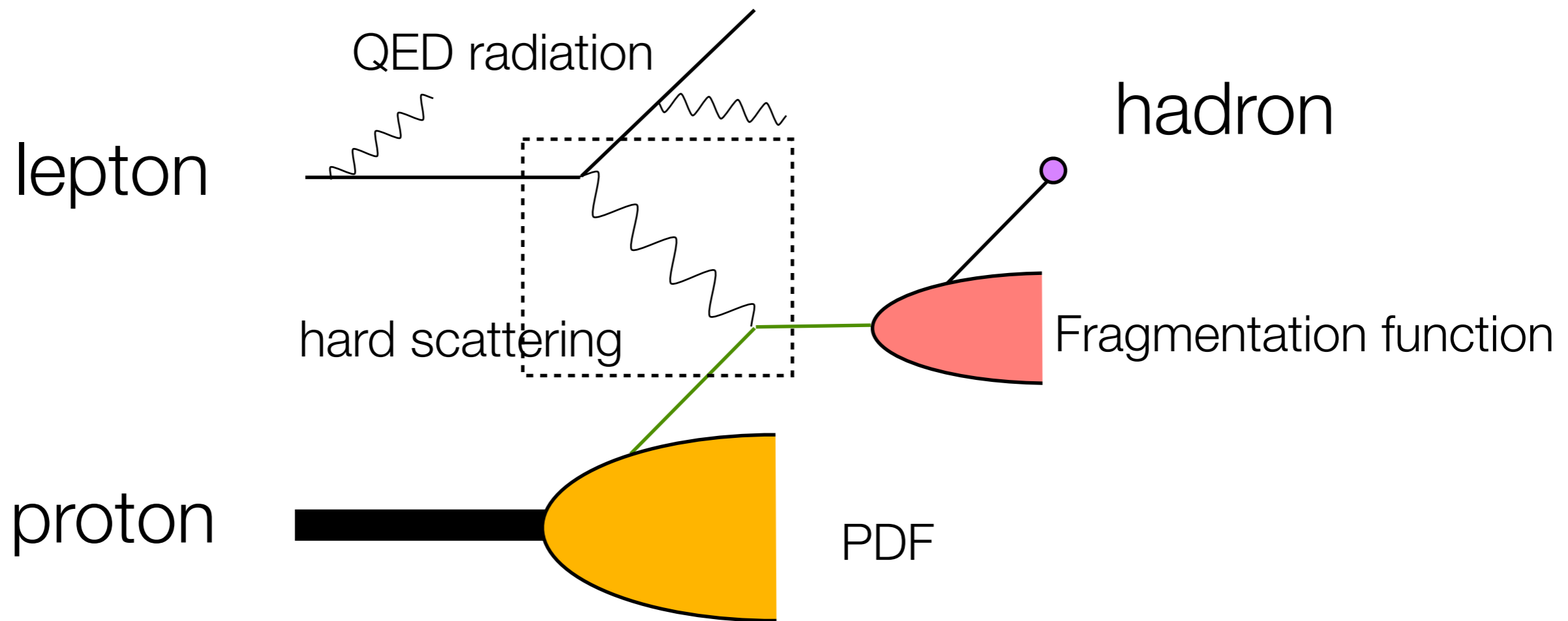
Single-particle DIS generator



Single-particle DIS generator



Single-particle DIS generator



Strong points of SIDIS generators

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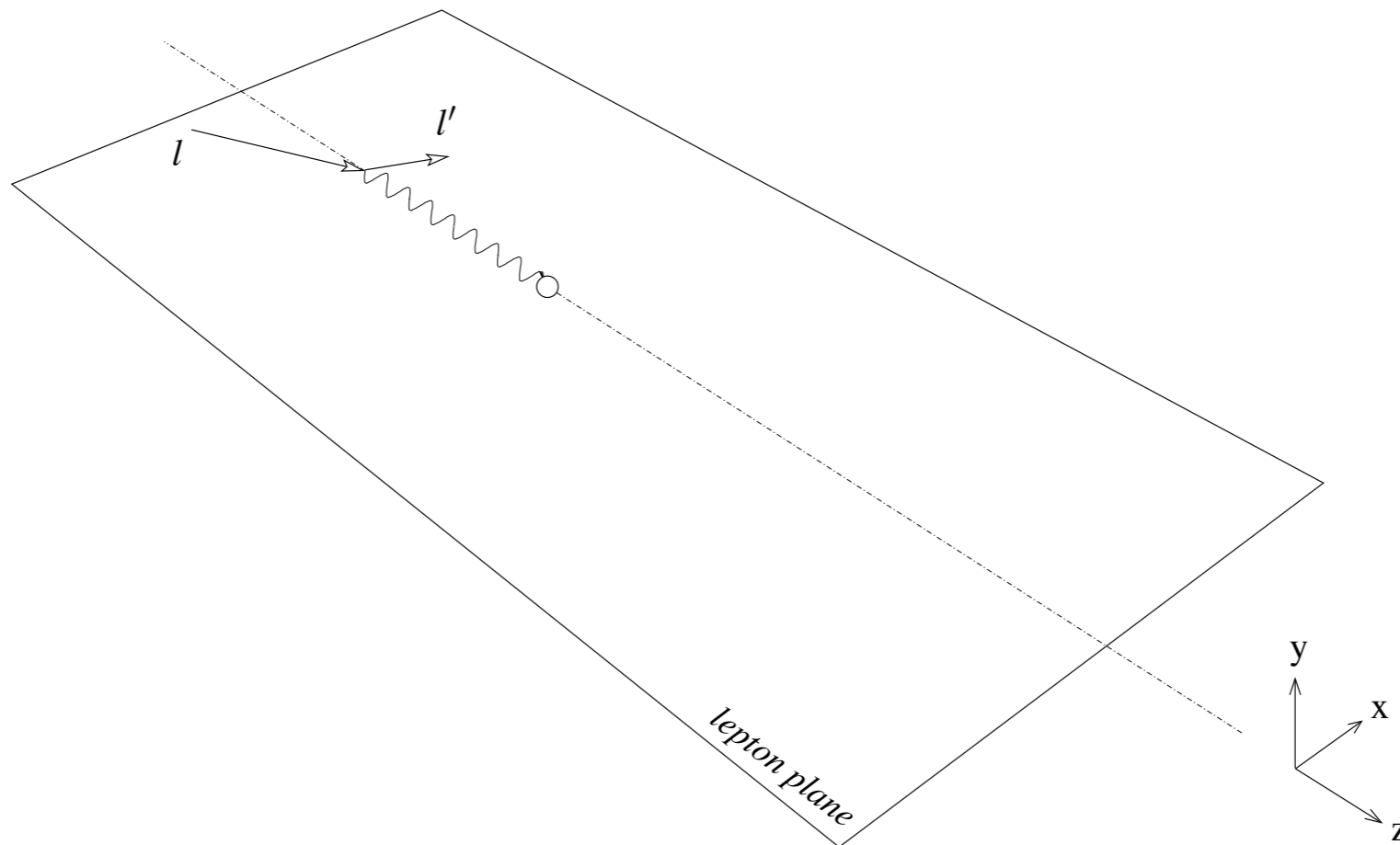
Strong points of SIDIS generators

- All kinds of signals can be introduced in principle
- Simple and fast
- Very close to theoretical formulas and theoretical parametrizations
- Can be in principle extended to higher orders

Inclusive DIS

$$\ell(l) + N(P) \rightarrow \ell(l') + X$$

$$x_B = \frac{Q^2}{2P \cdot q}, \quad y = \frac{P \cdot q}{P \cdot l}$$



Structure functions

$$\frac{d\sigma}{dx_B dy d\phi_S} = \frac{2\alpha^2}{x_B y Q^2} \left\{ \left(1 - y + \frac{y^2}{2}\right) F_{UU,T} + (1 - y) F_{UU,L} + S_L \lambda_e y \left(1 - \frac{y}{2}\right) F_{LL} \right. \\ \left. + |\mathbf{S}_T| \lambda_e y \sqrt{1 - y} \cos \phi_S F_{LT}^{\cos \phi_s} \right\}$$

see, e.g., A.B., Diehl, Goeke, Metz, Mulders, Schlegel, JHEP093 (07)

Structure functions

$$\frac{d\sigma}{dx_B dy d\phi_S} = \frac{2\alpha^2}{x_B y Q^2} \left\{ \left(1 - y + \frac{y^2}{2}\right) F_{UU,T}(x, Q^2) + (1 - y) F_{UU,L} + S_L \lambda_e y \left(1 - \frac{y}{2}\right) F_{LL} \right. \\ \left. + |\mathbf{S}_T| \lambda_e y \sqrt{1 - y} \cos \phi_S F_{LT}^{\cos \phi_s} \right\}$$

F_{UU,T}(x, Q²)

see, e.g., A.B., Diehl, Goeke, Metz, Mulders, Schlegel, JHEP093 (07)

Results for inclusive DIS

Results for inclusive DIS

$$F_{UU,T} = x_B \sum_a e_a^2 f_1^a(x_B)$$

$$F_{UU,L} = 0$$

$$F_{LL} = x_B \sum_a e_a^2 g_1^a(x_B)$$

$$F_{LT}^{\cos \phi_S} = -\gamma x_B \sum_a e_a^2 g_T^a(x_B)$$

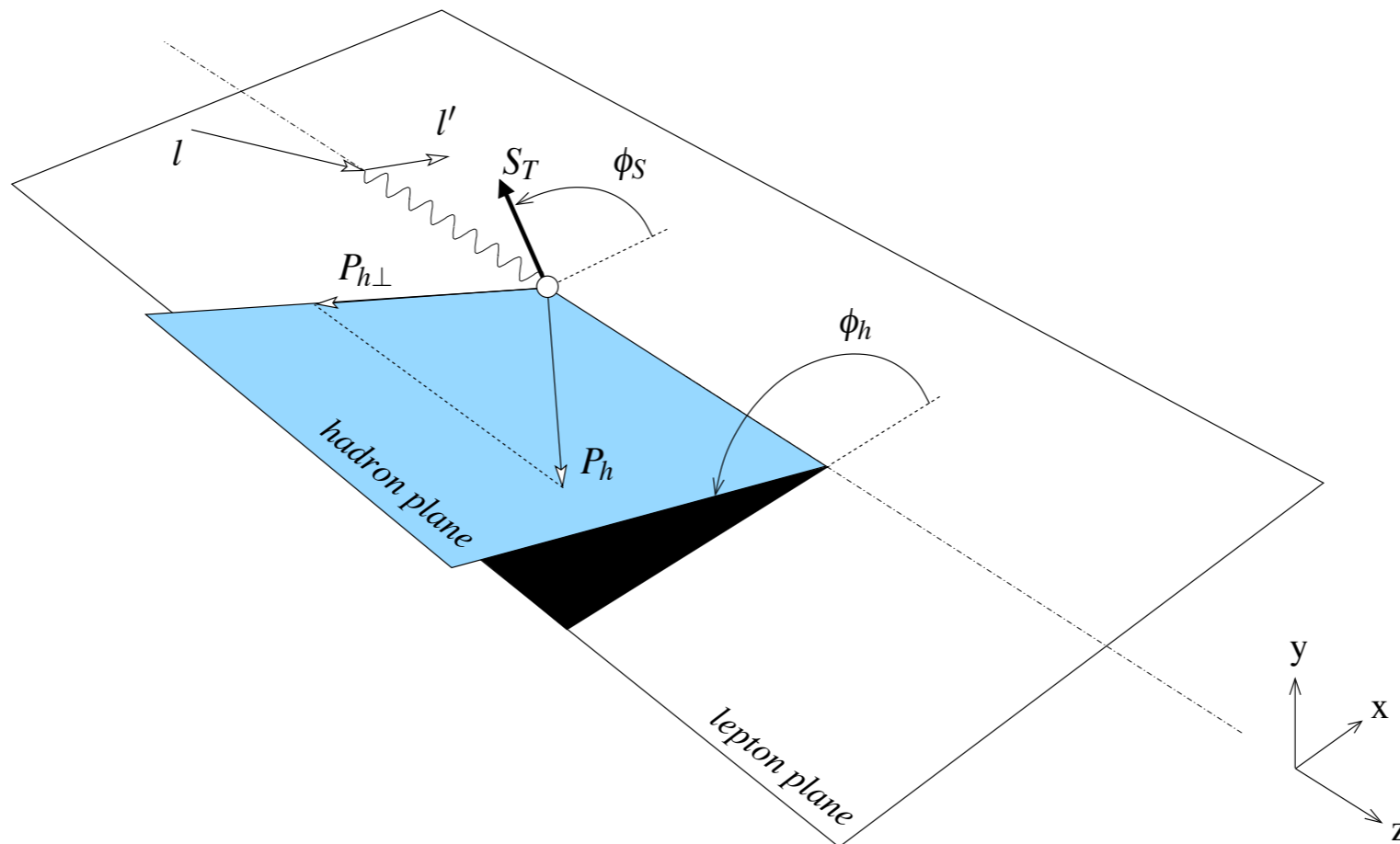
Semi-inclusive DIS

$$\ell(l) + N(P) \rightarrow \ell(l') + h(P_h) + X,$$

$$x_B = \frac{Q^2}{2P \cdot q},$$

$$y = \frac{P \cdot q}{P \cdot l},$$

$$z_h = \frac{P \cdot P_h}{P \cdot q}.$$



A.B., D'Alesio, Diehl, Miller, PRD70 (04)

Structure functions

$$\begin{aligned}
 & \frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2} \\
 &= \frac{\alpha^2}{x y Q^2} \frac{y^2}{2(1-\varepsilon)} \left\{ F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right. \\
 &+ \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\
 &+ S_L \lambda_e \left[\sqrt{1-\varepsilon^2} F_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_h F_{LL}^{\cos\phi_h} \right] \\
 &+ S_T \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right. \\
 &+ \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} + \sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_S F_{UT}^{\sin\phi_S} \\
 &+ \left. \left. \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] + S_T \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right. \right. \\
 &+ \left. \left. \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\}
 \end{aligned}$$

see e.g. AB, Diehl, Goeke, Metz, Mulders, Schlegel, JHEP093 (07)

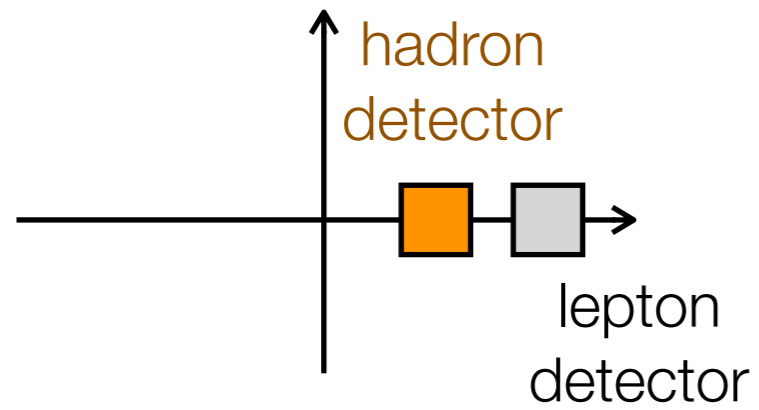
Structure functions

$$\begin{aligned}
 & \frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2} \\
 &= \frac{\alpha^2}{xy Q^2} \frac{y^2}{2(1-\varepsilon)} \left\{ \begin{aligned}
 & F_{UU,T}(x, z, P_{h\perp}^2, Q^2) \\
 & F_{UU,T} + \varepsilon F_{UU,L} + \sqrt{2\varepsilon(1+\varepsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \\
 & + \lambda_e \sqrt{2\varepsilon(1-\varepsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} + S_L \left[\sqrt{2\varepsilon(1+\varepsilon)} \sin\phi_h F_{UL}^{\sin\phi_h} + \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \\
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 & + S_T \left[\sin(\phi_h - \phi_S) \left(F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right. \\
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 & \left. + \sqrt{2\varepsilon(1+\varepsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] + S_T \lambda_e \left[\sqrt{1-\varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right. \\
 & \left. + \sqrt{2\varepsilon(1-\varepsilon)} \cos\phi_S F_{LT}^{\cos\phi_S} + \sqrt{2\varepsilon(1-\varepsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \left. \right\}
 \end{aligned}
 \right.
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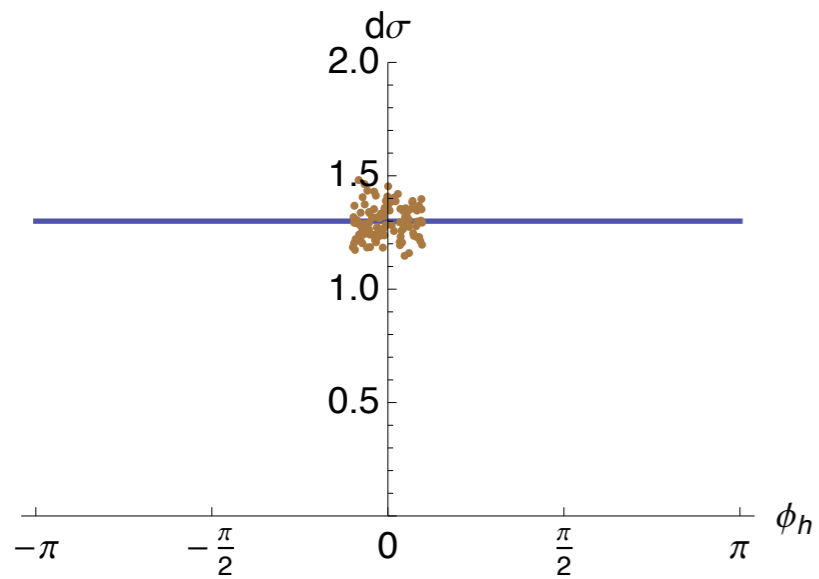
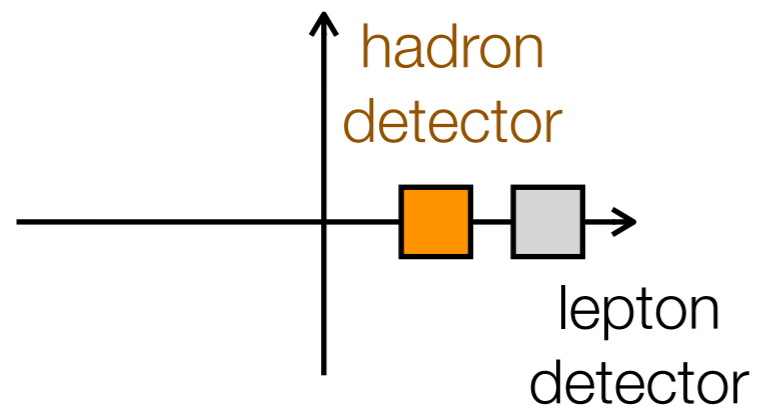
Beware: azimuthal coverage

$$d\sigma = A$$



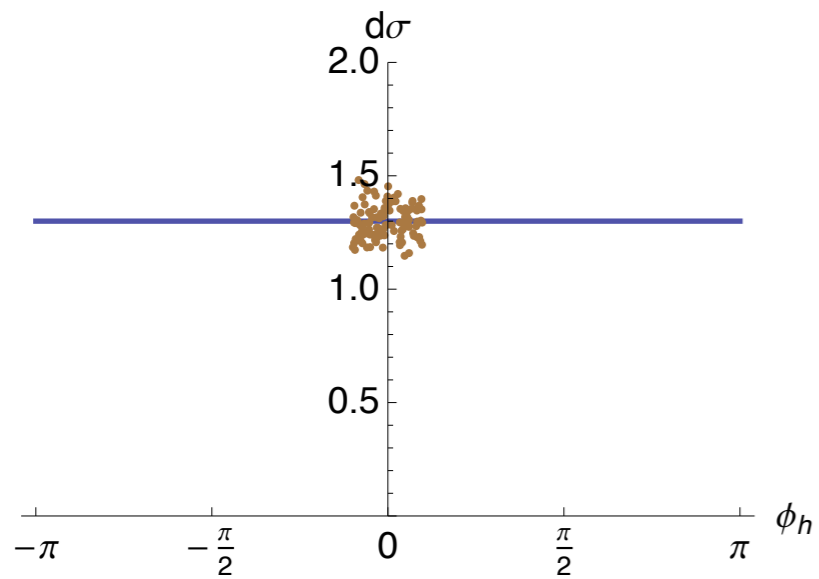
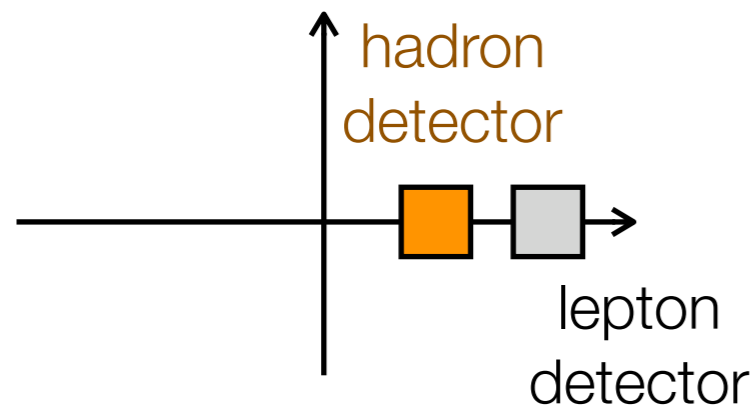
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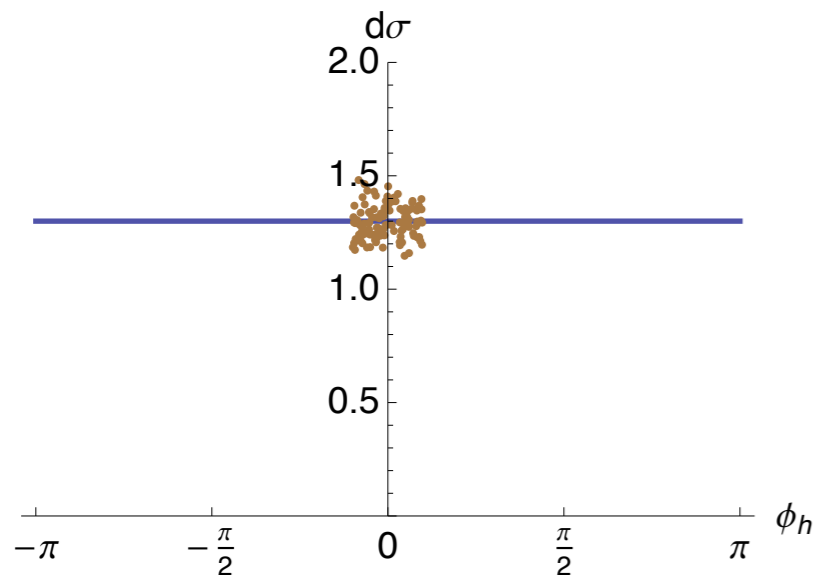
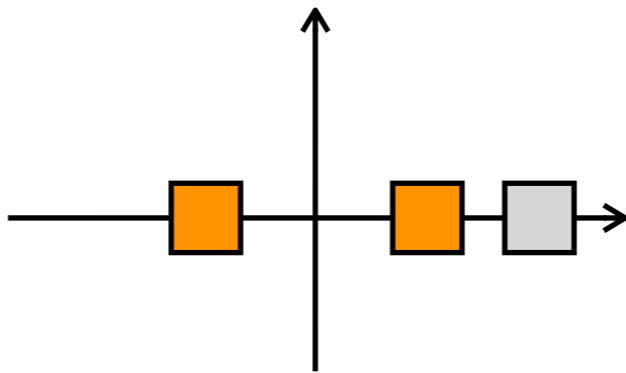
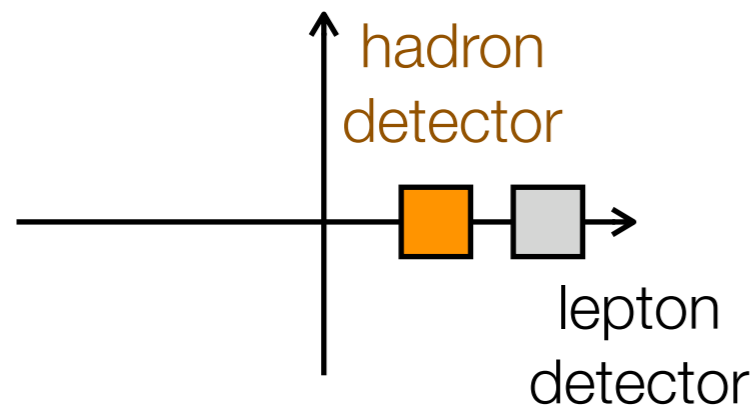
$$d\sigma = A$$



$$A = 1.3$$

Beware: azimuthal coverage

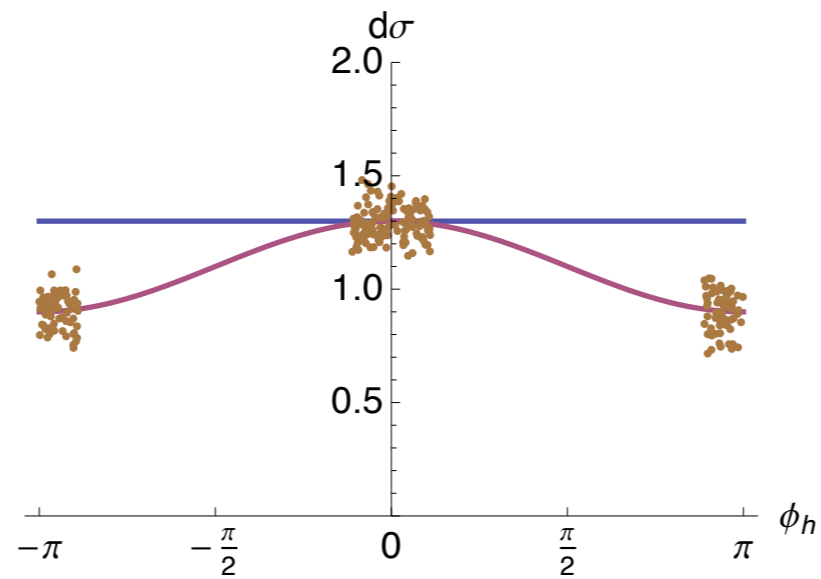
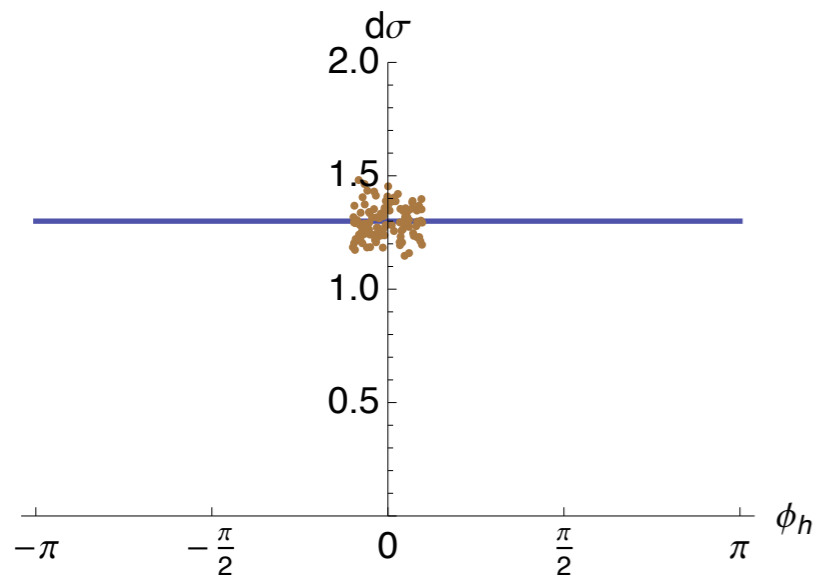
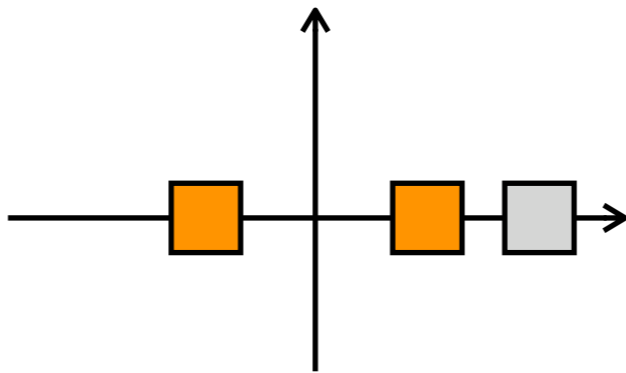
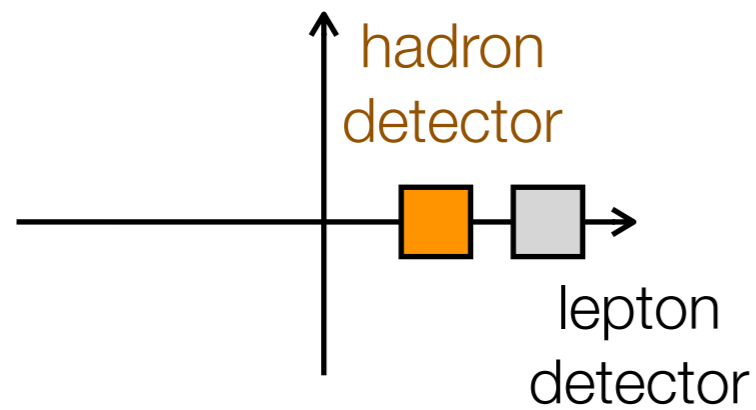
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Beware: azimuthal coverage

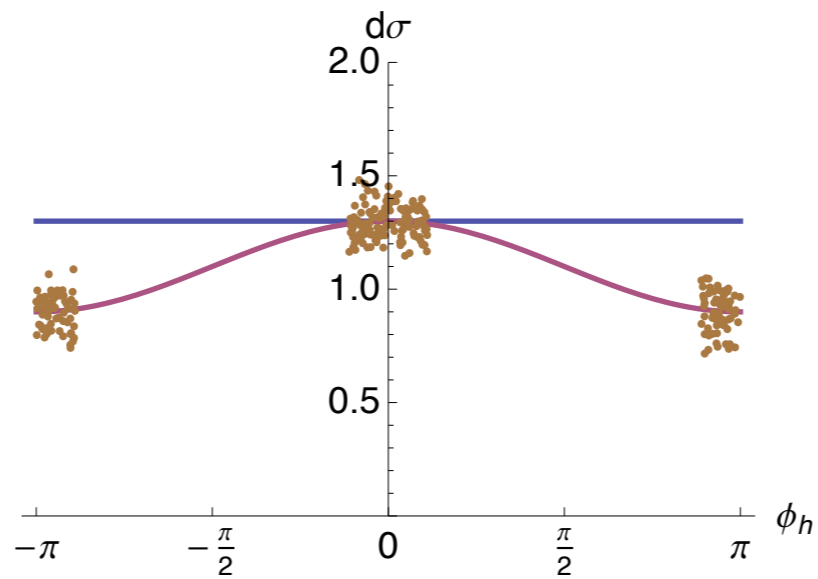
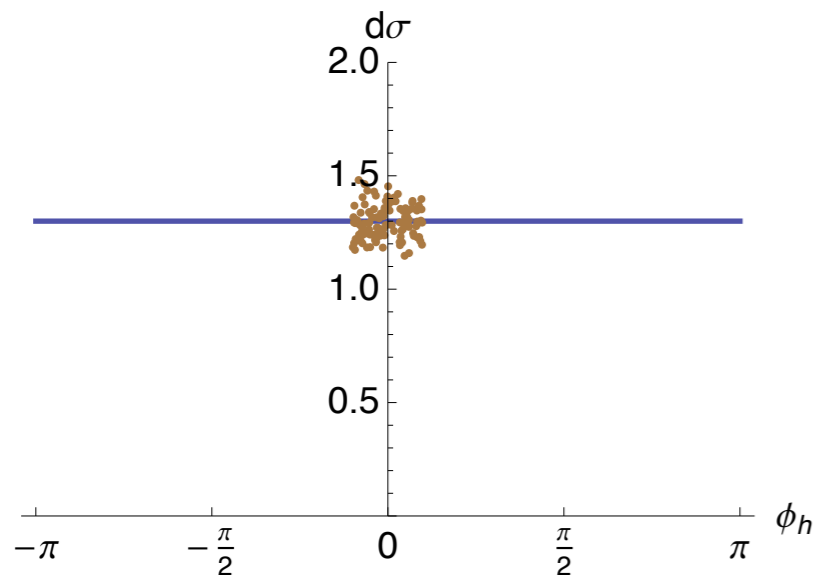
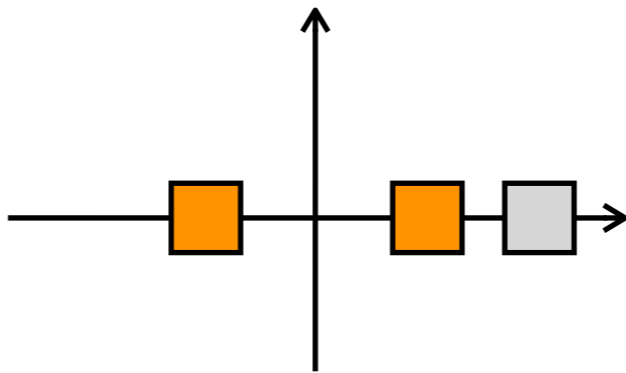
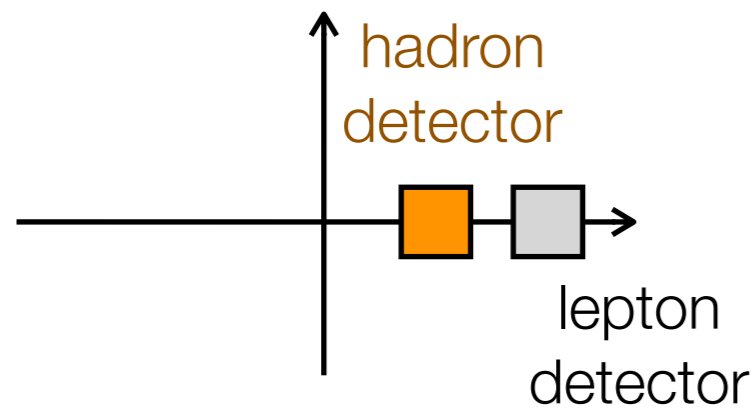
$$d\sigma = A$$



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Beware: azimuthal coverage

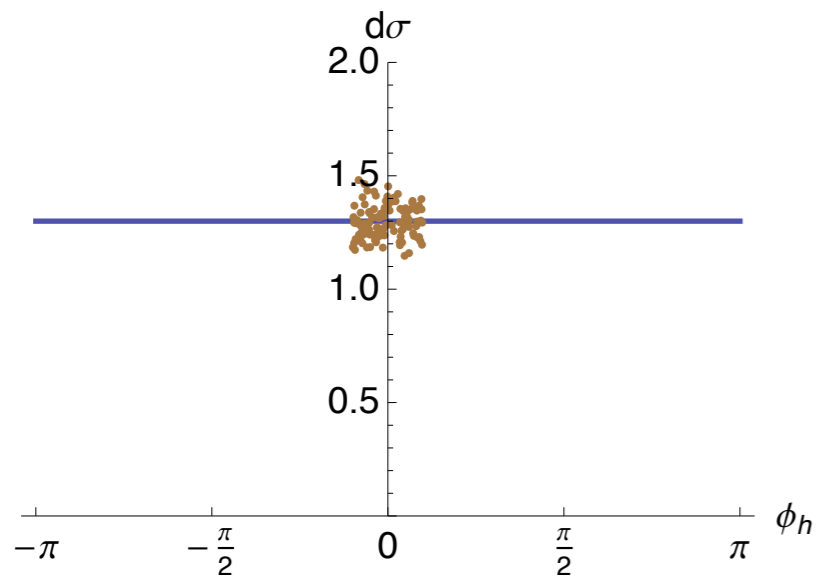
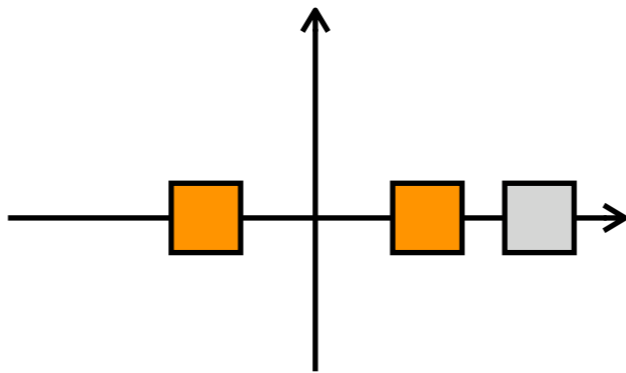
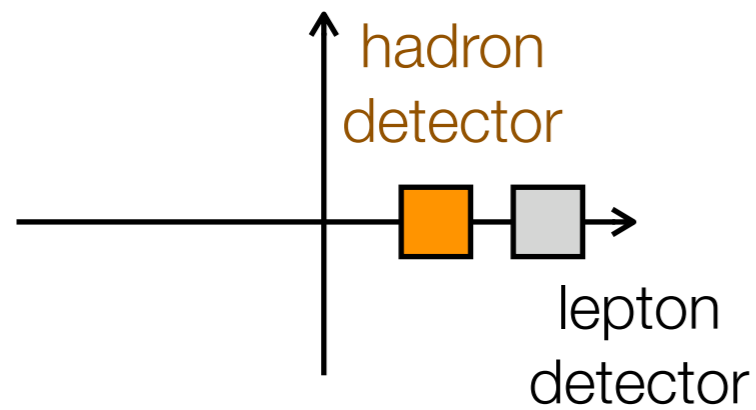
$$d\sigma = A + B \cos \phi$$



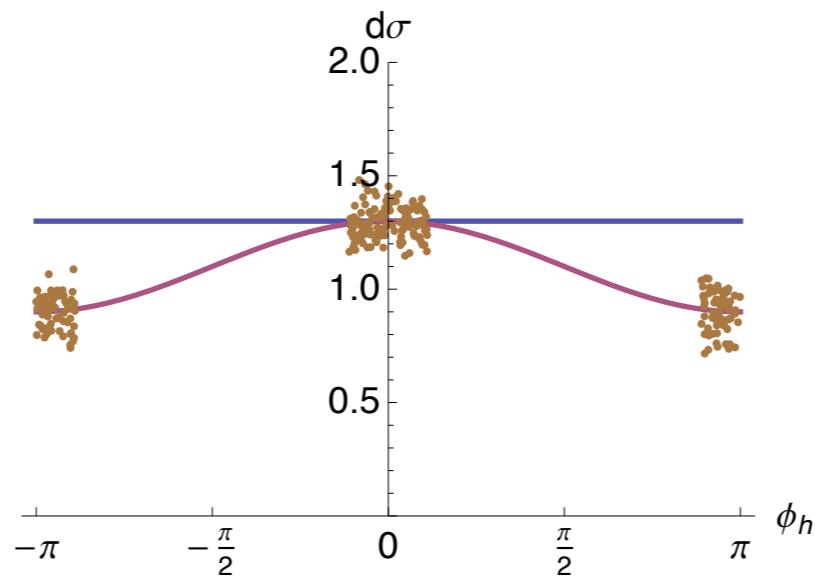
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Beware: azimuthal coverage

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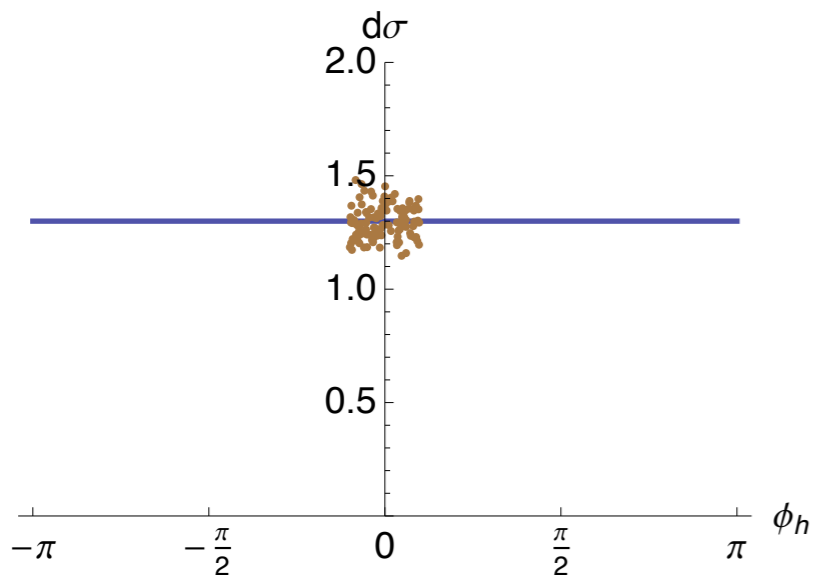
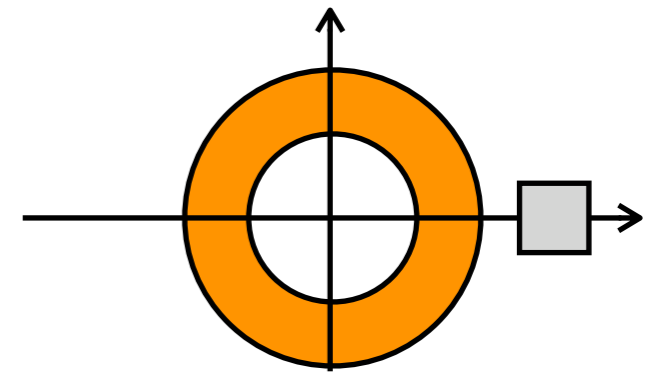
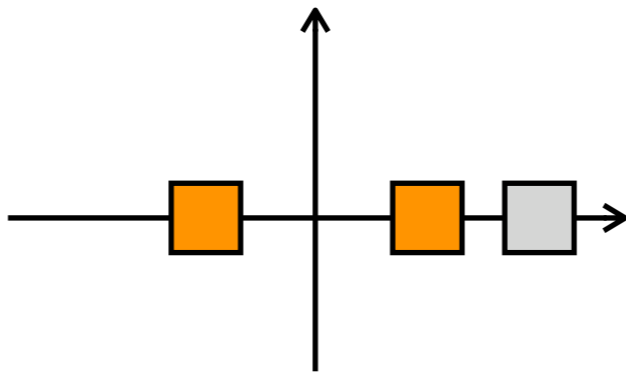
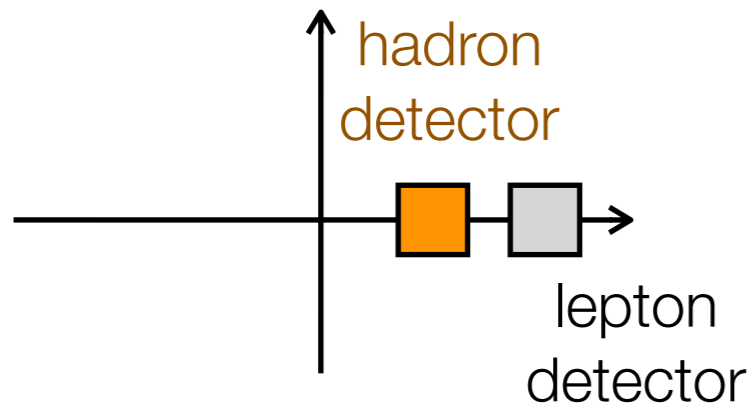
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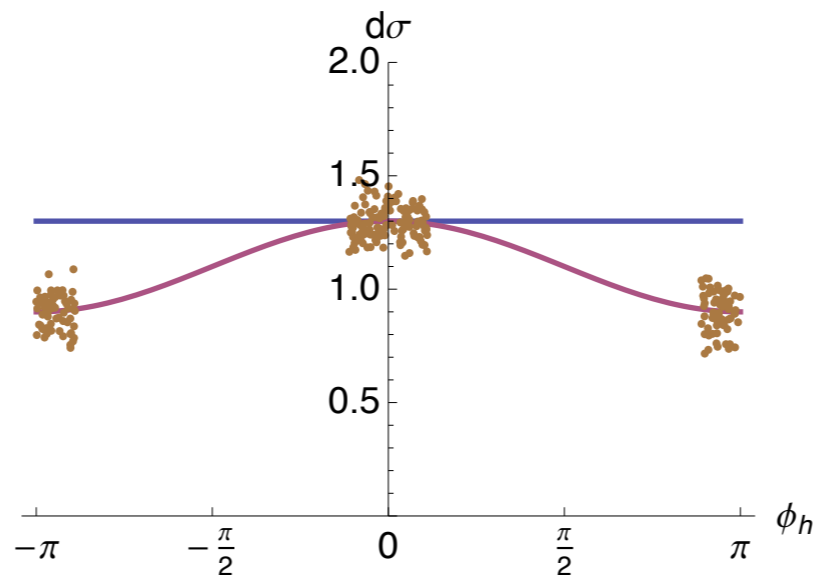
$$A = 1.1, \quad B = 0.2$$

Beware: azimuthal coverage

$$d\sigma = A + B \cos \phi$$



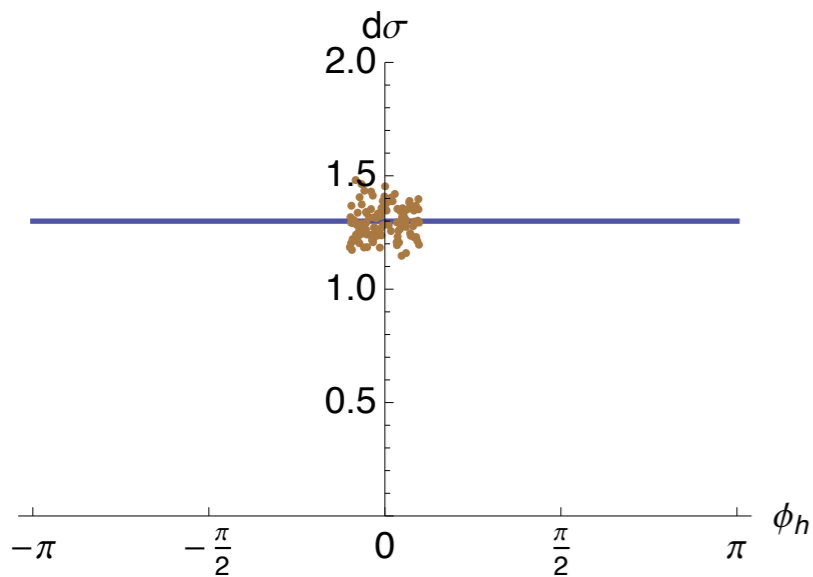
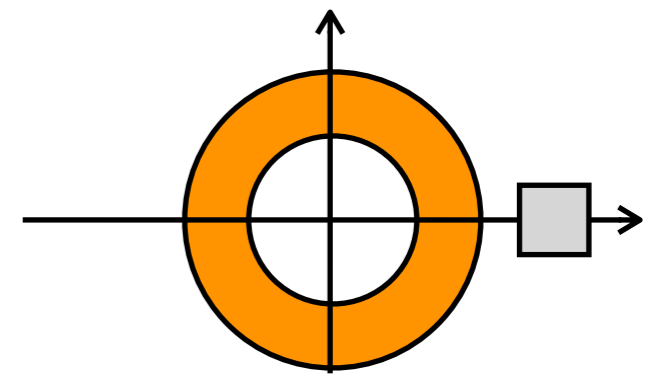
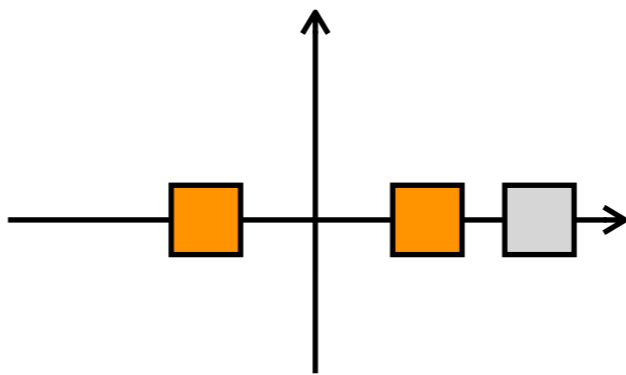
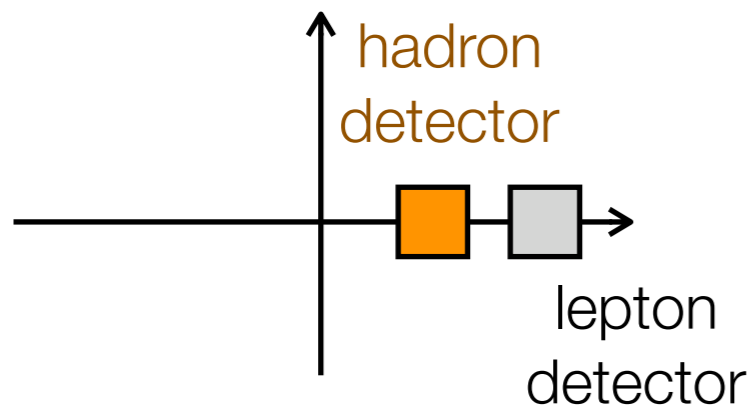
$$A = 1.3$$



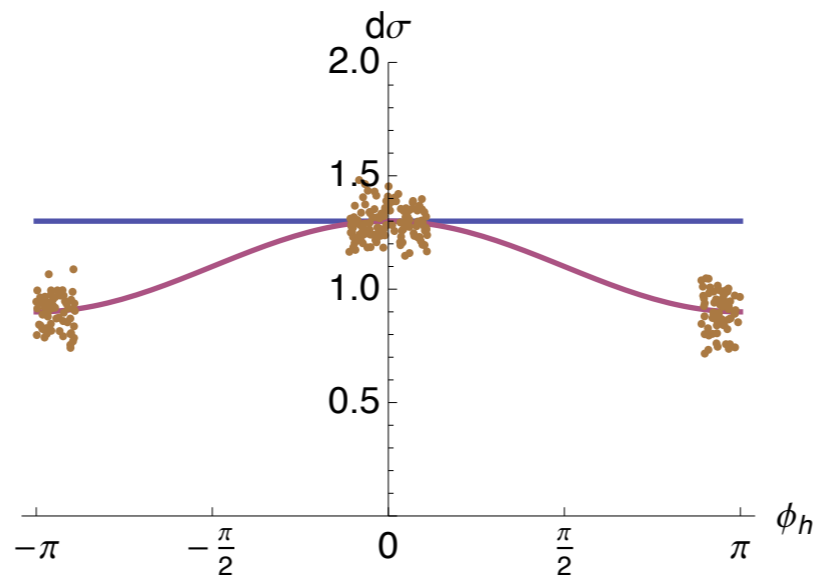
$$A = 1.1, \quad B = 0.2$$

Beware: azimuthal coverage

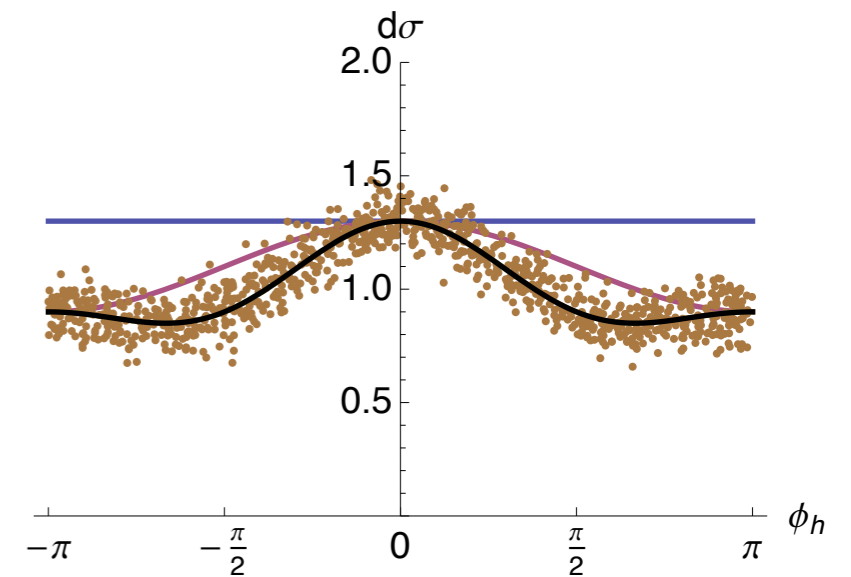
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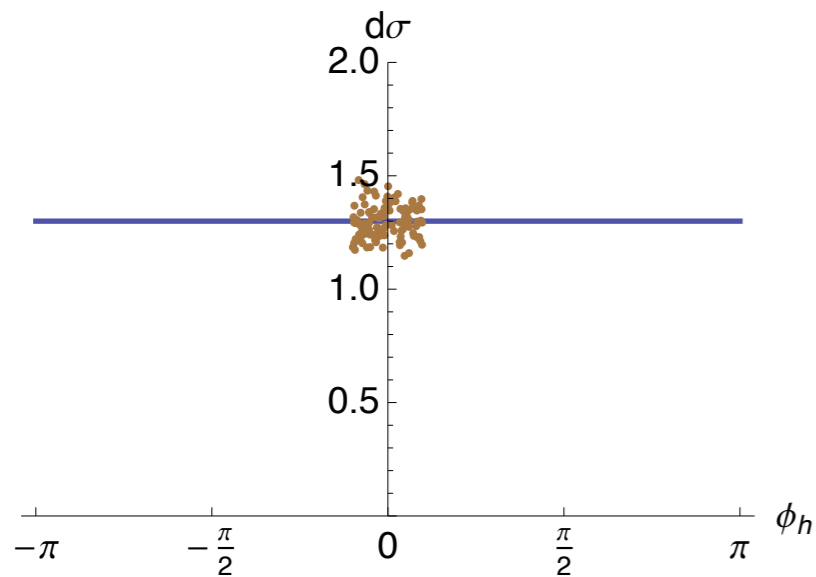
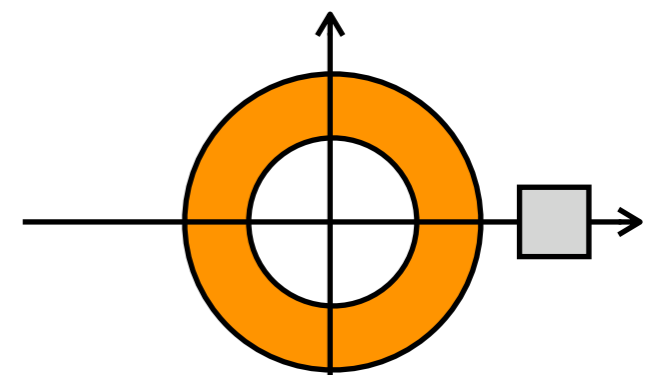
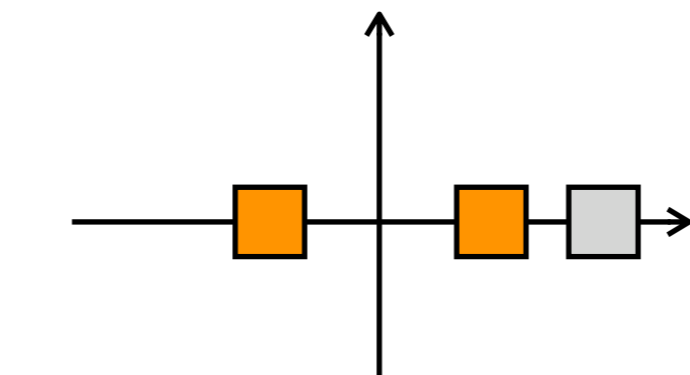
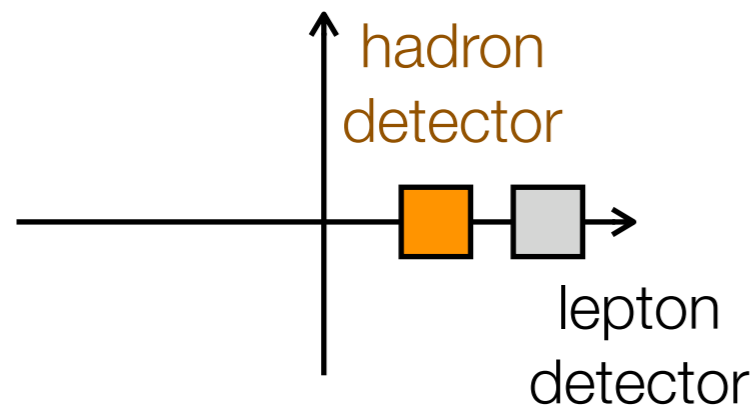


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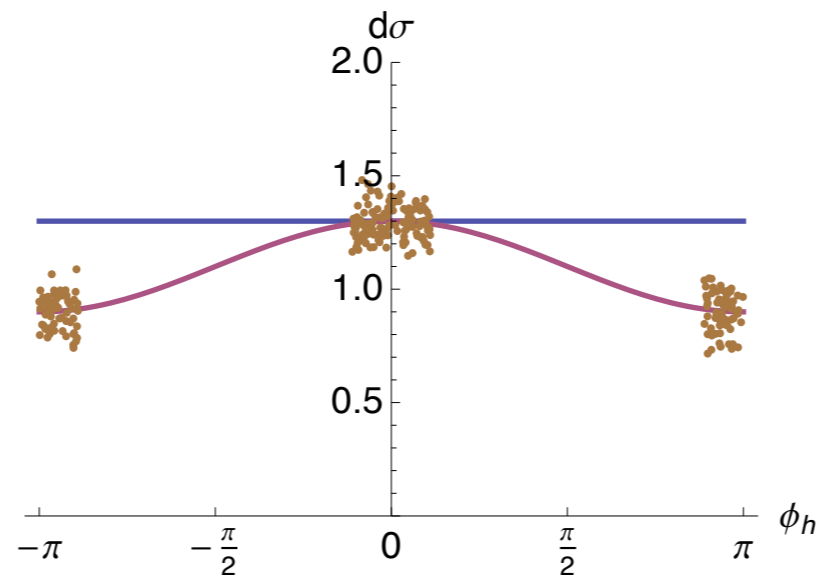


Beware: azimuthal coverage

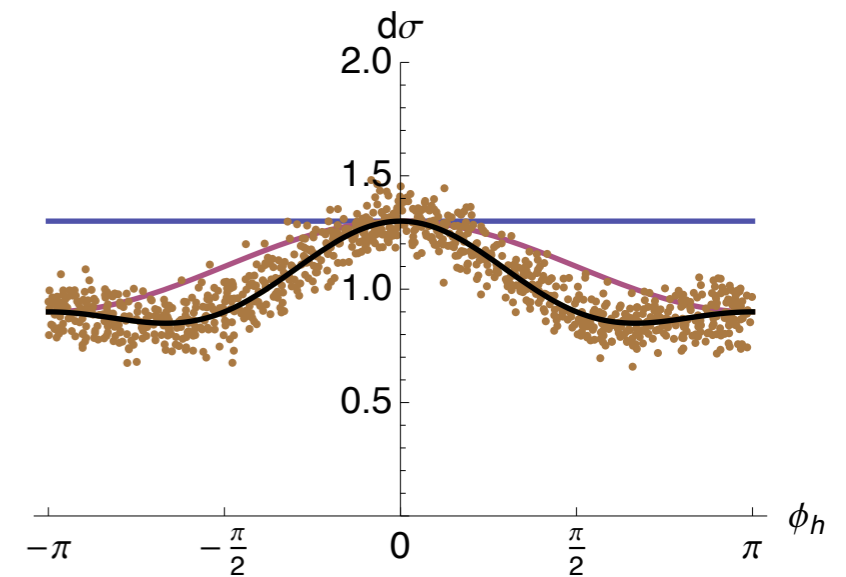
$$d\sigma = A + B \cos \phi_h + C \cos 2\phi_h$$



$$A = 1.3$$



$$A = 1.1, \quad B = 0.2$$



$$A = 1, \quad B = 0.2, \quad C = 0.1$$

Unpolarized sector

$$F_{UU,T} = \mathcal{C}[f_1 D_1],$$

$$F_{UU,L} = \mathcal{O}\left(\frac{M^2}{Q^2}, \frac{q_T^2}{Q^2}\right),$$

$$F_{UU}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{C} \left[-\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_T}{M_h} \left(xh H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{D}^\perp}{z} \right) - \frac{\hat{\mathbf{h}} \cdot \mathbf{p}_T}{M} \left(x f^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{H}}{z} \right) \right],$$

$$F_{UU}^{\cos 2\phi_h} = \mathcal{C} \left[-\frac{2 (\hat{\mathbf{h}} \cdot \mathbf{k}_T) (\hat{\mathbf{h}} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{MM_h} h_1^\perp H_1^\perp \right],$$

$$\mathcal{C}[wfD] = \sum_a x e_a^2 \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp}/z) w(\mathbf{p}_T, \mathbf{k}_T) f^a(x, p_T^2) D^a(z, k_T^2),$$

List of structure functions

| | observable | twist |
|---------------------|------------------------------------|-------|
| “SIDIS F_T ” | $F_{UU,T}$ | 2 |
| “SIDIS F_L ” | $F_{UU,L}$ | 4 |
| “Cahn” | $F_{UU}^{\cos \phi_h}$ | 3 |
| “Boer-Mulders” | $F_{UU}^{\cos 2\phi_h}$ | 2 |
| | $F_{LU}^{\sin \phi_h}$ | 3 |
| | $F_{UL}^{\sin \phi_h}$ | 3 |
| “Kotzinian-Mulders” | $F_{UL}^{\sin 2\phi_h}$ | 2 |
| “SIDIS g_1 ” | F_{LL} | 2 |
| “Polarized Cahn” | $F_{LL}^{\cos \phi_h}$ | 3 |
| “Sivers” | $F_{UT,T}^{\sin(\phi_h - \phi_S)}$ | 2 |
| | $F_{UT,L}^{\sin(\phi_h - \phi_S)}$ | 4 |
| “Collins” | $F_{UT}^{\sin(\phi_h + \phi_S)}$ | 2 |
| “Pretzelosity” | $F_{UT}^{\sin(3\phi_h - \phi_S)}$ | 2 |
| | $F_{UT}^{\sin \phi_S}$ | 3 |
| | $F_{UT}^{\sin(2\phi_h - \phi_S)}$ | 3 |
| “Worm gear” | $F_{LT}^{\cos(\phi_h - \phi_S)}$ | 2 |
| “SIDIS g_2 ” | $F_{LT}^{\cos \phi_S}$ | 3 |
| | $F_{LT}^{\cos(2\phi_h - \phi_S)}$ | 3 |

Unpolarized structure function

$$F_{UU,T} = \mathcal{C}[f_1 D_1]$$

$$\mathcal{C}[w f D] = \sum_a x e_a^2 \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp}/z) w(\mathbf{p}_T, \mathbf{k}_T) f^a(x, p_T^2) D^a(z, k_T^2),$$

Gaussian ansatz

$$F_{UU,T} = \mathcal{C}[f_1 D_1]$$

$$\mathcal{C}[w f D] = \sum_a x e_a^2 \int d^2 \mathbf{p}_T d^2 \mathbf{k}_T \delta^{(2)}(\mathbf{p}_T - \mathbf{k}_T - \mathbf{P}_{h\perp}/z) w(\mathbf{p}_T, \mathbf{k}_T) f^a(x, p_T^2) D^a(z, k_T^2),$$

$$f_1^a(x, p_T^2) = \frac{f_1^a(x)}{\pi \langle p_T^2 \rangle} e^{-\mathbf{p}_T^2 / \langle p_T^2 \rangle}, \quad D_1^a(z, k_T^2) = \frac{D_1^a(z)}{\pi \langle K_T^2 \rangle} e^{-z^2 \mathbf{k}_T^2 / \langle K_T^2 \rangle}$$

$$\mathcal{C}[f_1 D_1] = \sum_a x e_a^2 \frac{f_1(x) D_1(z)}{\pi (z^2 \rho_a^2 + \sigma_a^2)} e^{-\mathbf{P}_{h\perp}^2 / (z^2 \rho_a^2 + \sigma_a^2)}$$

$$f_1^a(x, p_T^2) = \frac{f_1^a(x)}{\pi \langle p_T^2(x) \rangle^a} e^{-\mathbf{p}_T^2 / \langle p_T^2(x) \rangle^a}, \quad D_1^a(z, k_T^2) = \frac{D_1^a(z)}{\pi \langle K_T^2(z) \rangle^a} e^{-z^2 \mathbf{k}_T^2 / \langle K_T^2(z) \rangle^a}$$

gmc_trans

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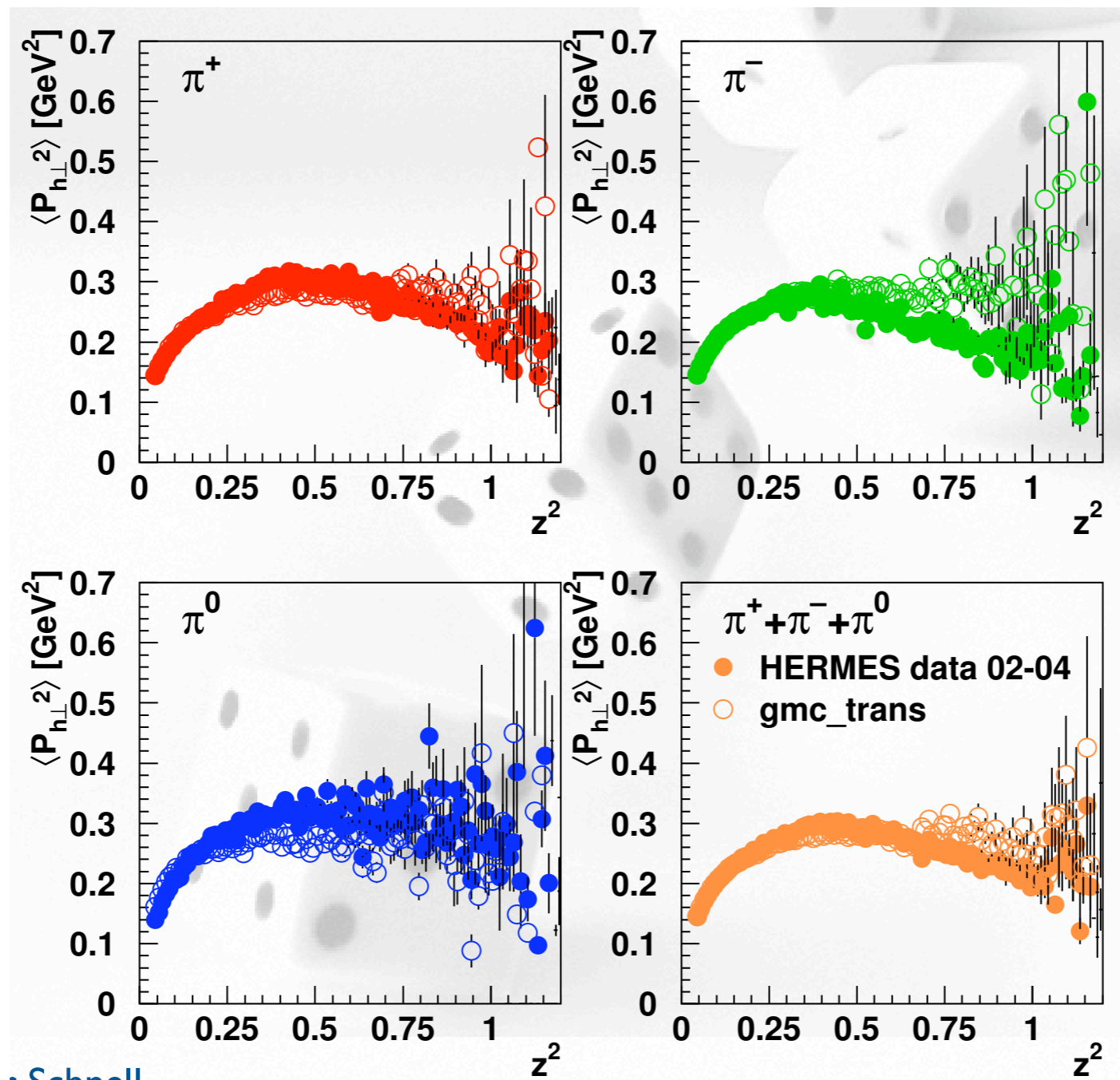
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gmc_trans

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- Implements several leading-twist terms of the cross section
- First attempt at tuning the parameters of the unpolarized TMDs
- Careful implementation of positivity bounds

Comparison with data

$$\langle k_{\perp}^2 \rangle = 0.14 \text{ GeV}^2, \quad \langle P_{\perp}^2 \rangle = 0.42 z^{0.54} (1 - z)^{0.37} \text{ GeV}^2.$$



unpublished!

TMDgen

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- Written in C++

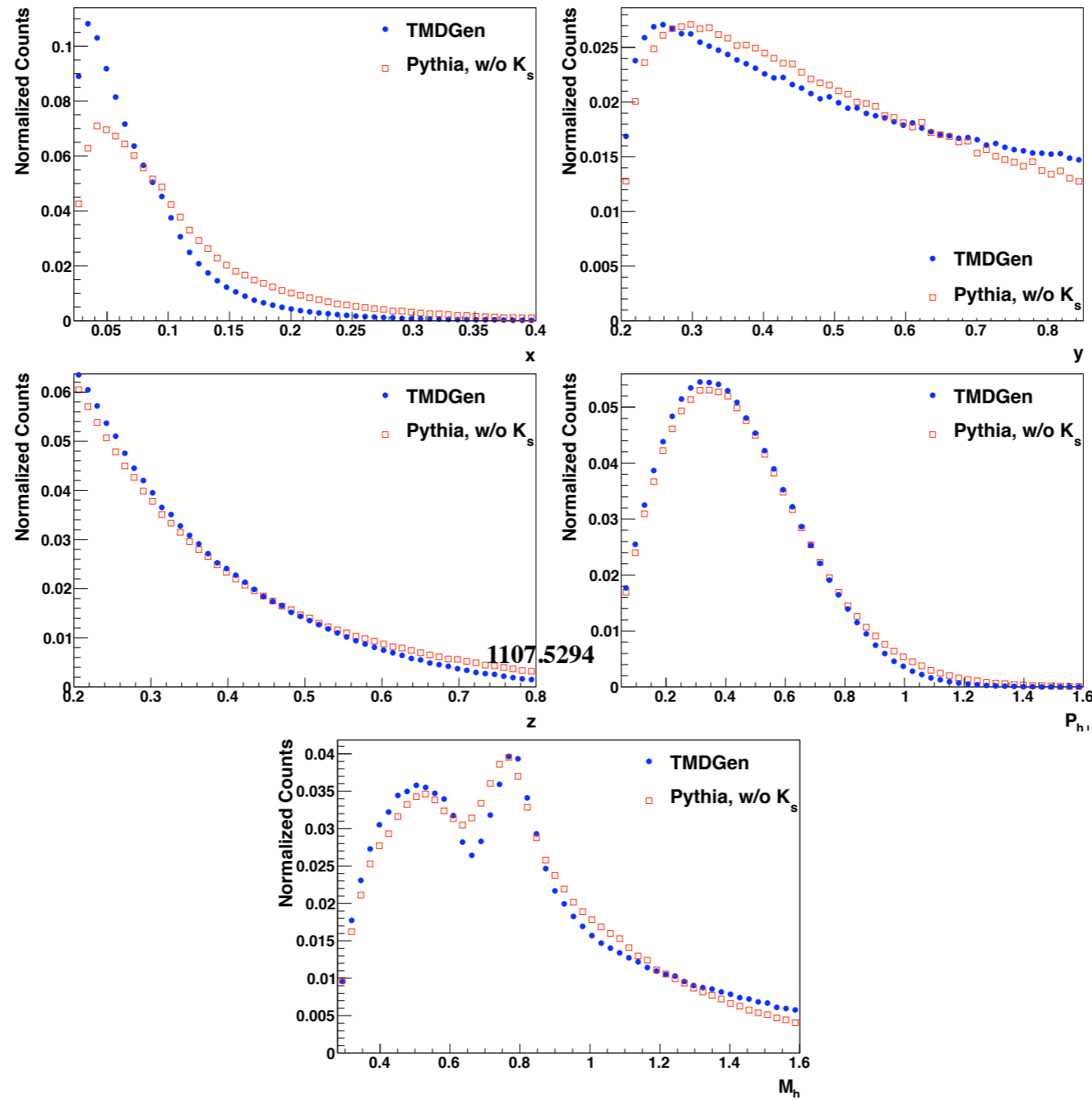


Figure 3.1: Comparison of 1D kinematic distributions from TMDGen and Pythia, in 4π , for $\pi^+\pi^0$ dihadrons. Listing the rows from top to bottom, and within each row from left to right, the panels are respectively the x , y , z , $P_{h\perp}$, and M_h distributions. TMDGen data is designated with blue circles, and Pythia data designated with red open squares.

TMDgen: still missing

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Unpol. TMD “state of the art”

$$f_1(x, k_T; Q) = \frac{1}{2\pi} \int d^2 b_T e^{-ik_T \cdot b_T} \left[C \otimes f_1 \left(\hat{x}; \frac{2e^{-\gamma_e}}{b_T} \right) \right] e^{-S'(b_T, Q)} e^{-S'_{\text{NP}}(x, b_T, Q, \alpha_i)}$$

T. Rogers, M. Aybat, arXiv:1101.5057

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collinear PDF



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pQCD

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nonperturbative part of TMD

T. Rogers, M. Aybat, arXiv:1101.5057

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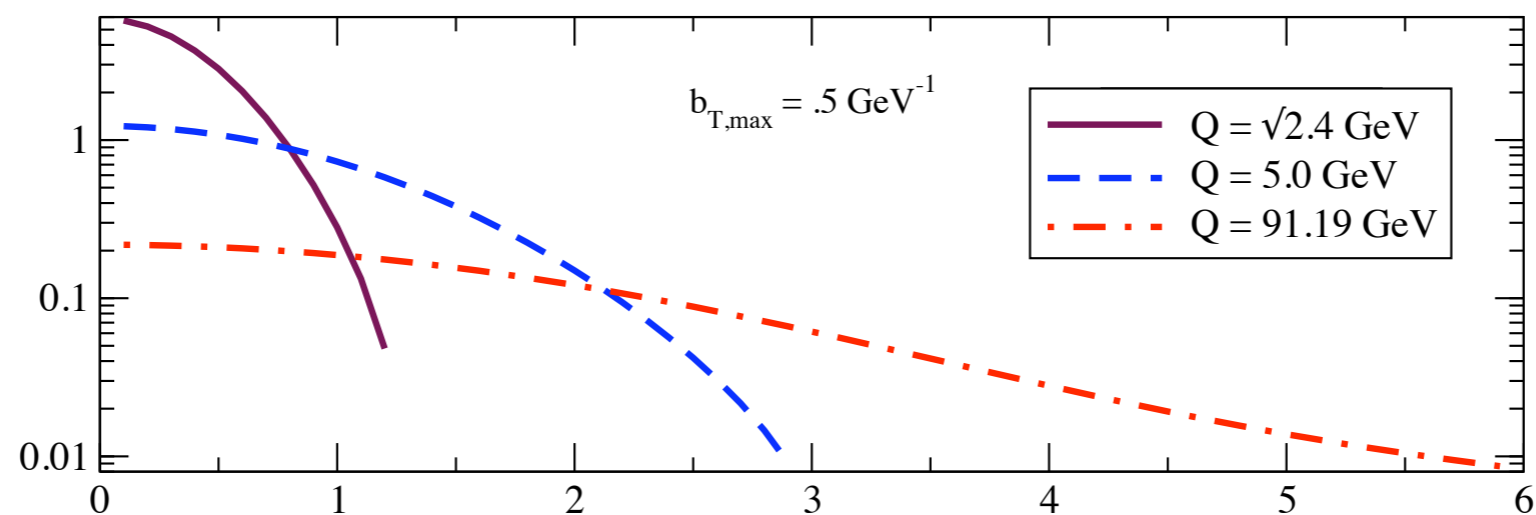
The diagram illustrates the components of the unpol. TMD equation. A dashed orange box encloses the terms $C \otimes f_1$, $e^{-S'(b_T, Q)}$, and $e^{-S'_{\text{NP}}(x, b_T, Q, \alpha_i)}$. Arrows point from the labels 'collinear PDF', 'pQCD', and 'nonperturbative part of TMD' to these respective terms. The text 'Fourier-transform of the TMD' is located at the bottom of the dashed box.

T. Rogers, M. Aybat, arXiv:1101.5057

Unpol. TMD “state of the art”

$$f_1(x, k_T; Q) = \frac{1}{2\pi} \int d^2b_T e^{-ik_T \cdot b_T} \left[C \otimes f_1 \left(\hat{x}; \frac{2e^{-\gamma_e}}{b_T} \right) \right] e^{-S'(b_T, Q)} e^{-S'_{\text{NP}}(x, b_T, Q, \alpha_i)}$$

Up Quark TMD PDF, $x = .09$



T. Rogers, M. Aybat, arXiv:1101.5057
Landry, Brock, Nadolsky, Yuan, PRD67 (03)
P. Schweitzer, T. Teckentrup, A. Metz, PRD81(10)

ResBos

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- <http://hep.pa.msu.edu/resum/index.html#SIDIS>

Fourier-transformed TMDs

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- Since the TMD evolution formalism is done in bT space, it may be useful to implement the Fourier-transformed formulas in the MC generator

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- Since the TMD evolution formalism is done in bT space, it may be useful to implement the Fourier-transformed formulas in the MC generator
- This may also be useful to study Bessel-weighted extraction methods
Boer, Gamberg, Musch, Prokudin, arXiv:1107.5294

Conclusions

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- Every collaboration and even every analysis group uses its own different solution.
- Not enough attention is devoted to publishing the ideas and share them.
- I would personally focus first on SIDIS generators, although I think the effort of modifying full event generators is extremely interesting