

Status of Unpolarized Fragmentation Functions

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Global Analyses of Unpolarized FFs

- Light charged hadrons (l.c.h.) $\pi^\pm, K^\pm, p/\bar{p}$
- Σ Hadron (quark) spins and charge

Most recent are

Kniesl-Kramer-Pötter (2000)

Albino-Kniesl-Kramer (2005)

$$D_u^{\pi^\pm}(x, M_0) = D_d^{\pi^\pm}(x, M_0)$$

$$D_u^{K^\pm}(x, M_0) = D_s^{K^\pm}(x, M_0)$$

$$D_u^{p/\bar{p}}(x, M_0) = 2D_d^{p/\bar{p}}(x, M_0)$$

- Update of KKP

- $D_{u,d,s}^h$ from OPAL tagging probabilities

- Also for K_0^S, Λ

Since 2000, l.c.h. studies also from

- Bourhis, Fontannaz, Guillet, Werlen (charged)
- Kretzer ($\pi^\pm, K^\pm$, charged)

Data

Rely mostly on $e^+ + e^- \rightarrow Z, \gamma \rightarrow X + h (= h^+ + h^-)$

- h identified
- ALEPH, DELPHI, SLD ($\sqrt{s} = 91$ GeV), TPC (29 GeV) (uds, c, b)
- **OPAL tagging probabilities** ($\sqrt{s} = 91$ GeV) (u, d, s, c, b)

OPAL data rather model independent

Primary quark info by tagging high energy hadrons

Excluded in AKK:

- h unidentified (contaminated with other charged particles) -
use for checking
- $x_p < 0.1$ (soft gluon logarithms)

Calculation

Factorization theorem I

$(e^+e^- \rightarrow \text{parton } i \rightarrow h)$

$$\frac{d\sigma^h}{dx_p}(x_p, s) = \sum_i \int_{x_p}^1 \frac{dy}{y} \frac{d\sigma^i}{d(x_p/y)}\left(\frac{x_p}{y}, M_f, s\right) D_i^h(y, M_f)$$

Factorization theorem II

(DGLAP evolution)

$$\frac{d}{d \ln M_f} D_i^h(x, M_f) = \sum_j \int_x^1 \frac{dy}{y} P_{ij}\left(\frac{x}{y}, a_s(M_f)\right) D_j^h(y, M_f)$$

Neglect $O(1/\sqrt{s})$ higher twist $D_i^h(x, M_f)$ are universal

Work to NLO, freedoms:

- Scale: $\mu = M_f = \sqrt{s}$
- Scheme: $\overline{\text{MS}}$
- $D_q^h(x, M_f < 2m_q) = 0$

$$D_{q=\bar{q},g}^h(x, M_0 = \sqrt{2} \text{ GeV}) = N x^\alpha (1-x)^\beta$$

$\alpha_s(M_Z)$ Determination

Experimental errors

Vary $\alpha_s(M_Z)$ until $\Delta\chi_{\text{DF}}^2 = 1$

Theoretical errors

Fits with $\frac{M_f}{\sqrt{s}} = \frac{1}{2}, 2$

AKK

$$\begin{aligned}\alpha_s(M_Z) &= 0.1176^{+0.0053(E)+0.0007(T)}_{-0.0067(E)-0.0009(T)} \\ &= 0.1176^{+0.0053}_{-0.0068}\end{aligned}$$

KKP

$$\alpha_s(M_Z) = 0.1170^{+0.0058}_{-0.0073}$$

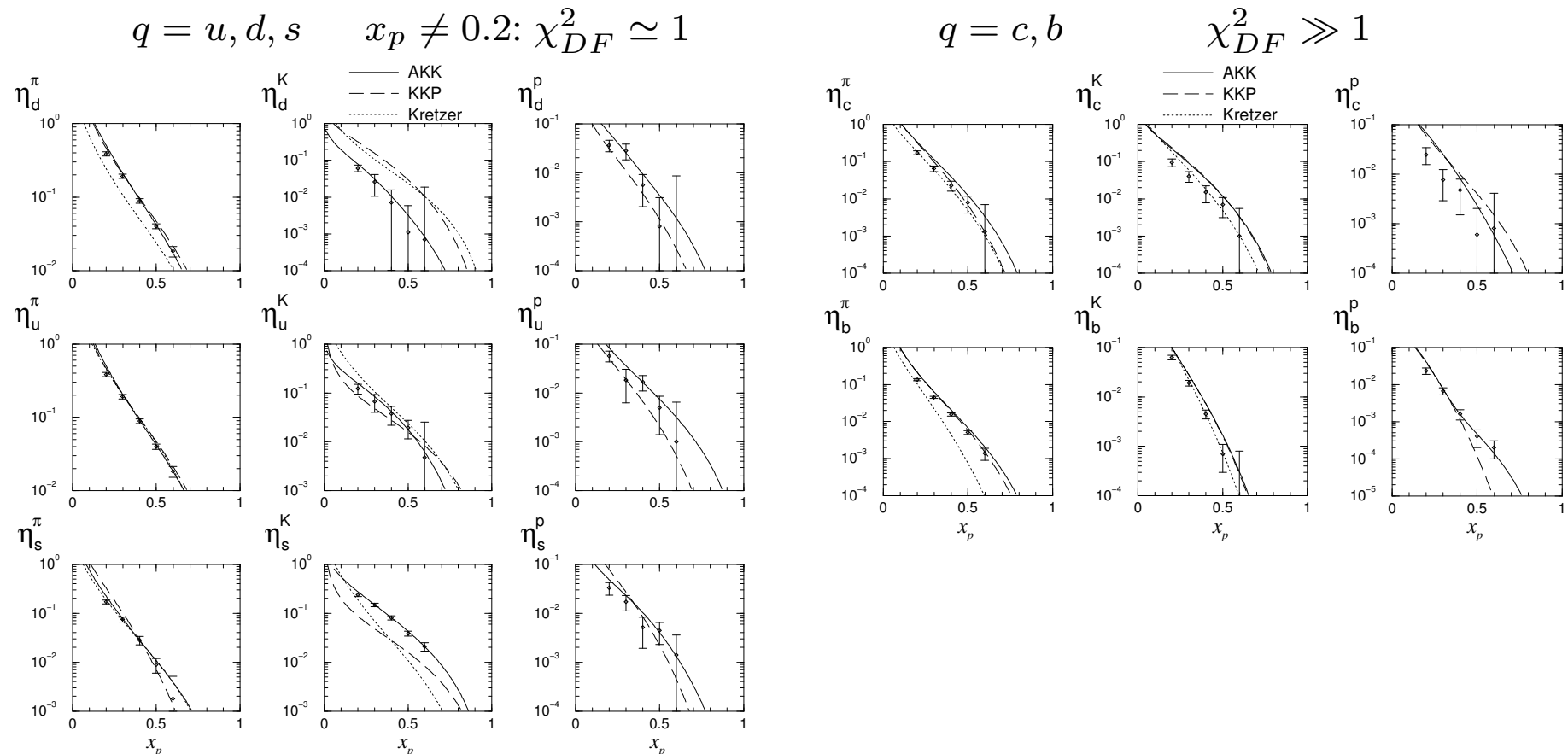
$$\text{PDG: } \alpha_s(M_Z) = 0.1187 \pm 0.002$$

Inclusive hadroproduction data sensitive to $\alpha_s(M_Z)$

OPAL tagging probabilities

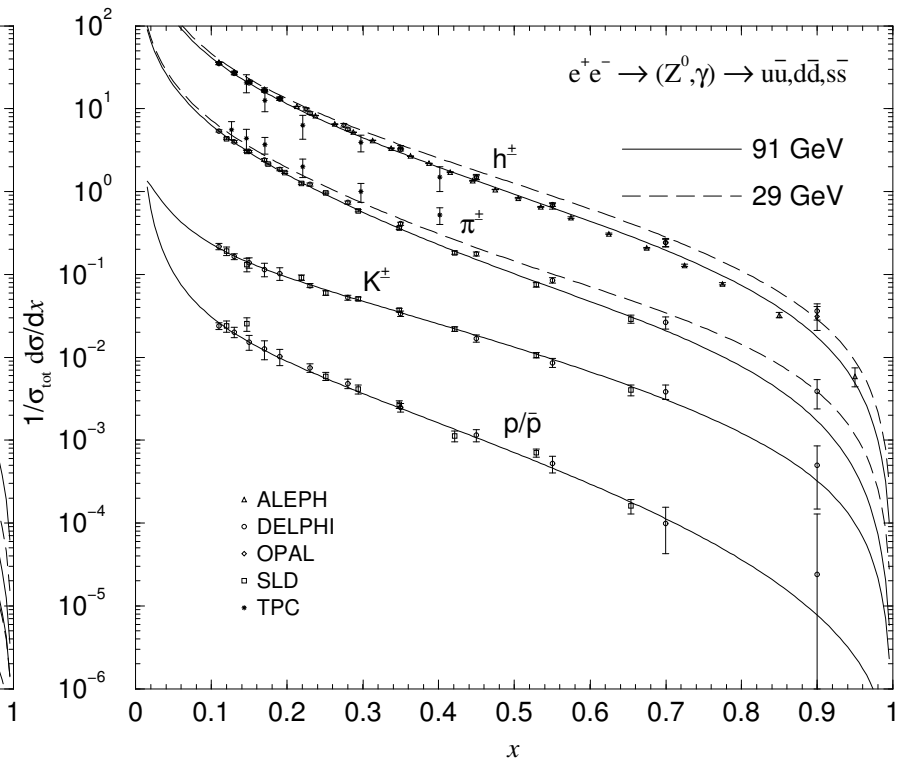
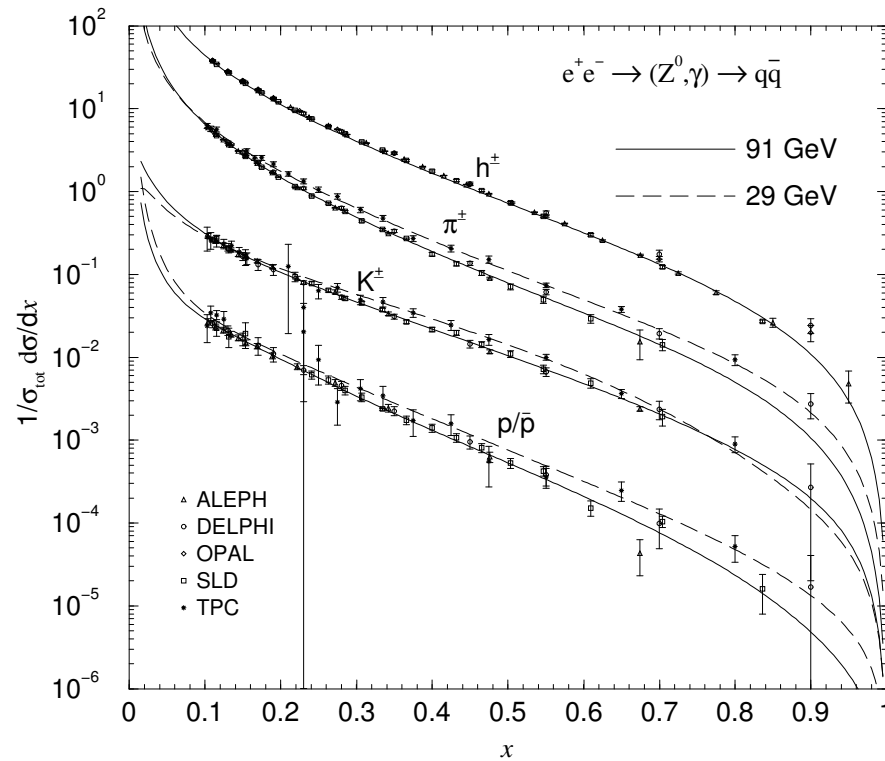
G. Abbiendi et al., Eur. Phys. J. C 16 (2000) 407

$$\eta_{q=\bar{q}}^h(x_p, s) = \int_{x_p}^1 dx \frac{\frac{d\sigma_q^h}{dx}(x, s)}{\sigma_q(s)}$$

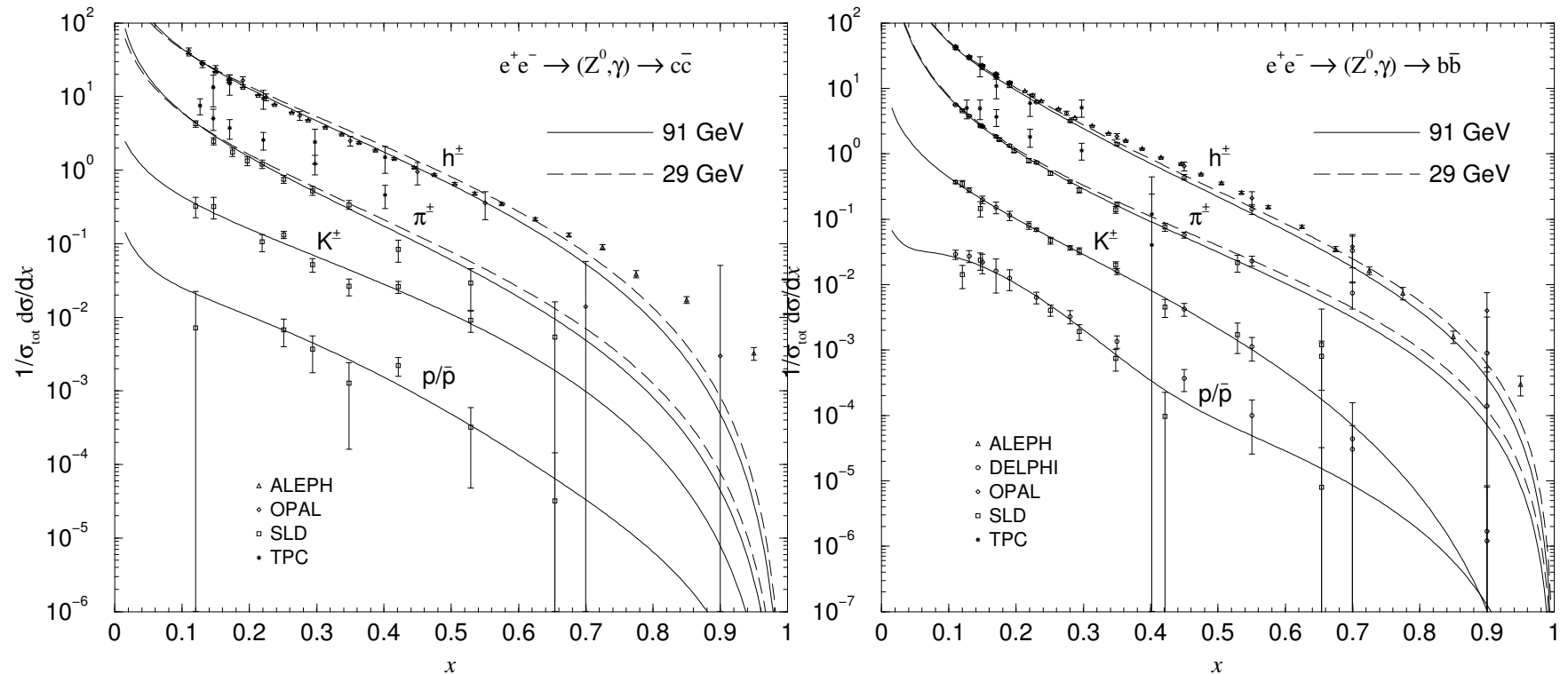


This framework: OPAL low x + heavy quark $\nleftrightarrow$ other data

Light charged hadron data



Light charged hadron data



ALEPH, OPAL summed l.c.h. data overshoot (see KKP work)

→ These data may contain other charged particles

Gluon sensitivity

Not included in fit

3-jet data $\simeq D_g(x, M_f = 2E_{\text{jet}})$

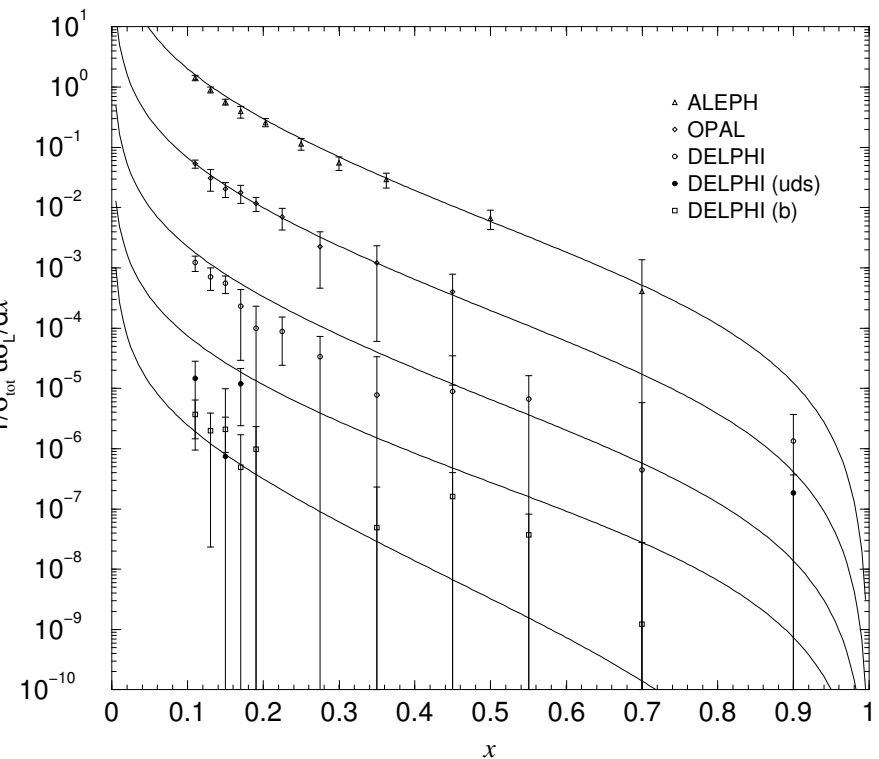
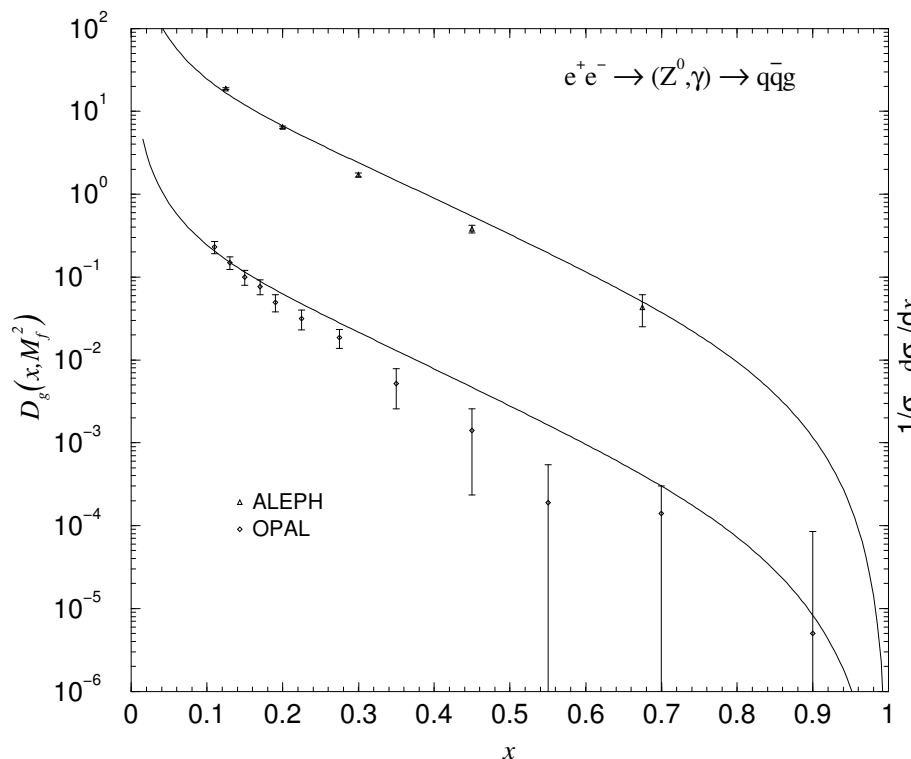
$E_{\text{jet}}(\text{ALEPH}) = 26.2 \text{ GeV}$

$E_{\text{jet}}(\text{OPAL}) = 40.1 \text{ GeV}$

$d\sigma_L$ well defined

D_g at LO

$\rightarrow D_g \text{ OK}$



$$p + p(\bar{p}) \rightarrow h + X$$

Not included in fit

$$M_f/p_T = 1/2, 1, 2$$

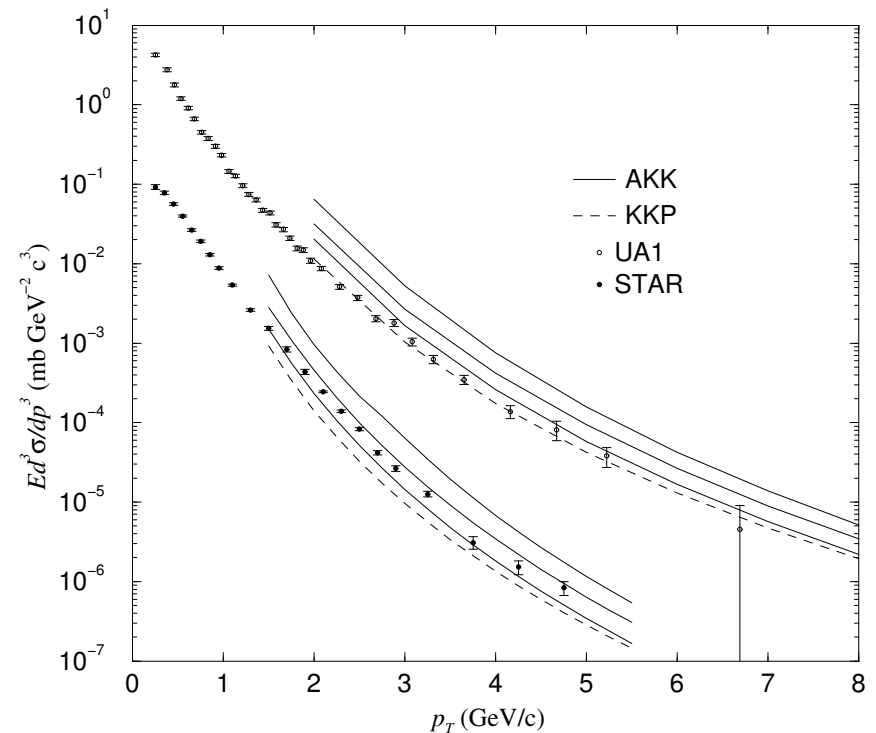
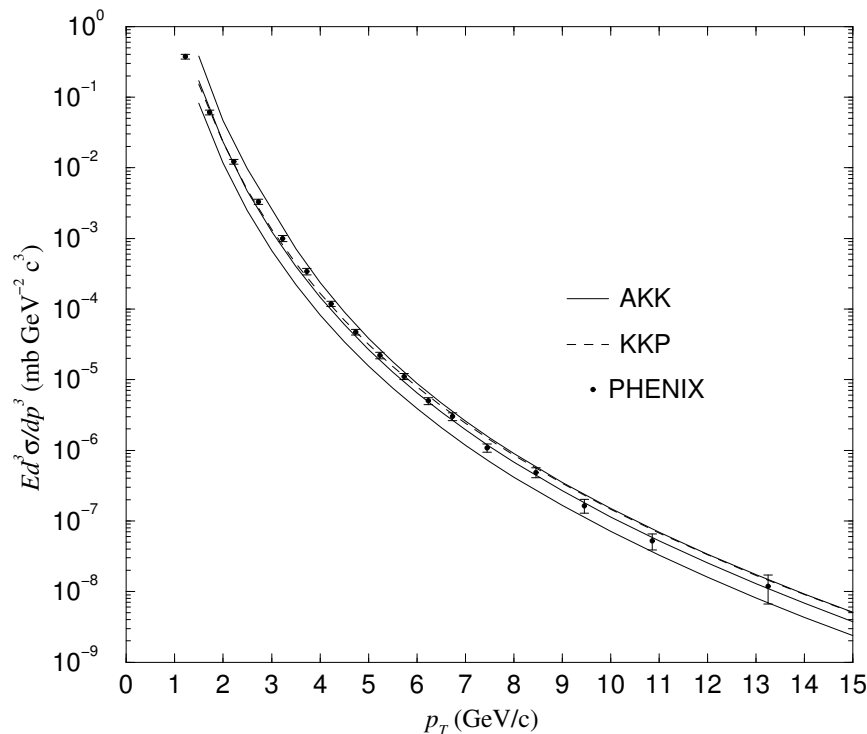
PHENIX 200 GeV

STAR / UA1 200 / 630 GeV

$$p + p \rightarrow \pi^0 + X$$

$$p + p/\bar{p} \rightarrow K_S^0 + X$$

$$D_a^{\pi^0}(x, M_f) = \frac{1}{2} D_a^{\pi^\pm}(x, M_f) \quad D_a^{K_S^0}(x, M_f) = \frac{1}{2} D_{a(u \leftrightarrow d)}^{K^\pm}(x, M_f)$$

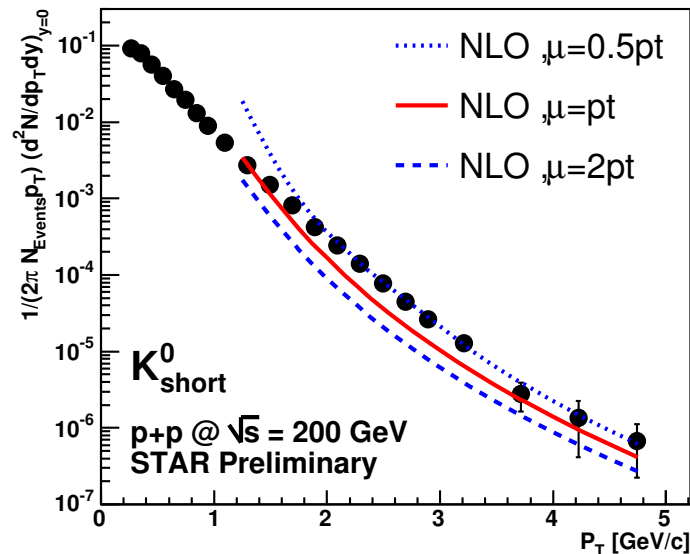


Neutral weakly decaying K_S^0 and Λ

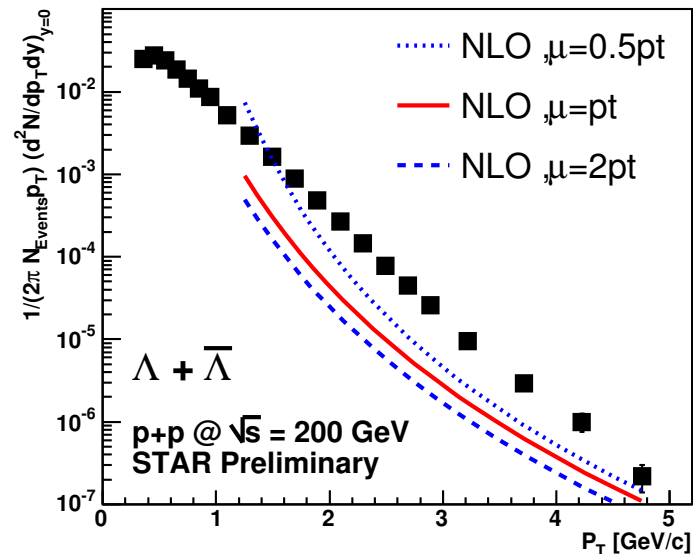
Decaying to charged particles $\rightarrow$ production observable

Previous determinations by

- K_S^0 : Greco, Rolli - HERWIG (1995)
- Λ : de Florian, Stratmann, Vogelsang (1998);
Bourrely, Soffer (2003)



KKP ($K^\pm$)



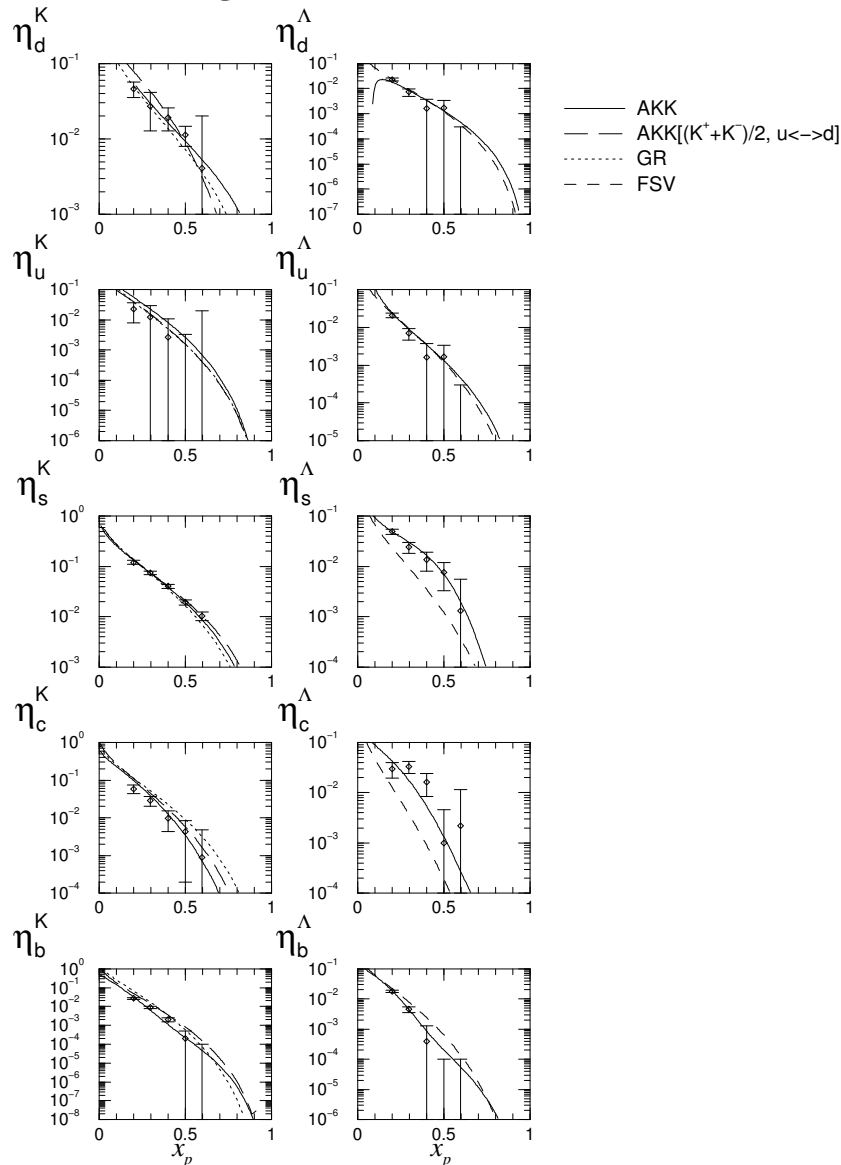
FSV

New n.w.h. data from STAR@RHIC merits improved FFs

K_S^0, Λ - OPAL tagging probabilities

Data quality: n.w.h. < l.c.h.

- Fix $\alpha_s(M_Z) = 0.1176$ (AKK central value)
- Fix gluon FF (see later slide)



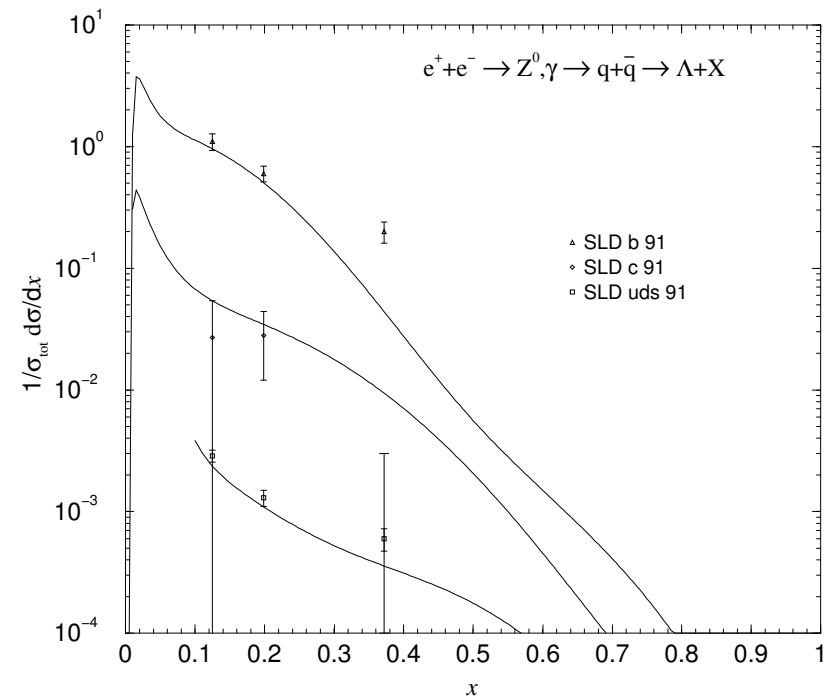
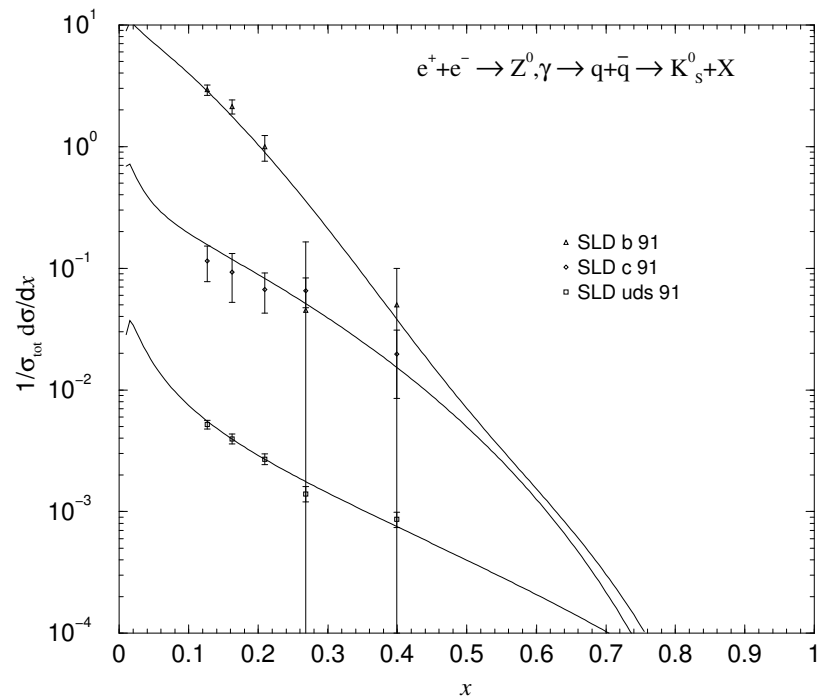
Again, separate u, d, s with OPAL tagging probabilities

Low x + heavy quark data:
good fit
(in contrast to l.c.h. data)

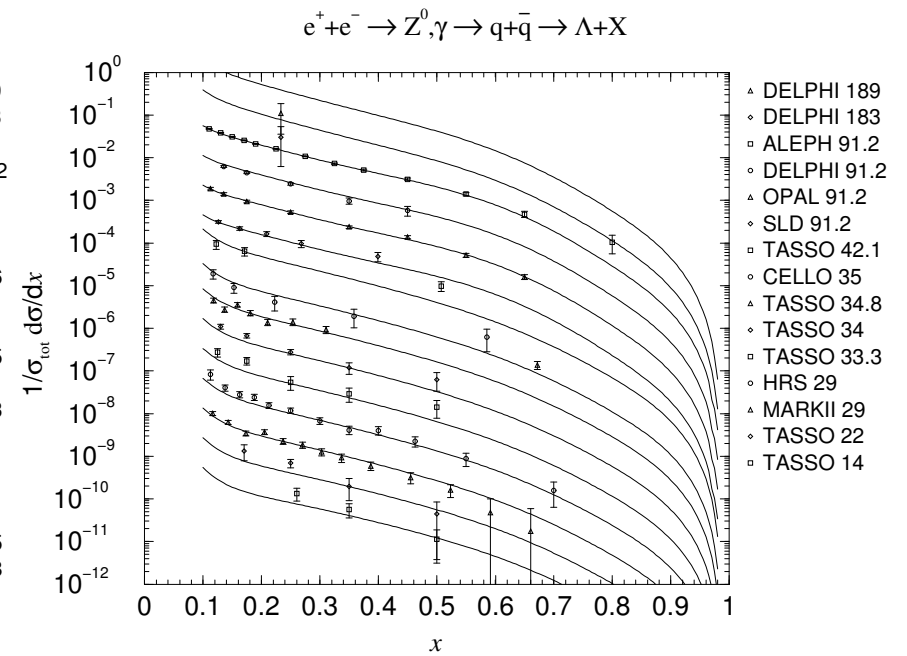
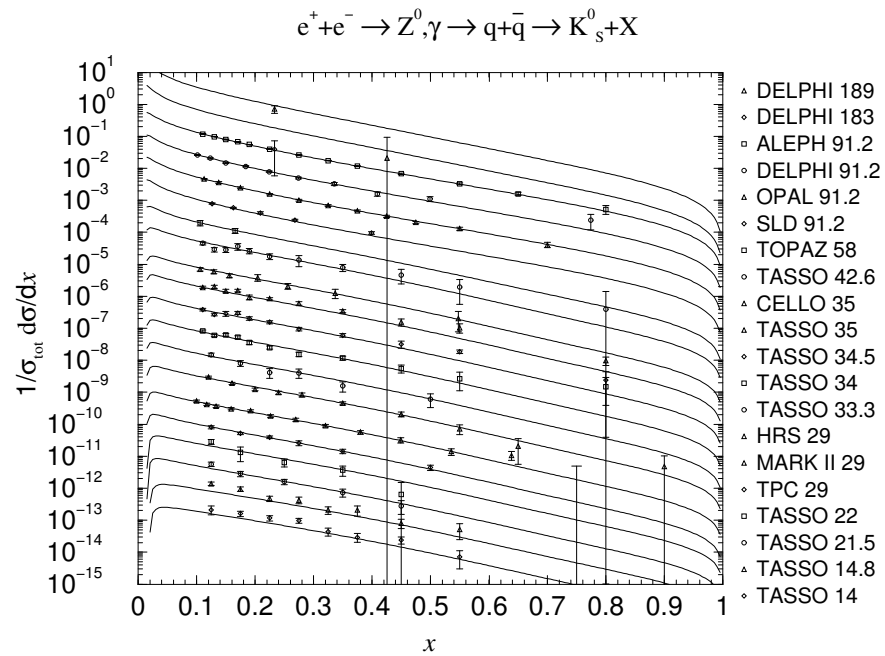
Λ , large x : $s, c \gg u, d, b$

Λ implicitly contains
 $\text{parton} \rightarrow \Sigma^0 \rightarrow \Lambda$

K_S^0, Λ - quark tagging

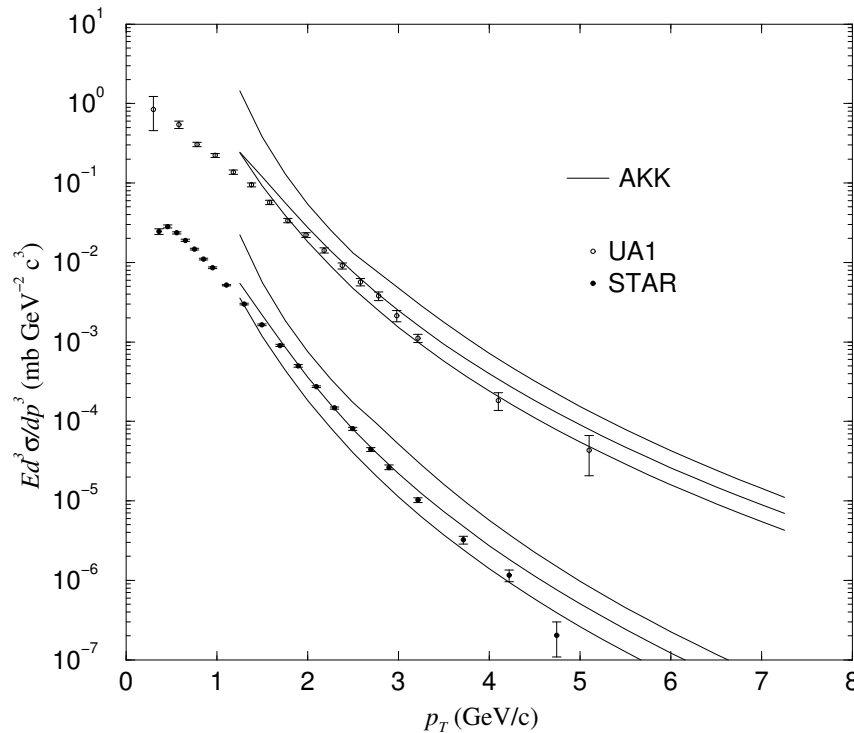


K_S^0, Λ - untagged



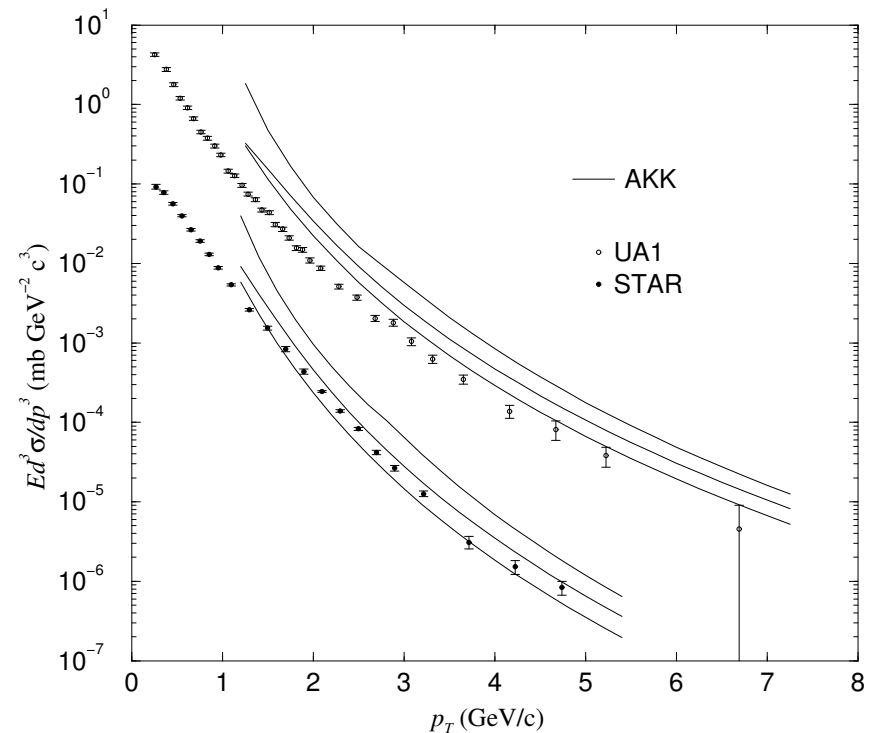
$$p + p(\bar{p}) \rightarrow K_S^0/\Lambda + X$$

$$D_g^\Lambda = \frac{D_g^p}{3} \text{ (3: STAR motivated)}$$



Strong dependence on D_g^Λ

$$D_g^{K_S^0} = \frac{1}{2} D_g^{K^\pm}$$



Summary

AKK: Includes OPAL tagging probabilities

$\rightarrow g, u, d, s, c, b$ for $\pi^\pm, K^\pm, p/\bar{p}, K_S^0, \Lambda$ for first time

Sensible result for $\alpha_s(M_Z)$

AKK l.c.h., compared to KKP:

- Smaller $d \rightarrow K^\pm$, larger $s \rightarrow K^\pm$
- Better agreement with K_S^0 @STAR, worse with K_S^0 @UA1

AKK n.w.h.:

- $K_S^0 \simeq$ GR's K_S^0 @STAR good, K_S^0 @UA1 not
- $s, c \rightarrow \Lambda \gg$ FSV's Λ @STAR+UA1 good

<http://www.desy.de/simon/AKK2005FF.html>

Simple to make KKP $\rightarrow$ AKK update to software