

GPD's for experts

Ch. Weiss (Jefferson Lab), QCD–N '06, June 12–16, 2006

3D quark/gluon structure
of nucleon

$$f(x_1, x_2, \vec{\rho})$$

longitud.
momentum **transverse
position**

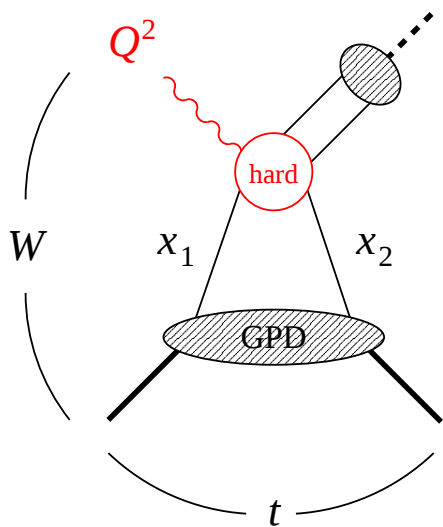
- Vector meson production at HERA ($J/\psi, \phi, \rho$)
 - Space–time evolution
 - Tests of factorization
 - Data on t –dependence

“Lessons” for
JLab at 12 GeV
future EIC
- Non-perturbative dynamics
 - Pion cloud at $\rho \sim 1/M_\pi, \dots$
- High–energy pp collisions with hard processes
 - Central collisions
 - Unitarity limit
 - Diffractive Higgs production

LHC
Tevatron

- Hard exclusive processes in ep scattering: Factorization

[D. Müller et al. 94, Brodsky et al. 94; Collins et al. 96; Radyushkin 96, Ji 96, . . .]

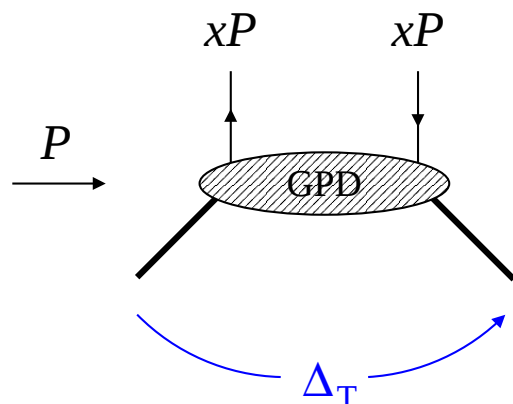


- γ^* reacts with quasi-free parton emitted/absorbed by target
- Generalized parton distribution $f(x_1, x_2, t)$ universal (process-independent)!

$$\gamma^* p \rightarrow \gamma + p \quad \text{Deeply virtual Compton scattering}$$
$$\gamma_L^* p \rightarrow \rho + p \quad \text{Vector meson production}$$

$J/\psi + p$ Heavy quarkonium
(gluon distribution)

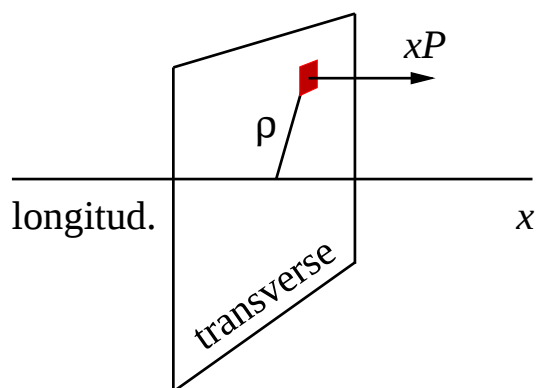
- Transverse spatial distribution of partons ($x_1 = x_2$) [Burkardt 02; Diehl 02]



$$f(x, t) = \int d^2\rho \, e^{-i\vec{\Delta}_T \cdot \vec{\rho}} \, q(x, \rho)$$

form factor
of quarks with
longitudinal
momentum xP

transverse spatial
distribution

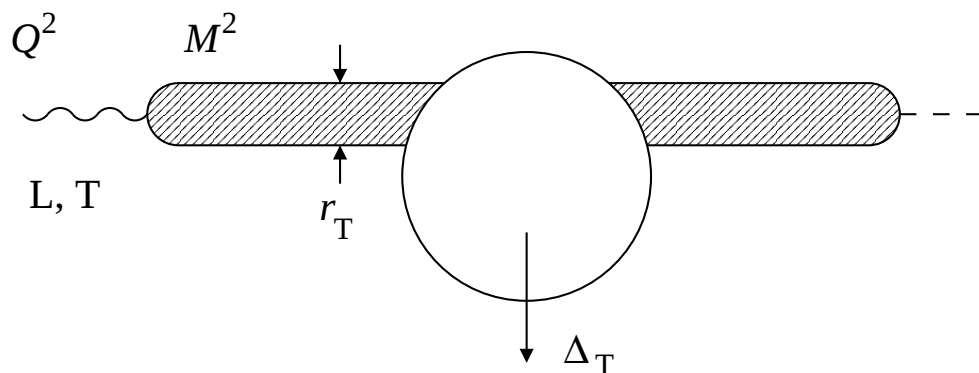


$$\int d^2\rho \, q(x, \rho) = q(x) \quad \text{total quark density}$$

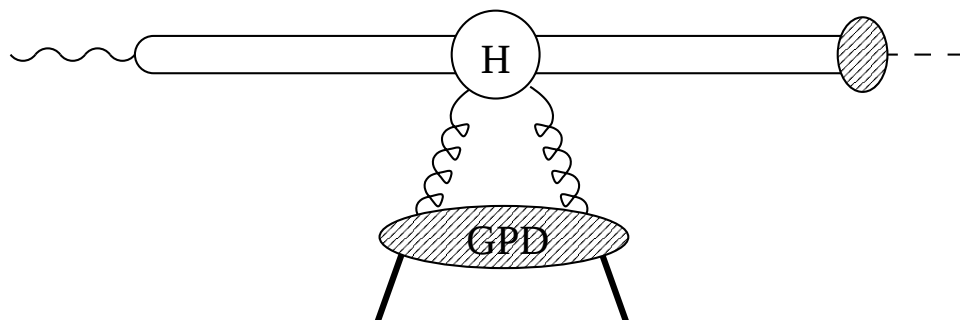
$$\langle \rho^2 \rangle = 4 \frac{\partial}{\partial t} \frac{f(x, t)}{f(x, t=0)} \quad \text{transv. size of nucleon, } x\text{-dependent!}$$

- Space–time evolution in target rest frame: $W^2 \gg Q^2$

[Review: Bauer et al. 78; Brodsky et al. 94]



$$l_{\text{coh}} = \frac{2\nu}{Q^2 + M^2}$$



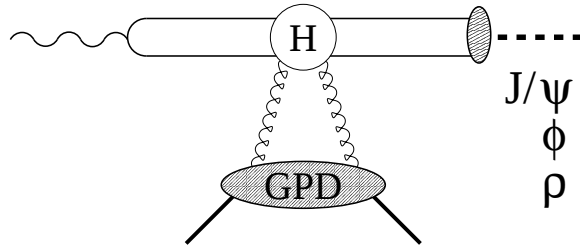
- “Mix” of configurations:
 r_T transv. size
 M^2 inv. mass

- Bjorken limit dominated by small–size configurations
 $r_T \sim 1/Q$ (“dipoles”)

$$\text{Amp} \sim r_T^2 G(x_1, x_2; t)$$

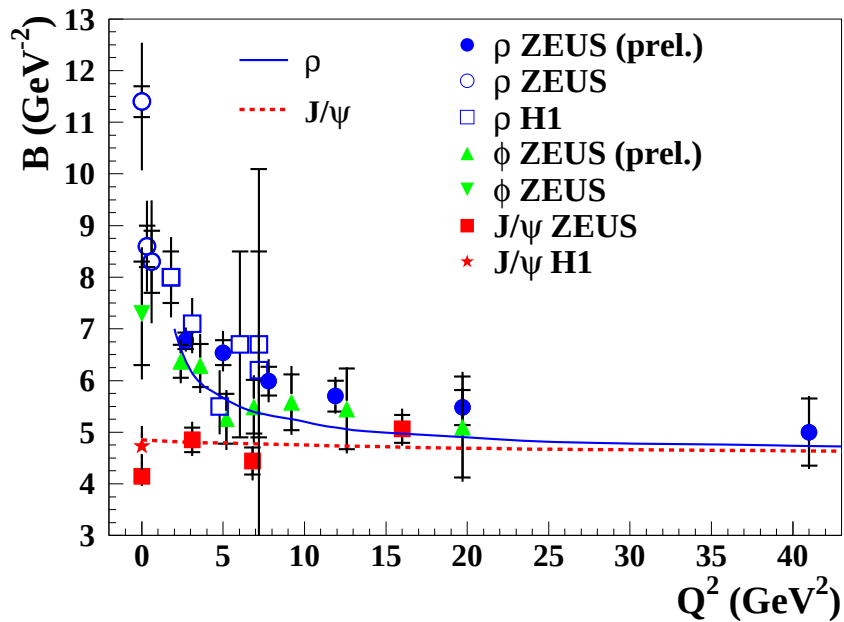
- Δ_T dependence probes transverse size of interacting system!

- Vector meson production at HERA: Tests of factorization

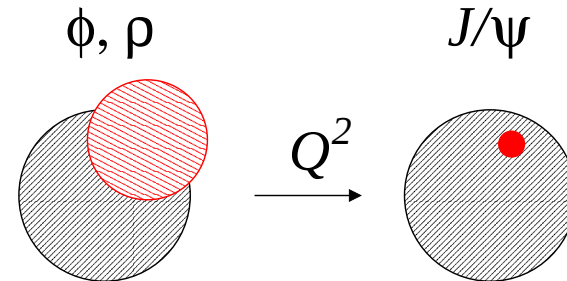


- J/ψ and ϕ, ρ (small x)
probe gluon GPD

- “Universality” of t -slopes
at large Q^2 shows dominance of
pointlike configurations

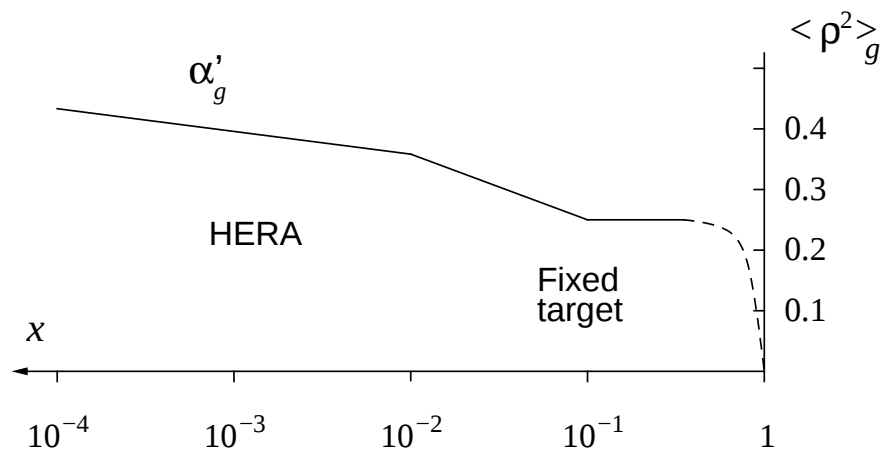
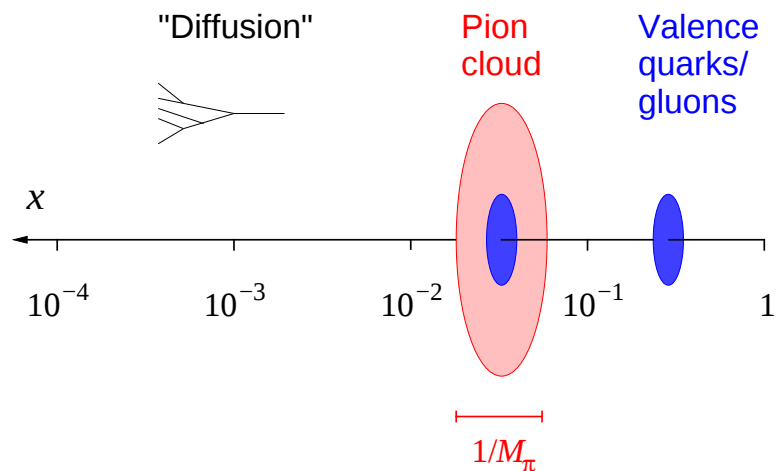


$$\frac{d\sigma}{dt} \propto \left[\frac{G(x_1, x_2, t)}{G(x_1, x_2, 0)} \right]^2$$



[A. Levy 05; Frankfurt, Strikman, CW 05]

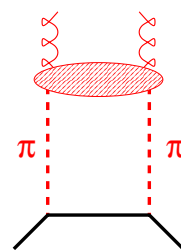
- Transverse gluonic size of nucleon: x -dependence



(Scale $Q^2 \approx 3 \text{ GeV}^2$)

- Gluonic transverse size increases with decreasing x

- Pion cloud contributes at $x < M_\pi/M_N$ [Strikman, CW 03]



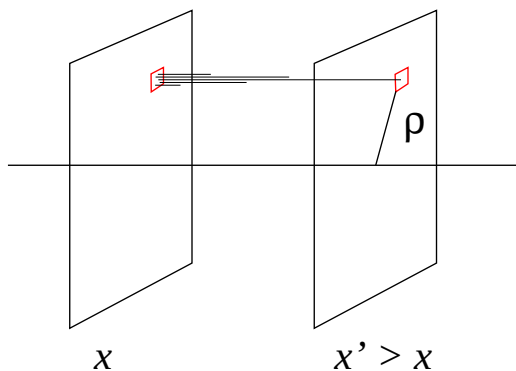
$$G(x, \rho) \sim e^{-2M_\pi \rho}$$

"Yukawa tail"

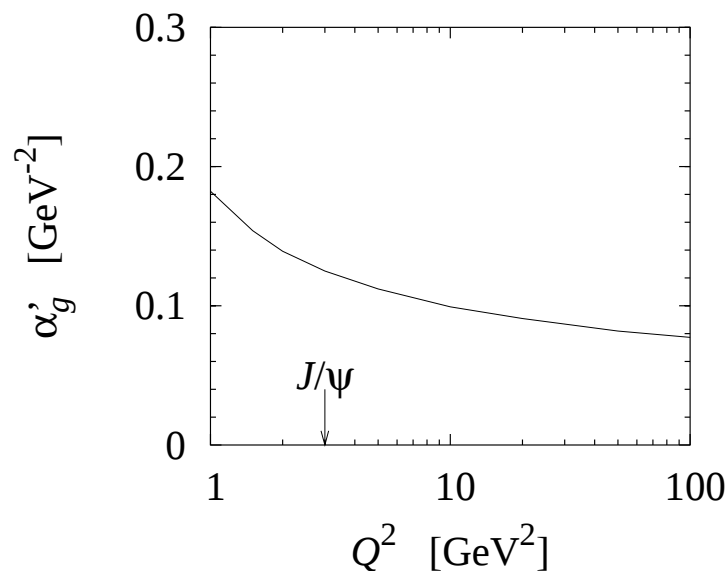
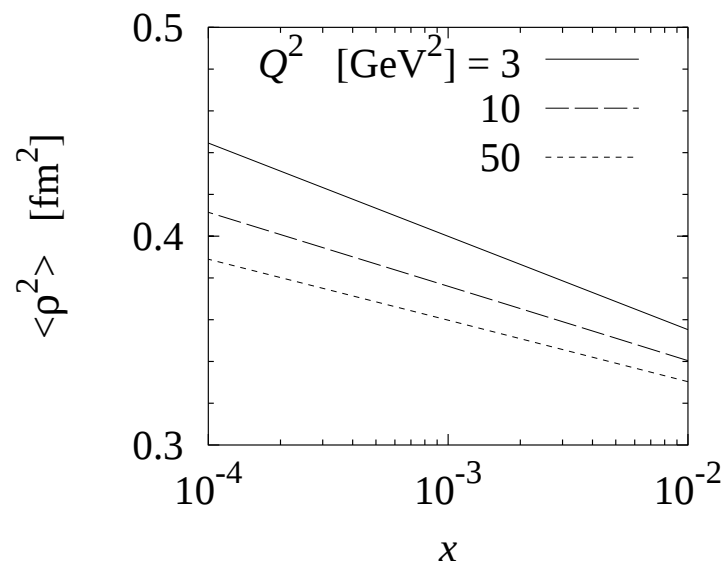
- Small x : Logarithmic growth with $\alpha'_g \ll \alpha'_{\text{soft}}$ ("diffusion")

- Effect of DGLAP evolution

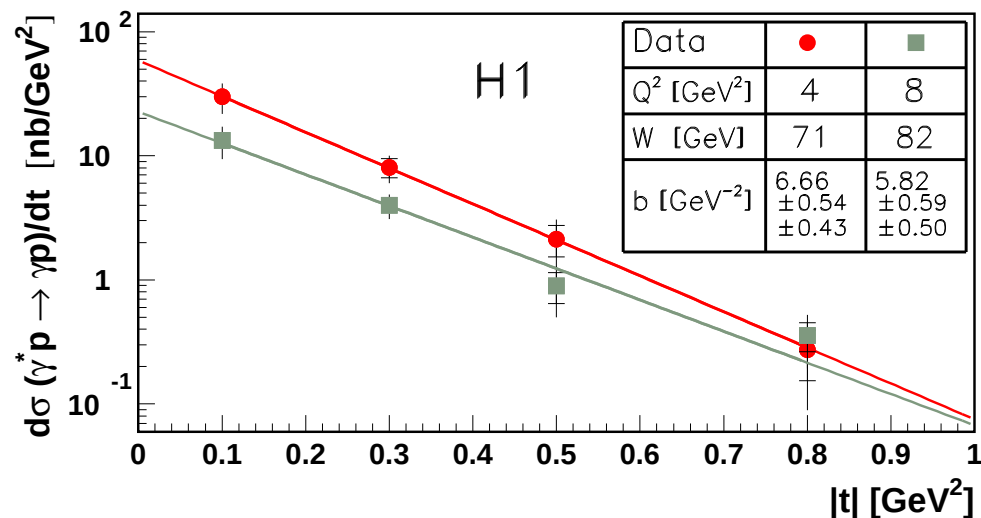
[Frankfurt, Strikman, CW 03]



- Partons decay locally in transverse position ($Q^2 \gg 1/R_{\text{nucl}}$)
- Transverse size $\langle \rho^2 \rangle$ decreases with increasing Q^2
- Higher Q^2 slows growth of size with $\log(1/x)$: α'_g decreases



- HERA DVCS data



[H1 Collab. (Aktas et al.) 05]

- Comparison of t -slopes

$$B(\text{DVCS}) \approx B(\rho) > B(J/\psi)$$

... suggests non-negligible hadronic-size contributions in DVCS!

- Evolution at small x implies

$$\langle \rho^2 \rangle_q \approx \langle \rho^2 \rangle_g$$

- Careful when using DVCS data to extract $\langle \rho^2 \rangle$

[D. Müller 06]

- Towards probing GPDs at fixed-target energies

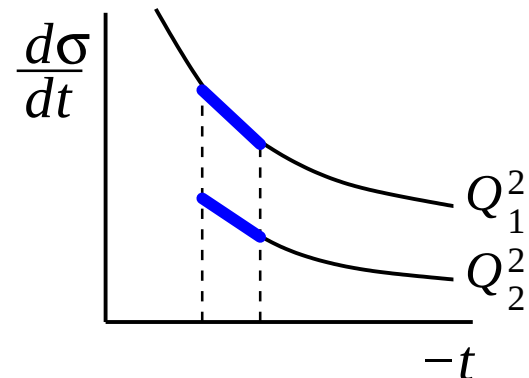
- Need to understand space-time evolution in target rest frame

$$\Delta_{\parallel} \neq 0, \quad l_{\text{coh}} \leq R_p$$

→ Limiting behavior of GPDs ($x_{1,2} \rightarrow 0$)

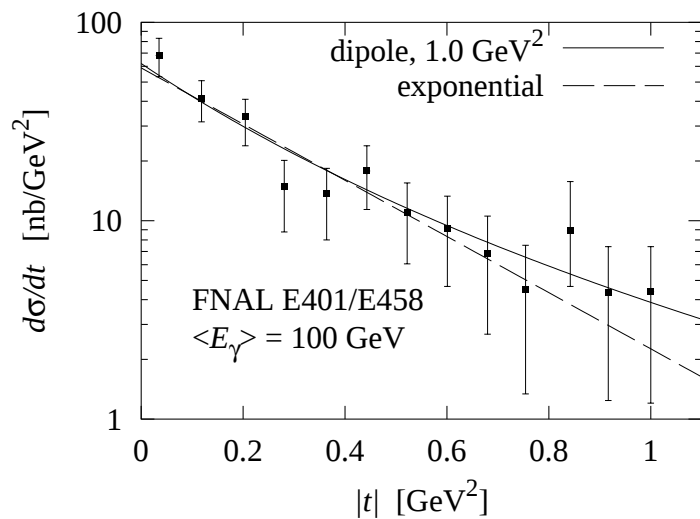
→ Physical scale of power corrections

- Measure t -slopes and their change with Q^2 ($t_{\text{min}} \neq 0$)

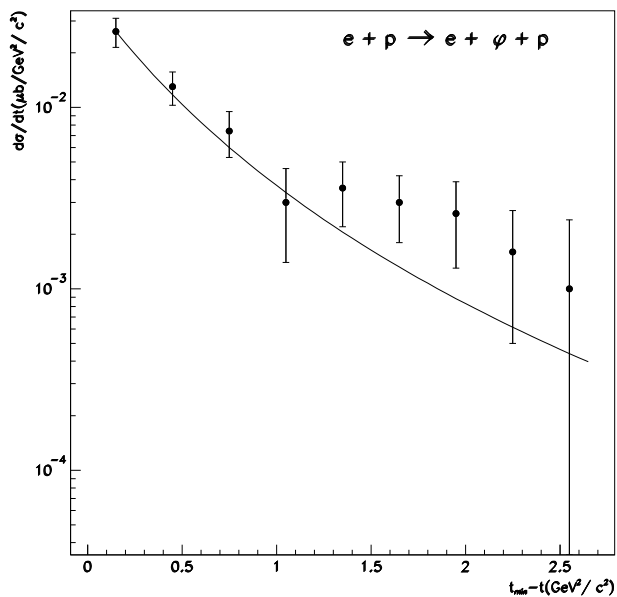


→ Transverse size of interacting configurations

→ Separate “hard” and “soft” components



[FNAL 458 (81), recoil proton det.]



[CLAS 02 Lukashin et al.]

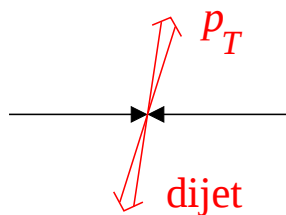
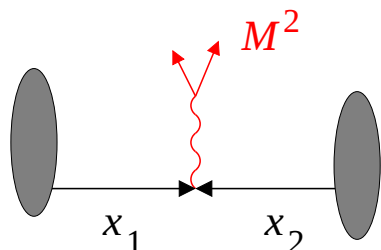
– Start from “simple” channels

$$J/\psi \rightarrow \phi \rightarrow \rho \rightarrow \gamma$$

gluon gluon gluon
quark

– t -dependence of gluon GPD
extracted from J/ψ data
consistent with CLAS ϕ data

- High-energy pp collisions with hard processes



- Hard scattering process induced by parton-parton collision

$$x_1 x_2 = M^2/s$$

→ QCD factorization

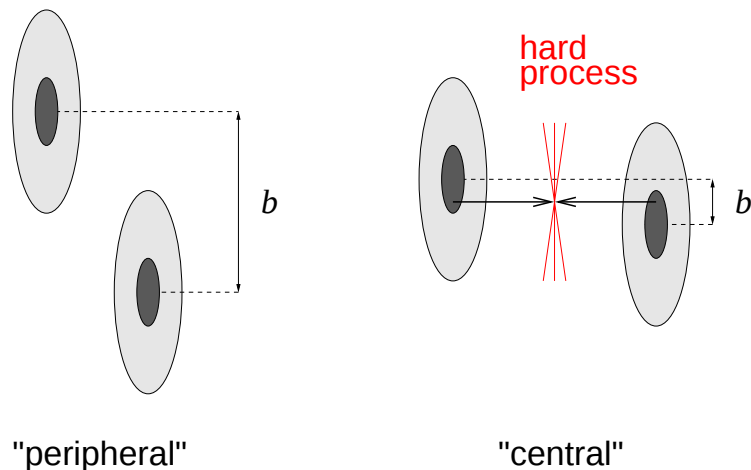
- Partonic initial state depends on soft spectator interactions ($\leftrightarrow$ hadronic final state)

$$pp \rightarrow \begin{matrix} e^+e^- \\ \text{dijet} \end{matrix} + \begin{matrix} X \\ X \end{matrix}$$

- Model parton distribution in terms of transverse spatial distributions known from ep scattering

$$\propto g(x_1, \rho_1) g(x_2, \rho_2)$$

- Hard processes as “filter” for central collisions [Frankfurt, Strikman, CW 03]

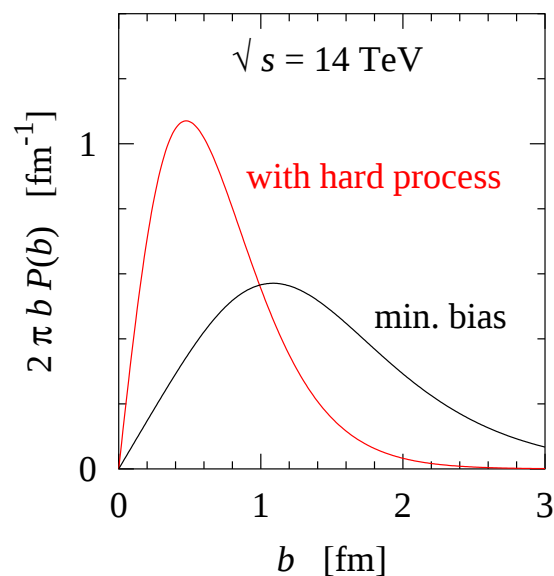


- Transverse radius of quarks/gluons with $x > 10^{-2}$ much smaller than radius of soft interactions

$$\langle \rho^2 \rangle_{q,g} \ll R_{\text{soft}}^2$$

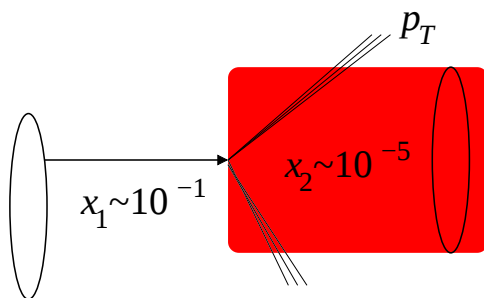
“Two-scale picture”

- Classification of pp collision: “Central” vs. “peripheral”

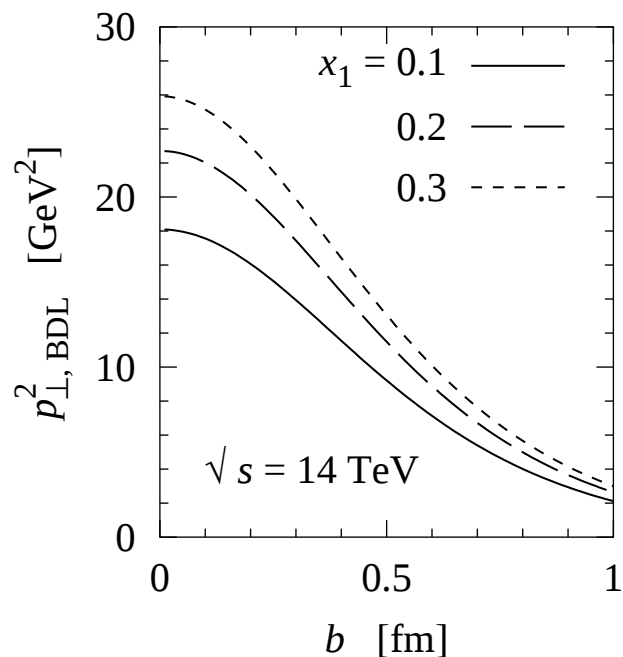


- Events with hard process are central collisions (trigger!)
- Impact parameter distribution calculable from transverse spatial distribution of gluons [← HERA]

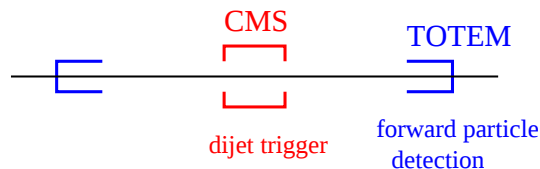
- Central collisions: Unitarity limit in spectator interactions [FSW 03/04]



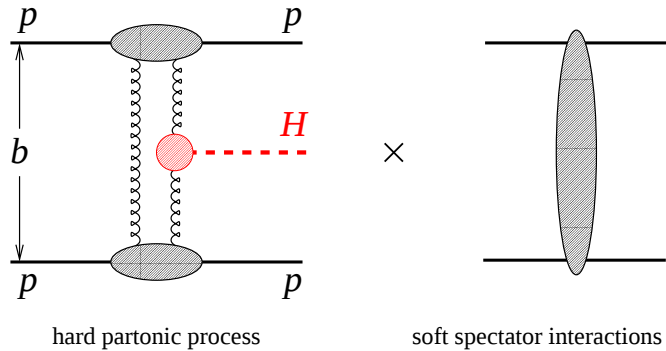
- Increase of gluon density at small x (DGLAP evolution)
- Interaction of large- x_1 spectator with small- x_2 gluons approaches “black-disk limit”: $P_{\text{inel}} \rightarrow 1$



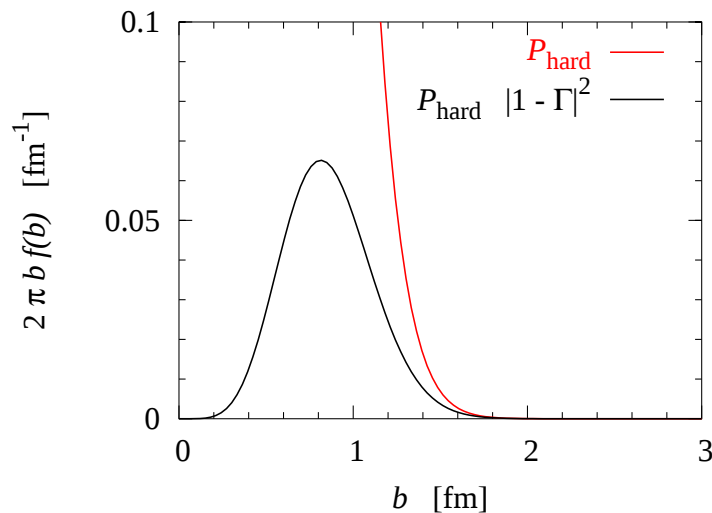
- Qualitative changes in forward particle production: Large $p_{\perp}$, energy loss, . . .
- Can be studied with LHC detectors



- Diffractive processes $pp \rightarrow p + H + p$: Rapidity gap survival



- Heavy particle produced in hard partonic process (2-gluon exchange)
- Soft spectator interactions must not destroy rapidity gaps!



- Gap survival probability

$$S^2 = \int d^2b P_{\text{hard}}(b) |1 - \Gamma(b)|^2$$

$$\approx 0.03 \quad (\text{Higgs at LHC})$$

... calculable, model-independent!

- Observable p_T dependence probes gluon GPD!

[Frankfurt, Hyde-Wright, Strikman, CW 06]

Summary

- J/ψ data (HERA + fixed-target) provide information on
“3D gluon density” in proton
 $\leftrightarrow$ non-perturbative dynamics
- Need to measure t -slopes and their Q^2 -dependence!
 - Size of interacting configurations — test of factorization
 - Transverse structure of nucleon
- Transverse spatial distribution of partons from ep
allows one to understand/control transverse geometry
of high-energy pp collisions with hard QCD processes
 - Next step: Probe GPDs in pp at LHC

“3D really works!”