



# Scalar meson exchange in $\phi \rightarrow P^0 P^0 \gamma$ decays

Rafel Escrivano

Grup de Física Teòrica and IFAE (UAB)

April 9, 2003  
Photon 2003 (Frascati, Italy)

## Motivation:

- excellent laboratory for investigating the light scalar meson resonances
- complements other analyses based on central production,  $D$  and  $J/\psi$  decays...

- Experimental data
- Theory review: scalar models market
- *Golden processes:*

$$\begin{aligned}\phi \rightarrow \pi^0 \pi^0 \gamma &\longleftrightarrow f_0(980) \\ \phi \rightarrow \pi^0 \eta \gamma &\longleftrightarrow a_0(980)\end{aligned}$$

- Other proc.:  $\phi \rightarrow K^0 \bar{K}^0 \gamma$
- Conclusions

# Experimental data

$$\phi \rightarrow \pi^0 \pi^0 \gamma$$

**SND** PL B485 (00) 349

$$B(\phi \rightarrow \pi^0 \pi^0 \gamma) = (1.221 \pm 0.098 \pm 0.061) \times 10^{-4}$$

**CMD-2** PL B462 (99) 380

$$B(\phi \rightarrow \pi^0 \pi^0 \gamma) = (1.08 \pm 0.17 \pm 0.09) \times 10^{-4}$$

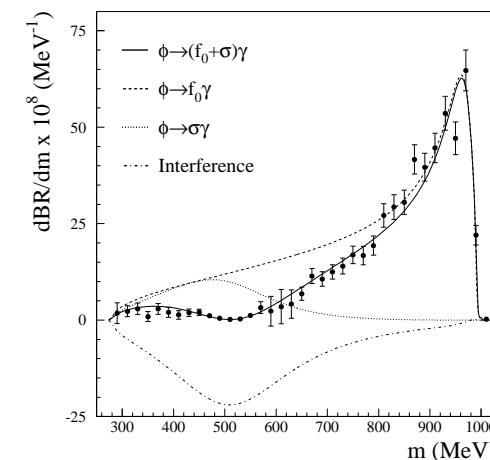
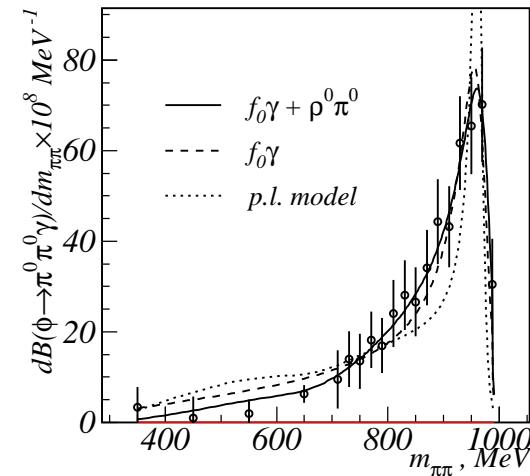
**KLOE** PL B537 (02) 21

$$B(\phi \rightarrow \pi^0 \pi^0 \gamma) = (1.09 \pm 0.03 \pm 0.05) \times 10^{-4}$$

significant enhancement at large  $\pi^0 \pi^0$  invariant mass



*manifestation of a sizable contribution of the  
 $f_0(980)\gamma$  intermediate state*



# Experimental data

$$\phi \rightarrow \pi^0 \eta \gamma$$

**SND** PL B479 (00) 53

$$B(\phi \rightarrow \pi^0 \eta \gamma) = (0.88 \pm 0.14 \pm 0.09) \times 10^{-4}$$

**CMD-2** PL B462 (99) 380

$$B(\phi \rightarrow \pi^0 \eta \gamma) = (0.90 \pm 0.24 \pm 0.10) \times 10^{-4}$$

**KLOE** PL B536 (02) 209

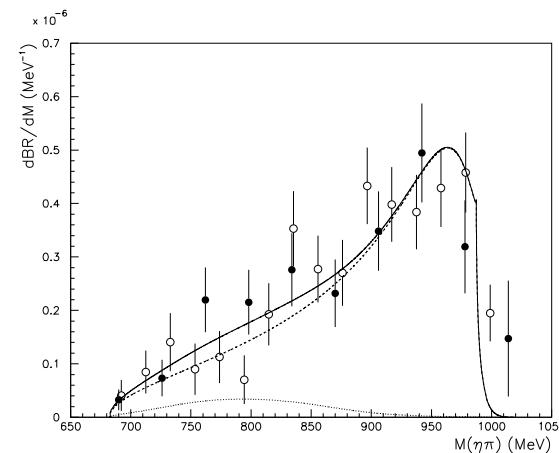
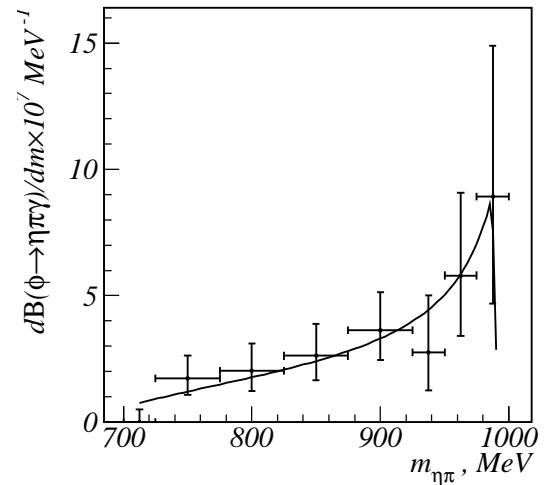
$$B(\phi \rightarrow \pi^0 \eta \gamma) = (0.851 \pm 0.051 \pm 0.057) \times 10^{-4} \quad (\eta \rightarrow \gamma \gamma)$$

$$B(\phi \rightarrow \pi^0 \eta \gamma) = (0.796 \pm 0.060 \pm 0.040) \times 10^{-4} \quad (\eta \rightarrow \pi^+ \pi^- \pi^0)$$

significant enhancement at large  $\pi^0 \eta$  invariant mass



*manifestation of a sizable contribution of the  
 $a_0(980)\gamma$  intermediate state*



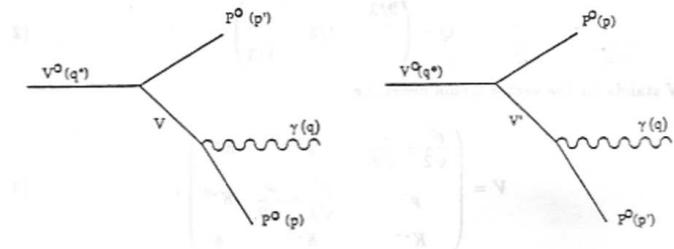
# Theory Review

## VMD

A. Bramon, A. Grau & G. Pancheri, PL B283 (92) 416

$$\begin{aligned}\mathcal{L}_{VVP} &= \frac{G}{\sqrt{2}} \epsilon^{\mu\nu\alpha\beta} \langle \partial_\mu V_\nu \partial_\alpha V_\beta P \rangle \\ \mathcal{L}_{V\gamma} &= -4f^2 e g A_\mu \langle Q V^\mu \rangle\end{aligned}$$

$$\begin{aligned}B_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\text{VMD}} &= 1.2 \times 10^{-5} \\ B_{\phi \rightarrow \pi^0 \eta \gamma}^{\text{VMD}} &= 5.4 \times 10^{-6} \\ B_{\rho \rightarrow \pi^0 \pi^0 \gamma}^{\text{VMD}} &= 1.3 \times 10^{-5}\end{aligned}$$



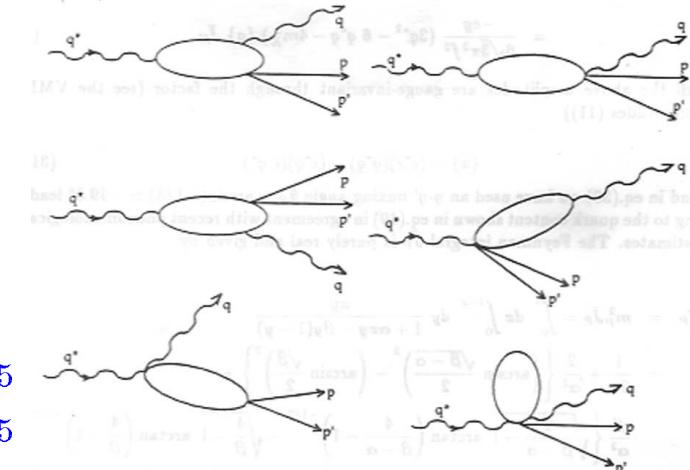
$$\begin{aligned}V &= V' = \rho \\ V &= \rho, V' = \omega \\ V &= V' = \omega\end{aligned}$$

## ChPT + $\rho \rightarrow \pi^+ \pi^- + \phi \rightarrow K^+ K^-$

A. Bramon, A. Grau & G. Pancheri, PL B289 (92) 97

$$\mathcal{L}_2 = \frac{f^2}{4} \langle D_\mu U^\dagger D^\mu U + M(U + U^\dagger) \rangle$$

$$\left. \begin{aligned} B^\chi &= 5.0 \times 10^{-5} \\ B^\chi &= 3.0 \times 10^{-5} \\ B^\chi &= 1.0 \times 10^{-5} \end{aligned} \right\} \Rightarrow \left\{ \begin{aligned} B^{\text{VMD}+\chi} &= 6.1 \times 10^{-5} \\ B^{\text{VMD}+\chi} &= 3.6 \times 10^{-5} \\ B^{\text{VMD}+\chi} &= 2.9 \times 10^{-5} \end{aligned} \right.$$



BUT both approaches do not contain the effect of scalar resonances

# Scalar models market

All the following models contain the scalar resonances **explicitly**

## No structure

excluded by experimental data on  $\phi \rightarrow \pi^0 \pi^0 \gamma$

## Kaon loop

N. N. Achasov & V. V. Gubin, PR D63 (01) 094007

used in the experimental analyses of  $\phi \rightarrow \pi^0 \pi^0 \gamma$  and  $\phi \rightarrow \pi^0 \eta \gamma$  decays

scalar resonances *ad hoc*

## $U\chi$ PT

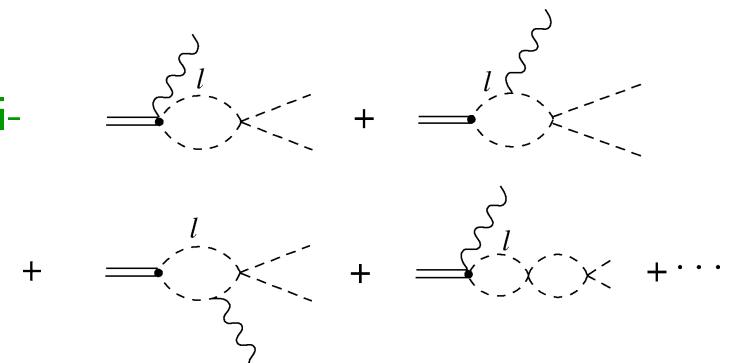
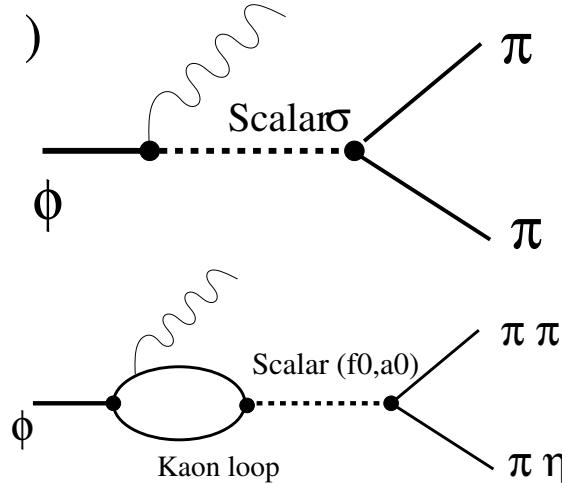
E. Oset *et al.*, PL B470 (99) 20, NP A707 (02) 161

scalar resonances are generated dynamically by unitarizing the one-loop amplitudes

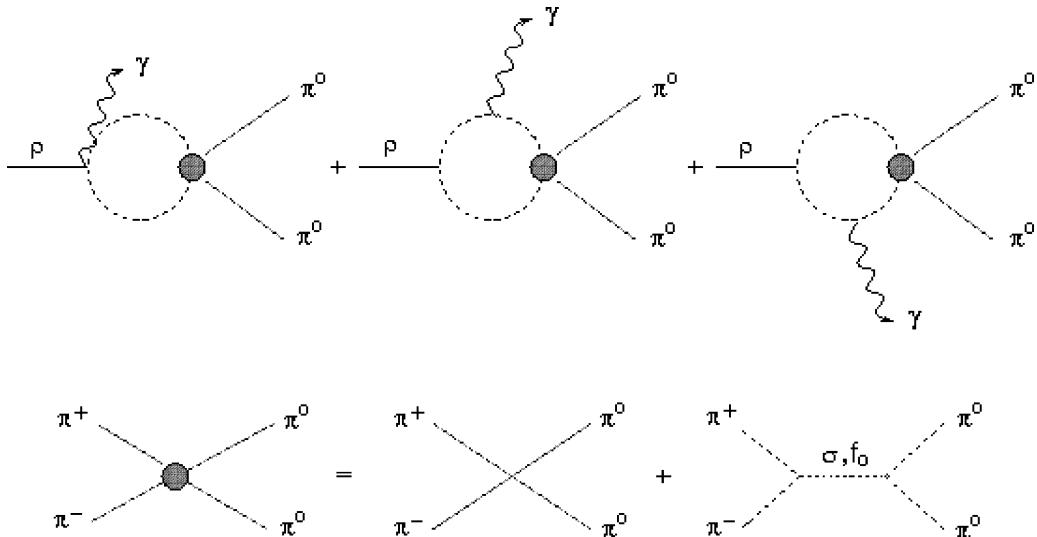
$$B_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\text{U}\chi\text{PT}} = 8 \times 10^{-5}$$

$$B_{\phi \rightarrow \pi^0 \eta \gamma}^{\text{U}\chi\text{PT}} = 8.7 \times 10^{-5}$$

$$B_{\rho \rightarrow \pi^0 \pi^0 \gamma}^{\text{U}\chi\text{PT}} = 1.5 \times 10^{-5}$$



The L $\sigma$ M is a well defined  $U(3) \times U(3)$  chiral model which incorporates *ab initio* both the pseudoscalar nonet together with its chiral partner the scalar nonet



$$\begin{aligned}
 \phi \rightarrow \pi^0 \pi^0 \gamma &\quad P^\pm = K^\pm \quad S = \sigma, f_0 \quad \sigma \ll f_0 \\
 \phi \rightarrow \pi^0 \eta \gamma &\quad P^\pm = K^\pm \quad S = a_0 \\
 \rho \rightarrow \pi^0 \pi^0 \gamma &\quad P^\pm = \pi^\pm \quad S = \sigma, f_0 \quad \sigma \gg f_0 \\
 \phi \rightarrow K^0 \bar{K}^0 \gamma &\quad P^\pm = K^\pm \quad S = \sigma, f_0, a_0 \quad f_0 \simeq a_0 \gg \sigma
 \end{aligned}$$

For the rest of the processes, the scalar contribution is not relevant

The complementarity between ChPT and the L $\sigma$ M will be used for including the scalar meson poles while keeping the correct behaviour at low dimeson invariant mass expected from ChPT



# Golden Processes



$$\phi \rightarrow \pi^0 \pi^0 \gamma$$

A. Bramon, R. E., J. L. Lucio M., M. Napsuciale & G. Pancheri,  
EPJ C26 (02) 253

$$\mathcal{A}(\phi \rightarrow \pi^0 \pi^0 \gamma)_{\text{L}\sigma\text{M}} \propto \text{kaon loop} \times \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{L}\sigma\text{M}}$$

with

$$\begin{aligned} \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{L}\sigma\text{M}} &= g_{K^+ K^- \pi^0 \pi^0} \\ &- \frac{g_{\sigma K^+ K^-} - g_{\sigma \pi^0 \pi^0}}{s - m_\sigma^2} - \frac{g_{f_0 K^+ K^-} - g_{f_0 \pi^0 \pi^0}}{s - m_{f_0}^2} - \frac{g_{\kappa \mp K^\pm \pi^0}^2}{t - m_\kappa^2} - \frac{g_{\kappa \mp K^\pm \pi^0}^2}{u - m_\kappa^2} \end{aligned}$$

and

$$\begin{aligned} g_{\sigma K \bar{K}} &= \frac{m_K^2 - m_\sigma^2}{2 f_K} (c\phi_S - \sqrt{2}s\phi_S) & g_{\sigma \pi \pi} &= \frac{m_\pi^2 - m_\sigma^2}{f_\pi} c\phi_S \\ g_{f_0 K \bar{K}} &= \frac{m_K^2 - m_{f_0}^2}{2 f_K} (s\phi_S + \sqrt{2}c\phi_S) & g_{f_0 \pi \pi} &= \frac{m_\pi^2 - m_{f_0}^2}{f_\pi} s\phi_S \end{aligned}$$

Using the soft-pion limit:

$$\begin{aligned} \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{L}\sigma\text{M}} &= \frac{s - m_\pi^2}{2 f_\pi f_K} \\ &\times \left[ \frac{m_K^2 - m_\sigma^2}{D_\sigma(s)} c\phi_S (c\phi_S - \sqrt{2}s\phi_S) + \frac{m_K^2 - m_{f_0}^2}{D_{f_0}(s)} s\phi_S (s\phi_S + \sqrt{2}c\phi_S) \right] \\ &+ \frac{t - m_K^2}{4 f_\pi f_K} \frac{m_\pi^2 - m_\kappa^2}{D_\kappa(t)} + \frac{u - m_K^2}{4 f_\pi f_K} \frac{m_\pi^2 - m_\kappa^2}{D_\kappa(u)} \end{aligned}$$

where

- $D_\sigma(s) = s - m_\sigma^2 + i m_\sigma \Gamma_\sigma$
- $D_{f_0}(s) = s - m_{f_0}^2 - \text{Re}\Pi(m_{f_0}^2) + \Pi(s)$   
the complete one-loop propagator to take into account finite width corrections
- $\phi_S$  is the scalar mixing angle in the quark-flavour basis



# Golden Processes



$$\phi \rightarrow \pi^0 \pi^0 \gamma$$

Remarks:

1.

$$\begin{aligned} \lim_{m_S \rightarrow \infty} \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{L}\sigma\text{M}} &= \frac{s - m_\pi^2}{2f_\pi f_K} + \frac{t+u-2m_K^2}{4f_\pi f_K} \\ &= \frac{s}{4f_\pi f_K} = \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{ChPT}} \quad \checkmark \end{aligned}$$

2. non-resonant contributions are integrated out:

$$\begin{aligned} \lim_{m_R \rightarrow \infty} \mathcal{A}_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\text{non-resonant}} &= \mathcal{A}_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\chi\text{-loops}} - \lim_{m_{\sigma, f_0} \rightarrow \infty} \mathcal{A}_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\text{L}\sigma\text{M}} \\ \implies & \end{aligned}$$

$$\mathcal{A}(\phi \rightarrow \pi^0 \pi^0 \gamma)_{\text{L}\sigma\text{M}} = \frac{eg_s}{2\pi^2 m_K^2} \{a\} L(s) \times \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{L}\sigma\text{M}}$$

with

$$\begin{aligned} \mathcal{A}(K^+ K^- \rightarrow \pi^0 \pi^0)_{\text{L}\sigma\text{M}} &= \frac{m_\pi^2 - s/2}{2f_\pi f_K} + \frac{s - m_\pi^2}{2f_\pi f_K} \\ &\times \left[ \frac{m_K^2 - m_\sigma^2}{D_\sigma(s)} c\phi_S(c\phi_S - \sqrt{2}s\phi_S) + \frac{m_K^2 - m_{f_0}^2}{D_{f_0}(s)} s\phi_S(s\phi_S + \sqrt{2}c\phi_S) \right] \end{aligned}$$

where now only the  $\sigma$  and  $f_0$  poles appear

$\implies$

this amplitude should be able to reproduce the  $\pi^0 \pi^0$  invariant mass spectrum for all  $s \equiv m_{\pi^0 \pi^0}^2$   $\checkmark$

3. if  $m_\sigma \simeq m_K$  and  $\Gamma_\sigma$  is large  $\implies \sigma \ll f_0$   $\checkmark$
4.  $\mathcal{A}_{K^+ K^- \rightarrow \pi^0 \pi^0}^{\text{L}\sigma\text{M}}$  and consequently  $\mathcal{A}_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\text{L}\sigma\text{M}}$  are very dependent on  $\phi_S$  and  $m_{f_0}$   $\checkmark$



# Golden Processes



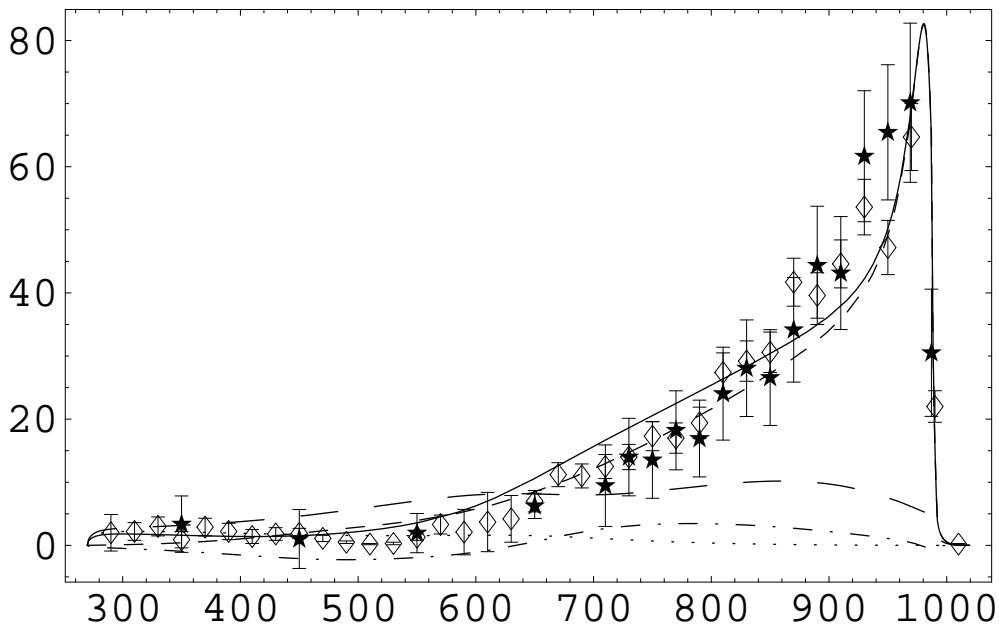
$$\phi \rightarrow \pi^0 \pi^0 \gamma$$

Results:

For

$$\left. \begin{array}{l} m_\sigma = 478 \text{ MeV} \\ \Gamma_\sigma = 324 \text{ MeV} \\ \text{E791 Coll., PRL 86 (01) 770} \\ m_{f_0} = 985 \text{ MeV} \\ \phi_S = -9^\circ \end{array} \right\} \implies B_{\phi \rightarrow \pi^0 \pi^0 \gamma}^{\text{L}\sigma\text{M+VMD}} = 1.16 \times 10^{-4}$$

in nice agreement with experimental results



**Figure 1:**  $dB(\phi \rightarrow \pi^0 \pi^0 \gamma)/dm_{\pi^0 \pi^0} \times 10^8$  (in  $\text{MeV}^{-1}$ ) versus  $m_{\pi^0 \pi^0}$  (in MeV). The dashed, dotted and dot-dashed lines correspond to the contributions from the L $\sigma$ M, VMD and their interference, respectively. The solid line is the total result. The long-dashed line is the chiral loop prediction. Experimental data are taken from SND (solid star) and KLOE (open diamond).



# Golden Processes



$$\phi \rightarrow \pi^0 \eta \gamma$$

A. Bramon, R. E., J. L. Lucio M., M. Napsuciale & G. Pancheri,  
PL B494 (00) 221

$$\mathcal{A}(\phi \rightarrow \pi^0 \eta \gamma)_{\text{L}\sigma\text{M}} = \frac{e g_s}{2 \pi^2 m_{K+}^2} \{a\} L(s) \times \mathcal{A}(K^+ K^- \rightarrow \pi^0 \eta)_{\text{L}\sigma\text{M}}$$

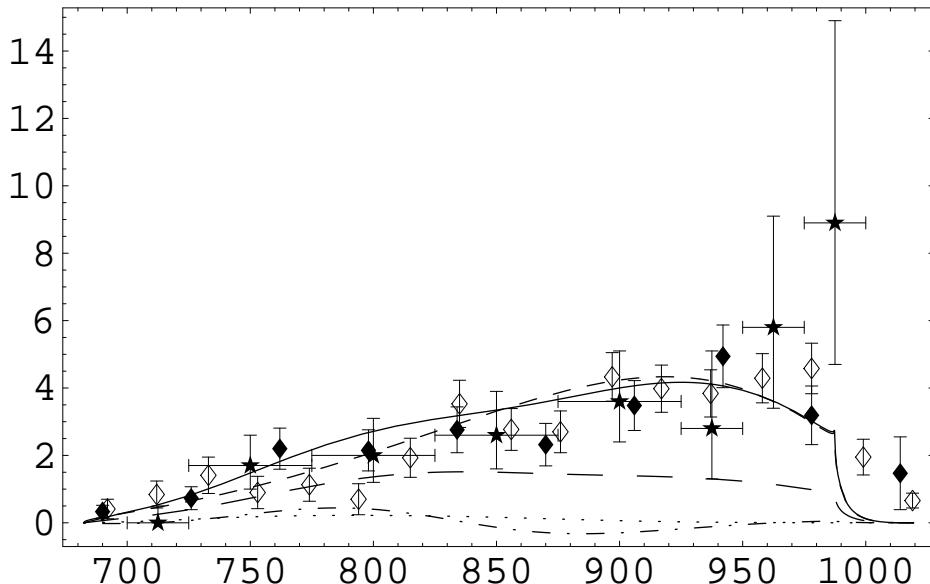
$$\mathcal{A}(K^+ K^- \rightarrow \pi^0 \eta)_{\text{L}\sigma\text{M}} = \frac{s - m_\eta^2}{2 f_\pi f_K} \frac{m_K^2 - m_{a_0}^2}{D_{a_0}(s)} c\phi_P + \frac{m_\eta^2 + m_\pi^2 - s}{4 f_\pi f_K} (c\phi_P - \sqrt{2} s\phi_P)$$

where

- $D_{a_0}(s) = s - m_{a_0}^2 - \text{Re}\Pi(m_{a_0}^2) + \Pi(s)$
- $\phi_P$  is the pseudoscalar mixing angle in the quark basis

Results:

$$\left. \begin{array}{l} m_{a_0} = 984.7 \text{ MeV PDG'02} \\ \phi_P = 41.8^\circ \text{ PL B541 (02) 45} \end{array} \right\} \Rightarrow B_{\phi \rightarrow \pi^0 \eta \gamma}^{\text{L}\sigma\text{M+VMD}} = 8.3 \times 10^{-5}$$



**Figure 2:**  $dB(\phi \rightarrow \pi^0 \eta \gamma) / dm_{\pi^0 \eta} \times 10^7$  (in  $\text{MeV}^{-1}$ ) versus  $m_{\pi^0 \eta}$  (in MeV). Experimental data are taken from SND (solid star) and KLOE: (open diamond) from  $\eta \rightarrow \gamma \gamma$  and (solid diamond) from  $\eta \rightarrow \pi^+ \pi^- \pi^0$ .



## Other Processes



$$\phi \rightarrow K^0 \bar{K}^0 \gamma$$

$$\mathcal{A}(\phi \rightarrow K^0 \bar{K}^0 \gamma)_{\text{L}\sigma\text{M}} = \frac{e g_s}{\sqrt{2} \pi^2 m_{K+}^2} \{a\} L(s) \times \mathcal{A}(K^+ K^- \rightarrow K^0 \bar{K}^0)_{\text{L}\sigma\text{M}}$$

$$\begin{aligned} \mathcal{A}(K^+ K^- \rightarrow K^0 \bar{K}^0)_{\text{L}\sigma\text{M}} &= \frac{m_K^2 - s/2}{2f_K^2} + \frac{s - m_K^2}{4f_K^2} \times \\ &\left[ \frac{m_K^2 - m_\sigma^2}{D_\sigma(s)} (c\phi_S - \sqrt{2}s\phi_S)^2 + \frac{m_K^2 - m_{f_0}^2}{D_{f_0}(s)} (s\phi_S + \sqrt{2}c\phi_S)^2 - \frac{m_K^2 - m_{a_0}^2}{D_{a_0}(s)} \right] \end{aligned}$$

Results:

$$\left. \begin{array}{l} m_{f_0} = 985 \text{ MeV}, \phi_S = -9^\circ \\ m_{a_0} = 984.7 \text{ MeV}_{\text{PDG'02}} \end{array} \right\} \Rightarrow B_{\phi \rightarrow K^0 \bar{K}^0 \gamma}^{\text{L}\sigma\text{M}} = 4 \times 10^{-8}$$

no background problem for testing CP violation at DaΦne

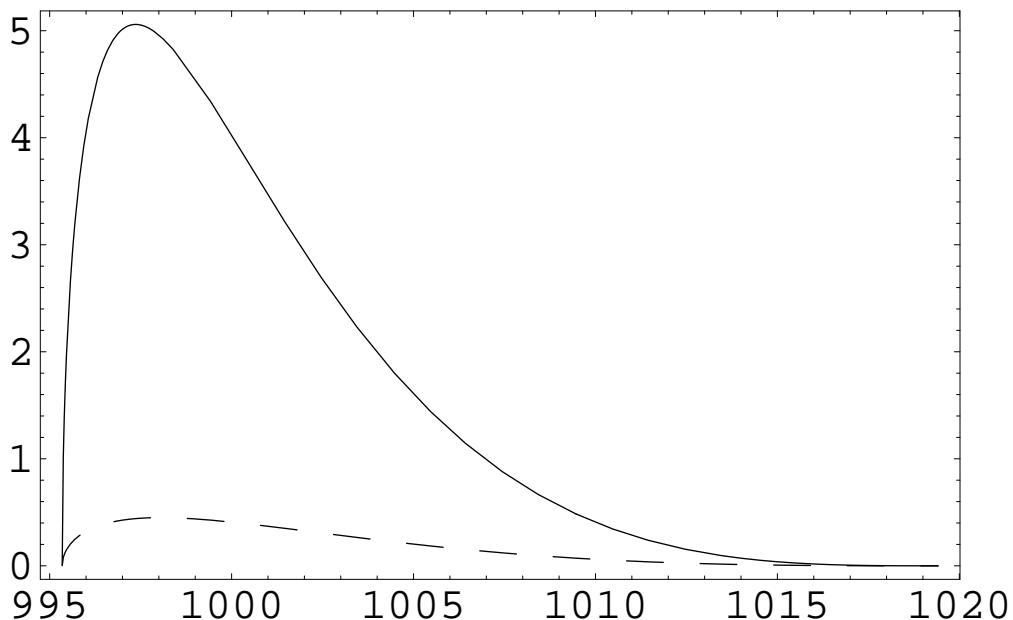


Figure 3:  $dB(\phi \rightarrow K^0 \bar{K}^0 \gamma) / dm_{K^0 \bar{K}^0} \times 10^9$  (in  $\text{MeV}^{-1}$ ) versus  $m_{K^0 \bar{K}^0}$  (in MeV). Total result (solid line); the chiral loop prediction (long-dashed line).



# Preliminary



$$\phi \rightarrow f_0\gamma/a_0\gamma$$

$$\mathcal{A}(\phi \rightarrow f_0\gamma)_{L\sigma M} = \frac{eg_s}{2\pi^2 m_{K^+}^2} \{a\} L(m_{f_0}^2) \times g_{f_0 K^+ K^-}$$

$$\mathcal{A}(\phi \rightarrow a_0\gamma)_{L\sigma M} = \frac{eg_s}{2\pi^2 m_{K^+}^2} \{a\} L(m_{a_0}^2) \times g_{a_0 K^+ K^-}$$

where

$$g_{f_0 K^+ K^-} = \frac{m_K^2 - m_{f_0}^2}{2f_K} (s\phi_S + \sqrt{2}c\phi_S) \quad g_{a_0 K^+ K^-} = \frac{m_K^2 - m_{a_0}^2}{2f_K}$$

$\implies$

$$\begin{aligned} R(\phi \rightarrow f_0\gamma/a_0\gamma)_{L\sigma M} &= \frac{|L(m_{f_0}^2)|^2}{|L(m_{a_0}^2)|^2} \frac{(1 - m_{f_0}^2/m_\phi^2)^3}{(1 - m_{a_0}^2/m_\phi^2)^3} \times \frac{g_{f_0 K^+ K^-}^2}{g_{a_0 K^+ K^-}^2} \\ &\simeq \frac{g_{f_0 K^+ K^-}^2}{g_{a_0 K^+ K^-}^2} \simeq (s\phi_S + \sqrt{2}c\phi_S)^2 \end{aligned}$$

Results:

For

$$\phi_S = -9^\circ \implies R(\phi \rightarrow f_0\gamma/a_0\gamma)_{L\sigma M} \simeq 1.5$$

to be compared with the KLOE measurement

[PL B537 (02) 21, PL B536 (02) 209]

$$R(\phi \rightarrow f_0\gamma/a_0\gamma)_{KLOE} = 6.1 \pm 0.6$$

However, this value is obtained from a large destructive interference between the  $f_0\gamma$  and  $\sigma\gamma$  contributions, in disagreement with other experiments



# Conclusions

- $\phi \rightarrow \pi^0 \pi^0 \gamma$ ,  $\phi \rightarrow \pi^0 \eta \gamma$  and  $\phi \rightarrow K^0 \bar{K}^0 \gamma$  can be used to extract relevant information on the properties of the  $f_0(980)$  and  $a_0(980)$  scalar resonances
- The complementarity between ChPT and the L $\sigma$ M can be used to parametrize the needed amplitudes
- The L $\sigma$ M predictions for these processes are compatible with experimental data
- $\boxed{\phi \rightarrow \pi^0 \pi^0 \gamma}$   
Dependent on  $m_{f_0}$  and  $\phi_S$   
Explanation for the suppression of the  $\sigma$  contribution
- $\boxed{\phi \rightarrow \pi^0 \eta \gamma}$   
Dependent on  $m_{a_0}$  and  $\phi_P$
- $\boxed{\phi \rightarrow K^0 \bar{K}^0 \gamma}$   
Confirmation that is not a problem for testing CP violation at DaΦne
- $\boxed{\phi \rightarrow f_0 \gamma / a_0 \gamma}$   
can be used to extract relevant information on the scalar mixing angle and on the nature of the  $f_0(980)$  and  $a_0(980)$
- Higher accuracy data and more refined theoretical analyses would contribute decisively to clarify the sector of the lowest lying scalar states