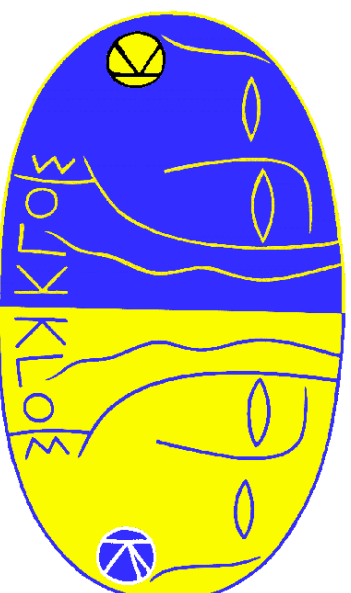


Measurement of the e^+e^- hadronic cross section at DAΦNE via radiative return

Stefan E. Müller

**Institut für Exp. Kernphysik,
Universität Karlsruhe**

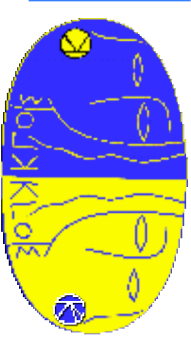
(for the KLOE collaboration)



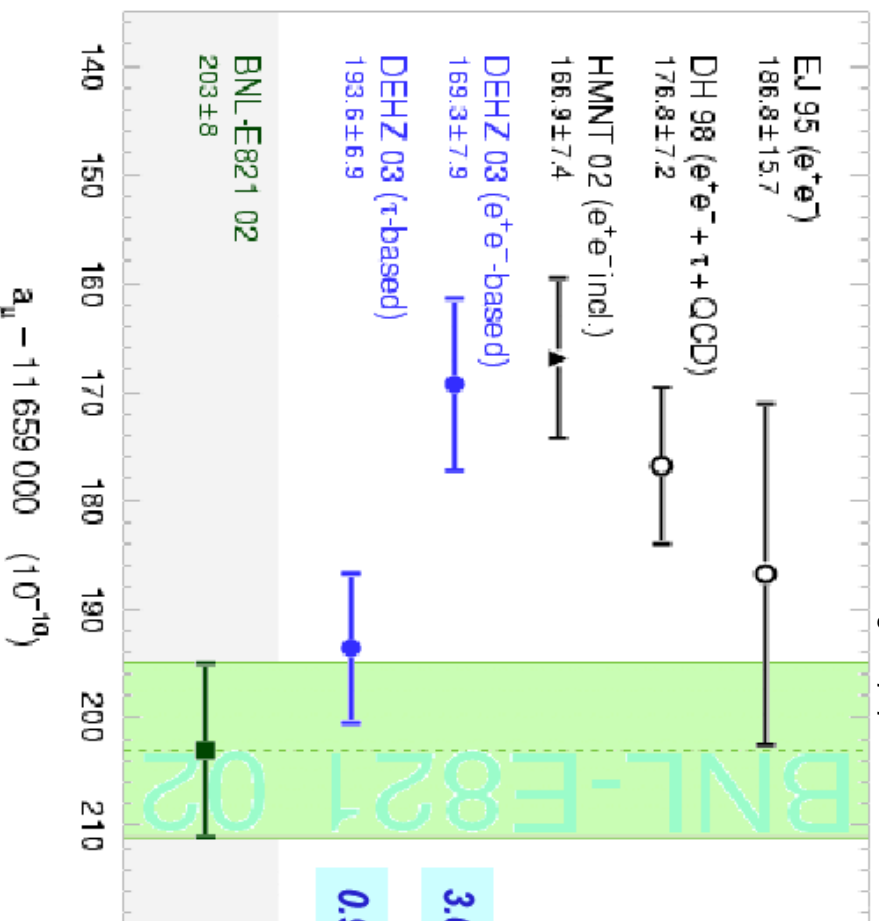
*Photon 2003 - International conference on the structure
and interactions of the photon*

Frascati, 7.-11. April 2003

Status on $(g-2)_\mu$:



Davier, Eidelman, Höcker, Zhang: hep-ph/0208177v3



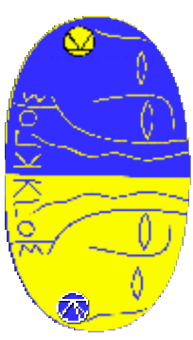
Disagreement between
e⁺e⁻ based and τ based
evaluations

3.0 σ

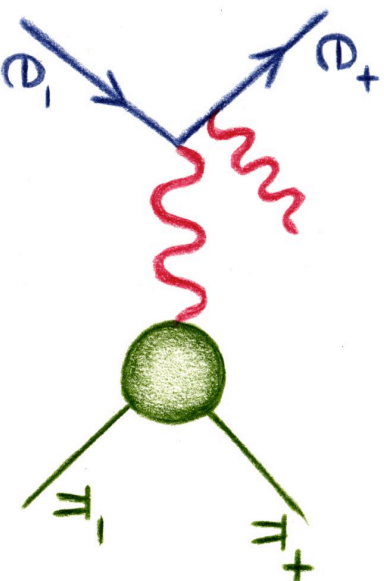
0.9 σ

- The nature of the difference in the two theoretical evaluations of a_μ^{had} has to be understood in order to claim a discrepancy between (SM-)theory and experiment
- More and better information on the **hadronic contribution** to the SM calculation of a_μ could help to clarify this difference and (together with a further reduction of the experimental error) give the discrepancy between theory and experiment a higher significance

$\sigma(e^+e^- \rightarrow \text{hadrons})$ with ISR:



Particle factories have the opportunity to measure the cross section $\sigma(e^+e^- \rightarrow \text{hadrons})$ as a function of the hadronic c.m.s energy M_{hadrons}^2 by using the radiative return.



$$\frac{d\sigma(e^+e^- \rightarrow \text{hadrons} + \gamma)}{dM_{\text{hadrons}}^2}$$

This method (S. Binner, J.H. Kühn, K. Melnikov, Phys. Lett. B 459, 1999) is a complementary approach to the standard energy scan.

advantage

Data comes as by-product of standard program

Systematic errors from **Luminosity**, **s**, ...
enter **only once** for each point of M_{hadrons}^2

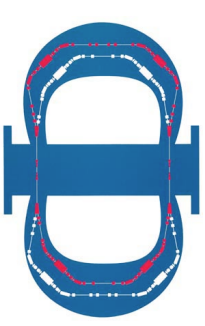
disadvantage

Requires precise calculations of Initial State Rad.

→ **EVA + Phokhara MC Generator**

Requires good suppression (or understanding) of Final State Rad.

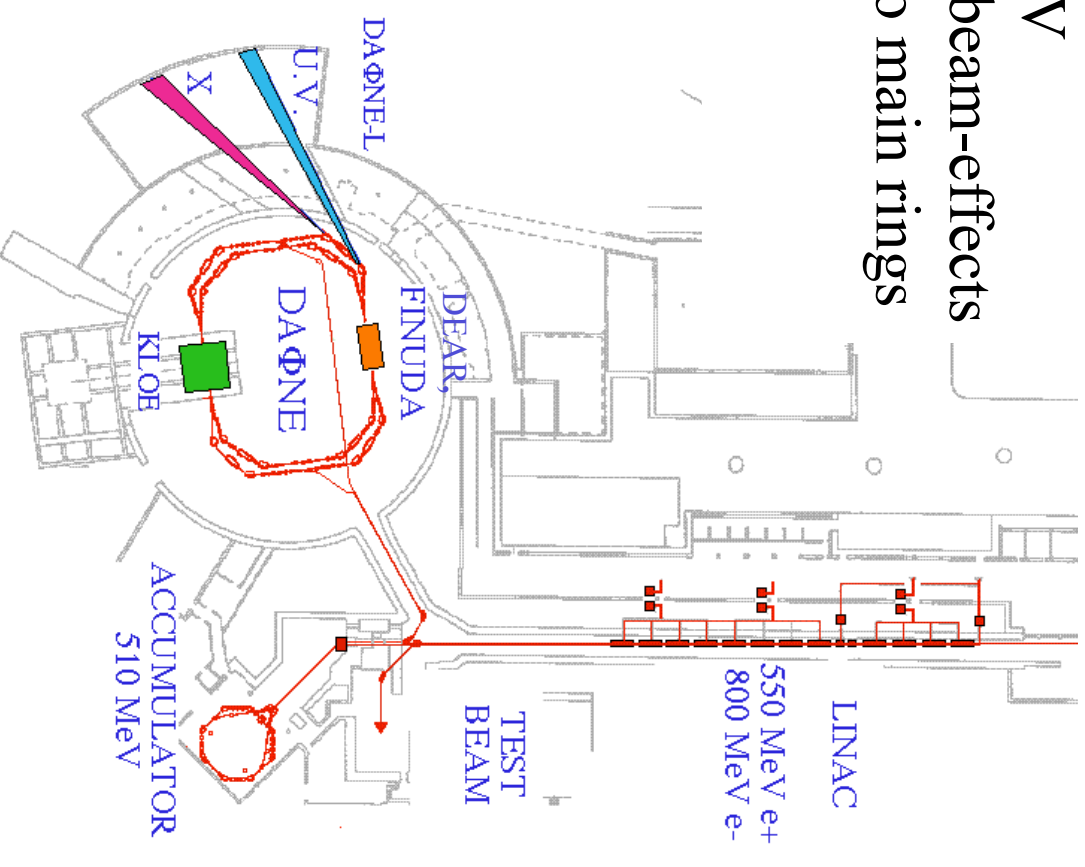
DAΦNE: A Υ -Factory



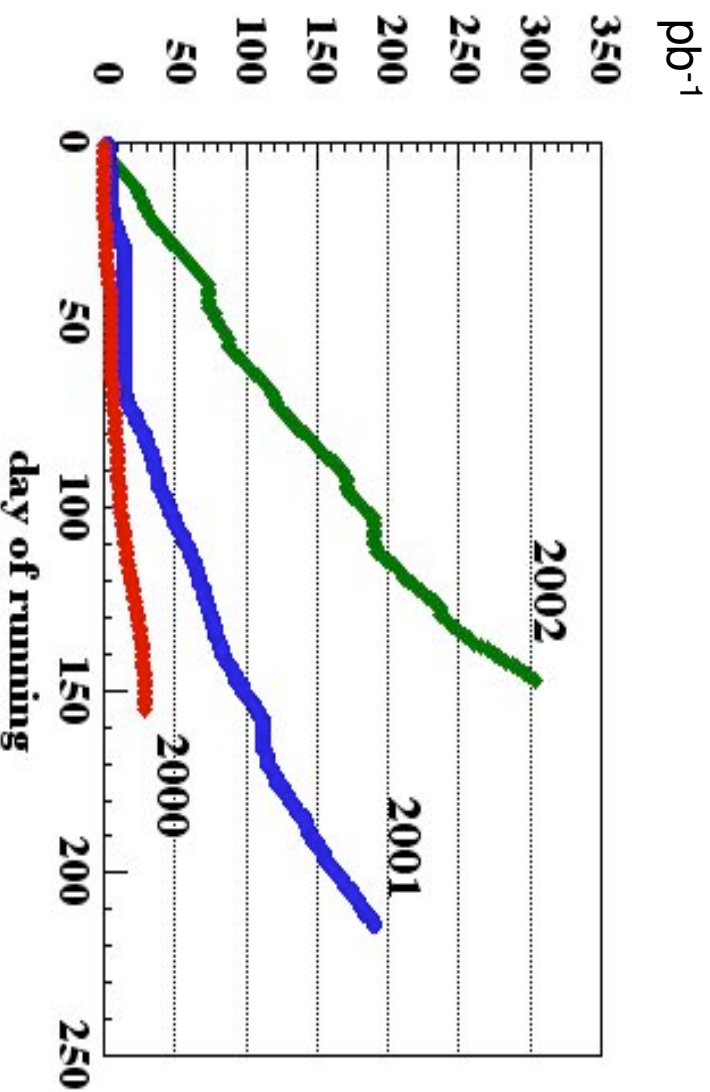
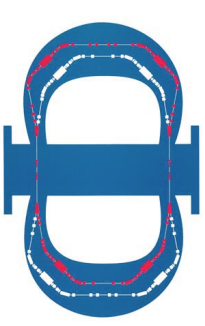
(Double Annular Υ -Factory for Nice Experiments)

- e^+e^- - collider with $\sqrt{s} = m_{\Upsilon} \approx 1.020$ GeV
- two separate rings to minimize beam-beam-effects
- accumulator for efficient injection into main rings
- two interaction points:
KLOE and DEAR/FINUDA

<i>BR's for selected Υ decays</i>	
K^+K^-	49.1%
$K_S K_L$	34.1%
$\pi^+\pi^+\pi^-\pi^0$	15.5%



DAΦNE: Performance



2000 run : 25 pb^{-1} 7.5 x 10^7 □

2001 run: 190 pb^{-1} 5.7 x 10^8 □

2002 run: 300 pb^{-1} 9.0 x 10^8 □

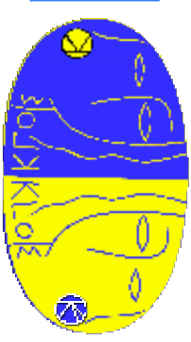
DAΦNE Backgr. reduced

Peak Luminosity@KLOE IP: 7.8·10³¹cm⁻²s⁻¹

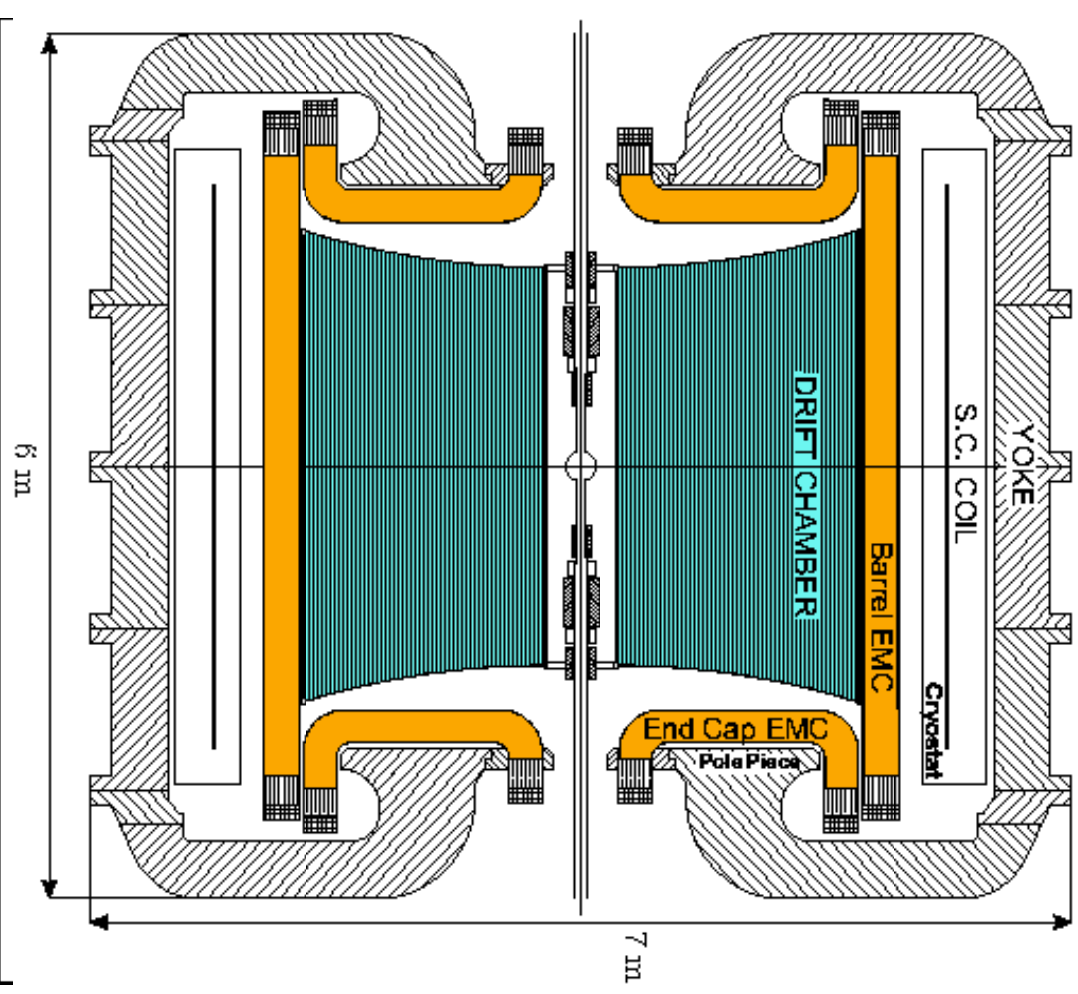
max int. Luminosity in one day: 4.5 pb^{-1}

KLOE:

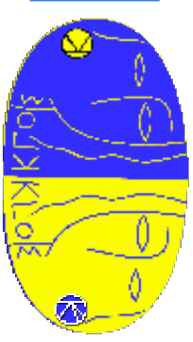
(KLOng Experiment)



- **Magnet:**
Superconducting coil ($B=0.5\text{ T}$)
- **EM Calorimeter:**
Lead/Scintillating fibres
4880 PM
- **Driftchamber:**
12582 Sense Wires
52140 wires in total
- **Beryllium Beampipe:**
 $R=10\text{ cm}$, 0.5 mm thick



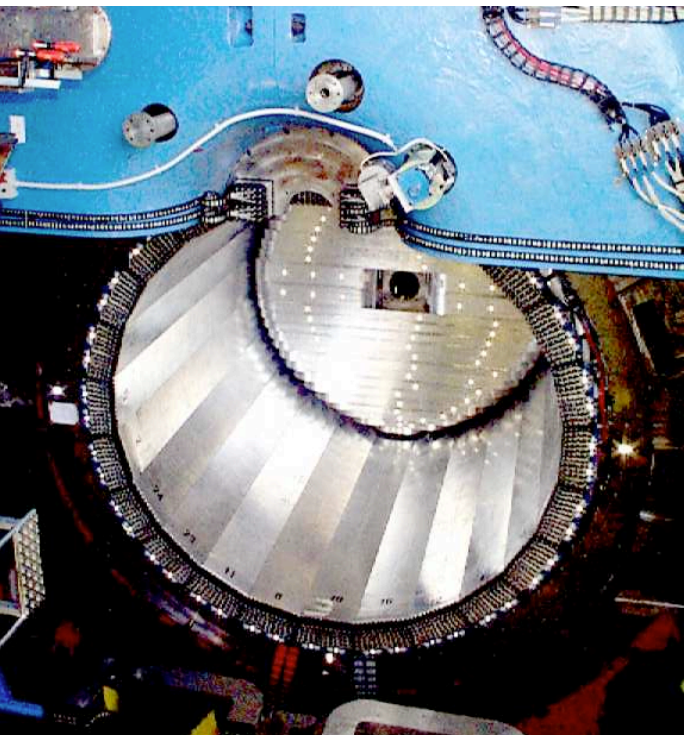
KLOE:



$$\sigma_E/E = 5.7\% / \sqrt{E(\text{GeV})}$$

$$\sigma_T = 54 \text{ ps} / \sqrt{E(\text{GeV})} \oplus 50 \text{ ps}$$

(Bunch length contribution subtracted from constant term)



Electromagnetic calorimeter

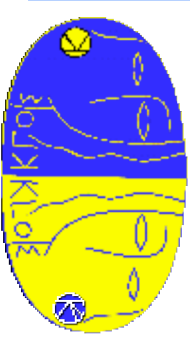
Drift chamber



$$\sigma_p/p = 0.4\% \text{ (for } 90^\circ \text{ tracks)}$$

$$\sigma_{xy} \approx 150 \mu\text{m}, \sigma_z \approx 2 \text{ mm}$$

Signal selection:



Pion tracks are measured at angles

$$40^\circ < \theta < 140^\circ$$

Photons are required to be within

$$\theta < 15^\circ \text{ and } \theta > 165^\circ$$

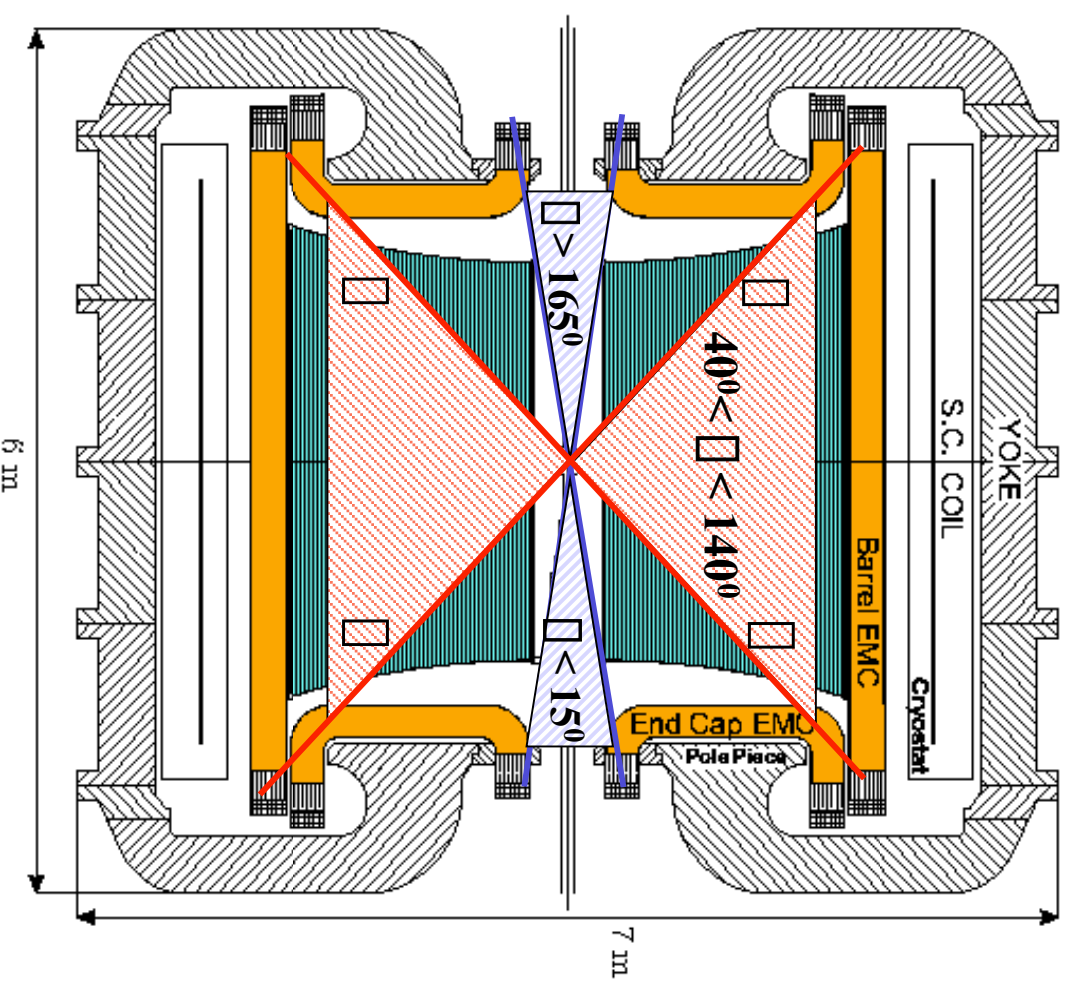
Photons cannot be detected efficiently with EmC,

untagged measurement in which we cut on the direction of the missing momentum

The choice of this kinematical region was motivated by:

- small relative contribution of **FSR**
- reduced background contamination:

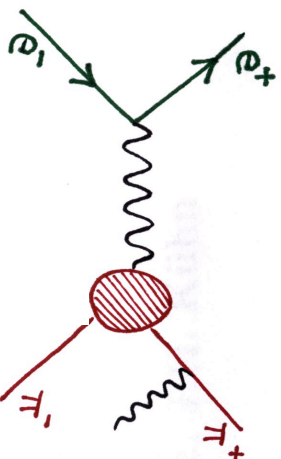
- $e^+e^- \rightarrow e^+e^- \gamma \gamma$
- $e^+e^- \rightarrow e^+e^- \mu^+\mu^- \gamma \gamma$
- $e^+e^- \rightarrow e^+e^- \mu^+\mu^- \gamma \gamma \gamma$



FSR suppression:

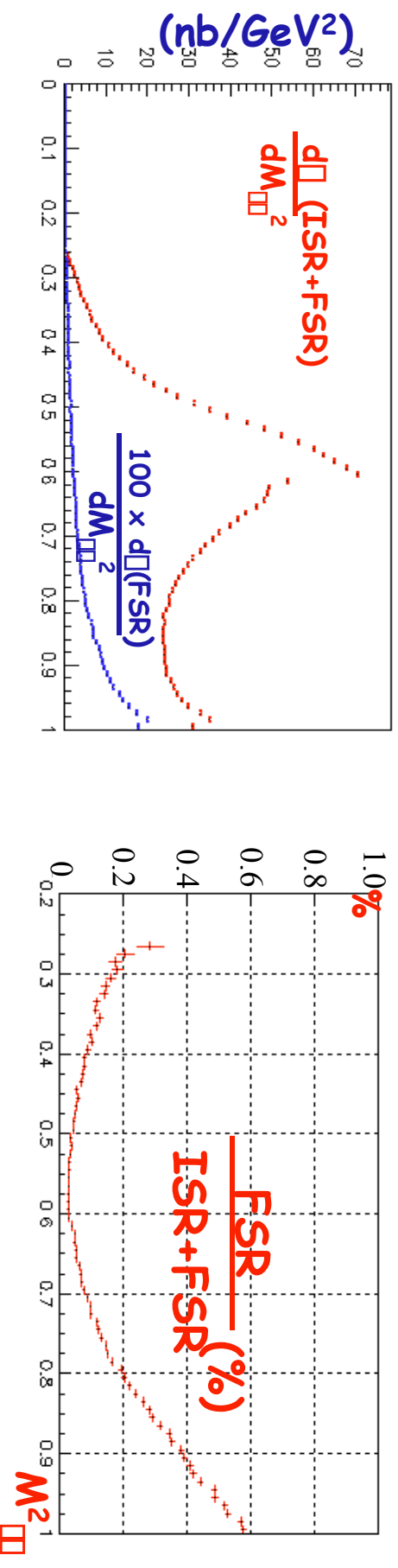


Our approach is to treat **Final State Radiation** of the pions as a „background“ and suppress it in the measurement using kinematical cuts.

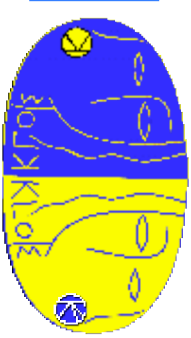


Initial **S**tate **R**adiation and **F**inal **S**tate **R**adiation contribution have been evaluated with MC (Binner, Kühn, Melnikov, Phys. Lett. B 459, 1999):

Contribution of **FSR <1%** for our selection cuts (i.e. model dependence negligible)



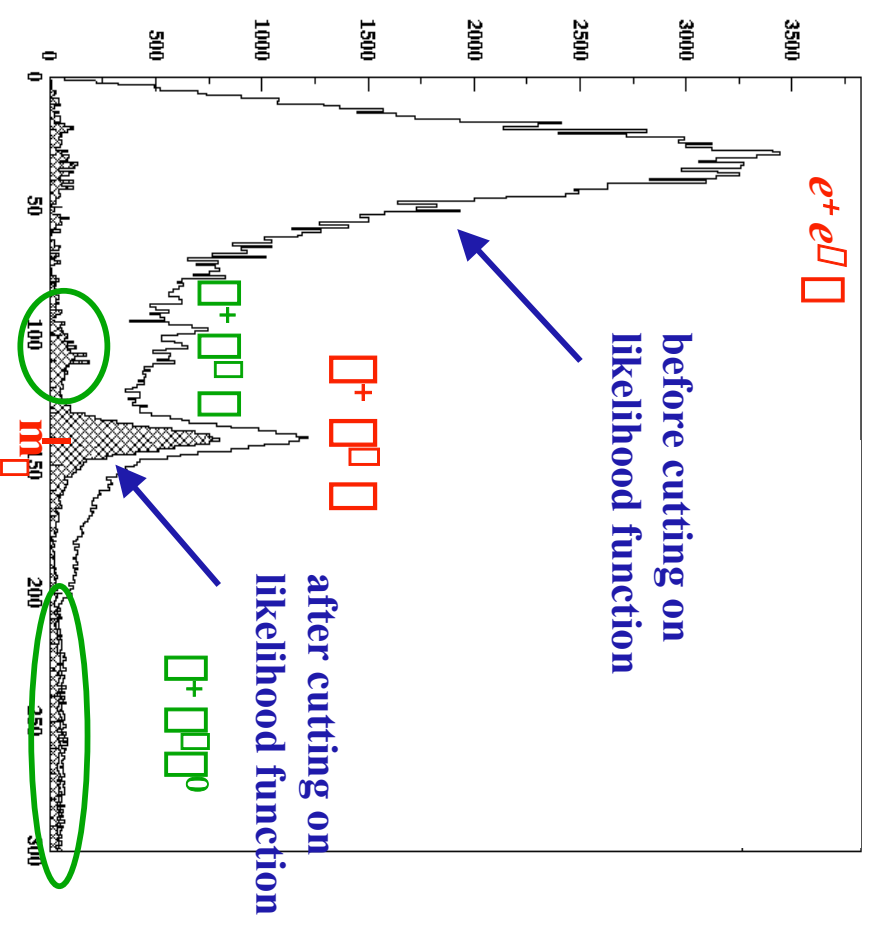
Background subtraction:



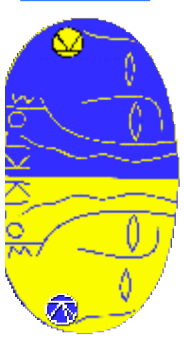
To reduce Bhabha contamination, a e^+e^- separation is performed using a Likelihood function based on:

- TOF of charged clusters
- Shape and energy deposition of the “charged” cluster

The event is selected if one of the charged tracks is identified to be a pion.



Background subtraction:



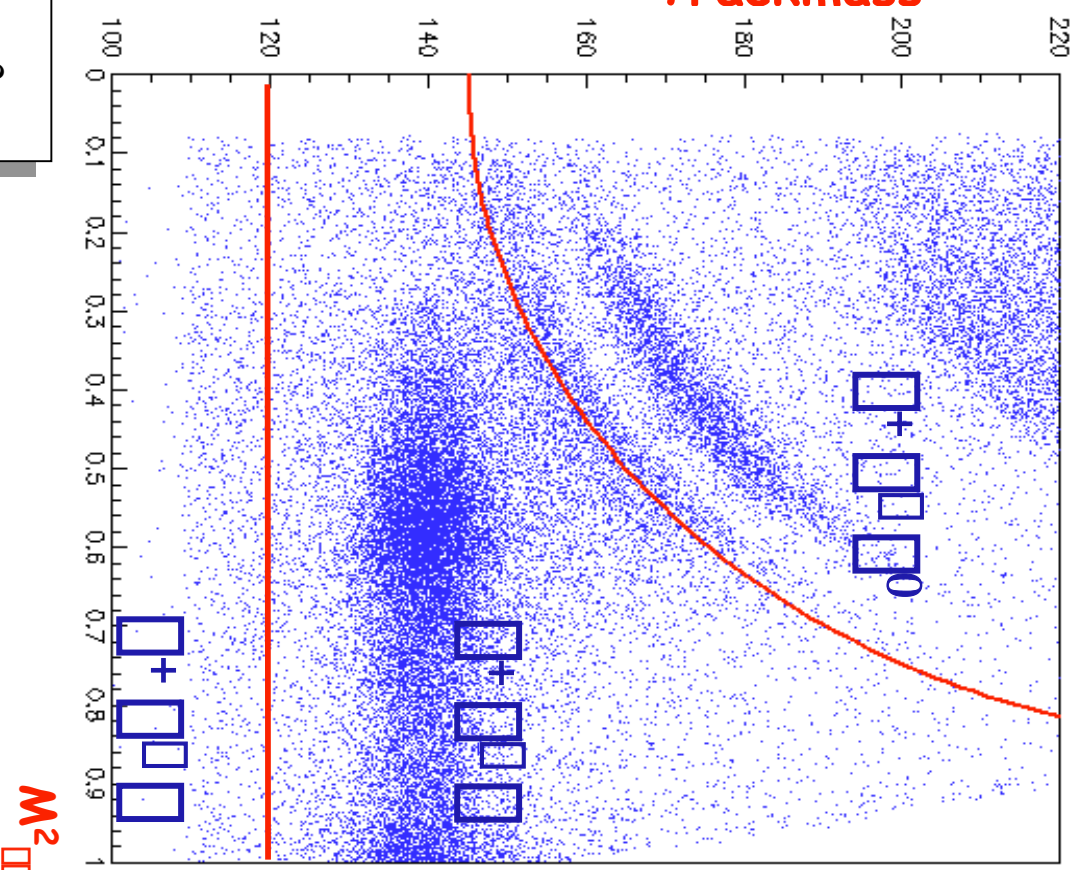
The signal is further selected by performing a cut in the kinetical variable **trackmass** in order to reduce **$\pi^+\pi^+\pi^0$ background**

$\pi^+\pi^+\pi^0$ background

($M_{\text{track}} \approx 105 \text{ MeV}$) is rejected by a cut on $M_{\text{track}} = 120 \text{ MeV}$

The trackmass is the particle mass for the two tracks obtained by using the 4-momentum-conservation and the assumption that both particles have the same mass M_{trk} :

Trackmass



$$q_{\vec{p}}^2 = M_{\vec{p}}^2 \sqrt{p_1^2 + M_{\text{trk}}^2} \sqrt{p_2^2 + M_{\text{trk}}^2} \left(\vec{p}_1 + \vec{p}_2 \right)^2 = 0$$

$M_{\pi\pi}^2$ -Spectrum:



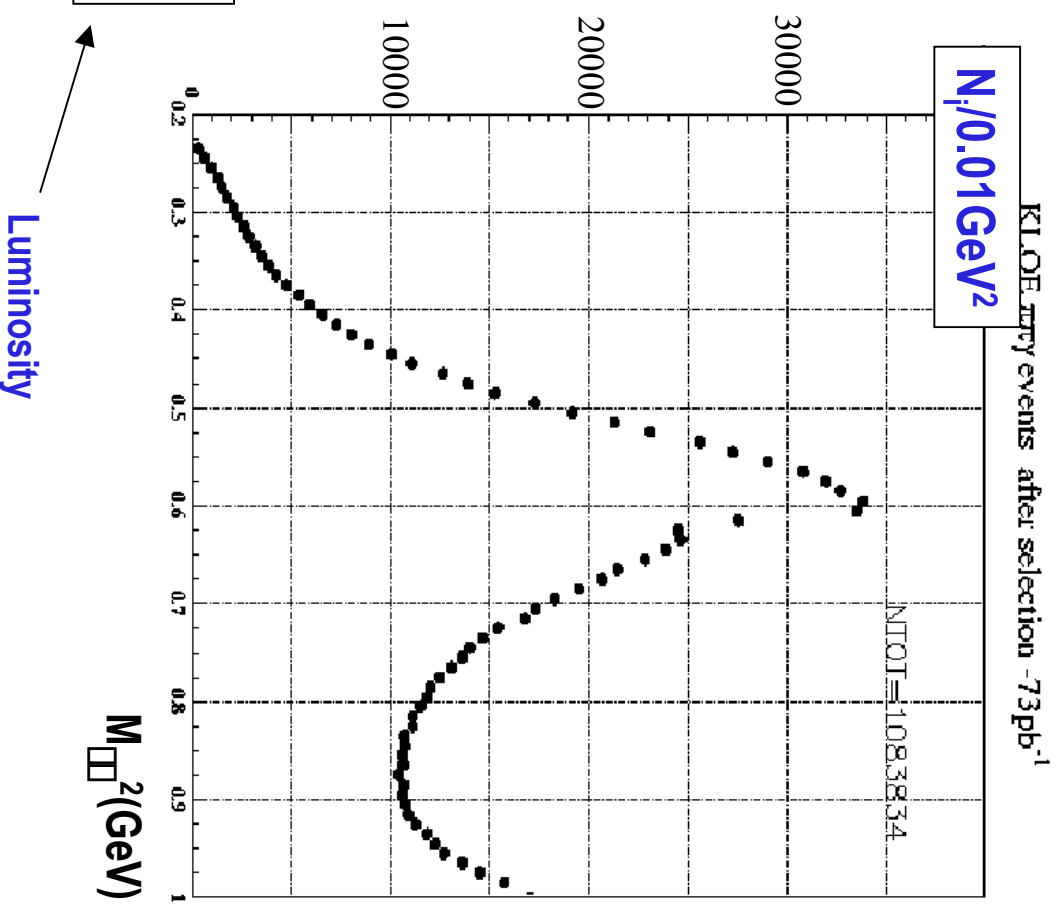
In a preliminary attempt to extract the pion form factor, we analyzed **73 pb⁻¹** of 2001 data according to the analysis items discussed

after selection: **1 100 000 events**
statistical error/bin < 1%
 for $M_{\pi\pi}^2 > 0.45 \text{ GeV}^2$

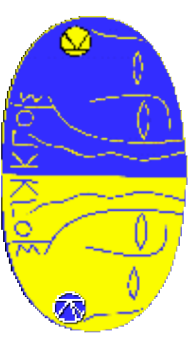
$$\frac{dN_{\pi\pi}}{dM_{\pi\pi}^2} = \frac{N^{\text{obs}} - N^{\text{bkg}}}{\Delta M_{\pi\pi}^2} \cdot \frac{1}{\epsilon_{\text{Select.}}} \cdot \frac{1}{L}$$

Signal
Background

Selection efficiency

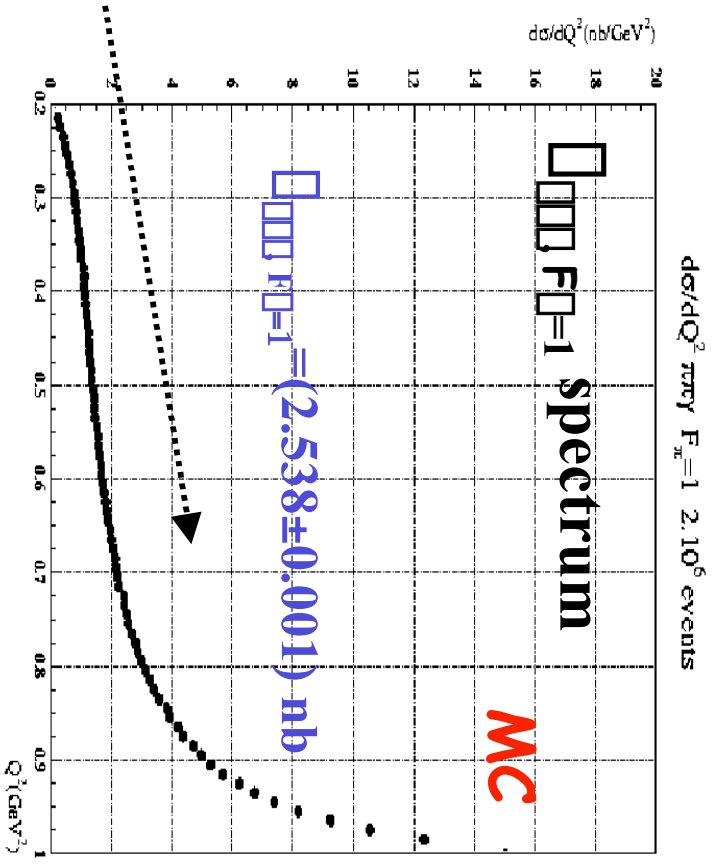
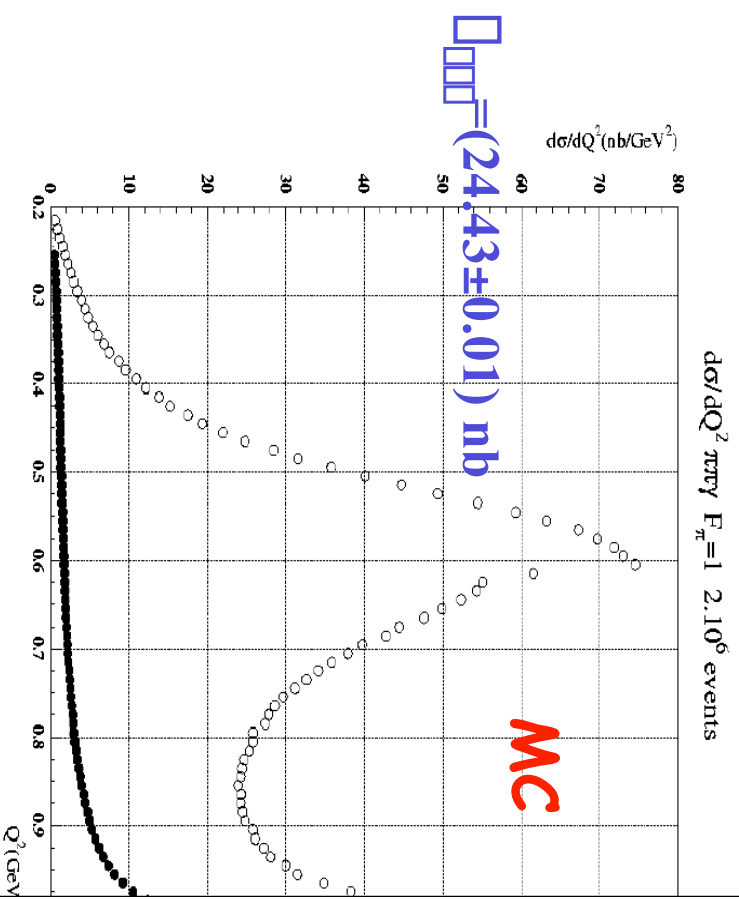


Extraction of pion form factor:



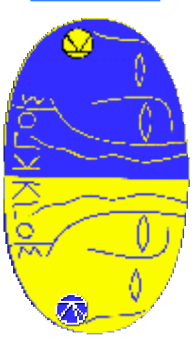
We divide the $\sigma_{\pi^+\pi^0}$ cross section by the cross section $\sigma_{\pi^+\pi^0}$ for “pointlike” pions which is obtained from the MC generator by setting $F_\pi = 1$.

$$\left| F_\pi(M_{\pi\pi}^2) \right|^2 = \frac{d\sigma_{\pi\pi}(M_{\pi\pi}^2)}{d\sigma_{\pi\pi, F_\pi=1}(M_{\pi\pi}^2)}$$



$\sigma_{\pi\pi} F_\pi=1$ was computed with $2 \cdot 10^6$ events of Monte Carlo with $F_\pi=1$, with the acceptance cuts of the analysis: $Q^2 < 15 \text{ GeV}^2$ ($Q^2 > 165 \text{ GeV}^2$), $40^\circ < \theta < 140^\circ$

Pion form factor:



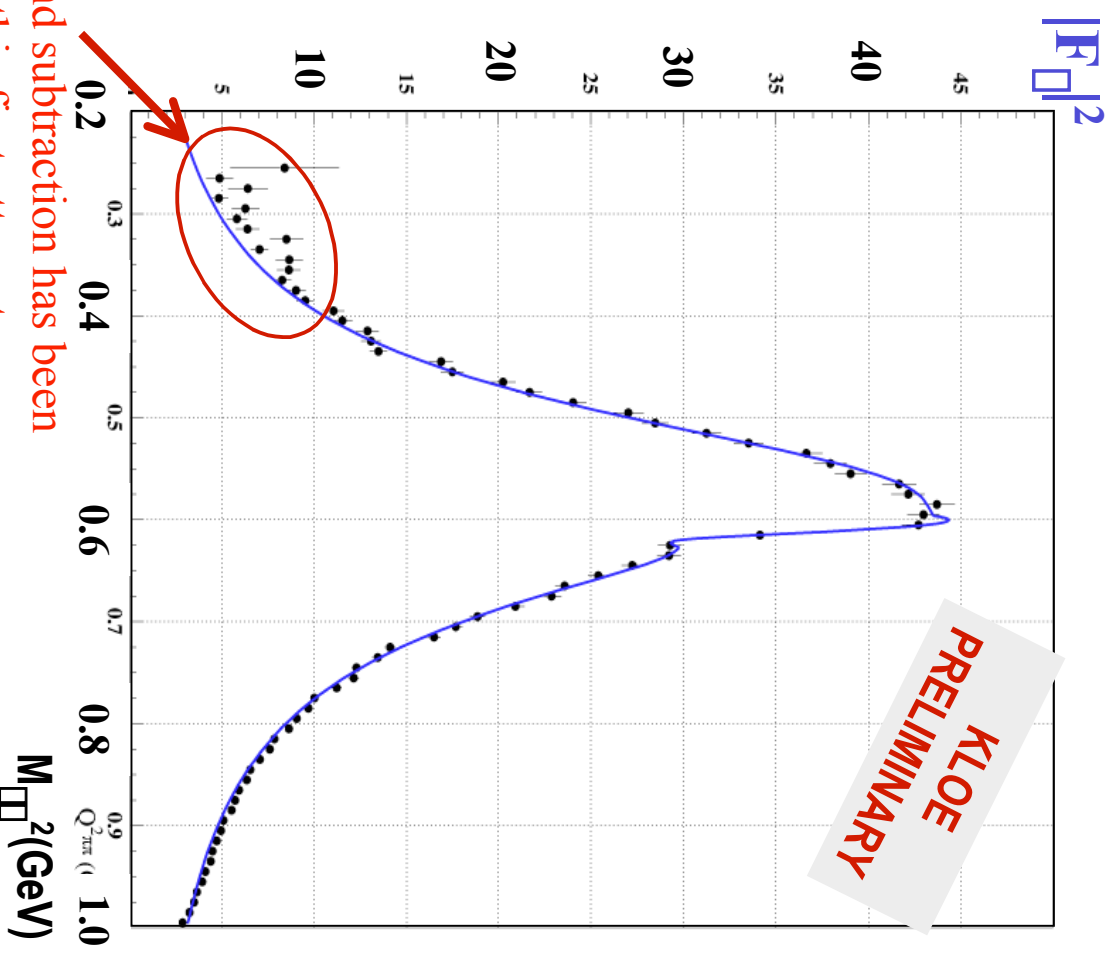
Correcting for efficiencies, normalising to luminosity and dividing the spectrum $d\Gamma/dM_{\pi^0}^2$ by the radiation function $H(M_{\pi^0}^2)$, we get a preliminary extraction of the pion form factor.

The next step is to refine the analysis with the full statistics of 2001 (ca. 170 pb^{-1}).

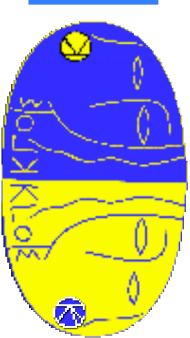
Current work is focused on:

- Efficiency estimation
- Luminosity
- Detector resolution (unfolding)
- Residual background subtraction

No background subtraction has been performed on this first attempt

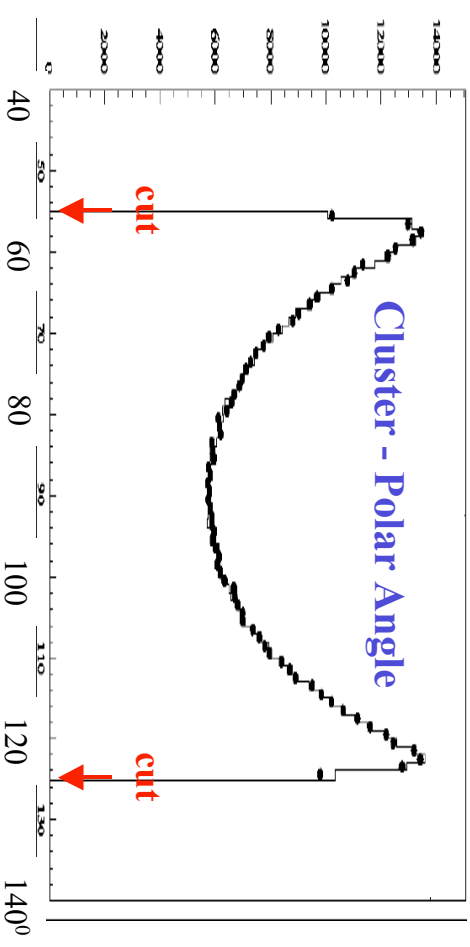


Luminosity:



KLOE uses “Large Angle Bhabhas”
 ($\sigma_{\text{eff}} = 430 \text{ nb}$) to measure the luminosity:

- $55^\circ < \theta_{+,-} < 125^\circ$
- $A_{\text{coll.}} < 9^\circ$
- $E_{+,-} \geq 400 \text{ MeV}$

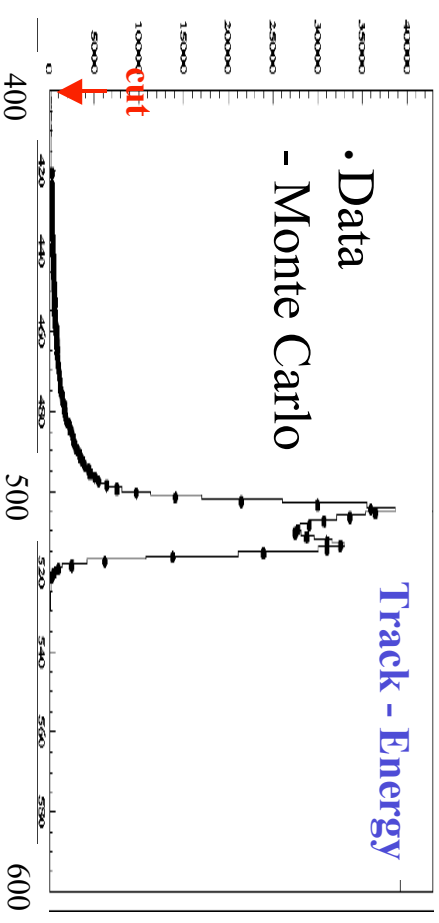


$$\int dt = \frac{N_{\text{Bhabhas}}(\int d\Omega) \cdot (1 - \int \text{Background})}{\int dE \cdot \sigma_{\text{MC}}(E)}$$

Bhabha - Candidates \rightarrow

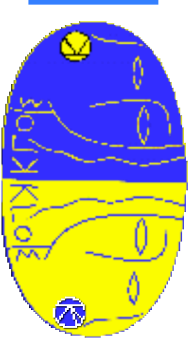
Theoret. Generators with rad. corrections \rightarrow

Background ($\int d\Omega \dots$) \rightarrow



MeV

Luminosity:



We use **2 independent theoretical generators** to calculate the effective cross section for the actual selection cuts:

- 1) Berends (Drago, Venanzoni)
- 2) BABAYAGA (Calame, Montagna)*

Agreement = $(0.1 \pm 0.1)\%$

* C.M.C. Calame et al.
Nucl. Phys., B 584 (2000)

Systematics



Difference DATA-MC:
Acceptance
Efficiencies (EmC, DC)

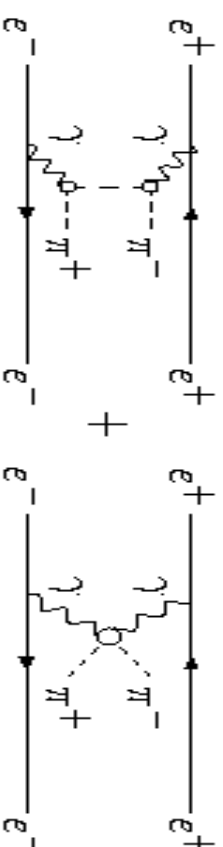
Running Conditions:
Changing s , p_{\perp} , beam position
Calibration of EmC and Drift Chamber

No limitation for luminosity precision < 1% found
→ final precision is currently under evaluation

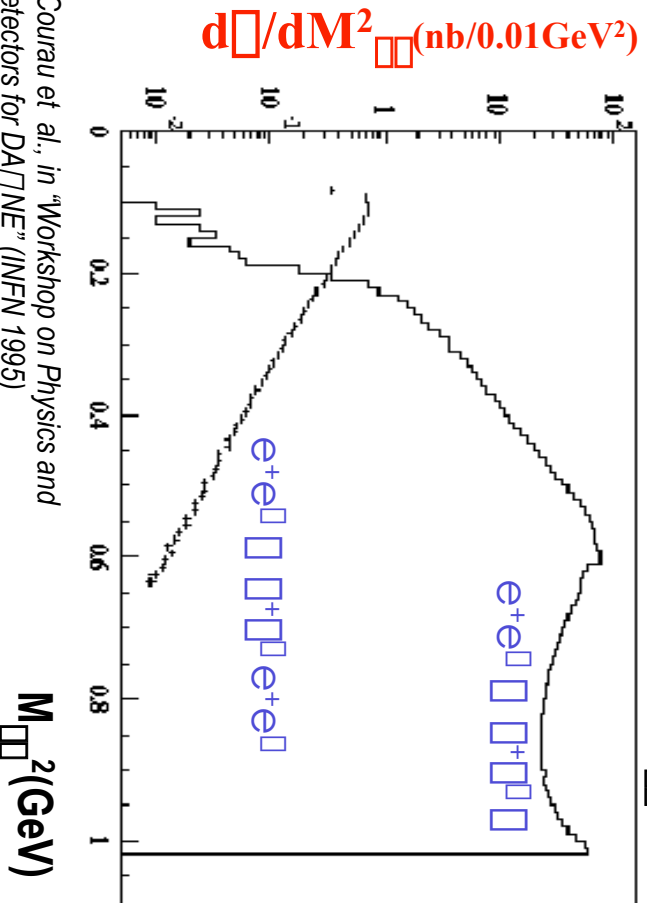
Background: $e^+e^- \rightarrow e^+e^- \pi^+\pi^-$



This process could create a background for our analysis if the electron and the positron go along the beampipe and can not be detected.

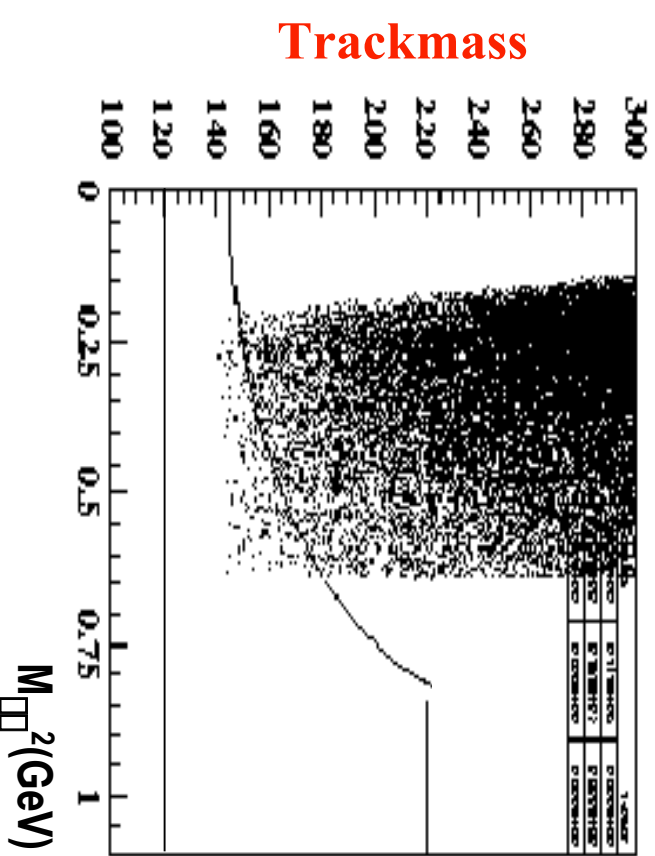


From MC*, we expect a background contribution at low values of $M_{\pi\pi}^2$

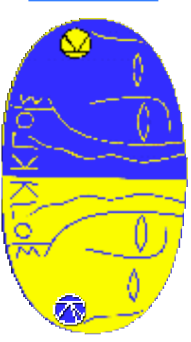


* Courau et al., in "Workshop on Physics and Detectors for DAΦNE" (INFN 1995)

The background is completely rejected by the trackmass cut:



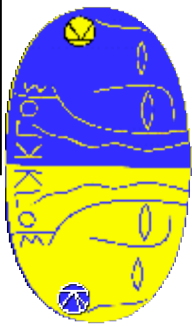
Conclusions:



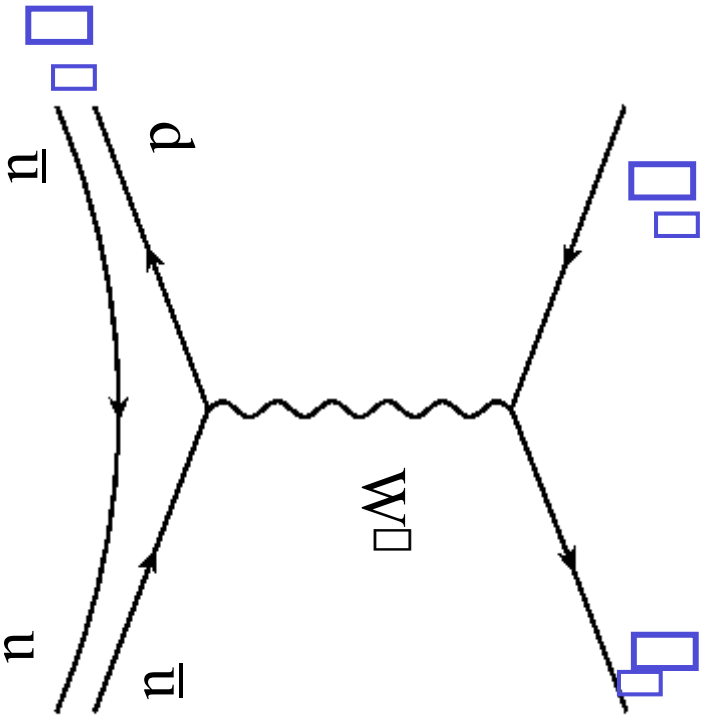
- Last year we have performed an „attempt“ on 73pb⁻¹ of data in order to test a method of getting the pion form factor from a measurement utilizing the radiative return
- Already with this reduced data sample, there are no limitations by statistics
- Now we are refining this measurement using the full statistics from 2001 (170 pb⁻¹) and evaluating systematics of the measurement (background contaminations, detector resolution etc).

We are in the final phase towards a publication of our results!

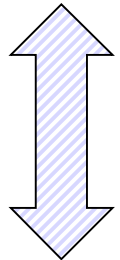
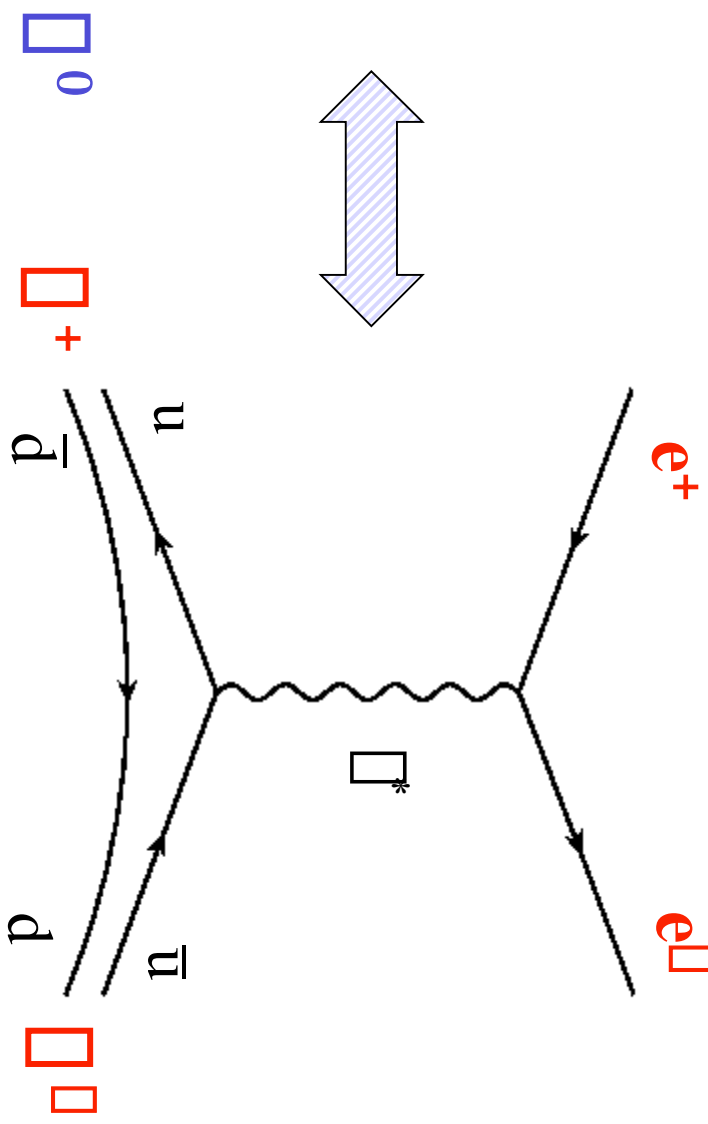
decays:



$$\sigma(e^+e^- \rightarrow \pi^+\pi^0)$$



$$\sigma(e^+e^- \rightarrow \pi^+\pi^-)$$

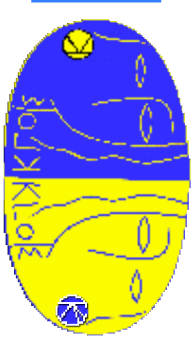


Isospin invariance assumed, one can relate the isovector cross sections $\sigma(e^+e^- \rightarrow \pi^+\pi^-)$ to the spectral function $V_{\pi^0\pi^0}$:

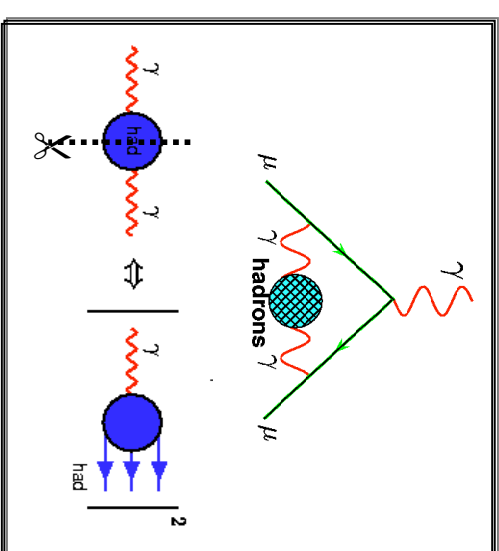
$$\sigma_{e^+e^-}^{I=1} = \frac{4\pi^2}{s} V_{\pi^0\pi^0}, \quad \sqrt{s} \leq M_{\pi^0}$$

Isospin symmetry breaking effects have to be taken into account!

Dispersion integral:



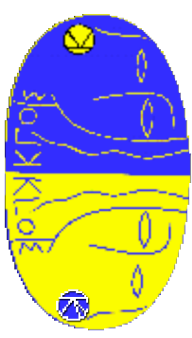
$a_{\square}^{\text{hadr}}$ can be expressed in terms of $\chi_{\square}(e^+e^- \rightarrow \text{hadrons})$ by the use of a **dispersion integral:**



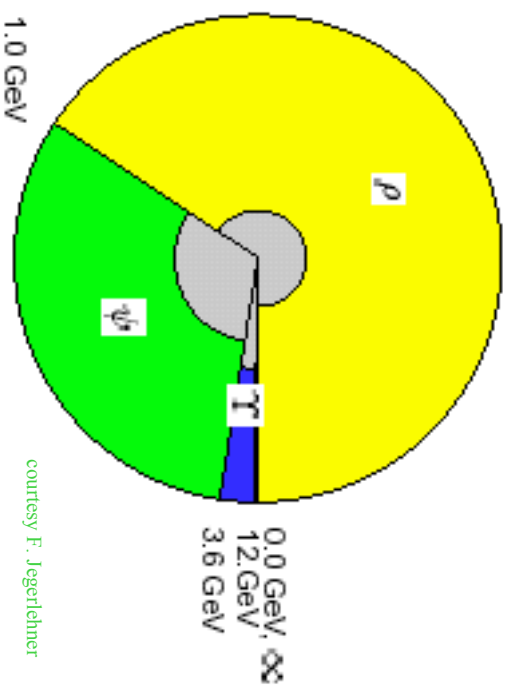
$$a_{\square}^{\text{hadr}} = \frac{1}{4\square^3} \int_{4m_{\square}^2}^{E_{\text{cut}}^2} \chi_{\square}^{\text{hadr,exp}}(s) K(s) ds + \int_{E_{\text{cut}}^2}^{\infty} \chi_{\square}^{\text{hadr,pQCD}}(s) K(s) ds$$

- E_{cut} is the threshold energy above which pQCD is possible
- s is the c.o.m.-energy squared of the hadronic system
- $K(s)$ is a steady function that goes with $1/s$, *enhancing low energy contributions of $\chi_{\square}^{\text{hadr}}(s)$*

Low energy contribution:



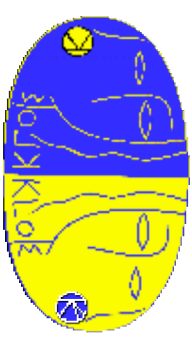
The region around the energy of the Υ -meson adds with ca. 72% to the total value of $a_{\Upsilon}^{\text{hadr}}$. [Jegerlehner; hep-ph/0104304]



The Υ -meson decays to 100% in $\Upsilon^+\Upsilon^-$, so in this energy region the analysis efforts concentrate on the determination of

$$\int (e^+e^- \rightarrow \Upsilon^+\Upsilon^-)$$

Status on $(g-2)_\mu$:



The current status of a_μ from experiment and (SM-) theory:

$$a_\mu^{\text{exp}} (g_\mu-2)/2 = (11\,659\,203.0 \pm 8.0) \times 10^{-10} \quad \text{E821, hep-ex/0208001}$$

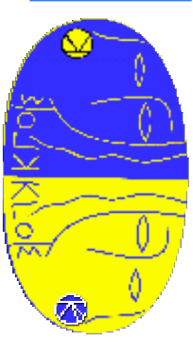
$$a_\mu^{\text{theor, SM}} (g_\mu-2)/2 = a_\mu^{\text{QED}} + a_\mu^{\text{had}} + a_\mu^{\text{weak}}$$

a_μ^{QED}	$= (11\,658\,470.6 \pm 0.3) \times 10^{-10}$	Nucl. Phys. B (Proc. Suppl.) 76, 245
a_μ^{weak}	$= (15.2 \pm 0.1) \times 10^{-10}$	KPPDR hep-ph/0205102
a_μ^{had}	$\left\{ \begin{array}{l} = (707.6 \pm 6.9) \times 10^{-10} \\ = (683.3 \pm 7.8) \times 10^{-10} \end{array} \right.$	DEHZ hep-ph/0208177 v3 based on $e+e-$ data

$$a_\mu^{\text{exp}} - a_\mu^{\text{theor, SM}} = 0.9 - 3.0 \times \text{difference}$$

- The nature of the difference in the two evaluations of a_μ^{had} is currently not understood
- The reduction of the error on the **hadronic contribution** to the SM calculation of a_μ could (together with a further reduction of the experimental error) give this discrepancy between theory and experiment a higher significance

a_{\square}^{had} :



$$a_{\square}^{\text{had}} = a_{\square}^{\text{had}}(l_0) + a_{\square}^{\text{had}}(nl_0) + a_{\square}^{\text{had}}(|b_l|)$$

(see Davier, Eidelmann, Höcker, Zhang hep-ph/0208177)

$$a_{\square}^{\text{had}}(l_0) \begin{cases} = (709.0 \pm 5.9) \square 10^{-10} \\ = (684.7 \pm 7.0) \square 10^{-10} \end{cases}$$

\square based

e+e- based

$$a_{\square}^{\text{had}}(nl_0) = (-10.0 \pm 0.6) \square 10^{-10}$$

Krause, hep-ph/9607259

KN, hep-ph/0111058

BPP, hep-ph/0112255

HK, hep-ph/0112102

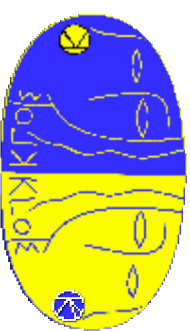
$$a_{\square}^{\text{had}}(|b_l|) = (+8.6 \pm 3.5) \square 10^{-10}$$

\square based

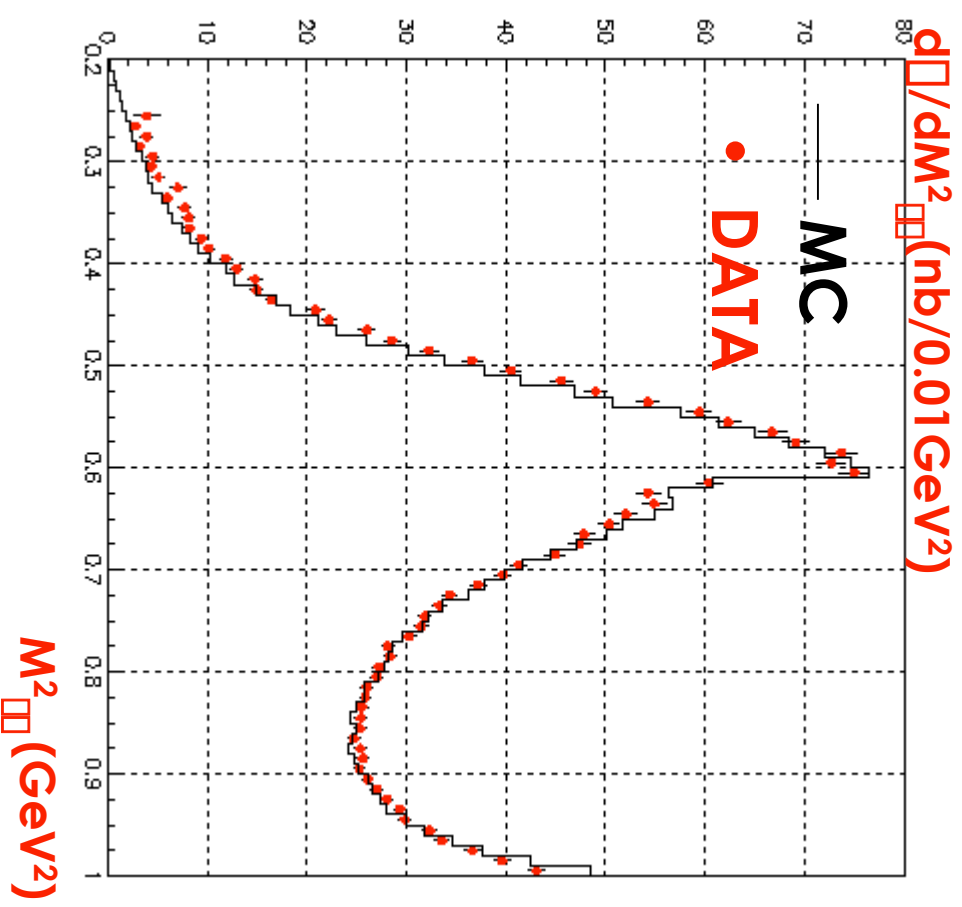
$$a_{\square}^{\text{had}} = \begin{cases} = (707.6 \pm 6.9) \square 10^{-10} \\ = (683.3 \pm 7.8) \square 10^{-10} \end{cases}$$

e+e- based

$d\sigma/dM_{\mu\mu}^2$:

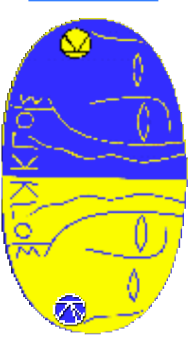


DATA compared with the MC
(MC output has been
interfaced with the detector
simulation program)



Only statistical errors have been taken
into account!

Pion form factor (prelim.):



Data points have been fitted with the
Gounaris-Sakurai-Parametrization

$$F_{\pi^+}(s) = \frac{BW_{\rho}^{GS} \left(1 + \frac{s}{m_{\rho}^2} BW_{\rho} \right) + \alpha BW_{\rho'}^{GS}}{1 + \alpha}$$

(G.J. Gounaris and J.J. Sakurai, Phys.Rev. Lett. 21 (1968), 244)

m_{ρ} , α , ρ , ρ' are free parameters of the fit, while $m_{\rho'}$, $m_{\rho''}$, $m_{\rho''}$ are fixed to CMD-2 values

- $m_{\rho} = 775.1 \pm 0.5 \text{ MeV}$
- $\rho = 147.1 \pm 0.8 \text{ MeV}$
- $\alpha = -0.08 \pm 0.002$
- $\rho' = (2.893 \pm 0.6) \cdot 10^{-3}$
- $\rho'' = (124.8 \pm 9.0)^0$

(Stat. Errors only)

