

# High $Q^2$ Proton Structure

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Photon 2003, Frascati  
7<sup>th</sup> April 2003

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## Contents:

- HERA
- Neutral Current Interactions
- Structure Functions
- Charged Current Interactions
- Parton Densities

## DIS Kinematics

- $Q^2$ : Resolving Power of the exchange boson.

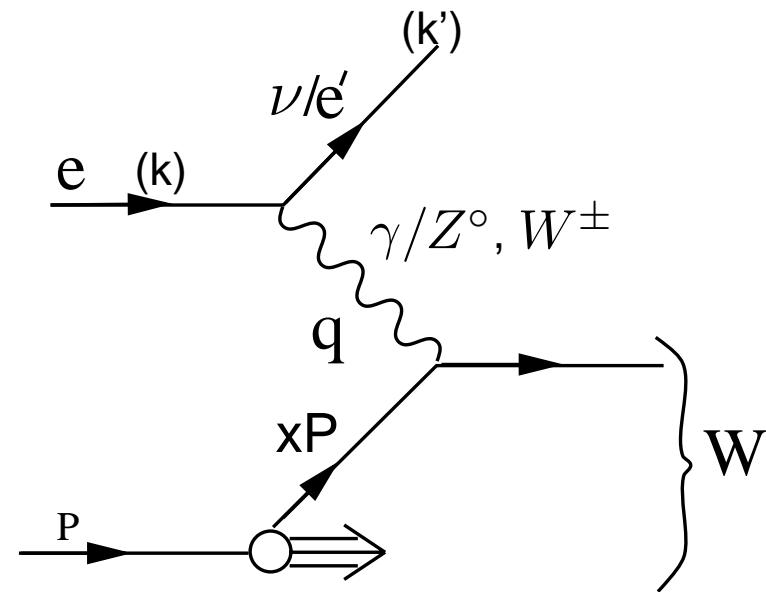
$$Q^2 = -q^2$$

- Bjorken  $x$ : Thought of as the Fraction of Proton momentum carried by Quark.

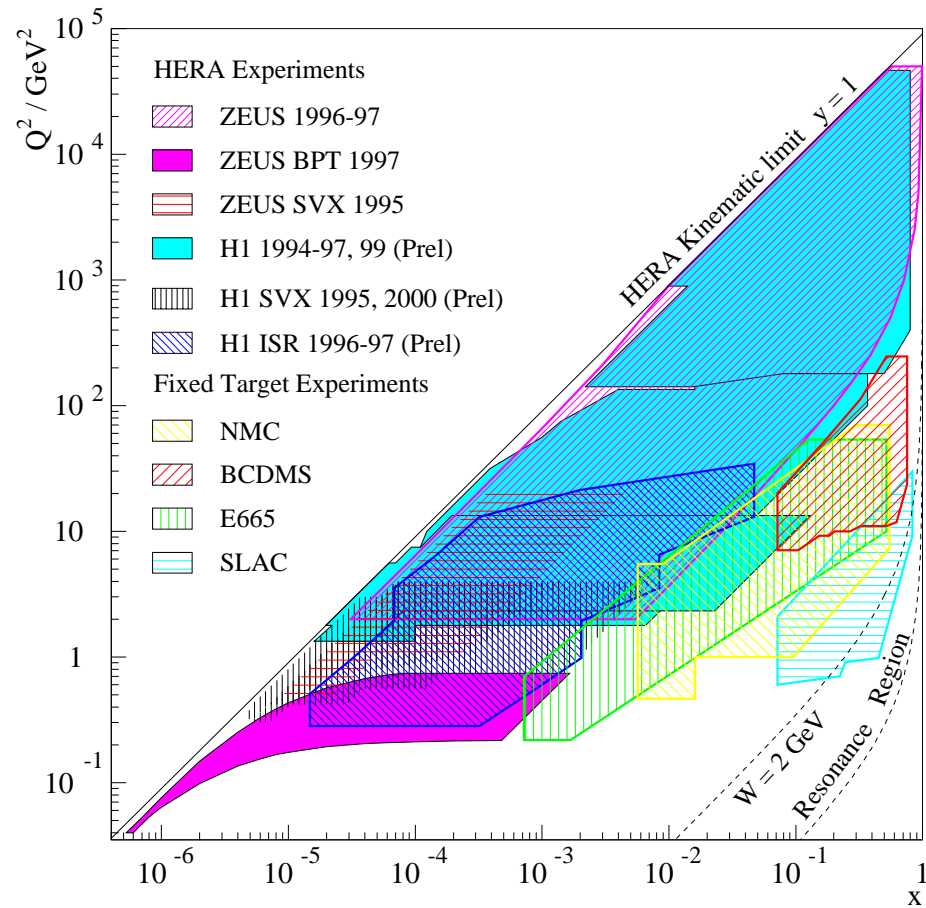
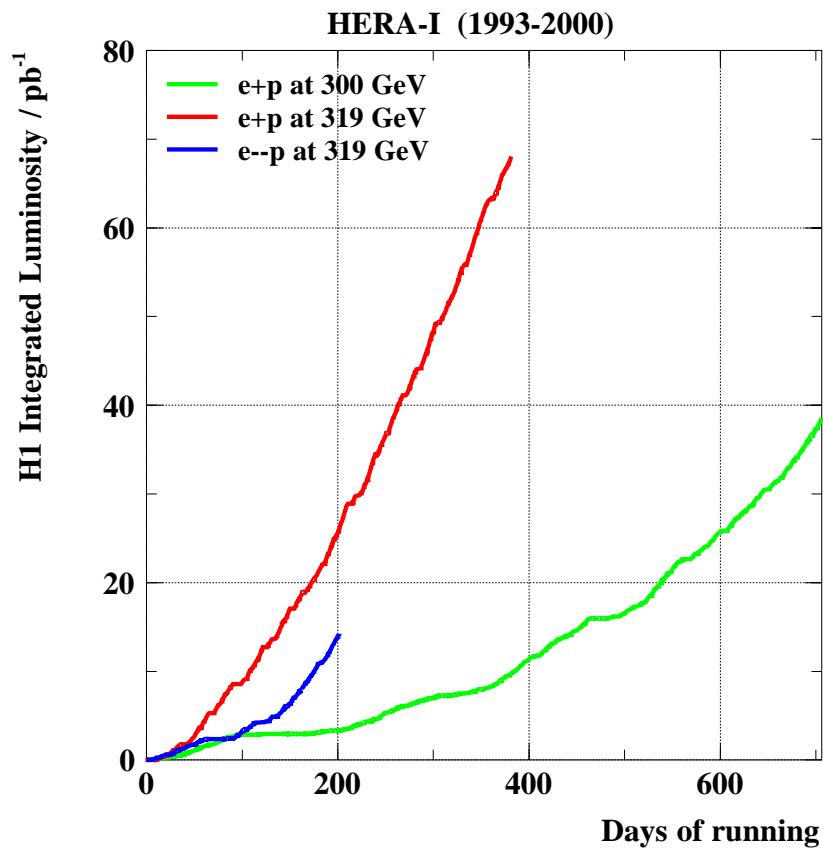
$$x = \frac{Q^2}{2P \cdot q}$$

- $y$ : Inelasticity, Fraction of lepton momentum carried by exchange.

$$y = \frac{P \cdot q}{P \cdot k}$$



# HERA



# Parton Distributions

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NC and CC cross sections are sensitive to the Parton Distribution Functions (PDFs)  
via the proton structure functions

We measure Cross Sections  $\Rightarrow$  Structure Functions

$\hookrightarrow$  access to [PDFs(x)]

Evolution in  $Q^2$  predicted by DGLAP  
(in perturbative range)

## Neutral Current Cross Section

$$\frac{d^2\tilde{\sigma}(e^\mp p)}{dx dQ^2} = \frac{2\pi\alpha^2}{xQ^4} \left[ Y_+ \tilde{F}_2(x, Q^2) - y^2 \tilde{F}_L(x, Q^2) \pm Y_- x \tilde{F}_3(x, Q^2) \right]$$

$$Y_\pm(y) = 1 \pm (1 - y)^2$$

$\tilde{F}_2$ : generalized structure function

$\tilde{F}_L$ : longitudinal structure function

$x\tilde{F}_3$ : term from  $Z^0$  exchange

In Leading Order:

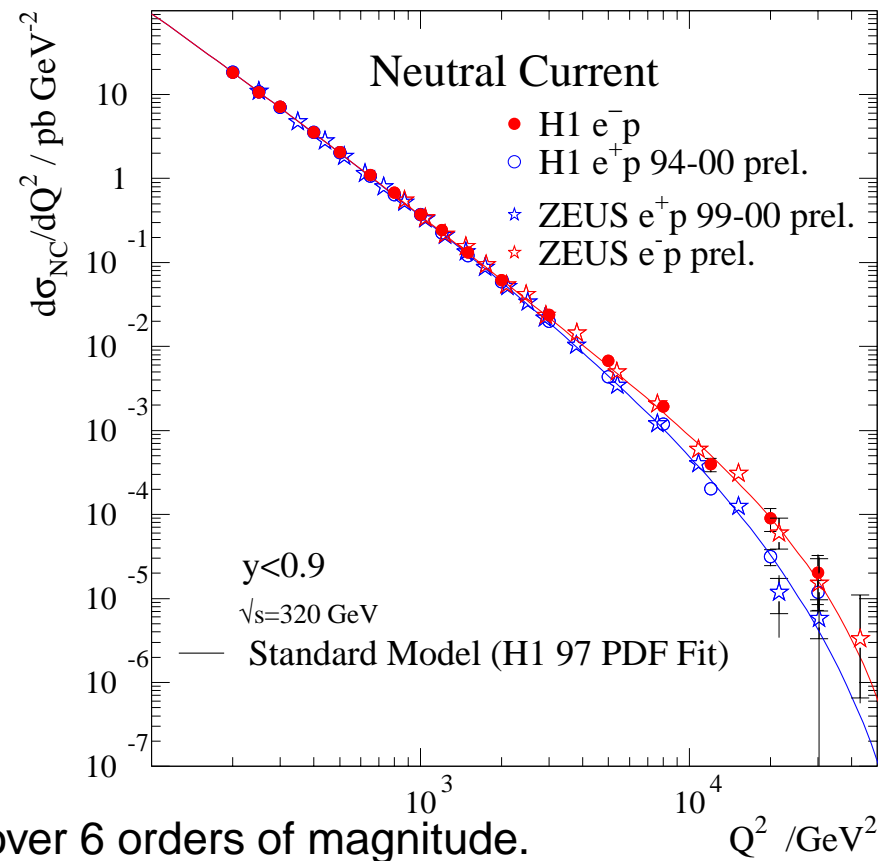
$$\tilde{F}_2 \propto \sum_i (xq_i + x\bar{q}_i)$$

$$x\tilde{F}_3 \propto \sum_i (xq_i - x\bar{q}_i)$$

And write Reduced Cross Section as:

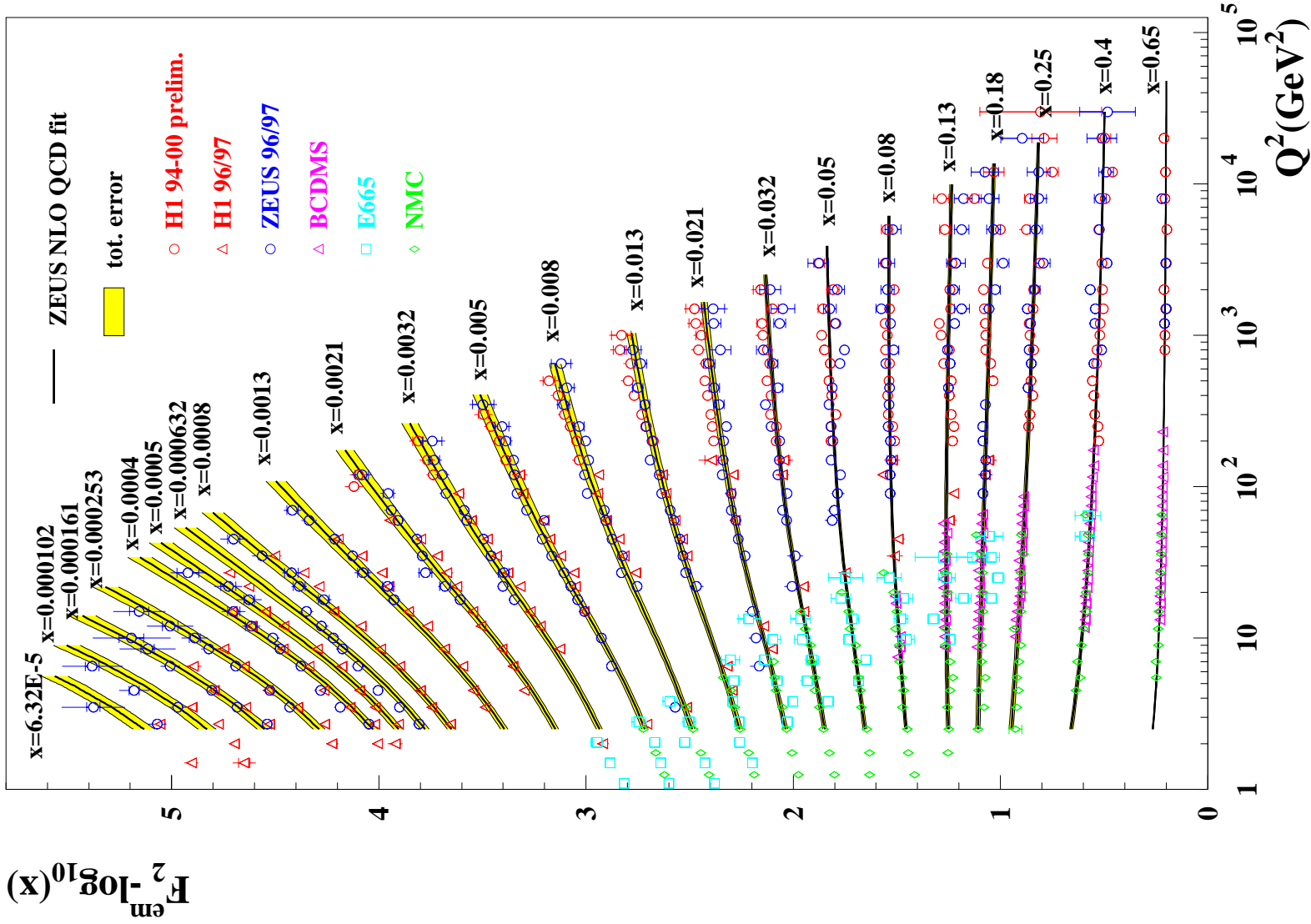
$$\tilde{\sigma}_{NC}^\pm \equiv \left[ \tilde{F}_2 \mp \frac{Y_-}{Y_+} x \tilde{F}_3 - \frac{y^2}{Y_+} \tilde{F}_L \right]$$

- Visible High  $Q^2$  effect ( $Z^0$  contribution).
- Good agreement with the Standard Model over 6 orders of magnitude.



$F_2^{em}$

HERA  $F_2$

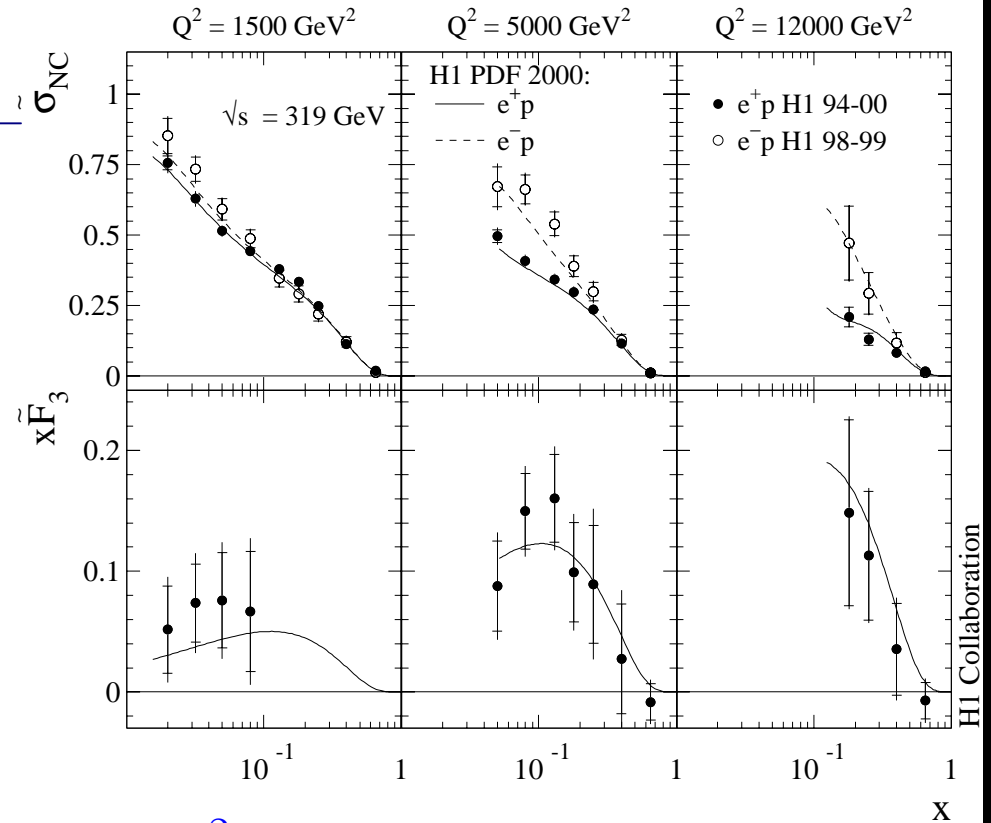
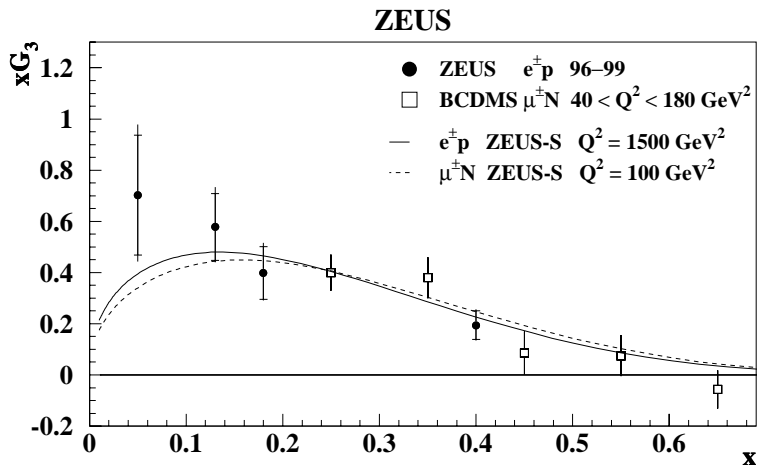


$$\tilde{F}_2 \equiv F_2^{em} - \nu_e \frac{\kappa_w Q^2}{Q^2 + M_Z^2} F_2^{\gamma Z} + (\nu_e^2 + a_e^2) \left[ \frac{\kappa_w Q^2}{Q^2 + M_Z^2} \right]^2 F_2^Z$$

# $x\tilde{F}_3$

$$\tilde{\sigma}_{NC}^{\pm} \approx \left[ \tilde{F}_2 \mp \frac{Y_-}{Y_+} x\tilde{F}_3 \right]$$

- $x\tilde{F}_3$  measured by subtracting  $\tilde{\sigma}^+$  from  $\tilde{\sigma}^-$
- Require  $Q^2 \simeq M_Z^2$  ( $10^4 \text{ GeV}^2$ )
- Direct sensitivity to valence quarks



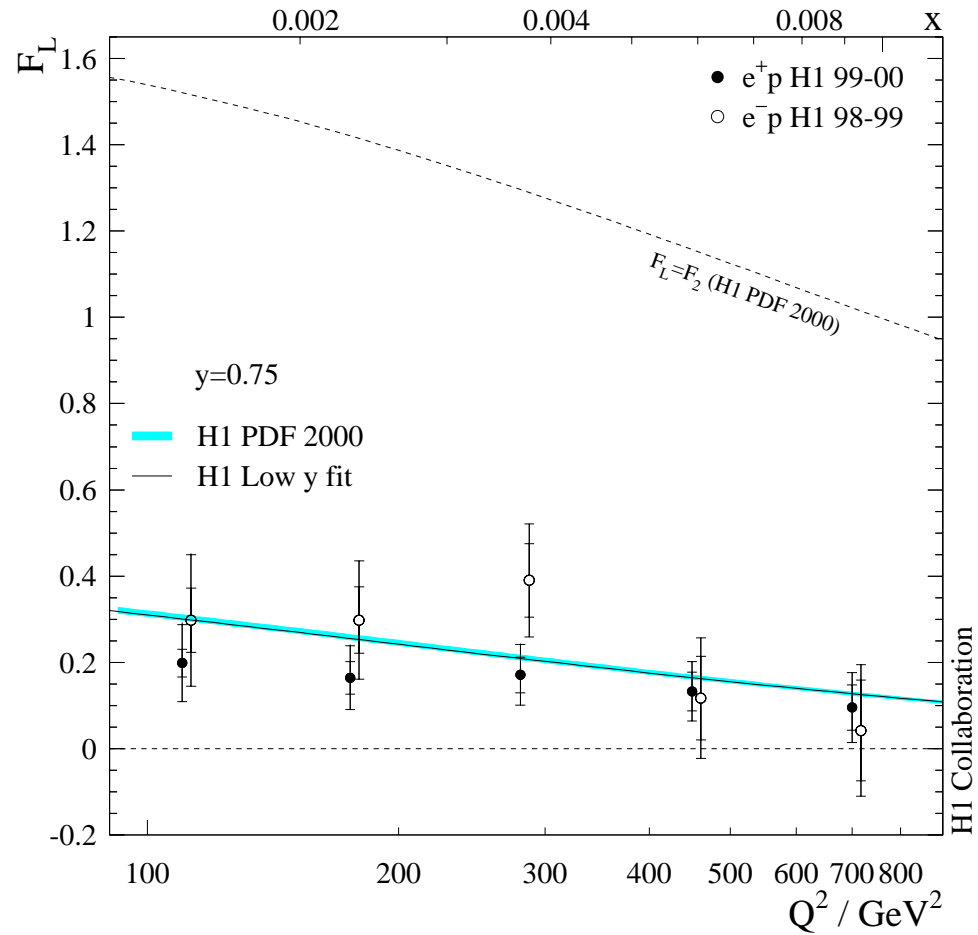
$$x\tilde{F}_3 \equiv -a_e \frac{\kappa_w Q^2}{Q^2 + M_Z^2} xF_3^{\gamma Z} + (2\nu_e a_e) \left[ \frac{\kappa_w Q^2}{Q^2 + M_Z^2} \right]^2 xF_3^Z$$

$$\tilde{F}_L$$

$$\tilde{\sigma} \approx \left[ \tilde{F}_2 - \frac{y^2}{Y_+} \tilde{F}_L \right]$$

$$\tilde{F}_L \sim xg$$

- Extracted at high  $y$  (and low  $Q^2$ )
- Assume  $\tilde{F}_2$  from NLO QCD Model
- $e^+$  and  $e^-$  data consistent
- Agreement with QCD prediction
- Inconsistent with  $\tilde{F}_L = 0$  and  $\tilde{F}_L = \tilde{F}_2$





## Charged Current DIS

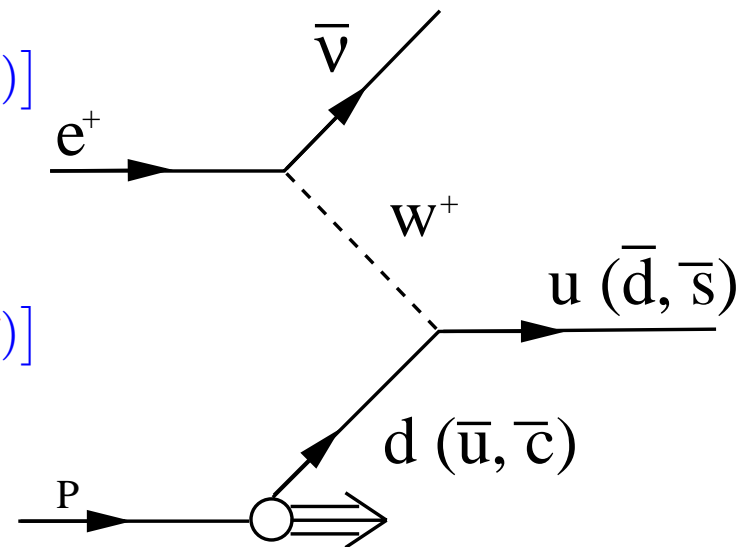
- $e^+ p \longrightarrow \bar{\nu} X$ : Probe  $d$  valence at high  $x$

$$\frac{d^2\sigma}{dx dQ^2} = \frac{G_F^2}{2\pi} \left[ \frac{Q^2}{Q^2 + M_W^2} \right]^2 [\bar{u} + \bar{c} + (1-y)^2(d+s)]$$

- $e^- p \longrightarrow \nu X$ : Probe  $u$  valence at high  $x$

$$\frac{d^2\sigma}{dx dQ^2} = \frac{G_F^2}{2\pi} \left[ \frac{Q^2}{Q^2 + M_W^2} \right]^2 [u + c + (1-y)^2(\bar{d} + \bar{s})]$$

- Sensitivity to separate parton densities
- Sensitive to **sea** quarks at low  $x$



Define  $u + c = U$  and  $d + s = D$

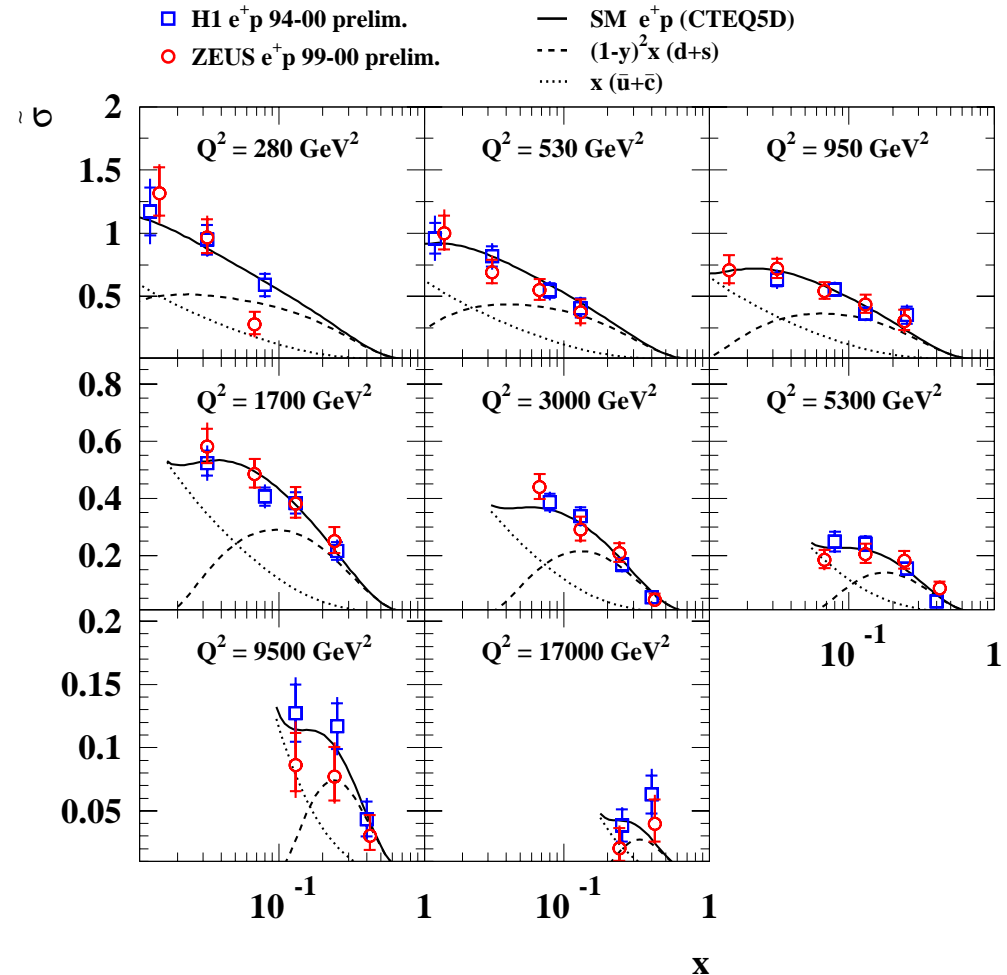
# $\tilde{\sigma}_{CC}$

$$\tilde{\sigma}_{CC}^+ = x \cdot [\bar{u} + \bar{c} + (1 - y)^2(d + s)]$$

$$\tilde{\sigma}_{CC}^- = x \cdot [u + c + (1 - y)^2(\bar{d} + \bar{s})]$$

- PDF agrees with Data points
- 2 Orders of Magnitude in  $Q^2$  and 2 Orders of Magnitude in  $x$
- At high  $x$ , D contribution dominates

## HERA I high $Q^2$ $e^+p$ Charged Current



## Extraction of the PDFs

Parton Distribution Functions are parametrised depending on x

### H1

Use only H1 Data

cross check with BCDMS

$$Q_o^2 = 4 \text{ GeV}^2$$

Data  $3.5 < Q^2 < 30,000 \text{ GeV}^2$

parametrisation of combinations:

$$xg, xU, xD, x\bar{U}, x\bar{D}$$

$$U = u + c, D = d + s$$

⇒ 13 free parameters

### ZEUS

Both Zeus only data and World data

cross check with NMC, BCDMS, E665, CCFR

$$Q_o^2 = 7 \text{ GeV}^2$$

Data  $2.5 < Q^2 < 30,000$  with  $W > 20 \text{ GeV}^2$

'classical' parametrisation:

$$xg, x\text{Sea}, u_v, d_v, (\bar{u} - \bar{d})$$

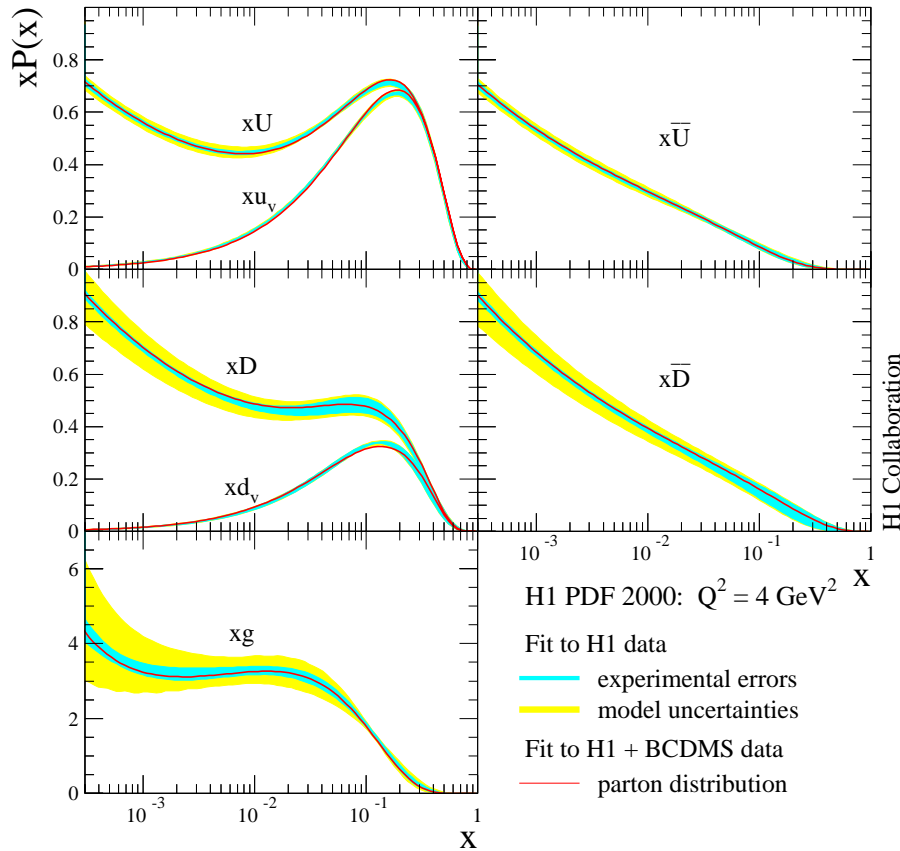
sum rules,

several assumptions, e.g. on sea distributions

⇒ 11 free parameters

# PDFs from NLO QCD Fits

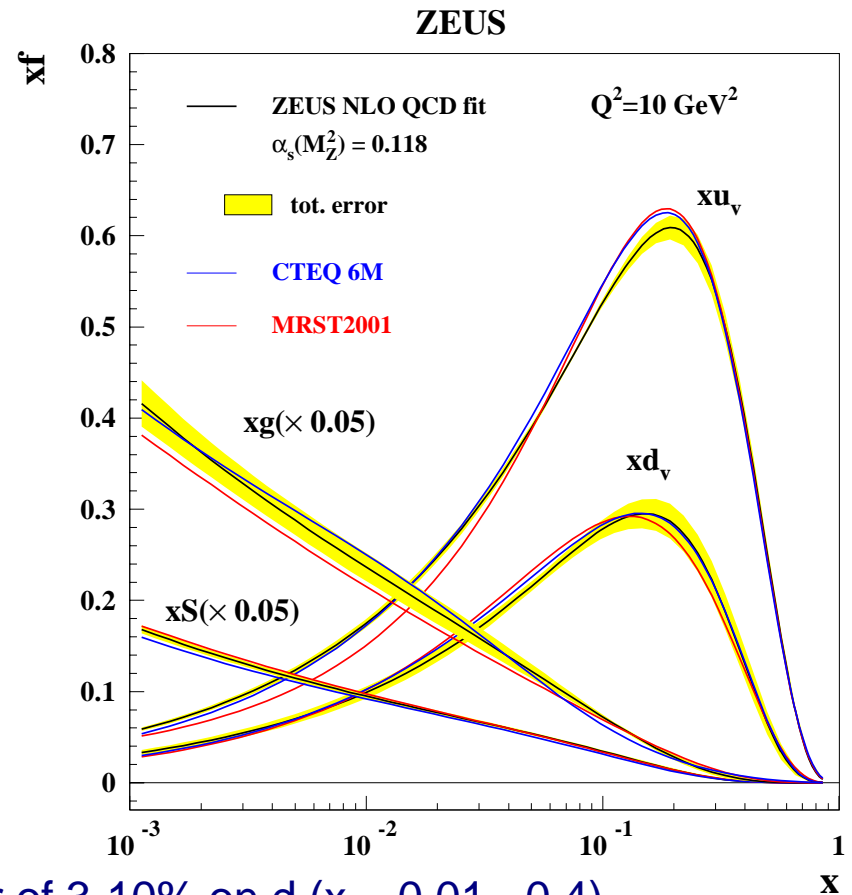
PDFs at  $Q^2 = 4\text{GeV}^2$



• Error of 1-2% on u ( $x = 0.01 - 0.4$ )

• Error of 3-10% on d ( $x = 0.01 - 0.4$ )

Zeus + Fixed Target fit compared to global fits:



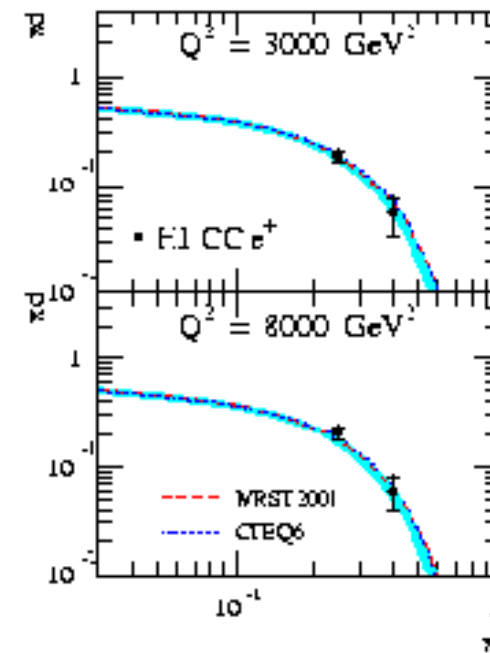
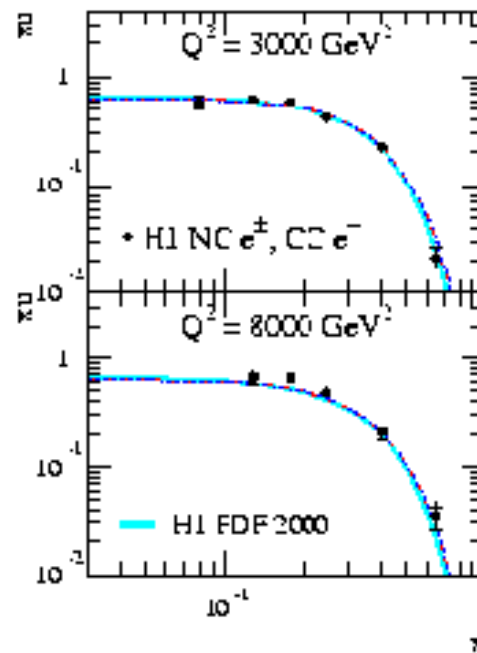
## xu and xd at large x

H1 local extraction of data points:

$$xq_{ex} = \tilde{\sigma}_{meas} \times \frac{xq_{th}}{\tilde{\sigma}_{th}}$$

- Ingredients:

- ▷ QCD assumptions on u and d (70% at high x)
- ▷ local NC and CC cross section measurement for quark separation
- ⇒ less sensitive to assumptions in other regions of phase space



# Summary

- $\tilde{\sigma}_{NC}$  and  $\tilde{\sigma}_{CC}$  well Measured
- $\tilde{F}_2$  errors to 2%
- $\tilde{F}_3$  errors statistically dominated (reduced with Hera II running)
- $\tilde{F}_L$  Measured with Hera II low energy running
- Hera PDFs Consistent with global fits
- Do not rely on global fits
- Error on u 1%( $x=0.01$ ) - 2%( $x=0.4$ ) [H1]
- Error on d 3%( $x=0.01$ ) - 10%( $x=0.4$ ) [H1]
- Error on quark sea  $\sim 5\%$  ( $x \leq 0.1$ ) [Zeus]
- Error on gluon  $\sim 10\%$  ( $x \leq 0.1$ ) [Zeus]

