

# Update of $\eta$ - $\eta'$ mixing from $J/\psi \rightarrow VP$ decays

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**PHI****PSI**08

"International Workshop on  $e^+e^-$  collisions from Phi to Psi"

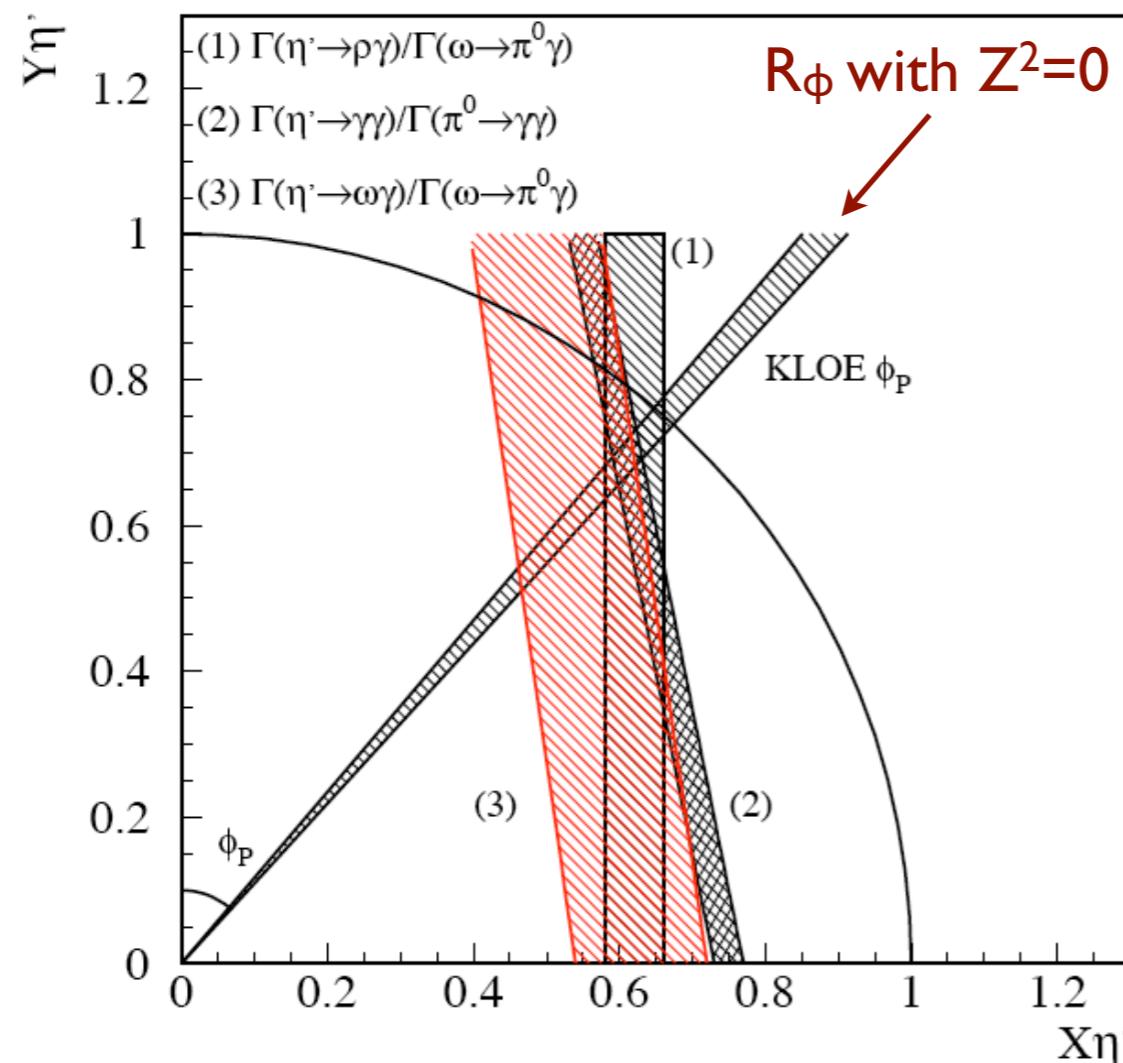
April 9, 2008

LNF, Frascati (Italy)

Work partly supported by the EU, MRTN-CT-2006-035482, "FLAVIAnet" network

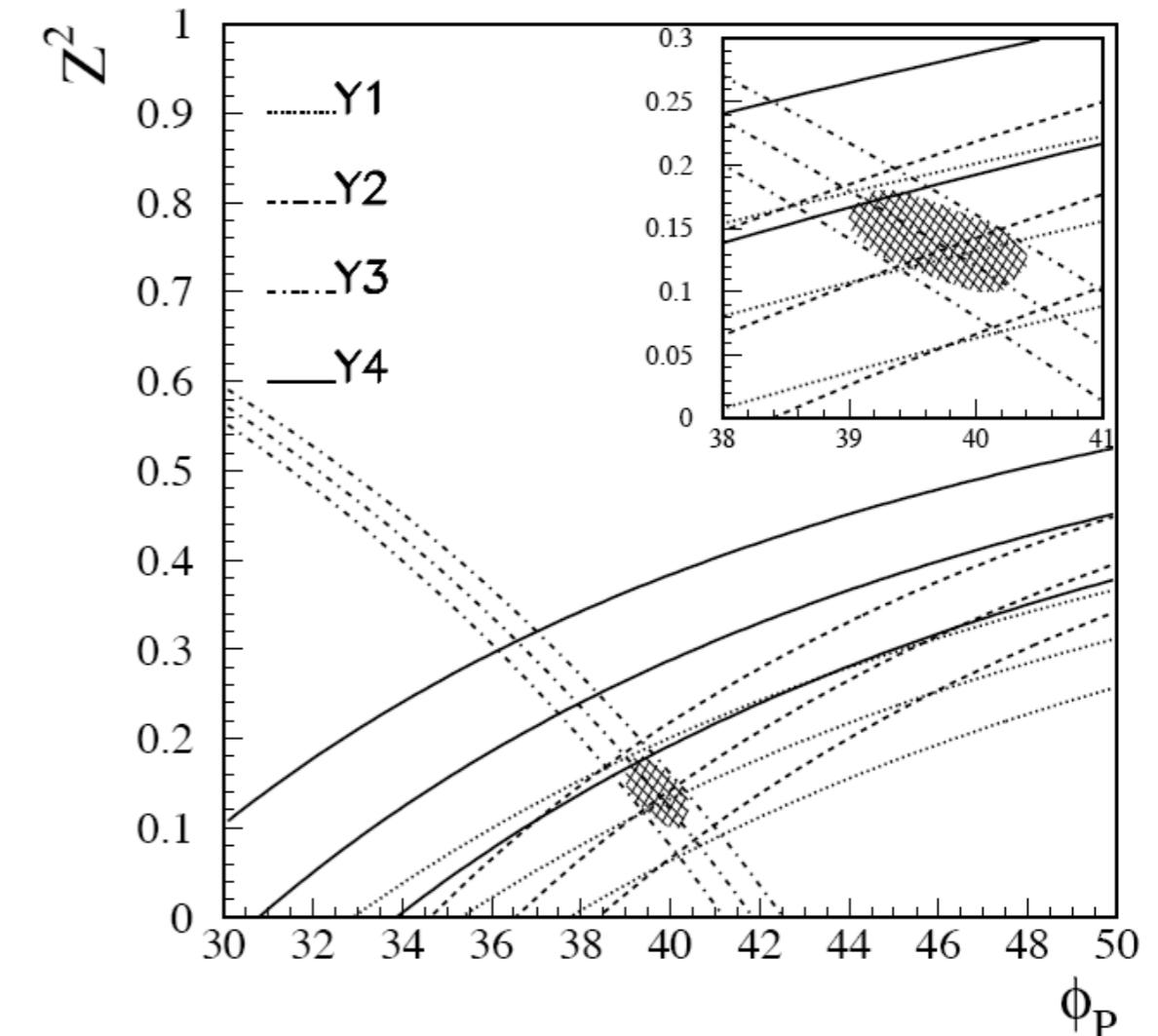
## • Motivation

KLOE Collaboration, Phys. Lett. B648 (2007) 267



$$\phi_P = (39.7 \pm 0.7)^\circ$$

$$Z_{\eta'}^2 = 0.14 \pm 0.04$$



$$\begin{aligned}
 Y1 &= \eta' \rightarrow \gamma\gamma / \pi^0 \rightarrow \gamma\gamma \\
 Y2 &= \eta' \rightarrow \rho\gamma / \omega \rightarrow \pi^0\gamma \\
 Y3 &= \phi \rightarrow \eta'\gamma / \phi \rightarrow \eta\gamma \\
 Y4 &= \eta' \rightarrow \omega\gamma / \omega \rightarrow \pi^0\gamma
 \end{aligned}$$

## • Motivation

R. E. and J. Nadal, JHEP 05 (2007) 6

Purpose: to perform a phenomenological analysis of radiative  $V \rightarrow P\gamma$  and  $P \rightarrow V\gamma$  decays, with  $V = \rho, K^*, \omega, \phi$  and  $P = \pi, K, \eta, \eta'$ , aimed at determining the gluonic content of the  $\eta$  and  $\eta'$  wave functions

Conclusions:

- i) assuming  $Z_\eta = Z_{\eta'} = 0$  from the beginning, we got  $\phi_P = (41.1 \pm 1.1)^\circ$  with  $\chi^2/\text{d.o.f.} = 4.4/5$
- ii) accepting the absence of gluonium for the  $\eta$  meson, the gluonic content of the  $\eta'$  wave function amounts to  $|\phi_{\eta'G}| = (12 \pm 13)^\circ$  or  $(Z_{\eta'})^2 = 0.04 \pm 0.09$  and the  $\eta$ - $\eta'$  mixing angle is found to be  $\phi_P = (41.4 \pm 1.3)^\circ$   $\chi^2/\text{d.o.f.} = 4.2/4$
- iii) accepting the absence of gluonium for the  $\eta'$  meson, the gluonic content of the  $\eta$  wave function amounts to  $|\phi_{\eta G}| \approx 0^\circ$  or  $(Z_\eta)^2 = 0.00 \pm 0.12$  and the  $\eta$ - $\eta'$  mixing angle is found to be  $\phi_P = (41.5 \pm 1.3)^\circ$   $\chi^2/\text{d.o.f.} = 4.4/4$



The current experimental data on  $VP\gamma$  transitions indicated within our model a negligible gluonic content for the  $\eta$  and  $\eta'$  mesons

**Purpose:** to perform a **phenomenological analysis** of  $J/\psi \rightarrow VP$  decays, with  $V=\rho, K^*, \omega, \phi$  and  $P=\pi, K, \eta, \eta'$ , aimed at determining the **gluonic content** of the  $\eta$  and  $\eta'$  wave functions

**Why?** to confirm or not the **gluonic content** of the  $\eta'$  wave function

**Feasible?** yes, because we have at our disposal all the **needed experimental information**

## Outline:

- *Notation*
- *Experimental input*
- *A model for  $J/\psi \rightarrow VP$  transitions*
- *Preliminary results*
- *Summary and conclusions*

## • Notation

J. L. Rosner, Phys. Rev. D27 (1983) 1101

We work in a **basis** consisting of the states

$$|\eta_q\rangle \equiv \frac{1}{\sqrt{2}}|u\bar{u} + d\bar{d}\rangle \quad |\eta_s\rangle = |s\bar{s}\rangle \quad |G\rangle \equiv |\text{gluonium}\rangle$$

The **physical states**  $\eta$  and  $\eta'$  are assumed to be the linear combinations

$$\begin{aligned} |\eta\rangle &= X_\eta |\eta_q\rangle + Y_\eta |\eta_s\rangle + Z_\eta |G\rangle , \\ |\eta'\rangle &= X_{\eta'} |\eta_q\rangle + Y_{\eta'} |\eta_s\rangle + Z_{\eta'} |G\rangle , \end{aligned}$$

with  $X_{\eta(\eta')}^2 + Y_{\eta(\eta')}^2 + Z_{\eta(\eta')}^2 = 1$  and thus  $X_{\eta(\eta')}^2 + Y_{\eta(\eta')}^2 \leq 1$

A **significant gluonic admixture** in a state is possible only if

$$Z_{\eta(\eta')}^2 = 1 - X_{\eta(\eta')}^2 - Y_{\eta(\eta')}^2 > 0$$

**Assumptions:**

- no mixing with  $\pi^0$  (isospin symmetry)
- no mixing with  $\eta_c$  states
- no mixing with radial excitations

- **Notation**

In absence of gluonium (standard picture)

$$Z_{\eta(\eta')} \equiv 0$$



$$\begin{aligned} |\eta\rangle &= \cos\phi_P|\eta_q\rangle - \sin\phi_P|\eta_s\rangle \\ |\eta'\rangle &= \sin\phi_P|\eta_q\rangle + \cos\phi_P|\eta_s\rangle \end{aligned}$$

with  $X_\eta = Y_{\eta'} \equiv \cos\phi_P$  and  $X_{\eta'}^2 + Y_{\eta'}^2 = 1$

$$X_{\eta'} = -Y_\eta \equiv \sin\phi_P$$

where  $\phi_P$  is the  $\eta$ - $\eta'$  mixing angle in the quark-flavour basis related to its octet-singlet analog through

$$\theta_P = \phi_P - \arctan \sqrt{2} \simeq \phi_P - 54.7^\circ$$

Similarly, for the vector states  $\omega$  and  $\phi$  the mixing is given by

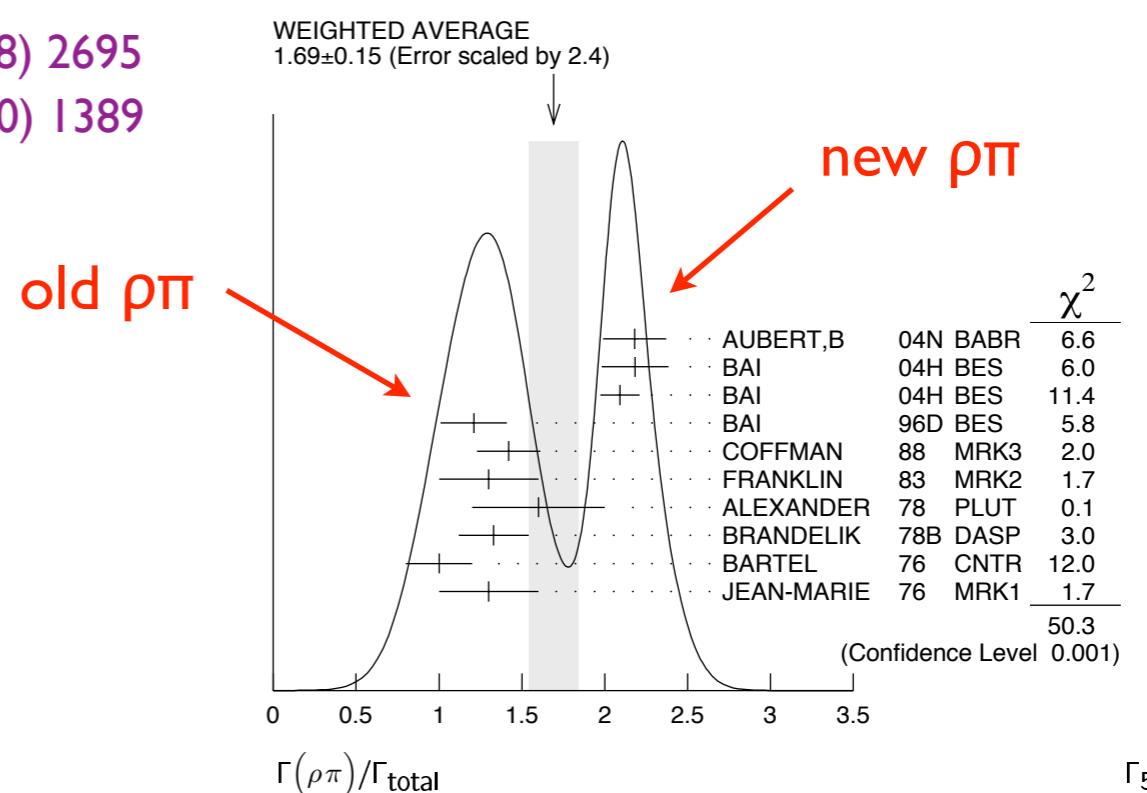
$$\begin{aligned} |\omega\rangle &= \cos\phi_V|\omega_q\rangle - \sin\phi_V|\phi_s\rangle \\ |\phi\rangle &= \sin\phi_V|\omega_q\rangle + \cos\phi_V|\phi_s\rangle \end{aligned}$$

where  $\omega_q$  and  $\phi_s$  are the analog non-strange and strange states of  $\eta_q$  and  $\eta_s$ , respectively.

- *Experimental input*

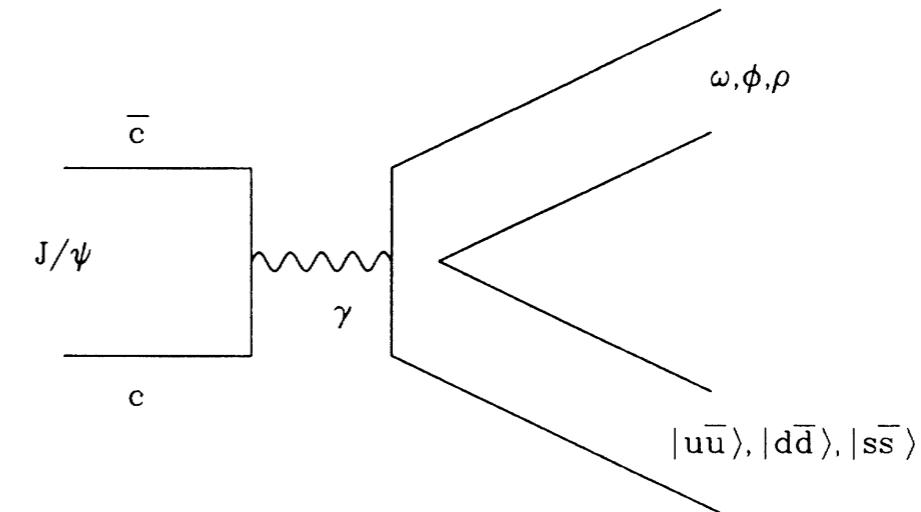
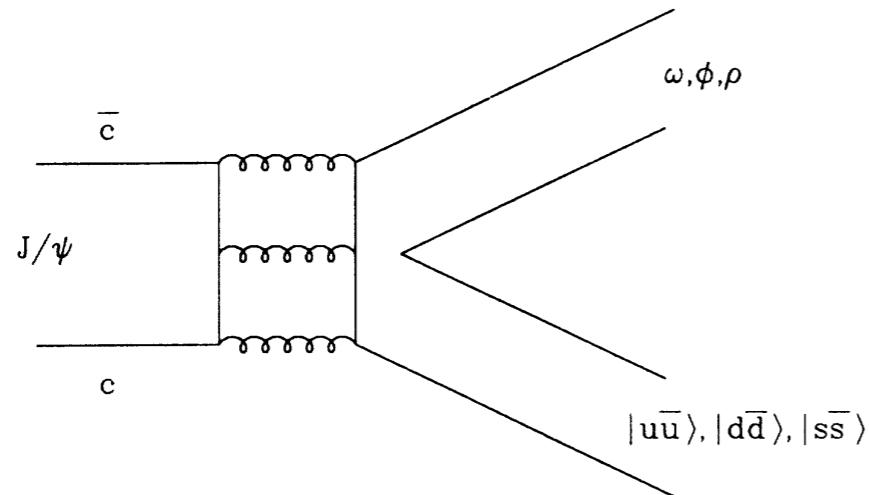
| $\text{BR} \times 10^{-3}$      | PDG'97*           | PDG'07              |   |
|---------------------------------|-------------------|---------------------|---|
| $\rho\pi$                       | $12.8 \pm 1.0$    | $16.9 \pm 1.5$      | BABAR Coll., Phys. Rev. D70 (04) 072004 |
| $K^{*+}K^- + \text{c.c.}$       | $5.0 \pm 0.4$     | =                   | BES Coll., Phys. Rev. D70 (04) 012005   |
| $K^{*0}\bar{K}^0 + \text{c.c.}$ | $4.2 \pm 0.4$     | =                   |   |
| $\omega\eta$                    | $1.58 \pm 0.16$   | $1.74 \pm 0.20$     | BABAR Coll., Phys. Rev. D73 (06) 052003 |
| $\omega\eta'$                   | $0.167 \pm 0.025$ | $0.182 \pm 0.021$   | BES Coll., Phys. Rev. D73 (06) 052007   |
| $\phi\eta$                      | $0.65 \pm 0.07$   | $0.74 \pm 0.08$     | BES Coll., Phys. Rev. D71 (05) 032003   |
| $\phi\eta'$                     | $0.33 \pm 0.04$   | $0.40 \pm 0.07$     |   |
| $\rho\eta$                      | $0.193 \pm 0.023$ | =                   |   |
| $\rho\eta'$                     | $0.105 \pm 0.018$ | =                   |   |
| $\omega\pi^0$                   | $0.42 \pm 0.06$   | $0.45 \pm 0.05$     | BES Coll., Phys. Rev. D73 (06) 052007   |
| $\phi\pi^0$                     | $< 0.0068$        | $< 0.0064$ C.L. 90% | BES Coll., Phys. Rev. D71 (05) 032003   |

\* MARK III Coll., Phys. Rev. D38 (88) 2695  
 DM2 Coll., Phys. Rev. D41 (90) 1389

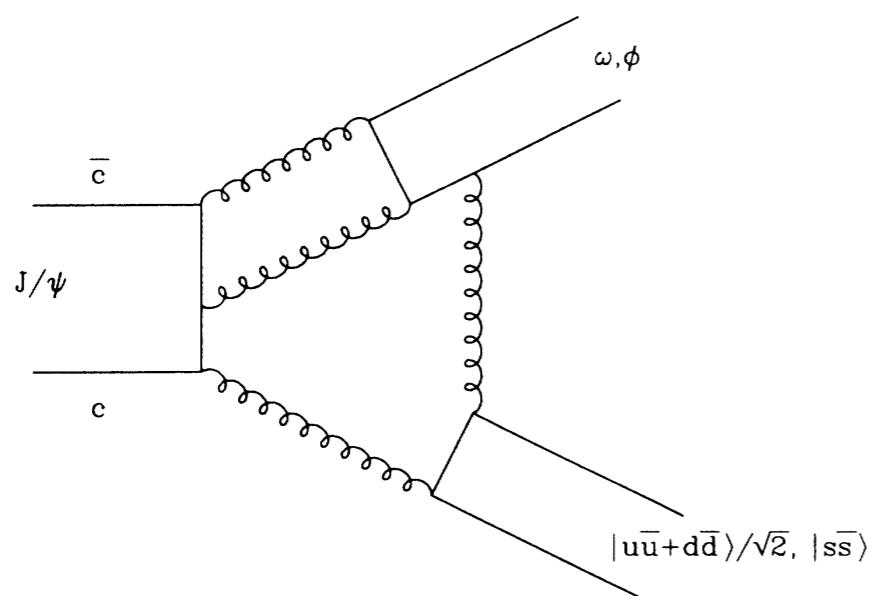


- A model for  $J/\psi \rightarrow VP$  transitions

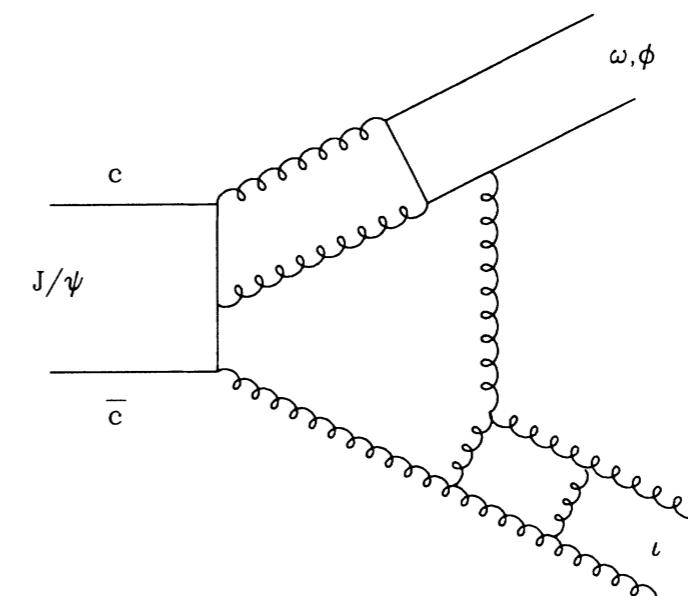
Amplitudes:



strong singly disconnected (SOZI)  $\equiv g$    electromagnetic singly disconnected (eSOZI)  $\equiv e$



strong doubly disconnected (DOZI)  $\equiv rg$



DOZI for  $J/\psi \rightarrow V + \text{Glueball} \equiv r'g$

- A model for  $J/\psi \rightarrow VP$  transitions

Amplitudes:

TABLE VIII. General parametrization of amplitudes for  $J/\psi \rightarrow P + V$ .

| Process  | Amplitude  |
|--|--|
| $\rho^+ \pi^-$ , $\rho^0 \pi^0$ , $\rho^- \pi^+$ | $g + e$  |
| $K^{*+} K^-$ , $K^{*-} K^+$                      | $g(1-s) + e(1+s_e)$  |
| $K^{*0} \bar{K}^0$ , $\bar{K}^{*0} K^0$          | $g(1-s) - e(2-s_e)$  |
| $\omega \eta$                                    | $(g + e)X_\eta + \sqrt{2}rg[\sqrt{2}X_\eta + (1-s_p)Y_\eta] + \sqrt{2}r'gZ_\eta$                         |
| $\omega \eta'$                                   | $(g + e)X_{\eta'} + \sqrt{2}rg[\sqrt{2}X_{\eta'} + (1-s_p)Y_{\eta'}] + \sqrt{2}r'gZ_{\eta'}$             |
| $\phi \eta$                                      | $[g(1-2s) - 2e(1-s_e)]Y_\eta + rg(1-s_v)[\sqrt{2}X_\eta + (1-s_p)Y_\eta] + r'g(1-s_v)Z_\eta$             |
| $\phi \eta'$                                     | $[g(1-2s) - 2e(1-s_e)]Y_{\eta'} + rg(1-s_v)[\sqrt{2}X_{\eta'} + (1-s_p)Y_{\eta'}] + r'g(1-s_v)Z_{\eta'}$ |
| $\rho^0 \eta$                                    | $3eX_\eta$   |
| $\rho^0 \eta'$                                   | $3eX_{\eta'}$  |
| $\omega \pi^0$                                   | $3e$   |
| $\phi \pi^0$                                     | $0$  |

A. Seiden et al., Phys. Rev. D38 (1988) 824

$s$ ,  $s_e$ ,  $s_p$  and  $s_v$  are SU(3)-breaking parameters

Simplifications of our analysis:

- second order SU(3)-breaking contributions  $s_p$  and  $s_v$  are neglected
- $x \equiv 1 - s_e = m/m_s$  with  $m_s/m = 1.24 \pm 0.07$  and  $\phi_v = (3.2 \pm 0.1)^\circ$
- $Z_\eta = 0$  from  $V \rightarrow P\gamma$  and  $P \rightarrow V\gamma$  decays

R. E. and J. Nadal, JHEP 05 (2007) 6

- *Preliminary results*

R. E., work in preparation

a) gluonium not allowed for  $\eta'$    $Z_{\eta'}=0$

i)  $x=1$  and  $\phi_V=0^\circ$    $\chi^2/d.o.f.=3.4/4$  with  $\Phi_P=(40.2\pm2.4)^\circ$

ii)  $x=0.81\pm0.05$  and  $\phi_V=(3.2\pm0.1)^\circ$    $\chi^2/d.o.f.=4.2/4$  with  $\Phi_P=(40.5\pm2.4)^\circ$

with  $s=(29\pm3)\%$  and  $|r|=(37\pm1)\%$  in i)

b) gluonium allowed for  $\eta'$    $Z_{\eta'}\neq0$

i)  $x=1$  and  $\phi_V=0^\circ$    $\chi^2/d.o.f.=1.9/2$  with  $\Phi_P=(45.0\pm4.3)^\circ$  and  $(Z_{\eta'})^2=0.30\pm0.20$

ii) as before   $\chi^2/d.o.f.=3.0/2$  with  $\Phi_P=(44.5\pm4.4)^\circ$  and  $(Z_{\eta'})^2=0.28\pm0.23$

with  $s=(27\pm3)\%$ ,  $|r|=(36\pm8)\%$  and  $|r'|=(12\pm23)\%$  in i)

Remarks:

- the effect of second order SU(3)-breaking contributions  $s_p$  and  $s_v$  is negligible
- the same fits with the pion modes removed are slightly better
- the same fits with the old data are worse,  $\chi^2/d.o.f.=7.3/4$  vs.  $\chi^2/d.o.f.=3.4/4$  for instance

- *Summary and preliminary conclusions*

We have performed an **updated phenomenological analysis** of an accurate and exhaustive set of  $J/\psi \rightarrow VP$  decays with the **purpose** of determining the **quark and gluon content** of the  $\eta$  and  $\eta'$  mesons

- I) The **current experimental data** on  $J/\psi \rightarrow VP$  decays are described in terms of **one mixing angle** in a **consistent way**
- 2) Accepting the **absence** of **gluonium** for the  $\eta'$  meson, the  $\eta$ - $\eta'$  **mixing angle** is found to be  $\Phi_P = (40.2 \pm 2.4)^\circ$  or  $\theta_P = (-14.5 \pm 2.4)^\circ$ , in **agreement** with **recent phenomenological estimates**
- 3) The values found for  $(Z_{\eta'})^2 = 0.30 \pm 0.20$  or  $\phi_{\eta'G} = (33 \pm 15)^\circ$  suggest within the model some **small gluonic component** of the  $\eta'$
- 3) The **inclusion** of the **vector mixing angle** (**not included** in previous analyses) is **irrelevant**
- 4) The **recent values** of  $BR(J/\psi \rightarrow \rho\pi)$  by **BABAR** and **BES Coll.** are **crucial** in order to get a **consistent description** of data

- *Euler angles*

In presence of gluonium,

$$\begin{array}{lcl}
 |\eta\rangle & = & X_\eta|\eta_q\rangle + Y_\eta|\eta_s\rangle + Z_\eta|G\rangle \\
 \text{glueball-like state} \\
 \eta(1440)? & \searrow & \\
 |\eta'\rangle & = & X_{\eta'}|\eta_q\rangle + Y_{\eta'}|\eta_s\rangle + Z_{\eta'}|G\rangle \\
 |\iota\rangle & = & X_\iota|\eta_q\rangle + Y_\iota|\eta_s\rangle + Z_\iota|G\rangle
 \end{array}$$

Normalization:

$$X_\eta^2 + Y_\eta^2 + Z_\eta^2 = 1$$

$$X_{\eta'}^2 + Y_{\eta'}^2 + Z_{\eta'}^2 = 1$$

$$X_\iota^2 + Y_\iota^2 + Z_\iota^2 = 1$$

Orthogonality:

$$X_\eta X_{\eta'} + Y_\eta Y_{\eta'} + Z_\eta Z_{\eta'} = 0$$

$$X_\eta X_\iota + Y_\eta Y_\iota + Z_\eta Z_\iota = 0$$

$$X_{\eta'} X_\iota + Y_{\eta'} Y_\iota + Z_{\eta'} Z_\iota = 0$$



3 independent parameters:  $\phi_P$ ,  $\phi_{\eta G}$  and  $\phi_{\eta' G}$

$$\begin{pmatrix} \eta \\ \eta' \\ \iota \end{pmatrix} = \begin{pmatrix} c\phi_{\eta\eta'}c\phi_{\eta G} & -s\phi_{\eta\eta'}c\phi_{\eta G} & -s\phi_{\eta G} \\ s\phi_{\eta\eta'}c\phi_{\eta' G} - c\phi_{\eta\eta'}s\phi_{\eta' G}s\phi_{\eta G} & c\phi_{\eta\eta'}c\phi_{\eta' G} + s\phi_{\eta\eta'}s\phi_{\eta' G}s\phi_{\eta G} & -s\phi_{\eta' G}c\phi_{\eta G} \\ s\phi_{\eta\eta'}s\phi_{\eta' G} + c\phi_{\eta\eta'}c\phi_{\eta' G}s\phi_{\eta G} & c\phi_{\eta\eta'}s\phi_{\eta' G} - s\phi_{\eta\eta'}c\phi_{\eta' G}s\phi_{\eta G} & c\phi_{\eta' G}c\phi_{\eta G} \end{pmatrix} \begin{pmatrix} \eta_q \\ \eta_s \\ G \end{pmatrix}$$

- *Euler angles*

$$X_\eta = \cos \phi_P \cos \phi_{\eta G} , \quad X_{\eta'} = \sin \phi_P \cos \phi_{\eta' G} - \cos \phi_P \sin \phi_{\eta G} \sin \phi_{\eta' G} ,$$

$$Y_\eta = - \sin \phi_P \cos \phi_{\eta G} , \quad Y_{\eta'} = \cos \phi_P \cos \phi_{\eta' G} + \sin \phi_P \sin \phi_{\eta G} \sin \phi_{\eta' G} ,$$

$$Z_\eta = - \sin \phi_{\eta G} , \quad Z_{\eta'} = - \sin \phi_{\eta' G} \cos \phi_{\eta G} .$$

In the limit  $\phi_{\eta G}=0$ :

$$X_\eta = \cos \phi_P ,$$

$$Y_\eta = - \sin \phi_P ,$$

$$Z_\eta = 0 ,$$

$$X_{\eta'} = \sin \phi_P \cos \phi_{\eta' G} ,$$

$$Y_{\eta'} = \cos \phi_P \cos \phi_{\eta' G} ,$$

$$Z_{\eta'} = - \sin \phi_{\eta' G} .$$