

# **WG4:**

# **Slow Muon Physics**

Yoshitaka Kuno

Osaka University

June 22nd, 2005

NuFACT05, Frascati, Italy

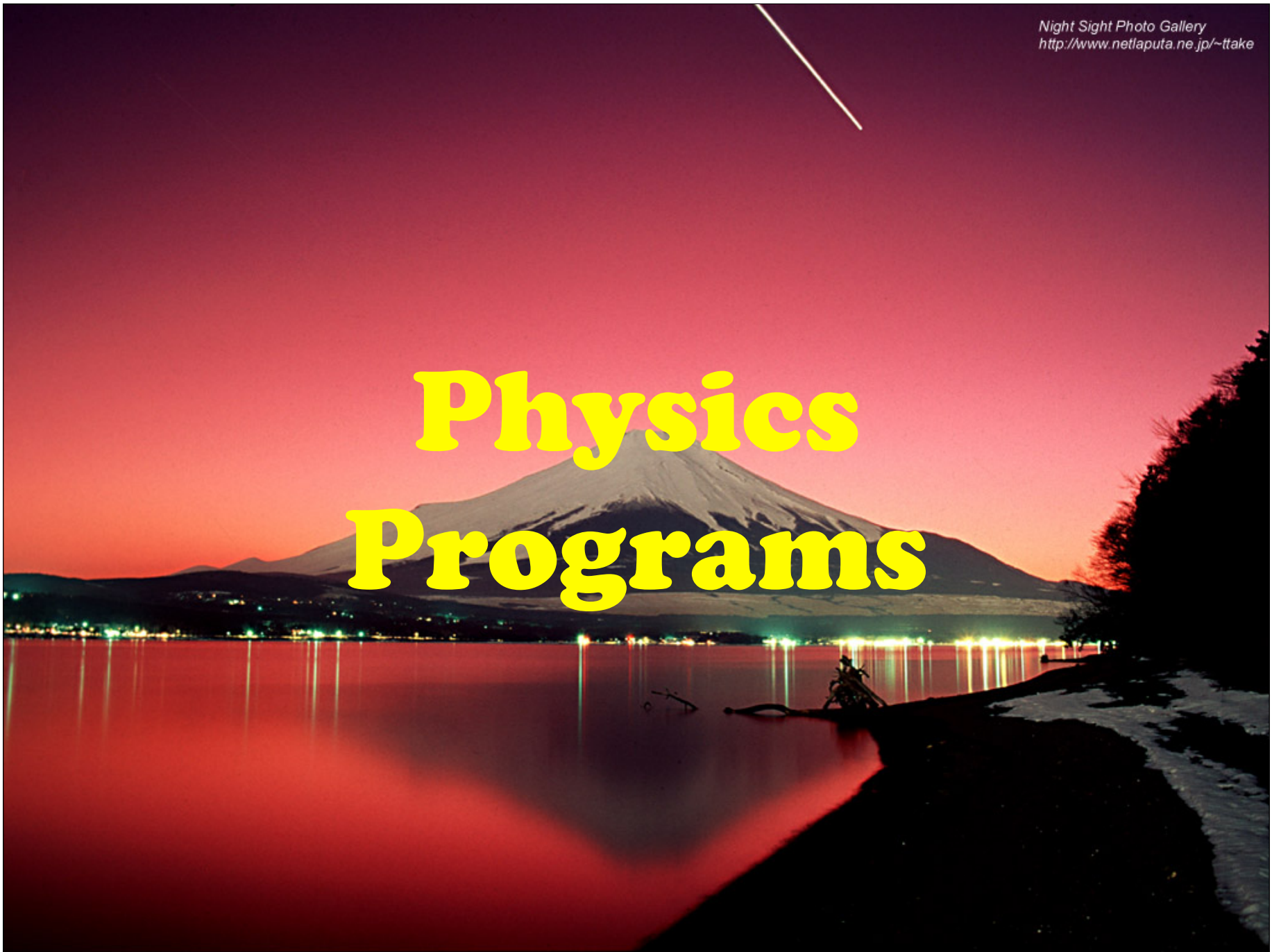
# WG4 : Slow Muon Physics

## \* Outline

- Physics Programs
- Muon Trio
  - (Particle) Physics Motivation
  - Experimental
- Muon Beams
- Other topics

WG4: Conveners  
Lee Roberts (Boston)  
Marco Grassi (Pisa)  
AKira Sato (Osaka)

# Physics Programs



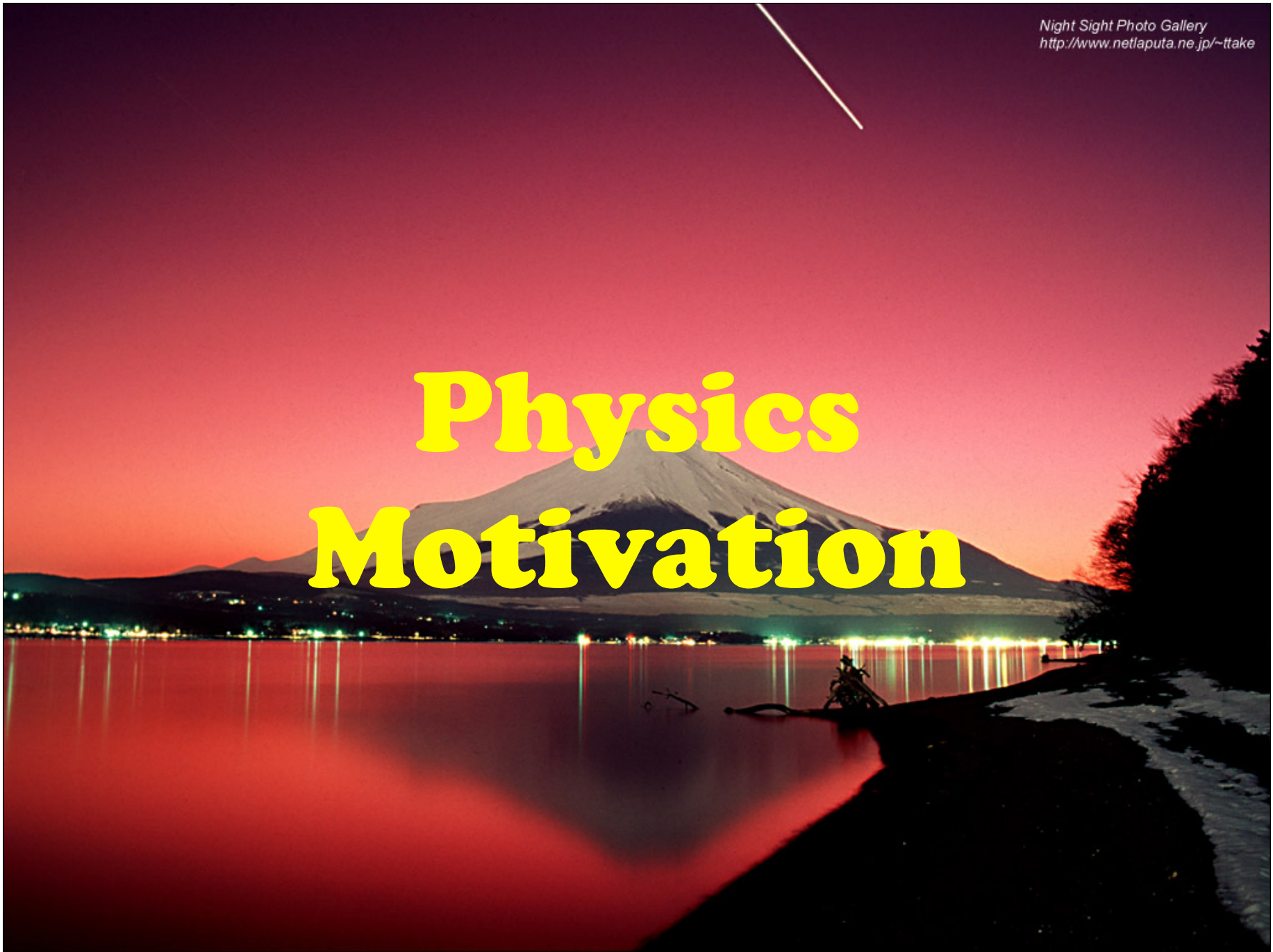
# Slow Muon Physics

Categories	Topics	Comments	Beams
Precision measurements	Muon lifetime	$G_F$	pulsed
	Muon $g-2$	New physics search	pulsed
Rare Muon processes	Muon EDM	SM suppressed	pulsed
	Charged lepton mixing	SM forbidden	pulsed / DC
Applications	Catalyzed fusion	Break even ?	pulsed
	Materials science		DC

# Slow Muon Physics

Category	Topic	Comments	Beams
<b>Muon Trio</b>		$G_F$	pulsed
measurements	Muon $g-2$	New physics search	pulsed
Rare Muon processes	Muon EDM	SM suppressed	pulsed
	Charged lepton mixing	SM forbidden	pulsed / DC
Applications	Catalyzed fusion	Break even ?	pulsed
	Materials science		DC

# Physics Motivation



# Future Extrapolation

Muon  $g-2$

$$0.7 \text{ ppm} \rightarrow 0.05 \text{ ppm}$$

Muon LFV

$$B(\mu \rightarrow e \gamma) < 10^{-18}$$

Muon EDM

$$d_{\mu} < 10^{-19} e \cdot \text{cm} \rightarrow d_{\mu} < 10^{-24} e \cdot \text{cm}$$

# The Physics Case

... following the discussions at the FNAL proton driver workshop (a la Lee Roberts)

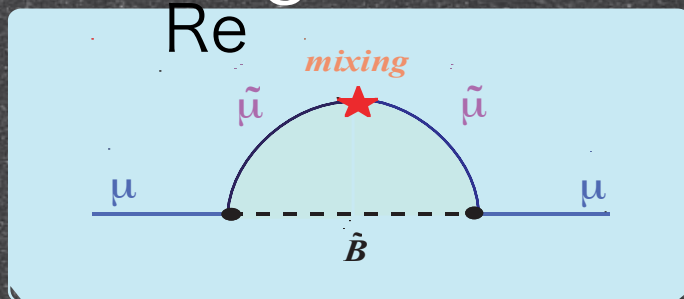
Scenario 1 :  
LHC finds SUSY

All three in the trio have significant contributions from SUSY.



# The Muon Trio

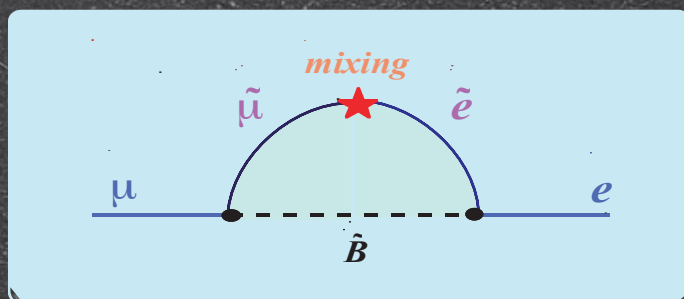
Muon  $g-2$



in SUSY case

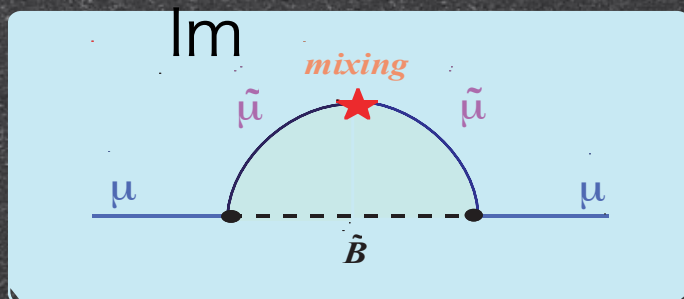
Slepton mixing matrix

Muon LFV



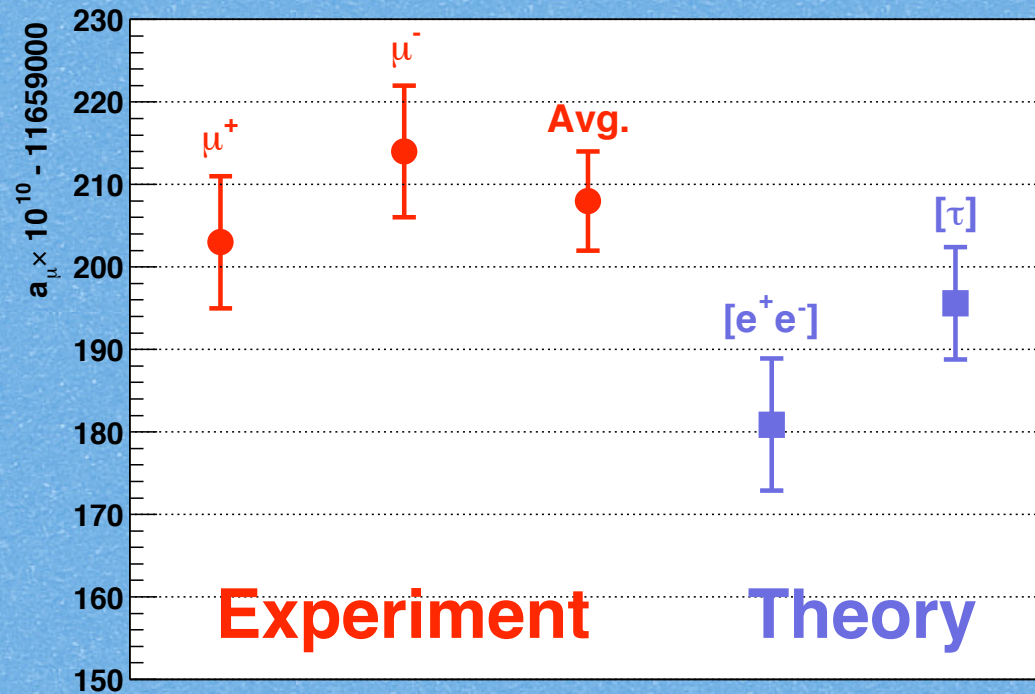
$$\begin{pmatrix} m_{\tilde{e}\tilde{e}}^2 & \Delta m_{\tilde{e}\tilde{\mu}}^2 & \Delta m_{\tilde{e}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\mu}\tilde{e}}^2 & m_{\tilde{\mu}\tilde{\mu}}^2 & \Delta m_{\tilde{\mu}\tilde{\tau}}^2 \\ \Delta m_{\tilde{\tau}\tilde{e}}^2 & \Delta m_{\tilde{\tau}\tilde{\mu}}^2 & m_{\tilde{\tau}\tilde{\tau}}^2 \end{pmatrix}$$

Muon EDM



Hints for SUSY breaking

# BNL Muon g-2 Result



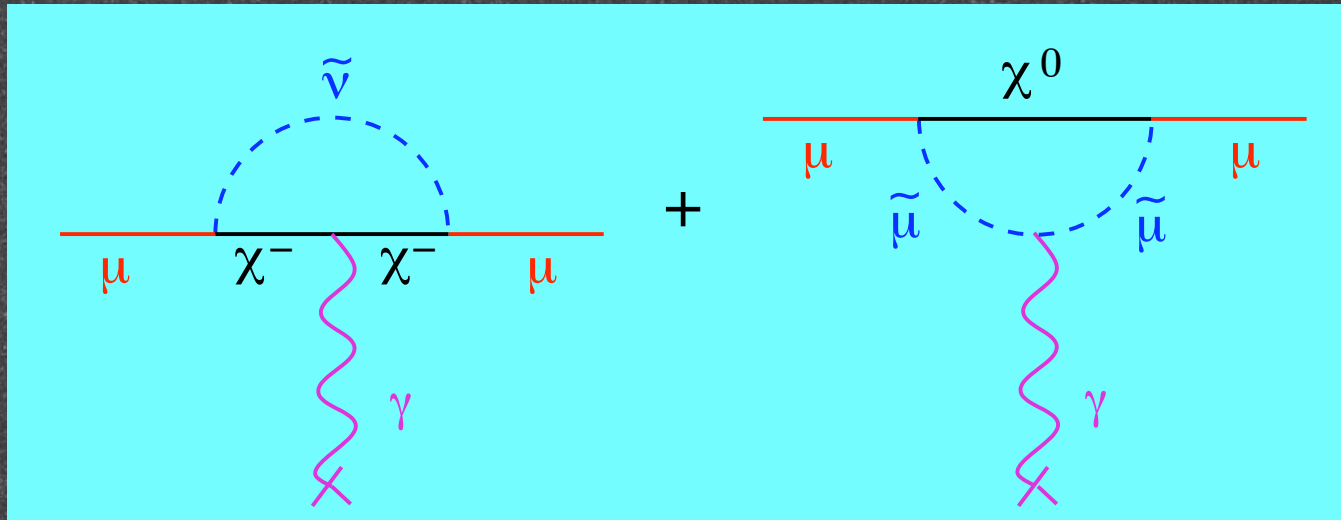
$$a_\mu = 11659208(6)$$

$\mu^\pm$  combined

$$\Delta a_\mu(ee) = (23.9 \pm 9.9) \times 10^{-10} \quad 2.7 \text{ s.d.}$$

$$\Delta a_\mu(\tau) = (7.6 \pm 8.9) \times 10^{-10} \quad 0.9 \text{ s.d.}$$

# g-2 sensitivity to SUSY



$$\begin{aligned}
 a_{\mu}(SUSY) &\sim \frac{\alpha(M_Z)}{8\pi \sin^2 \theta_W} \cdot \frac{m_{\mu}^2}{\tilde{m}^2} \cdot \tan \beta \left(1 - \frac{4\alpha}{\pi} \ln \frac{\tilde{m}}{m_{\mu}}\right) \\
 &\sim 13 \times 10^{-10} \tan \beta \left(\frac{100 \text{ GeV}}{\tilde{m}_{\mu}}\right)^2
 \end{aligned}$$

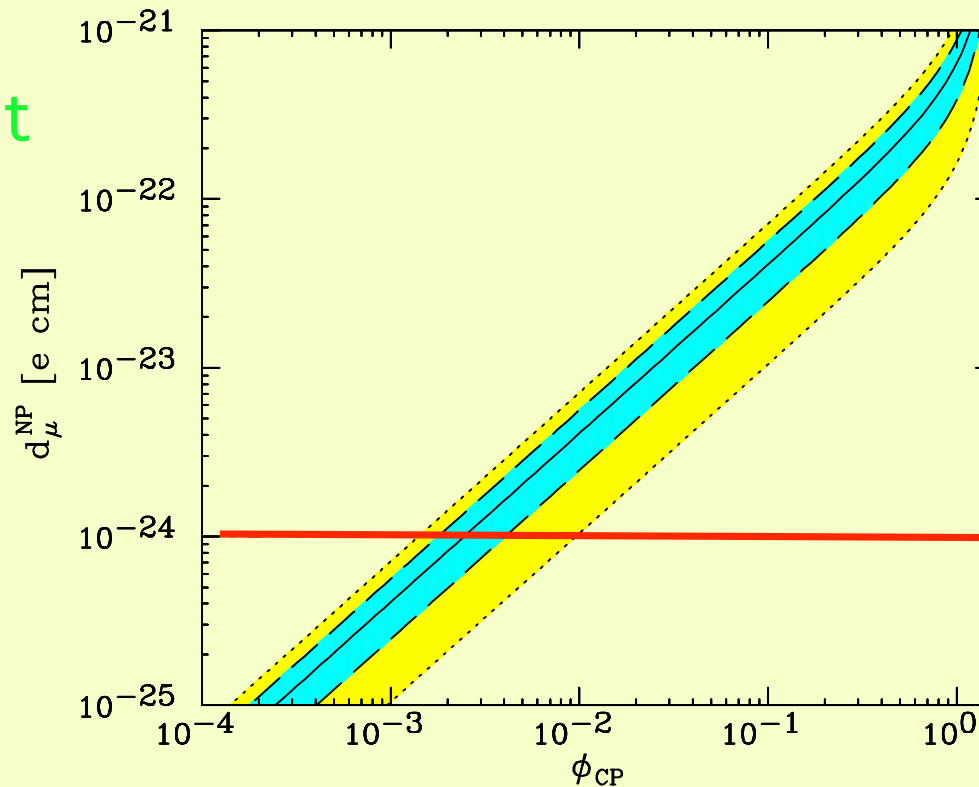
Significant for large  $\tan \beta$  and  $\tilde{m}$  in the LHC range

# Muon EDM

## SUSY contribution to muon EDM

Muon (g-2)  
and EDM might  
be related.

hints for  
leptogenesis

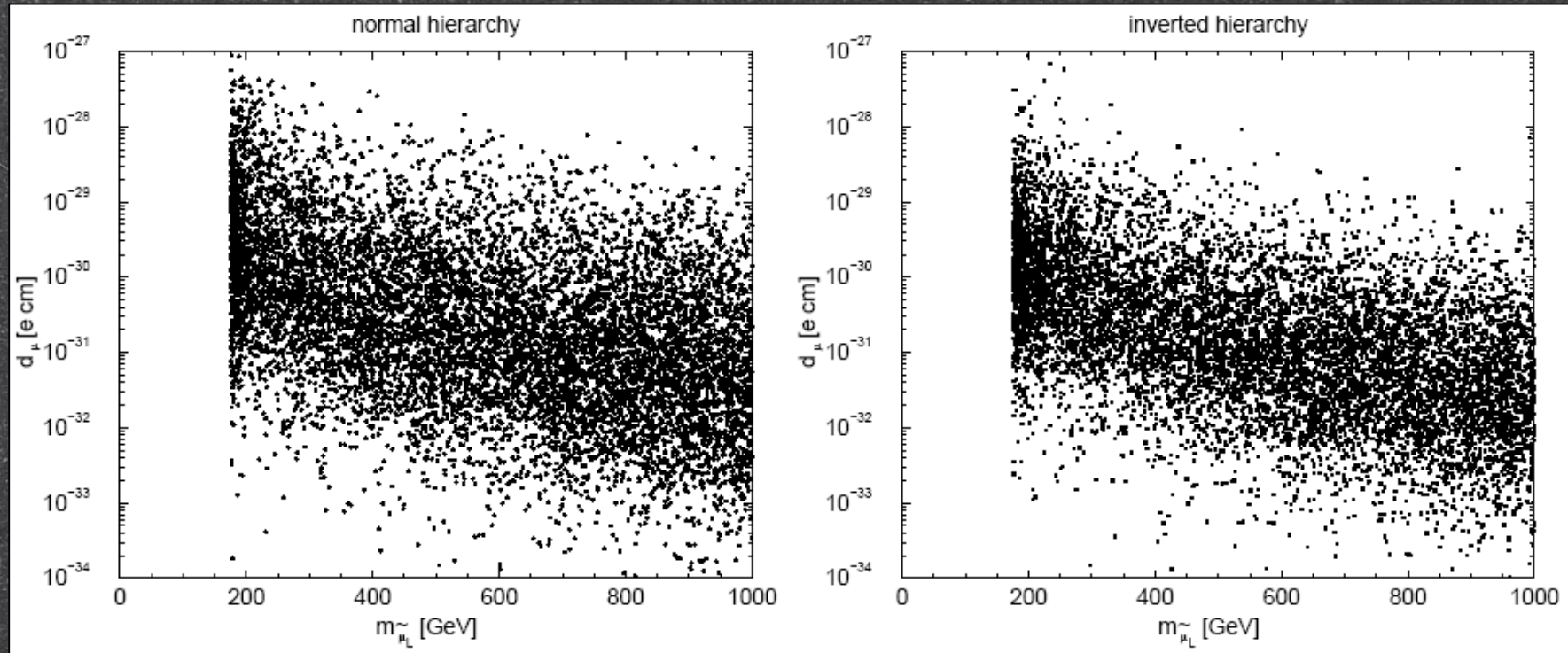


$$d_{\mu}^{NP} \approx 3 \times 10^{-22} \left( \frac{a_{\mu}^{NP}}{3 \times 10^{-9}} \right) \tan \phi_{CP} \text{ e} \cdot \text{cm}, \quad a_{NP} = a_{\mu}^{exp} - a_{\mu}^{SM} \approx 3(1) \times 10^{-9}$$

Feng, Matchev, Shadmi, NP B613, 366(2001)

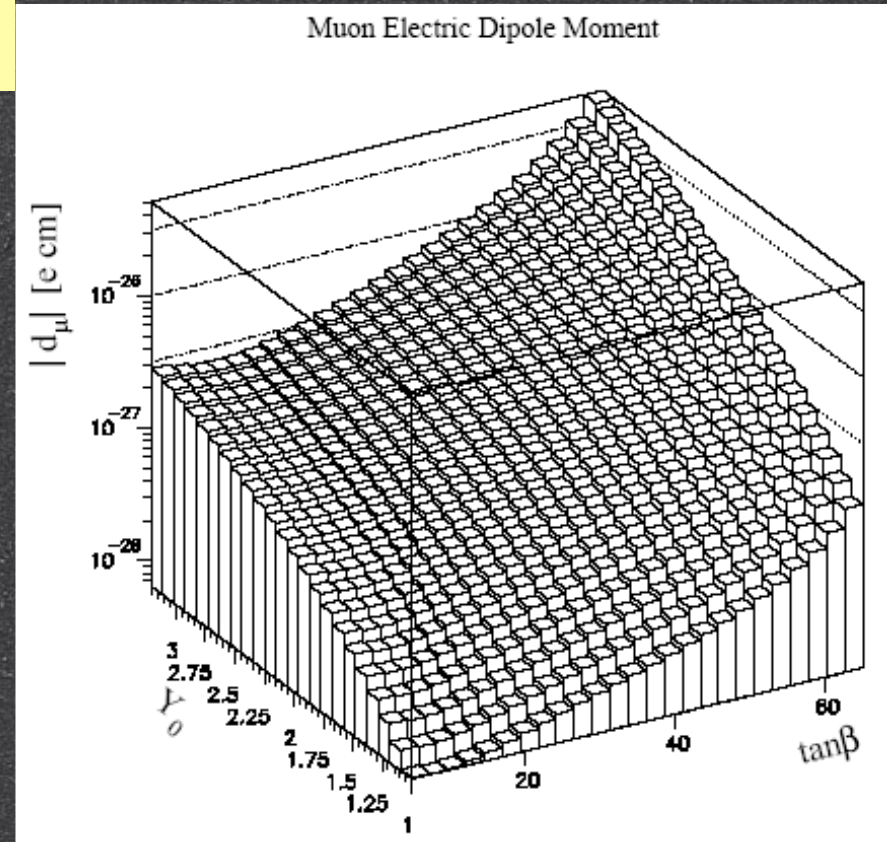
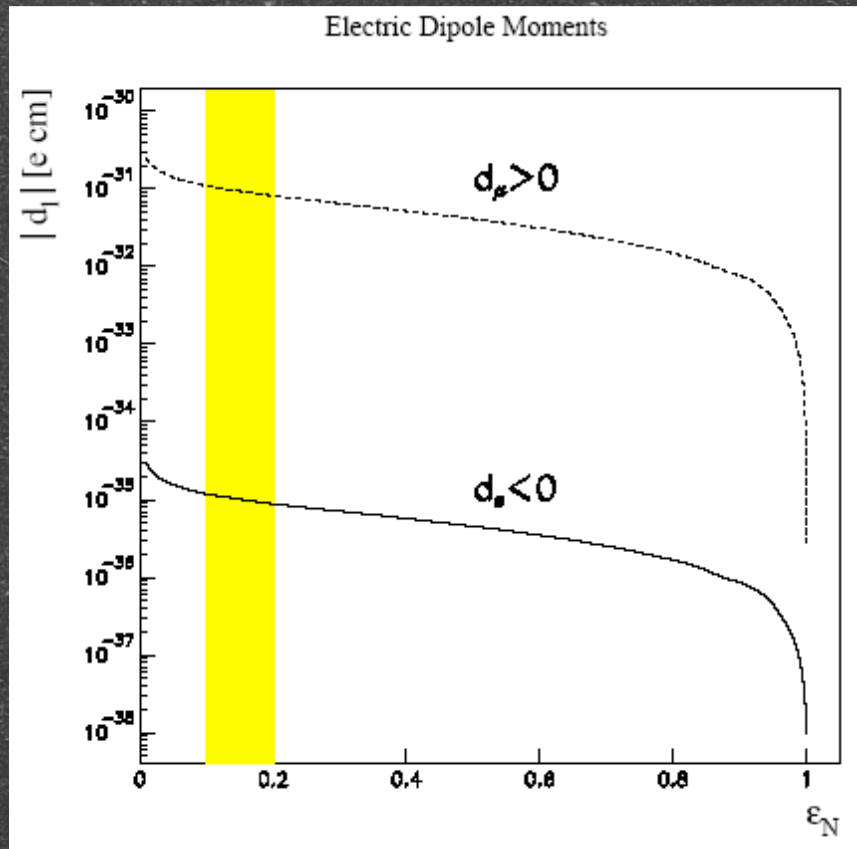
# Muon EDM from SUSY

In minimal supersymmetric seesaw models consistent with neutrino oscillation data : assuming  $CP$  violation in soft supersymmetry-breaking parameters induced neutrino Yukawa couplings.



# SUSY to Muon EDM

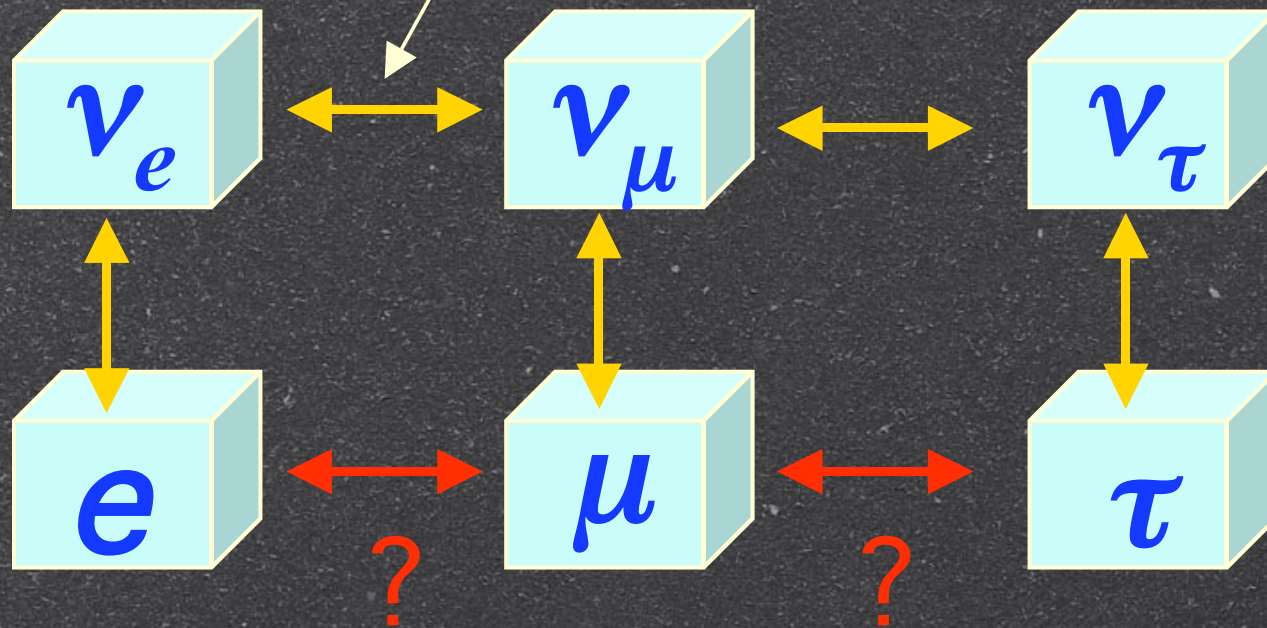
muon EDM may be enhanced by more than  $m(\mu)/m(e)$



muon EDM greatly enhanced when heavy neutrino non-degenerate

# Charged Lepton Mixing (CLM)

Neutrino Mixing

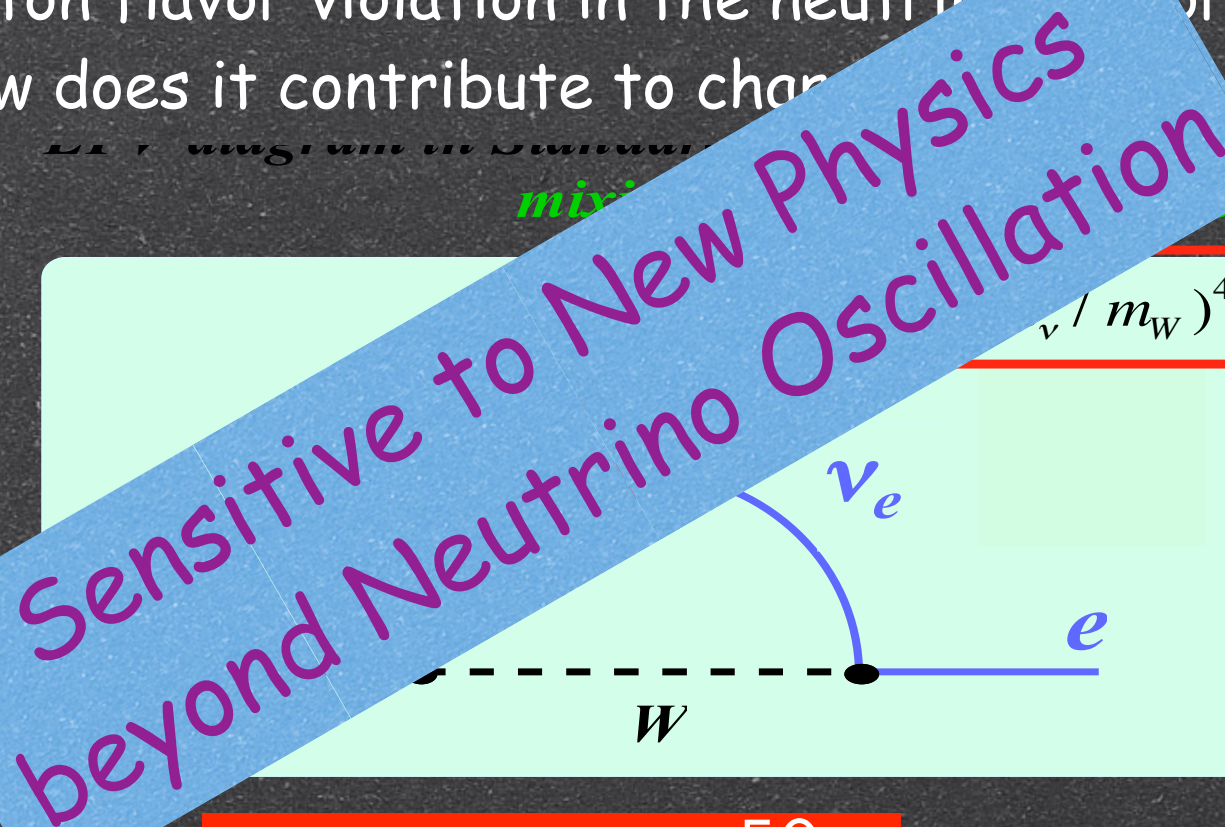


Charged Lepton Mixing

not discovered

# Neutrino Mixing for CLM

- Observed neutrino oscillation (mixing) implies lepton flavor violation in the neutrino sector. How does it contribute to charge lepton number violation?



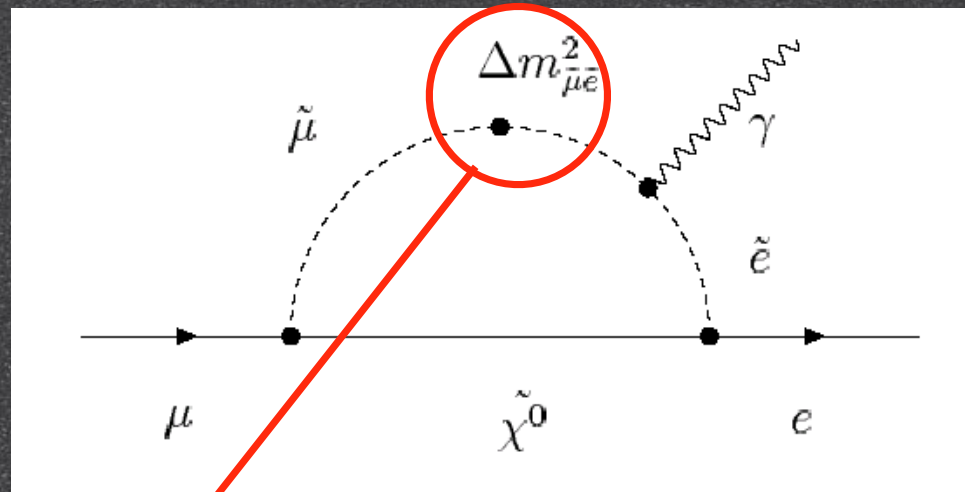
Sensitive to New Physics beyond Neutrino Oscillation

Very Small ( $10^{-50}$ )



# SUSY for LFV

$$\mu^+ \rightarrow e^+ \gamma$$



$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{11}^2 & m_{12}^2 & m_{13}^2 \\ m_{21}^2 & m_{22}^2 & m_{23}^2 \\ m_{31}^2 & m_{32}^2 & m_{33}^2 \end{pmatrix}$$

In SUSY, LFV processes are induced by the off-diagonal terms in the slepton mass matrix. In MSSM, no off-diagonal terms exist @Planck, and need more. **How?**

# How Sleptons Mixed ?

SUSY-GUT

$$(m_{\tilde{l}}^2)_{ij} = m_0^2 \delta_{ij} \quad @ M_{\text{planck}}$$

GUT Yukawa interaction

SUSY Seesaw Model

Neutrino Yukawa interaction

$$(\Delta m_{\tilde{l}}^2)_{ij} \neq 0$$

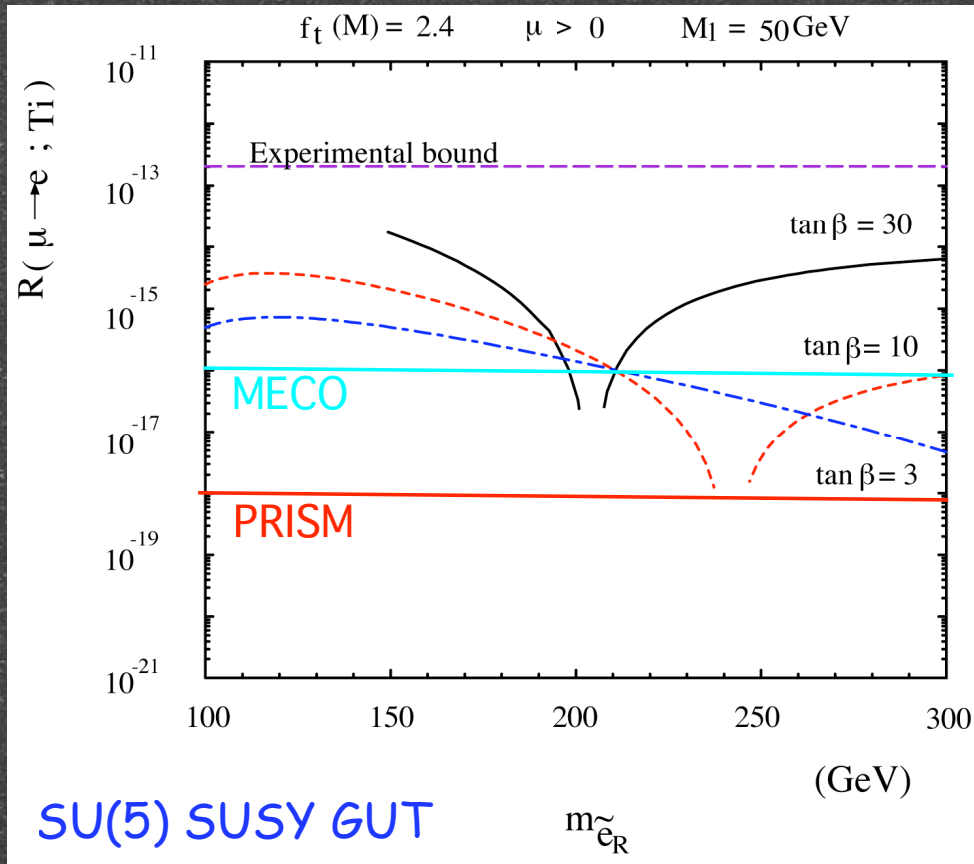
$$(m_{\tilde{L}}^2)_{21} \sim \frac{3m_0^2 + A_0^2}{8\pi^2} h_t^2 V_{td} V_{ts} \ln \frac{M_{GUT}}{M_{R_s}}$$

CKM matrix

$$(m_{\tilde{L}}^2)_{21} \sim \frac{3m_0^2 + A_0^2}{8\pi^2} h_i^2 U_{i1} U_{i2} \ln \frac{M_{GUT}}{M_{R_s}}$$

Neutrino oscillation

# SUSY-GUT



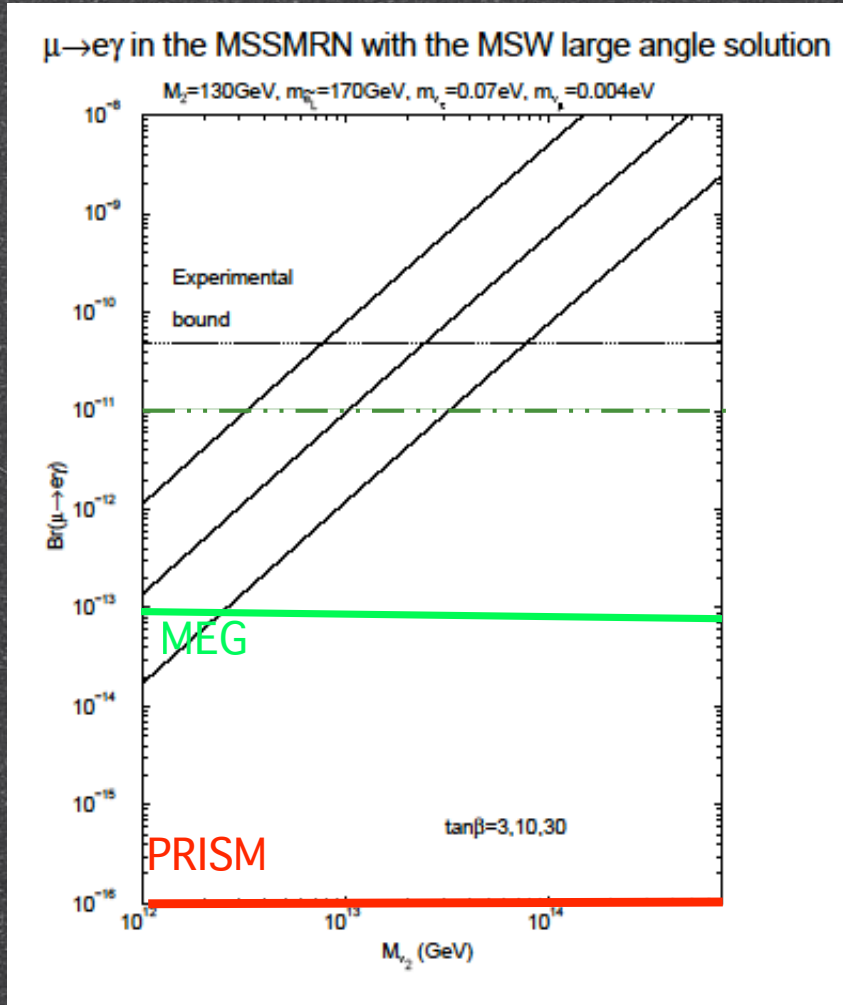
right-handed slepton mass

Slepton mixing is induced through radiative correction from GUT (where quarks and leptons are in the same multiplet) to weak scale.

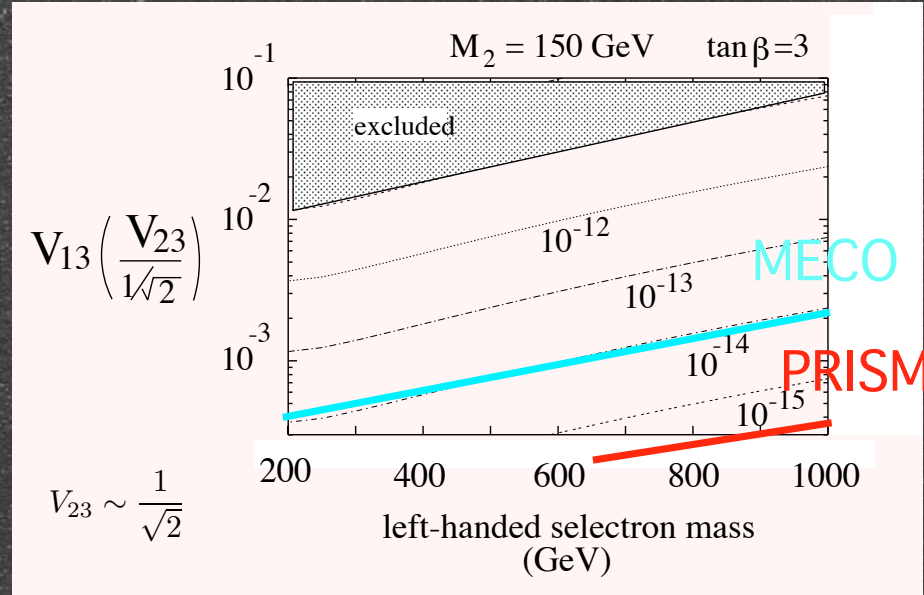
- SUSY SU(5) predictions  
 $BR(\mu \rightarrow e\gamma) \approx 10^{-14} \div 10^{-13}$
- SUSY SO(10) predictions  
 $BR_{SO(10)} \approx 100 BR_{SU(5)}$

Predictions are just a few orders of magnitude smaller than the present limit. Future experiments might cover.

# SUSY Seesaw Model



right-handed neutrino mass



Through SUSY, only way to access heavy right-handed neutrinos in seesaw models.

# CLM : SUSY after LHC

If LHC finds SUSY

- ✓ Search for charged lepton mixing becomes more important, with less risk
- ✓ Search for charged lepton mixing is sensitive to SUSY-GUT and/or SUSY-Seesaw (not just MSSM).

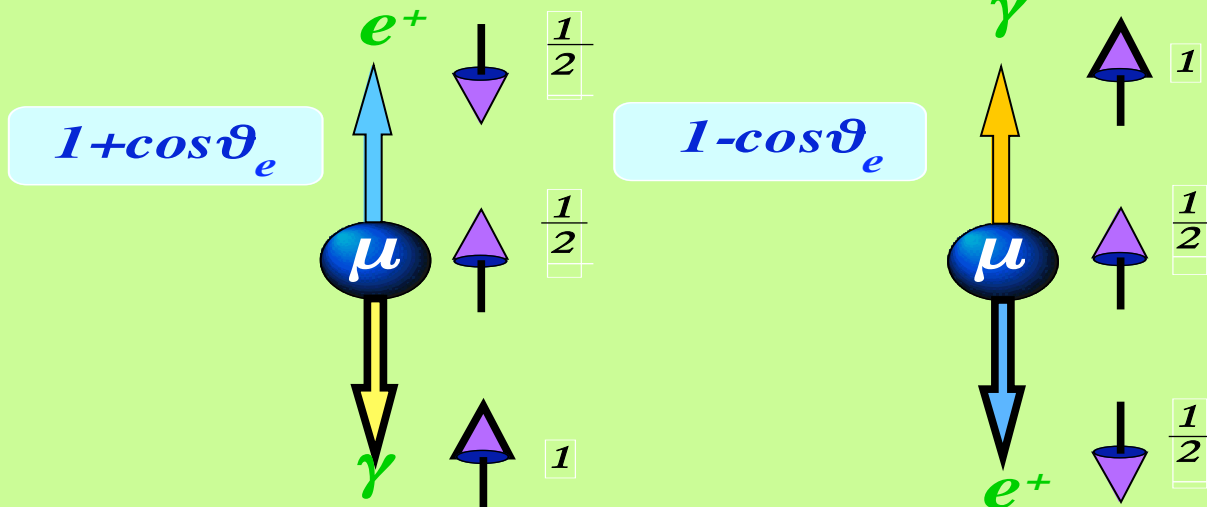


Is this only way to study Seesaw ?

**after observation** **Polarized  $\mu \rightarrow e\gamma$**

*Left handed  $e^+$*

*Right handed  $e^+$*



*useful to distinguish different theoretical models*

*SU(5) SUSY-GUT*

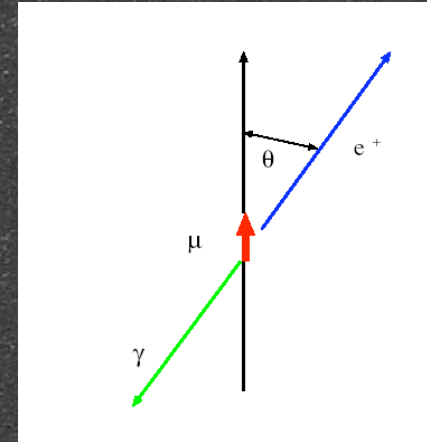
*non-unified SUSY  
with heavy neutrino*

*Left-right symmetric model*

*SO(10) SUSY-GUT*

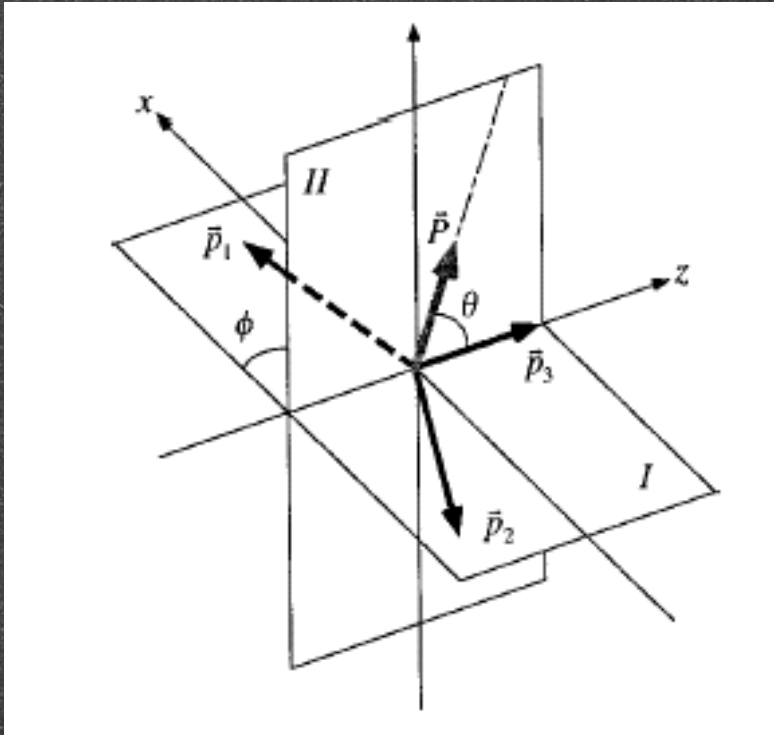
*Y.Kuno and Y. Okada, Physical Review Letters 77 (1996) 434*

*Y.Kuno, A. Maki and Y. Okada, Physical Reviews D55 (1997) R2517-2520*



P-odd  
asymmetry  
reflects  
whether right  
or left-handed  
slepton have  
flavor mixing,

# after observation **T-odd (CPV) in CLM**



Two P-odd and one T-odd asymmetry

$$\vec{P}_\mu \cdot (\vec{p}_{e^+} \times \vec{p}_{e^-})$$

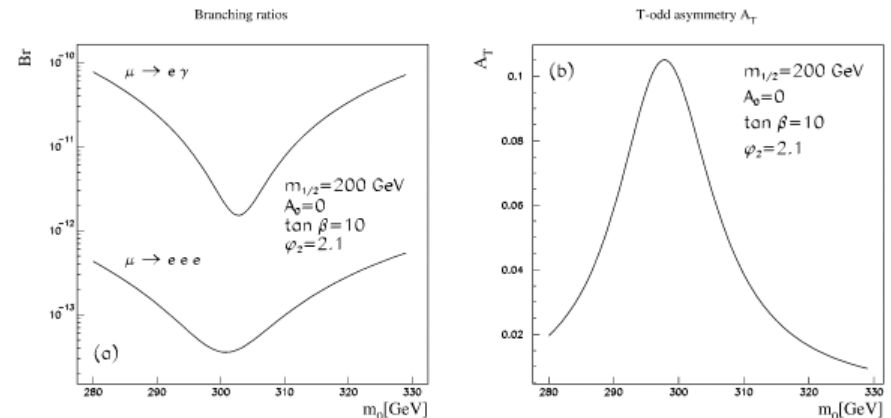
P and T-odd asymmetries in SUSY GUT models

	SU (5)	SO (10)
$A_{\mu \rightarrow e\gamma}$	+100%	-100% - +100%
$A_{P_1}$	-30% - +40 %	$\simeq -A_{\mu \rightarrow e\gamma}/10$
$A_{P_2}$	-20% - +20 %	$\simeq -A_{\mu \rightarrow e\gamma}/6$
$ A_T $	$\lesssim 15\%$	$\lesssim 0.01\%$

Y.Okada, K.Okumura and Y.Shimizu, 2000

Y.Okada,K.Okumura,and Y.Shimizu, 2000

T-odd asymmetry in the SUSY seesaw model



Leptogenesis

J.Ellis,J.Hisano,S.Lola, and M.Raidal, 2001

# The Physics Case

Scenario 2 :  
LHC not find SUSY

Either no SUSY or heavy SUSY ?

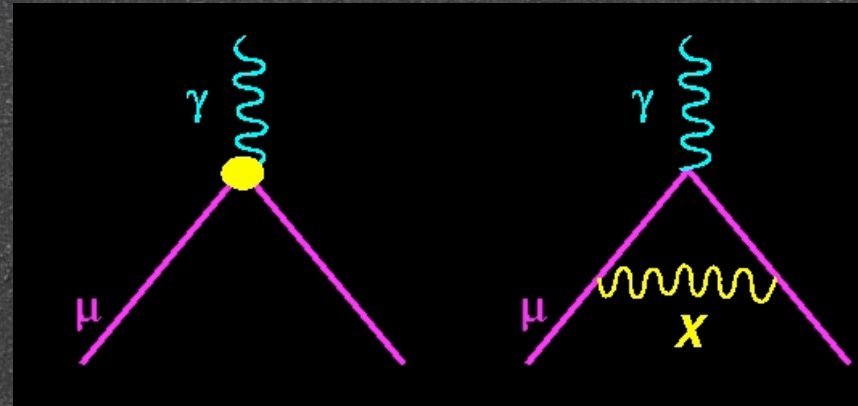
High intensity frontier (precision measurements and searches for rare process) comes to the forefront, since it is sensitive to heavier mass scale.



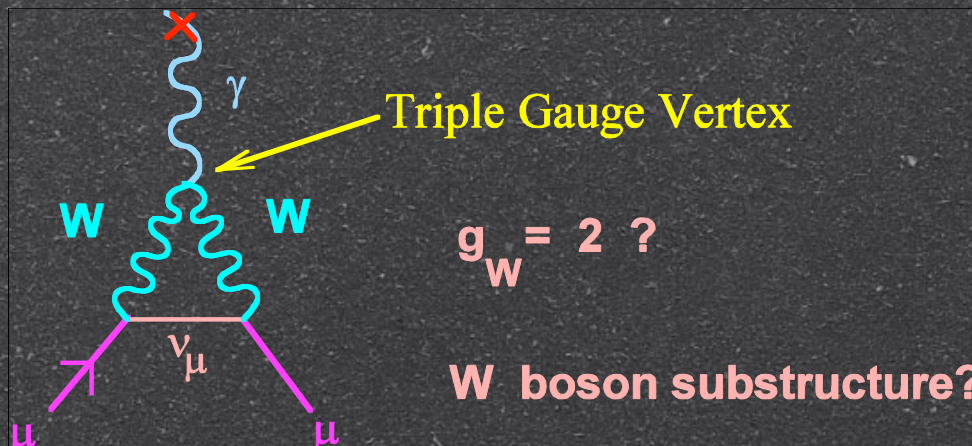
# g-2 sensitivity to NP

Muon substructure

$$\delta a_\mu(\Lambda_\mu) \simeq \frac{m_\mu^2}{\Lambda_\mu^2}$$



Anomalous  $W\gamma\gamma$  Couplings

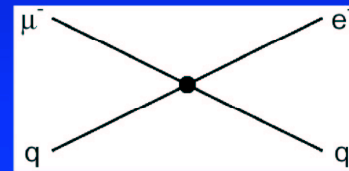
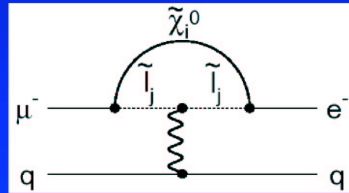


# CLM Models beyond SM

## Sensitivity to Different Muon Conversion Mechanisms



Supersymmetry  
Predictions at  $10^{-15}$

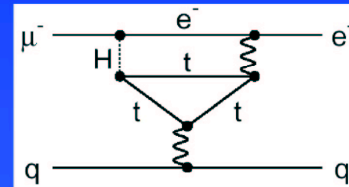
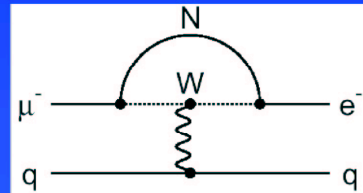


Compositeness

$$\Lambda_c = 3000 \text{ TeV}$$

Heavy Neutrinos

$$|U_{\mu N}^* U_{eN}|^2 = 8 \times 10^{-13}$$

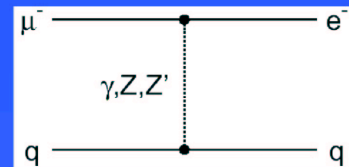
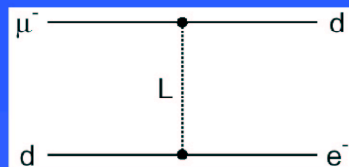


Second Higgs doublet

$$g_{H_{\mu e}} = 10^{-4} \times g_{H_{\mu\mu}}$$

Leptoquarks

$$M_L = 3000 (\lambda_{\mu d} \lambda_{ed})^{1/2} \text{ TeV}/c^2$$



Heavy  $Z'$ ,  
Anomalous  $Z$   
coupling

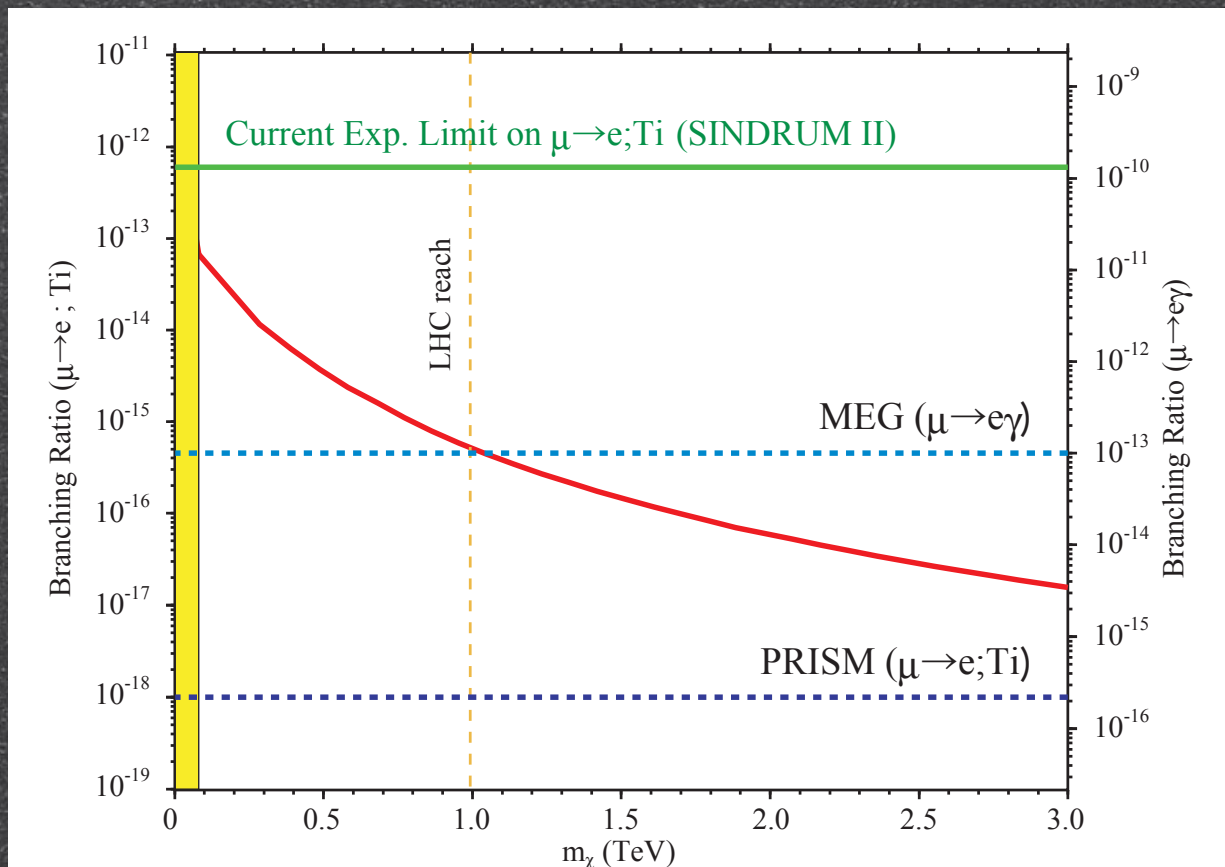
$$M_{Z'} = 3000 \text{ TeV}/c^2$$

$$B(Z \rightarrow \mu e) < 10^{-17}$$

After W. Marciano

# CLM : SUSY beyond LHC

If LHC not finds SUSY



from A.Masiero et al.

... if  
sufficient  
sensitivity is  
achieved.



# Experimental



# Muon EDM

$$\vec{\omega} = -\frac{e}{m} \left[ a\vec{B} + \left( \frac{1}{\gamma^2 - 1} - a \right) \frac{\vec{\beta} \times \vec{E}}{c} + \frac{\eta}{2} \left( \frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right) \right]$$

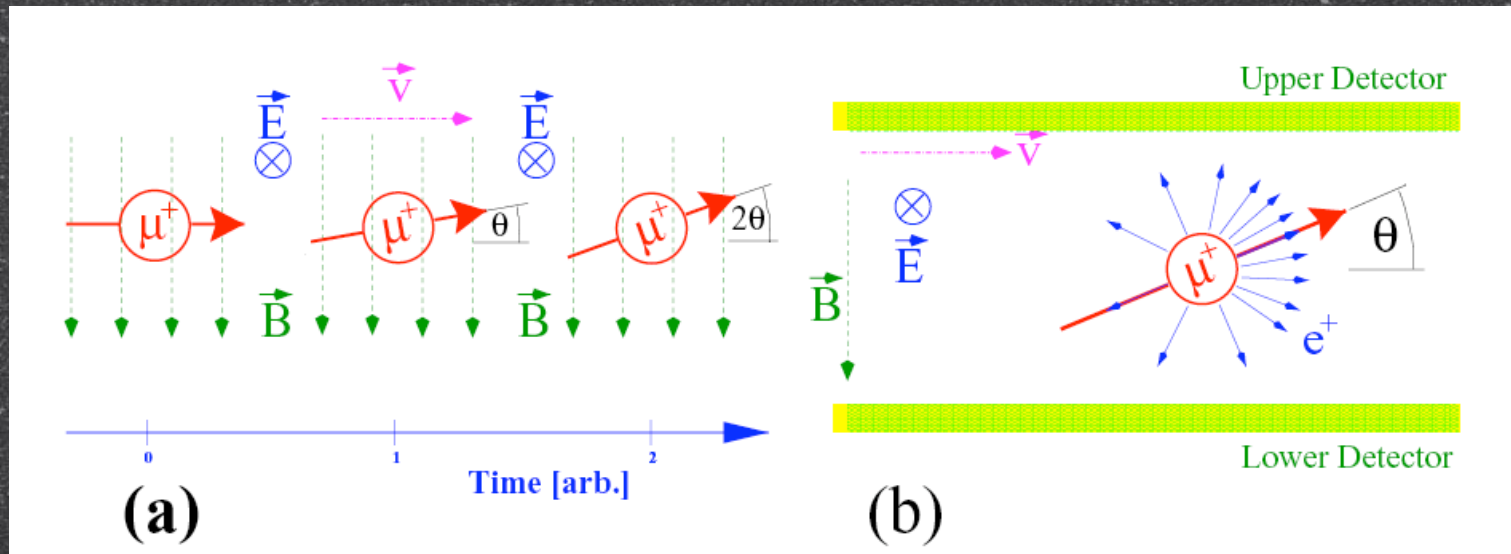
$$= 0$$

Cancellation E field

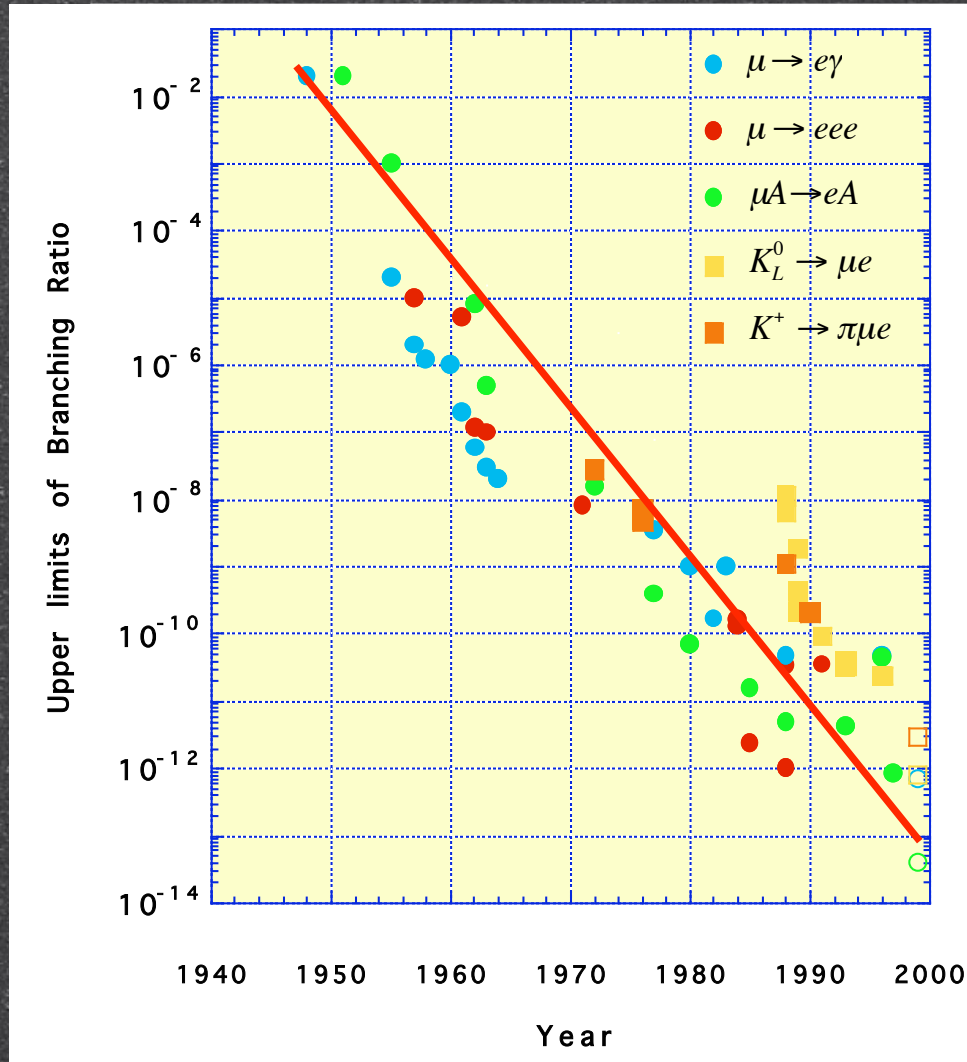
$$E = \frac{aBc(\gamma^2 - 1)}{\beta}$$

E field for EDM rotation

$$E = Bc\beta$$



# History of LFV Searches



Lepton Flavor Violation  
(LFV)

No (charged) LFV  
in the Standard  
Model

Upper limits improved  
by two orders of  
magnitude per decade.

# Why the Muon for CLM ?

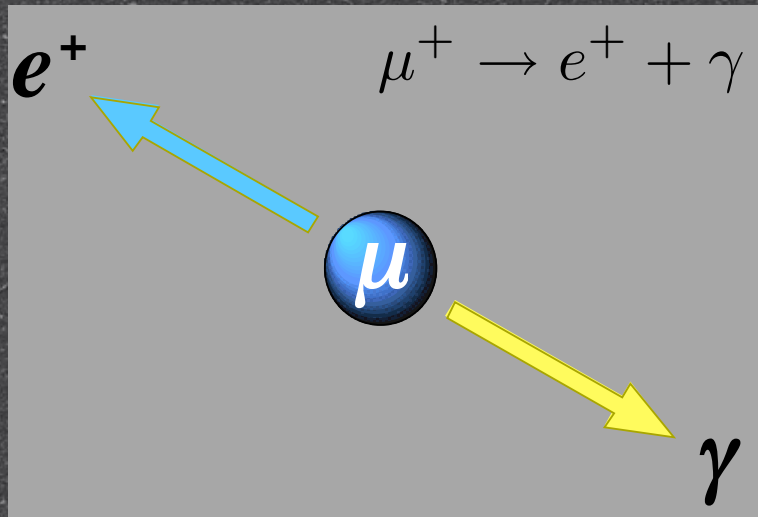
- CLM Sensitivity in the **muon** will be the highest over the other systems because of enormous beam intensity ( $\sim 10^{12}$ /sec) thanks to R&D studies of **neutrino factory front-end**.
- The **muon** provides a clean test ground, on the contrast to hadrons where QCD corrections needed introduces sensitivity limits,

# Upper Limits for CLM

Process	Current	Future
$\mu^+ \rightarrow e^+ \gamma$	$1.2 \times 10^{-11}$	$<10^{-13}$ (MEG)
$\mu^+ \rightarrow e^+ e^+ e^-$	$1.0 \times 10^{-12}$	
$\mu^- A \rightarrow e^- A$ (Ti)	$6.1 \times 10^{-13}$	$<10^{-18}$ (PRISM)
$\mu^- A \rightarrow e^- A$ (Al)		$<10^{-16}$ (MECO)
$\tau \rightarrow \mu \gamma$	$3.2 \times 10^{-7}$	
$\tau \rightarrow lll$	$1.4 - 3.1 \times 10^{-7}$	
$G_{Mu\bar{M}u}/G_F$	$3 \times 10^{-3}$	$\Delta L_f = 2$



# $\mu \rightarrow e\gamma$ & $\mu$ -e conversion



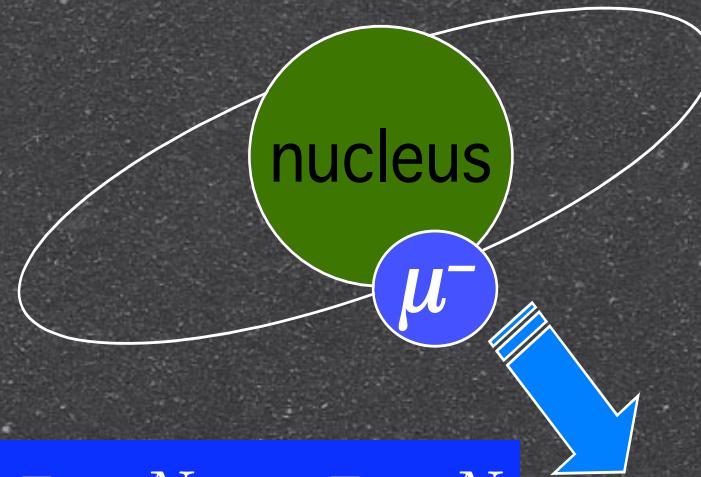
Signature

$$E_e = E_\gamma = m_\mu/2$$

back-to-back, same time

Background

- (1) radiative decay
- (2) accidentals



Signature:

$$E_e = m_\mu - B_\mu$$

monoenergetic electron

Background:

- (1) bound muon decay
- (2) radiative pion/muon capture
- (3) cosmic rays, etc.

# Photon-mediated SUSY LFV

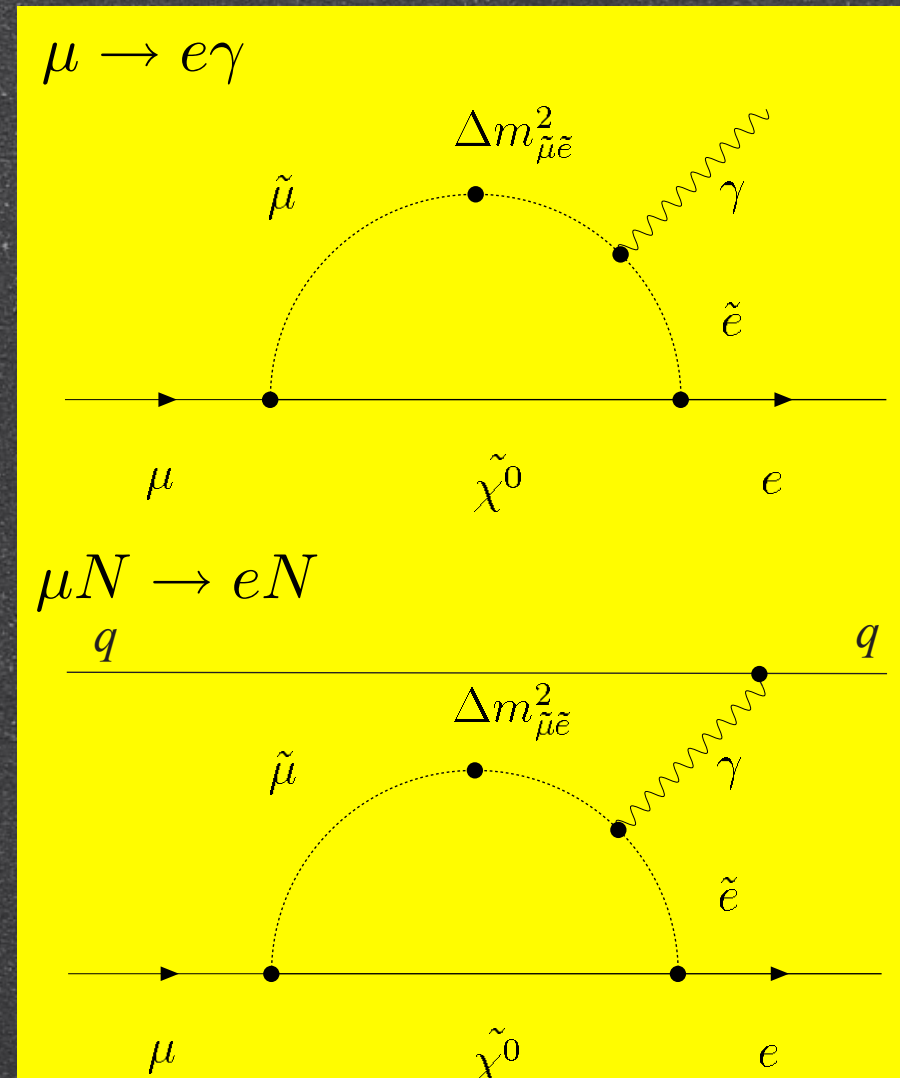
$\mu - e$  conversion vs.  
 $\mu \rightarrow e\gamma$

If photon-mediated,

$$\frac{B(\mu N \rightarrow e N)}{B(\mu \rightarrow e\gamma)} \sim \frac{1}{100}$$

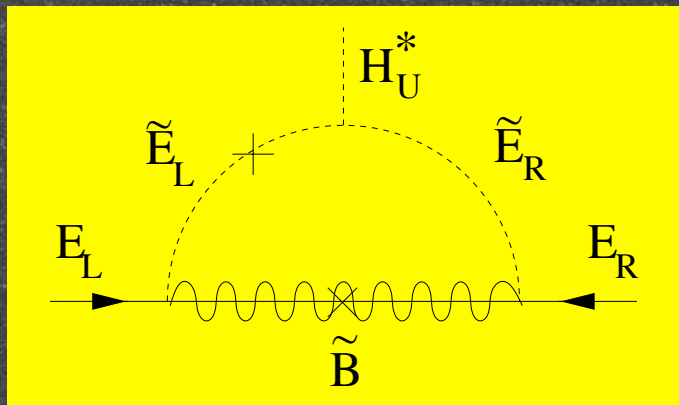
But, experimentally,

$\mu \rightarrow e\gamma$	$< 1.2 \times 10^{-11}$
$\mu N \rightarrow e N$	$< 6 \times 10^{-13}$



# Higgs-mediated SUSY LFV

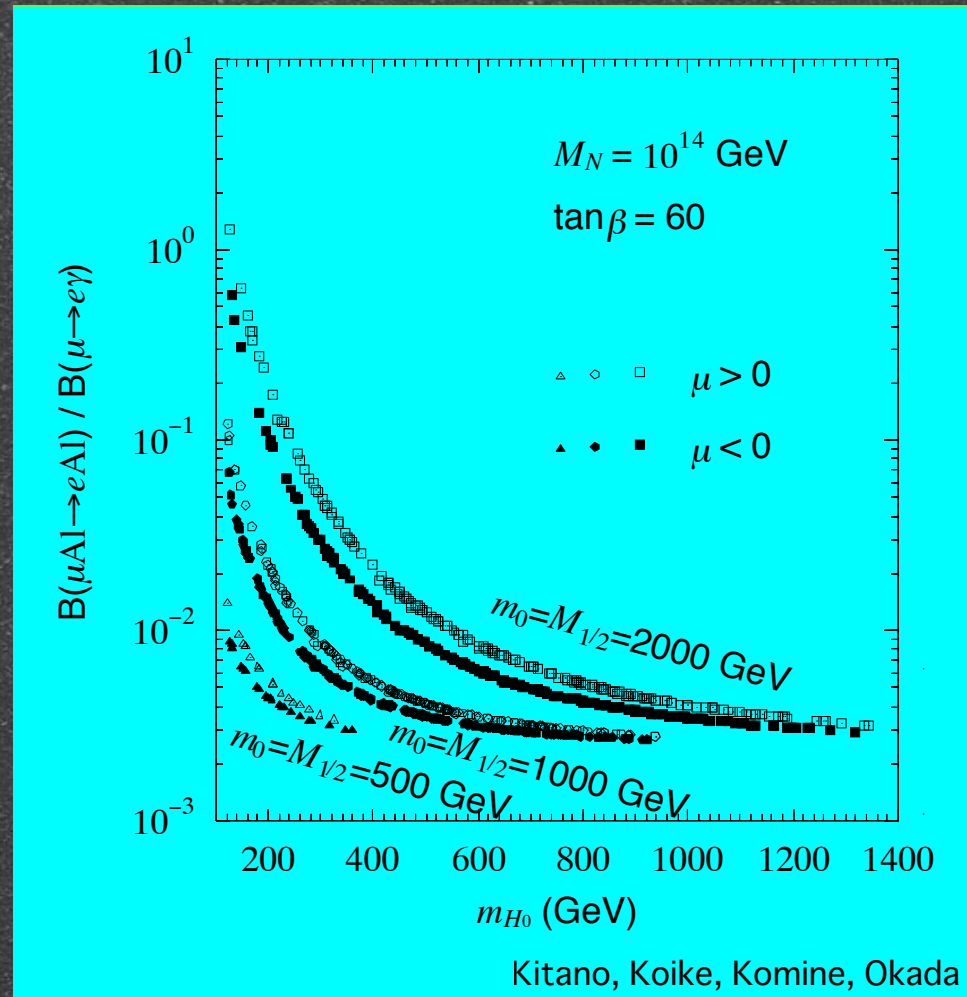
Higgs-exchange for LFV in SUSY Seesaw model



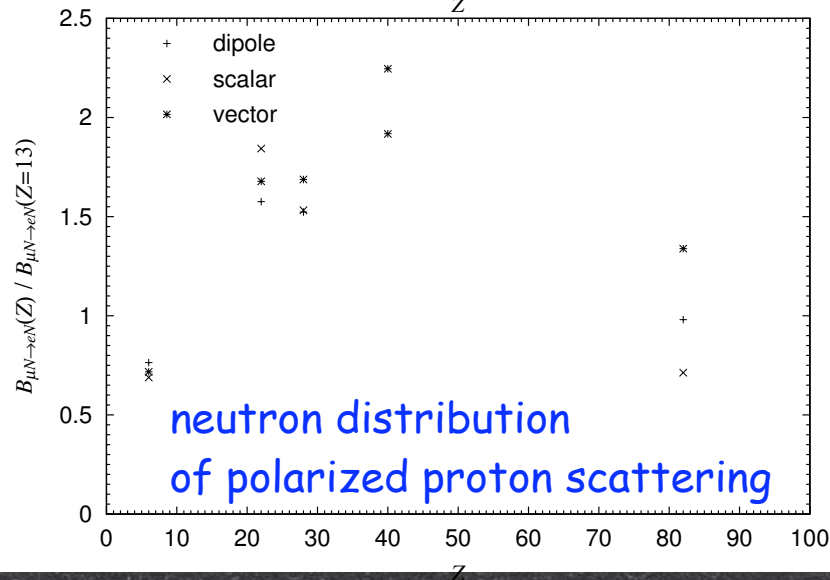
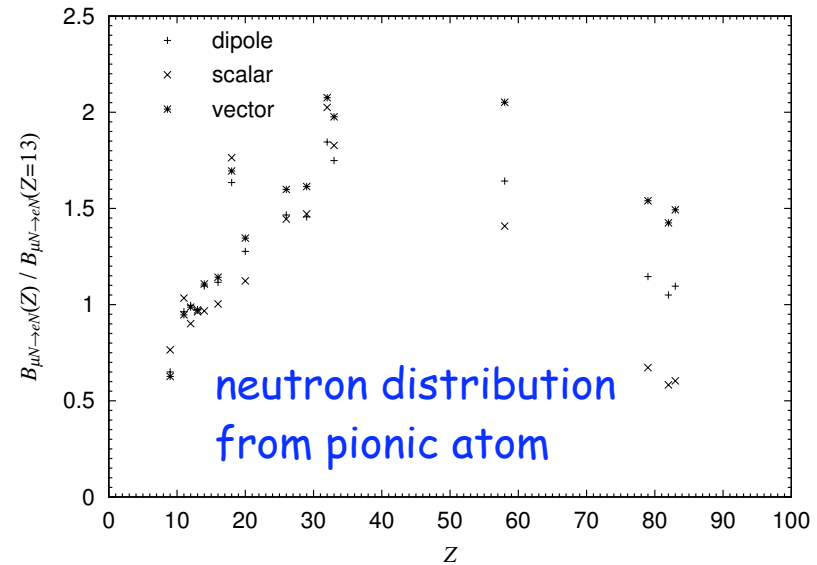
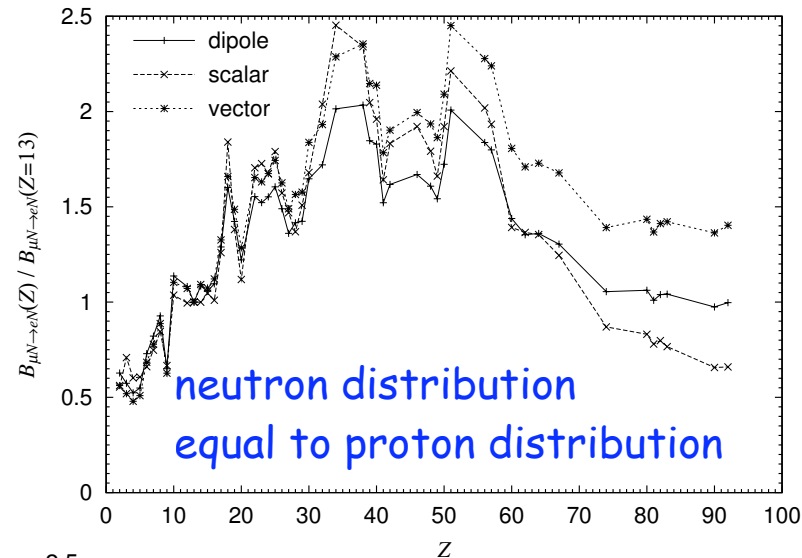
As the  $H_0$  mass is light, the contribution of the Higgs-mediated diagram becomes larger.

$$\frac{B(\mu N \rightarrow eN)}{B(\mu \rightarrow e\gamma)} \sim O(1)$$

at  $H_0 \sim 200$  GeV



# $\mu$ -e conversion : Z dependence



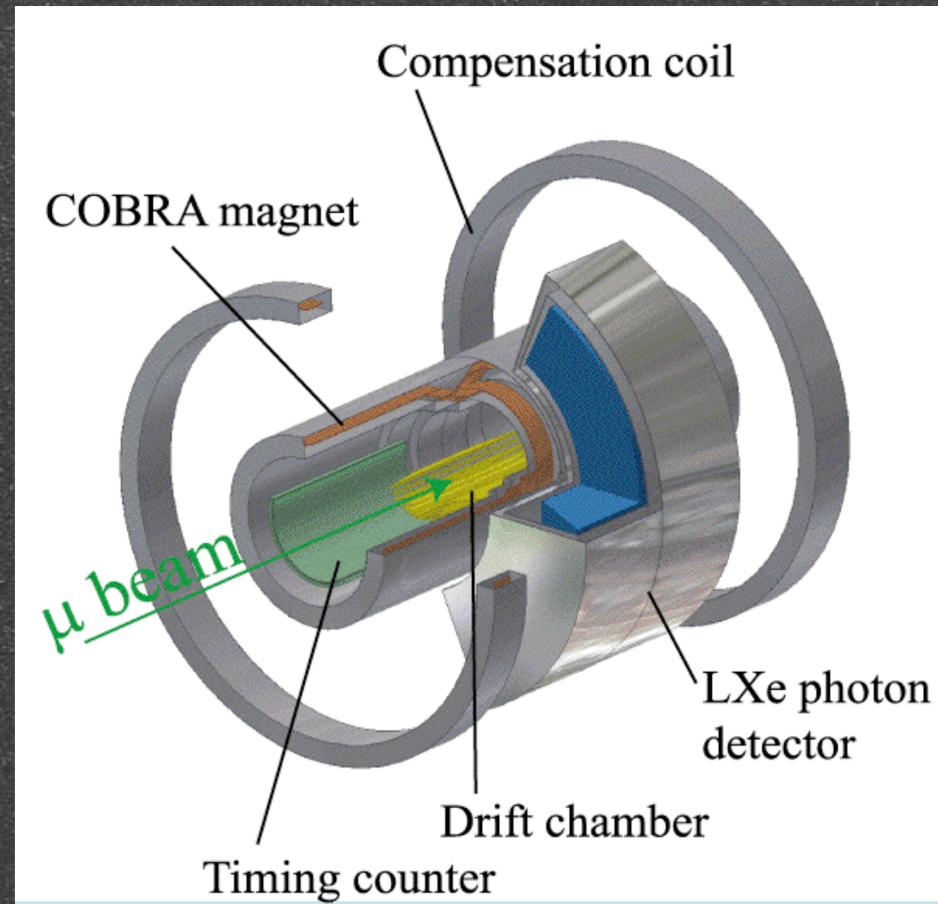
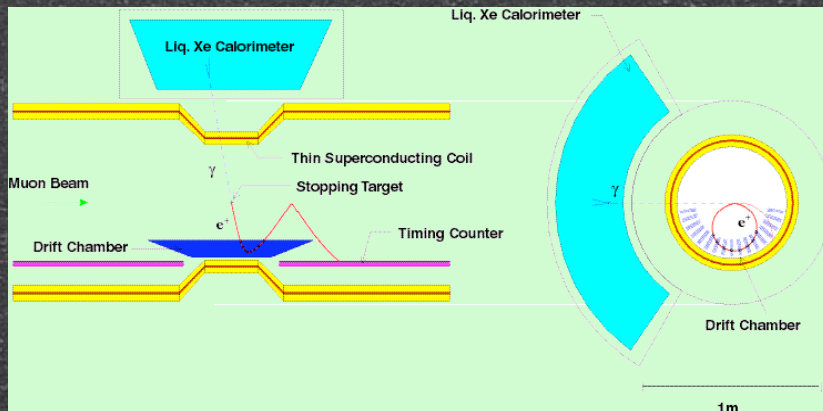
normalized at Al target.

For heavy target, difference of the interactions might be seen ?

R. Kitano, M. Koike, and Y. Okada, 2002

# MEG at PSI

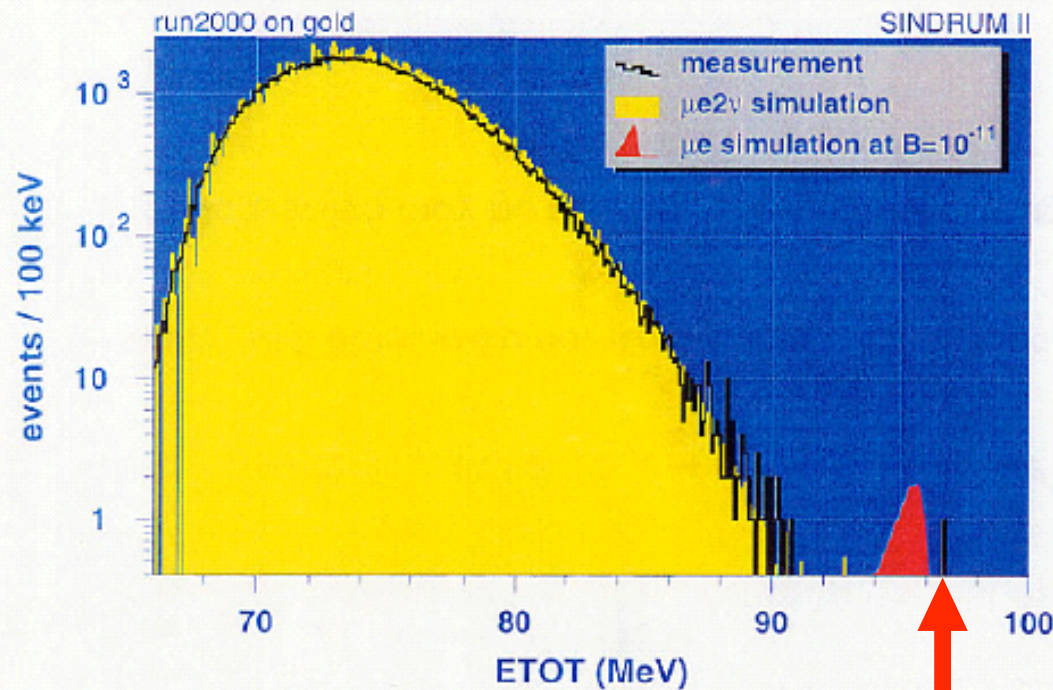
- $\mu \rightarrow e \gamma$ 
  - MEG at PSI, 2004~
    - DC beam  $10^8 \mu/s$
    - BR  $\sim 10^{-13}$
  - Accidental background
  - Detector Improvement
  - Polarization



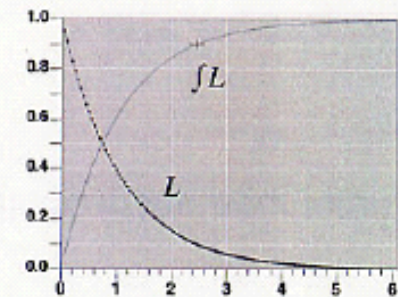
start engineering in 2006

# SINDRUM-II $\mu$ -e conversion

## Final result



$\mu e$  Conversion on Gold



$\mathcal{L}(N_{\mu e})$  and  $\int_0^{N_{\mu e}^{\max}} \mathcal{L}(n) dn$ .

$\mu^-$ stops	$4.4 \pm 0.3 \times 10^{13}$
$f_{\text{cap}} \times \Omega \times \epsilon_{\text{tot}}$	7.0%
single event sensitivity	$3.3 \pm 0.2 \times 10^{-13}$
90% C.L. limit	2.45 events

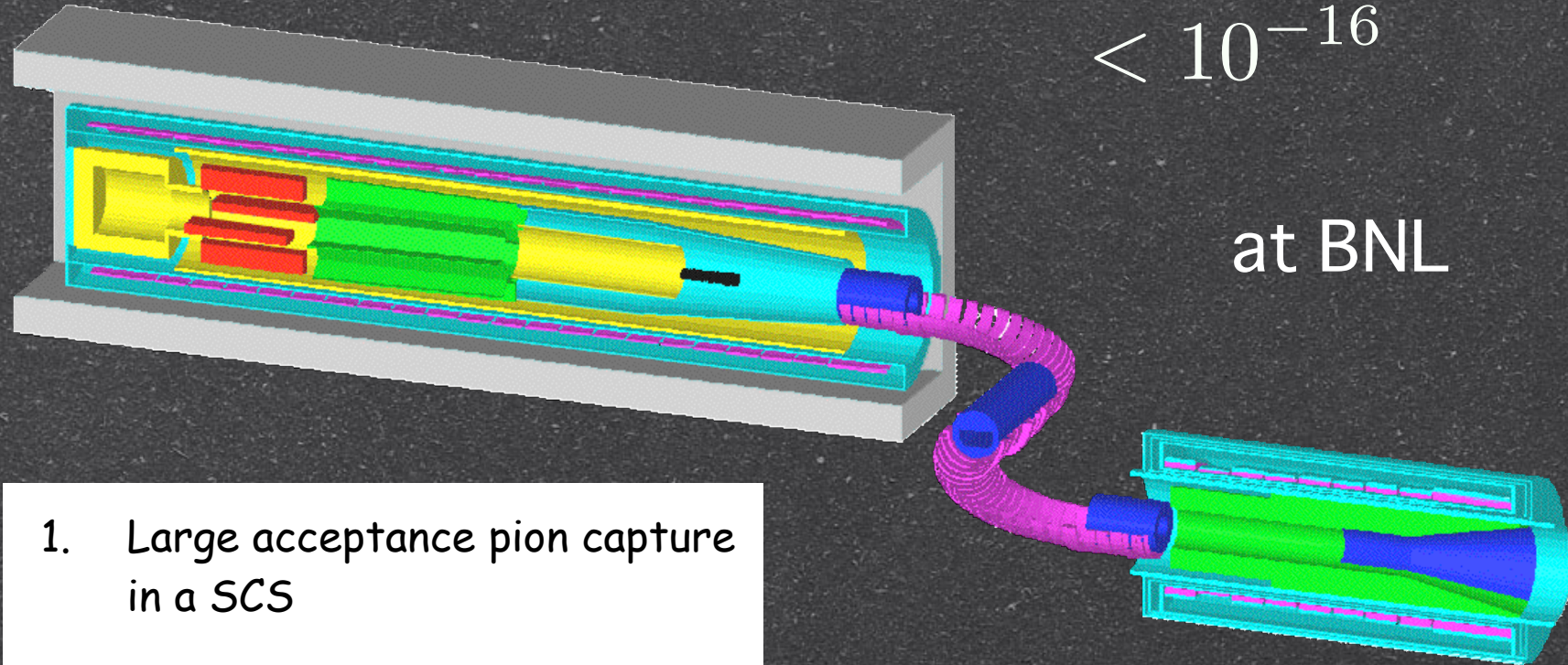
In the likelihood analysis of the energy distribution a flat background from cosmic rays and radiative pion capture was allowed.

Result:  $B_{\mu e}^{\text{gold}} < 8 \times 10^{-13}$  90% C.L.

# MECO $\mu$ -e conversion

$< 10^{-16}$

at BNL



1. Large acceptance pion capture in a SCS
2. Muon transport (60 - 120 MsV/c) in a curved solenoid
3. Long detector solenoid with muon stopping target and tracking system

start in 2011 ?  
NSF Review, 2005

# Muon Beams





# Muon Statistics

## Meson Factory (PSI, TRIUMF, LAMPF)

proton energy  $\sim 500$  MeV

beam current  $\sim 10^{15} - 10^{16}$  protons/sec

$10^6 - 10^8$  muons /secs

about  $10^{-8}$  muons/proton

## Neutrino Factory

proton energy  $\sim$  a few to several 10 GeV

beam current  $\sim$  a few  $10^{14}$  protons/sec

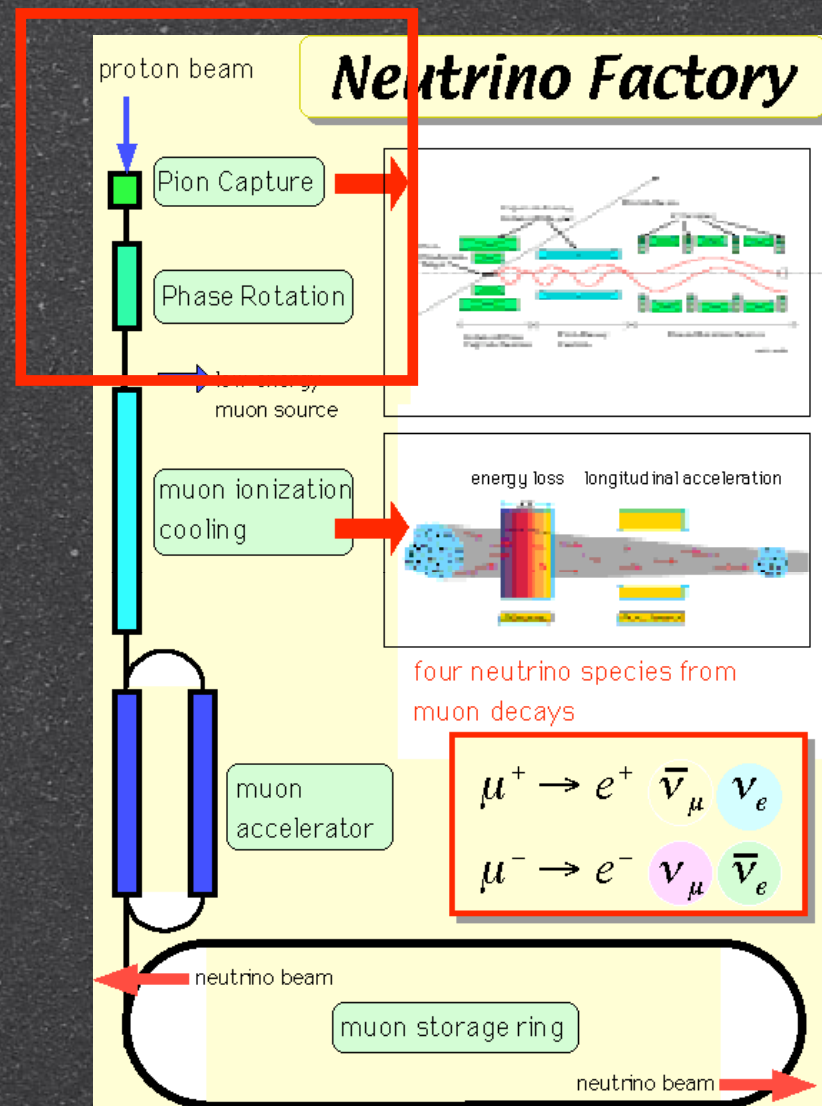
$10^{13} - 10^{14}$  muons /sec

about 0.1 - 0.3 muons/proton

# NuFACT or Proton Driver

The front end of Neutrino Factory aims to produce about  $10^{14}$  muons/sec with given time structure.

The proton driver associated with neutrino factory would produce high intensity muon beam with more variety of beam specifications.



# Muon Beam Requirements

**Table 6:** Beam requirements for new muon experiments. Given are required sign of charge  $q_\mu$  and the minimum of the total usable number of muons  $\int I_\mu dt$  above which significant progress can be expected in the physical interpretation. The experiments which require pulsed beams (see Fig. 27) are sensitive to the muon suppression  $I_0/I_m$  between pulses of length  $\delta T$  and separation  $\Delta T$ . This does not apply (n/a) for continuous beams. Most experiments require energies below 4 MeV corresponding to 29 MeV/c momentum. Thin targets and storage ring acceptances, demand rather small momentum bites  $\Delta p_\mu/p_\mu$ .

Experiment	$q_\mu$	$\int I_\mu dt$	$I_0/I_m$	$\delta T$ [ns]	$\Delta T$ [ $\mu s$ ]	$E_\mu$ [MeV]	$\Delta p_\mu/p_\mu$ [%]
$\mu^- N \rightarrow e^- N^\dagger$	-	$10^{21}$	$< 10^{-10}$	$\leq 100$	$\geq 1$	$< 20$	$< 10$
$\mu^- N \rightarrow e^- N^\ddagger$	-	$10^{20}$	n/a	n/a	n/a	$< 20$	$< 10$
$\mu \rightarrow e\gamma$	+	$10^{17}$	n/a	n/a	n/a	1...4	$< 10$
$\mu \rightarrow eee$	+	$10^{17}$	n/a	n/a	n/a	1...4	$< 10$
$\mu^+ e^- \rightarrow \mu^- e^+$	+	$10^{16}$	$< 10^{-4}$	$< 1000$	$\geq 20$	1...4	1...2
$\tau_\mu$	+	$10^{14}$	$< 10^{-4}$	$< 100$	$\geq 20$	4	1...10
transvers. polariz.	+	$10^{16}$	$< 10^{-4}$	$< 0.5$	$> 0.02$	30-40	1...3
$g_\mu - 2$	$\pm$	$10^{15}$	$< 10^{-7}$	$\leq 50$	$\geq 10^3$	3100	$10^{-2}$
$edm_\mu$	$\pm$	$10^{16}$	$< 10^{-6}$	$\leq 50$	$\geq 10^3$	$\leq 1000$	$\leq 10^{-3}$
$M_{HFS}$	+	$10^{15}$	$< 10^{-4}$	$\leq 1000$	$\geq 20$	4	1...3
$M_{1s2s}$	+	$10^{14}$	$< 10^{-3}$	$\leq 500$	$\geq 10^3$	1...4	1...2
$\mu^-$ atoms	-	$10^{14}$	$< 10^{-3}$	$\leq 500$	$\geq 20$	1...4	1...5
condensed matter (incl. bio sciences)	$\pm$	$10^{14}$	$< 10^{-3}$	$< 50$	$\geq 20$	1...4	1...5

<sup>†</sup> Scenario in which a pulsed beam is utilized.

<sup>‡</sup> Scenario in which a continuous beam after the muon cooling stage is employed.

# Muon Factory

- Use of the Front End of NuFACT
  - sharing a beam ?
- Use of parts of of the proton machine complex for NuFACT and construct dedicated facility (muon factory)
  - **Accumulator ring** needed to change beam time structure as demanded from muon experiment
  - ex. **50 GeV** + 3 GeV @J-PARC, FNAL, MI (120 GeV) + **8 GeV** (recycler) @FNAL

# Which Muon Programs ?

- Not all the muon programs need high intensity muon beams. High quality beam is obtained from high intensity beam. Need studies.

Topics	high intensity needed ?	high quality needed ?
muon g-2		
muon EDM		
muon mixing (LFV)		
muon lifetime		
catalyzed fusion		
muSR		

# For CLM Processes ?

	issue	beam requirement
$\mu \rightarrow e\gamma$	detector-limited	a continuous beam
$\mu \rightarrow eee$	detector-limited	a continuous beam
$\mu N \rightarrow eN$	beam-limited	a pulsed beam

# Beam Requirements for $\mu$ -e conversion



Beam is critical element for  $\mu$ -e conversion

## MECO

- Higher muon intensity
  - more than  $10^{12} \mu^-/\text{sec}$
- pulsed beam
  - rejection of background from proton beam

- Less beam contamination
  - no pion contamination
    - ⇒ long flight path
  - beam extinction between pulses
    - ⇒ kicker magnet

- Narrow energy spread
  - allow a thinner muon-stopping target
    - ⇒ better  $e^-$  resolution and acceptance

- Point Source
  - allow a beam blocker behind the target
    - ⇒ isolate the target and detector
    - ⇒ tracking close to a beam axis

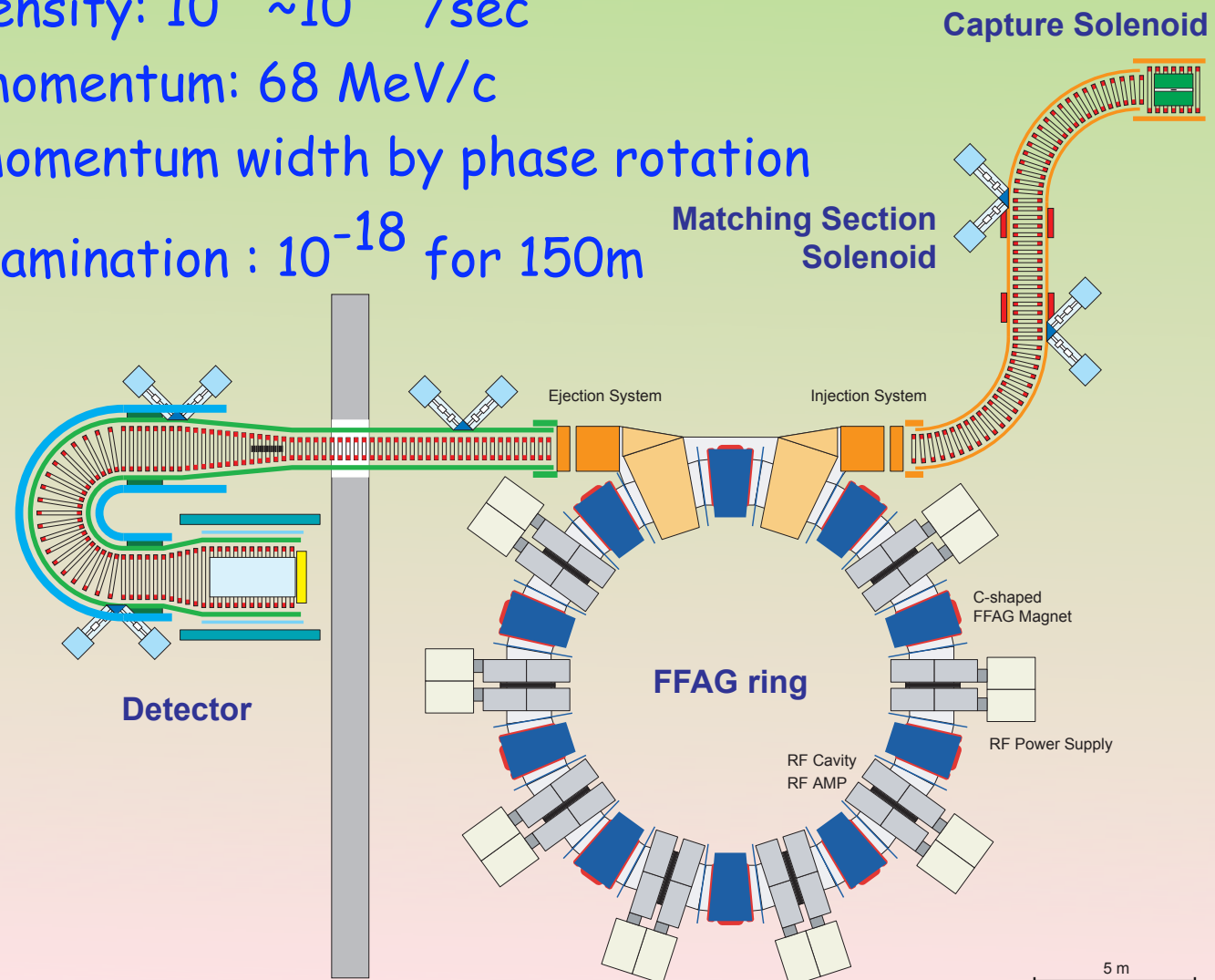
## PRISM

# PRISM

PRISM=Phase Rotated  
Intense Slow Muon source



- muon intensity:  $10^{11} \sim 10^{12}$  /sec
- central momentum: 68 MeV/c
- narrow momentum width by phase rotation
- pion contamination :  $10^{-18}$  for 150m

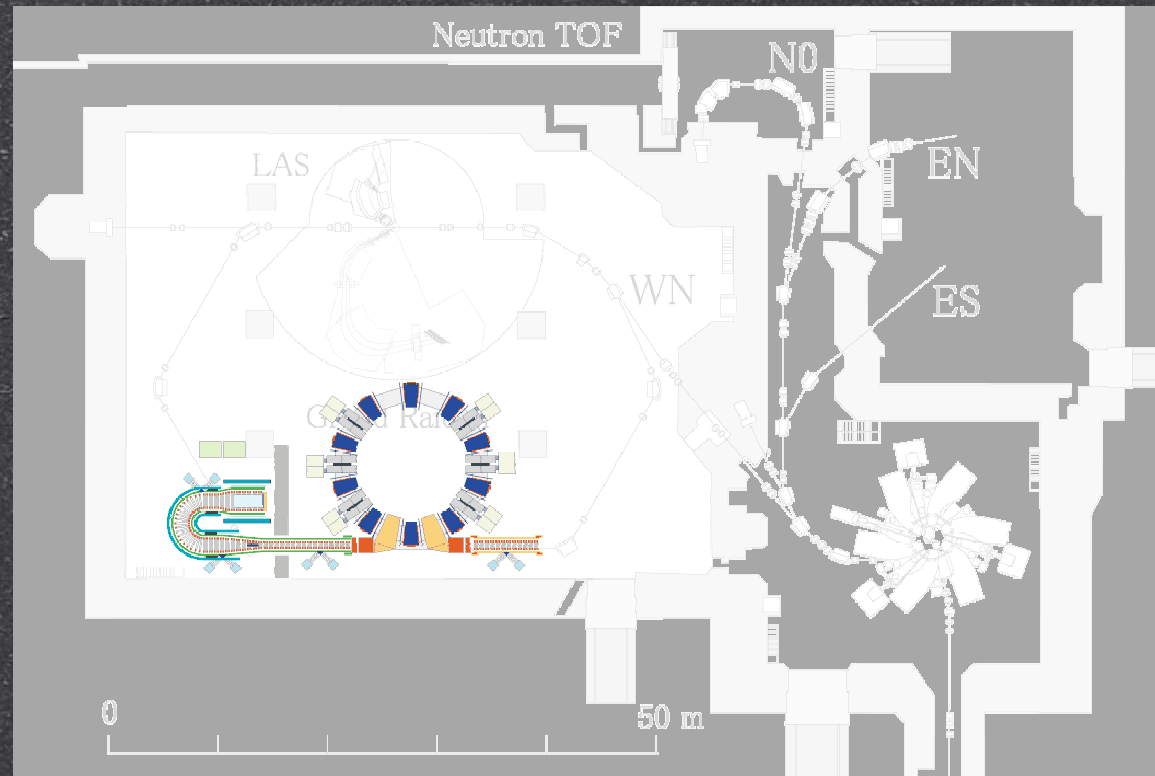




# PRISM -Phase I @ RCNP

- Research Center for Nuclear Physics (RCNP), Osaka University
- 400 MeV proton (above pion production threshold)
- upto 5 micro A

Purpose : Test of fundamental performance of PRISM with muons.



# Other Topics



# Other Topics

- Muon Lifetime Measurements
- Determination of  $G_F$
- CLM Deep Inelastic Reaction (tau appearance)  
•  $\mu + N \rightarrow \tau + X, e + N \rightarrow \tau + X$
- Proposal on Enhanced Lepton Number Non-conservation
- Muon Catalyzed Fusion
- MuSR
- Slow-Muon Production by Laser
- and others.....

*End of My Slides*