

NA48 future program :
measurement of the
direct CP violation
in charged Kaon decays

E. Iacopini

Phys. Dept. Florence Univ. and INFN-Florence

Frescati 15 May 2000

Spring School in Nuclear Subnuclear and
Astroparticle Physics : 15-20 May 2000

■ The origin of CP violation in particle physics is still an open problem ... (1)

From the pioneering experiment of Christenson, Cronin, Fitch and Turlay [Phys. Rev. Lett. 13 (1964), 128] we know that, in neutral Kaon decays

CP was violated; however,

because of the mixing of the two CP eigenstates K_1 and K_2 in the K_L, K_S (described by $\epsilon \dots$),

only the most recent measurements of ϵ'/ϵ

[KTeV : Phys. Rev. Lett. 83 (1999), 22 $\rightarrow (28.0 \pm 4.1) \times 10^{-4}$

NA48 : Phys. Lett. 465 B (1999), 335 $\rightarrow (18.5 \pm 7.3) \times 10^{-4}$]

have shown that, besides the mixing, there must be also a direct CP violation in the neutral Kaon decay dynamics

(described by $\epsilon' \dots$)

■ Another very interesting decay that could shed some light on the problem of the direct CP violation, is the decay

$$K^{\pm} \rightarrow \pi^{\pm} \pi^{\mp} \pi^{\pm} \equiv (3\pi)^{\pm} \quad [BR = 5.59\%]$$

Up to now, indirect/direct CP violation has been observed only in the neutral kaon system ($K \rightarrow 2\pi$), where $\epsilon \sim 23 \cdot 10^{-3}$; $\epsilon' \sim 6.7 \cdot 10^{-6}$.

Here, the indirect (mixing) contribution ϵ is possible since K_1 and K_2 are neutral, ... and this tends to make $\epsilon' \dots$!

In $K^{\pm}$ decays, where $CP |K^{\pm}\rangle = |K^{\mp}\rangle$, no indirect contribution is possible, because charge superselection rule prevents mixing ... $\Rightarrow$ only direct violation (if any...)!

Let us consider in its rest frame, the decay

$$K^{\pm} \rightarrow (3\pi)^{\pm}$$

the differential decay rate $d\Gamma$ reads

$$d\Gamma = \frac{1}{2M} |\mathcal{M}|^2 d\phi$$

$\uparrow$ K mass $\nwarrow$ decay amplitude $\swarrow$ phase space

the 3-pion final state is completely defined (modulo a rotation) in terms of the two variables

[cfr. S. Weinberg, Phys Rev Lett 4 (1960), 87]

$$(u) \quad u = \frac{S_0 - S_3}{M^2} \quad ; \quad v = \frac{S_1 - S_2}{M^2}$$

$\swarrow$ $\searrow$
 pion mass

where

$$S_i = (P_K - p_{\pi_i})^2 = M^2 + m^2 - 2ME_i$$

$$S_0 = \frac{1}{3} (S_1 + S_2 + S_3) = m^2 + M^2/3$$

and $i=3$ refers to the "odd" pion.

The **allowed** (u, v) region is defined by energy momentum conservation: we obtain

$$(u, v): -u^3 \frac{m^2}{4M^2} + v^2 \frac{m^2}{4M^2} + 3u^2 \frac{m^2}{4M^2} + uv^2 \frac{m^2}{4M^2} + \frac{v^2}{12} + \frac{u^2}{4} - 3 + \frac{2}{3} \left(\frac{M}{m} \right)^2 - \frac{1}{27} \left(\frac{M}{m} \right)^4 \leq 0 \rightarrow$$

... and, in terms of these variables, $d\phi$ reads

$$d\phi = (2\pi)^4 \delta^4(P_f - P_i) \prod_{j=1}^3 \frac{d^3K_j}{(2\pi)^3 2E_j} = \frac{1}{4(2\pi)^3} dE_1 dE_2 = \left(\frac{1}{2\pi} \right)^3 \left(\frac{m^2}{4M} \right)^2 \underline{du dv}$$

therefore any structure in the decay scatter plot yields informations about $|M|^2$!

(if also the acceptance is flat in (u, v) ...).

[**Dalitz-Fabri plot concept ...**

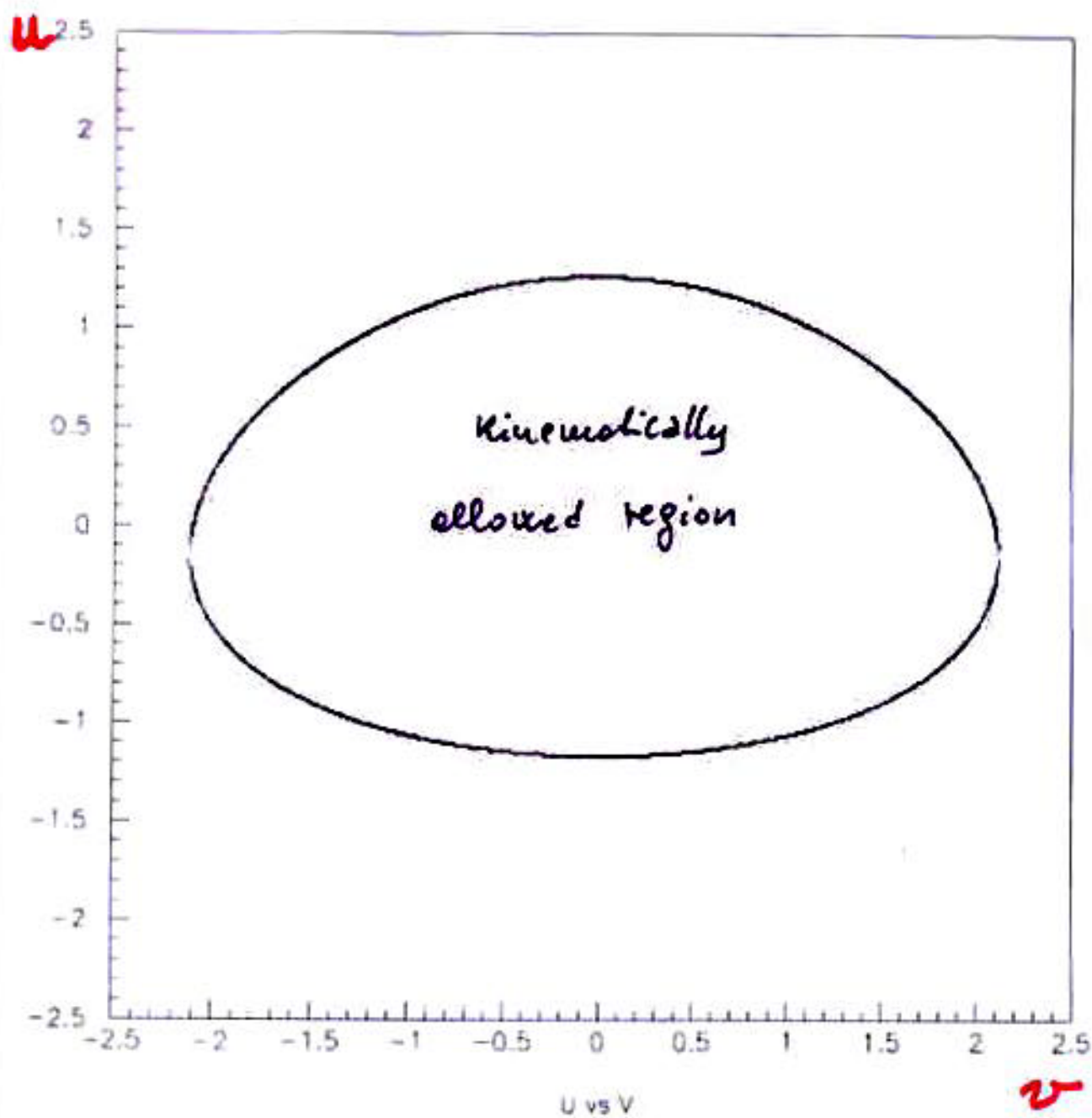
Phil. Mag. 44 (1953), 1068

Phys. Rev. 94 (1954), 1046

Il Nuovo Cimento 11 (1954), 479

]

00/05/05 18.56



The matrix element $|\mathcal{M}|^2$ is usually parametrized as follows [P.D.G. Eur. Phys. J. C3 (1998), 449]

$$|\mathcal{M}(u, v)|^2 \propto 1 + g u + h u^2 + \kappa v^2 + \dots$$

If the slope g for K^+ and K^- is not the same, i.e. if the asymmetry

$$A_g \equiv \frac{g^+ - g^-}{g^+ + g^-} \equiv \frac{\Delta g}{2g_0} \neq 0 \quad \left[g^{\pm} \equiv g^0 \pm \Delta g/2 ; \right. \\ \left. g^0 = -0.2154 \pm 0.0035 \right]$$

Then, this would indicate the presence of a direct CP violation in the decay process.

According to recent theoretical results, we can expect A_g asymmetries as high as 10^{-4}

(5 bis)

INFNNA-99/39
LPT ORSAY 99/99

Direct CP violation in $K \rightarrow 3\pi$ decays induced by SUSY chromomagnetic penguins*

G. D'Ambrosio^a, G. Isidori^b and G. Martinelli^{c,d}

^a INFN, Sezione di Napoli and Dipartimento di Scienze Fisiche,
Università di Napoli, I-80125 Napoli, Italy

^b INFN, Laboratori Nazionali di Frascati, P.O. Box 13, I-00044 Frascati, Italy

^c LAL and Laboratoire de Physique Théorique,
Laboratoire associé Centre National de la Recherche Scientifique,
Université de Paris XI, Bât 211, 91405 Orsay Cedex, France

Abstract

An analysis of the CP violating asymmetry in $K^\pm \rightarrow (3\pi)^\pm$ decays in the Standard Model and, by means of the mass insertion approximation, in a wide class of possible supersymmetric extensions, is presented. We find that the natural order of magnitude for this asymmetry is $\mathcal{O}(10^{-5})$ in both cases. Within supersymmetric models effects as large as $\mathcal{O}(10^{-4})$ are possible, but only in a restricted range of the relevant parameters.



November 1999

* Work supported in part by TMR, EC-Contract No. ERBFM RX-CT980169 (EURODAΦNE).

^d On leave of absence from Dipartimento di Fisica, Università di Roma "La Sapienza" and INFN, Sezione di Roma, P.le A. Moro 2, I-00185 Rome, Italy.

- The quantity to be measured in order to extract Δg , is the ratio

$$r(u) = \frac{\int dv |\mathcal{M}^+(u,v)|^2}{\int dv |\mathcal{M}^-(u,v)|^2} \approx \frac{1 + g^+ u}{1 + g^- u}$$

and, since the differential decay rate $d\Gamma$ reads

$$d\Gamma^\pm = \frac{1}{2M} |\mathcal{M}^\pm|^2 d\phi^\pm = K (1 + g^\pm u + \dots) du dv$$

with K independent from the kaon charge (CPT...),

to evaluate Δg we can measure

$$\frac{\int \mathcal{N}^+(u,v) dv}{\int \mathcal{N}^-(u,v) dv} \equiv \frac{\mathcal{N}^+(u)}{\mathcal{N}^-(u)} = \frac{\mathcal{N}_0^+}{\mathcal{N}_0^-} \cdot r(u)$$

Total number of decays

where $\mathcal{N}^\pm(u)$ are the differential spectra of the $K^\pm \rightarrow (3\pi)^\pm$ decays happened.

However, the $K^\pm \rightarrow (3\pi^\pm)$ spectra
observed experimentally $N^\pm(u, v)$ are only
proportional to $\mathcal{N}^\pm(u, v)$ through the
detector acceptance:

$$N^\pm(u, v) = \mathcal{N}^\pm(u, v) * A^\pm(u, v)$$

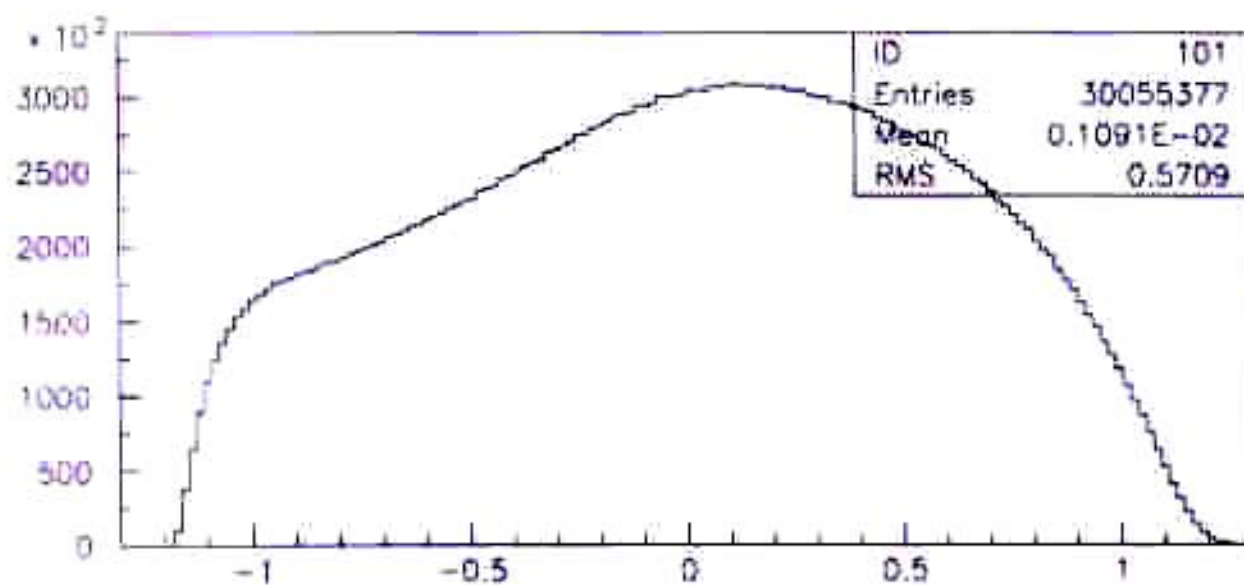
and only if the acceptance is independent
from the K charge, we still have

$$R(u) \equiv \frac{\int N^+(u, v) dv}{\int N^-(u, v) dv} \equiv \frac{N^+(u)}{N^-(u)} = \frac{N_0^+}{N_0^-} \cdot r(u)$$

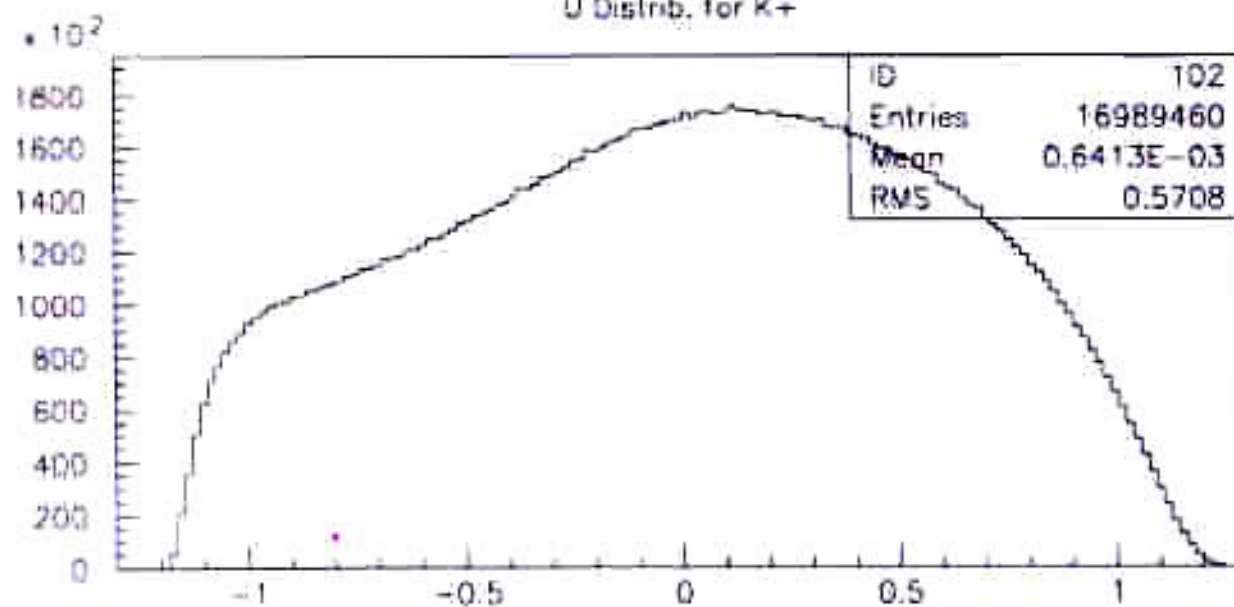
i.e., we can evaluate $r(u)$ without
needing to introduce acceptance (MC)
corrections !

(7bis

00/05/01 09.02



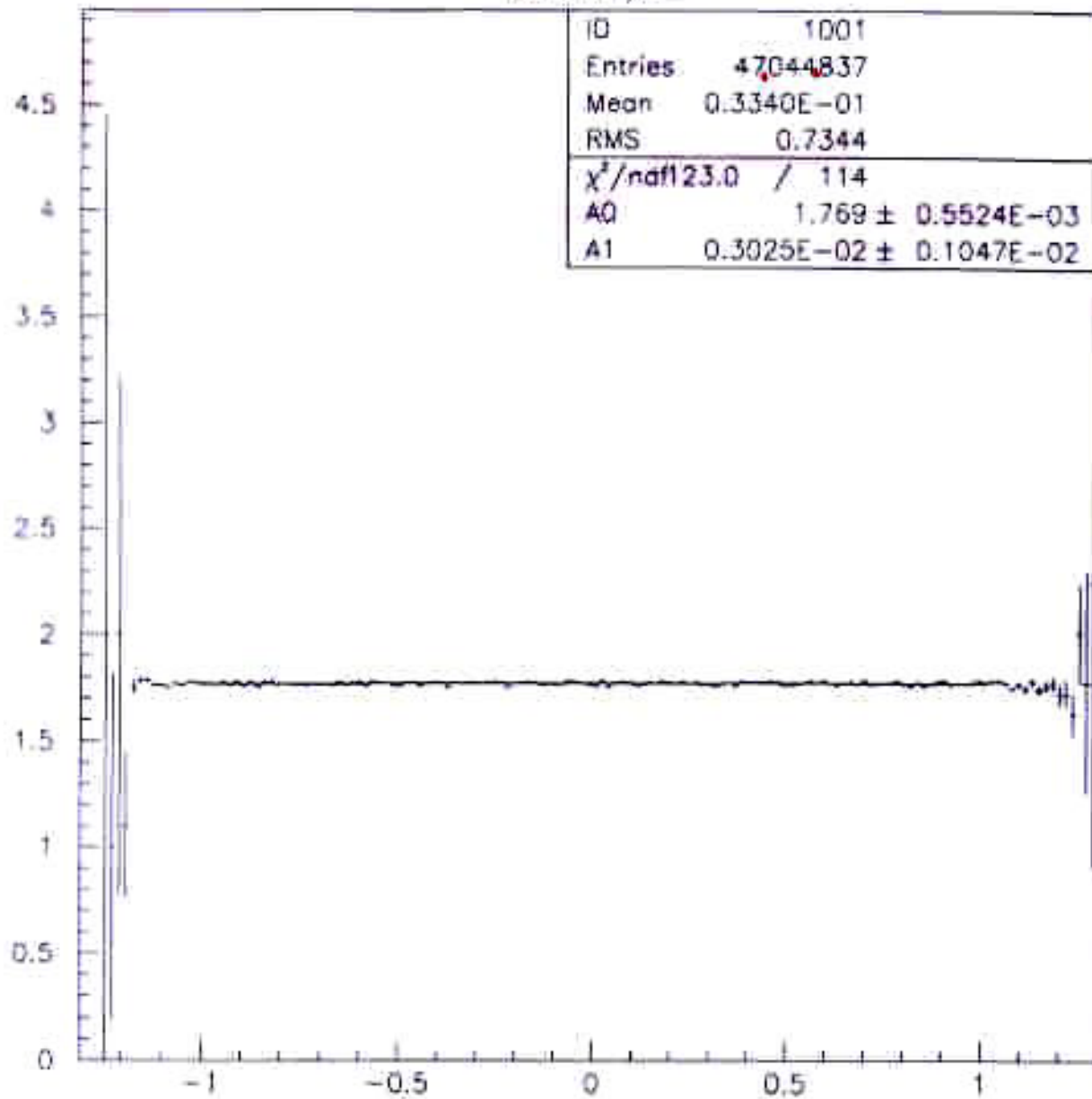
U Distrib. for K+



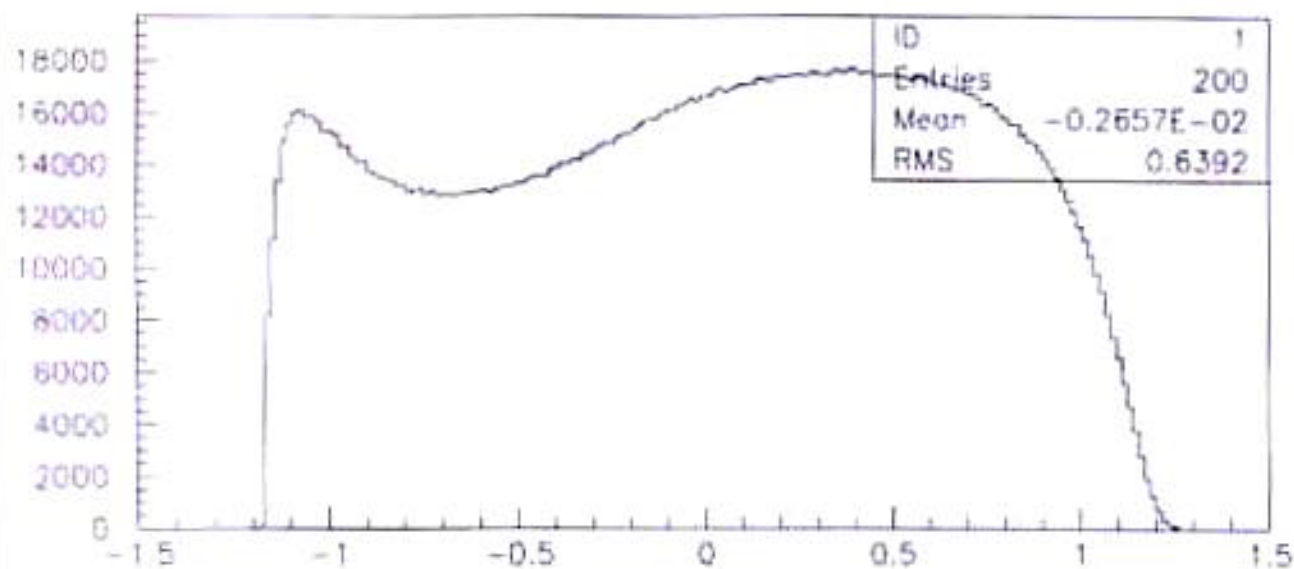
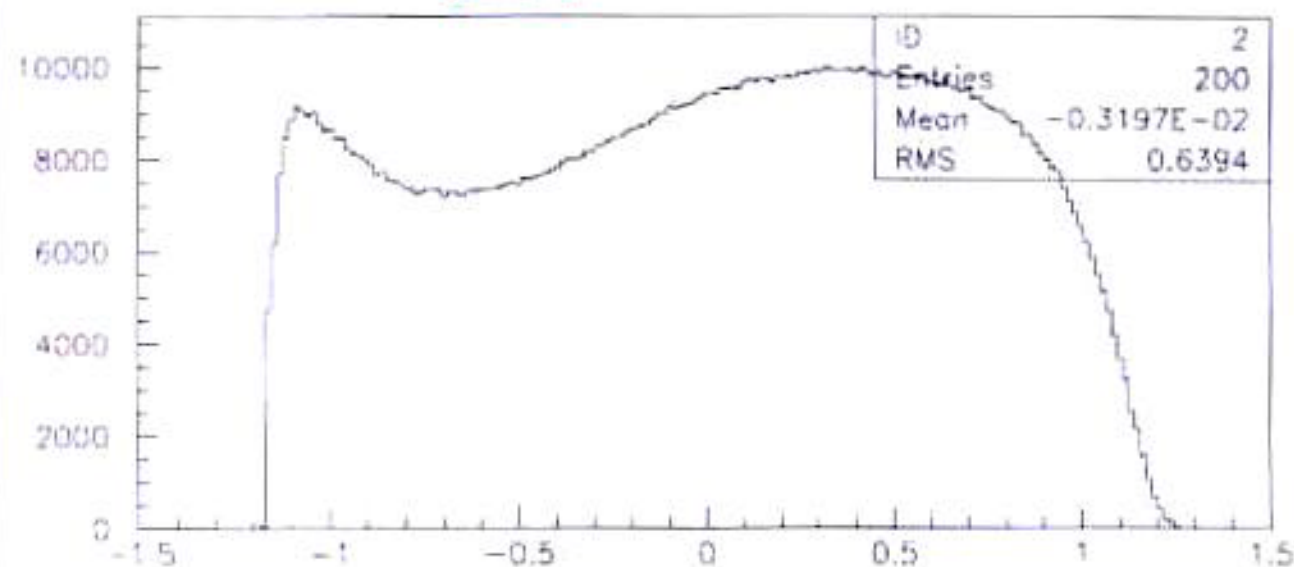
U Distrib. for K-

00/05/06 17.04

Ratio N+/N-



00/05/05 20.03

U weighted distrib. for reconstructed K^+ U weighted distrib. for reconstructed K^-

weight $\propto \frac{1}{\text{phase space}}$

ADDENDUM III
(to Proposal P253/CERN/SPSC)
for a Precision Measurement of Charged Kaon Decay Parameters with an
Extended NA48 Setup

R. Batley, A. Bevan, R.S. Dosanjh, T.J. Gershon, G.E. Kalmus¹⁾, D.J. Munday,
E. Olaiya, M.A. Parker, S.A. Wotton
Cavendish Laboratory, University of Cambridge, Cambridge, CB3 0HE, UK²⁾

G. Barr, G. Bocquet, J. Bremer, A. Ceccucci, T. Cuhadar, D. Cundy, N. Dohle,
V. Falaleev, L. Gatignon, A. Gonidec, B. Gorini, G. Govi, P. Grafström, W. Kubischta,
A. Lacourt, M. Lenti³⁾, A. Norton, B. Panzer-Steindel, D. Schinzel, G. Tatishvili⁴⁾,
H. Taureg, H. Wahl
CERN, CH-1211, Geneva 23, Switzerland

C. Cheshkov, A. Gaponenko, P. Hristov, V. Kekelidze, D. Madigojine, N. Molokanova,
Yu. Potrebenikov, A. Tkatchev, A. Zinchenko
Joint Institute for Nuclear Research, Dubna, 141980, Russian Federation

W. Baldini, D. Bettoni, R. Calobrevre, M. Contalbrigo, P. Dalpiaz, J. Duclos,
P.L. Frabetti, A. Gianoli, E. Luppi, M. Martini, F. Petrucci, M. Savrié
*Dipartimento di Fisica dell'Università e Sezione dell'INFN di Ferrara, I-44100 Ferrara,
Italy*

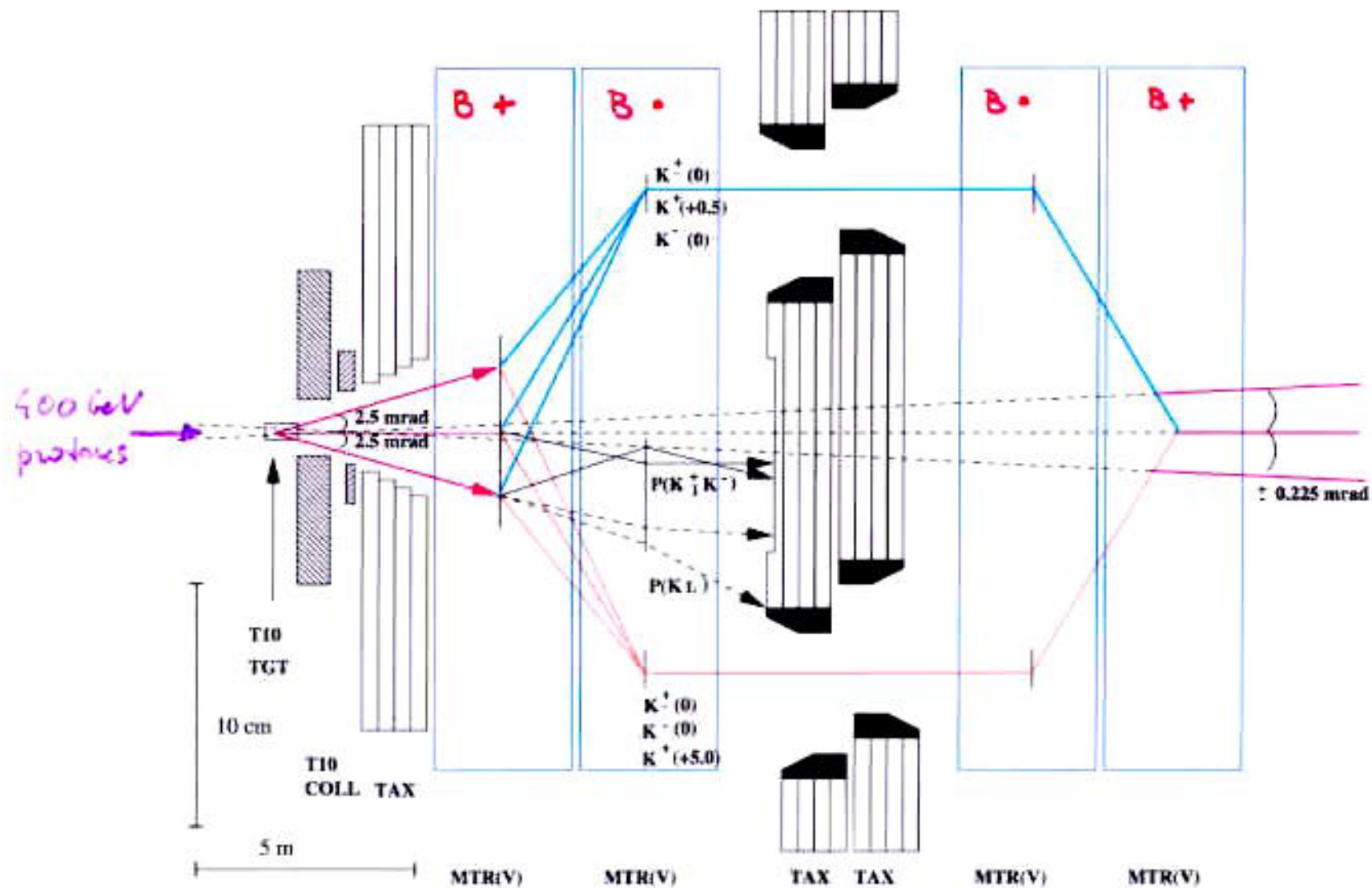
F. Becattini, A. Bizzeti⁵⁾, M. Calvetti, G. Collazuol, G. Graziani, E. Iacopini,
F. Martelli⁶⁾, M. Veltri⁶⁾
*Dipartimento di Fisica dell'Università e Sezione dell'INFN di Firenze, I-50125 Firenze,
Italy*

M. Eppard, A. Hirstius, K. Holtz, K. Kleinknecht, U. Koch, L. Köpke, P. Lopes da
Silva, I. Pellmann, A. Peters, B. Renk, S.A. Schmidt, Y. Schué, R. Wanke, A. Winhart,
M. Wittgen
Institut für Physik, Universität Mainz, D-55099 Mainz, Germany⁷⁾

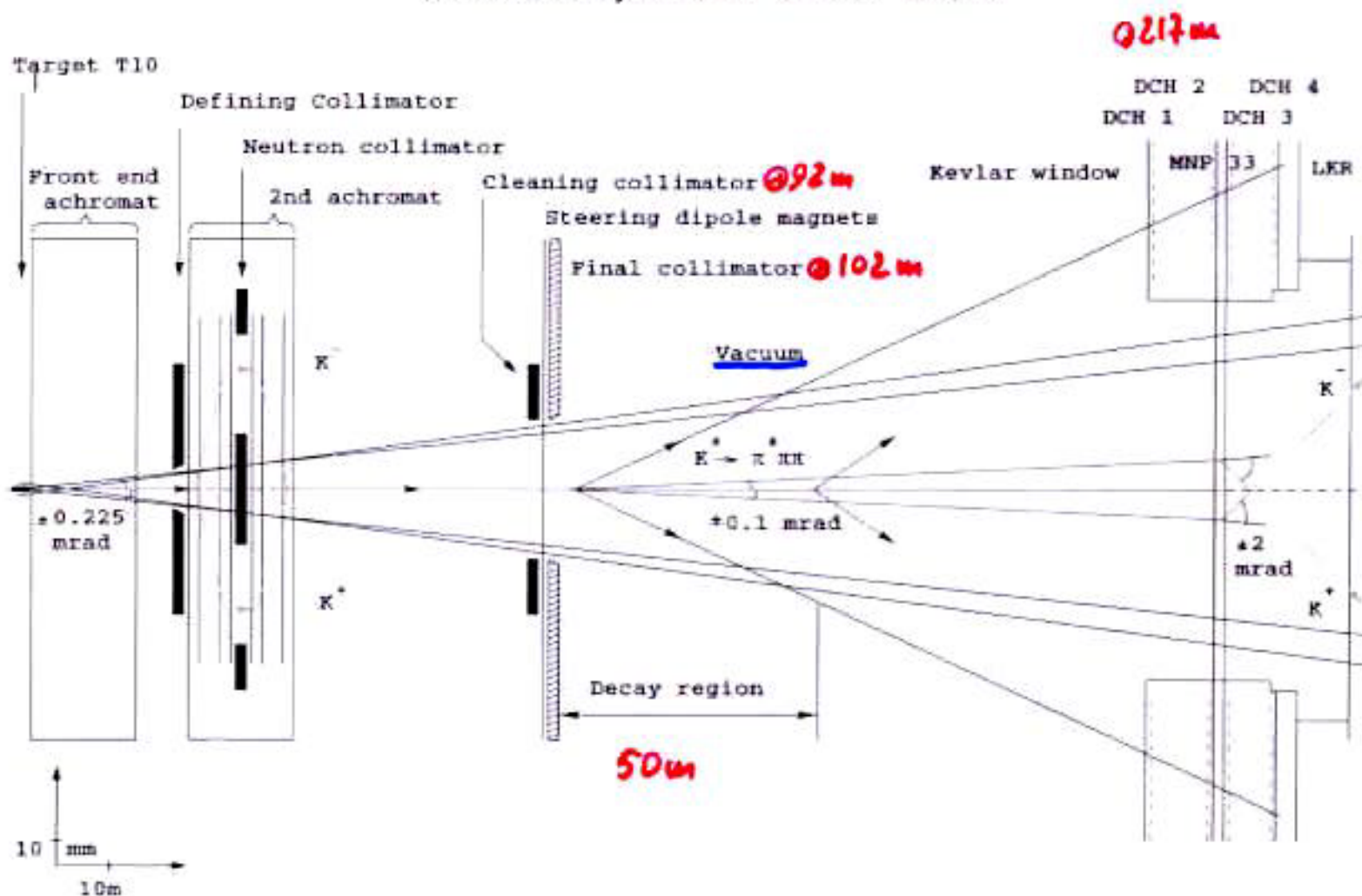
G. Anzivino, P. Cenci, E. Imbriani, P. Lubrano, A. Mestvirishvili, A. Nappi, M. Pepe,
M. Piccini, M. Valdata
*Dipartimento di Fisica dell'Università e Sezione dell'INFN di Perugia, I-06100 Perugia,
Italy*

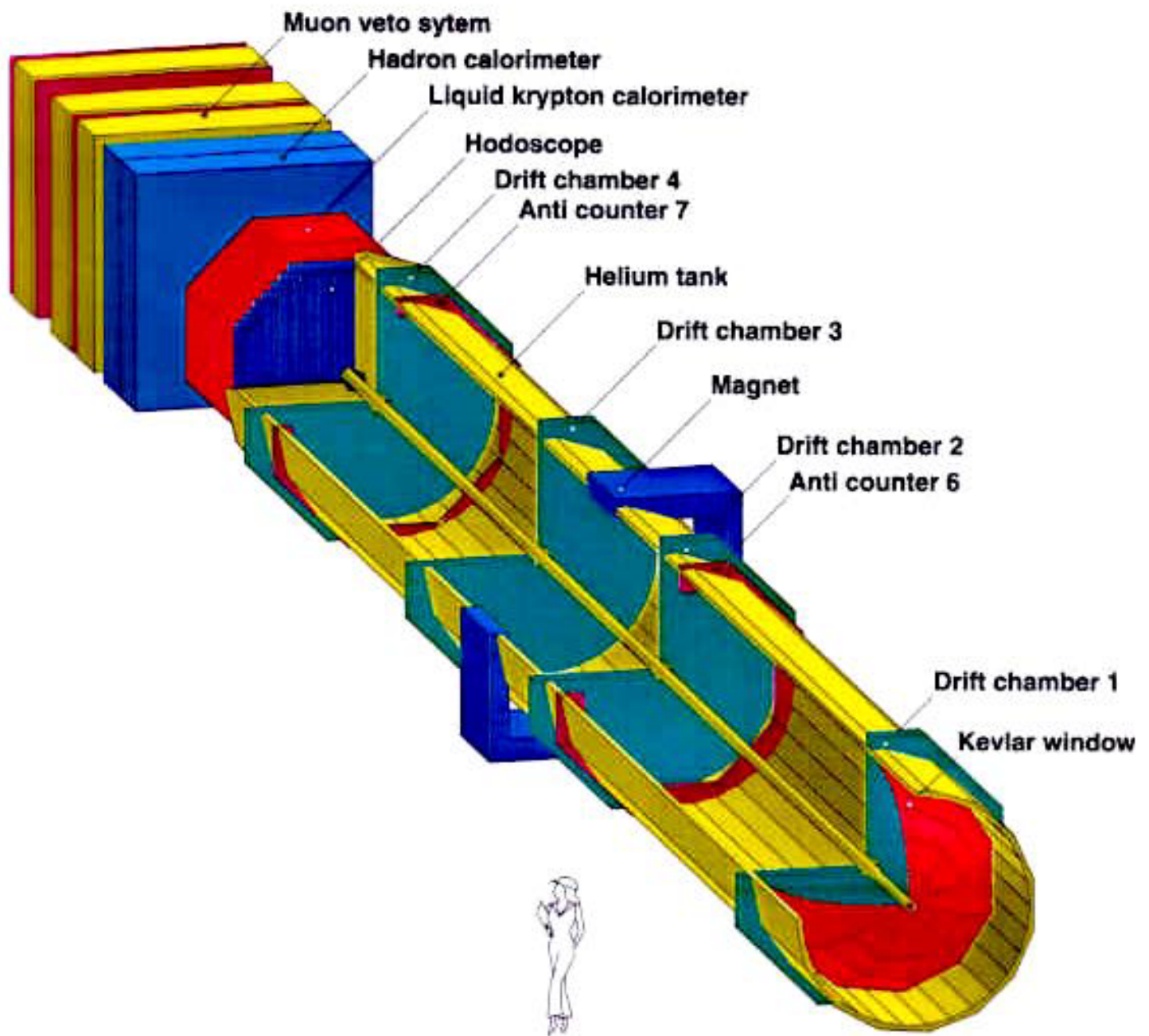
L. Bertanza, A. Bigi, R. Carosi, R. Casali, C. Cerri, M. Cirilli, F. Costantini,
R. Fantechi, S. Guidici, I. Mannelli, G. Pierazzini, M. Sozzi
*Dipartimento di Fisica, Scuola Normale Superiore e Sezione dell'INFN di Pisa, I-56100
Pisa, Italy*

Simultaneous K^+ and K^- beams (front end achromat)

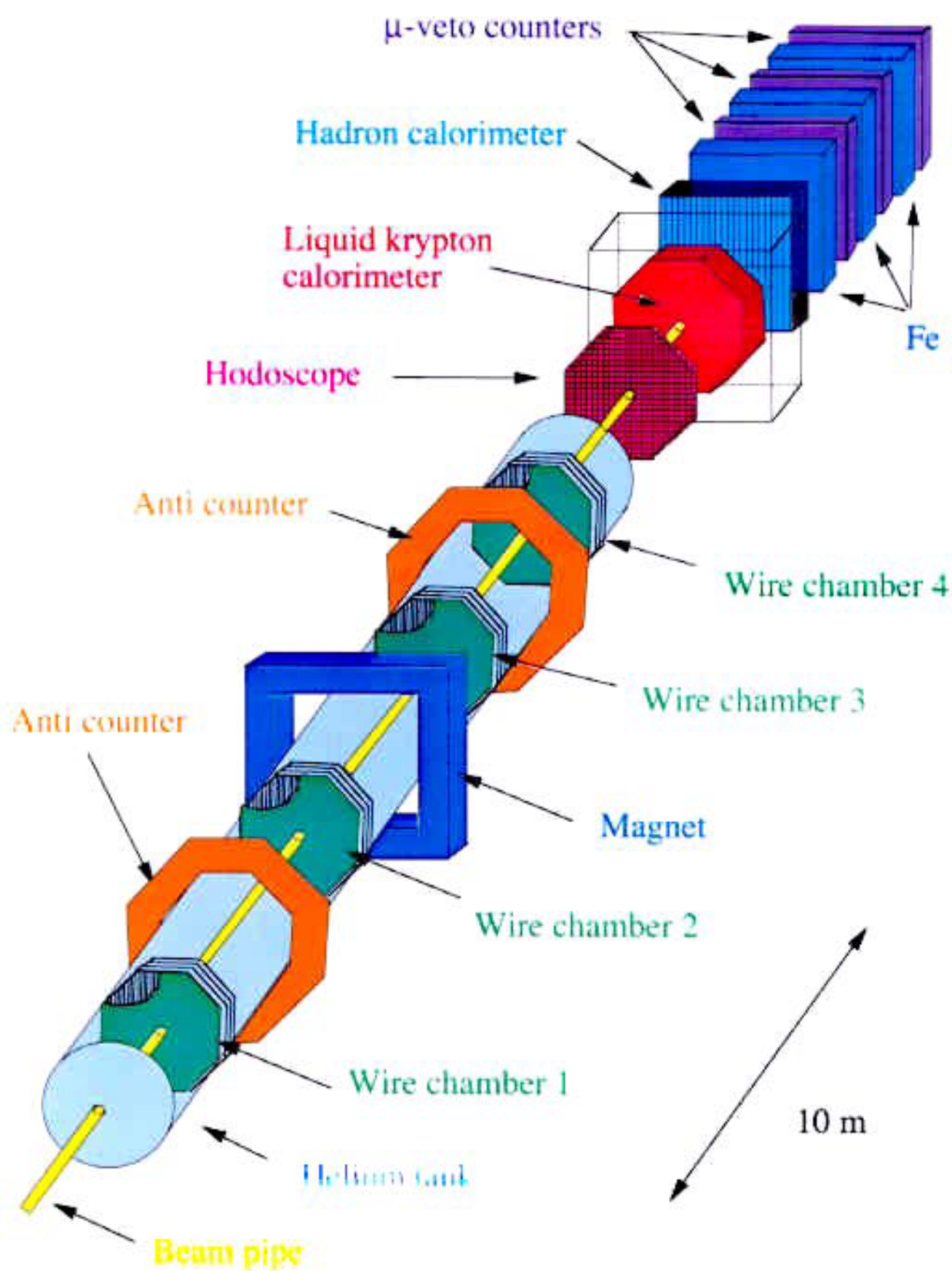


Schematic layout of K^+ and K^- beams



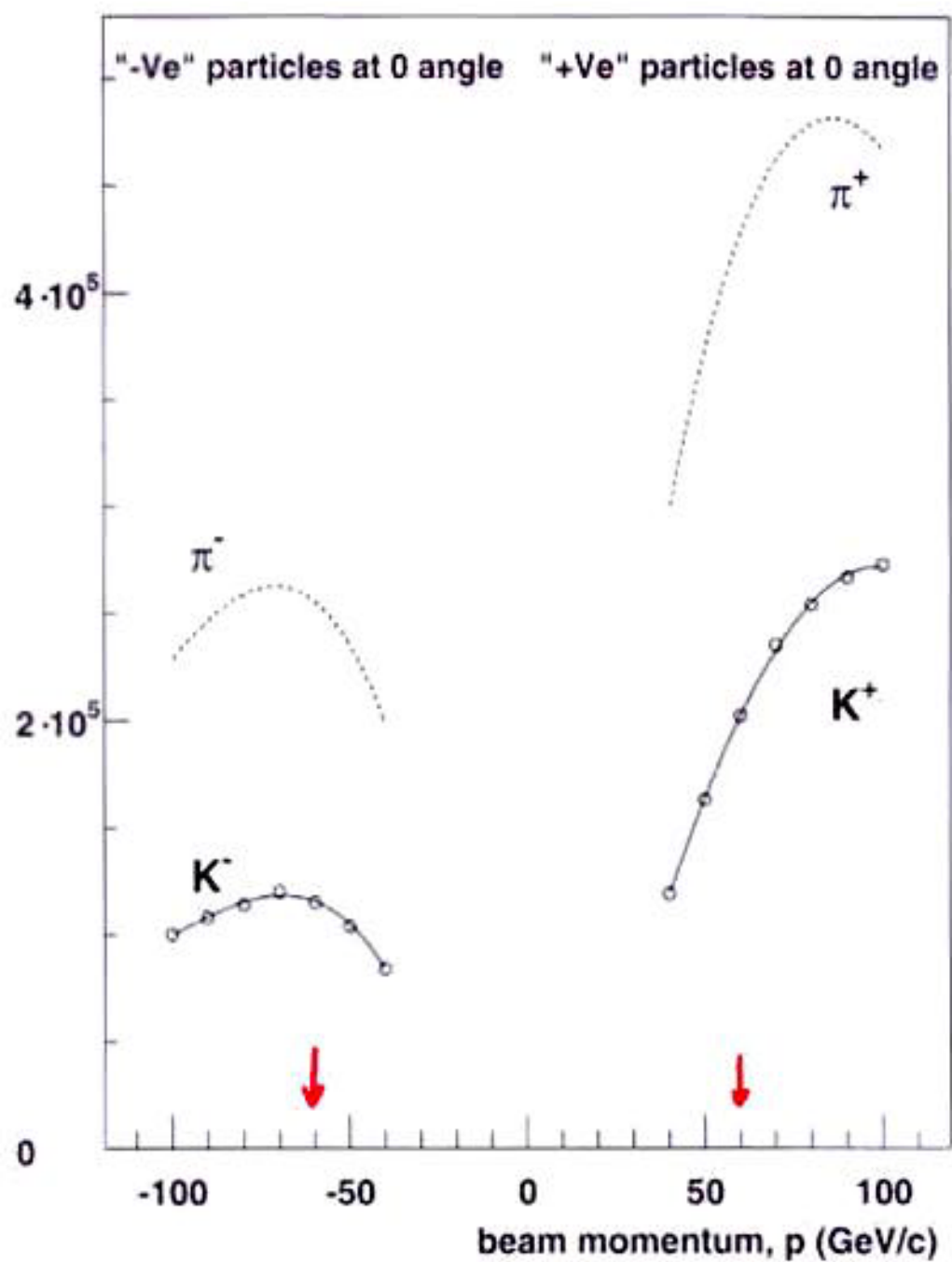


The NA48 Detector



Guidelines of the experiment
that we are proposing ...

- A) the **simultaneous** $K^\pm$ beams,
overlapping in space ; →
- B) the a detector as **symmetric** as possible
around the decay axis ; →
- C) Operate at **alternate magnetic field** in
the spectrometer, to average any residual
acceptance difference for K^+ and K^- ;
- D) Evaluate the ratio $R(x)$ independently
in each $K^\pm$ energy bin .



- The $K^{\pm}$ beams have been optimized to obtain maximum acceptances, given the NA60 detector geometry

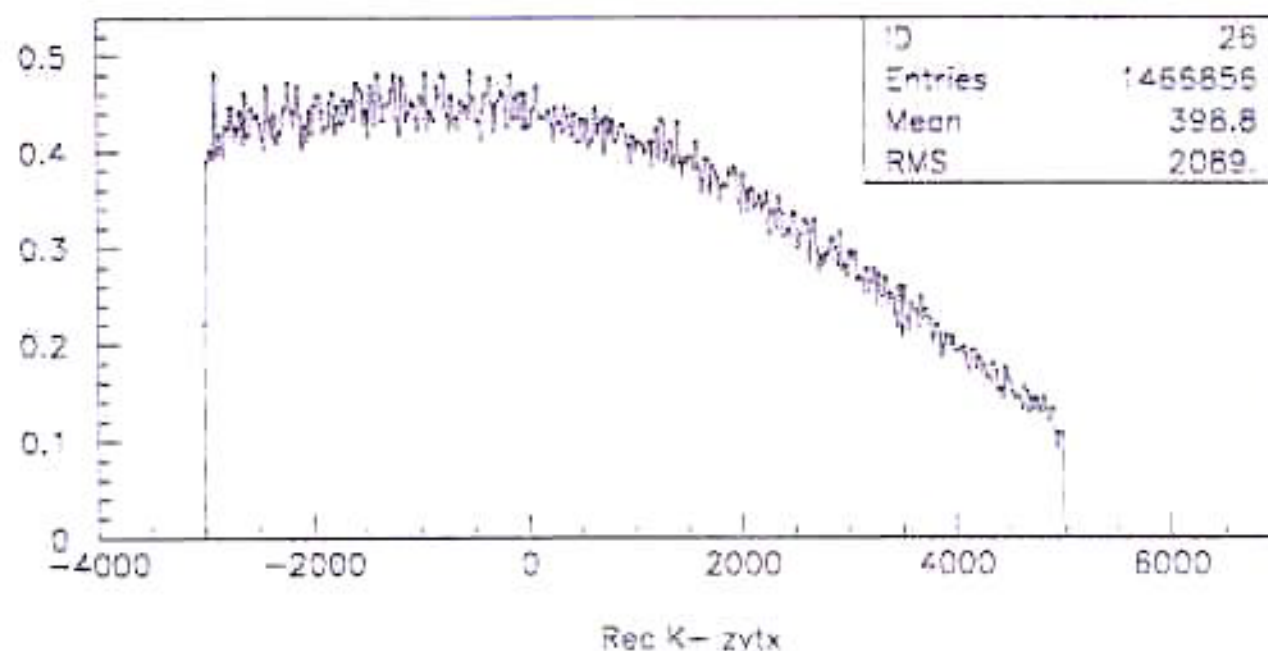
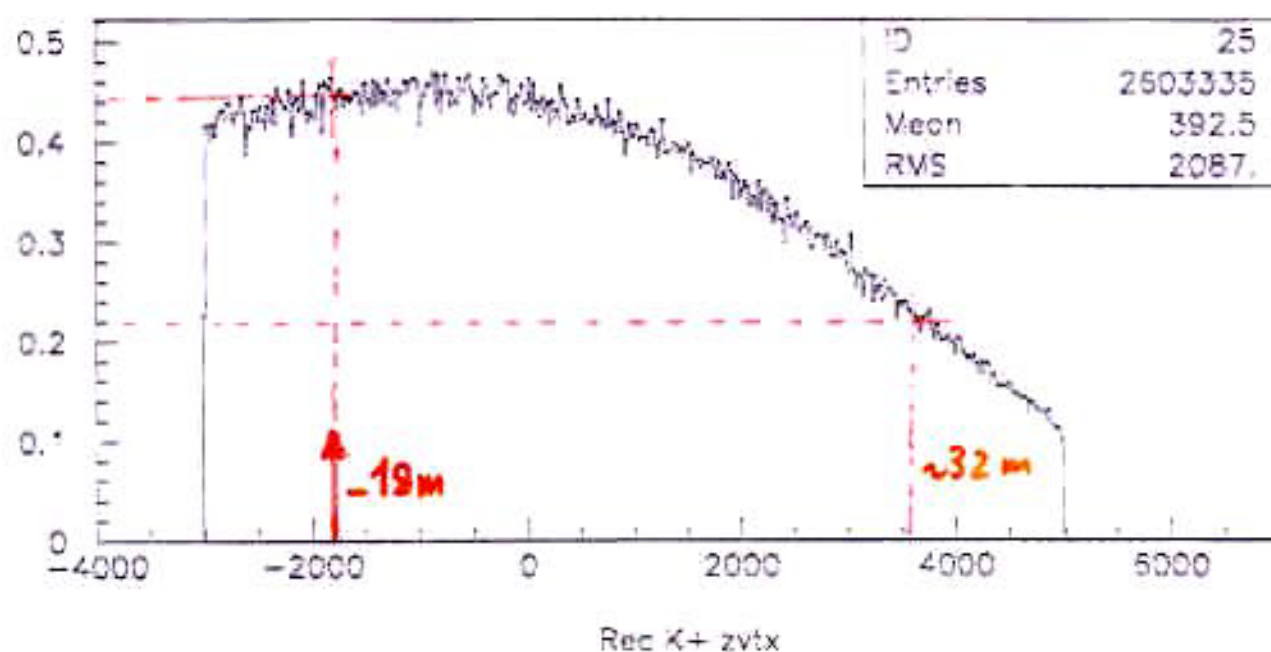


Beam characteristics

Proton energy	400 GeV
Protons per pulse on target	$1. \times 10^{12}$
Production angle	0°
Beam acceptance	± 0.225 mrad
Target-to-first coll. distance	102 m
Decay region	$107 \leq Z \leq 157$ m
Central $K^{\pm}$ energy	60 GeV
Momentum spread	$\Delta p/p = \pm 10\%$
Average acceptance	38 %
Number of $K^{\pm}/K^{\mp}$ reconstructed (per pulse)	<u>5000/3000</u>

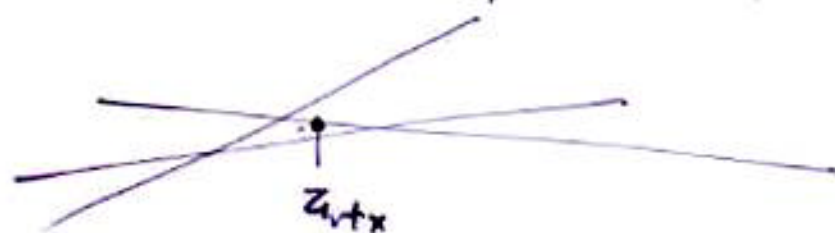
Acceptance @ $E = (60 \pm 6) \text{ GeV}$

99/11/12 10.00



■ Event reconstruction

- i) at least 3 space points at each chamber;
- ii) at least 3 straight lines in the non bending plane;
- iii) a suitable value of the minimum distance in the Transverse plane among the 3 above tracks, as a function of z .



$$CDA \leq 2.5 \text{ cm}$$

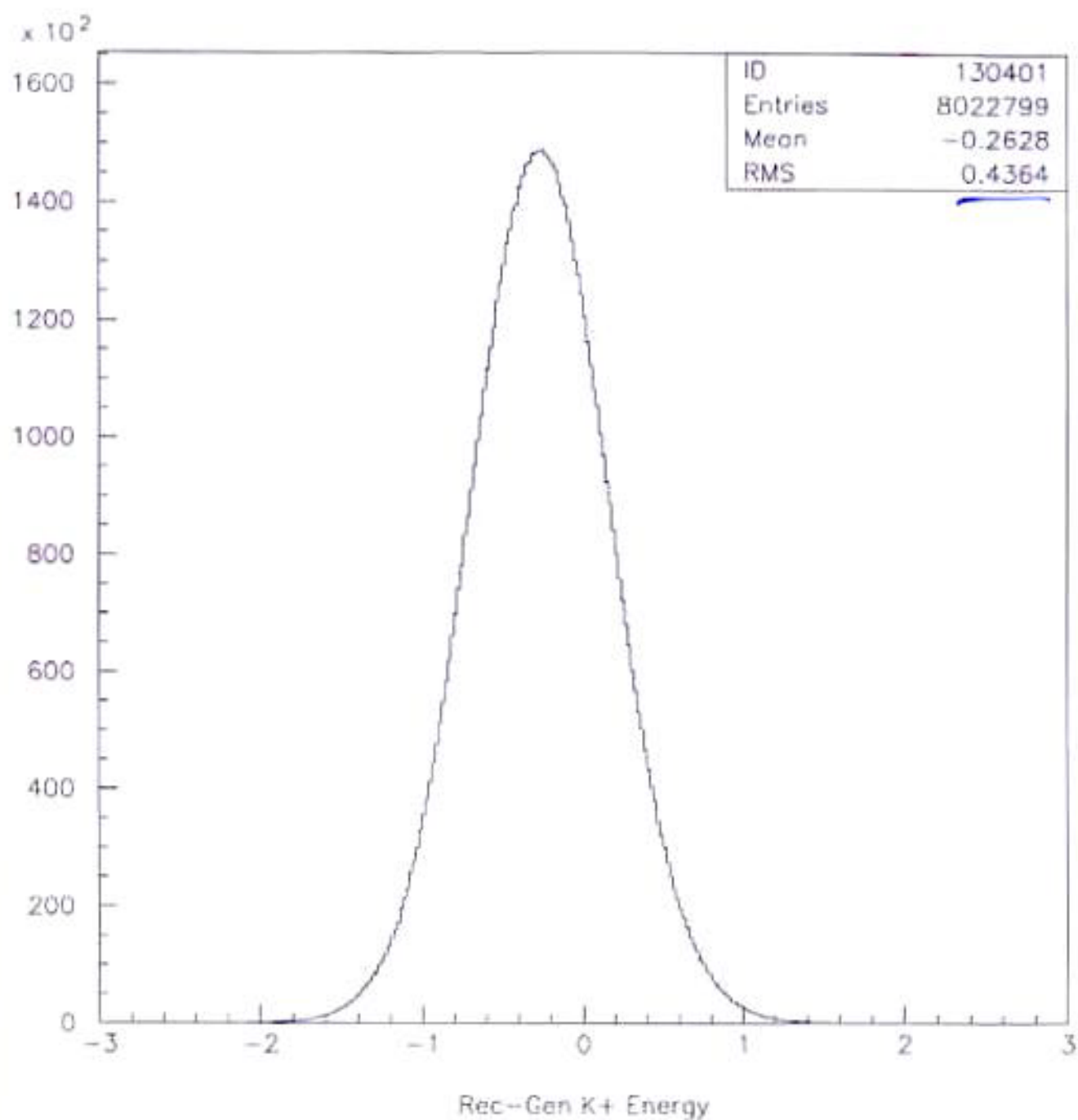
iv) no more hits



-) K mass resolution 1.5 MeV
-) K energy resolution 0.44 GeV (x)
-) z vertex resolution 65 cm
- v) μ resolution 3.3×10^{-2}

106.3

00/05/11 15.37



Systematic uncertainties

B-odd effects:

In principle, the B-odd systematic **cancel**s if both runs ($B\uparrow$ and $B\downarrow$) have been taken with the detector **in the same conditions, i.e.**

- a) with the same B intensity in the spectrometer;
- b) with the same detector efficiencies,
- $\Rightarrow$ reverse the field $\sim$ 8 hours ...

Systematic effects of this type are due, f.i., to

- o) L-R non symmetric chamber efficiency;
- ..) L-R non symmetric trigger efficiency;
- ...) off-axis $K^{\pm}$ beams displacements;
-

B even effects:

We have considered, f.i.

-) different $K^\pm$ acceptances, due to $\neq$ energy spectra
 $\Rightarrow$ need to evaluate $R(u)$ independently, in the various energy bins ... ($\Delta E = \pm 0.5 \text{ GeV}$)
-) Earth magnetic field + residual spurious B fields;
-) different $\pi^\pm \nu$ cross sections;
-) possible chamber inefficiencies **B correlated**;
-) differential backgrounds effects;
 (two close track ch. ineff. ...)
-) punch-through $\pi^\pm$ differential effects;
-) accidental inefficiencies;
-) residual systematic of **B-odd type** due to
 $B^\uparrow \neq B^\downarrow$ (0.5% ...)
- ...

$$\Rightarrow \Delta A_9 < 5 \cdot 10^{-5}$$

Statistical limit

The ratio to be evaluated is

$$R(u_i) = \frac{N^+(u_i)}{N^-(u_i)} = a + b u_i$$

$\uparrow = a \cdot \Delta g$

From the best fit ($\chi^2_{\min.}$) analysis

$$a = \frac{\gamma D - \beta F}{\alpha \gamma - \beta^2} ; \quad b = \frac{\alpha F - \beta D}{\alpha \gamma - \beta^2}$$

$$(\delta a)^2 = \frac{\gamma}{\alpha \gamma - \beta^2} ; \quad (\delta b)^2 = \frac{\alpha}{\alpha \gamma - \beta^2}$$

where

$$\alpha = \sum_i \frac{1}{\sigma_i^2} ; \quad D = \sum_i \frac{R(u_i)}{\sigma_i^2}$$

$$\beta = \sum_i \frac{u_i}{\sigma_i^2} ; \quad E = \sum_i \frac{R^2(u_i)}{\sigma_i^2}$$

$$\gamma = \sum_i \frac{u_i^2}{\sigma_i^2} ; \quad F = \sum_i \frac{u_i R(u_i)}{\sigma_i^2}$$

In our case

$$\sigma_i \approx \frac{N_i^+}{N_i^-} \sqrt{\frac{1}{N_i^+} + \frac{1}{N_i^-}}$$

and, since $b \ll 1 \Rightarrow N_i^+ \approx a N_i^-$ [$a \sim 1.78 \dots$]

$$\Rightarrow \sigma_i \approx (1+a) \sqrt{\frac{a}{N_i}} \quad \text{where } N_i \equiv N_i^+ + N_i^-$$

We obtain ($\mathcal{N}_T \equiv \sum_i N_i$)

$$\alpha = \frac{\mathcal{N}_T}{a(1+a)^2} ; \quad \beta = \frac{\sum u_i N_i}{a(1+a)^2} ; \quad \gamma = \frac{\sum u_i^2 N_i}{a(1+a)^2}$$

$$\Rightarrow (\delta A_g)^2 \approx \left(\frac{\delta b}{a}\right)^2 = \frac{(1+a)^2}{a} \cdot \frac{1}{\mathcal{N}_T \cdot \sigma^2}$$

where σ^2 is the rms of the u -distribution of the $K^+ + K^-$ accepted decays ... [$\sigma \sim 0.57 \dots$]

$$\Rightarrow \boxed{\delta A_g = 10^{-4} \Leftrightarrow \mathcal{N} \sim 7 * 10^9 \text{ decays}}$$

i.e. $\sim 900\,000$ bursts (8000 accept. ev./burst ...)

$\Rightarrow 1.5$ years of data taking

Conclusions

The measurement appears to be, essentially,
statistically limited and it should reach
the interesting sensitivity of

$$\delta A_g \sim 10^{-4}$$

in 1.5 years of data taking.

This would be ~ 50 times better

than the present result $A_g = (-7 \pm 5) \cdot 10^{-3}$

[Ford et al.: Phys. Rev. Lett. 25, 1370 (1970)]

