

Main experimental predictions

in particle colliders

- Longit. TeV dims  $\Rightarrow$  gauge interactions
- Transverse submm dims  $\Rightarrow$  strong gravity
- TeV strings  $\Rightarrow$  Regge excitations, black holes ?

TeV dims: tower of Kaluza-Klein excitations

for SM particles

$$X \equiv X + 2\pi R \quad \Rightarrow \quad p = \frac{n}{R} \quad n=0, \pm 1, \dots$$

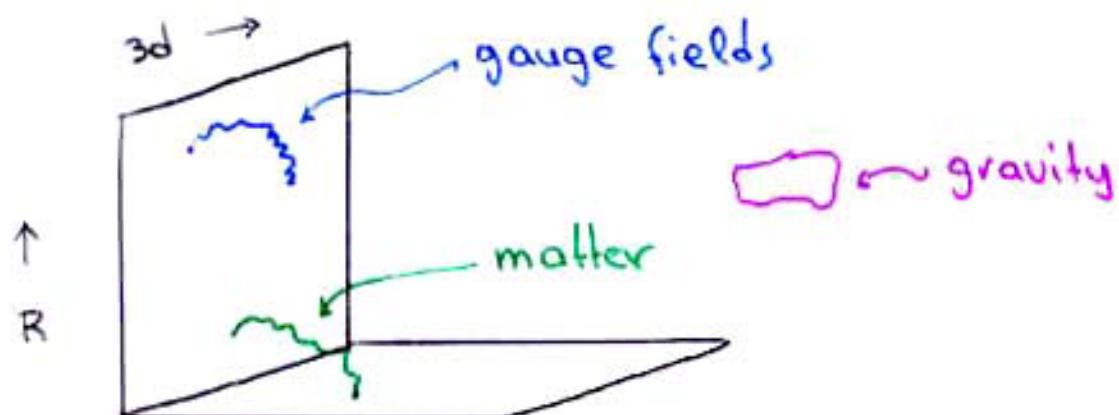
$$m_n^2 = m_0^2 + \frac{n^2}{R^2} \quad R_s^{-1} \lesssim M_S$$

$$\Rightarrow T_n, Z_n, W_n^\pm, G_n^a$$

- In general SM gauge groups on different branes
- Quarks + leptons: on brane intersections
  - localized in 3d  $\rightarrow$  no KK
  - automatic chirality
  - KK of gauge bosons unstable

otherwise KK momentum conservation

$\Rightarrow$  stable charged excitations



similar to  $Z_2$ -orbifolds of heterotic string I.A. '90

I.A. - Benakli '94

## Exp. constraints

- \* equal couplings

$$\begin{array}{c} \text{Diagram: Two fermions } n_1 \text{ and } n_2 \text{ with momenta } -n_1 \text{ and } -n_2 \text{ meeting at a vertex labeled } = g. \\ \text{Diagram: A fermion } f \text{ with momentum } n \text{ and an antifermion } \bar{f} \text{ with momentum } \bar{n} \text{ meeting at a vertex.} \\ \text{Equation: } f = g \delta^{-\frac{n^2}{R^2 M_s^2}} \text{ for } \delta \geq 1. \text{ As } R M_s \rightarrow \infty, \text{ the coupling } \sim g. \end{array}$$

- \* bounds from  $\zeta$ -fermion eff ops (compositeness)

$$\sum_{n \neq 0} \text{Diagram: } n \text{ fermions meeting at a vertex} \approx E \ll R^{-1} \text{ (approximation)} \sim R^2 \sum_{n \neq 0} \frac{1}{n^2}$$

for more than  $d=2$  dims  $\Rightarrow$  regulated sum

$$\Rightarrow \sim R^2 (RM_s)^{d-2} \quad \text{modulo logs for } d=2$$

$$\Rightarrow \boxed{R^{-1} \gtrsim \text{TeV}} \quad \text{up to 2 dims if } RM_s \gg 1$$

I.A.-Benakli '94

high precision of  $Z$ -width +  $G_F \Rightarrow R^{-1} \gtrsim 2.5 \text{ TeV } d=2$

Nath-Yamaguchi  
Masip-Pomarol  
Mesciano

## Experimental constraints

bounds from 4-fermion effective operators (compositeness)

$$\sum_{n \neq 0} \left( \frac{1}{n} \right) \stackrel{\simeq}{=} E \ll R^{-1} \quad \sim R^2 \sum_{n \neq 0} \frac{1}{n^2}$$

more than 2 dims  $\Rightarrow$  regulated sum

$$\Rightarrow \sim R^2 (RM_s)^{d-2} \text{ modulo logs for } d=2$$

$$\Rightarrow R^{-1} \gtrsim \text{TeV} \quad \text{I.A.-Benakli '94}$$

$$\text{high precision of } Z\text{-width + } G_F \Rightarrow R^{-1} \gtrsim 3 \text{ TeV}$$

Nath-Yamaguchi

Masip-Pomarol

Marciano, Strumia

Delgado-Pomarol-Quirós

'99

$$\Rightarrow \text{LHC: production at most one KK resonance} \quad R^{-1} \leq 6 \text{ TeV}$$

I.A.-Benakli-Quirós '94, '99

Nath-Yamada-Yamaguchi

Rizzo-Wells '99

I.A.-Acquando-Benakli

I.A.-Benakli-Quiros '94, '99

$q\bar{q} \rightarrow \Omega_n, Z_n \rightarrow \ell^+ \ell^-$  I.A.-Accomando-Benakli '99

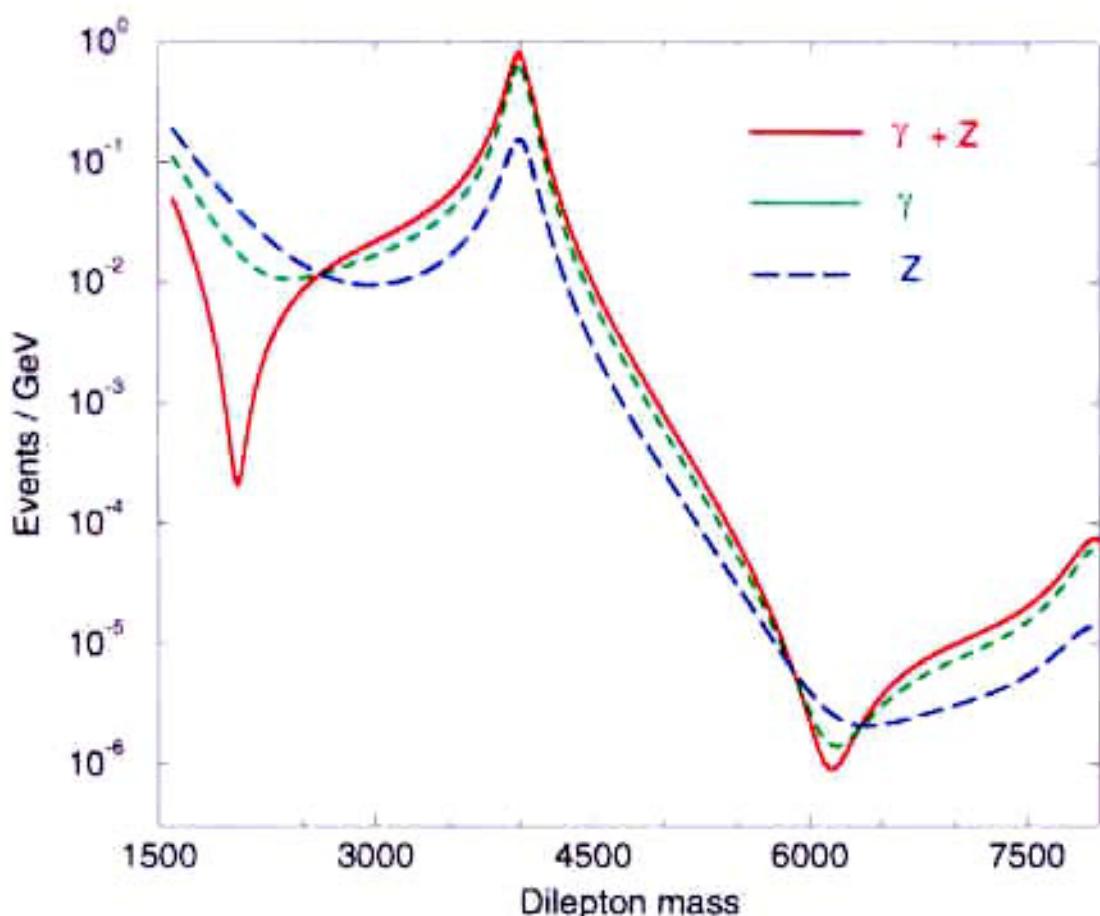


Figure 5: First resonances in the LHC experiment due to a KK excitation of photon and  $Z$  for one extra-dimension at 4 TeV. From highest to lowest: excitation of photon+ $Z$ , photon and  $Z$  boson.

$$Q\bar{Q} \rightarrow W_n^\pm \rightarrow \ell^\pm \nu$$

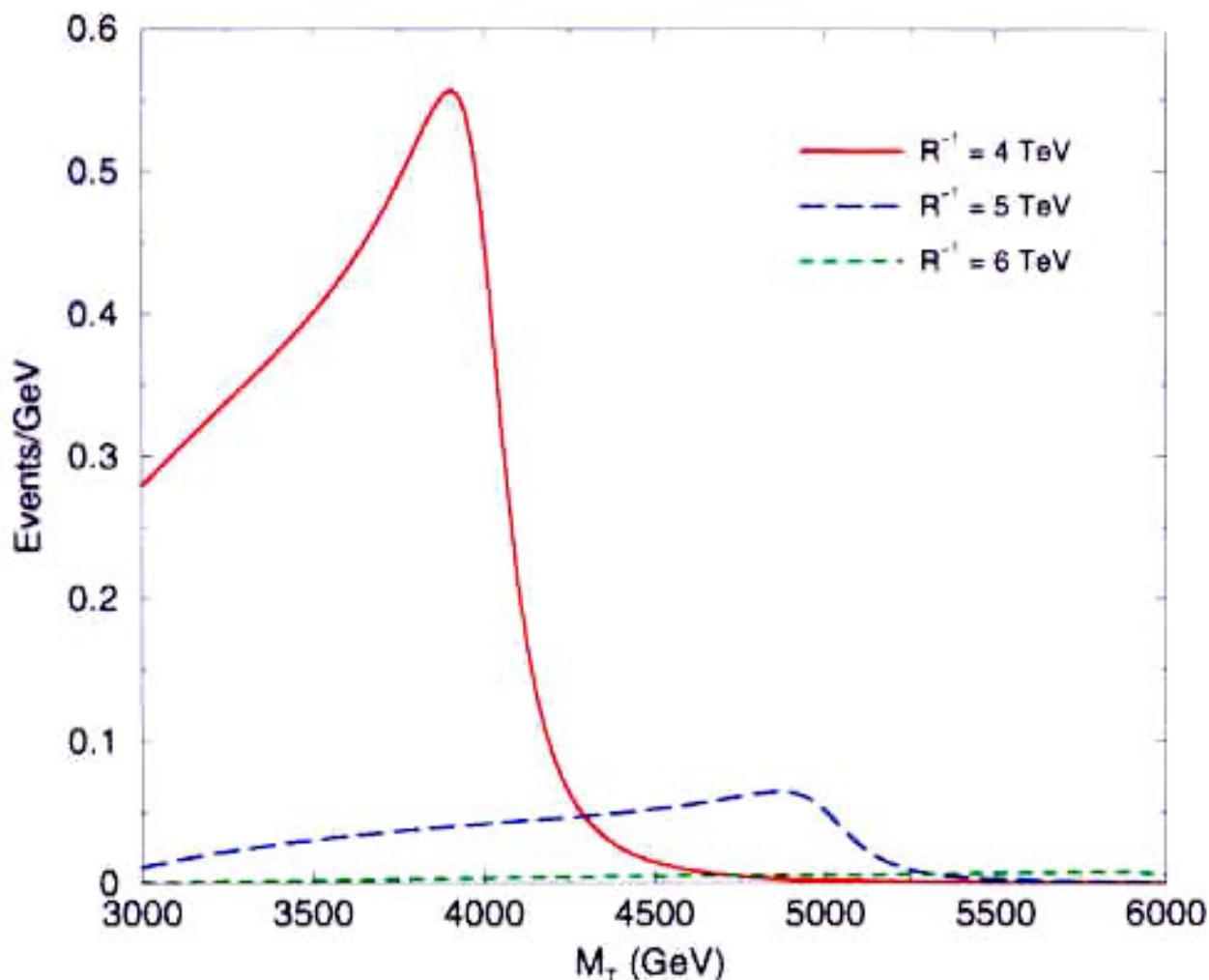


Figure 3: First resonances in the LHC experiment due to a KK excitation of  $W_\pm^{(n)}$  for one extra-dimension at 4, 5 and 6 TeV. We plot the differential cross section as function of the transverse mass for the  $W$ s.

$$q\bar{q} \rightarrow G_u \rightarrow 2 \text{ jets}$$

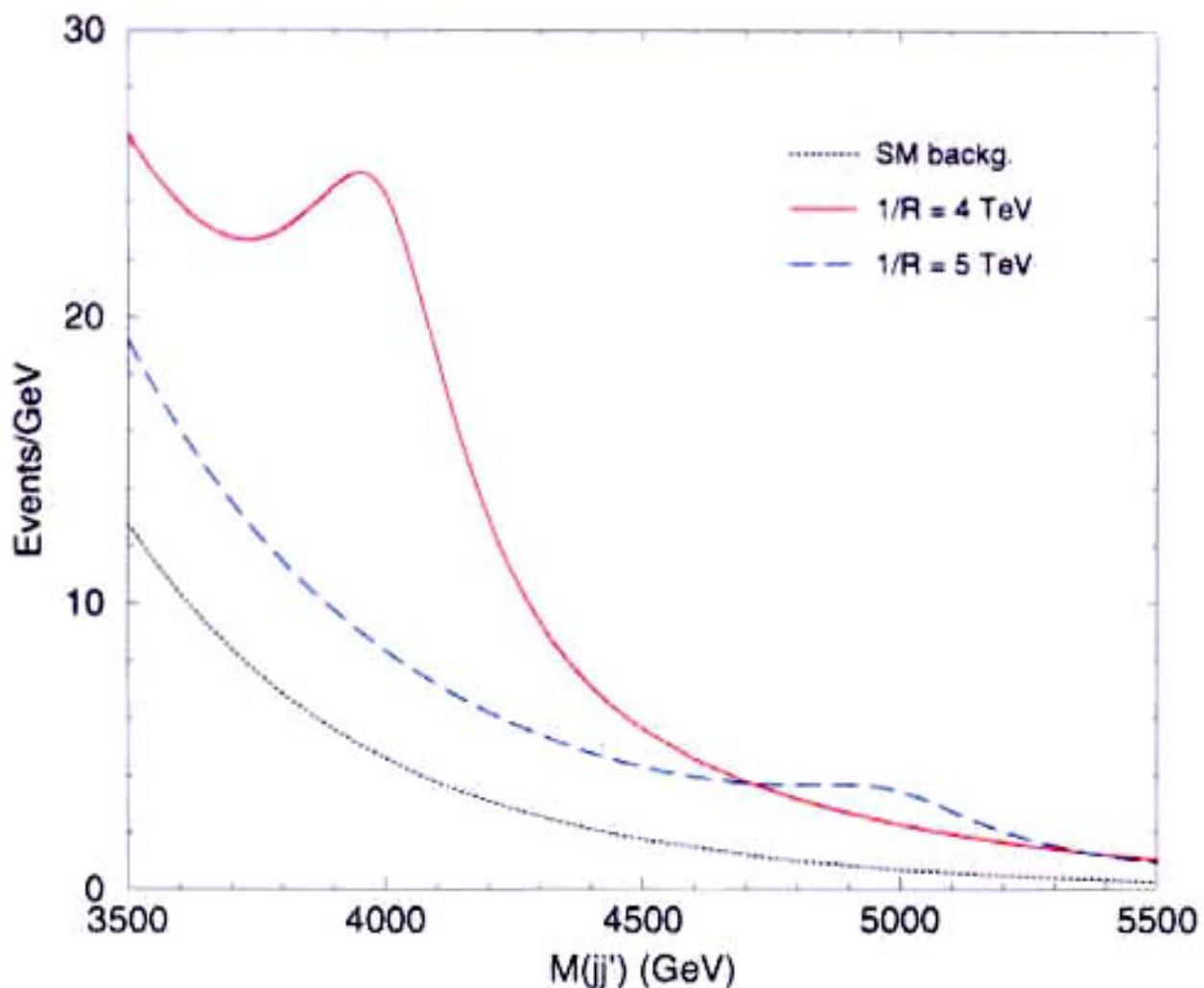


Figure 1: First resonances in the LHC experiment due to a KK excitation of gluon for one extra-dimension at 4 and 5 TeV.

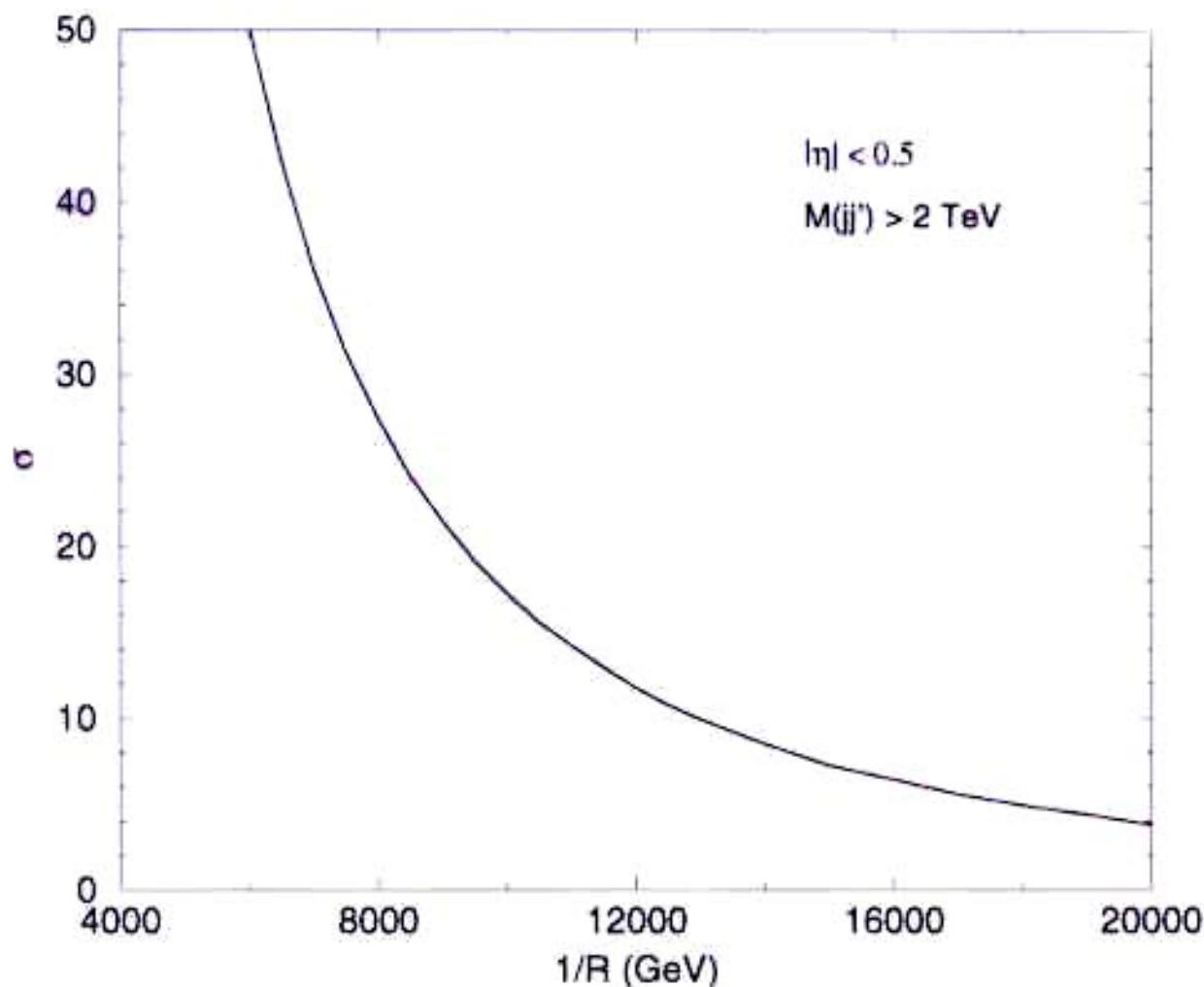


Figure 2: Number of standard deviation in number of observed dijets from the expected standard model value, due to the presence of a TeV-scale extra-dimension of compactification radius  $R$ .

$$R^{-1} \gtrsim 20 \text{ TeV} \quad 95\% \text{ CL}$$

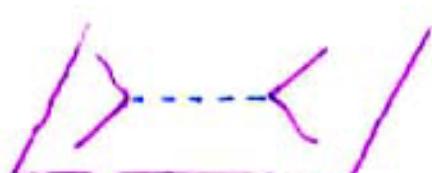
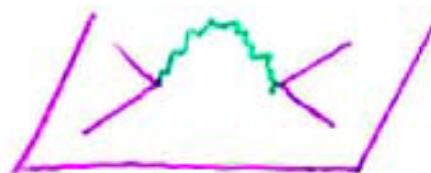
TEVATRON : 4 TeV

If no longitudinal dims with  $R \ll M_I \rightarrow$

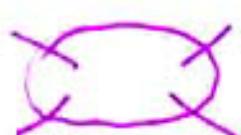
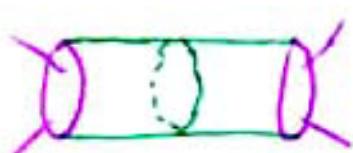
main signal :- graviton emission in the bulk

→ low scale quantum gravity

- indirect effects → probe string modes



Type I string theory: graviton emission subdominant compared to Regge exchanges



1-loop  $\Rightarrow \lambda^2$

disk  $\Rightarrow \lambda$

$\lambda \sim g^2 \Rightarrow$  loop factor enhancement ↑

A-A-B '99

Ullén - Perelstein - Peskin '00

for each KK level.

## A.2 Vertex Feynman Rules

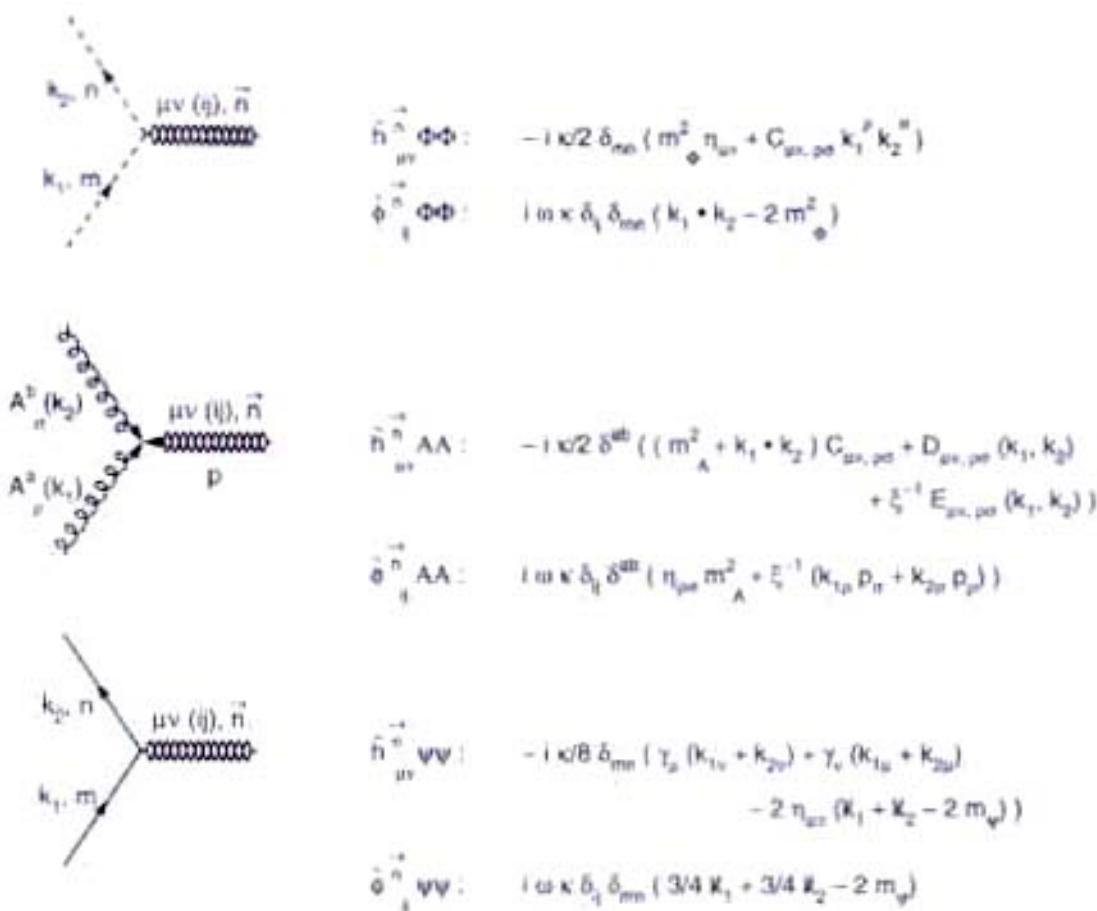


Figure 4: Three-point vertex Feynman rules. The KK states are plotted in double-sinusoidal curves. The symbols  $C_{\mu\nu,\rho\sigma}$ ,  $D_{\mu\nu,\rho\sigma}(k_1, k_2)$  and  $E_{\mu\nu,\rho\sigma}(k_1, k_2)$  are defined in Eqs. (A.10), (A.11) and (A.12) respectively.  $m_\Phi$ ,  $m_A$  and  $m_\psi$  are masses of the scalar, vector and fermion.  $\omega = \sqrt{\frac{2}{3(n+2)}}$ ,  $\kappa = \sqrt{16\pi G_N}$  and  $\xi$  is the gauge-fixing parameter.

In the following we list the complete leading order Feynman rules in three figures, Figs. 4, 5 and 6. Some of the symbols used are defined as follows:

$$C_{\mu\nu,\rho\sigma} = \eta_{\mu\rho}\eta_{\nu\sigma} + \eta_{\mu\sigma}\eta_{\nu\rho} - \eta_{\mu\nu}\eta_{\rho\sigma}, \quad (\text{A.10})$$

$$D_{\mu\nu,\rho\sigma}(k_1, k_2) = \eta_{\mu\nu} k_{1\rho} k_{2\sigma} - [\eta_{\mu\rho} k_{1\nu} k_{2\sigma} + \eta_{\mu\sigma} k_{1\nu} k_{2\rho} - \eta_{\rho\sigma} k_{1\nu} k_{2\rho}] + (\mu \leftrightarrow \nu), \quad (\text{A.11})$$

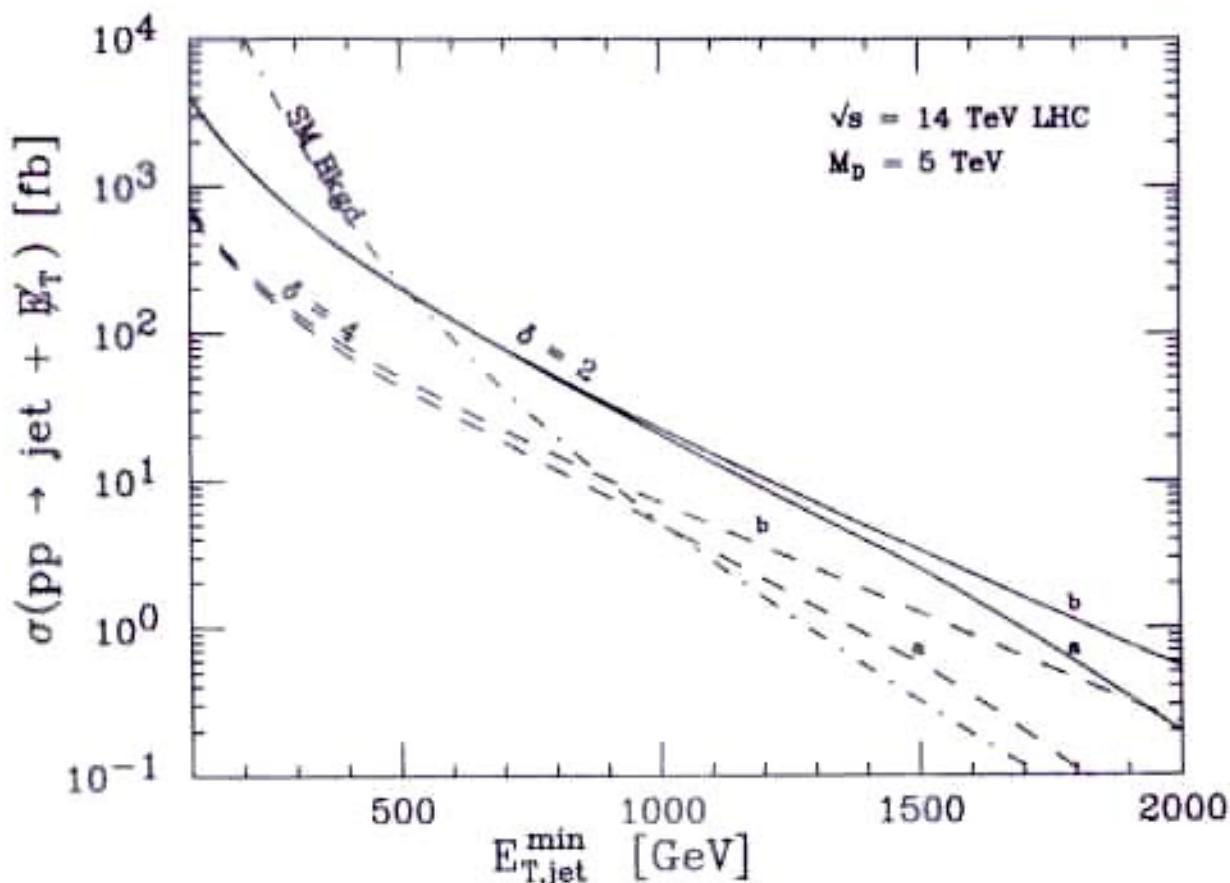
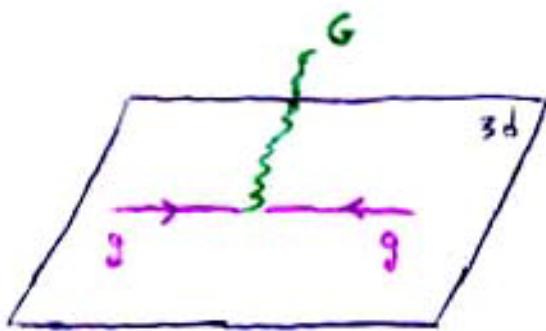
$$pp \rightarrow jet + G$$


Figure 3: The total jet + nothing cross-section at the LHC integrated for all  $E_{T,jet} > E_{T,jet}^{\min}$  with the requirement that  $|\eta_{jet}| < 3.0$ . The Standard Model background is the dash-dotted line, and the signal is plotted as solid and dashed lines for fixed  $M_D = 5 \text{ TeV}$  with  $\delta = 2$  and 4 extra dimensions. The a (b) lines are constructed by integrating the cross-section over  $\hat{s} < M_D^2$  (all  $\hat{s}$ ).

$gg \rightarrow G$



$$\sigma(E) \sim \frac{E^P}{M_I^{P+2}} \frac{\Gamma(1 - 2E/M_I^2)^2}{\Gamma(1 - E^2/M_I^2)^4}$$

- $E < M_I \Rightarrow \sim E^P / M_I^{P+2}$  gravity in 4+p dims
- $E \sim M_I \Rightarrow$  sequence of poles due to RR resonances
- $E > M_I \Rightarrow$  exp decay due to the uv softness of strings

J.A.-Arkani Hamed-Dimopoulos-Dvali '98

$E < M_I$ : reliable computations within eff. field theory

$\Rightarrow$  model independent predictions

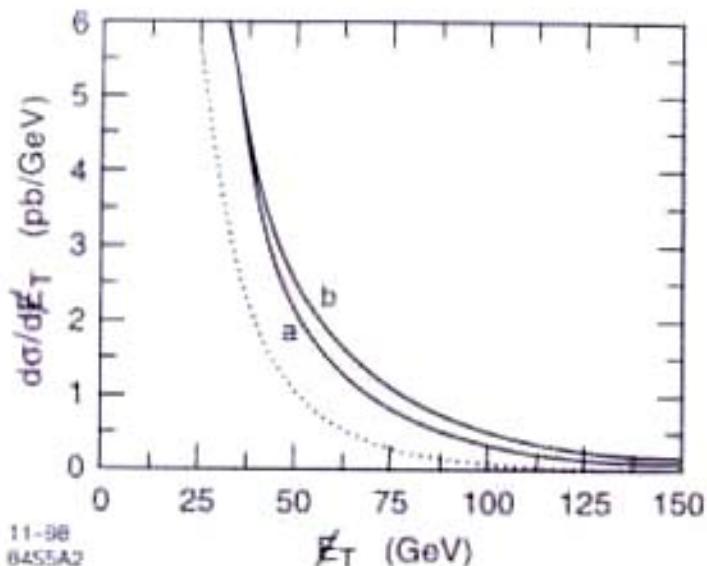
$p\bar{p} \rightarrow \text{jet} + G$ 


Figure 2: Spectrum of missing energy in events with one jet, computed for  $p\bar{p}$  collisions at  $\sqrt{s} = 1.8$  TeV, with a rapidity cut  $|y| < 2.4$ . The dotted curve is the Standard Model expectation. The solid curves show the additional cross section expected in the model of ref. [4] with (a)  $n = 2$ ,  $M = 750$  GeV, (b)  $n = 6$ ,  $M = 610$  GeV.

Current and future limits on  $M_{P(n+4)}$

Collider	$R / M (n = 2)$	$R / M (n = 4)$	$R / M (n = 6)$
Present:	$4.8 \times 10^{-2} / 1200$	$1.9 \times 10^{-9} / 730$	$6.9 \times 10^{-12} / 520$
	$11.0 \times 10^{-2} / 750$	$2.4 \times 10^{-9} / 610$	$5.8 \times 10^{-12} / 610$
Future:	$3.9 \times 10^{-2} / 1300$	$1.4 \times 10^{-9} / 900$	$4.0 \times 10^{-12} / 810$
	$1.2 \times 10^{-3} / 7700$	$1.2 \times 10^{-10} / 4500$	$6.5 \times 10^{-13} / 3100$
	$3.4 \times 10^{-3} / 4500$	$1.9 \times 10^{-10} / 3400$	$6.1 \times 10^{-13} / 3300$

Table 1: Current and future sensitivities to large extra dimensions, expressed as 95% confidence limits on the size of extra dimensions  $R$  (in cm) and the effective Planck scale  $M$  (in GeV). The assumptions of each analysis are explained in the text.

- virtual graviton exchange



$$\lim_{r \rightarrow \infty} \frac{1}{M_P^2} \sum_{\vec{n}} \frac{1}{s - \frac{\vec{n}^2}{r^2}}$$

$$M_P^2 = \frac{1}{g^4} M_I^{2+p} r^p$$

more than 2 dims  $\Rightarrow$  regulated sum

$$\simeq \frac{g^4}{M_I^{2+p} r^{p-2}} \sum_{\vec{n}} \underbrace{\frac{\delta^{-\frac{\vec{n}^2}{r^2} M_I^2}}{\vec{n}^2 - s r^2}}_{\frac{2}{p-2} (r M_I)^{p-2}}$$

$\Rightarrow$  dimension 8 effective operator  $(\bar{\psi} \gamma \psi)^2$ :

$$\frac{g^4}{M_I^4} \cdot \begin{cases} \frac{2}{p-2} & p > 2 \\ \ln \frac{M_I^2}{s} & p = 2 \end{cases}$$

- open string Regge exchanges:  $\frac{g^2}{M_I^4}$  for every  $p$

$\Rightarrow$  stronger limits for  $p > 2$ :  $M_I \gtrsim 1 \text{ TeV}$

Cullen-Perezstein-Pestkin

## Gravity modification at submm scales

1) Change of Newton's law

$$\frac{1}{r^2} \rightarrow \frac{1}{r^2 + p}$$

⋮

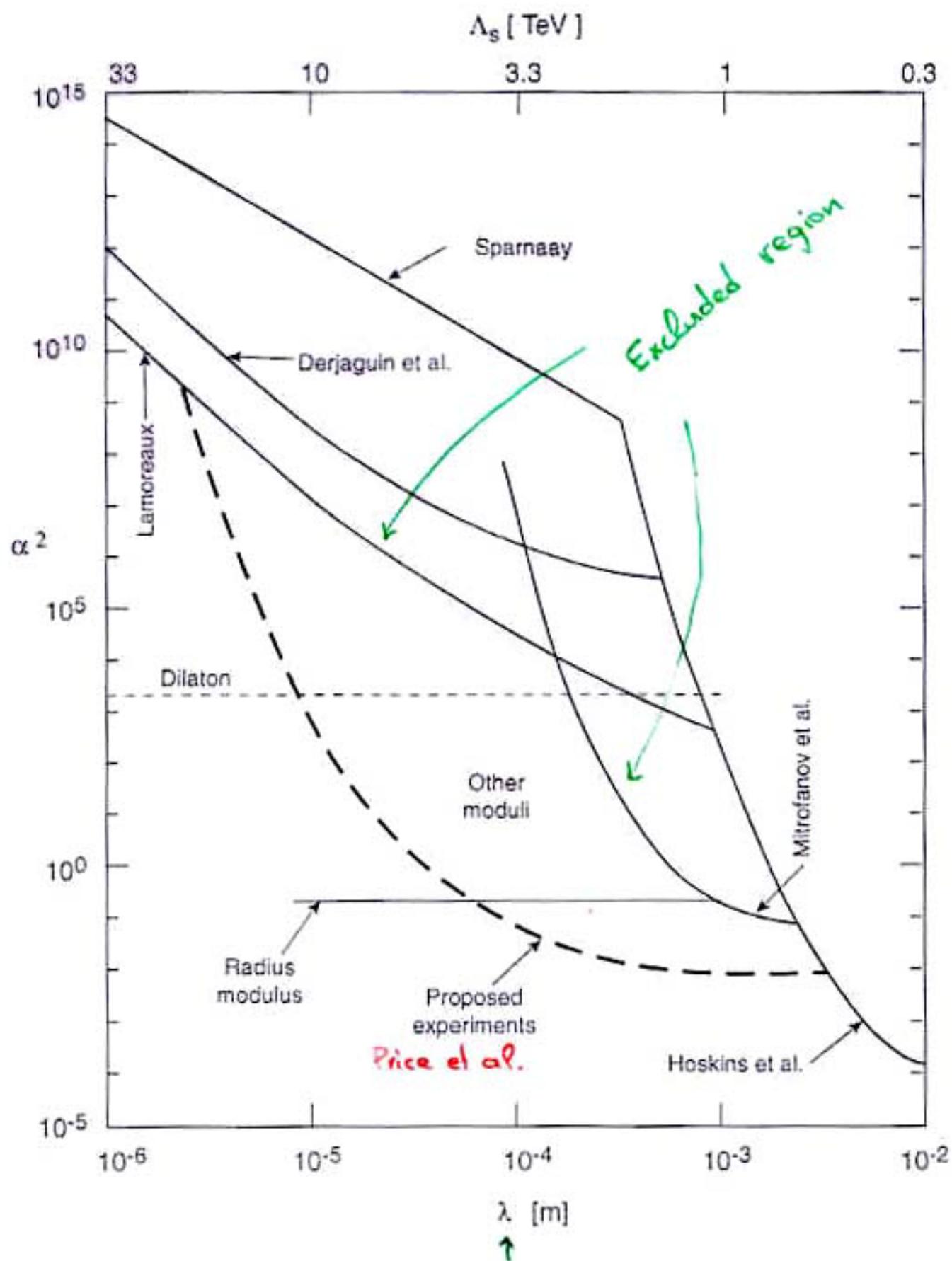
$$p=2 \Rightarrow \frac{1}{r^4} \text{ in (sub)mm} \leftarrow \text{testable}$$
$$p=6 \Rightarrow \frac{1}{r^8} \text{ in (sub)fm}$$

2) susy breaking  $\Rightarrow$  light scalars:  $\frac{(TeV)^2}{M_P} \sim 10^{-6} \text{ eV} = 1 \text{ mm}^{-1}$

(i) primordially on the brane  $\Rightarrow$  suppressed in the bulk

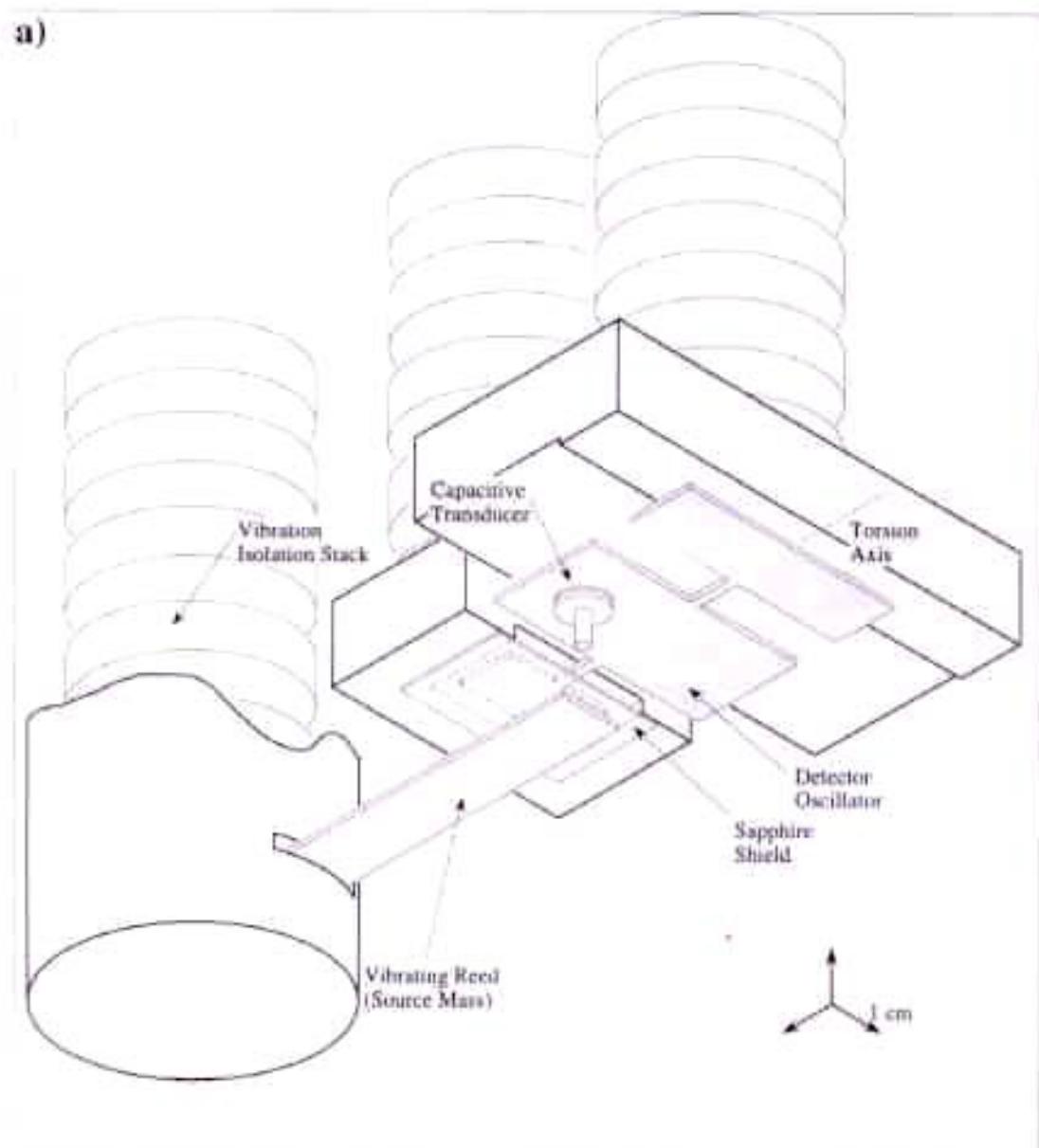
$$\rho_{\text{brane}} \sim M^4 \quad \Rightarrow \quad \rho_{\text{bulk}} \sim M^4 / r^P$$

$$\Rightarrow M_{\text{modulus}}^2 \sim \frac{M^4}{M_P^2} \quad \text{modulus} \equiv \ln r$$



Experimental Status of Gravitational-Strength Forces in the Sub-Centimeter Regime Figure 2

a)



b)



## Gauge hierarchy

$M_p \gg M_\pi \Rightarrow$  why large transverse dims?

$$r M_I \simeq \left( g^2 M_p / M_I \right)^{2/n} \sim \begin{cases} n=2 & 10^{15} \\ n=6 & 10^5 \end{cases}$$

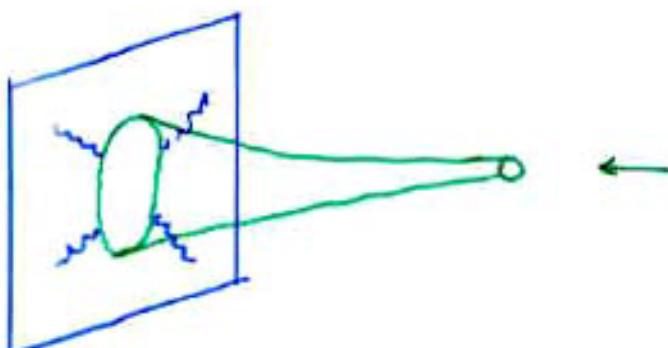
or  $\lambda_{II} \simeq 10^{-14}$

Technical aspect: stability in a non susy vacuum

no large corrections to SM couplings as  $r M_I \rightarrow \infty$

In general no decoupling if massless bulk fields propagate in less than 2 large transv. dims

I.A.-Bachas '98



IR divergence: emission

of massless closed string

UV divergence: open string loop

$\delta_L = \delta$ : linear IR diu  $\Rightarrow$  quadratic UV  $r \sim M_p^2$

Condition: no bulk propagation in one large dim  
or local tadpole cancellation  $\Rightarrow$  severe constraints

$d_s=2$ : log divergences

can be absorbed into a finite number of parameters:

values of bulk massless fields at the brane position

similar to renormalizable field theory

RGE resum  $\rightarrow$  classical 2d eqs in the transverse space

Log dependence  $\Rightarrow$  higher orders irrelevant

$\rightarrow$  hierarchy could be determined by minima SM eff. potential

$\rightarrow$  No susy TeV strings:

some protection of hierarchy as softly susy at TeV

Do we need SUSY if  $M_{\text{str}} \sim \text{TeV}$ ?

Type I: non SUSY string models  $\Rightarrow$

$$\Lambda_{\text{bulk}} \sim M_I^{4+n} \Rightarrow \Lambda_{\text{brane}} \sim M_I^{4+n} r^n \sim M_I^2 M_P^2$$

analog of quadratic div. to  $\Lambda$  in softly broken SUSY

absence of quadratic sensitivity:

-  $\Lambda = 0$  (special models)

$$- \Lambda_{\text{brane}} \sim M_I^4 \Rightarrow \Lambda_{\text{bulk}} \sim M_I^4 / r^n$$

satisfied if approximate SUSY in the bulk

e.g. SUSY is broken primordially only on the brane

explicit realization: Brane SUSY breaking

I.A. - Dudas - Sagnotti '99  
Aldazabal - Uranga '99

No susy in our world (brane)

but it may exist  $\pm$  mm away!

to protect the gauge hierarchy against gravit. corrections

Prediction: possible new forces at submm scales

e.g. light scalars:  $\frac{(TeV)^L}{M_P} \sim 10^{-4} \text{ eV} = 1 \text{ mm}^{-1}$

modulus  $\equiv \ln r$

coupling to nucleons relative to gravity:

$$\frac{\frac{1}{m_N} \frac{\partial m_N}{\partial \ln r}}{\frac{\partial \ln \Lambda_{QCD}}{\partial \ln r}} = \frac{\partial \ln \Lambda_{QCD}}{\partial \ln r} \quad m_N \sim \Lambda_{QCD} \sim e^{-\frac{1}{\Lambda_{QCD}}} \frac{2\pi}{\alpha_{QCD}}$$
$$\sim \frac{\partial}{\partial \ln r} \alpha_{QCD}$$

O(1) in models with log sensitivity in  $r$  e.g.  $d_L = 2$

$\Rightarrow$  can be experimentally tested

Origin of EW symmetry breaking?

mild hierarchy:  $\frac{m_w}{M_s} \lesssim 0(10^{-1})$

string tree-level: -  $m_w = 0$

-  $m_w \sim n M_s \quad n \gtrsim 0(1)$

-  $m_w \sim a \leadsto$  flat direction

⇒ only possibility: radiative breaking

$$Y = \lambda (h^+ h)^2 + \mu^2 (h^+ h)$$

(a)  $\mu = 0$  at tree

$\mu' < 0$  at one loop non susy vacuum

(b)  $\langle h \rangle$  flat at tree

(lifted radiatively) (2 higgses)

Simplest case: one SM higgs on our brane-world  
open string with both ends on the brane  $\Rightarrow$

(1) tree-level potential = same as susy

$$\lambda = \frac{1}{8} (g^2 + g'^2) \quad \text{D-terms}$$

$$(2) \quad b^2 = -\frac{1}{N} g^2 \epsilon^2 M_s^2$$

$N$ : order of the orbifold group

$\epsilon$ : estimated by an explicit computation in  
a toy model

$$\langle b \rangle = (0, v/\sqrt{\epsilon}) : \quad v^2 = -b^2/\lambda \quad \Rightarrow$$

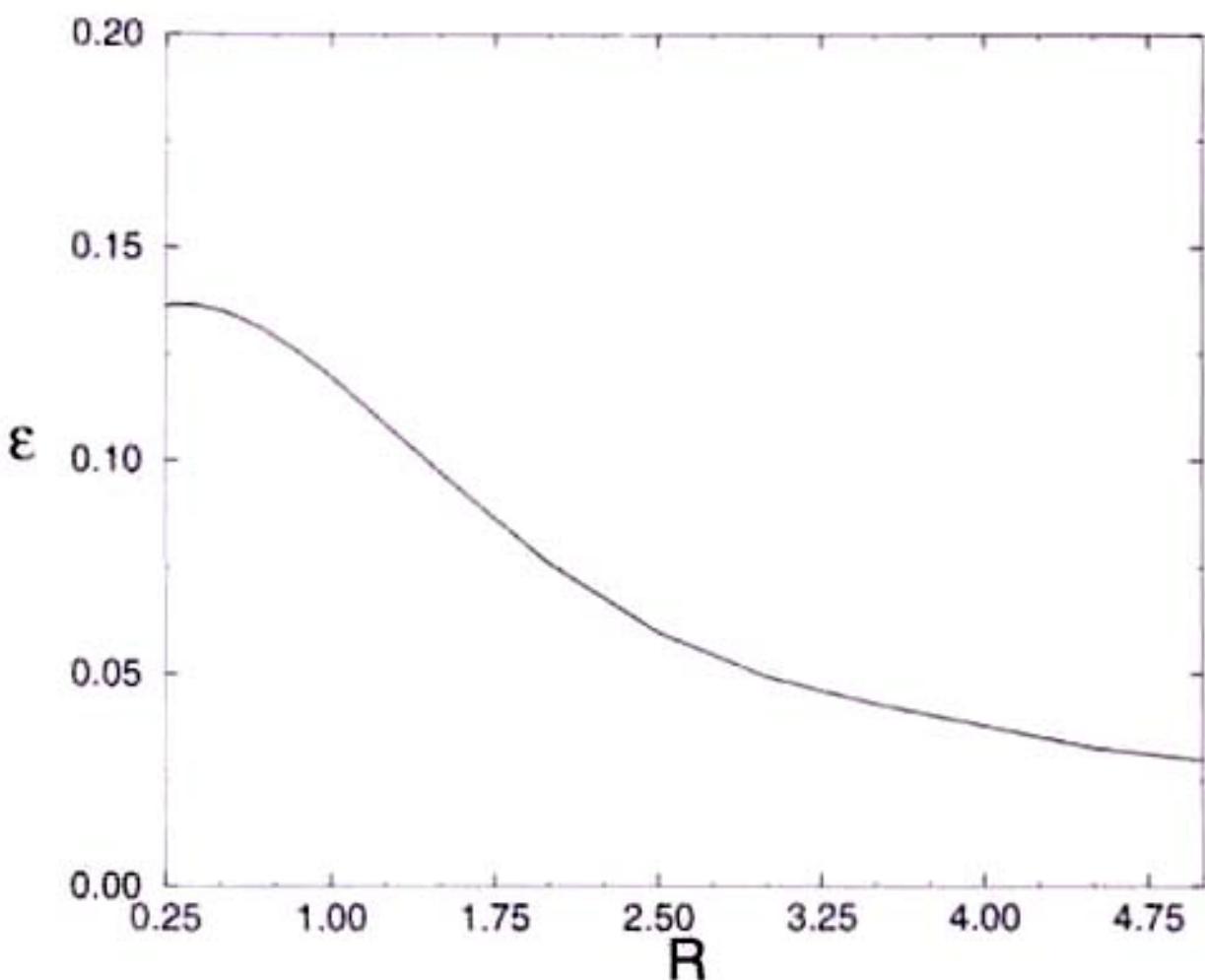
Expansion around the origin

gauge invariance:  $\alpha^2 \rightarrow \text{Tr } \tilde{\Phi}^2$

$$V_{\text{eff}} = V_0 + \frac{1}{2} \mu^2 \text{Tr } \tilde{\Phi}^2 + \mathcal{O}(\tilde{\Phi}^4)$$

$$\mu^2 = -\varepsilon^2(R) g^2 M_s^2$$

$$\varepsilon^2(R) = \frac{R^3}{2n^2} \int_0^\infty \frac{d\ell}{(2\ell)^{5/2}} \frac{\theta_2^4}{4\eta^{12}} \left(i\ell + \frac{1}{2}\right) \sum_n n^2 e^{-2\pi n^2 R\ell}$$



$$(1) \quad M_h = M_Z$$

same as MSSM for  $\tan\beta, m_A \rightarrow \infty$

$$(2) \quad M_s = \frac{M_h \sqrt{N}}{\sqrt{2} g \epsilon}$$

- Low-energy SM radiative corrections top-quark sector

$$\Rightarrow M_h \sim 120 \text{ GeV}$$

$$M_s \sim \text{a few TeV} \quad \mathcal{O}(1-10)$$

- string threshold corrections

- model dependent

- can be very important

e.g. for two large dims in the bulk

$$\ln R_\perp M_s \sim \ln M_p / M_s$$

$\Rightarrow$  both  $M_s$  and  $M_h$  can be increased

Sufficiently low  $M$  allows power-law running

in the region  $R^{-1} \rightarrow M$

number of KK

$$\frac{1}{g_i^L(\mu)} = \frac{1}{g_i^L(R^{-1})} - \frac{b_i^{SM}}{8\pi^L} \ln(\mu R) - \frac{b_i^{KK}}{8\pi^2} \left( 2\mu R - \ln \mu R \right)$$

$N=1$  SUSY  $\Rightarrow$  KK at least  $N=2$

minimal choice: No KK for chiral states

•  $SU(3) \times SU(2) \times U(1)$  1 vector + 2 W-fermions + 2 scalars

• 1 Higgs hypermultiplet 2 fermions + 4 scalars

$\Rightarrow$  approximate unification at weak coupling

Dienes - Dudas - Gherghetta '98

e.g.  $R^{-1} = 2 \text{ TeV} \Rightarrow M \approx 45 \text{ TeV}$  within 2%

however power UV sensitivity  $\Rightarrow$

(string) thresholds are important

Alternative possibility:

Bochas '98

$M_I$  is at TeV but gauge couplings unify at a higher scale due to log sensitivity for  $d_\perp = 2$

$$\ln v M_I = \ln \frac{v M_I^2}{M_I}$$

winding scale:  $v_d^{-1} \equiv v M_I^2 \sim 10^{16}$  GeV for  $\begin{cases} d_\perp = 2 \\ M_I = 10 \text{ TeV} \end{cases}$   
T-dual to  $r^{-\epsilon} \sim \text{mm}^{-1}$

effective "running" in the transverse space (bulk)

however in  $N=1$  orientifolds logs are also controlled by  $N=2$   $\beta$ -functions  $\Rightarrow$  model dependent

I.A.-Bochas-Dubas '99

$$\frac{1}{g_a^2} = \underbrace{\frac{1}{g^2}}_{\text{tree}} + s_a m + \underbrace{\sum_{i=1}^3 \hat{b}_a^i}_{\text{1-loop}} (\ln T_i + f(U_i))$$

- $\frac{1}{g^2}$ : same collection of branes
- $m$ : twisted (blow-up) moduli  
in all examples: anomalous U(1)'s  $\Rightarrow m=0$
- $T = R_1 R_2$        $U = \frac{R_1}{R_2}$       for every torus  $i=1,2,3$

$$R_1 \sim R_2 \rightarrow \infty \Rightarrow b_a \ln R_1 R_2 \quad d_\perp = 2$$

$$R_1 \gg R_2 \Rightarrow \begin{matrix} b_a R_1 / R_2 \\ \uparrow \\ f(U) \sim R_1 / R_2 \end{matrix} \quad d_\perp = 1$$

# A D-brane embedding of the Standard Model

I.A. - Kiritsis - Tomaros hep-ph/0006214

$N$  coincident branes  $\Rightarrow U(N)$

$U(1)$  : coupling =  $g_N / \sqrt{2N}$

with charge of  $\tilde{N} = 1$

$\rightarrow$  gauged "baryon" number

$\Rightarrow$  minimal choice :  $U(3) \times U(2) \times U(1)$

color branes ( $g_3$ )      weak branes ( $g_2$ )       $g_1$

$U(1)$  brane with  $\left\{ \begin{array}{l} U(3) \Rightarrow g_1 = g_3 \\ U(2) \Rightarrow g_1 = g_2 \end{array} \right.$

fermion generation  $U(3) \times U(2) \times U(1)$

$$Q \quad (\mathbf{3}, \mathbf{2}; \mathbf{1}, w, 0)_{\gamma_6} \quad w = \pm 1$$

$$u^c \quad (\bar{\mathbf{3}}, \mathbf{1}; -\mathbf{1}, 0, x)_{-\gamma_3} \quad x = \pm 1 \text{ or } 0$$

$$d^c \quad (\bar{\mathbf{3}}, \mathbf{1}; -\mathbf{1}, 0, y)_{\gamma_3} \quad y = \pm 1 \text{ or } 0$$

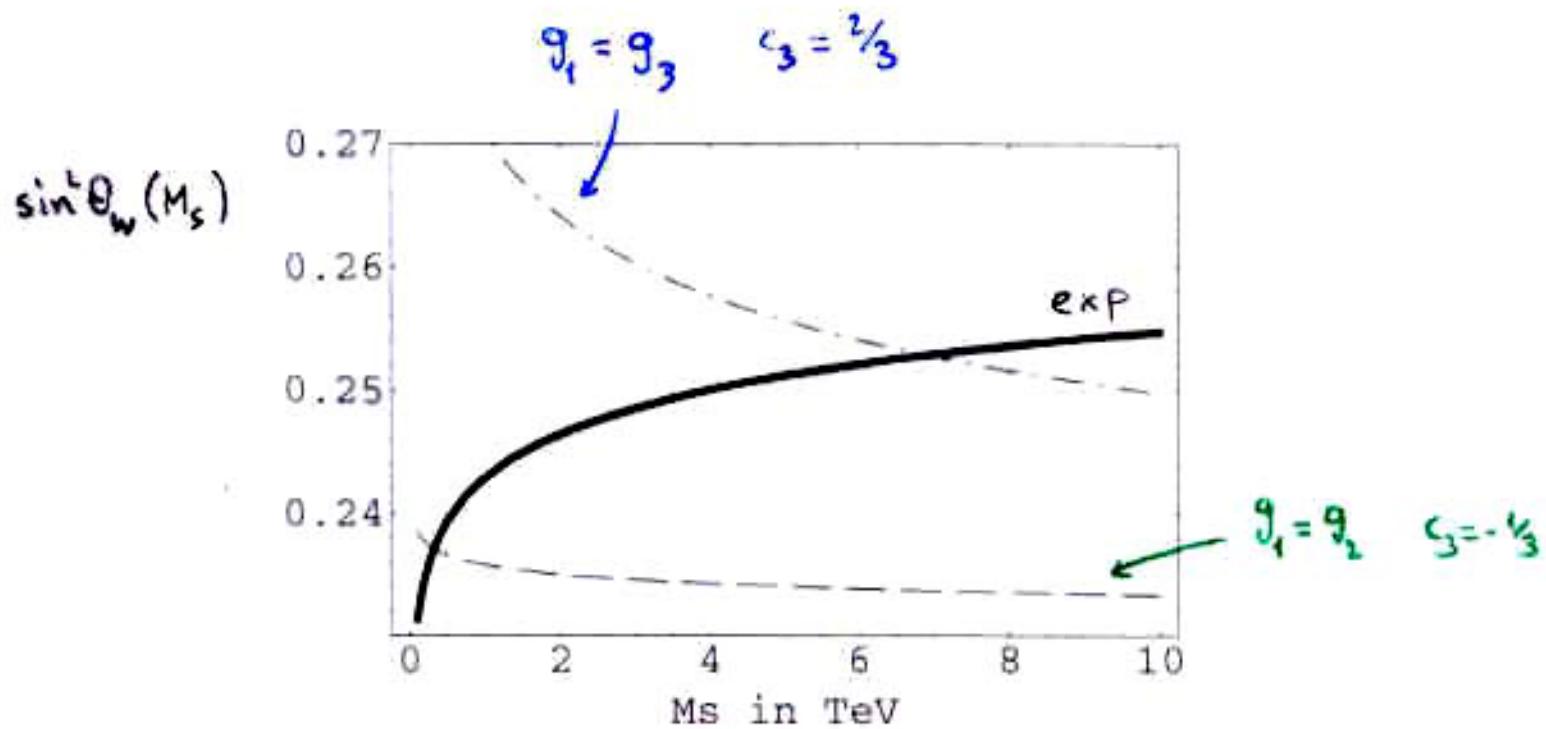
$$L \quad (\mathbf{1}, \mathbf{2}; 0, \mathbf{1}, z)_{-\gamma_2} \quad z = \pm 1 \text{ or } 0$$

$$e^c \quad (\mathbf{1}, \mathbf{1}; 0, 0, 1)_{\gamma_1}$$

hypercharge  $Y = c_1 Q_1 + c_2 Q_2 + c_3 Q_3 \Rightarrow 4 \text{ possibilities}$

$$c_3 = -\frac{1}{3} \quad c_2 = \pm \frac{1}{2} \quad x = -1 \quad y = 0 \quad w = \pm 1 \quad z = -1/0$$

$$c_3 = \frac{2}{3} \quad c_2 = \pm \frac{1}{2} \quad x = 0 \quad y = 1 \quad w = \mp 1 \quad z = -1/0$$



correct prediction for  $\sin^2 \theta_W$  for  $M_s \sim \text{few TeV}$

$U(1)$  with color branes

- masses to all quarks + leptons  $\Rightarrow$  2 Higgs doublets
- the remaining two  $U(1)$ 's : anomalous

Green-Schwarz anomaly cancellation:

shifting of 2 axions  $\Rightarrow U(1)$ 's become massive

$\Rightarrow$  global (perturbative) symmetries:

- baryon number  $\Rightarrow$  proton stability
- PQ-type symmetry  $\Rightarrow$  electroweak axion  
 $\uparrow$   
can be explicitly broken by moving slightly away from the orbifold point

- R-neutrinos: open strings in the bulk

Arkani-Hamed - Dimopoulos - Dvali - March-Russell

Dienes - Dudas - Gherghetta '98

$$\text{Higgs : } c_2 = -\frac{1}{2} \quad H (1, 2; 0, 1, 1)_{\chi_1} \quad H' (1, 2; 0, -1, 0)_{\chi_2}$$

$$H' Q u^c \quad H^+ L e^c \quad H^+ Q d^c$$

$$c_2 = \frac{1}{2} \quad \tilde{H} (1, 2; 0, -1, 1)_{\chi_1} \quad \tilde{H}' (1, 2; 0, 1, 0)_{\chi_2}$$

$$\tilde{H}' Q u^c \quad \tilde{H}^+ L e^c \quad \tilde{H}^+ Q d^c$$

$H' L \nu_R$

$\tilde{H} L \nu_R$

R-neutrinos in the bulk

$$\int d^4x \bar{\nu} \not{D} \nu \quad \nu = (\nu_R, \bar{\nu}_R^c) \Rightarrow$$

$$\int d^4x (r M_s)^p \sum_n \left\{ \bar{\nu}_{Rn} \not{D} \nu_{Rn} + \bar{\nu}_{Rn}^c \not{D} \nu_{Rn}^c + \frac{n}{r} \nu_{Rn} \bar{\nu}_{Rn}^c + c.c. \right\}$$

$$S_{int} = 2 \int d^4x H(x) L(x) \nu_R(x, \vec{y}=0)$$

$$\langle H \rangle = v \Rightarrow \frac{\lambda v}{(r M_s)^p} \sum_n \nu_L \nu_{Rn}$$

$$\frac{\lambda v}{(r M_s)^{p/2}} \ll \frac{1}{r} \Leftrightarrow \frac{\lambda v}{M_s} \ll (r M_s)^{\frac{p}{2}-1} \Rightarrow$$

- $n \neq 0$ : masses of  $\nu_n$  unaffected

- $n=0$ : Dirac mass for neutrino  $m_\nu = \frac{\lambda v}{(r M_s)^{p/2}}$

$$M_P = \frac{1}{g_L} M_s^{1+\frac{p}{2}} r^{\frac{p}{2}} \Rightarrow$$

$$m_\nu = \frac{\lambda}{g_L} v \frac{M_s}{M_P} \sim 10^{-2} \text{ eV} \quad \text{for } M_s \simeq 10 \text{ TeV}$$