Cosmological surveys

Lecture 2

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Cosmology from surveys



Gravitational lensing



Abell 2218 Cluster of galaxies 2 billion light years away, Background galaxies 6 billion light years away

So what's happening?



Assumptions:

- weak field limit v²/c²<<1 •
- stationary field t_{dyn}/t_{cross}<<1 thin lens approximation L_{lens}/L_{bench}<<1 •
- transparent lens
- small deflection angle ٠



Photons travel along null geodesics

Solve for photon path by extremizing the Lagrangian for force-free motion

$$L = \frac{1}{2} g_{\mu\nu} \dot{x}^{\mu} \dot{x}^{\nu}$$

This leads to the following Euler-Lagrange equations

$$\frac{dp_{\mu}}{d\lambda} = \frac{\partial L}{\partial x^{\mu}}; \ p_{\mu} = \frac{\partial L}{\partial \dot{x}^{\mu}}$$

For the weak-field metric

$$ds^{2} = -(1+2\Phi)dt^{2} + (1-2\Phi)d\mathbf{x}^{2}$$

We obtain to first order in ϕ

$$p_{\parallel}^{-1}\frac{dp_{\perp}}{d\lambda} = -2\nabla_{\perp}\Phi\dot{x}_{\parallel}$$



The bend angle depends on the gravitational potential through

$$lpha = rac{2}{c}\int
abla_{ot} \Phi d\ell$$

So the lens equation can be written in terms of a lensing potential

$$\theta_I - \theta_S = \frac{D_{LS}}{D_{OS}} \alpha \equiv \nabla_{\theta} \psi(\theta_I)$$

The lensing will produce a first order mapping distortion (Jacobian of the lens mapping)

$$rac{d heta_S}{d heta_I} = A = egin{pmatrix} 1 - \partial_{xx}\psi & -\partial_{xy}\psi \ -\partial_{xy}\psi & 1 - \partial_{yy}\psi \end{pmatrix}$$



We can write the Jacobian of the lens mapping as

$$A = \begin{pmatrix} 1-\kappa - \gamma_1 & -\gamma_2 \\ -\gamma_2 & 1-\kappa + \gamma_1 \end{pmatrix} = (1-\kappa) \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} + \begin{pmatrix} -\gamma_1 & -\gamma_2 \\ -\gamma_2 & +\gamma_1 \end{pmatrix}$$

In terms of the convergence

$$\kappa = rac{1}{2} [\partial_{xx} \psi + \partial_{yy} \psi]$$

And shear

$$\gamma = (\gamma_1, \gamma_2) = [(\partial_{yy}\psi - \partial_{xx}\psi)/2, \partial_{xy}\psi]$$

 κ represents an isotropic magnification. It transforms a circle into a larger / smaller circle γ Represents an anisotropic magnification. It transforms a circle into an ellipse with axes

$$b = (1 - \kappa + \gamma)^{-1}, \quad a = (1 - \kappa - \gamma)^{-1}$$

Galaxy ellipticities provide a direct measurement of the shear field (in the weak lensing limit)

Need an expression relating the lensing field to the matter field, which will be an integral over galaxy distances χ

$$P_{\kappa}(\ell) = \frac{9\pi}{4\ell} \Omega_m^2 H_0^4 \int_0^{\chi_{\infty}} d\chi \frac{g^2(\chi)}{\chi^2 a^2(\chi)} P_m(\ell/\chi)$$

The weight function, which depends on the galaxy distribution is

$$g(\chi) \equiv 2\chi \int_{\chi}^{\chi_{\infty}} d\chi' \left(1 - \frac{\chi}{\chi'}\right) W(\chi')$$

The shear power spectra are related to the convergence power spectrum by

$$P_{\gamma_1}(\ell, \phi_\ell) = \cos^2(2\phi_\ell) P_\kappa(\ell)$$
$$P_{\gamma_2}(\ell, \phi_\ell) = \sin^2(2\phi_\ell) P_\kappa(\ell)$$

As expected, from a measurement of the convergence power spectrum we can constrain the matter power spectrum (mainly amplitude) and geometry



In practice

- Convergence field can be measured by cross-correlating foreground galaxies with background galaxies
 - expect galaxies to be brighter behind mass concentrations
- Shear field can be measured from galaxy ellipticities •
 - percent level effect •
 - requires accurate knowledge of PSF



Galaxies: Intrinsic galaxy shapes to measured image:







Intrinsic star

(point source)

Gravitaional lensing causes a shear (g)



Atmosphere and telescope

cause a convolution

cause a convolution





Detectors measure a pixelated image

Image also contains noise

Stars: Point sources to star images:





Detectors measure

a pixelated image



Image also contains noise



Intrinsic alignments

- Galaxy formation processes can align galaxies, giving a false shear signal
 - correlations can be galaxy-galaxy
 - correlations can be galaxy-shear
- In general, these have a different dependence with redshift compared with the weak lensing signal itself



Directly depends on the mass distribution







CFHTLenS



CFHT Lensing Survey: 154deg² of deep multi-colour imaging

Recent CFHTLenS results



Heymans et al. 2013; arXiv:1303.1808

Recent CFHTLenS results



Redshift-space distortions

Comoving velocities

Locally, galaxies act as test particles in the flow of matter

On large-scales, the distribution of galaxy velocities is unbiased if galaxies fully sample the velocity field

expect a small peak velocity-bias due to motion of peaks in Gaussian random fields differing from that of the mass



Redshift-Space Distortions

When making a 3D map of the Universe the radial distance is usually obtained from a redshift assuming Hubble's law; this differs from the real-space because of its peculiar velocity:

$$\vec{s}(r) = \vec{r} - v_r(r)\frac{\vec{r}}{r}$$

Where **s** and **r** are positions in redshift- and real-space and v_r is the peculiar velocity in the radial direction

Two key regimes of interest



Fingers-of-God clearly visible in maps



Linear plane-parallel redshift-space

Transition from real to redshift space, with peculiar velocity v in units of the Hubble flow

$$\mathbf{s} = \mathbf{r} + v_{\rm los} \mathbf{\hat{r}}_{\rm los}$$

Jacobian for transformation

$$\frac{d^3s}{d^3r} = \left(1 + \frac{v_{\rm los}}{r_{\rm los}}\right)^2 \left(1 + \frac{dv_{\rm los}}{dr_{\rm los}}\right)$$

Conservation of galaxy number

$$n^{r}(\mathbf{r})d^{3}r = n^{s}(\mathbf{s})d^{3}s \qquad 1 + \delta_{g}^{s} = (1 + \delta_{g}^{r})\frac{d^{3}r}{d^{3}s}\frac{\bar{n}^{r}(\mathbf{r})}{\bar{n}^{s}(\mathbf{s})}$$

Trick to understand velocity field derivative

$$\frac{\partial v_{\rm los}}{\partial r_{\rm los}} = \left(\frac{\partial}{\partial r_{\rm los}}\right)^2 \nabla^{-2} \theta = \left(\frac{k_{\rm los}}{k}\right)^2 \theta = \mu^2 \theta, \ \theta = \nabla \cdot \mathbf{v}$$

Gives to first order

$$\delta_g^s = \delta_g^r - \mu^2 \theta$$

Kaiser 1987, MNRAS, 227, 1

 $\mu = cos(\alpha)$ $\theta = \nabla \cdot \mathbf{u}$

what do linear z-space distortions measure?

linear scales,

$$\delta_{g}^{s}(\mu) = \delta_{g} + \mu^{2}\theta$$

$$P_{g}^{s}(\mu) = \langle |\delta_{g} + \mu^{2}\theta|^{2} \rangle$$

$$= P_{gg} + 2\mu^{2}P_{g\theta} + \mu^{4}P_{\theta\theta}$$
Galaxy-galaxy power
Galaxy-velocity divergence cross power
In linear regime

$$\delta_{g} = b\delta(\text{mass}), \ \theta = -f\delta(\text{mass}), \ f = \frac{d\ln G}{d\ln a}$$
Linear growth rate
So, the simplest model for the power spectrum is

$$P_{g}^{s}(k,\mu) = \left[b + \mu^{2}f\right]^{2}P_{\text{mass}}(k)$$
Kaiser 1987, MNRAS, 227, 1

Modeling redshift space distortions

Include model for both "regimes"

$$P_{g}^{s}(k,\mu) = \left[P_{gg}(k) + 2\mu^{2} P_{g\theta}(k) + \mu^{4} P_{\theta\theta}(k) \right] F(k,\mu^{2})$$

Note that non-linear model is not necessarily more accurate then the linear one. If we assume linear bias

$$P_g^s(k,\mu) = P_m^r(k) \left[b^2 + 2\mu^2 f b + \mu^4 f^2 \right] F(k,\mu^2)$$

On small scales, galaxies lose all knowledge of initial position. If pairwise velocity dispersion has an exponential distribution (superposition of Gaussians), then we get this damping term for the power spectrum.

$$F(k,\mu^2) = (1 + k^2 \mu^2 \sigma_p^2 / 2)^{-1}$$

Modeling redshift space distortions

Alternative for the data is to try to "correct" the data by "collapsing the clusters"

- Velocity dispersion of the Luminous Red Galaxies (LRGs) shifts them along the line of sight by ~ 9 h⁻¹Mpc, and the distribution of intrahalo velocities has long tails.
- Use an asymmetric "friends-offriends" (FOF) finder to match galaxies in the same clusters, and collapse to spherical profile
- Parameters of FOF calculated by matching simulations

Cosmology improved with RSD

- Anisotropic clustering allows huge improvement on w!
- w = -0.95 \pm 0.25 (WMAP + $D_v(0.57)/r_s$)
- w = -0.88 ± 0.055 (WMAP + anisotropic)
- Provided a number of GR tests

The Alcock-Paczynski Effect

The Alcock-Paczynski Effect

- If the Universe is isotropic, clustering is same radial & tangential
- Stretching at a single redshift slice (for galaxies expanding with Universe) depends on
 - H⁻¹(z) (radial)
 - D_A(z) (angular)
- Analyze with wrong model -> see anisotropy
- AP effect measures D_A(z)H(z)
- RSD limits test to scales where can be modeled

Anisotropic BAO fits ...

Anderson et al. 2013; arXiv:1303.4666

Anisotropic BAO fits ...

	$D_{ m A}(z)(r_s^{ m fid}/r_{ m s})$	$H(z)(r_{ m s}/r_{s}^{ m fid})$	$ ho_{D_AH}$
Before Reconstruction			
$(\xi_0(s),\xi_2(s))$	1367 ± 44	86.6 ± 6.2	0.65
$(\xi_{\perp}(s),\xi_{\parallel}(s))$	1379 ± 42	88.3 ± 5.1	0.52
After Reconstruction			
$(\xi_0(s),\xi_2(s))$	1424 ± 43	95.4 ± 7.5	0.63
$(\xi_{\perp}(s),\xi_{\parallel}(s))$	1386 ± 36	90.6 ± 6.7	0.50
Consensus	1408 ± 45	92.9 ± 7.8	0.55

- correlation function is easier to split into line-of-sight and transverse directions
- can decompose into multipoles or other bases (e.g. wedges see Kazin et al. 2013)
- Results are consistent and a concordance value is given

Anderson et al. 2013; arXiv:1303.4666

Anisotropic BAO measurements vs CMB

Can we use the AP effect on small scales?

1.0

use isolated galaxy pairs use voids Marinoni & Buzzi 2011 Lavaux & Wandelt 2011 arXiv:1110.0345 Nature 468, 539 Jennings et al. 2012 MNRAS 420, 1079 02 0.3 0.4 0.5 0.6 0.7 0.8 0.9 0.5 Fiducial ($\Omega_m = 0.3, \Omega_A = 0.7$) 0.4 Best ($\Omega_m = 0.25, \Omega_A = 0.65$) Einstein-de Sitter ($\Omega_m = 1.0, \ \Omega_{\Lambda} = 0$) <sin²(t)> 5'0 Open ($\Omega_{m} = 0.3, \Omega_{h} = 0$) 0.1 0.4 0.3 ≥ 0.2 88 79 72 65 63 42 0.1 2 0.0 $d(h^{-1}Mpc)$ 0.0 0.2 0.6 0.8 1.2 0.4 1.0

z

Both try to isolate objects where the RSD signal is known or weak

Collapsed structures

Live in static region of space-time

Velocity from growth exactly cancels Hubble expansion

Two static galaxies in same structure have same observed redshift irrespective of distance from us

Redshift difference only tells us properties of system

Two collapsed similar regions observed in different background cosmologies give same Δz

No cosmological information from Δz

Cannot be used for AP tests

Belloso et al. 2012: arXiv:1204.5761

Large-scale RSD & AP measurements
Linking z-space distortions and BAO

We should allow for the coupling between the redshift-space distortions and the geometrical squashing caused by getting the geometry wrong. Effects are not perfectly degenerate



Measuring F & $f\sigma_8$



Reid et al. 2012; arXiv:1203.6641

Degradation of RSD measurements by AP effect



BOSS AP & RSD measurement degeneracy



Dotted: free growth, geometry, ACDM prior on large-scale linear P(k) shape at z=0.57

Solid: F forced to match ACDM model

Dashed: WMAP ACDM+GR prediction

Reid et al. 2012; arXiv:1203.6641

BOSS F measurements in context



BOSS RSD measurements in context



Primordial non-Gaussianity

Measuring primordial non-Gaussianity: f_{NL} g_{NL}

δ is sourced from a potential field **Φ**, whose form $\nabla^2 \Phi(\mathbf{x}) = 4\pi G \delta(\mathbf{x})$ might not be Gaussian

$$\Phi(\mathbf{x}) \sim \phi(\mathbf{x}) + f_{NL}\phi^2(\mathbf{x}) + \dots$$

 ϕ is a Gaussian field. the non-linear terms in Φ make Φ non-Gaussian. This map completely specifies Φ statistics.

skewness ~ f_{NL} kurtosis ~ f_{NL}^2

Salopek and Bond 1990; Gangui, Lucchin, Matarrese, Mollerach 1994; Komatsu and Spergel 2001

> skewness ~ 0 kurtosis ~ g_{NL}

 f_{NL} is not the only option for local potential fluctuations ... you can go even further down this route ...

 $\Phi(\mathbf{x}) \sim \phi(\mathbf{x}) + g_{NL}\phi^3(\mathbf{x}) + \dots$

Non-local models introduce non-trivial higher order correlations in $\boldsymbol{\Phi}$

Okamoto and Hu 2002; Enqvist and Nurmi 2005



Measuring non-Gaussianity: halo abundance



Peak-background split bias model



Halo formation much easier with additional long-wavelength fluctuation



Sheth & Tormen 1999, arXiv:9901122



Peak-background split galaxy bias model

This is altered by f_{NL} signal



Peak-background split for non-Gaussianity

Halo formation much easier with additional long-wavelength fluctuation



K² dependence in simulations



Dalal, Doré, Huterer, Shirokov 2007 ; Smith, LoVerde 2010; Smith, Ferraro, LoVerde 2011; Pillepich, Porciani, Hahn 2008; Desjacques, Seljak, Iliev 2008; Grossi et al 2009; Shandera, Dalal, Huterer 2010; Hamaus et al. 2011

Model testing with data

Bayes theory

Modern observational cosmology relies on Bayes theory



e.g. review by Trotta 2008; arXiv:0803.4089

Model parameters (describing LSS & CMB)

content of the Universe total energy density

 $\begin{array}{c} \Omega_{tot} \ (=1?) \\ matter density \\ \Omega_m \\ baryon density \\ \Omega_b \\ neutrino density \\ \Omega_n \ (=0?) \\ Neutrino species \\ f_n \\ dark energy eq^n of \\ state \\ \hline w(a) \ (=-1?) \\ Or \quad W_0, W_1 \end{array}$

perturbations after inflation

scalar spectral index n_s (=1?) normalisation σ_8

running $a = dn_s/dk$ (=0?) tensor spectral index n_t (=0?) tensor/scalar ratio r (=0?) evolution to present day Hubble parameter h Optical depth to CMB

Т

parameters usually marginalised and ignored galaxy bias model galaxy bias model b(k) (=cst?) or b,Q CMB beam error B CMB calibration error C

Assume Gaussian, adiabatic fluctuations

Multi-parameter fits to multiple data sets

- Given CMB data, other data are used to help break degeneracies (although CMB is now doing a pretty good job by itself) and understand dark energy
- Main problem is keeping a handle on what is being constrained and why
 - difficult to allow for systematics
 - you have to believe all of the data!
- Have two sets of parameters
 - those you fix (part of the prior)
 - those you vary
- Need to define a prior
 - what set of models
 - what prior assumptions to make on them (usual to use uniform priors on physically motivated variables)
- Need a sampling method for exploring multi-dimensional parameter space

degeneracies: CMB



degeneracies: CMB



degeneracies: CMB



Bayesian model selection

A lot of the big questions to be faced by future experiments can be reduced to:

Is the most simple model (e.g. Λ) correct?

Bayes theory can test the balance between quality of fit and predictivity

A model with more parameters will always fit the data better than a model with less parameters (provided it replicates the original model).

But does the improvement show the parameter is needed?

$$p(H|d,I) = \frac{p(d|H,I)p(H|I)}{p(d|I)}$$
Bayesian evidence

Bayesian evidence is average of Likelihood under the prior. Splitting into model and parameters

$$p(d|I) = \int_{\theta} p(d|\theta, M) p(\theta|M) d\theta$$

e.g. review by Trotta 2008; arXiv:0803.4089

Bayesian model selection

Bayes factor is ratio of evidence for 2 models

$$B_{01} = \frac{p(d|I_0)}{p(d|I_1)}$$

Jeffries scale

$ \ln B_{01} $	Odds	Probability	Strength of evidence
$< 1.0 \\ 1.0 \\ 2.5 \\ 5.0$	$\lesssim 3:1 \ \sim 3:1 \ \sim 12:1 \ \sim 150:1$	$< 0.750 \\ 0.750 \\ 0.923 \\ 0.993$	Inconclusive Weak evidence Moderate evidence Strong evidence

Problem: depends on prior on new parameter. More stringent criteria can be set

Other options are available ... about a lecture's worth!

e.g. review by Trotta 2008; arXiv:0803.4089

Future surveys: next 4-6 years

Dark Energy Survey (DES)

- New wide-field camera on the 4m Blanco telescope
- Survey started, with first data in hand
- $\Omega = 5,000 \text{deg}^2$
- multi-colour optical imaging (g,r,i,z) with link to IR data from VISTA hemisphere survey
- 300,000,000 galaxies
- Aim is to constrain dark energy using 4 probes LSS/BAO, weak lensing, supernovae cluster number density
- Redshifts based on photometry weak radial measurements weak redshift-space distortions
- See also: Pan-STARRS, VST-VISTA, SkyMapper



DARK ENERGY SURVEY





eBOSS / SDSS-IV

- The new cosmology project with SDSS
- Use the Sloan telescope and MOS to observe to higher redshift
- Basic parameters
 - $\Omega = 1,500 \text{deg}^2 7,500 \text{deg}^2$
 - ~ 1,000,000 galaxies (direct BAO)
 - ~ 60,000 quasars (BAO from Ly-α forest)
- Distance measurements
 - 0.9% at z=0.8 (LRGs)
 - 1.8% at z=0.9 (ELGs)
 - 2.0% at z=1.5 (QSOs)
 - 1.1% at z=2.5 (Ly-α forest, inc. BOSS)
- Survey will start 2014, lasting 6 years
- Received \$10M from Sloan foundation and significant funding from partners



Future surveys: > 4 years

MOS on 4m-telescope

- New fibre-fed spectroscopes proposed for 4m telescopes
 - Mayall (BigBOSS)
 - Blanco (DESpec)
 - WHT (WEAVE)
 - VISTA (4MOST)
- Various stages of planning & funding
 - DESI has DOE CD-1 in April
 - 4MOST chosen by ESO, 1-year delay
 - WEAVE waiting for UK/Spain/Holland/France

DESI

- All capable of observing
 - Ω =5--14,000deg²
 - 2--20,000,000 galaxies (direct BAO)
 - 1--600,000 quasars (BAO from Ly-α forest)
 - Cosmic variance limited to z ~ 1.4



MOS on 10m-telescope

- New fibre-fed spectroscopes proposed for 10m telescopes
 - Hobby-Eberly (HETDEX)
 - Subaru (PFS)
- Different baseline strategies
- HETDEX
 - 420deg² Ly-alpha emitters
 - 800,000 galaxies 1.9<z<3.5
 - Greig, Komatsu & Wyithe, 2012, arXiv:12120977
- PFS
 - 1400deg² ELGs
 - 3,000,000 galaxies 0.6<z<2.4
 - Ellis et al., 2012, arXiv:1206.0737



The ESA Euclid Mission

SURVEYS							
	Area (deg2)		Description				
Wide Survey	15,000 (required)		Step and stare with 4 dither pointings per step.				
	20,000 (goal)						
Deep Survey	40		In at least 2 patches of $> 10 \text{ deg}^2$				
			2 magnitudes deeper than wide survey				
PAYLOAD							
Telescope	1.2 m Korsch, 3 mirror anastigmat, f=24.5 m						
Instrument	VIS	NISP					
Field-of-View	$0.787 \times 0.709 \text{ deg}^2$	$0.763 \times 0.722 \text{ deg}^2$					
Capability	Visual Imaging	NIR Imaging Photometry		NIR Spectroscopy			
Wavelength range	550–900 nm	Y (920-	J (1146-1372	Н (1372-	1100-2000 nm		
		1146nm),	nm)	2000nm)			
Sensitivity	24.5 mag	24 mag	24 mag	24 mag	3 10 ⁻¹⁶ erg cm-2 s-1		
	10σ extended source	5σ point	5σ point	5σ point	3.5σ unresolved line		
		source	source	source	flux		
Detector	36 arrays	16 arrays					
Technology	4k×4k CCD	2k×2k NIR sensitive HgCdTe detectors					
Pixel Size	0.1 arcsec	0.3 arcsec 0.3 arcsec		0.3 arcsec			
Spectral resolution		R=250					
SPACECRAFT							
Launcher	Soyuz ST-2.1 B from Kourou						
Orbit	Large Sun-Earth Lagrange point 2 (SEL2), free insertion orbit						
Pointing	25 mas relative pointing error over one dither duration						
	30 arcsec absolute pointing error						
Observation mode	Step and stare, 4 dither frames per field, VIS and NISP common $FoV = 0.54 \text{ deg}^2$						
Lifetime	7 years						
Operations	4 hours per day contact, more than one ground station to cope with seasonal visibility						
	variations;						
Communications	Communications maximum science data rate of 850 Gbit/day downlink in K band (26GHz), steerable HGA						



The Euclid spectroscopic survey

- Wide survey
 - 15,000deg²
 - 4 dithers
 - NIR Photometry
 - Y, J, H
 - 24mag, 5σ point source
 - NIR slitless spectroscopy
 - 1100-2000nm
 - 3×10⁻¹⁶ergcm⁻²s⁻¹ 3.5σ line flux
 - 3 or 4 dispersion directions, 1 broad wavebands 0.9<z<1.8</p>
 - 45M galaxies
- Deep survey
 - 40deg²
 - 48 dithers
 - 12 passes, as for wide survey
 - dispersion directions for 12 passes >10deg apart



BAO measurements for future surveys



BOSS CMASS DR9 galaxy clustering



Predicted Euclid galaxy clustering



Improvement in precision



... but what about systematics? ...
Testing with subsamples

Testing with blue / red subsamples



Testing with blue / red subsamples



Getting the likelihood right

Getting the likelihood calculation 100% correct

The Likelihood under the standard assumption of a set of data drawn from a multi-variate Gaussian distribution is given by

$$\mathcal{L}(\mathbf{x}|\mathbf{p}, \Psi^t) = \frac{|\Psi^t|}{\sqrt{2\pi}} \exp\left[-\frac{1}{2}\chi^2(\mathbf{x}, \mathbf{p}, \Psi^t)\right],$$

ere $\chi^2(\mathbf{x}, \mathbf{p}, \Psi^t) \equiv \sum_{ij} \left[x_i^d - x_i(\mathbf{p})\right] \Psi_{ij}^t \left[x_j^d - x_j(\mathbf{p})\right].$

now suppose that the covariance matrix (size $n_b \times n_b$) has been calculated from n_s simulations

$$\mu_{i} = \frac{1}{n_{s}} \sum_{s} x_{i}^{s} \qquad C_{ij} = \frac{1}{n_{s} - 1} \sum_{s} (x_{i}^{s} - \mu_{i})(x_{j}^{s} - \mu_{j})$$

then an unbiased estimator of the inverse covariance matrix is

$$\Psi = \frac{n_s - n_b - 2}{n_s - 1} C^{-1}$$

wh

Hartlap J., Simon P., Schneider P., 2007, A&A, 464, 399

Errors in the covariance matrix

Simply providing an unbiased estimator of the inverse covariance matrix is not enough

The inverse covariance matrix also has its own error

$$\langle \Delta \Psi_{ij} \Delta \Psi_{i'j'} \rangle = A \Psi_{ij} \Psi_{i'j'} + B(\Psi_{ii'} \Psi_{jj'} + \Psi_{ij'} \Psi_{ji'}),$$

$$A = \frac{2}{(n_s - n_b - 1)(n_s - n_b - 4)}$$

$$B = \frac{(n_s - n_b - 2)}{(n_s - n_b - 1)(n_s - n_b - 4)}$$

Strictly, we should form a joint likelihood

$$\mathcal{L}(\mathbf{x}, \Psi | \mathbf{p}, \Psi^t) = \mathcal{L}(\mathbf{x} | \mathbf{p}, \Psi) \mathcal{L}(\Psi | \Psi^t)$$

If we don't, this leads to an additional error on the np parameters being fitted

$$\langle p_{\alpha} p_{\beta} \rangle |_{s.o.} = B(n_b - n_p) F_{\alpha\beta}^{-1},$$

Taylor et al., 2012, arXiv:1212.4359; Dodelson & Schneider 2007, arXiv:1212.4359

Errors in likelihood calculations

Given a set of mocks, we can form two possible estimates of the errors:

- 1. From the individual likelihood surface from each mock
- 2. From the distribution of recovered measurements from the set of mocks

These should agree!

The estimates from each are biased in subtly different ways gives errors in the covariance matrix



Application to BOSS



Percival et al., 2013: arXiv:1312.4841

Getting the model right

BAO from simulations



BAO from simulations



What will you be showing in 15 years time?

At the same time as my PhD



Photo: U. Montan
Saul Perlmutter

Photo: U. Montan

Brian P. Schmidt



The Nobel Prize in Physics 2011 was divided, one half awarded to Saul Perlmutter, the other half jointly to Brian P. Schmidt and Adam G. Riess *"for the discovery of the accelerating expansion of the Universe through observations of distant supernovae"*.

SDSS-II LRG BAO vs other data



Euclid BAO predictions



Cosmology from surveys

