

Beyond the Standard Model: the LHC reach

XIV Frascati Spring School "Bruno Touschek"



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BSM: the LHC reach

- Higgs mechanism. SM Higgs.
- EW precision tests. The Higgs as a UV moderator of EW interactions. Needs for New Physics beyond the Higgs.
- Review of possible scenarios: Little Higgs, Gauge-Higgs Unification, (5D) Higgsless models, Composite Higgs.

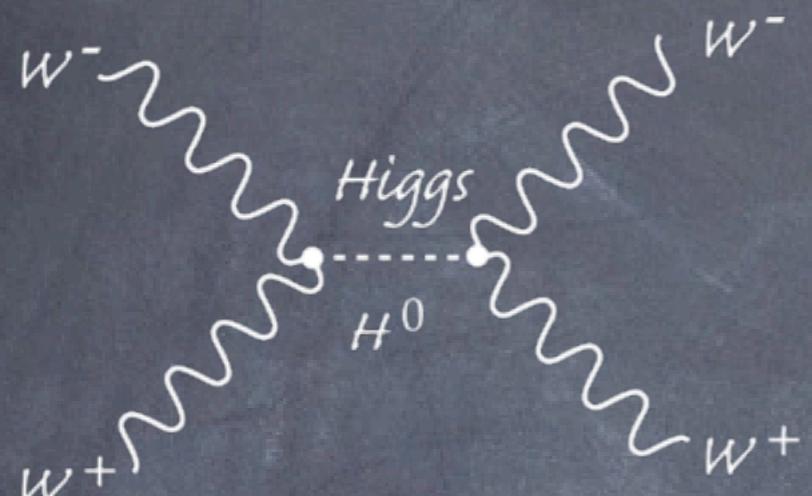
$$E = \hbar\nu$$

$$\mathcal{R}_{\mu\nu} - \frac{1}{2}\mathcal{R}g_{\mu\nu} = 16\pi G T_{\mu\nu}$$

Composite Higgs Models

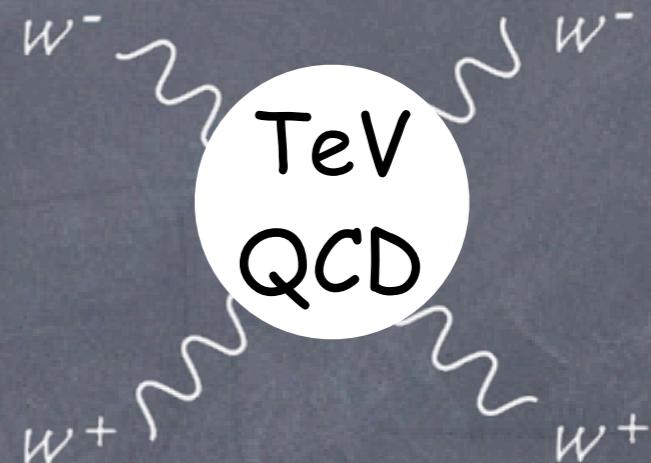
Drawbacks of Usual Approaches

Weakly coupled models



prototype: Susy
susy partners ~ 100 GeV

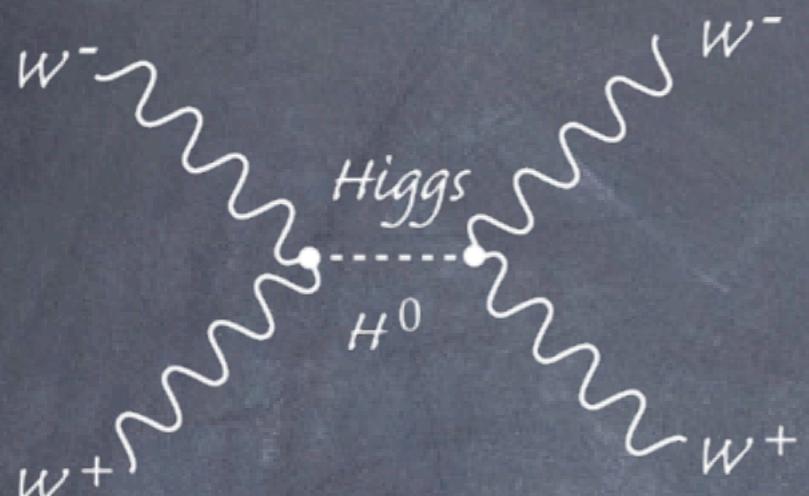
Strongly coupled models



prototype: Technicolor
rho meson ~ 1 TeV

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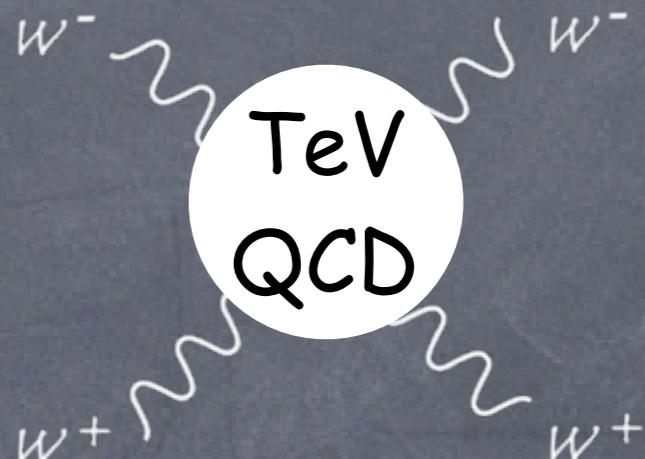
need new particles to stabilize
the Higgs mass

bounds on the masses of these particles



fine-tuning $O(1\%)$

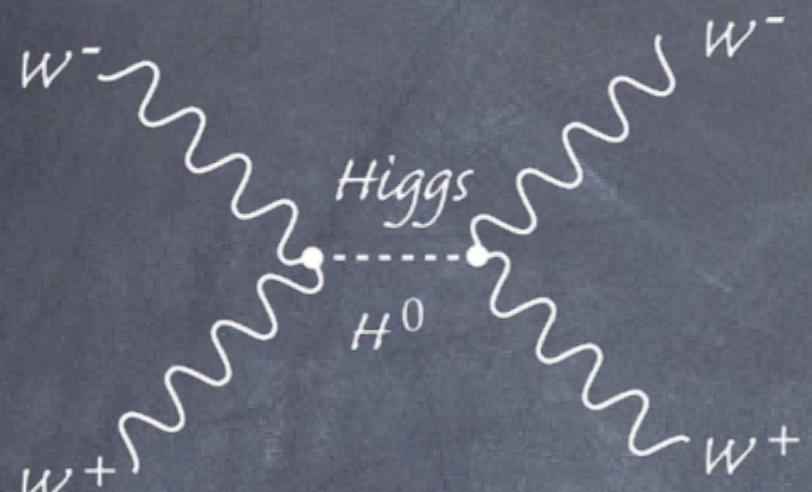
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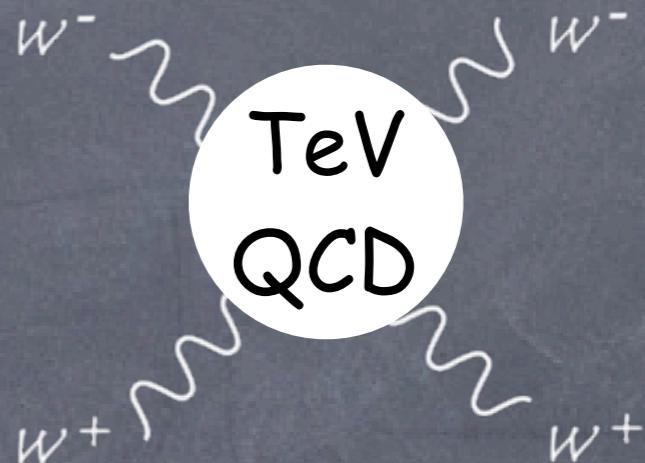
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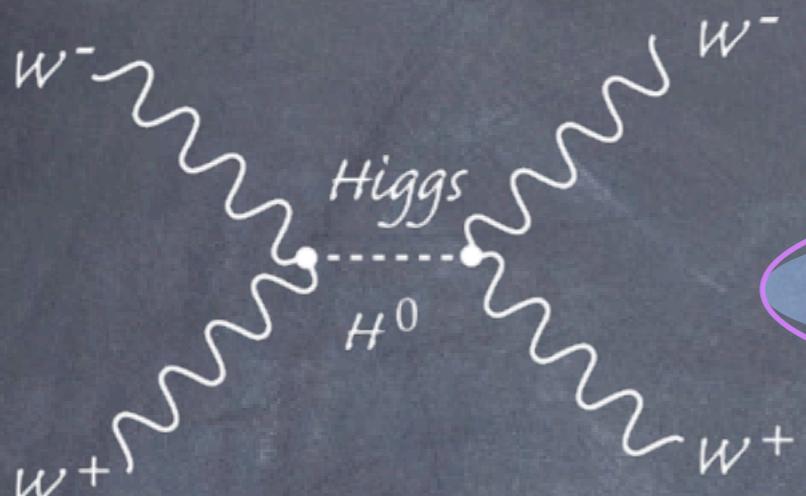
resonances needed for
unitarization generate EW
oblique corrections

$$\hat{S} \sim \frac{m_W^2}{m_\rho^2} \quad |\hat{S}| < 10^{-3}$$

$\xrightarrow{\text{@ 95% CL}}$ $m_\rho > 2.5$ TeV

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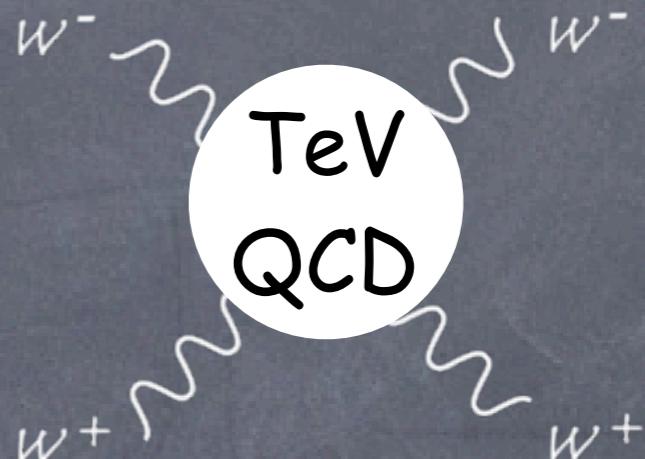
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Scattering amplitudes

non-linear realization of the gauge symmetry

W_L, Z_L are Goldstone bosons \sim pions of QCD

$$\Sigma = e^{i\sigma^a \pi^a/v} \quad \text{2x2 matrix: } \pi^a \sim W_L, Z_L \quad \Sigma \rightarrow SU(2)_L \cdot \Sigma \cdot U(1)_Y$$

$$\mathcal{L}_{\text{mass}} = \frac{v^2}{4} \text{Tr} \left(D_\mu \Sigma^\dagger D_\mu \Sigma \right)$$

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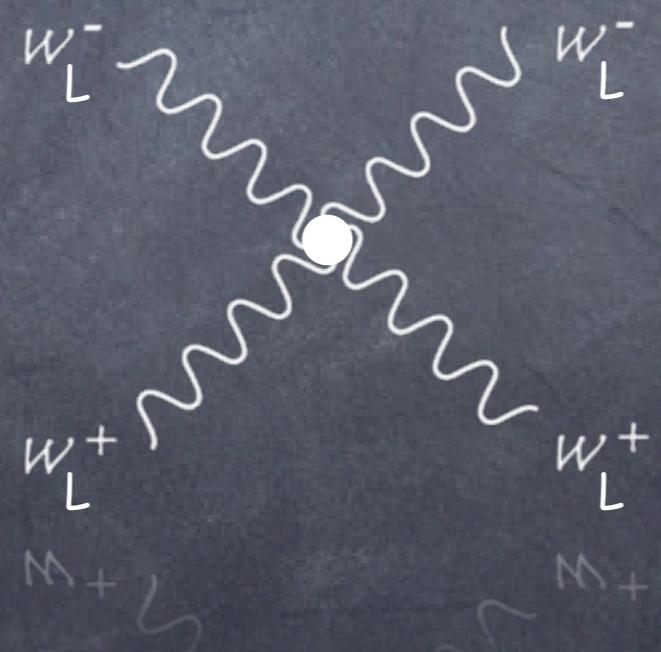
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bad behavior of scattering amplitudes

$$\epsilon_l = \left(\frac{|\vec{k}|}{M}, \frac{E}{M} \frac{\vec{k}}{|\vec{k}|} \right)$$

scattering of W_L

scattering of QCD pions
(Goldstone equivalence theorem)



$$\mathcal{A} = g^2 \left(\frac{E}{M_W} \right)^2$$

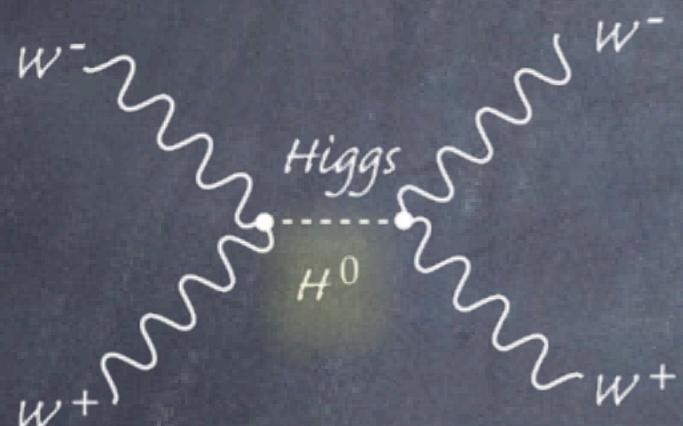
loss of perturbative unitarity
around 1.2 TeV

SM Higgs as a peculiar scalar resonance

A single scalar degree of freedom with no charge under $SU(2)_L \times U(1)_Y$

$$\mathcal{L}_{\text{EWSB}} = a \frac{v}{2} h \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma) + b \frac{1}{4} h^2 \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma)$$

'a' and 'b' are arbitrary free couplings



$$\mathcal{A} = \frac{1}{v^2} \left(s - \frac{a^2 s^2}{s - m_h^2} \right)$$

growth cancelled for
 $a = 1$
restoration of
perturbative unitarity

For $b = a^2$: perturbative unitarity also maintained in inelastic channels

— 'a=1' & 'b=1' define the SM Higgs —

$\mathcal{L}_{\text{mass}} + \mathcal{L}_{\text{EWSB}}$ can be rewritten as $D_\mu H^\dagger D_\mu H$

$$H = \frac{1}{\sqrt{2}} e^{i\sigma^a \pi^a/v} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

h and π^a (ie W_L and Z_L) combine to form a linear representation of $SU(2)_L \times U(1)_Y$

Unitarity with Composite Higgs

Technicolor: W_L and Z_L are part of the strong sector

Higgs = composite object (part of the strong sector too)
its couplings deviate from a point-like scalar

Georgi, Kaplan '84

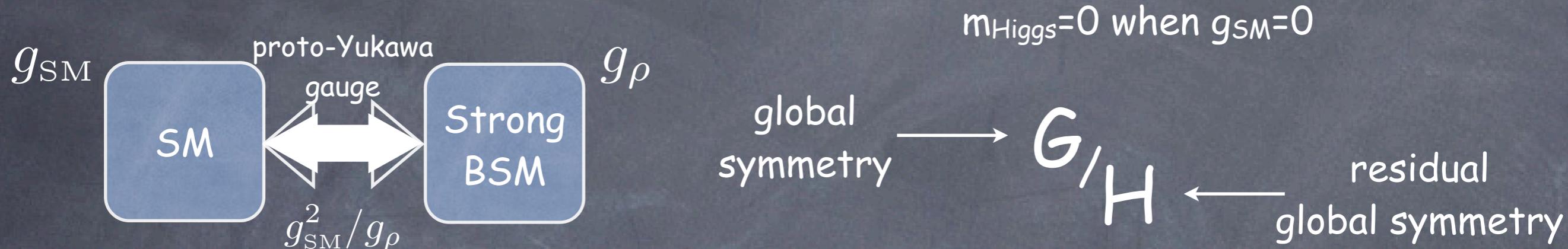


unitarization halfway between weak and strong unitarizations!

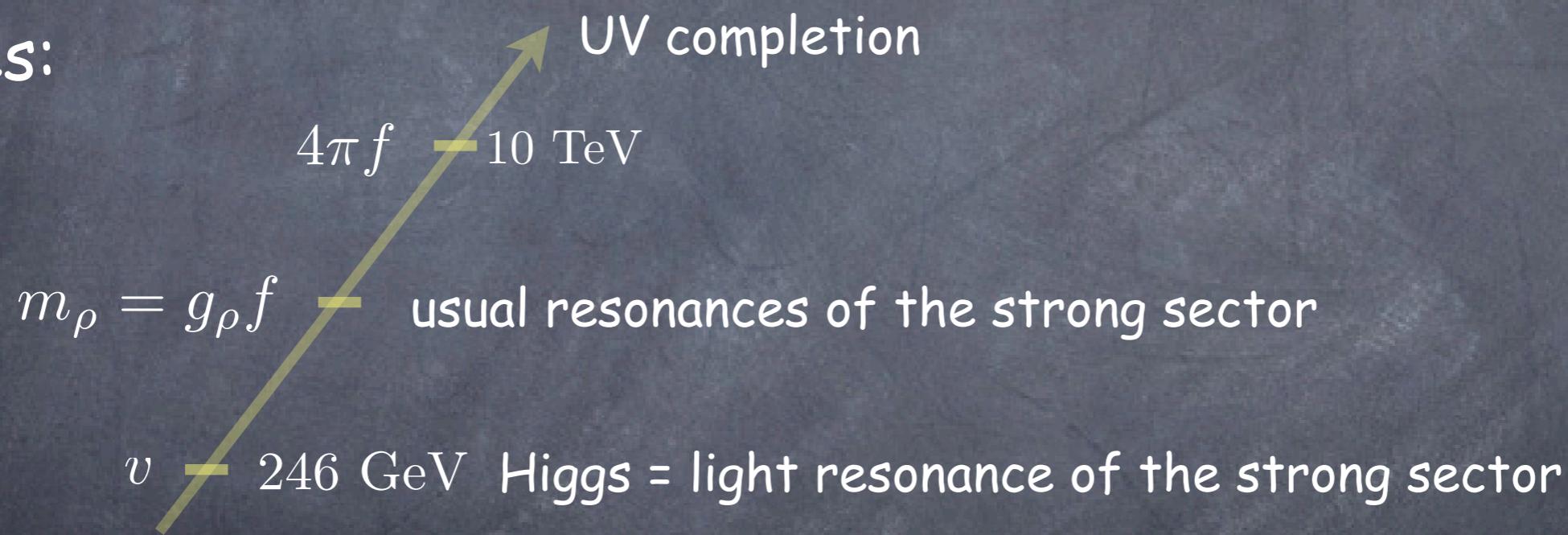
- ≠ susy: composite particle \supset no naturalness pb \supset no need for new particles
- ≠ technicolor: amplitude partially cancelled by Higgs \supset allows for heavier rho \supset smaller oblique corrections.

How to obtain a light composite Higgs?

Higgs=Pseudo-Goldstone boson of the strong sector



3 scales:

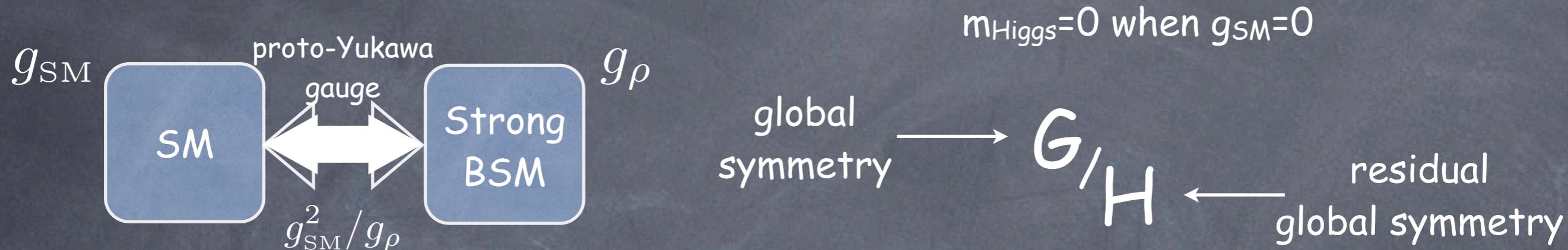


strong sector broadly characterized by 2 parameters

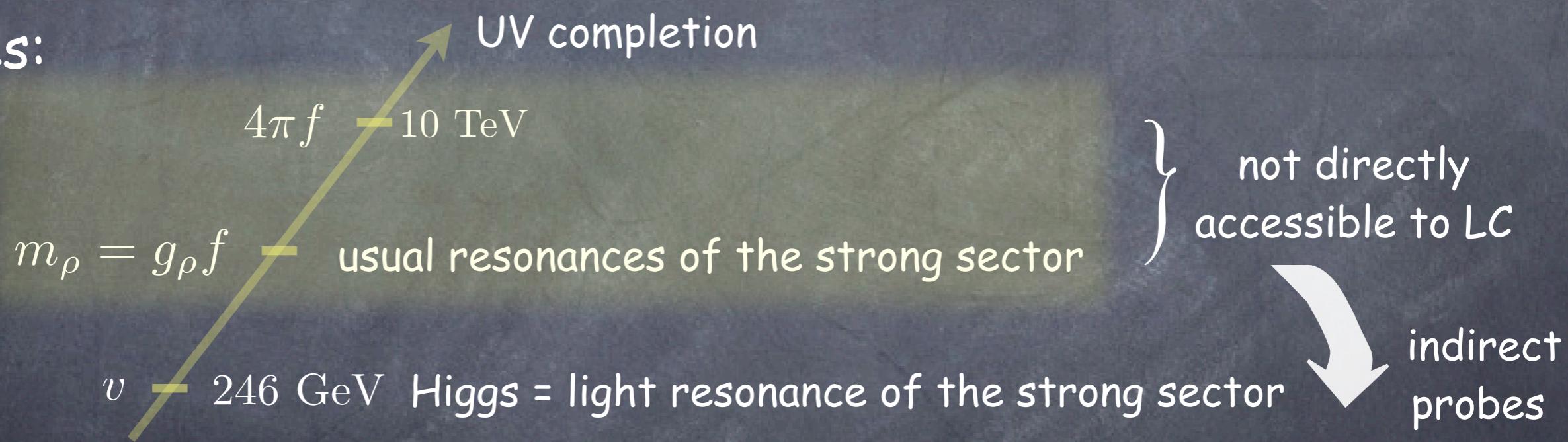
m_ρ = mass of the resonances
 g_ρ = coupling of the strong sector or decay cst of strong sector $f = \frac{m_\rho}{g_\rho}$

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Continuous interpolation between SM and TC

$$\xi = \frac{v^2}{f^2} = \frac{(\text{weak scale})^2}{(\text{strong coupling scale})^2}$$

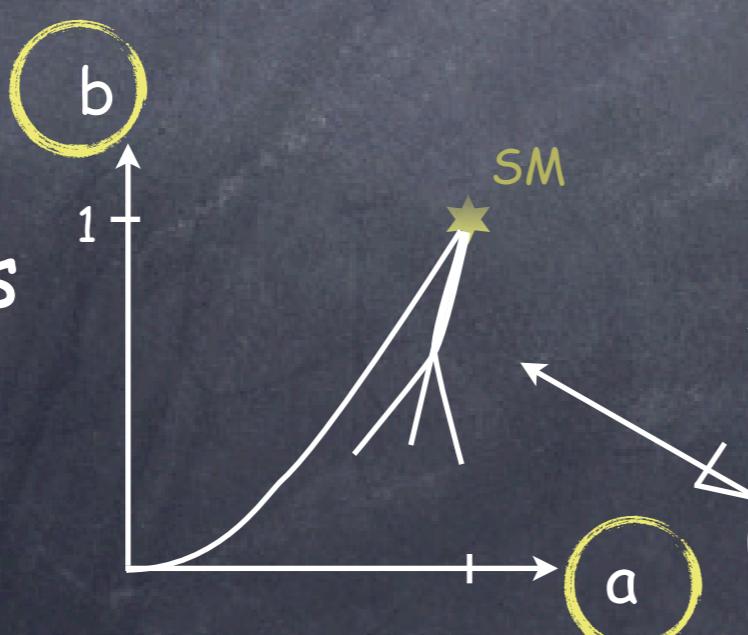
$\xi = 0$
SM limit

all resonances of strong sector,
except the Higgs, decouple

$\xi = 1$
Technicolor limit

Higgs decouple from SM;
vector resonances like in TC

Composite Higgs
vs.
SM Higgs



$$\mathcal{L}_{\text{EWSB}} = \left(a \frac{v}{2} h + b \frac{1}{4} h^2 \right) \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma)$$

Composite Higgs
universal behavior for large f
 $a=1-v/2f$ $b=1-2v/f$

Continuous interpolation between SM and TC

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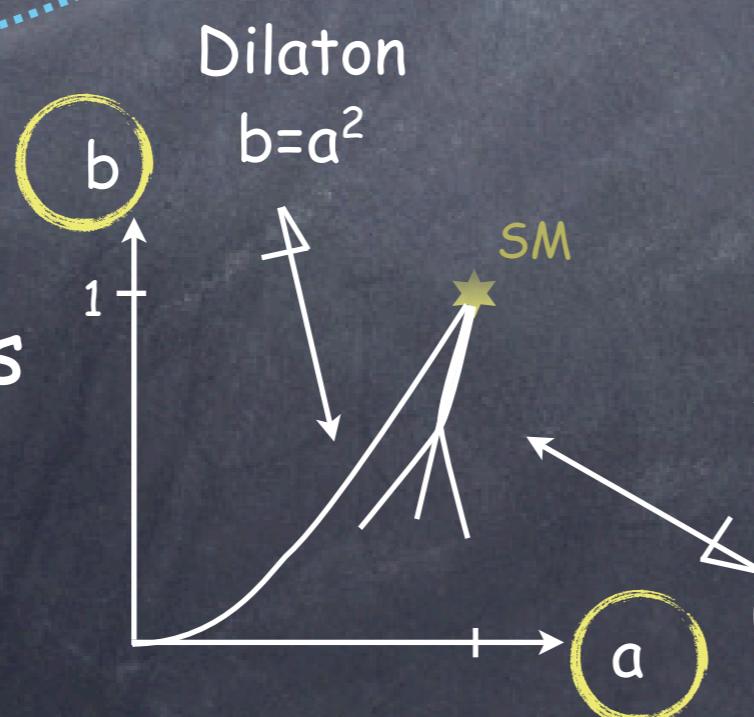
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Technicolor limit

Higgs decouple from SM;
vector resonances like in TC

Composite Higgs
vs.
Dilaton



$$\mathcal{L}_{\text{EWSB}} = \left(a \frac{v}{2} h + b \frac{1}{4} h^2 \right) \text{Tr} (D_\mu \Sigma^\dagger D_\mu \Sigma)$$

Composite Higgs
universal behavior for large f
 $a=1-v/2f$ $b=1-2v/f$

Testing the composite nature of the Higgs?

if LHC sees a Higgs and nothing else*:
is it elementary or composite?

?? evidence for fine-tuning & string landscape ???

?? Higgs forces have a secret hidden gauge origin ???

- ⌚ Model-dependent: production of resonances at m_ρ
- ⌚ Model-independent: study of Higgs properties & W scattering
 - ⌚ strong WW scattering
 - ⌚ strong HH production
 - ⌚ Higgs anomalous coupling
 - ⌚ anomalous gauge bosons self-couplings

* a likely possibility that precision data seems to point to,
at least in strongly coupled models

What distinguishes a composite Higgs?

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

$$U = e^{i \begin{pmatrix} & H/f \\ H^\dagger/f & \end{pmatrix} U_0}$$

$$f^2 \text{tr} (\partial_\mu U^\dagger \partial^\mu U) = |\partial_\mu H|^2 + \frac{\sharp}{f^2} (\partial |H|^2)^2 + \frac{\sharp}{f^2} |H|^2 |\partial H|^2 + \frac{\sharp}{f^2} |H^\dagger \partial H|^2$$

Anomalous Higgs Couplings

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

$$H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \longrightarrow \mathcal{L} = \frac{1}{2} \left(1 + c_H \frac{v^2}{f^2} \right) (\partial^\mu h)^2 + \dots$$

Modified Higgs propagator \sim Higgs couplings rescaled by $\frac{1}{\sqrt{1 + c_H \frac{v^2}{f^2}}} \sim 1 - c_H \frac{v^2}{2f^2} \equiv 1 - \xi/2$

SILH Effective Lagrangian

(strongly-interacting light Higgs)

Giudice, Grojean, Pomarol, Rattazzi '07

- extra Higgs leg: H/f
- extra derivative: ∂/m_ρ

- **Genuine strong operators** (sensitive to the scale f)
- **Form factor operators** (sensitive to the scale m_ρ)

SILH Effective Lagrangian

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extra Higgs leg: H/f

extra derivative: ∂/m_ρ

Genuine strong operators (sensitive to the scale f)

$$\frac{c_H}{2f^2} \left(\partial_\mu (|H|^2) \right)^2$$

$$\frac{c_T}{2f^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right)^2$$

custodial breaking

$$\frac{c_y y_f}{f^2} |H|^2 \bar{f}_L H f_R + \text{h.c.}$$

$$\frac{c_6 \lambda}{f^2} |H|^6$$

Form factor operators (sensitive to the scale m_ρ)

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Form factor operators (sensitive to the scale m_ρ)

$$\frac{i c_W}{2m_\rho^2} \left(H^\dagger \sigma^i \overleftrightarrow{D^\mu} H \right) (D^\nu W_{\mu\nu})^i$$

$$\frac{i c_B}{2m_\rho^2} \left(H^\dagger \overleftrightarrow{D^\mu} H \right) (\partial^\nu B_{\mu\nu})$$

$$\frac{i c_{HW}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i$$

$$\frac{i c_{HB}}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

minimal coupling: $h \rightarrow \gamma Z$

loop-suppressed strong dynamics

$$\frac{c_\gamma}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

$$\frac{c_g}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{y_t^2}{g_\rho^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu}$$

Goldstone sym.

EWPT constraints

$$\hat{T} = c_T \frac{v^2}{f^2} \rightarrow |c_T \frac{v^2}{f^2}| < 2 \times 10^{-3}$$

removed
by custodial symmetry

$$\hat{S} = (c_W + c_B) \frac{m_W^2}{m_\rho^2} \rightarrow m_\rho \geq (c_W + c_B)^{1/2} \text{ 2.5 TeV}$$

There are also some 1-loop IR effects

Barbieri, Bellazzini, Rychkov, Varagnolo '07

$$\hat{S}, \hat{T} = a \log m_h + b$$



modified Higgs couplings to matter

$$\hat{S}, \hat{T} = a ((1 - c_H \xi) \log m_h + c_H \xi \log \Lambda) + b$$

effective
Higgs mass

$$m_h^{eff} = m_h \left(\frac{\Lambda}{m_h} \right)^{c_H v^2 / f^2} > m_h$$

LEPII, for $m_h \sim 115$ GeV: $c_H v^2 / f^2 < 1/3 \sim 1/2$

IR effects can be cancelled by heavy fermions (model dependent)

Flavor Constraints

$$\left(1 + \frac{c_{ij}|H|^2}{f^2}\right) y_{ij} \bar{f}_{Li} H f_{Rj} = \left(1 + \frac{c_{ij}v^2}{2f^2}\right) \frac{y_{ij}v}{\sqrt{2}} \bar{f}_{Li} f_{Rj}$$

mass terms



$$+ \left(1 + \frac{3c_{ij}v^2}{2f^2}\right) \frac{y_{ij}}{\sqrt{2}} h \bar{f}_{Li} f_{Rj}$$

Higgs fermion interactions



mass and interaction matrices are not diagonalizable simultaneously
if c_{ij} are arbitrary

⇒ FCNC

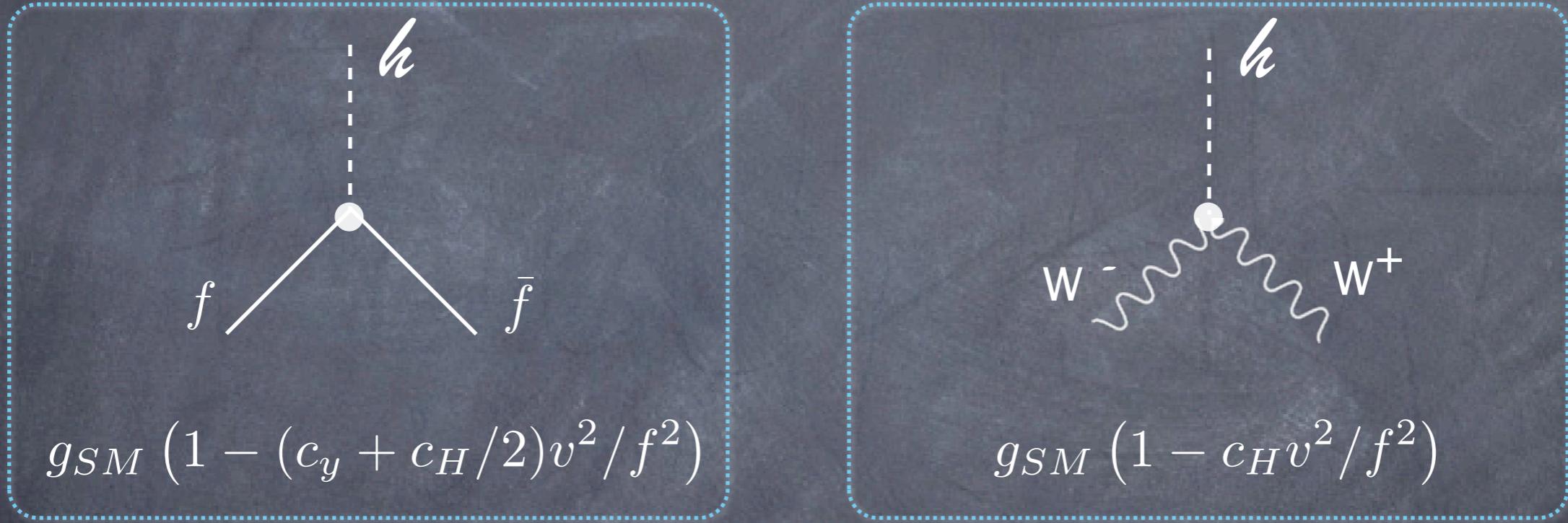
SILH: c_y is flavor universal

⇒ Minimal flavor violation built in

Higgs anomalous couplings

Lagrangian in unitary gauge

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \left(-\frac{m_H^2}{2v} (c_6 - 3c_H/2) h^3 + \frac{m_f}{v} \bar{f} f (c_y + c_H/2) h - c_H \frac{m_W^2}{v} h W_\mu^+ W^{-\mu} - c_H \frac{m_Z^2}{v} h Z_\mu Z^\mu \right) \frac{v^2}{f^2} + \dots$$



$$\Gamma (h \rightarrow f \bar{f})_{\text{SILH}} = \Gamma (h \rightarrow f \bar{f})_{\text{SM}} [1 - (2c_y + c_H) v^2/f^2]$$

$$\Gamma (h \rightarrow gg)_{\text{SILH}} = \Gamma (h \rightarrow gg)_{\text{SM}} [1 - (2c_y + c_H) v^2/f^2]$$

Note: same Lorentz structure as in SM. Not true anymore if form factor ops. are included

Higgs anomalous couplings for large v/f

The SILH Lagrangian is an expansion for small v/f

The 5D MCHM gives a completion for large v/f

$$m_W^2 = \frac{1}{4} g^2 f^2 \sin^2 v/f \quad \Rightarrow \quad g_{hWW} = \sqrt{1 - \xi} g_{hWW}^{\text{SM}}$$

Fermions embedded in spinorial of $SO(5)$

$$m_f = M \sin v/f$$



$$g_{hff} = \sqrt{1 - \xi} g_{hff}^{\text{SM}}$$

universal shift of the couplings
no modifications of BRs

$$(\xi = v^2/f^2)$$

Fermions embedded in 5+10 of $SO(5)$

$$m_f = M \sin 2v/f$$

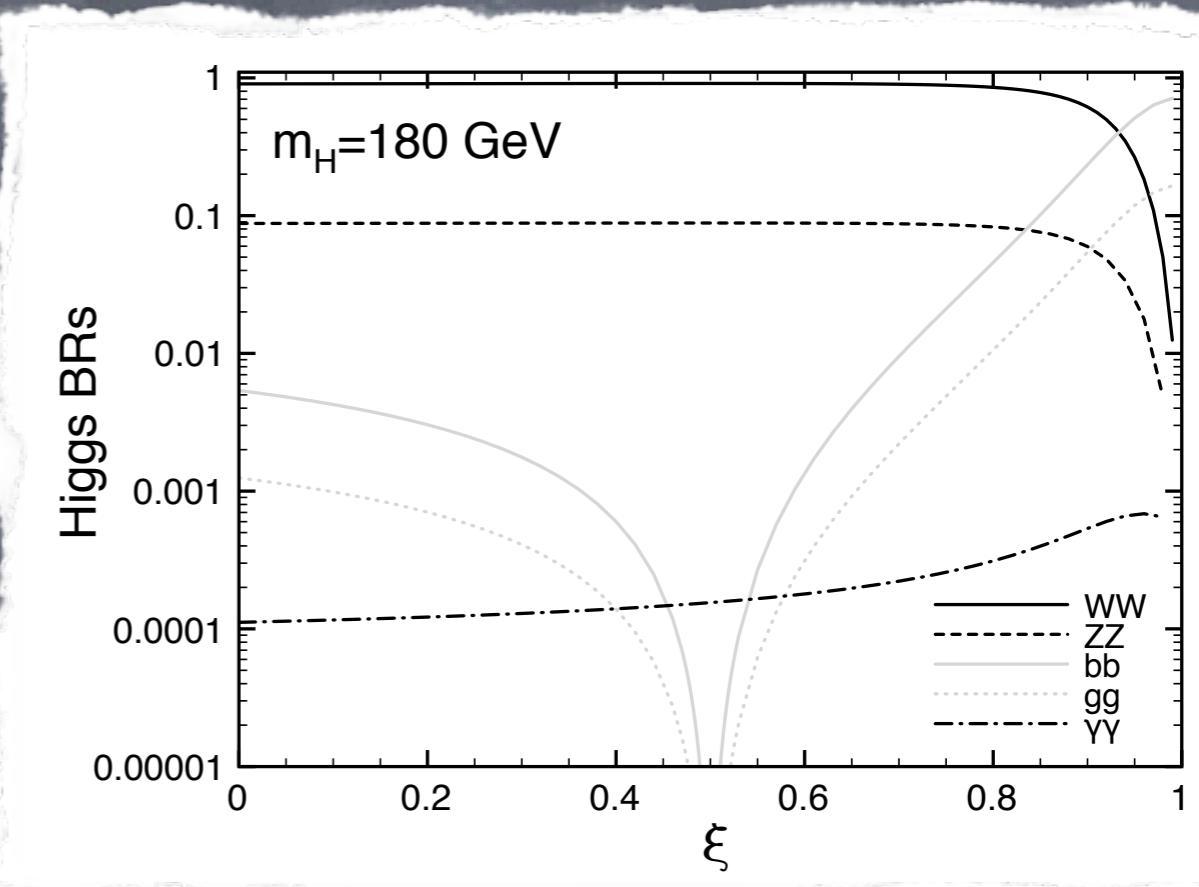
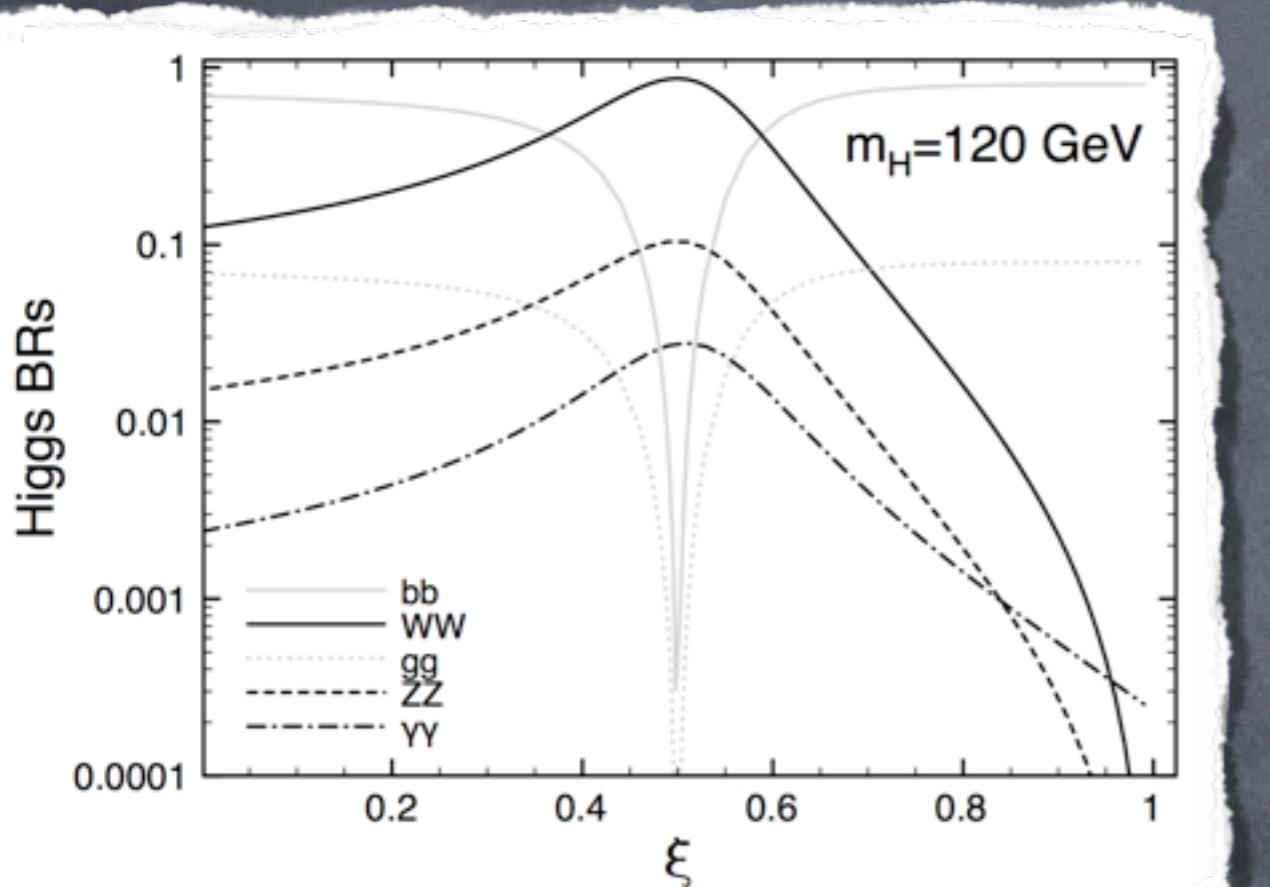


$$g_{hff} = \frac{1 - 2\xi}{\sqrt{1 - \xi}} g_{hff}^{\text{SM}}$$

BRs now depends on v/f

Higgs BRs

Fermions embedded in 5+10 of $SO(5)$



$h \rightarrow WW$ can dominate even for low Higgs mass

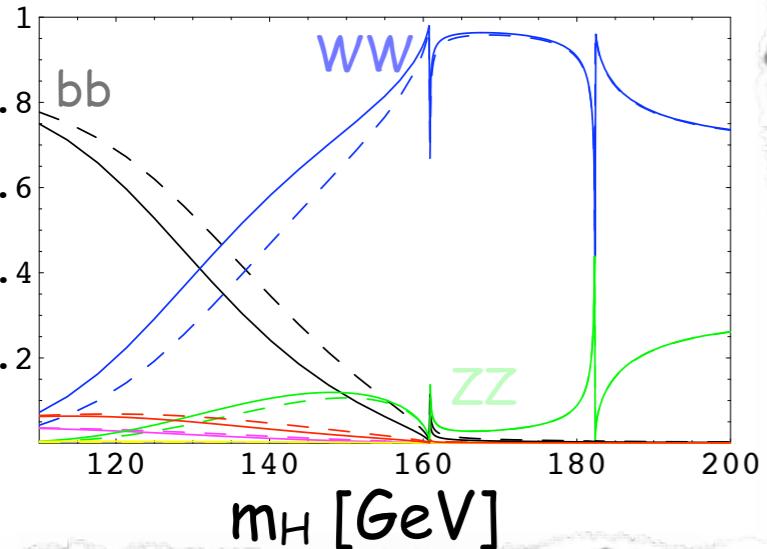
BRs remain SM like except for very large values of v/f

Higgs BRs and total width

Fermions embedded in 5+10 of SO(5)

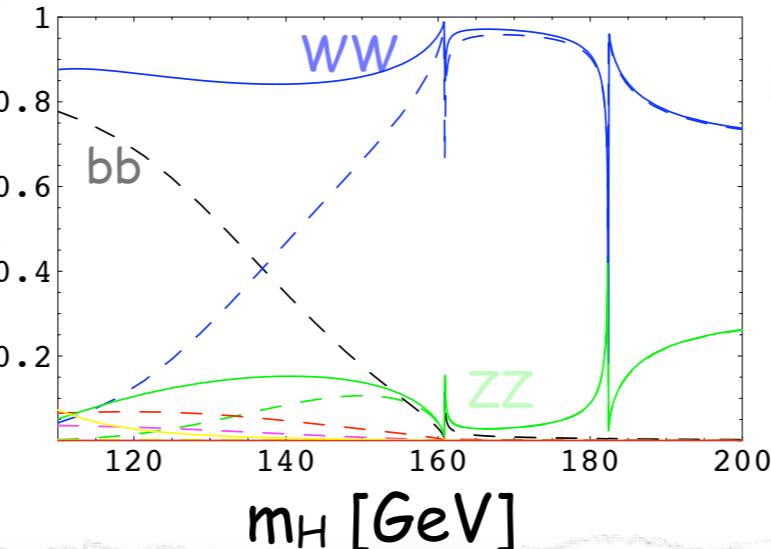
BRs

$v^2/f^2=0.2$



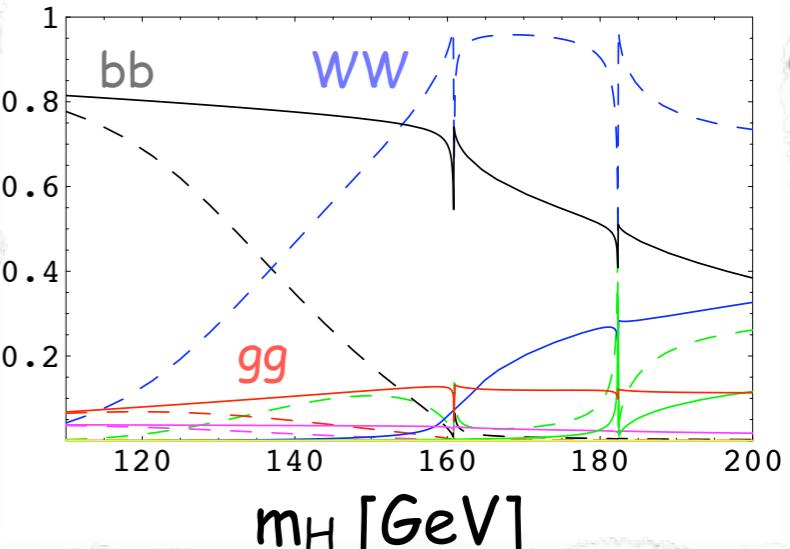
BRs

$v^2/f^2=0.5$



BRs

$v^2/f^2=0.95$

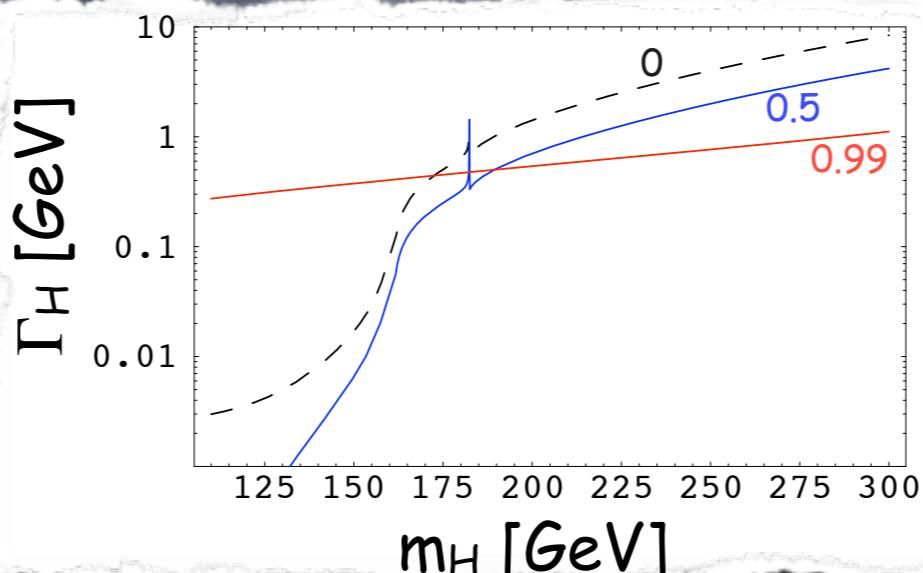


slight modifications

suppress bb

suppress WW

Higgs total width

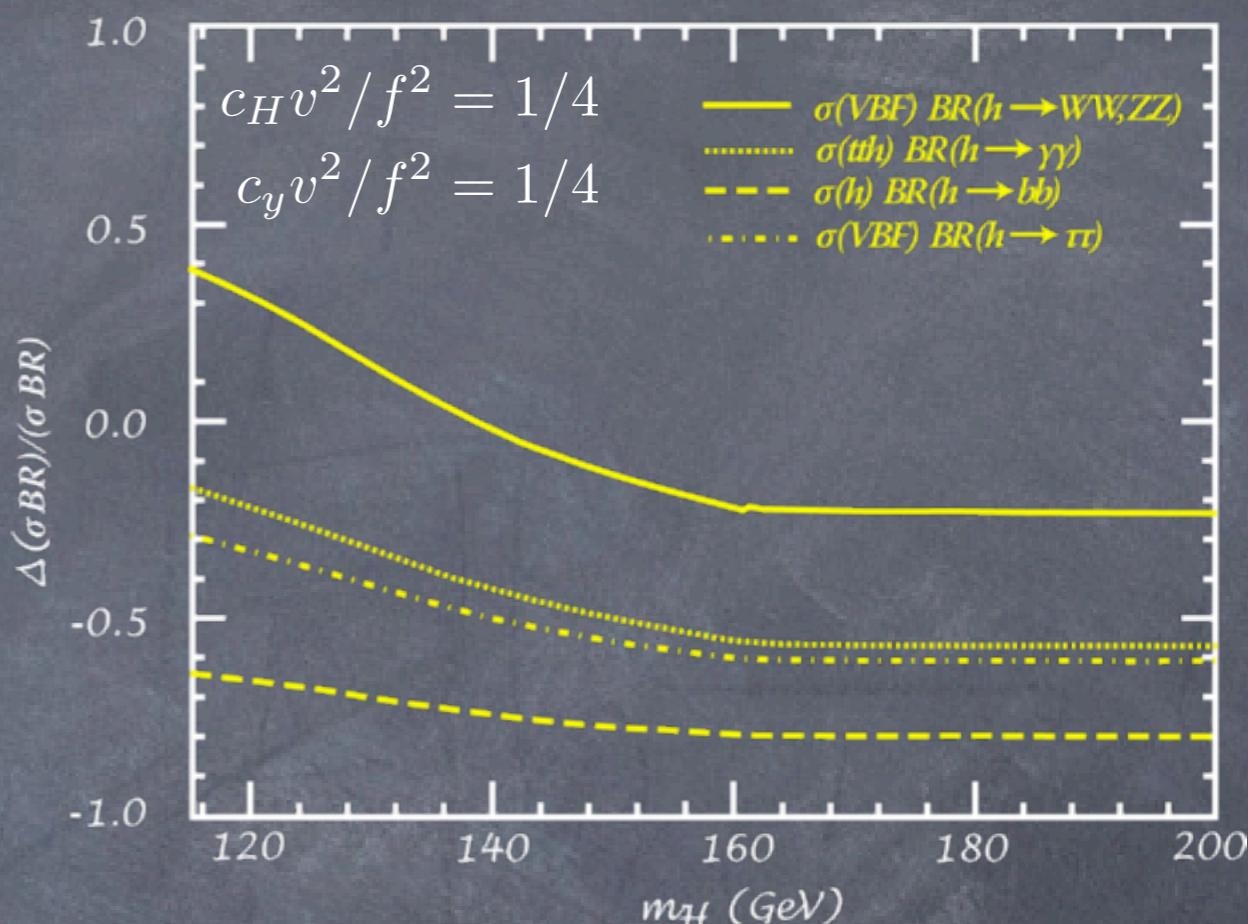
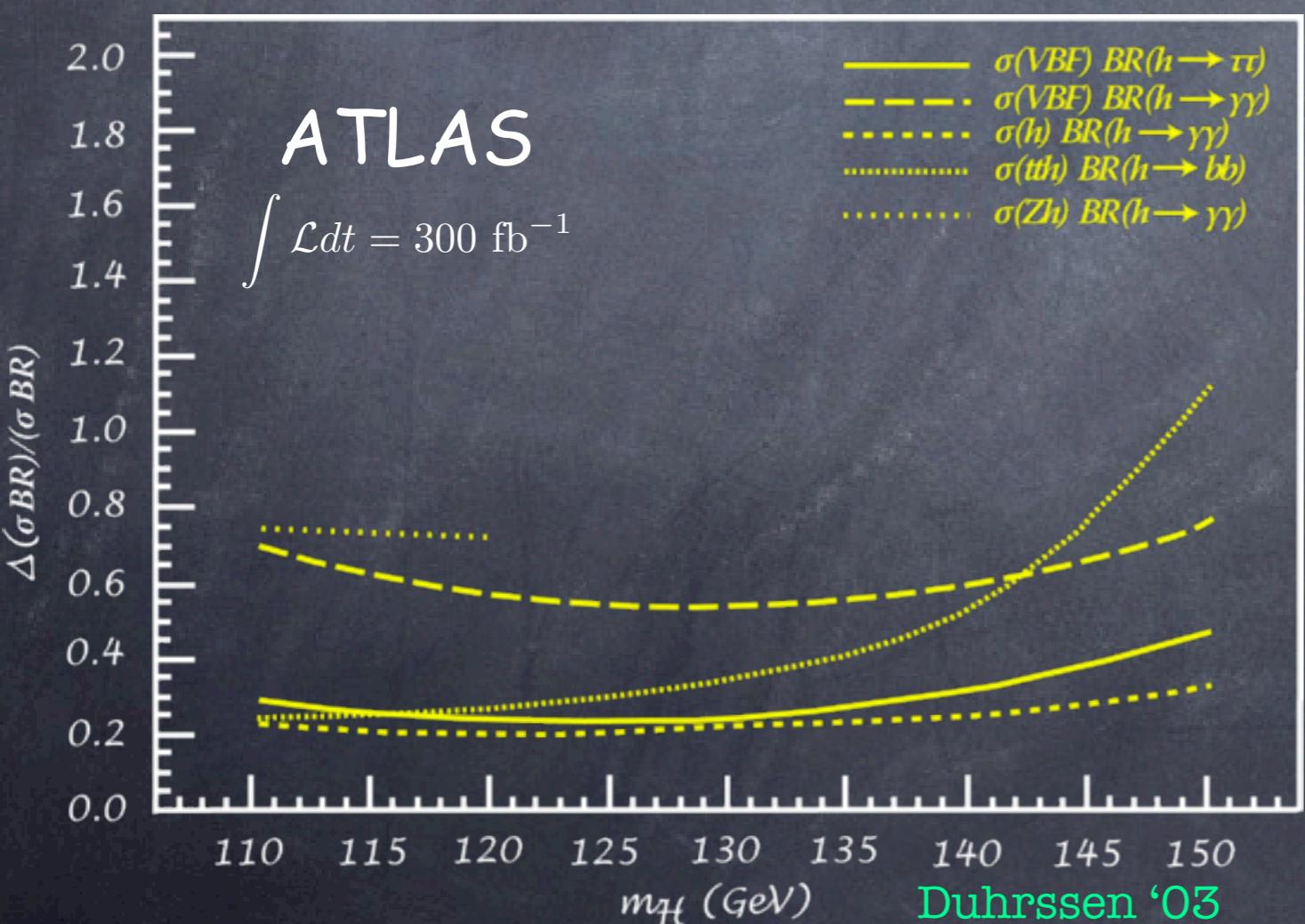


Higgs anomalous couplings @ LHC

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$$\Gamma(h \rightarrow gg)_{\text{SILH}} = \Gamma(h \rightarrow gg)_{\text{SM}} [1 - (2c_y + c_H) v^2/f^2]$$

observable @ LHC?



LHC can measure

$$c_H \frac{v^2}{f^2}, \quad c_y \frac{v^2}{f^2}$$

up to 0.2-0.4

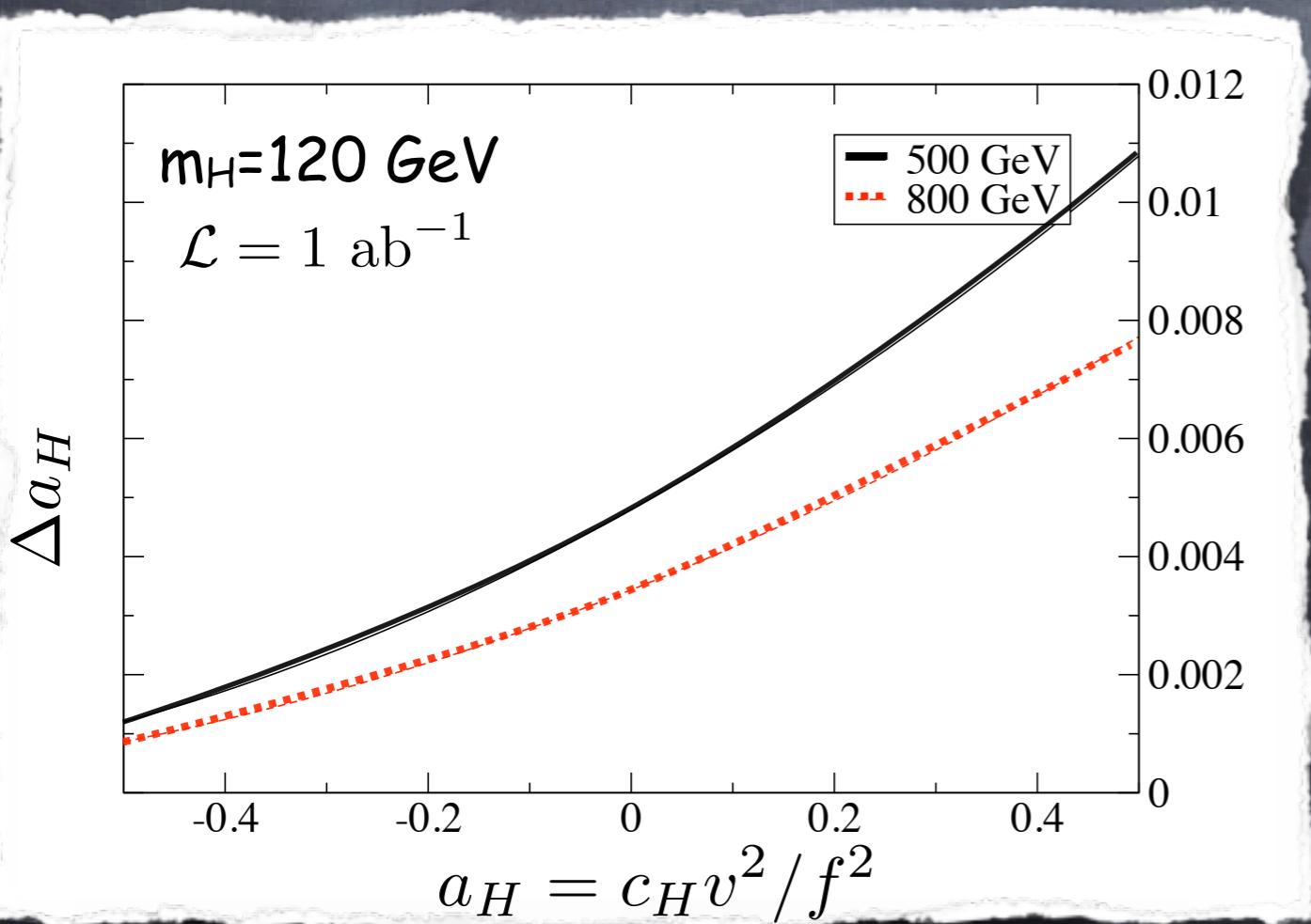
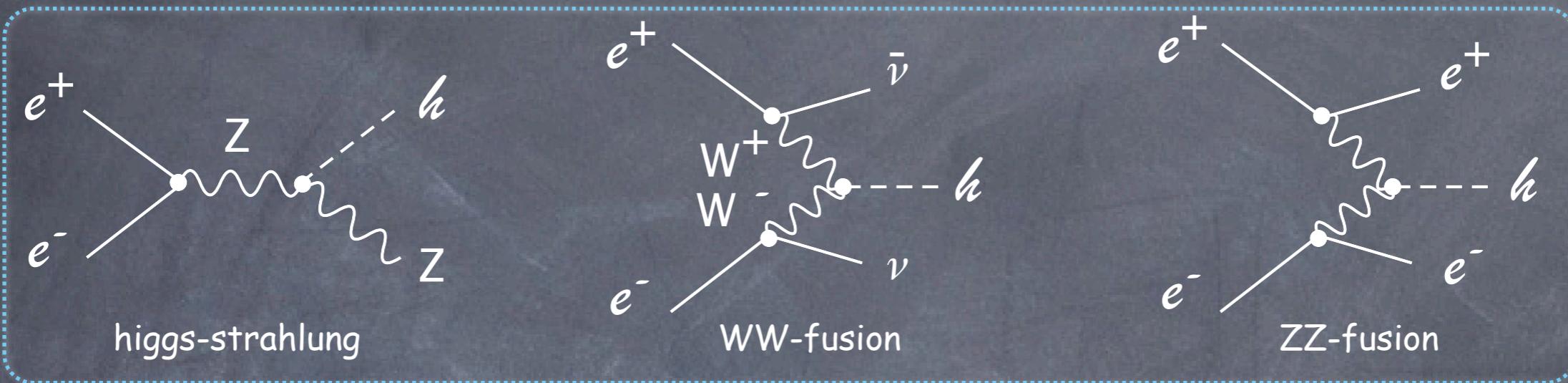
i.e. $4\pi f \sim 5 - 7 \text{ TeV}$

(ILC could go to few % ie
test composite Higgs up to $4\pi f \sim 30 \text{ TeV}$)

Higgs anomalous couplings @ LC

Barger et al. hep-ph/0301097

single Higgs production



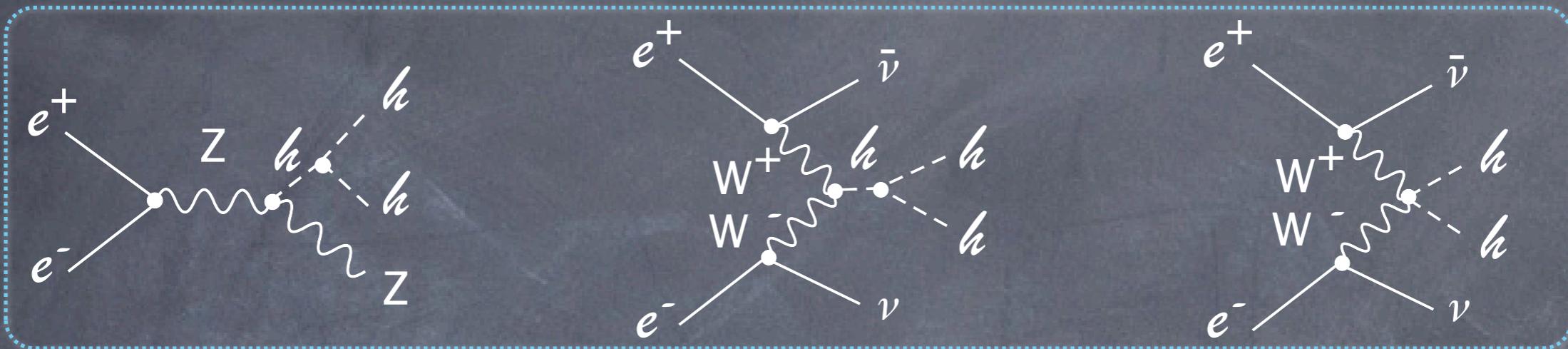
$$\Delta a_H \sim 0.005 \implies 4\pi f \sim 44 \text{ TeV}$$

$$\Delta a_H \sim 0.02 \implies 4\pi f \sim 22 \text{ TeV}$$

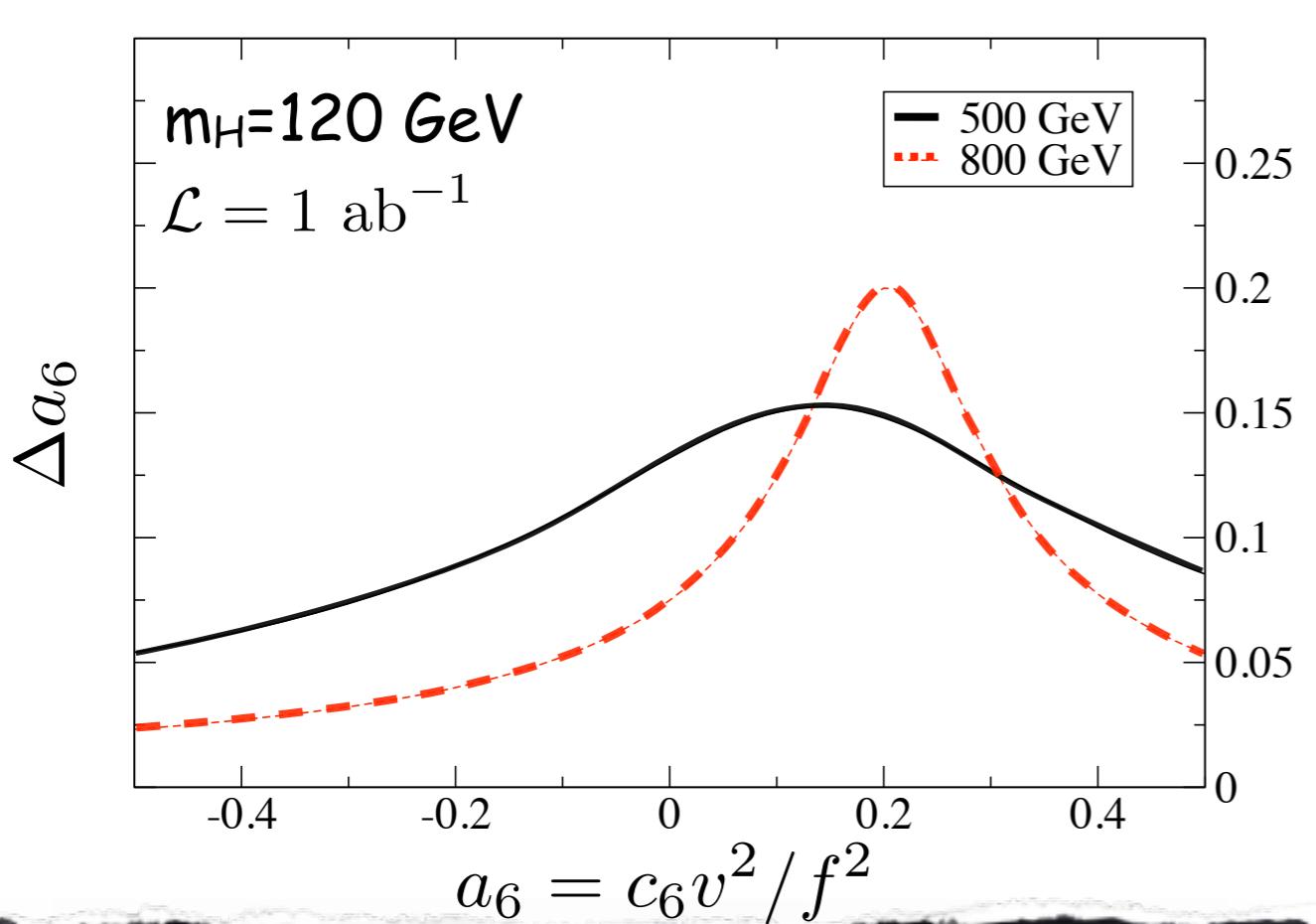
Higgs anomalous (self-)couplings @ LC

Barger et al. hep-ph/0301097

double Higgs production



the accuracy on a_H is not competitive compared to single Higgs production

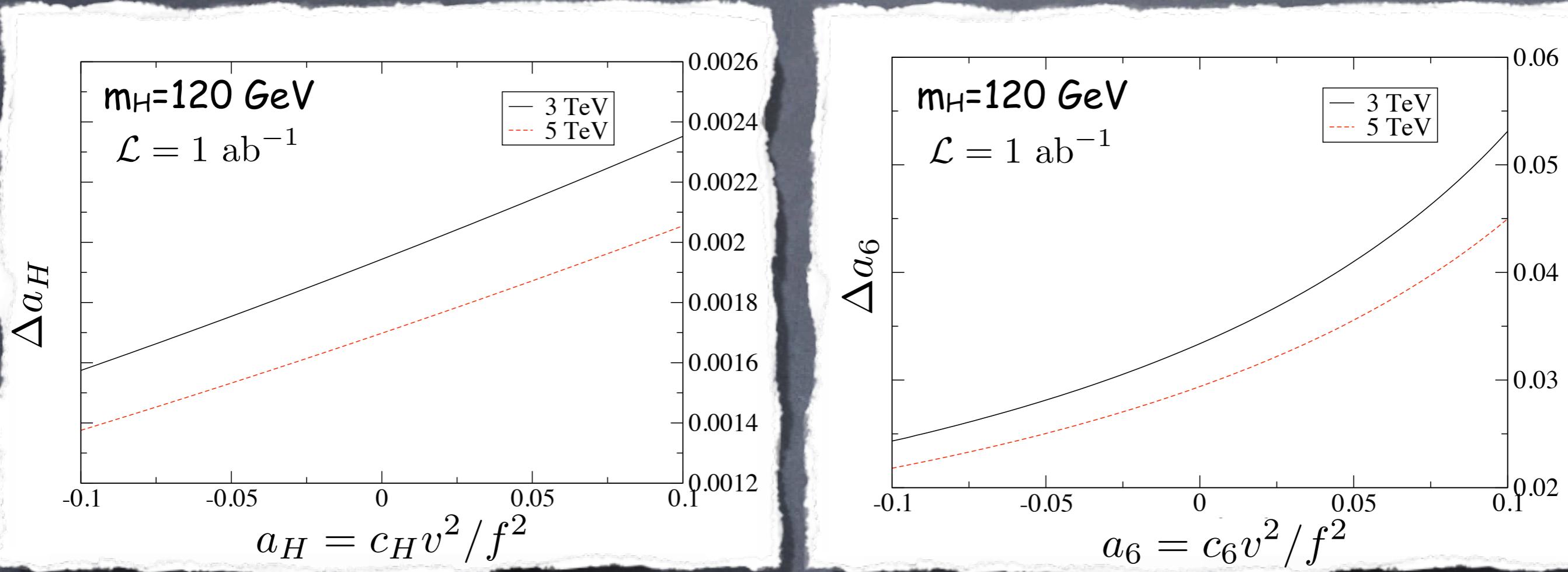


it allows to constrain a_6

$$m_H = 120 \text{ GeV} \\ \Delta a_6 \sim 0.1 \implies 4\pi f \sim 10 \text{ TeV}$$

Higgs anomalous couplings @ CLIC

Barger et al. hep-ph/0301097



$$\Delta a_H \sim 0.002 \Rightarrow 4\pi f \sim 70 \text{ TeV}$$

$$\Delta a_6 \sim 0.04 \Rightarrow 4\pi f \sim 15 \text{ TeV}$$

a factor 2 better than ILC

Triple gauge boson couplings (TGC) @ LC

$$\mathcal{L}_V = -ig \cos \theta_W g_1^Z Z^\mu (W^{+\nu} W_{\mu\nu}^- - W^{-\nu} W_{\mu\nu}^+) - ig (\cos \theta_W \kappa_Z Z^{\mu\nu} + \sin \theta_W \kappa_\gamma A^{\mu\nu}) W_\mu^+ W_\nu^-$$

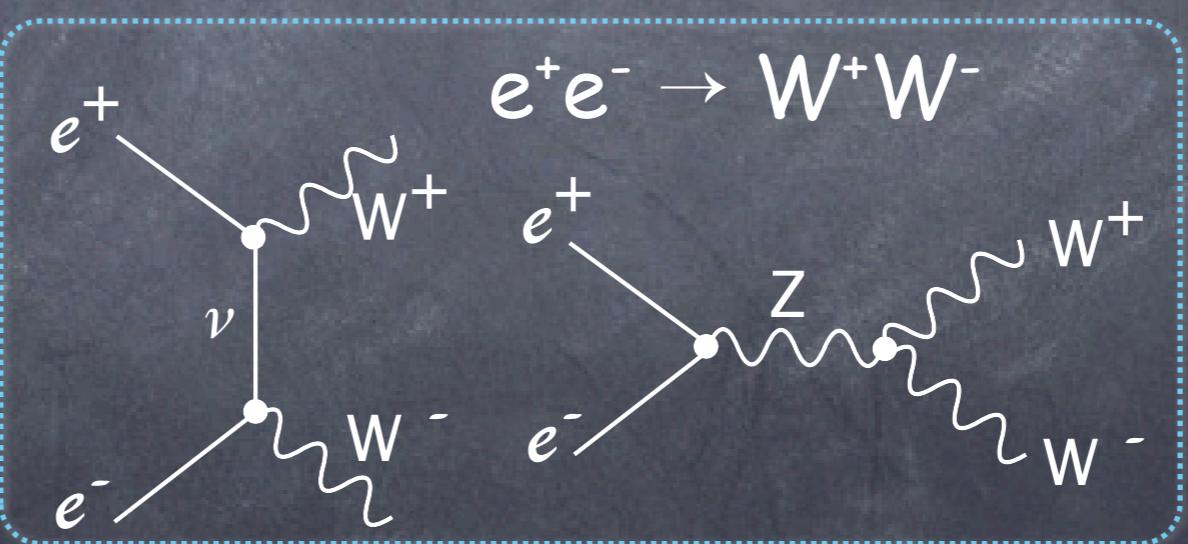
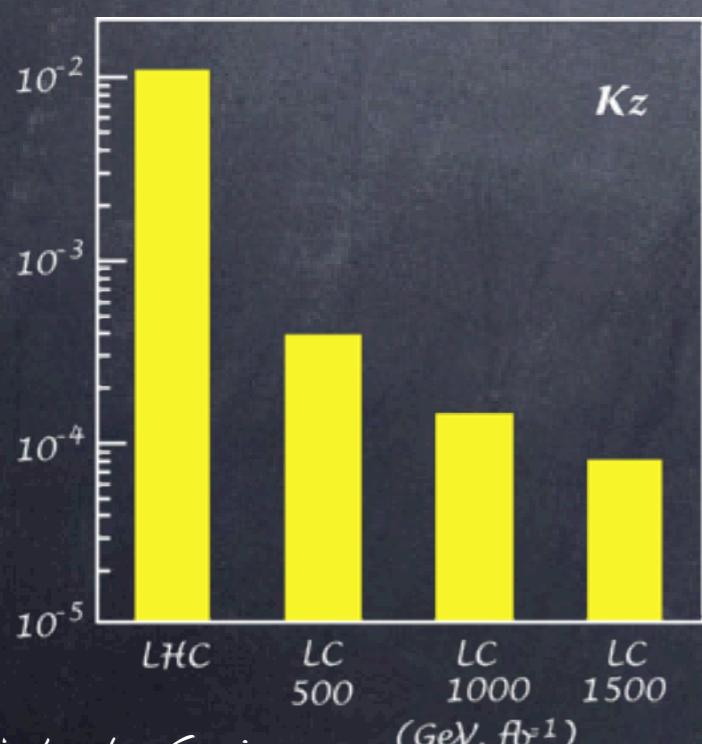
TGC are generated by heavy resonances

$$g_1^Z = \frac{m_Z^2}{m_\rho^2} c_W \quad \kappa_\gamma = \frac{m_W^2}{m_\rho^2} \left(\frac{g_\rho}{4\pi} \right)^2 (c_{HW} + c_{HB}) \quad \kappa_Z = g_1^Z - \tan^2 \theta_W \kappa_\gamma$$

@ LHC 100fb^{-1} $g_1^Z \sim 1\%$ $\kappa_\gamma \sim \kappa_Z \sim 5\%$ sensitive to resonance up to $m_\rho \sim 800 \text{ GeV}$

not competitive with the measure of S at LEPII

@ ILC



0.1% accuracy \Rightarrow

sensitive to resonance up to $m_\rho \sim 8 \text{ TeV}$

T. Abe et al, Snowmass '01

Strong WW scattering

Giudice, Grojean, Pomarol, Rattazzi '07

$$\mathcal{L} \supset \frac{c_H}{2f^2} \partial^\mu (|H|^2) \partial_\mu (|H|^2) \quad c_H \sim \mathcal{O}(1)$$

$$H = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \rightarrow \mathcal{L} = \frac{1}{2} \left(1 + c_H \frac{v^2}{f^2} \right) (\partial^\mu h)^2 + \dots$$

Modified Higgs propagator \sim Higgs couplings rescaled by $\frac{1}{\sqrt{1 + c_H \frac{v^2}{f^2}}} \sim 1 - c_H \frac{v^2}{2f^2} \equiv 1 - \xi/2$

$$= -(1 - \xi) g^2 \frac{E^2}{M_W^2}$$

no exact cancellation
of the growing amplitudes

Even with a light Higgs, growing amplitudes (at least up to m_ρ)

$$\mathcal{A}(W_L^a W_L^b \rightarrow W_L^c W_L^d) = \mathcal{A}(s, t, u) \delta^{ab} \delta^{cd} + \mathcal{A}(t, s, u) \delta^{ac} \delta^{bd} + \mathcal{A}(u, t, s) \delta^{ad} \delta^{bc}$$

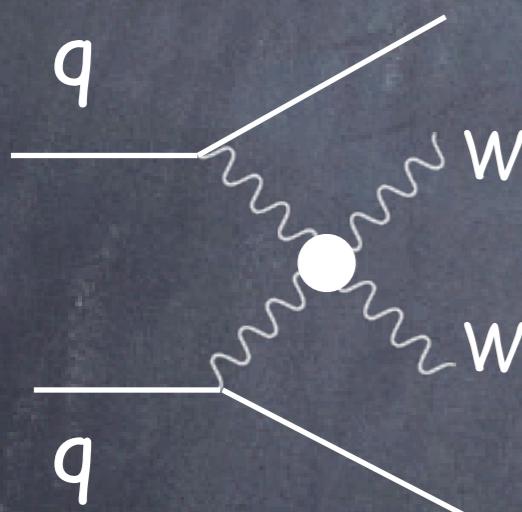
$$\mathcal{A}_{\text{LET}}(s, t, u) = \frac{s}{v^2} \quad \rightarrow \quad \mathcal{A}_\xi = \xi \mathcal{A}_{\text{LET}}$$

LET=SM-Higgs

Strong WW scattering @ LHC

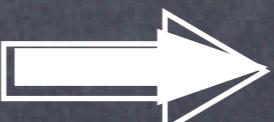
Even with a light Higgs, growing amplitudes (at least up to m_ρ)

$$\begin{aligned}\mathcal{A}(Z_L^0 Z_L^0 \rightarrow W_L^+ W_L^-) &= \mathcal{A}(W_L^+ W_L^- \rightarrow Z_L^0 Z_L^0) = -\mathcal{A}(W_L^\pm W_L^\pm \rightarrow W_L^\pm W_L^\pm) = \frac{c_H s}{f^2} \\ \mathcal{A}(W^\pm Z_L^0 \rightarrow W^\pm Z_L^0) &= \frac{c_H t}{f^2}, \quad \mathcal{A}(W_L^+ W_L^- \rightarrow W_L^+ W_L^-) = \frac{c_H(s+t)}{f^2} \\ \mathcal{A}(Z_L^0 Z_L^0 \rightarrow Z_L^0 Z_L^0) &= 0\end{aligned}$$



$$\sigma(pp \rightarrow V_L V_L X)_\xi = \xi^2 \sigma(pp \rightarrow V_L V_L X)_{\text{LET}}$$

leptonic vector decay channels
forward jet-tag, back-to-back lepton, central jet-veto



Bagger et al '95
Butterworth et al. '02

	LET($\xi = 1$)	SM bckg
ZZ	4.5	2.1
$W^+ W^-$	15.0	36
$W^\pm Z$	9.6	14.7
$W^\pm W^\pm$	39	11.1

$\mathcal{L} = 300 \text{ fb}^{-1}$

Scale of Strong WW scattering?

NDA estimates

$$\mathcal{A}_{TT \rightarrow TT} \sim g^2$$

$$\mathcal{A}_{LL \rightarrow LL} \sim \frac{s}{v^2}$$

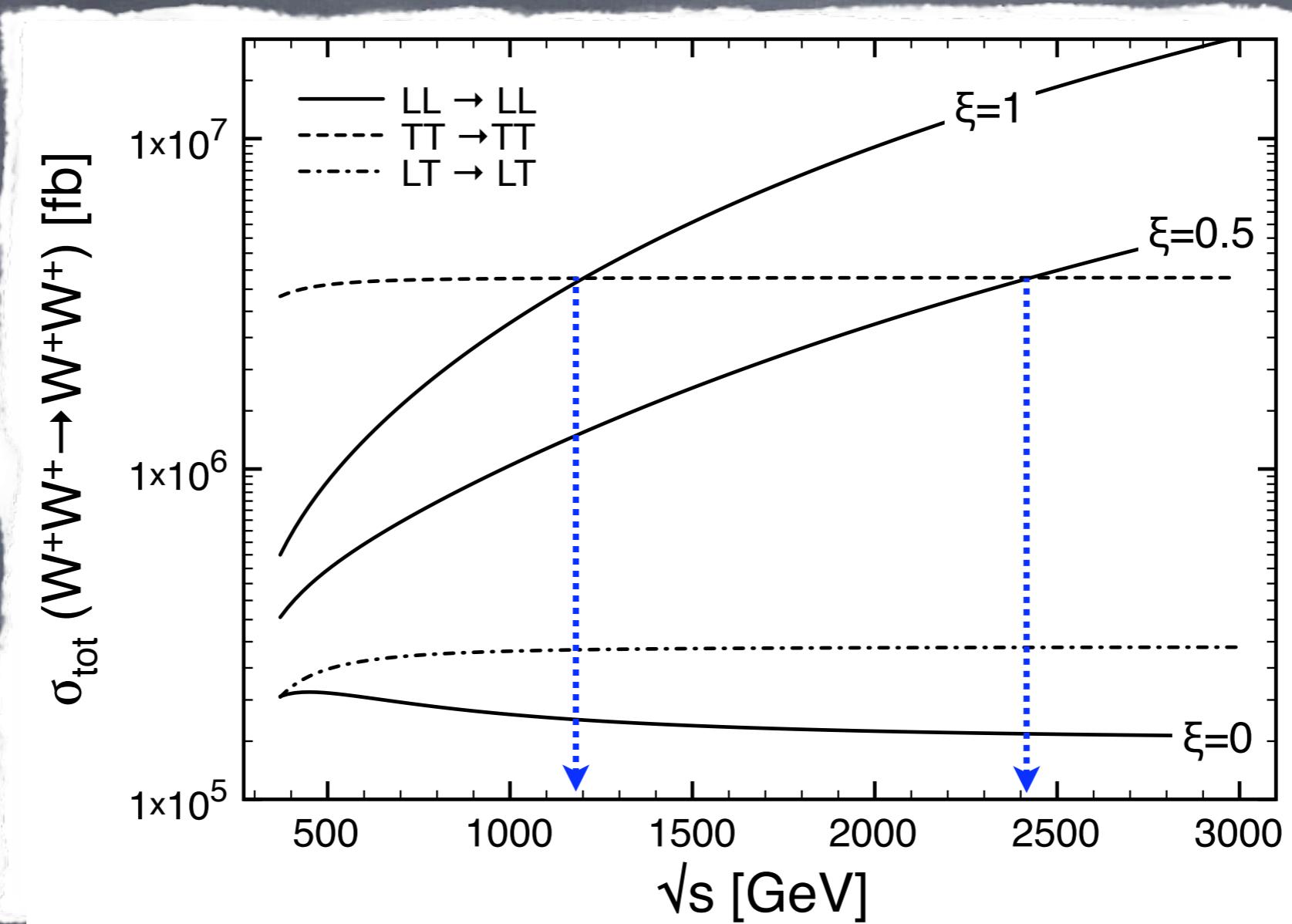
$$\mathcal{A}_{LL \rightarrow LL} \sim \mathcal{A}_{TT \rightarrow TT}$$

for

$$\sqrt{s} \sim 2 M_W$$

Total cross sections

disentangling L from T polarization is hard



The onset of strong scattering is delayed to larger energies due to the dominance of $TT \rightarrow TT$ background

The dominance of T background will be further enhanced by the pdfs since the luminosity of W_T inside the proton is $\log(E/M_W)$ enhanced

Coulomb enhancement (SM)

the total cross section is dominated by the poles
in the exchange of γ and Z in the t- and u-channels

$$W^+ W^+ \rightarrow W^+ W^+$$

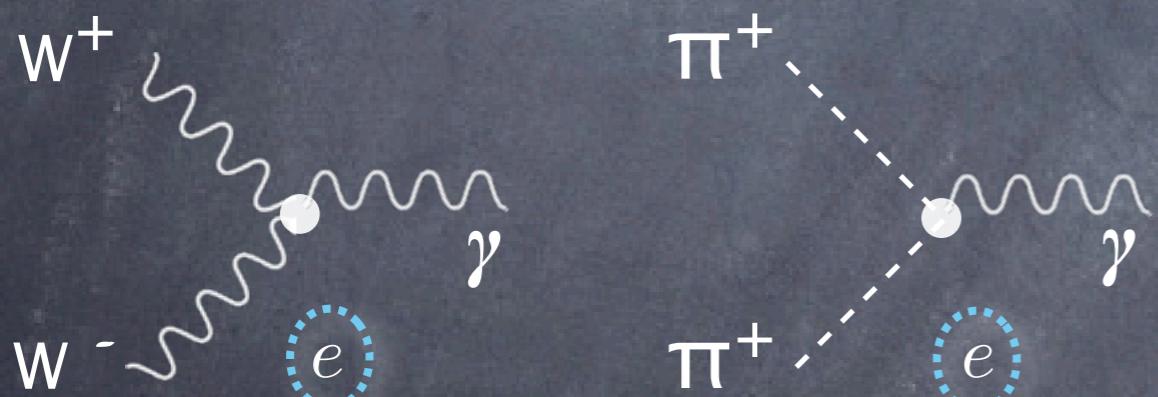
$$\mathcal{A} = \frac{a_\gamma^t s}{t} + \frac{a_Z^t s}{t - M_Z^2} + \frac{a_\gamma^u s}{u} + \frac{a_Z^u s}{u - M_Z^2} + \dots \Rightarrow \sigma \sim \frac{1}{16\pi} \left(\frac{{a_\gamma^t}^2 + {a_\gamma^u}^2}{M_\gamma^2} + \frac{{a_Z^t}^2 + {a_Z^u}^2}{M_\gamma^2 + M_Z^2} \right)$$

M_γ = régulateur of Coulomb singularity=off-shellness of $W \sim M_W$

eikonal limit

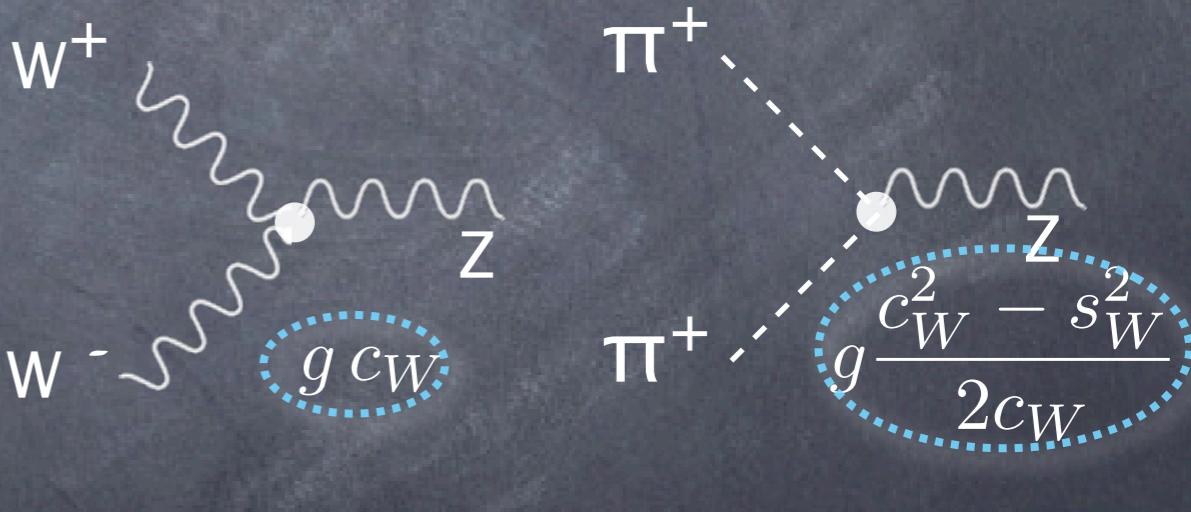
$$a_\gamma = 2 \cdot (\text{electric charge of } W^+)^2$$

universal for T and L



$$a_Z = 2 \cdot (\text{"SU(2) charge" of } W^+)^2$$

different for T and L



SM

$$\frac{\sigma_{TT \rightarrow TT}}{\sigma_{LL \rightarrow LL}} \sim 20$$

(for $M_\gamma \sim M_Z$)

⇒ T-dominance is the result of multiplicity and larger SU(2) charges ⇐

Coulomb enhancement (Composite Higgs)

$$W^+ W^+ \rightarrow W^+ W^+$$

■ Transverse channels are still dominated by the Coulomb singularities

$$\sigma_{TT \rightarrow TT} \sim \frac{2g^4}{\pi} \left(\frac{s_W^4}{M_\gamma^2} + \frac{c_W^4}{M_\gamma^2 + M_Z^2} \right).$$

■ Longitudinal channel: the contact interactions will win over the Coulomb singularities

$$\sigma_{LL \rightarrow LL} \sim \frac{\xi^2 s}{16\pi v^4}$$

$$\frac{\sigma_{LL \rightarrow LL}}{\sigma_{TT \rightarrow TT}} \simeq \frac{\xi^2}{512} \left(\frac{s_W^4}{-t_{\min}} + \frac{c_W^4}{-t_{\min} + M_Z^2} \right)^{-1} \frac{s}{M_W^4}$$

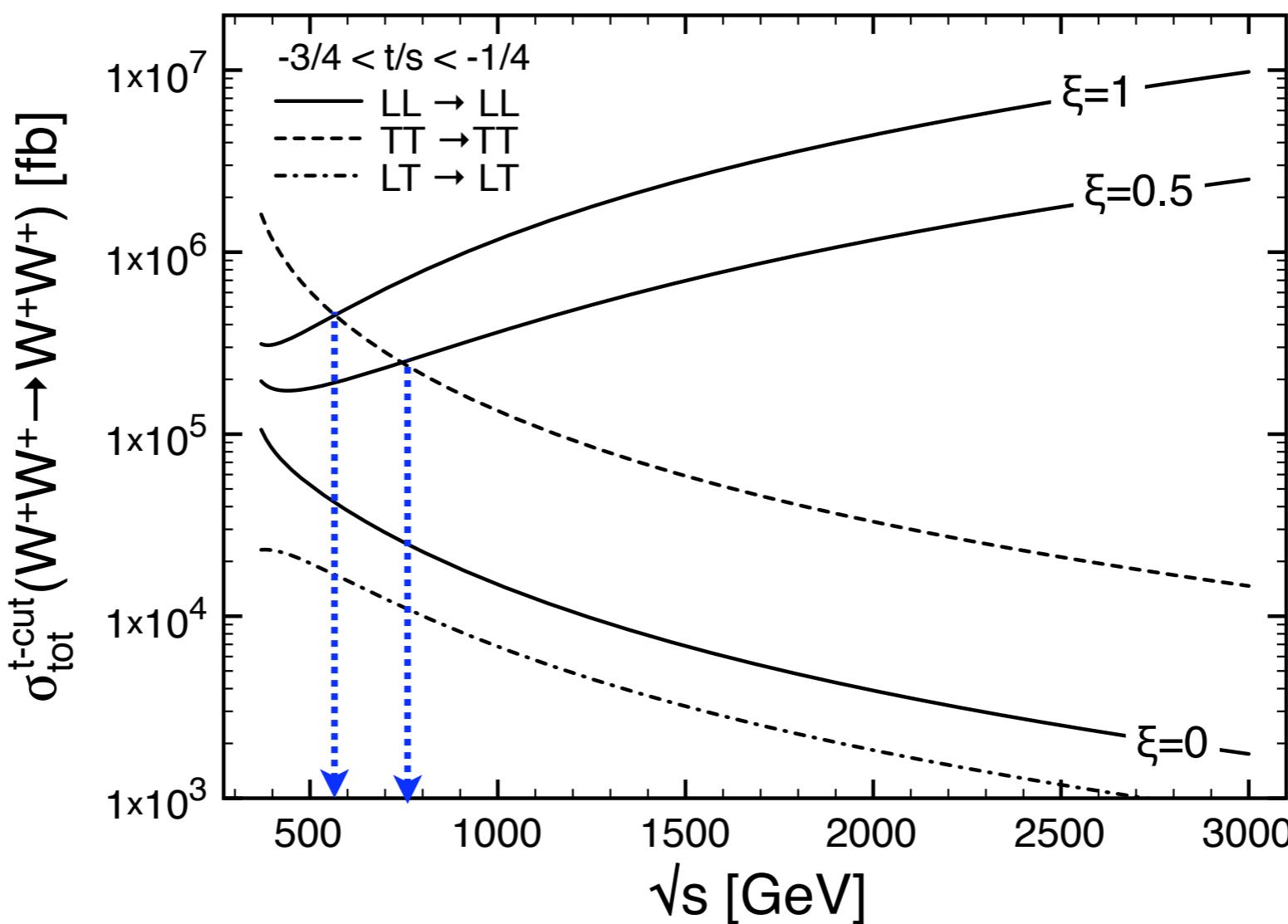
~ 1 @ $\sqrt{s} \sim 13M_W/\xi$

~ 1 @ $\sqrt{s} \sim 5M_W^2/(M_\gamma\xi)$

onset of strong scattering is delayed to higher energies compared to NDA estimates
 σ_{tot} is very sensitive to IR physics: not good observable to probe EWSB sector

Hard scattering (central region)

we need to look at the central region, i.e. large scattering angle,
to be sensitive to strong EWSB



$$\frac{\sigma_{LL \rightarrow LL}^{\text{hard}}}{\sigma_{TT \rightarrow TT}^{\text{hard}}} \simeq \left(\frac{\sqrt{s}}{7.4 M_W} \right)^4 \xi^2$$

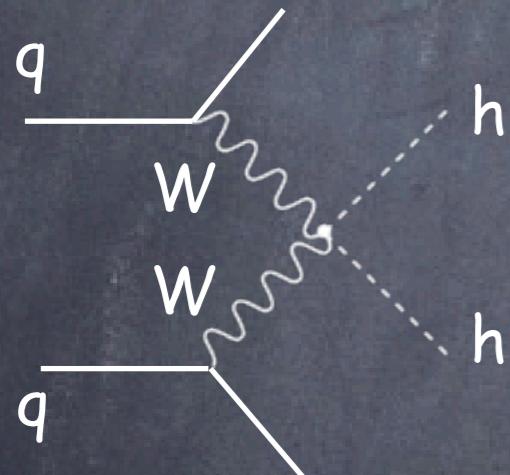
- hard cross-section = faster growth with energy
- onset of strong scattering still at high scale

Strong Higgs production

$O(4)$ symmetry between W_L, Z_L and the physical Higgs

strong boson scattering \Leftrightarrow strong Higgs production

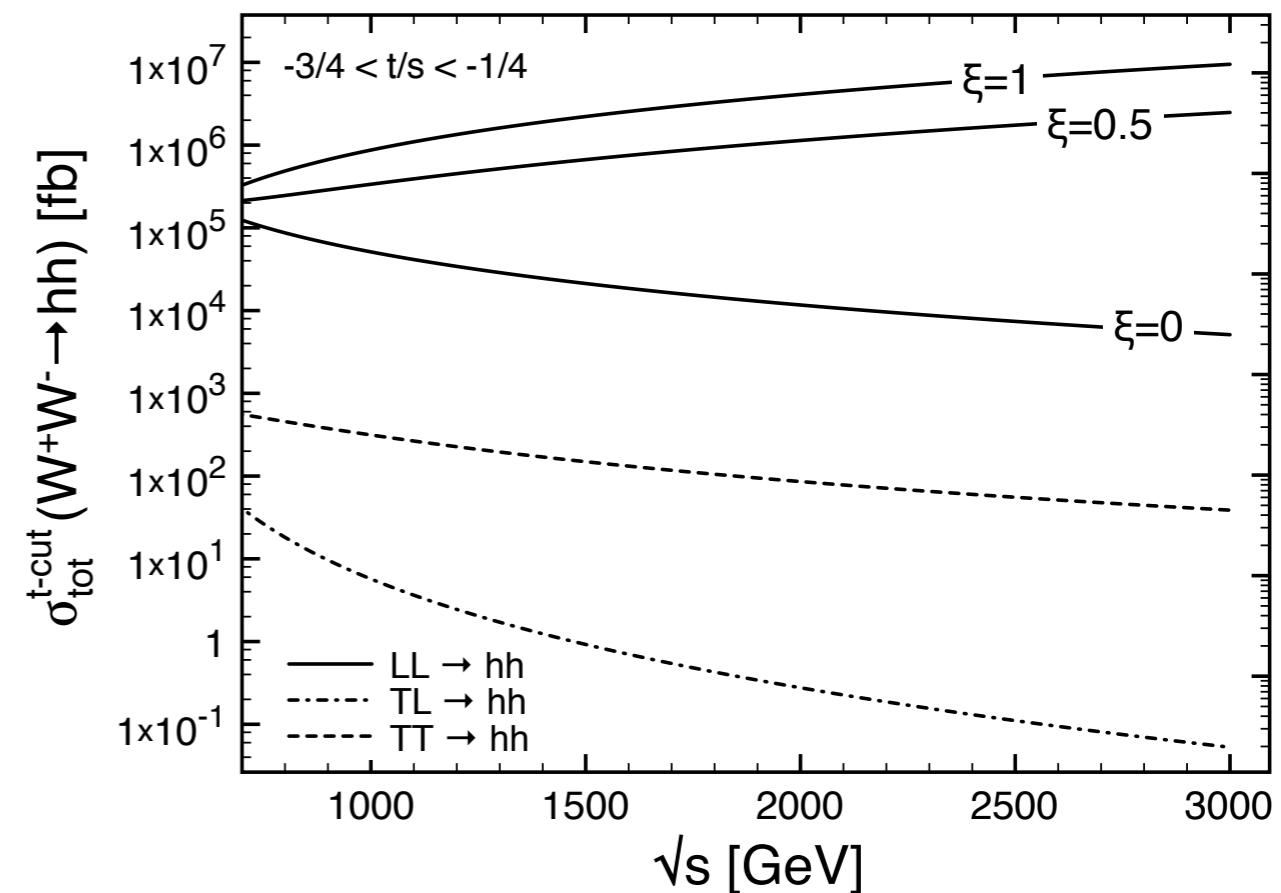
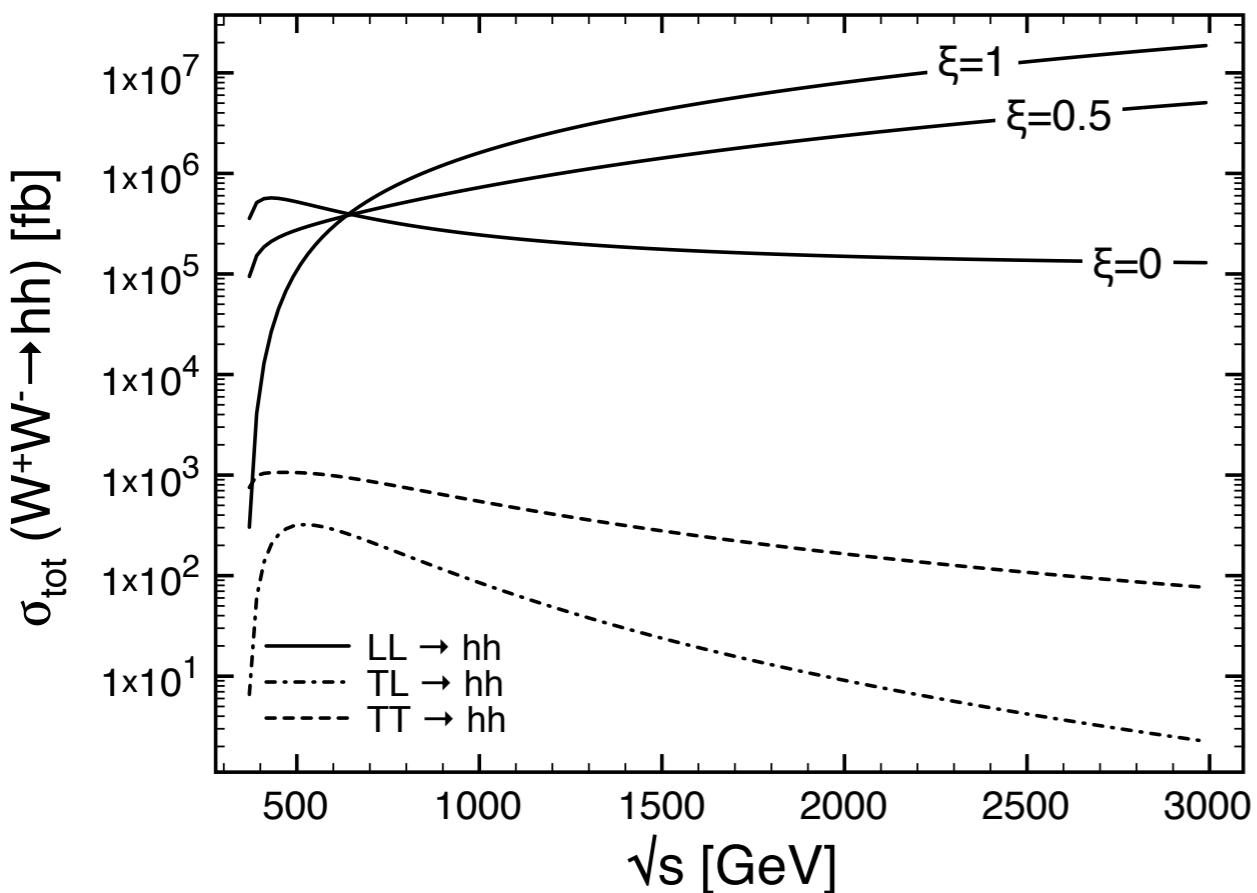
$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow hh) = \mathcal{A}(W_L^+ W_L^- \rightarrow hh) = \frac{c_{HS}}{f^2}$$



- signal:
- $hh \rightarrow bbbb$
 - $hh \rightarrow 4W \rightarrow 3l^\pm 3\nu + \text{jets}$

More complicated final states than for $WW \rightarrow WW$,
smaller BRs,
but no T polarization pollution

EW bckg for $WW \rightarrow hh$



$$\frac{d\sigma^{LL \rightarrow hh}/dt}{d\sigma^{TT \rightarrow hh}/dt} = \frac{1}{8} \frac{\xi^2}{\xi^2 + (1 - \xi)^2} \left(\frac{\sqrt{s}}{M_W} \right)^4$$

no T polarization pollution,
neither in the total cross section,
nor in the central region

Strong Higgs production: (3L+jets) analysis

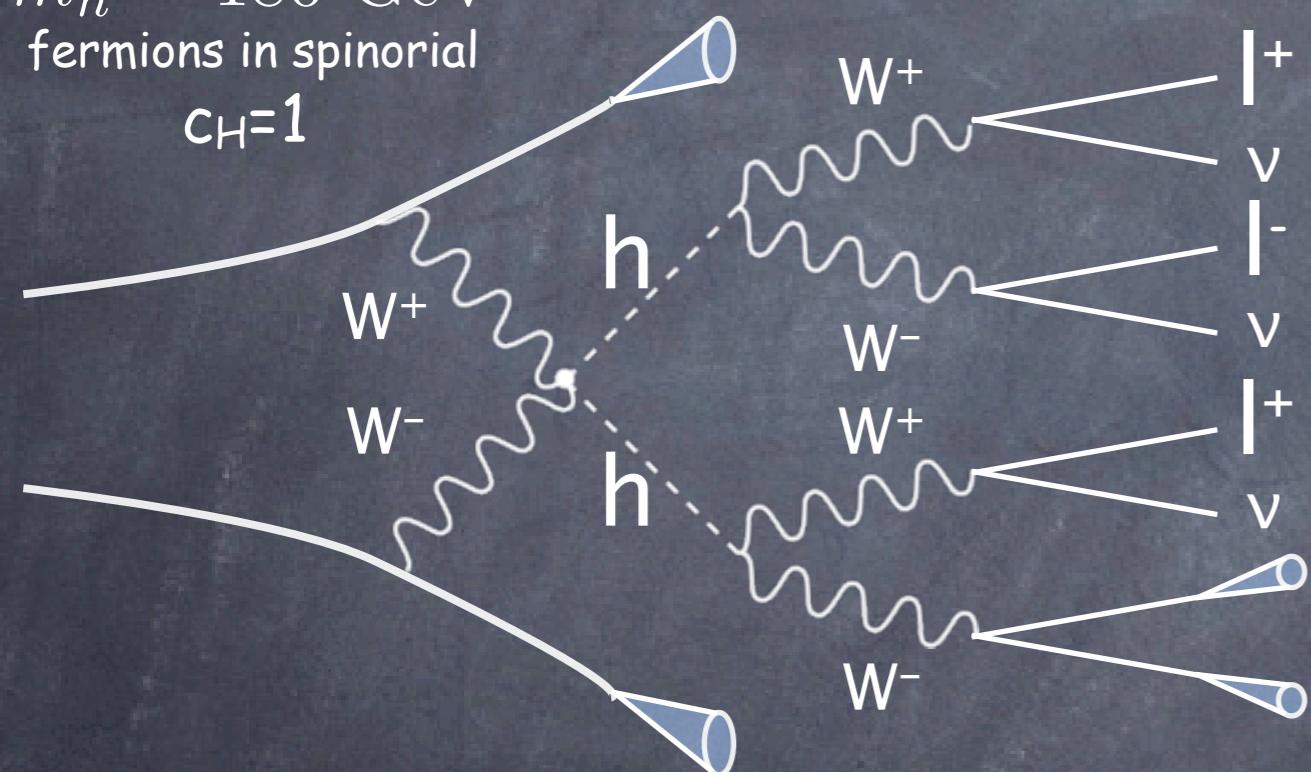
Contino, Grojean, Moretti, Piccinini, Rattazzi ‘in progress’

strong boson scattering \Leftrightarrow strong Higgs production

$$\mathcal{A}(Z_L^0 Z_L^0 \rightarrow hh) = \mathcal{A}(W_L^+ W_L^- \rightarrow hh) = \frac{c_H s}{f^2}$$

$m_h = 180$ GeV
fermions in spinorial

$$c_H=1$$



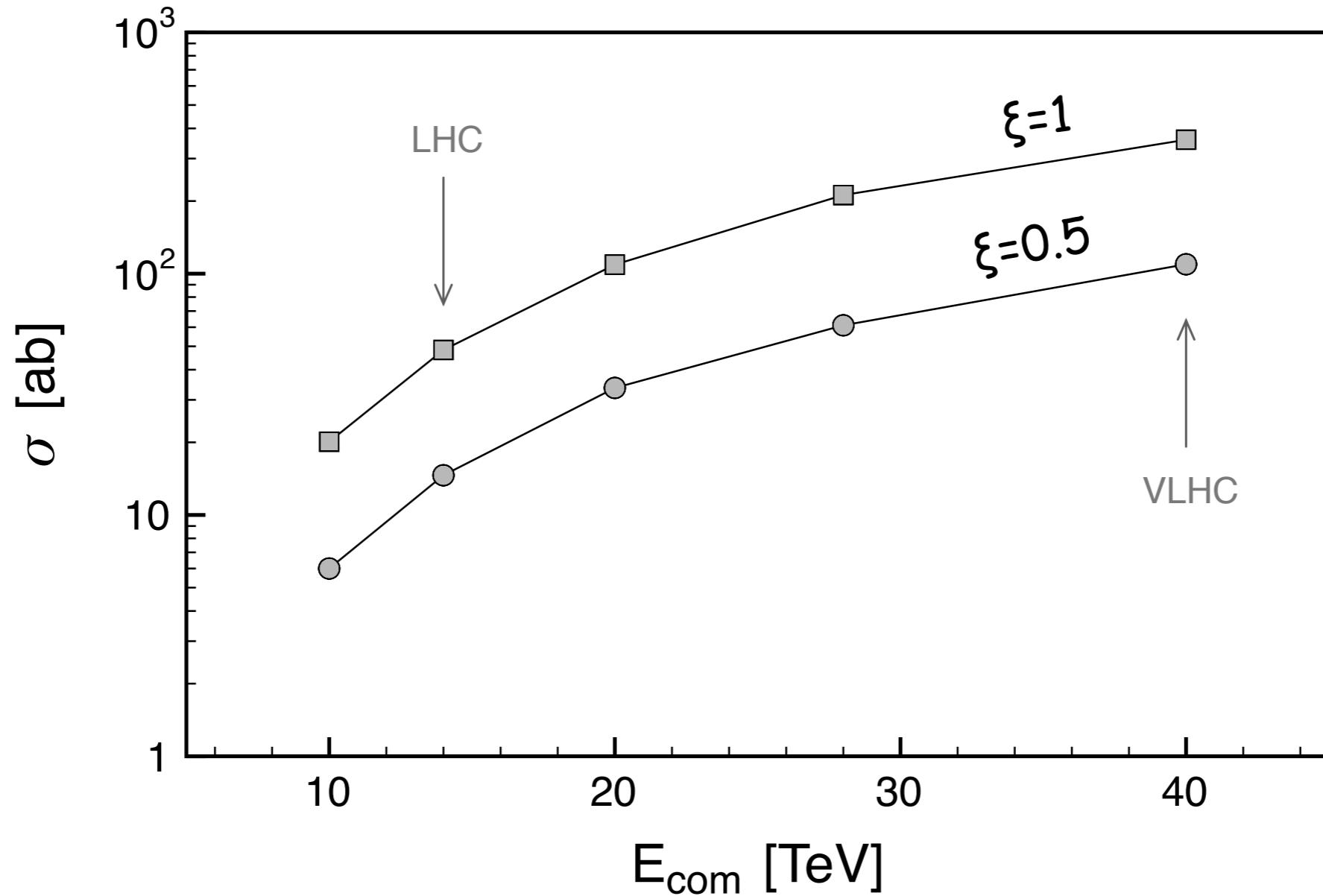
acceptance cuts	
jets	leptons
$p_T \geq 30$ GeV	$p_T \geq 20$ GeV
$\delta R_{jj} > 0.7$	$\delta R_{lj(l\bar{l})} > 0.4(0.2)$
$ \eta_j \leq 5$	$ \eta_j \leq 2.4$

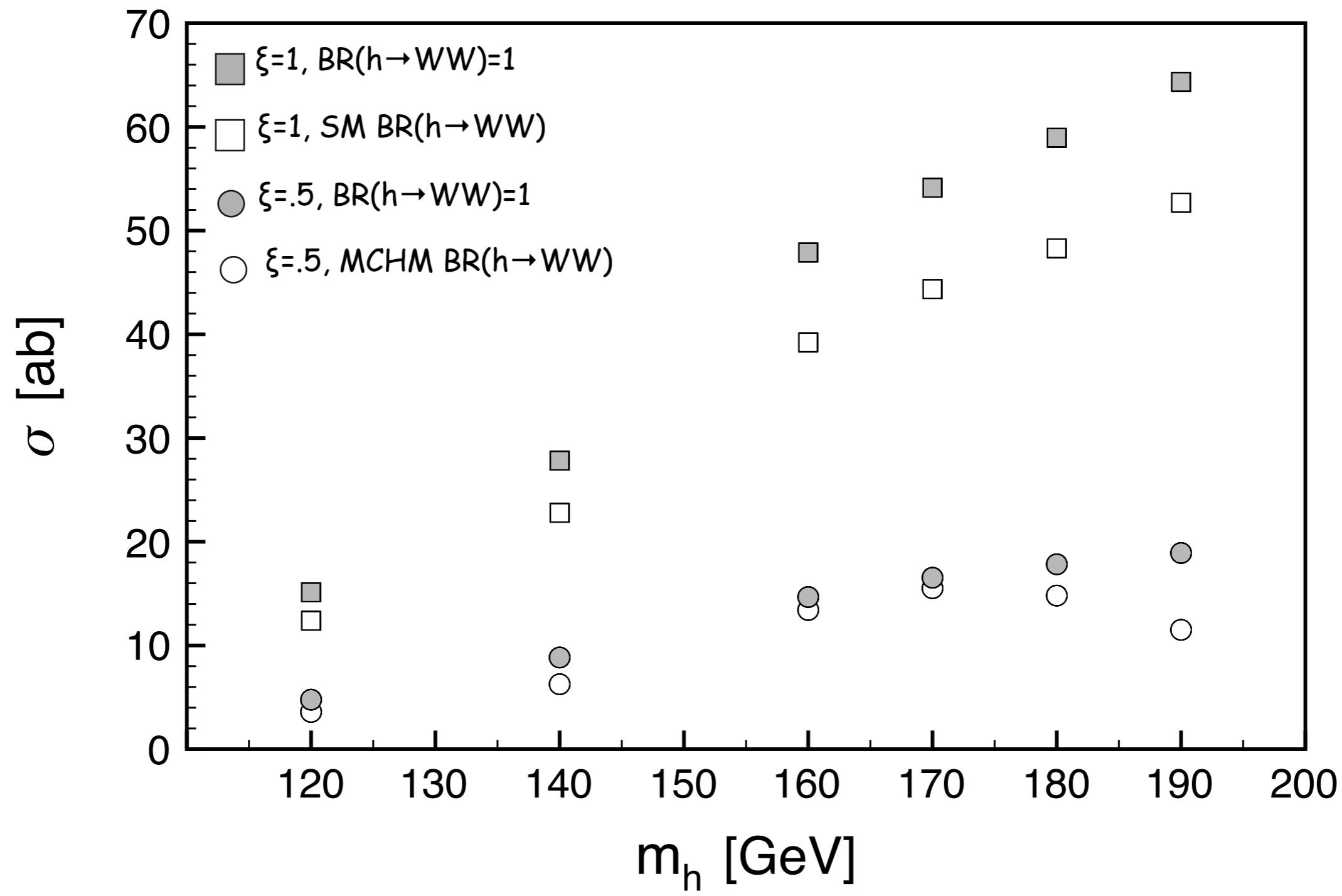
Dominant backgrounds: $Wl\bar{l}4j$, $t\bar{t}W2j$, $t\bar{t}2W$, $3W4j$...

forward jet-tag, back-to-back lepton, central jet-veto

v/f	1	$\sqrt{.8}$	$\sqrt{.5}$
significance (300 fb $^{-1}$)	4.0	2.9	1.3
luminosity for 5σ	450	850	3500

◀ good motivation to SLHC





Conclusions

EW interactions need Goldstone bosons to provide mass to W, Z

EW interactions need a UV moderator/new physics
to unitarize WW scattering amplitude

Not just the search for the Higgs boson
(still another particle, even though the missing one?)

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Not just the search for the Higgs boson
(still another particle, even though the missing one?)

	LHC	ILC	CLIC
1/ is there a Higgs?	✓	✓	✓
2/ what are the Higgs mass/couplings	✓/-	✓	✓
3/ is the Higgs a SM like weak doublet?	?	✓	✓
4/ is the Higgs elementary or composite?	?	✓	✓✓
5/ is EWSB natural or fine-tuned?	?	✓	✓✓
6/ are there new dimensions? new strong forces?	-	✓	✓

"theorists are getting cold feet" J. Ellis

"they have done their best to predict the possible and impossible"

G. Giudice

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I guess, during these lectures, I gave you a flavour of what the impossible could be!



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LHC is prepared to discover the "Higgs"

collaboration EXP-TH is important to make sure

e.g. that no unexpected physics is missed (triggers, cuts...)

and in this regards, approaches like "unparticle" or "hidden valleys" might be useful.

Thank you for your attention