

Low energy parameters
and new physics

or

What you might need from low energy physics
if and when you find new physics

Paolo Franzini

Frascati, 16 May 2008

1. History
2. Introduction
3. KLOE
4. K_L , K_S , K^\pm decays
5. $|V_{us}|^2$
6. $|V_{us}|^2/|V_{ud}|^2$
7. Unitarity and universality



History

1947: Rochester and Butler, $K^0 \rightarrow \pi^+ \pi^-$, $K^+ \rightarrow \pi^+ \pi^0$

... 60 Years of hard work...

2008: KLOE first round, $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9996 \pm 0.0007$



Standard Model

$$\frac{g}{\sqrt{2}} W_\alpha^+ (\bar{\mathbf{U}}_L \mathbf{V}_{CKM} \gamma^\alpha \mathbf{D}_L + \bar{e}_L \gamma^\alpha \nu_{eL} + \bar{\mu}_L \gamma^\alpha \nu_{\mu L} + \bar{\tau}_L \gamma^\alpha \nu_{\tau L}) + \text{h.c.}$$

There is just one gauge coupling g , $G_F = g^2 / (4\sqrt{2} M_W^2)$

The quarks are mixed by a unitary matrix \mathbf{V}

Quarks and leptons have the same weak charge

At the opposite extreme:

$$g_q, g_e, g_\mu, g_\tau$$

\mathbf{V} is not unitary

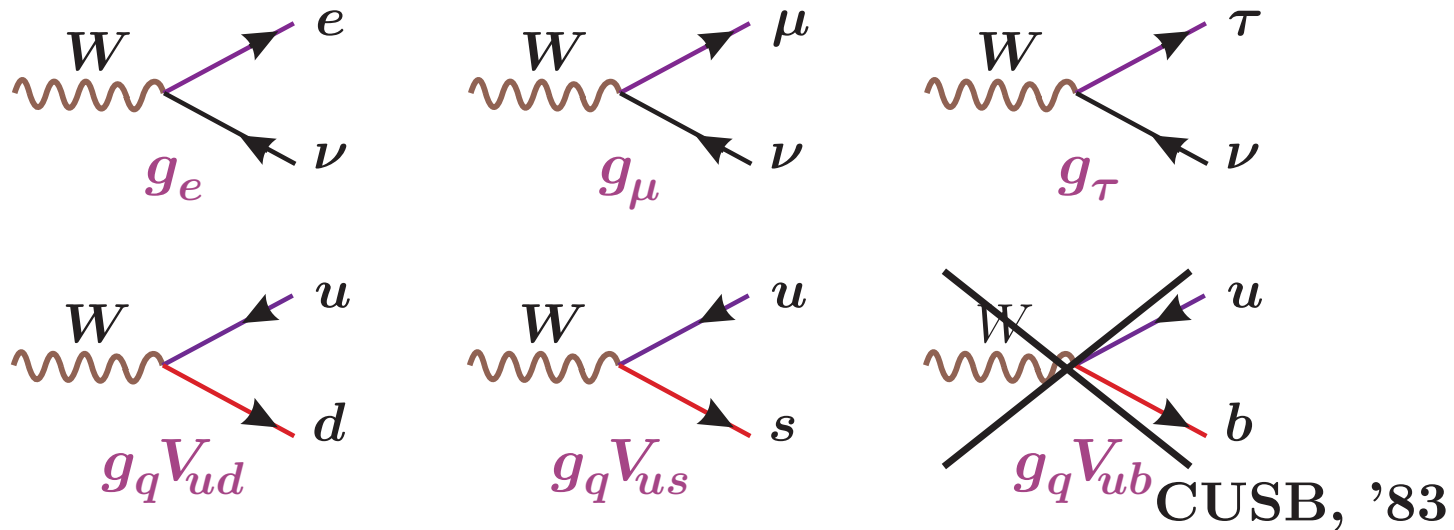
(But probabilities are conserved!)

$$\mathbf{U} = \begin{pmatrix} u \\ c \\ t \end{pmatrix}, \quad \mathbf{D} = \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$$\mathbf{V} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{ud} & V_{us} & V_{ub} \\ V_{ud} & V_{us} & V_{ub} \end{pmatrix}$$



We can measure



With kaons, pions, nuclear β -decay, and muons we can measure

g_e, g_μ, g_q, V_{ud} and V_{us}

and check whether $g_e = g_\mu = g_q, |V_{ud}|^2 + |V_{us}|^2 = 1$



Decay Width

From $\langle f | J_\alpha J^\alpha | i \rangle \Rightarrow$

$$\Gamma(|\Delta S|=1) = |V_{us}|^2 \times G^2 \times F_1(wi) \times F_2(\text{emi}) \times F_3(\text{si}).$$

- ~~1. F_1 : kinematics, spinor algebra, phase space, OK~~
- ~~2. F_2 : Cannot turn off electromagnetism. Painfull but calculable. Few % correction. to .1% accuracy~~
- ~~3. F_3 : Strong interactions are hardest to compute, can have large effects, choose best processes, lattice to the rescue!~~



Radiation inclusive branching ratios

Inclusion (or exclusion) of photons does affect event acceptance. It is modern practice to give results fully inclusive of radiation up to the kinematic limit. This requires correct accounting of radiation in the Monte Carlo detector simulation program.

In the KLOE MC simulation, Geant4, radiation is included at the event generation level, event by event. In the following, even if not explicitly stated, BRs are totally inclusive of radiation.

$BR(K \rightarrow f(\gamma))$ stands for $BR(K \rightarrow f, f+\gamma, 0 < \omega < \omega_{\max})$

I will also just use $BR(K \rightarrow f)$



F₃ – SI – Hadrons vs Quarks

Nuclear β -decay. Look at $0^+ \rightarrow 0^+$ transitions. No axial current.
 CVC helps with nuclear matrix elements.

$|\Delta S| = 1$ decays. Corrections to

$$\langle f | \bar{u} \gamma_\alpha s | i \rangle$$

appear only at 2nd order in $m_s - m_d$. A-G theorem.

Kaon semileptonic decays. $K \rightarrow \pi \ell \nu \Rightarrow 0^- \rightarrow 0^-$.

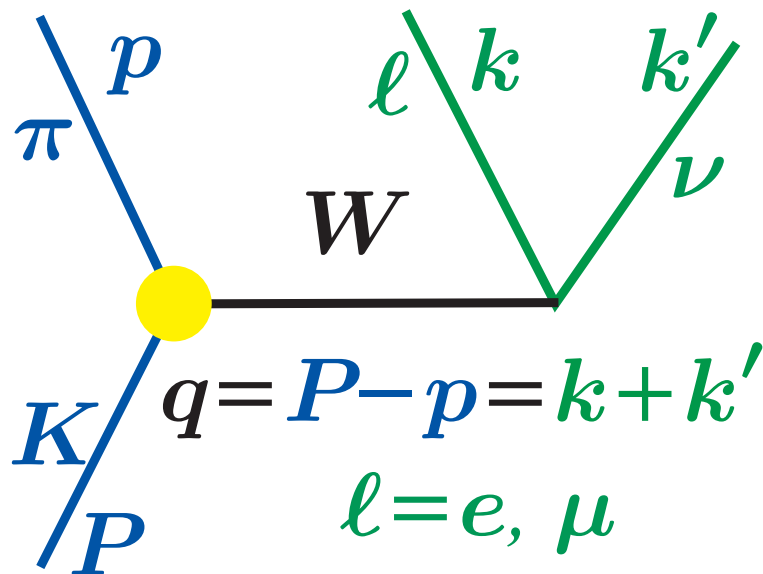
Only vector part of current contributes to

$$\langle \pi | \bar{u}_L \gamma_\alpha s_L | K \rangle$$

$$\langle \pi | \bar{u} \gamma_\alpha s | K \rangle = f_+(t)(P + p)_\alpha + f_-(t)(P - p)_\alpha$$



Vector Current is protected



$$\langle \pi | J_\alpha | K \rangle = f_+(0) \times \left((P + p)_\alpha \tilde{f}_+(t) + (P - p)_\alpha (\tilde{f}_0(t) - \tilde{f}_+(t)) \frac{\Delta}{t} \right)$$

$$\Delta = M^2 - m^2$$

Form factor because K , π are not point like

Scalar and vector FFs equal at $t=0$ (by construction)

Factor out $f_+(0)$. $f_+(0) < 1$ because $K \neq \pi$

$f_+(0) - 1 \ll 1$ (0.04) – small SU(3) breaking

$$\tilde{f}_+(0) = \tilde{f}_0(0) = 1$$



Decay Width

$$\Gamma(K_{\ell 3}(\gamma)) = \frac{C_K^2 G_F^2 M_K^5}{768 \pi^3} S_{EW} \boxed{|V_{us}|^2 f_+(0)^2} I_{K\ell} \times \left(1 + \delta_K^{SU(2)} + \delta_{K\ell}^{EM} \right)$$

192
128

$C_K^2 = 1(1/2)$ for $K^0(K^\pm)$; $S_{EW} = 1.0232(3)$, EW corr, Sirlin
 $I_{K\ell}$ phase space integral

Define

$f_+(0)$ as

$f_+^{K^0 \rightarrow \pi^\pm}(0)$

| | $\delta_K^{SU(2)} (\%)$ | $\delta_{K\ell}^{EM} (\%)$ |
|---------------|-------------------------|----------------------------|
| K_{e3}^0 | 0 | +0.57(15) |
| K_{e3}^+ | 2.36(22) | +0.08(15) |
| $K_{\mu 3}^0$ | 0 | +0.80(15) |
| $K_{\mu 3}^+$ | 2.36(22) | +0.05(15) |



Phase space integral, K_{e3}

$$\rho(E_e, E_\nu) \propto \sum_{\text{spins}} |\mathfrak{M}|^2 \propto G^2 C_K^2 M^4 \left[\frac{E_e}{M} \frac{E_\nu}{M} + \frac{\vec{k} \cdot \vec{k}'}{M^2} \right]$$

$$I_{K\ell} \propto \iint \rho(E_e E_\nu) dE_e dE_\nu$$

$$\Gamma = \frac{G^2 C_K^2 M_K^5}{768 \pi^3} \underbrace{\int_{z_m}^{z_M} dz f(t)^2 \int_{x_m(z)}^{x_M(z)} \frac{24}{((z+x-1)(1-x) - \alpha)} dx}_{I_{K\ell}}$$

With 768 in the denominator, $f(t)=1$, all final state masses zero:

$$I_{K\ell} = 1.0$$

768 corresponds to 192 in muon decay rate. $I_{K\ell}$ is dimensionless.

$$x = \frac{2E_e}{M}, \quad y = \frac{2E_\nu}{M}, \quad z = \frac{2E_\pi}{M}, \quad \alpha = \frac{m}{M}$$

End of introduction



DAΦNE

An e^+e^- collider operated (mostly) at $W = M_\phi$

$$e^+e^- \rightarrow \phi \rightarrow \begin{cases} K_S + K_L & 34.0\% \text{ tagged } K_S, K_L \text{ beams} \\ K^+ + K^- & 49.3\% \text{ tagged } K_S, K_L \text{ beams} \end{cases}$$

⇒ Tagged, monochromatic, pure K_S, K_L, K^+, K^- beams

$$\text{BR}(K_S \rightarrow \pi \ell \nu) = (7.04 + 4.69) \times 10^{-4} \quad \text{“difficult”}$$

$$\text{BR}(K^\pm \rightarrow \pi \ell \nu) = (4.98 + 3.32) \times 10^{-2} \quad \text{“so so”}$$

$$\text{BR}(K_L \rightarrow \pi \ell \nu) = (4.06 + 2.71) \times 10^{-1} \quad \text{“best”}$$

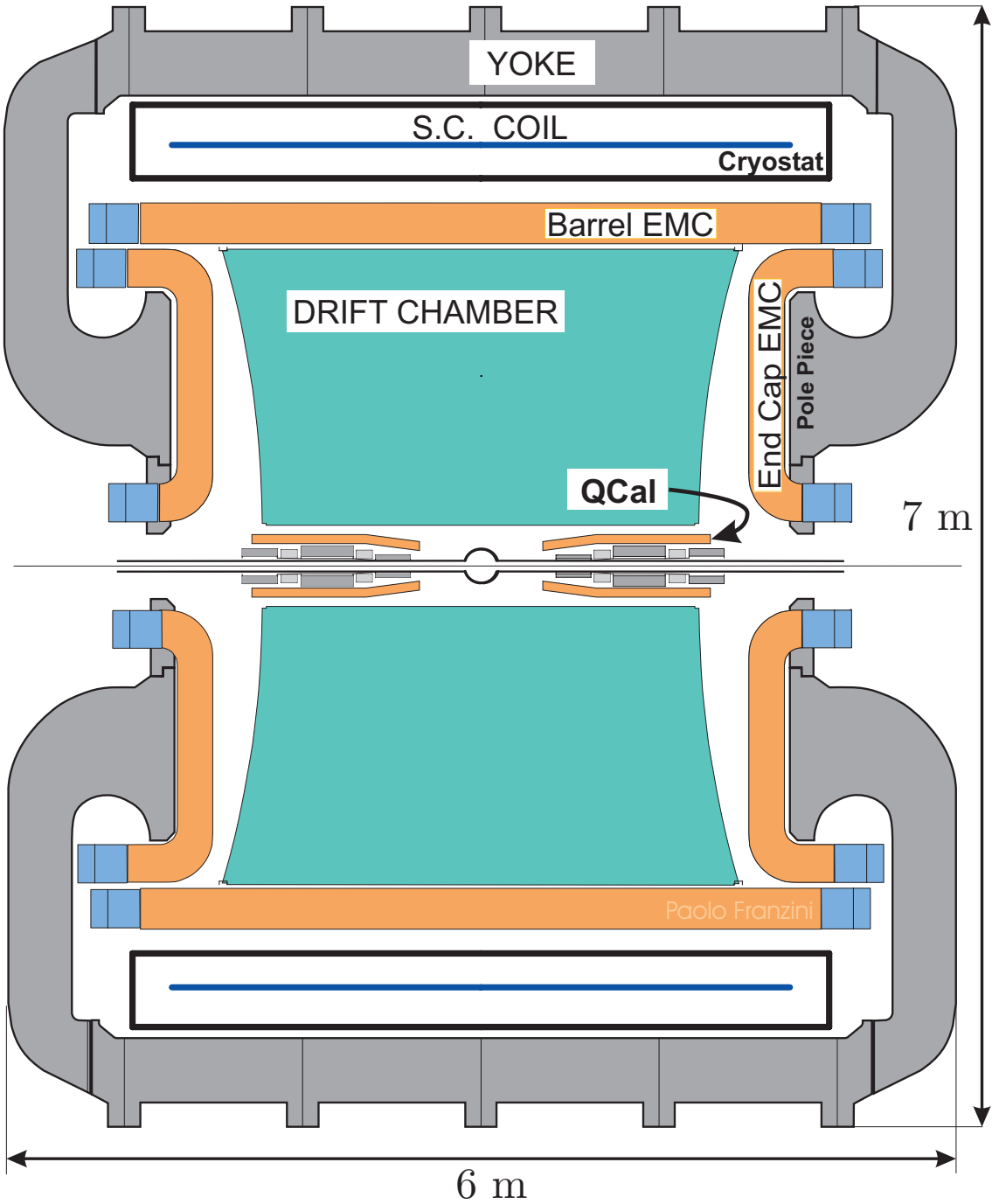
$e \quad \mu$

KLOE: measure all **BR**, lifetimes,

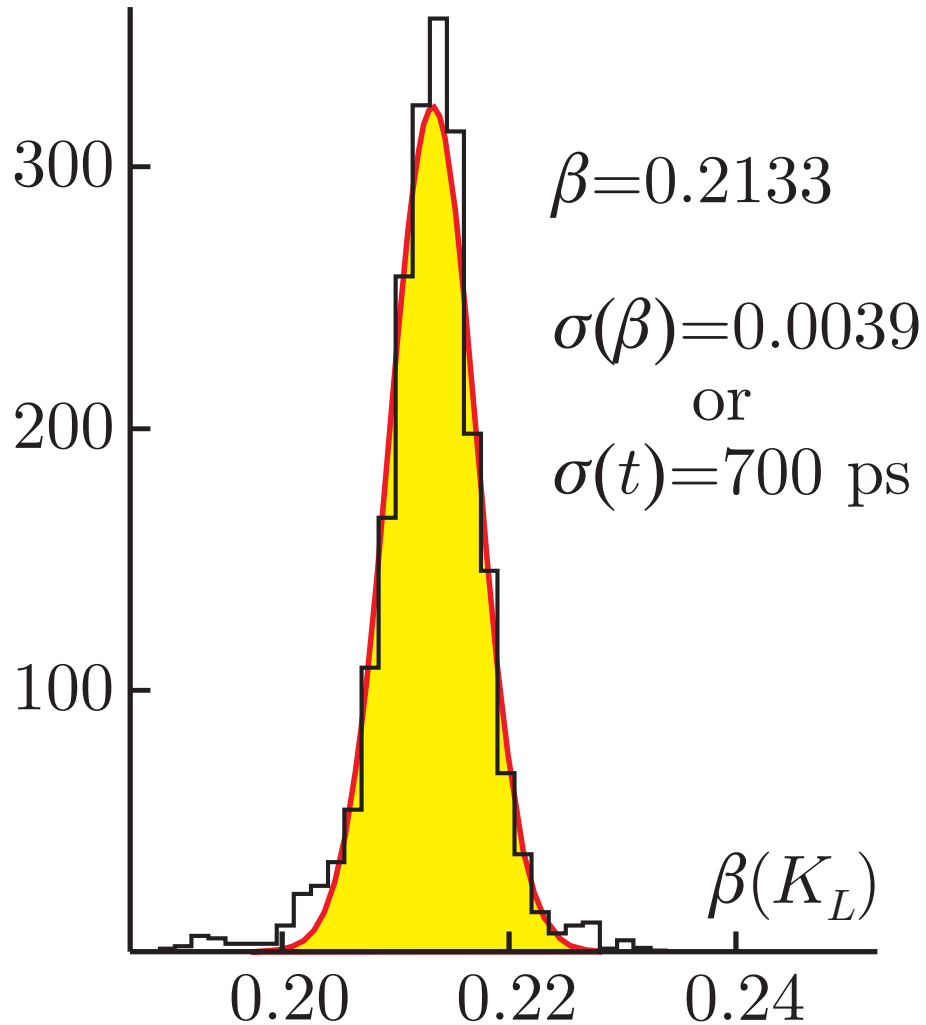
FF parameters $\Rightarrow \Rightarrow \Gamma(K_i \rightarrow f)$



KLOE



The K_S beam

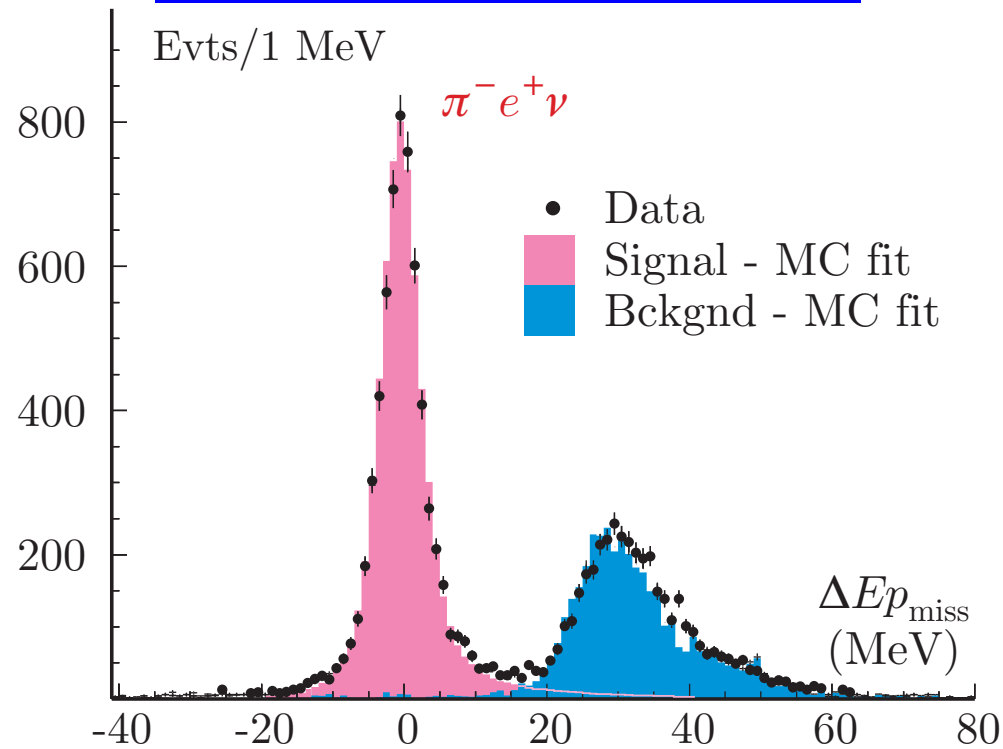


$\sim 50\%$ of the K_L -mesons reach the calorimeter where most interact. Since $\beta(K^0) \sim 0.2$, we identify kaon interactions by TOF.

$\delta W(\text{DA}\Phi\text{NE}) = 1 \text{ MeV}$
gives $\delta\beta = 0.004$



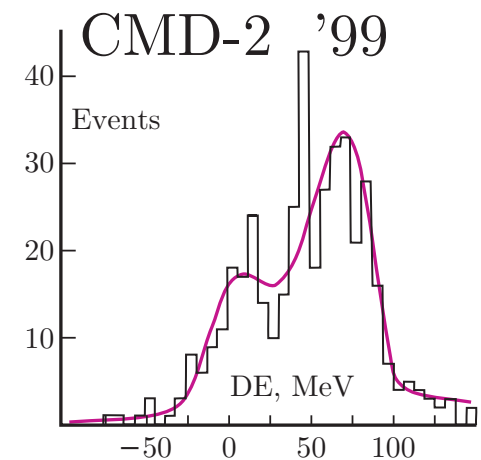
$K_S \rightarrow \pi e \nu$, 2005



$\sim 13,000$ signal events

$$\text{BR}(K_S \rightarrow \pi e \nu) = (7.046 \pm 0.091) \times 10^{-4}$$

$|V_{us}|$ to 0.7%



K_L decays

$$\text{BR}(K_{e3}) + \text{BR}(K_{\mu3}) + \text{BR}(K \rightarrow 3\pi^0) + \text{BR}(K \rightarrow \pi^{+-0}) = 1 - \Delta$$

Solve for : $\begin{cases} 4 \text{ BRs} \\ K_L \text{ lifetime} \end{cases}$

$$\text{BR}(K_{Le3}) = 0.4009 \pm 0.0015$$

$$\text{BR}(K_{L\mu3}) = 0.2699 \pm 0.0014$$

$$\text{BR}(K_L \rightarrow 3\pi^0) = 0.1996 \pm 0.0020$$

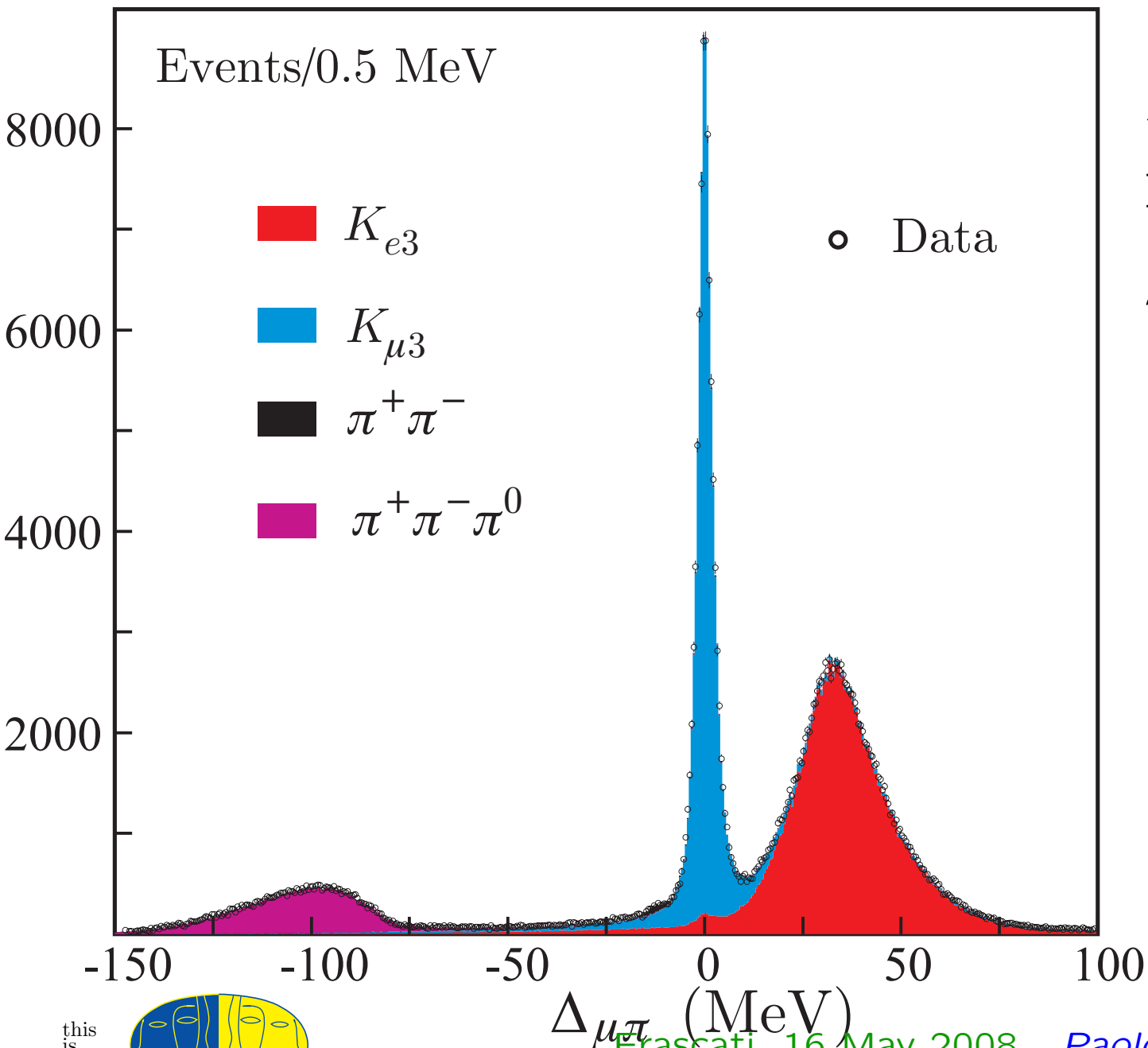
$$\text{BR}(K_L \rightarrow \pi^{+-0}) = 0.1261 \pm 0.0011$$

$$\tau(K_L) = 50.72 \pm 0.37 \text{ ns}$$

There are of course correlations...



K_L → two track events



For $K_L \rightarrow \pi^\pm \ell^\mp \nu$:

$E_{\text{miss}} \neq 0$

$\mathbf{p}_{\text{miss}} \neq 0$

$m_\nu = 0 \rightarrow$

$\Delta = E_{\text{miss}} - |\mathbf{p}_{\text{miss}}| = 0$

$\Delta_{\mu\pi} = \text{smallest of}$

$\Delta_{\mu^+\pi^-}, \Delta_{\pi^+\mu^-}$

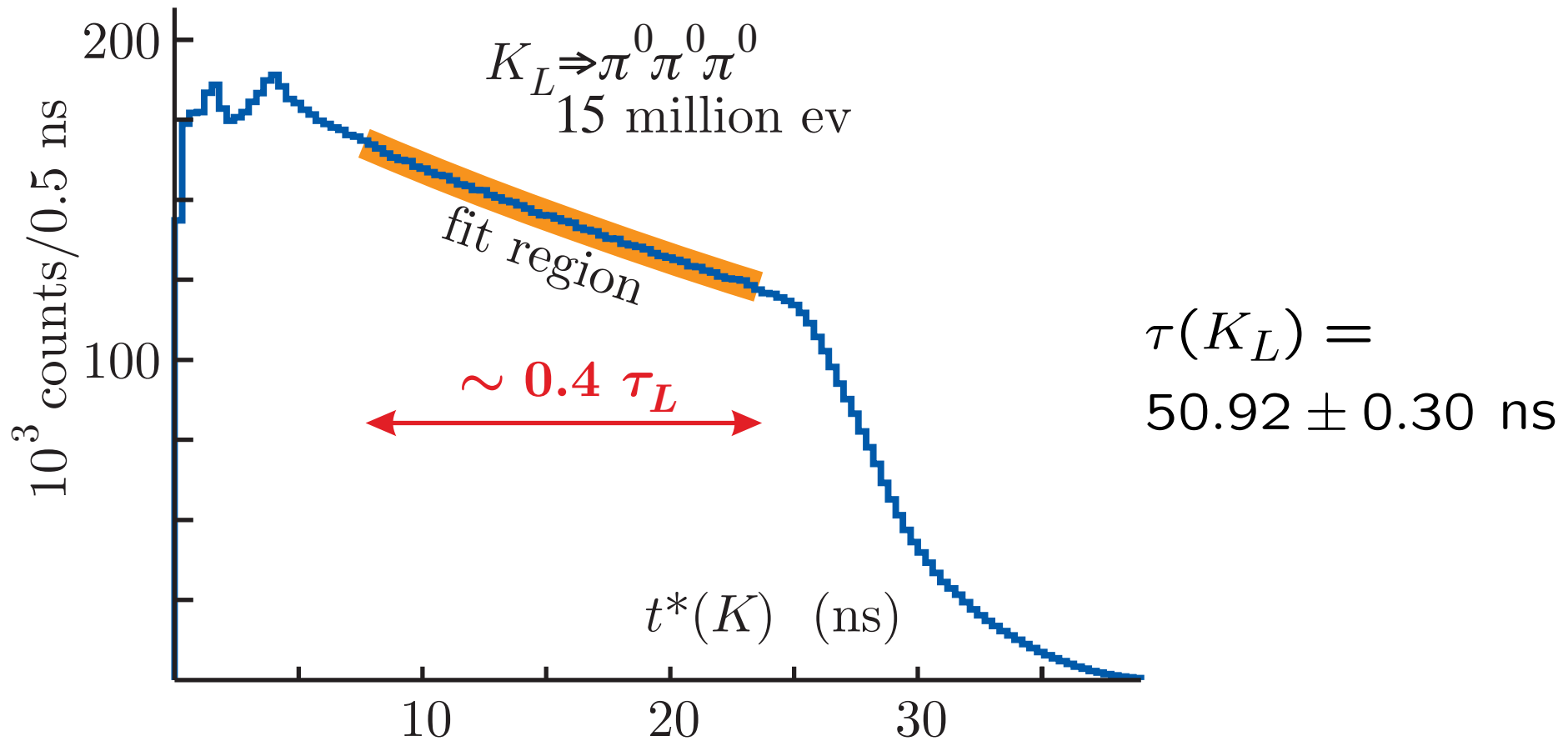
Fit to MC shapes

Count, BRs

14 sub-samples



Time dependence of $K_L \rightarrow \pi^0 \pi^0 \pi^0$



All KLOE K_L results

| Param. | Value | Correlation coefficients | | | | | | |
|--------------------|--------------------------|--------------------------|-------|-------|-------|-------|-------|-------|
| $BR(K_{Le3})$ | 0.4008(15) | | | | | | | |
| $BR(K_{L\mu3})$ | 0.2699(14) | -0.31 | | | | | | |
| $BR(3\pi^0)$ | 0.1996(20) | -0.55 | -0.41 | | | | | |
| $BR(\pi^+\pi^-)$ | 0.1261(11) | -0.01 | -0.14 | -0.47 | | | | |
| $BR(\pi^+\pi^-)$ | $1.96(2) \times 10^{-3}$ | -0.15 | 0.50 | -0.21 | -0.07 | | | |
| $BR(\pi^0\pi^0)$ | $8.49(9) \times 10^{-4}$ | -0.15 | 0.48 | -0.20 | -0.07 | 0.97 | | |
| $BR(\gamma\gamma)$ | $5.57(8) \times 10^{-4}$ | -0.37 | -0.28 | 0.68 | -0.32 | -0.14 | -0.13 | |
| τ_L | 50.84(23) ns | 0.16 | 0.22 | -0.14 | -0.26 | 0.11 | 0.11 | -0.09 |

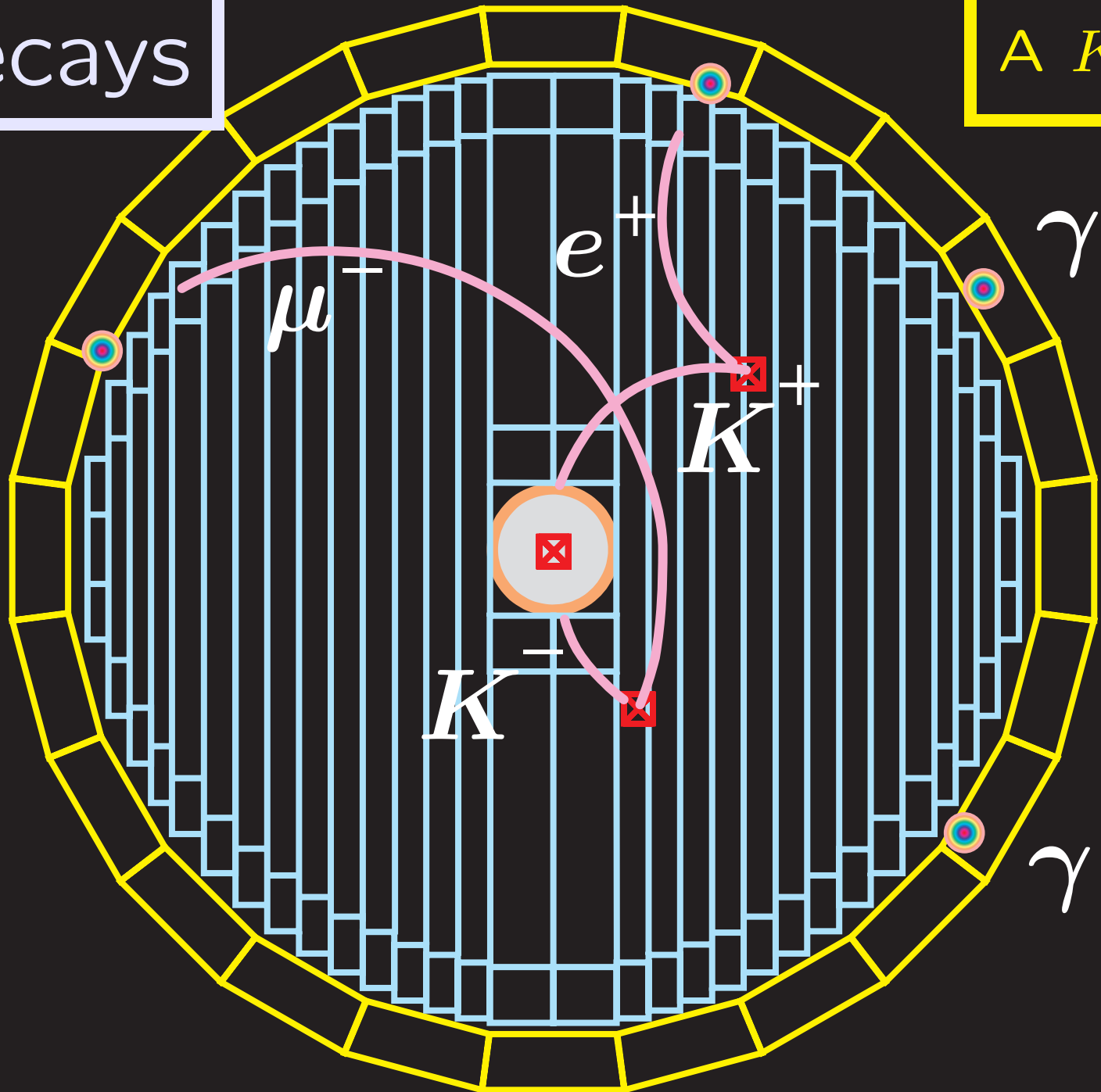
We can do it!

When PDG does it, combining inconsistent results from different experiments it can be a disaster!!!

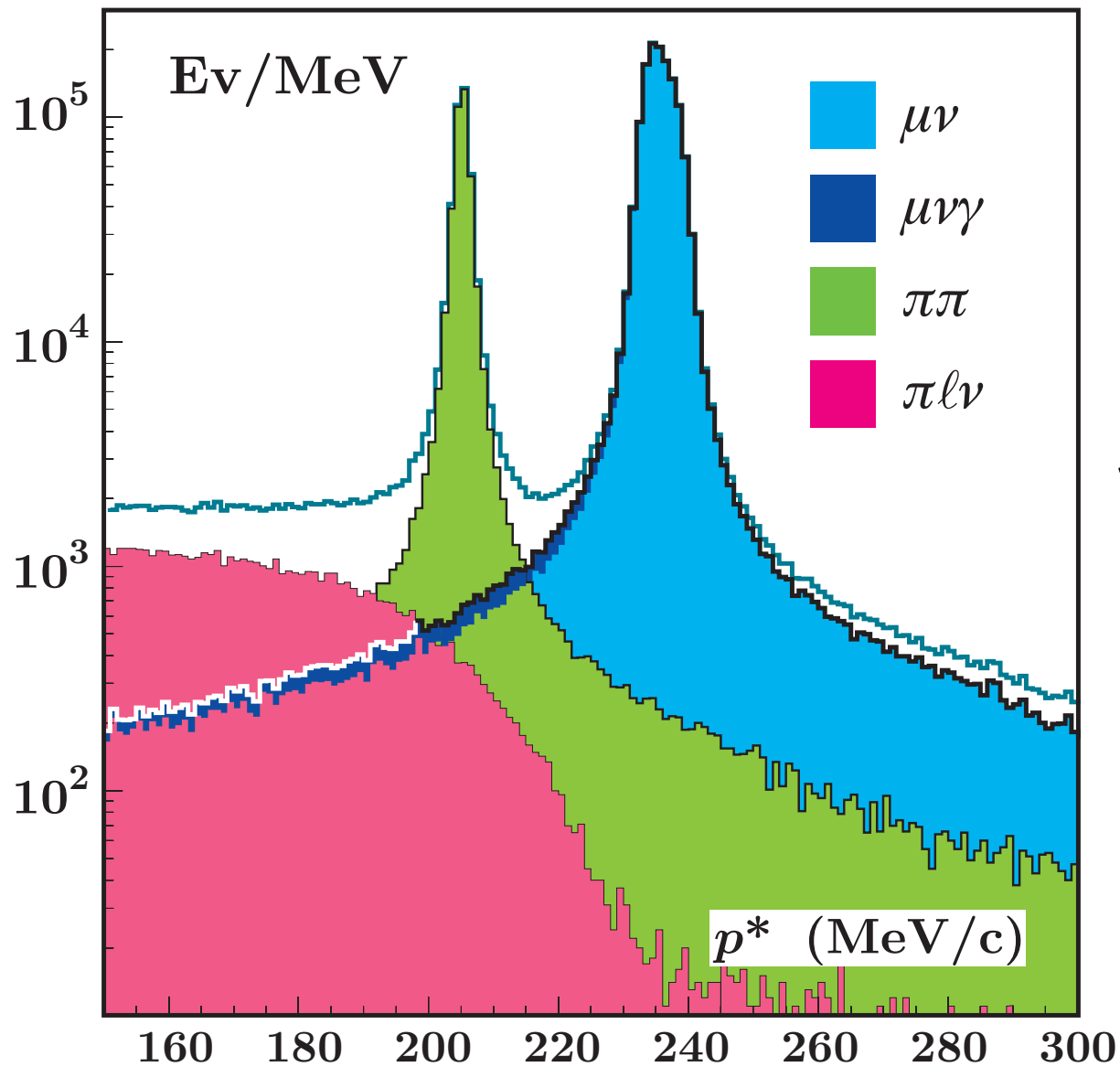


K^\pm decays

A K_{e3}^\pm decay



Tagging decays and $K^\pm \rightarrow \mu\nu$ decays



Compute CM momentum using $m(\pi)$. The $\mu\nu$ decay peak is distorted but quite recognizable for tagging.

We also get

$\text{BR}(K \rightarrow \mu\nu(\gamma))$ and

$\text{BR}(K \rightarrow \pi\pi^0(\gamma))$

Note the radiative tail!

$$\text{BR}(K^+ \rightarrow \mu^+\nu(\gamma)) = 0.6366 \pm 0.0009 \pm 0.0015.$$



All KLOE K^\pm results

Constrained fit:

$$\text{BR}(K^\pm \rightarrow \mu^\pm \nu) = 0.63766 \pm 0.0012$$

$$\text{BR}(K^\pm \rightarrow \pi^\pm \pi^0) = 0.2071 \pm 0.0009$$

$$\text{BR}(K^\pm \rightarrow \pi^\pm \pi^+ \pi^-) = 0.0553 \pm 0.0009 \text{ (input PDG '04)}$$

$$\text{BR}(K^\pm \rightarrow e^\pm \pi^0 \nu) = 0.0498 \pm 0.0005$$

$$\text{BR}(K^\pm \rightarrow \mu^\pm \pi^0 \nu) = 0.0324 \pm 0.0004$$

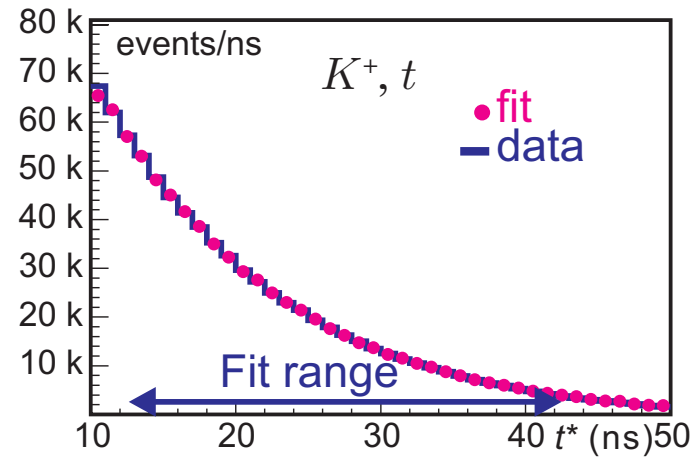
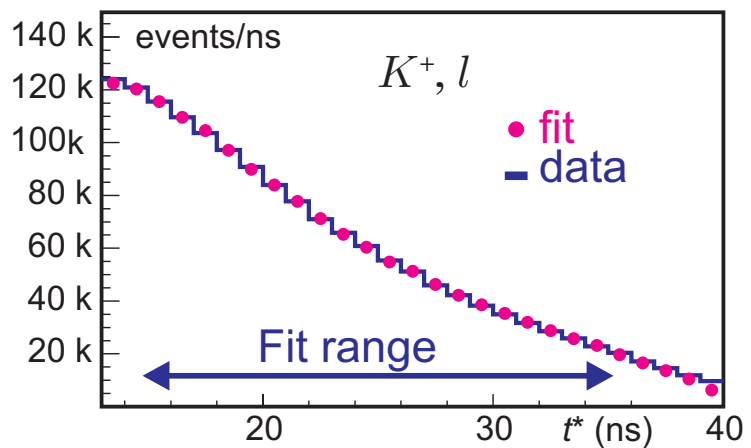
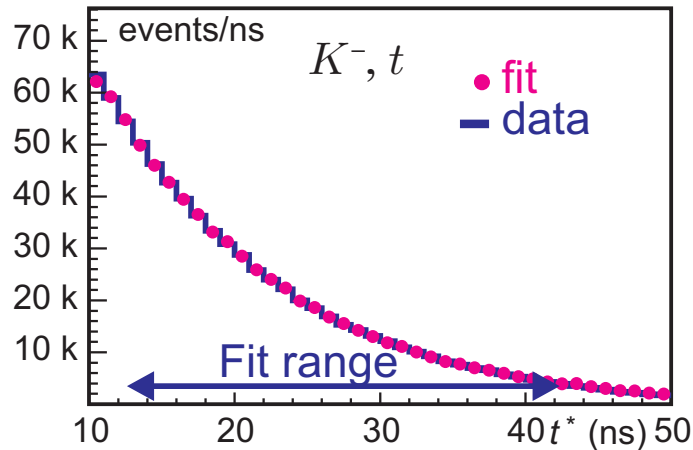
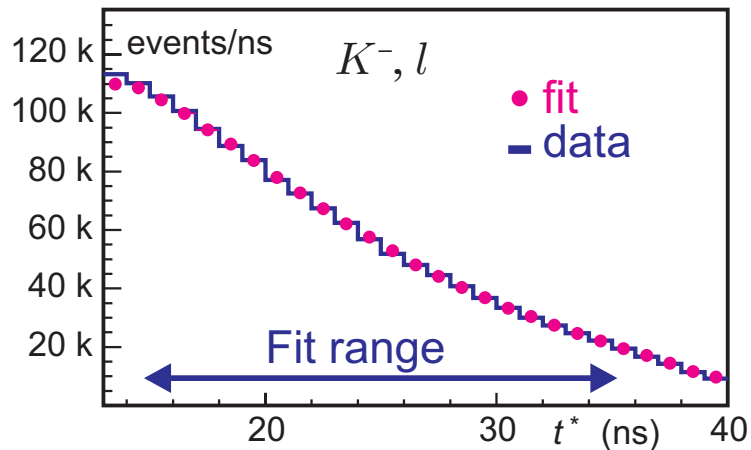
$$\text{BR}(K^\pm \rightarrow \pi^\pm \pi^0 \pi^0) = 0.01765 \pm 0.00025$$

$$\tau \text{ (ns)} = 12.344 \pm 0.029$$

$$\chi^2/\text{dof} = 0.59/1, \text{ CL}=44\%$$



KLOE $\tau(K^\pm)$



4 measurement
of τ –

Consistent –

Can average

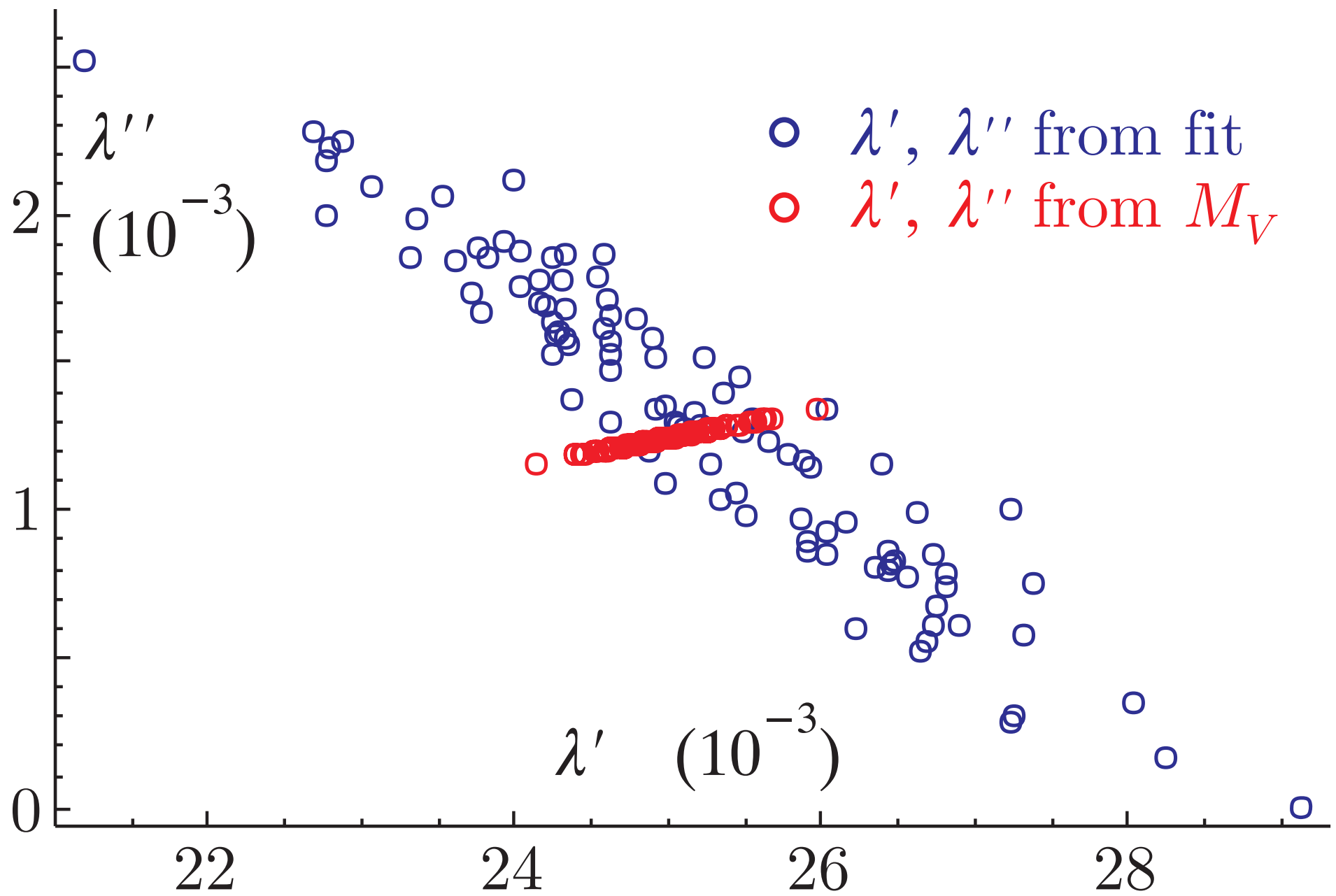
Use only our result

$$\tau(K^\pm) = 12.347 \pm 0.030, \quad 0.25\%$$

$$\tau(K^+)/\tau(K^\pm) = 1.004 \pm 0.004$$



FF: quadratic, pole, disp.



$$f(0)|V_{us}|$$

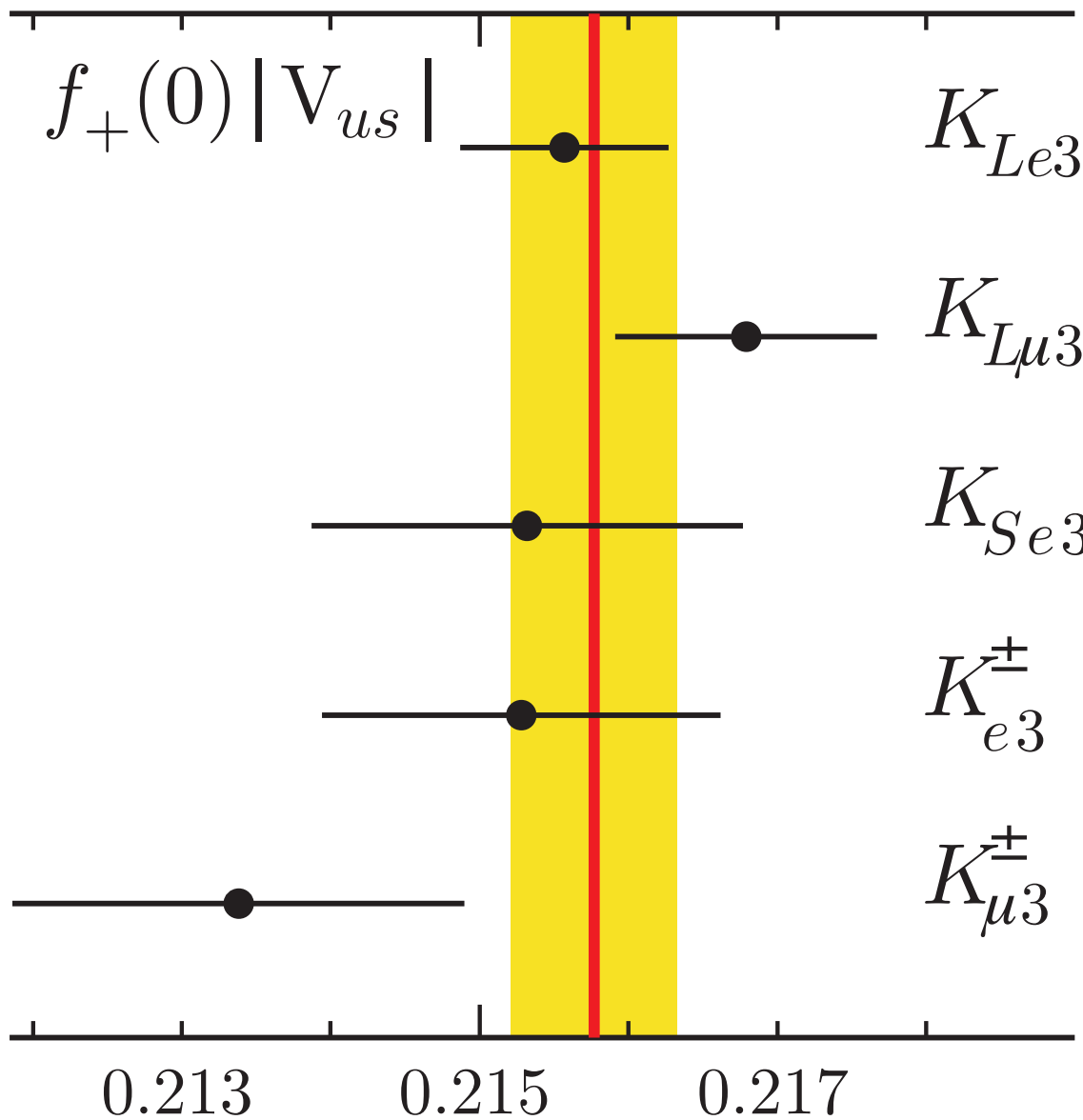
We are almost there. Let us begin with $f(0)|V_{us}|$. $f(0)$, by definition, belongs to $K^0 \rightarrow \pi^\pm$. If we know the I-spin corrections and the long distance EM corrections all decays must give the same value for $f(0)|V_{us}|$.

This is in fact a check of the $\delta \dots$ estimates and of the experiment. We find

| Channel | $f(0) V_{us} $ | Correlation coefficients | | | |
|----------------|----------------|--------------------------|------|------|------|
| K_{Le3} | 0.2155(7) | | | | |
| $K_{L\mu3}$ | 0.2167(9) | 0.28 | | | |
| K_{Se3} | 0.2153(14) | 0.16 | 0.08 | | |
| K_{e3}^\pm | 0.2152(13) | 0.07 | 0.01 | 0.04 | |
| $K_{\mu3}^\pm$ | 0.2132(15) | 0.01 | 0.18 | 0.01 | 0.67 |



$$f(0)|V_{us}|$$



$$\langle \rangle = -0.2157 \pm 0.0006$$

$$\chi^2/\text{ndf} = 7.0/4$$

(CL=13%)

$SU(2)$ corrections are verified to 1.1σ .



Lepton Universality

From:

$$R_{\mu e} \equiv \frac{[f(0)V_{us}]_{\mu 3}^2}{[f(0)V_{us}]_{e 3}^2} = \frac{\Gamma_{\mu 3} I_{e 3} (1 + \delta_e)^2}{\Gamma_{e 3} I_{\mu 3} (1 + \delta_\mu)^2}$$

\Rightarrow

$$R_{\mu e} = \frac{g_e^2}{g_\mu^2} = 1.000 \pm 0.008$$

Competitive with pure leptonic processes, τ decays

$$(R_{\mu e})_\tau = 1.000 \pm 0.004$$

Also with $\pi \rightarrow \ell \nu$ results

$$(R_{\mu e})_\pi = 1.0042 \pm 0.0033$$



$$f(0) \text{ and } |V_{us}|$$

The accepted value was $f(0) = 0.961 \pm 0.008$, Roos & Leutwyler, 1984. Recently Lattice results have become convincing. We take $f(0) = 0.9644 \pm 0.0049$, RBC and UKQCD, 2007. Then

$$|V_{us}| = 0.2237 \pm 0.0013$$

$$|V_{us}|^2 = 0.05002 \pm 0.00057$$

$$0^+ \rightarrow 0^+ \text{ and } |V_{ud}|^2$$

$$|V_{ud}|^2 = 0.9490 \pm 0.0005$$

$$1 - |V_{us}|^2 - |V_{ud}|^2 = 0.0009 \pm 0.0008 \quad (\sim 1.1\sigma)$$

But we can do better



$$K \rightarrow \mu\nu/\pi \rightarrow \mu\nu$$

$$\frac{\Gamma(K_{\mu 2}(\gamma))}{\Gamma(\pi_{\mu 2}(\gamma))} = \frac{|V_{us}|^2}{|V_{ud}|^2} \frac{f_K^2}{f_\pi^2} \frac{m_K (1 - m_\mu^2/m_K^2)^2}{m_\pi (1 - m_\mu^2/m_\pi^2)^2} \times (0.9930 \pm 0.0035)$$

Cancellations in f_K^2/f_π^2 . From lattice

Cancellations in rad. cor. From Marciano.

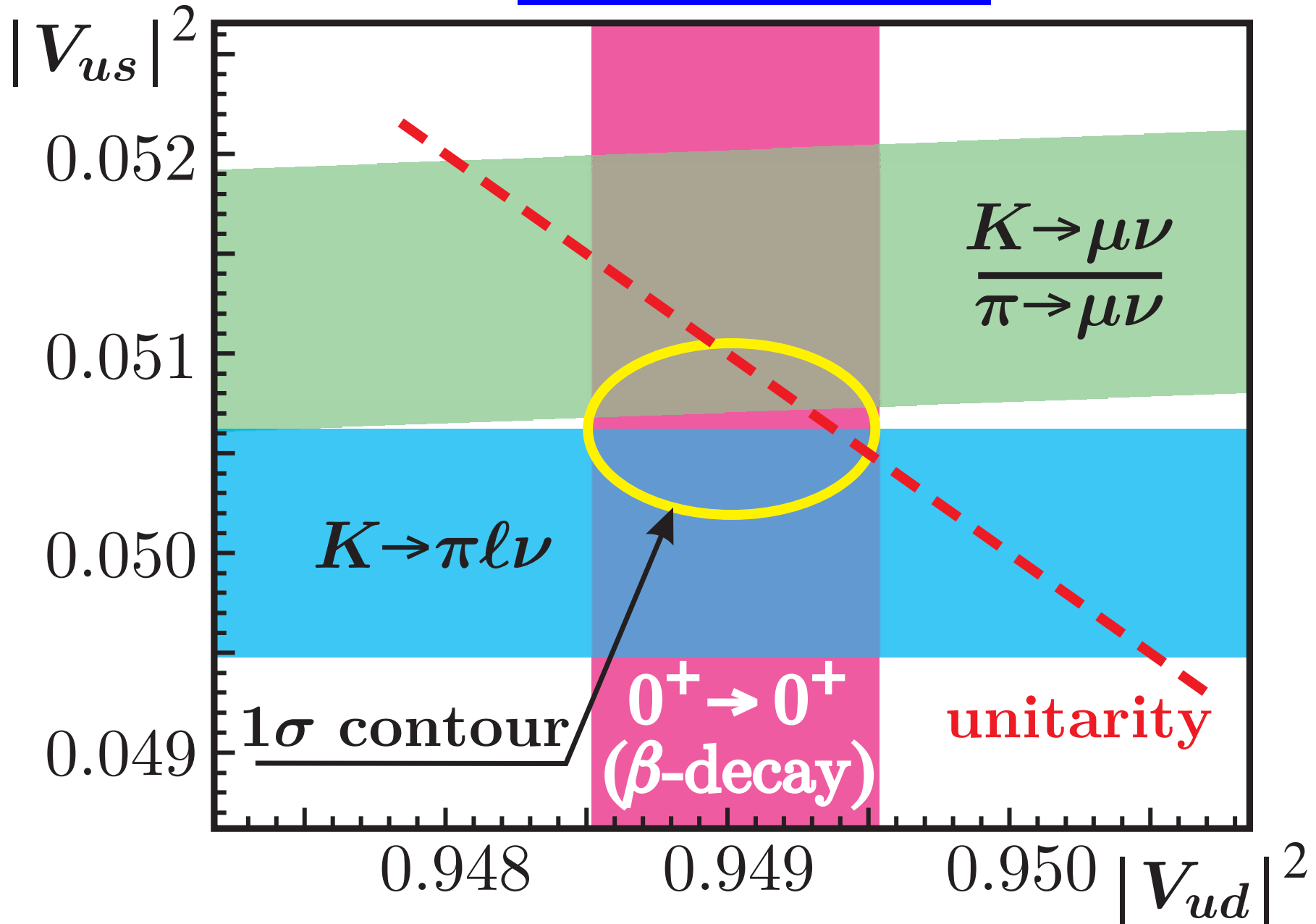
$$\text{KLOE} \Rightarrow |V_{us}/V_{ud} \times f_K/f_\pi|^2 = 0.0765 \pm 0.0005$$

$$\text{HPQCD/UKQCD} \Rightarrow f_K/f_\pi = 1.189 \pm 0.007$$

$$|V_{us}/V_{ud}|^2 = 0.0541 \pm 0.0007$$



CKM Unitarity



From the fit

$$1 - |V_{us}|^2 - |V_{ud}|^2 = 0.0004 \pm 0.0007 \quad (\sim 0.6\sigma)$$

$$|V_{us}| = 0.2249 \pm 0.0010$$

$$|V_{ud}| = 0.97417 \pm 0.00026$$

Fit with unitarity as constraint

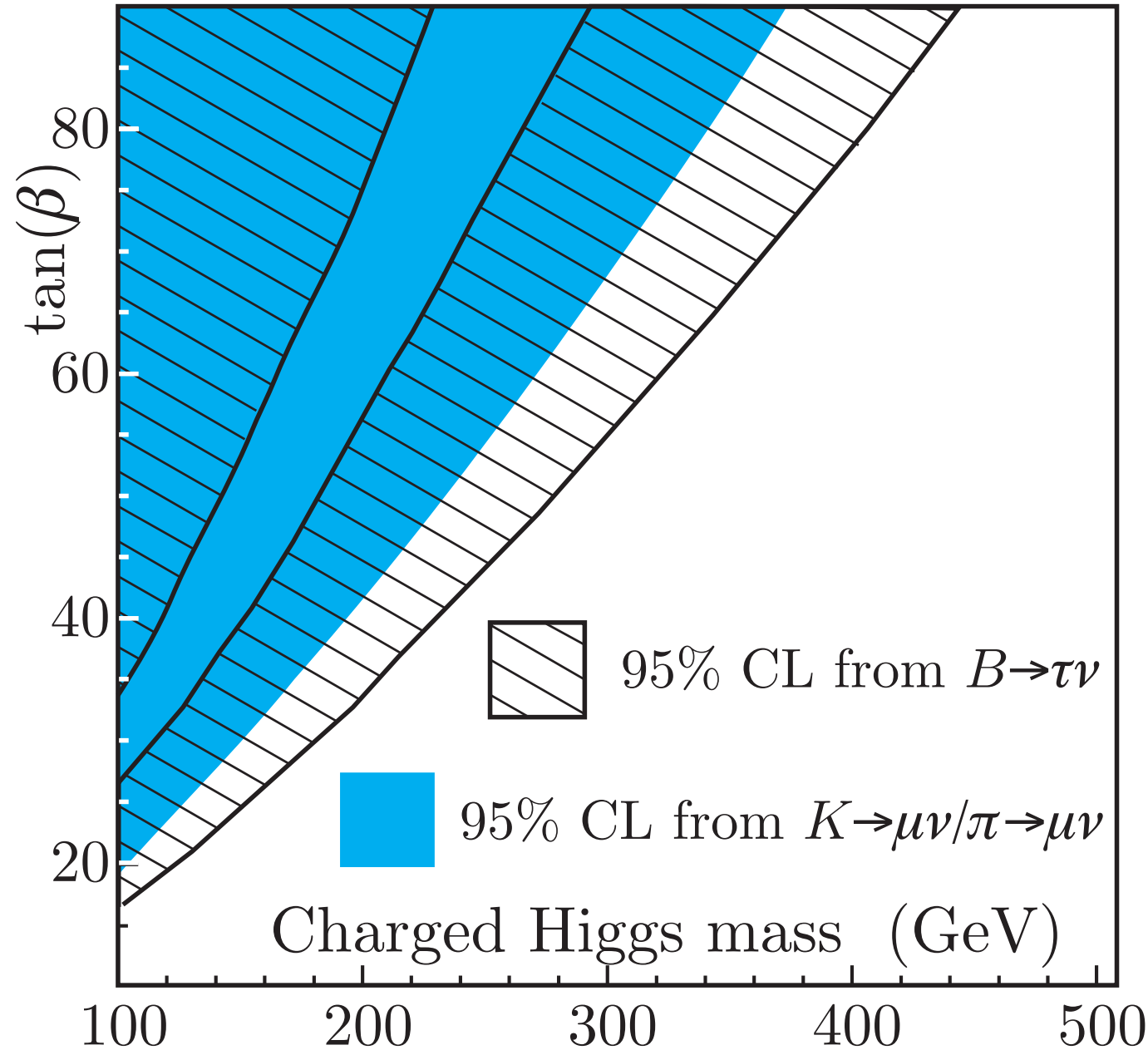
$$|V_{us}| = 0.2253 \pm 0.0007$$

$$|V_{ud}| = \sqrt{1 - |V_{us}|^2} = 0.97429 \pm 0.00017.$$

$$\theta_C = 13.02^\circ \pm 0.06^\circ$$



tan β – $M(\text{Higgs}^\pm)$



$$R_{\ell 23} = \left| \frac{V_{us}(K_{\mu 2})}{V_{us}(K_{\ell 3})} \times \frac{V_{ud}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\mu 2})} \right| = 1$$

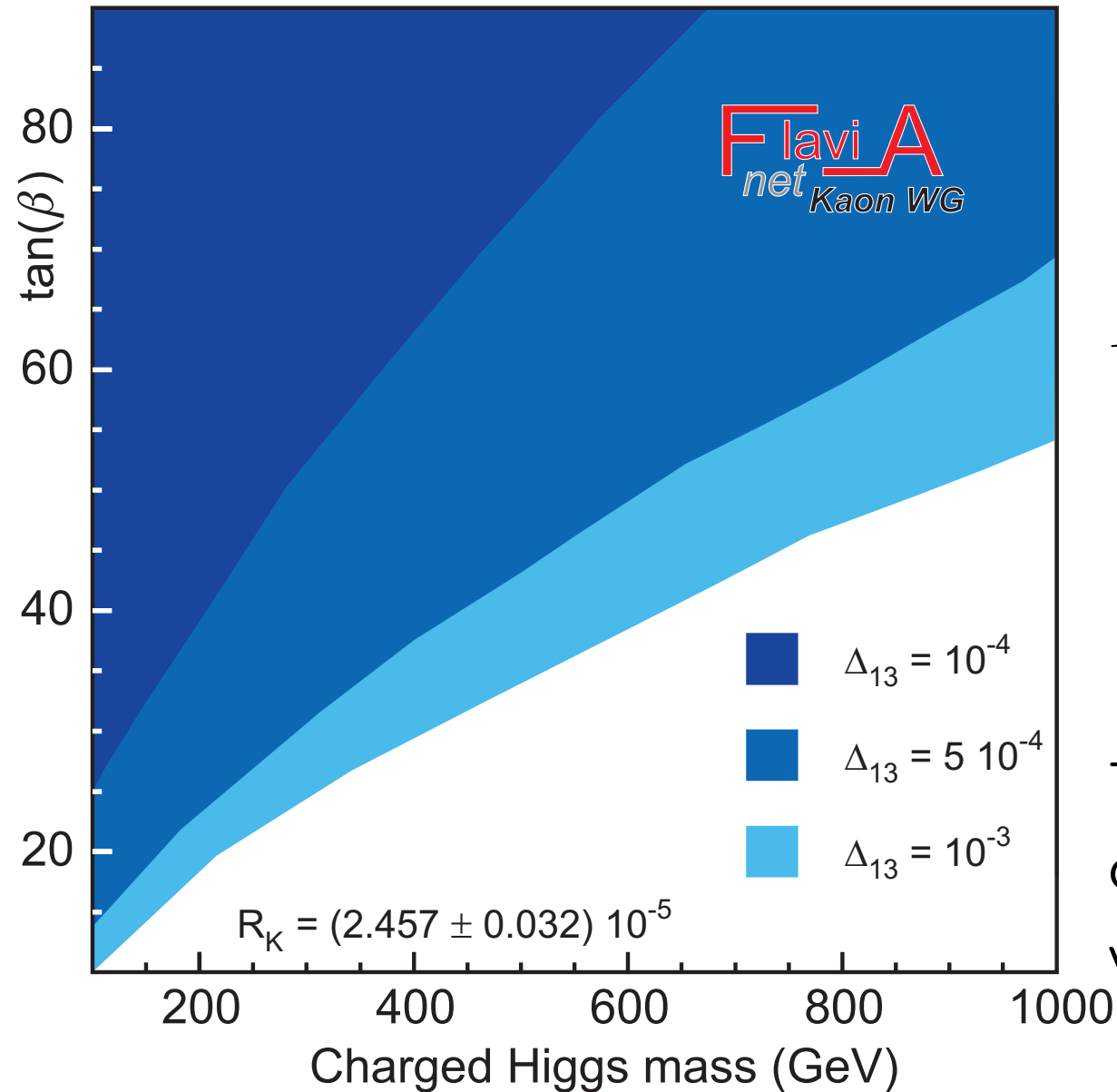
in the SM. With charged Higgs exchange $R_{\ell 23} =$

$$\left| 1 - \frac{m_{K^+}^2}{m_{H^+}^2} \left(1 - \frac{m_{\pi^+}^2}{m_{K^+}^2} \right) \times \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|$$

$\epsilon_0 \approx 1/(16\pi^2)$



$$K^\pm \rightarrow e^\pm \nu$$



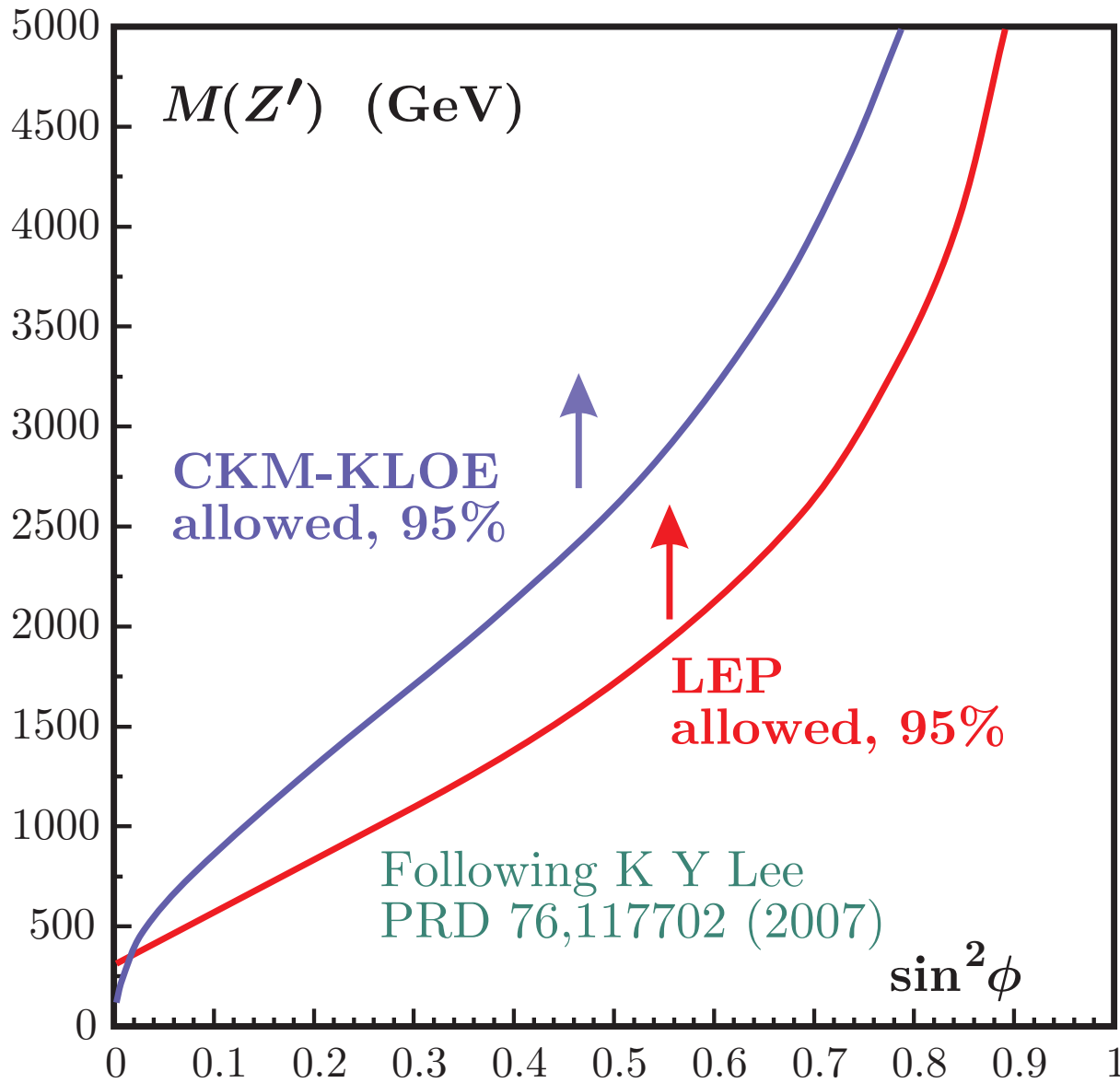
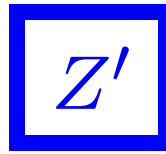
$$R_K = \frac{\Gamma(K \rightarrow e\nu)}{\Gamma(K \rightarrow \mu\nu)}$$

$$R_K^{\text{SM}} = (2.477 \pm 0.001) \times 10^{-5}$$

$$R_K^{\text{LFV}} \approx R_K^{\text{SM}} \left[1 + \left(\frac{m_K^4}{M_{H^\pm}^4} \right) \left(\frac{m_\tau^2}{M_e^2} \right) |\Delta_{13}|^2 \tan^6 \beta \right]$$

The lepton flavor violating coupling Δ_{13} could reach values of $\mathcal{O}(10^{-3})$





Gauge group is $SU(2)_L \times SU(2)_L \times U(1)_Y$.
 $SU(2)_L$ for light quarks (u, d, c, s)
 $SU(2)_H$ for heavy (t, b)
2 Z bosons
2 mixing angle



Conclusions

Unitarity is verified at the 0.1% level

$$1 - |V_{us}|^2 - |V_{ud}|^2 = 0.0004 \pm 0.0007$$

Muons, electrons and quarks

carry the same weak charge to better than 0.5%

Kaon properties limit the parameter space
for some new physics models

