

GReAT: General Relativity Accuracy Test EP test balloon experiment

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GReAT experiment

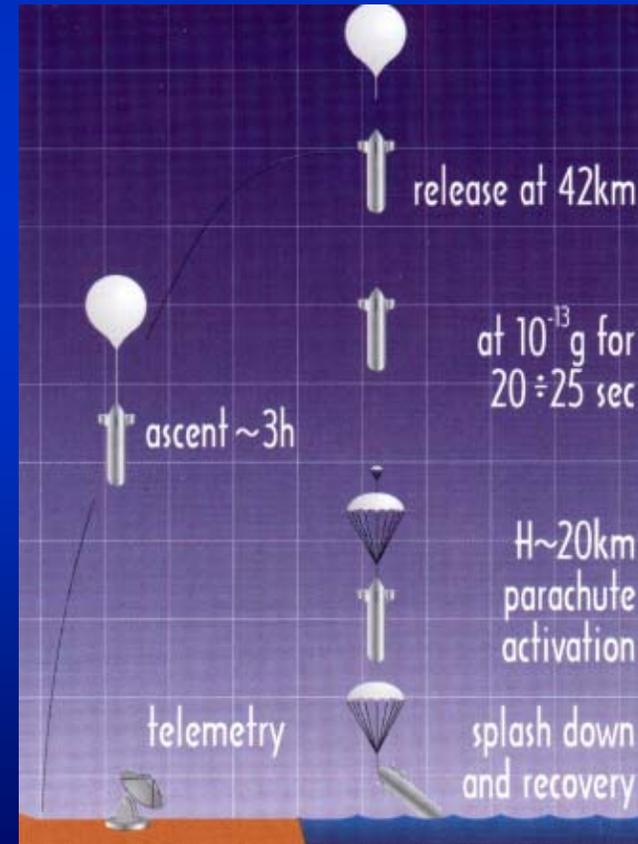
GReAT compared to the other proposed flying experiments to test the **WEP**:

- STEP: 10^{-18} (drag-free satellite) NASA;
- GG: 10^{-17} (drag-free satellite) INFN/ASI;
- MicroScope: 10^{-15} (drag-free satellite) CNES/ESA;
- GReAT: $5*10^{-15}$ (drag-shielded capsule) ASI/NASA;

GReAT experiment

The goal of the **GReAT** experiment is to test the Weak–Equivalence–Principle (**WEP**) with an accuracy of a few parts in 10^{15} , i.e., 2 orders–of–magnitude better than the actual ground–based measurements:

- The differential accelerometer composed of two test masses of different material free falls inside a 3 m long cryostat dropped from a 40 km altitude balloon;
- the **FF** duration is about 30 s inside an evacuated capsule;
- the falling masses are part of a high–sensitivity differential accelerometer with a sensitivity in detecting differential accelerations of about $10^{-15} g_{\oplus} / \sqrt{\text{Hz}}$ at the liquid–helium temperature (4.2 K);

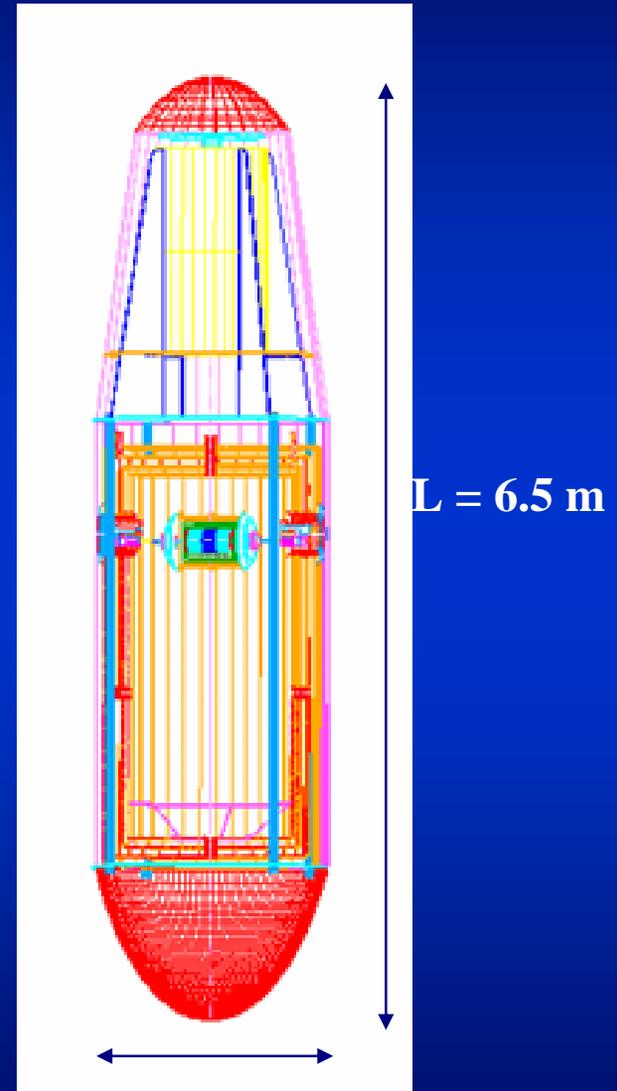


GReAT experiment

- the differential accelerometer apparatus is spun about an horizontal axis at a frequency of 1 Hz (1ω) in order to modulate the signal during free fall;
- the experiment is isolated from external noise sources acting on the capsule, such as air drag;
- a non-zero differential acceleration appearing at the rotation frequency will indicate a violation of the Equivalence Principle;
- once the instrument package reaches the capsule's floor, the capsule is decelerated by a parachute for retrieval and re-flight;

M = 1300 kg

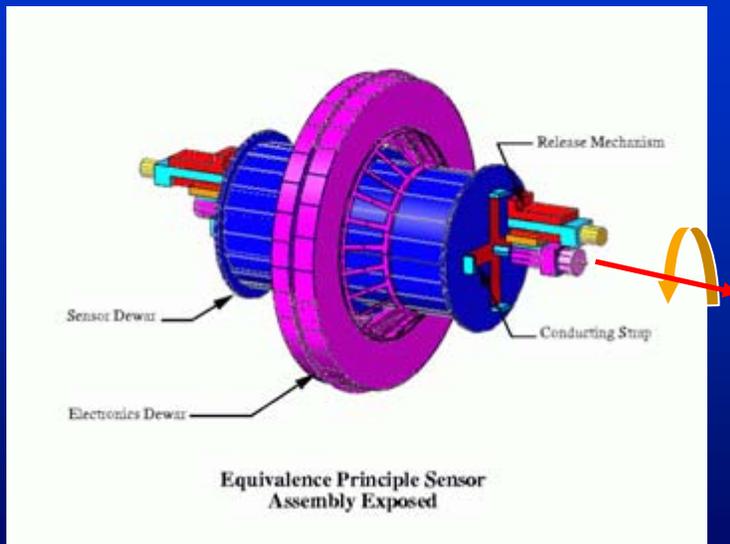
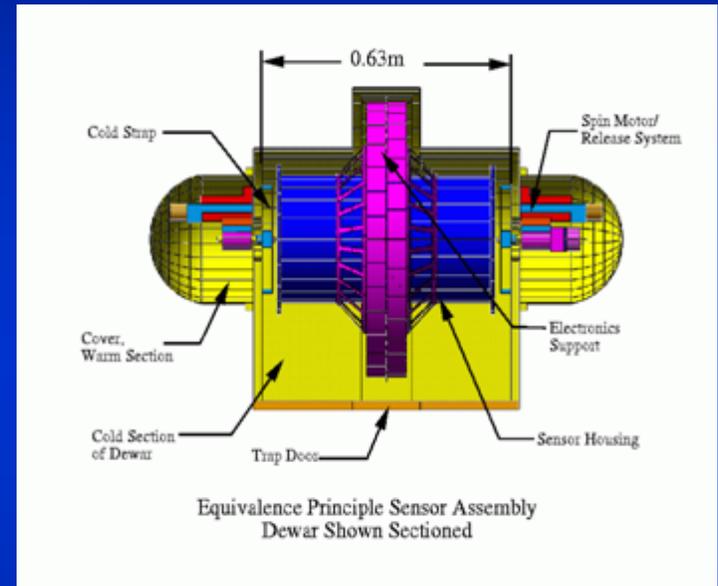
D = 1.4 m



GReAT experiment

The liquid–helium refrigeration is important to provide:

- low thermal noise;
- high thermal stability;
- low thermal gradients;
- high Q–factors of the differential accelerometer detector;



- Small cryostat to refrigerate the instrument package (blue/purple);
- Open doors at bottom of cryostat;
- Instrument package span at ≤ 1 Hz before release into room–temperature capsule;

GReAT experiment

GReAT has several advantages with respect to other ground-based experiments:

- full Earth's gravity signal: $1g_{\oplus}$;
- acceleration noise of the **FF** detector $\leq 10^{-12}g_{\oplus}$ for a residual pressure of 10^{-6} mbar;
- drag-shielded vertical **FF**;
- longer integration time;


$$\eta = \frac{\Delta a}{g}$$

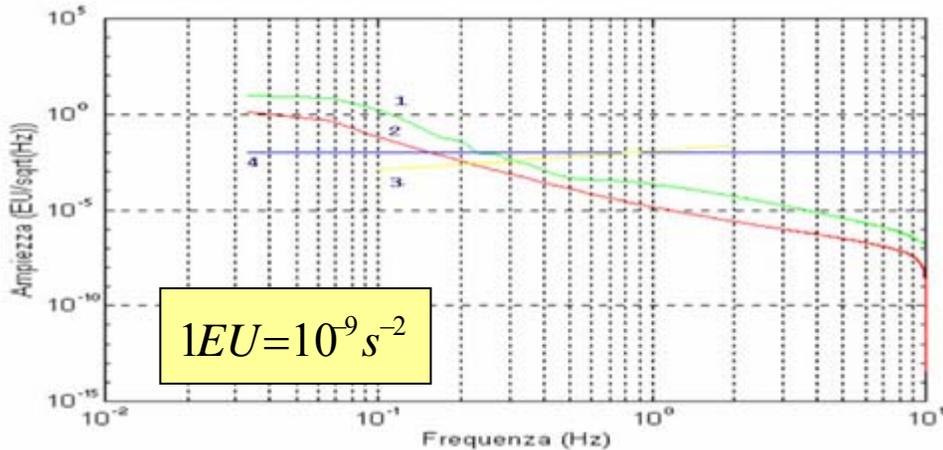
GReAT experiment

The work of the teams involved in the **GReAT** experiment to test the **WEP** has been subdivided in the following main aspects:

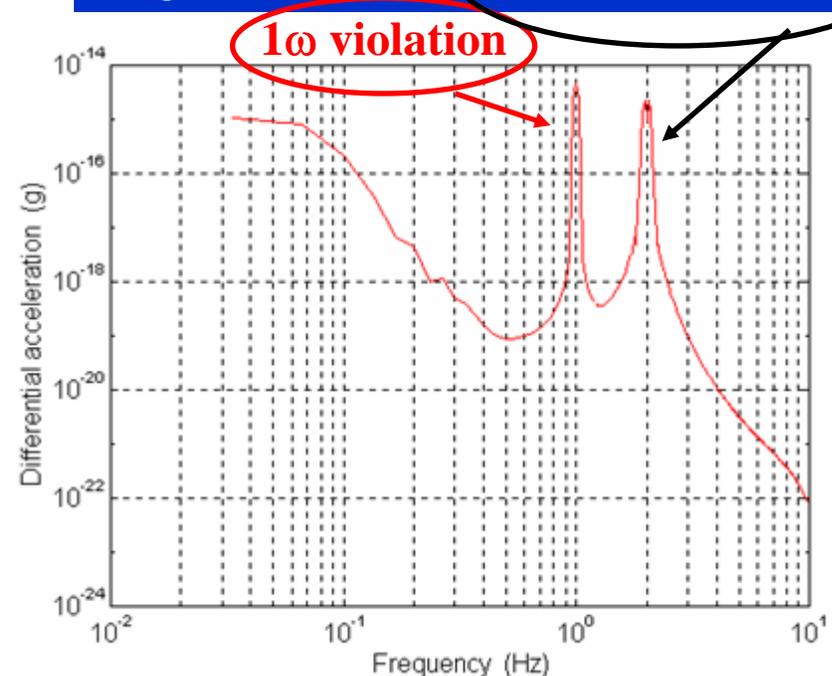
- Free–Fall system (SAO):
 - cryogenic system (with Janis Research);
 - release mechanism (cooling and clean release);
 - room temperature electronics and detector power source;
- Detector (IFSI/CNR):
 - achieving the required values (e.g., Q–factor);
 - attenuating initial transients;
 - common–mode rejection;

GReAT experiment

Numerical simulations.



FF simulation with the instrument package spun at 1 Hz including a possible violation of the **WEP** at the level of $10^{-15} g_{\oplus}$. The violation signal at 1ω is well separated from the 2ω signals.



Spectral densities:

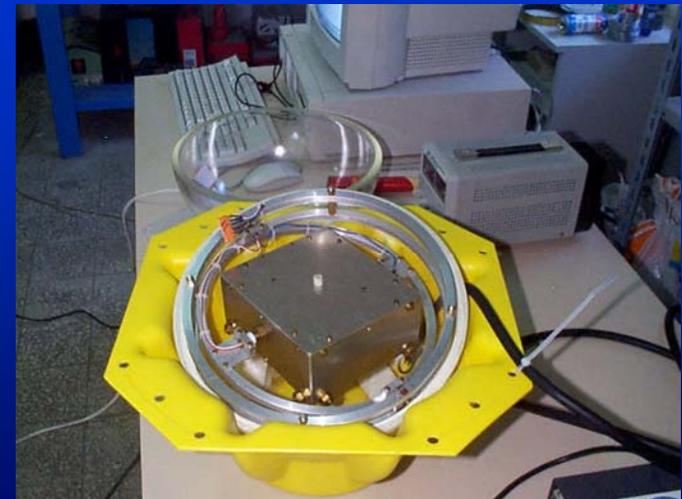
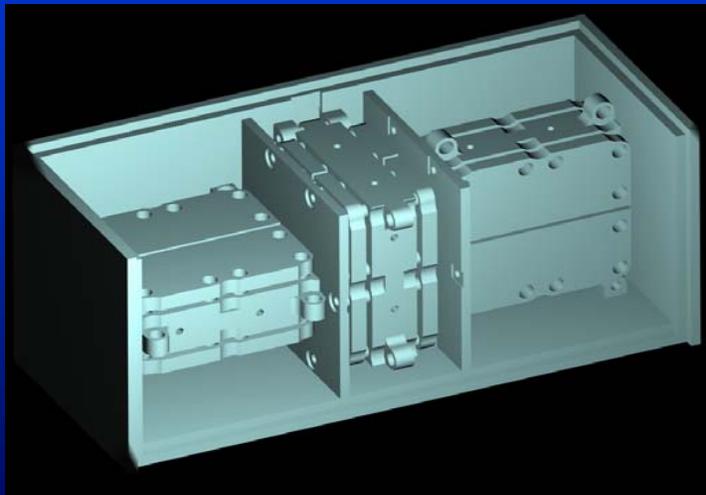
- Capsule gravity gradients;
- Earth's gravity gradients;
- Inertial gradients due to the vibrations of the capsule walls and to the platform, via the residual gas in the capsule;
- Reference gravity gradient: $10^{-2} \text{ EU}/\sqrt{\text{Hz}}$;

The ISA accelerometer

BepiColombo



GEOSTAR

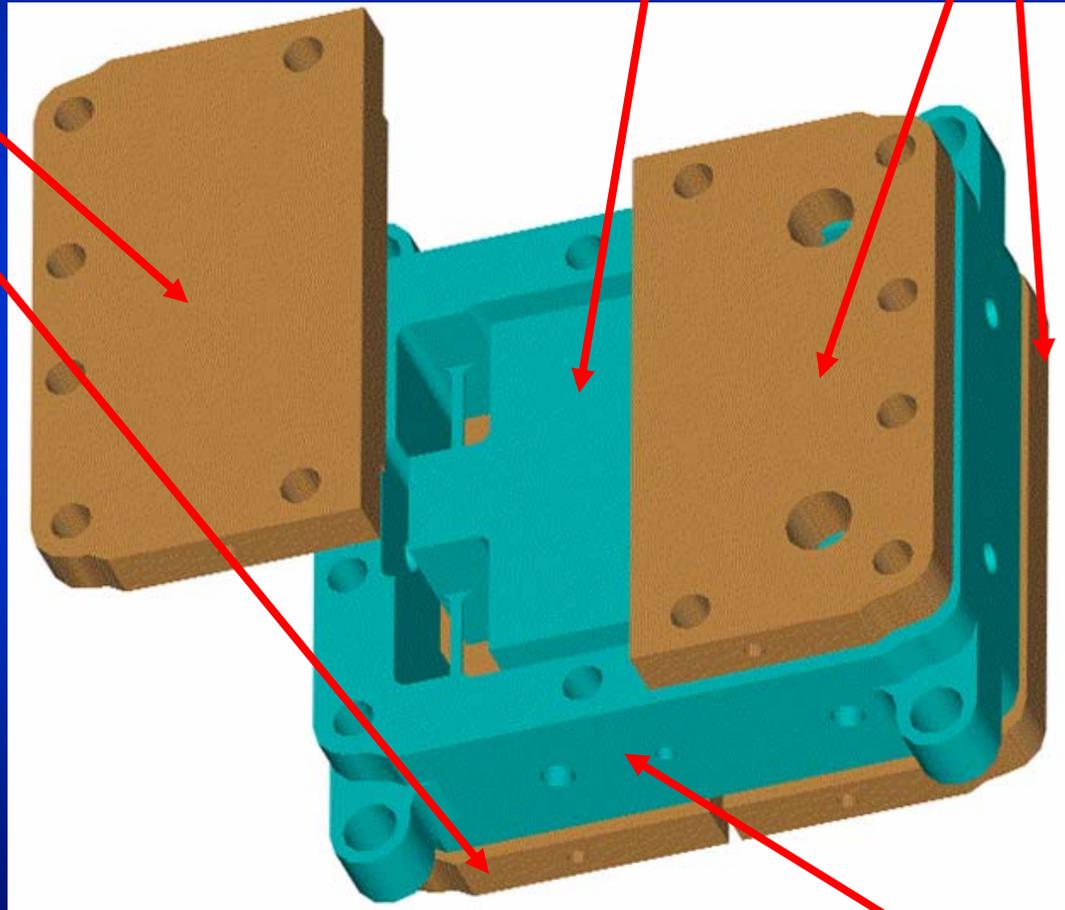


The ISA accelerometer

Actuator Capacitors

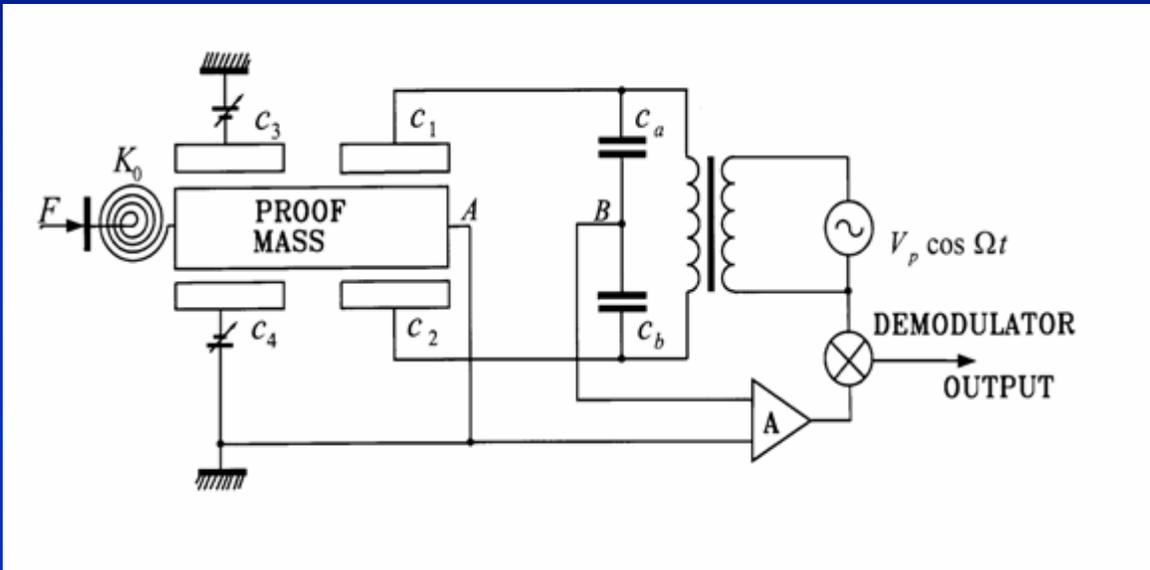
Test Mass

Detector Capacitors



Reference Frame

Base concept of the accelerometer



$$\beta = \frac{\alpha^2 C}{m_r \omega_o^2}$$

$$\frac{1}{Q_e} = \left(4 \frac{\omega_o}{\Omega_p} \frac{\text{tg} \delta}{\beta} \right)$$

$$\frac{1}{Q} = \left(\frac{1}{Q_m} + \frac{1}{Q_{de}} \right)$$

$$a_t^2(\omega) \approx \frac{4k_b \omega_o}{m_r} \left[\frac{T}{Q} + T_n \frac{2Z_n C \omega_o}{\beta} \right] \Delta f$$

no matching

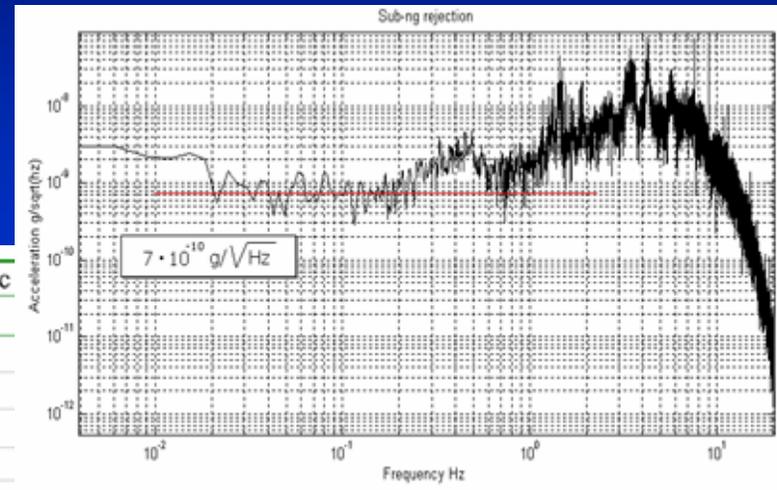
$$a_t^2(\omega) \approx \frac{4k_b \omega_o}{m_r} \left[\frac{T}{Q} + T_n \frac{2}{\beta} \frac{\omega_o}{\Omega_p} \right] \Delta f$$

matching

$$a_{bW} = \left(\frac{4k_b T \omega_o}{m_r Q} \right)^{1/2}$$

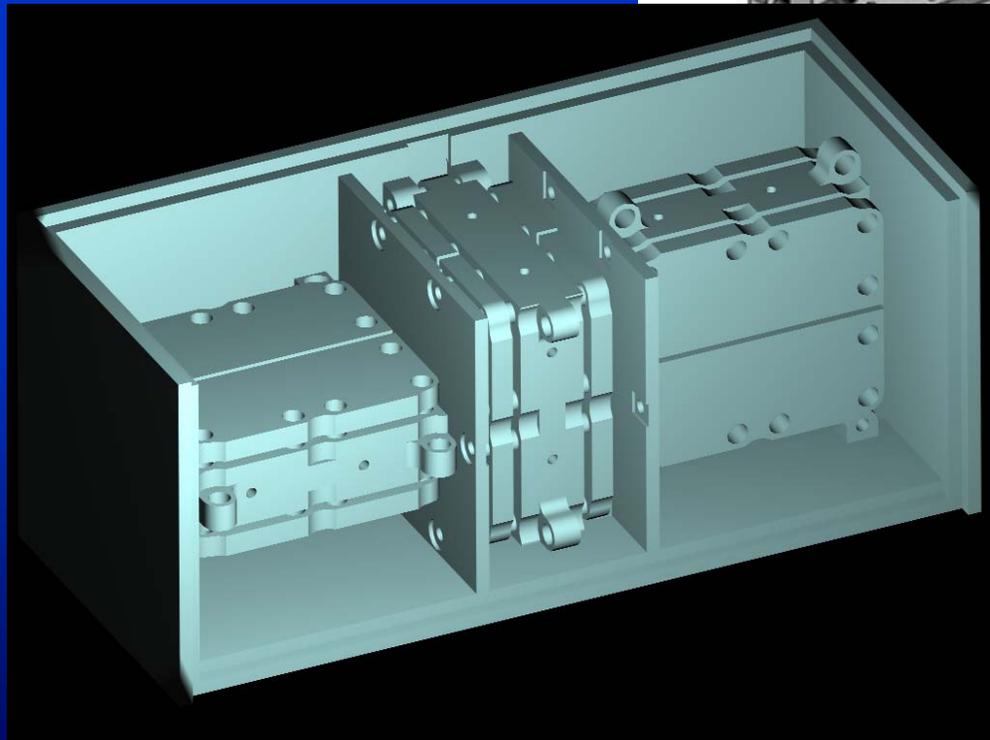
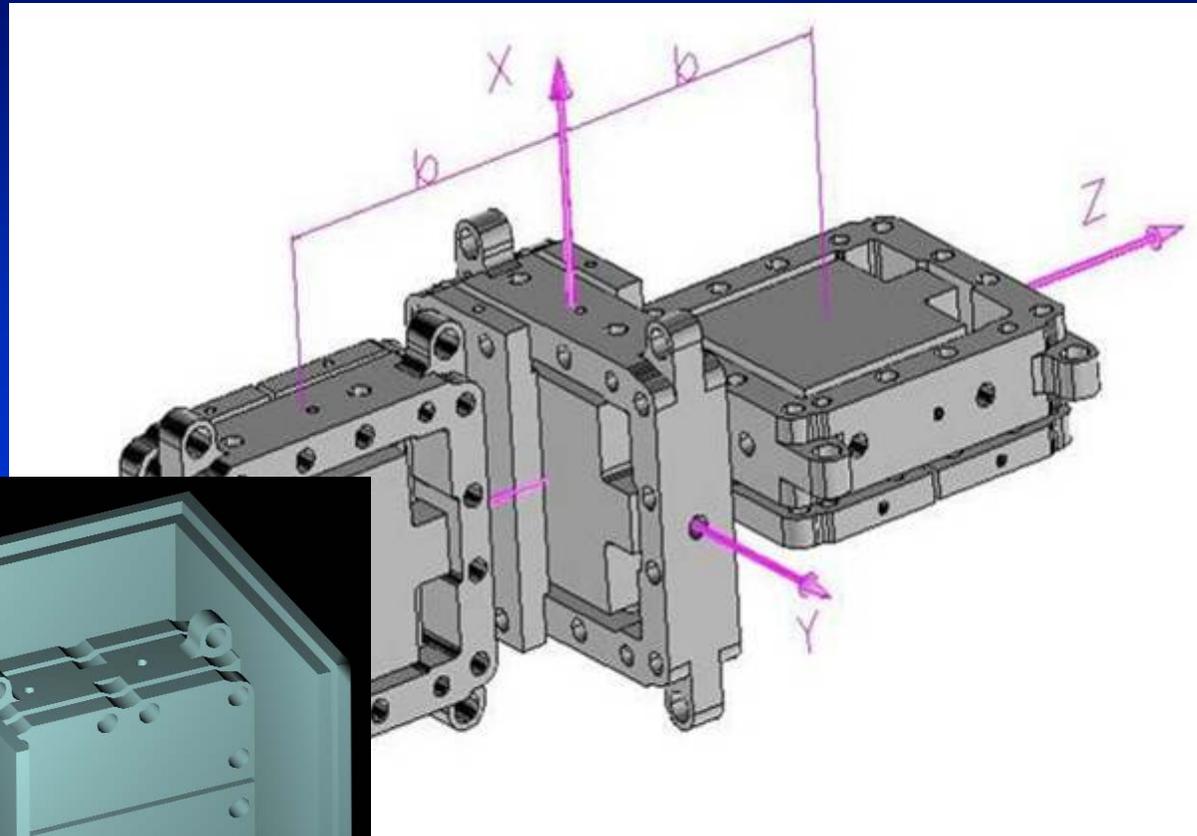
Accelerometer for space use

		Actual value	Possible value	Cryogenic
a_{min}	Sensitivity g/\sqrt{Hz}	$3.3 \cdot 10^{-12}$	$4 \cdot 10^{-14}$	$5.7 \cdot 10^{-15}$
m_r	Proof mass (Kg)	0.22	10	10
f_o	Frequency of resonance (Hz)	3.5	1	1
f_p	Polarisation frequency (KHz)	10	10	10
P	Pressure condition (mbar)	10^{-4}	10^{-6}	10^{-6}
C_1	Sensing capacity (pF)	300	300	300
$tg\delta_{c_1}$	Angle of loss of C_1 condenser	$4 \cdot 10^{-4}$	$4 \cdot 10^{-4}$	$4 \cdot 10^{-4}$
C_a	External fixed capacity (pF)	300	300	300
$tg\delta_{c_a}$	Angle of loss of C_a condenser	$3 \cdot 10^{-4}$	$3 \cdot 10^{-4}$	$3 \cdot 10^{-4}$
	Electronic device	AD743/AD	OPA128	OPA128
v_n	Voltage noise of amplifier (V/\sqrt{Hz})	$3 \cdot 10^{-9}$	$15 \cdot 10^{-9}$	$15 \cdot 10^{-9}$
i_n	Current noise of amplifier (A/\sqrt{Hz})	$7 \cdot 10^{-15}$	$0.1 \cdot 10^{-15}$	$0.1 \cdot 10^{-15}$
T_n	Temperature noise of amplifier (K)	0.76	0.06	0.06
α	Transducer factor (V/m)	10^5	10^5	$5 \cdot 10^5$
β	Electromechanical transducer factor	$2.8 \cdot 10^{-2}$	$7.6 \cdot 10^{-3}$	$1.9 \cdot 10^{-1}$
Q_e	Electric merit factor	$6.6 \cdot 10^4$	$6.3 \cdot 10^4$	$1.5 \cdot 10^6$
Q_m	Mechanical merit factor	$5.7 \cdot 10^3$	10^5	10^5
Q	Total merit factor	$5.7 \cdot 10^3$	$6.3 \cdot 10^4$	10^5
a_{bw}^2	Brownian noise (m/sec^2) ² / Hz	$2.9 \cdot 10^{-22}$	$1.6 \cdot 10^{-25}$	1.410^{-27}
a_{el}^2	Electronic noise (m/sec^2) ² / Hz	$8.4 \cdot 10^{-22}$	$4.9 \cdot 10^{-26}$	$1.9 \cdot 10^{-27}$

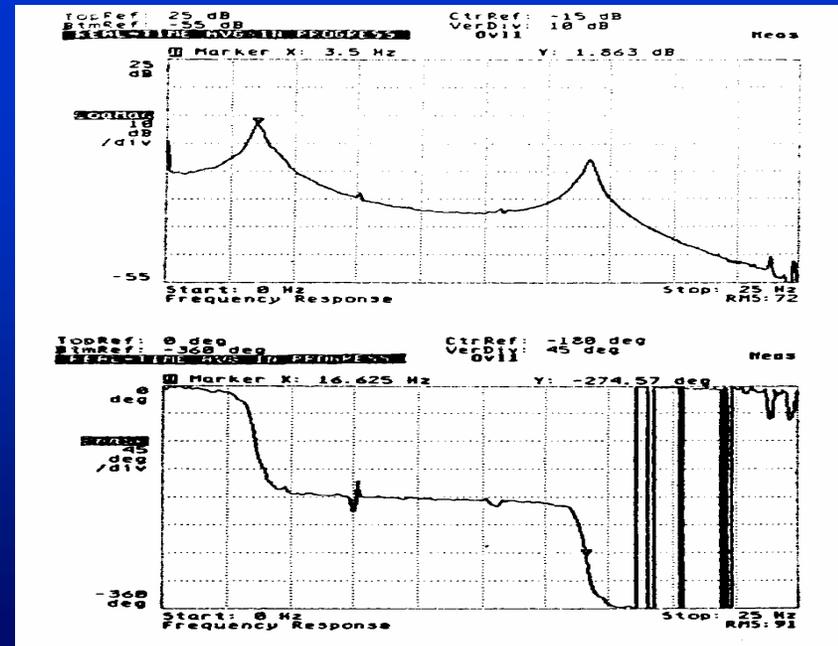
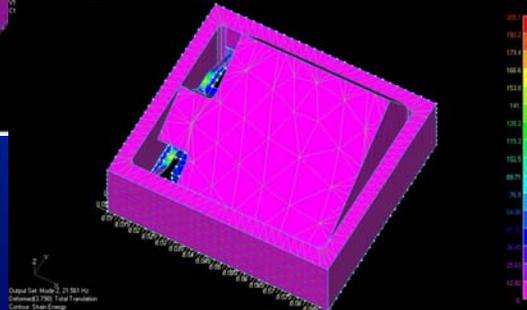
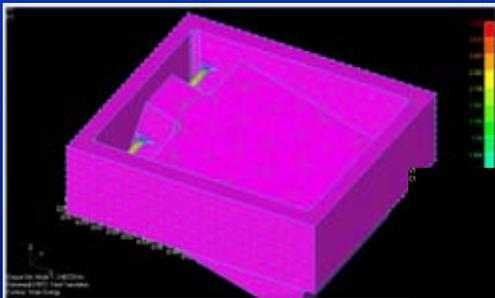
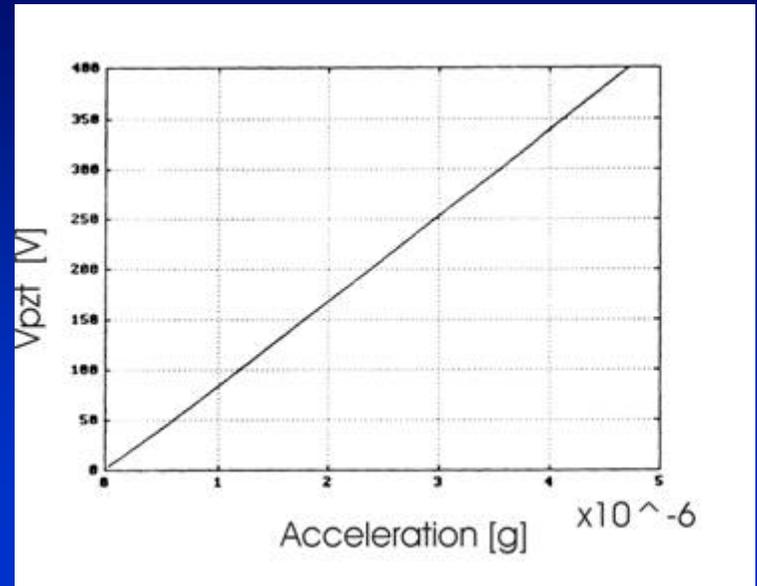
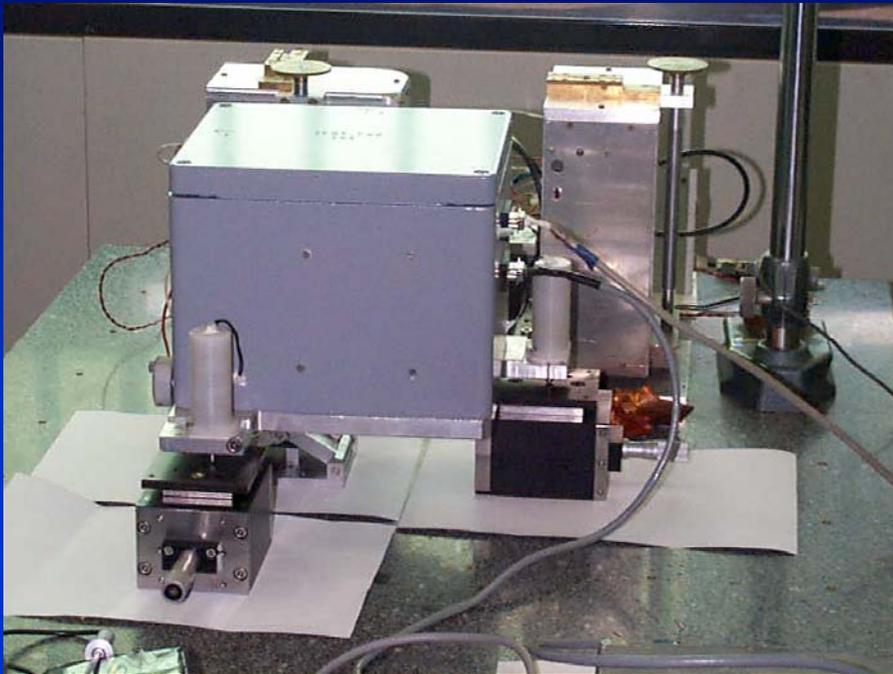


Differential measurement in order to eliminate the seismic noise in the laboratory performed with two accelerometers with sensitive axes parallel. The residual flat noise is due to the electronics. The setup electronic (that used for the geophysics) was not the best one in order to reach the actual sensitivity of $3.3 \cdot 10^{-12} g_{\oplus}/\sqrt{Hz}$. Anyway the level of the mechanical rejection is quite good.

ISA (Italian Spring Accelerometer) Three-axis

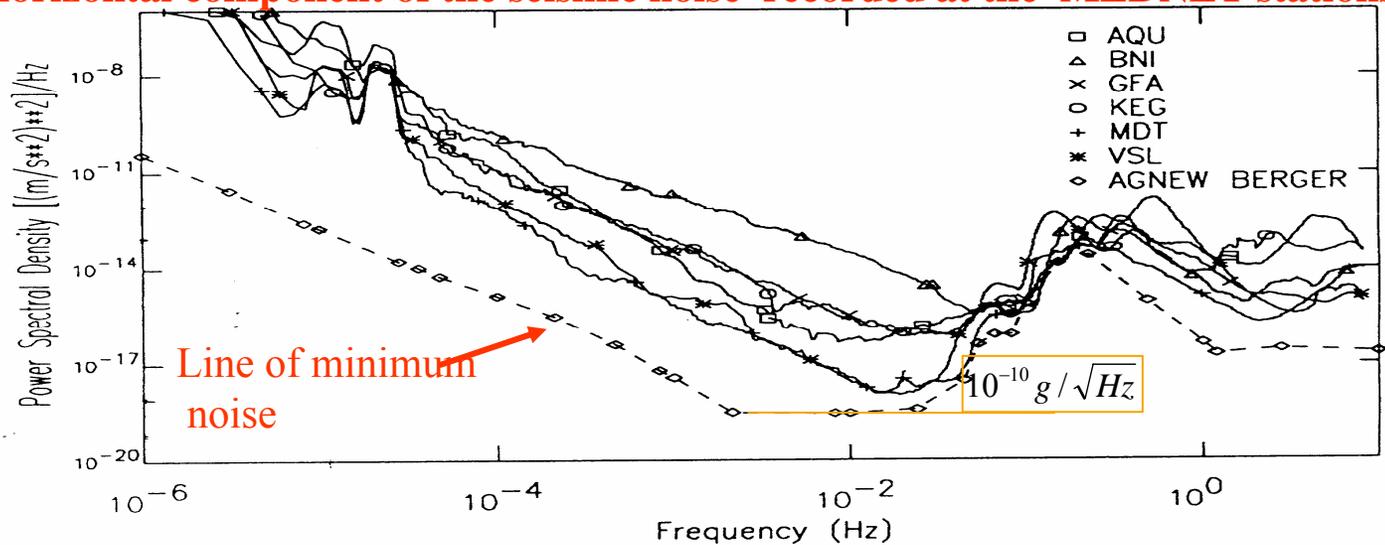


ISA laboratory calibrations

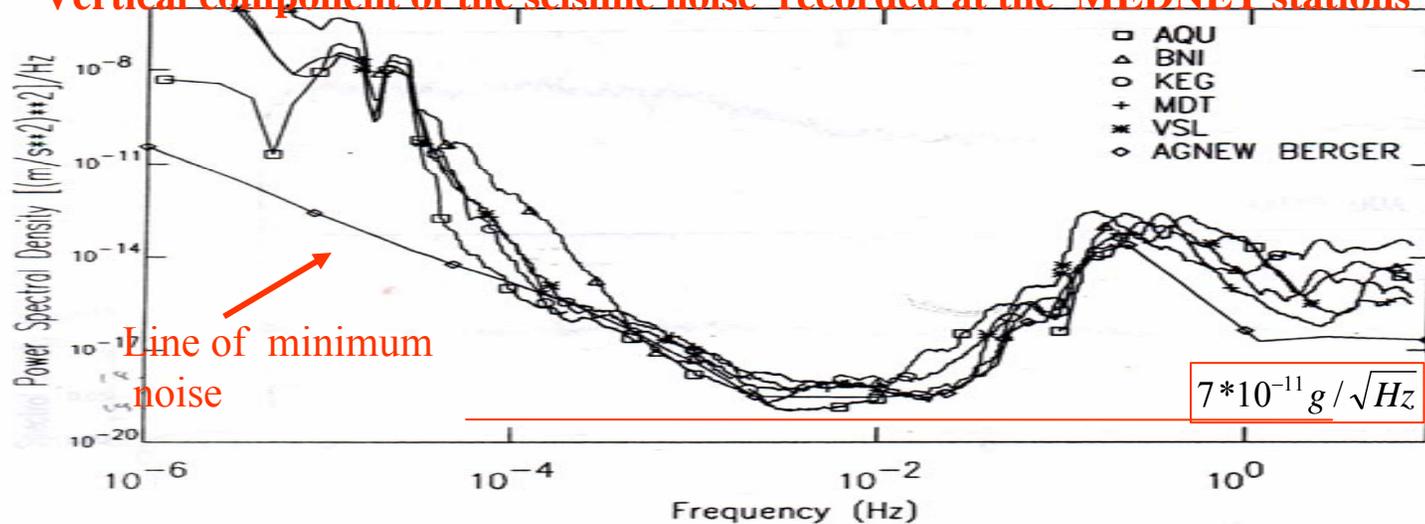


Geophysical Measurements

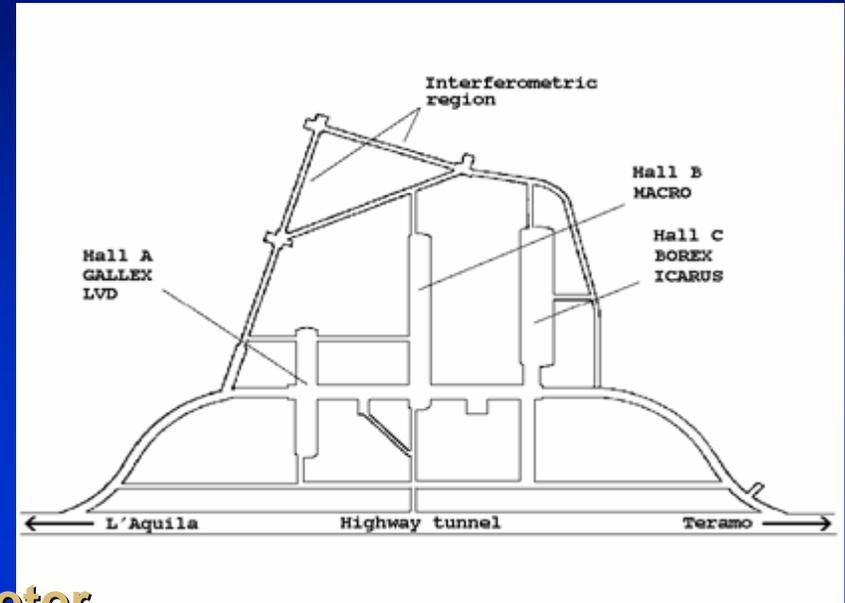
Horizontal component of the seismic noise recorded at the MEDNET stations



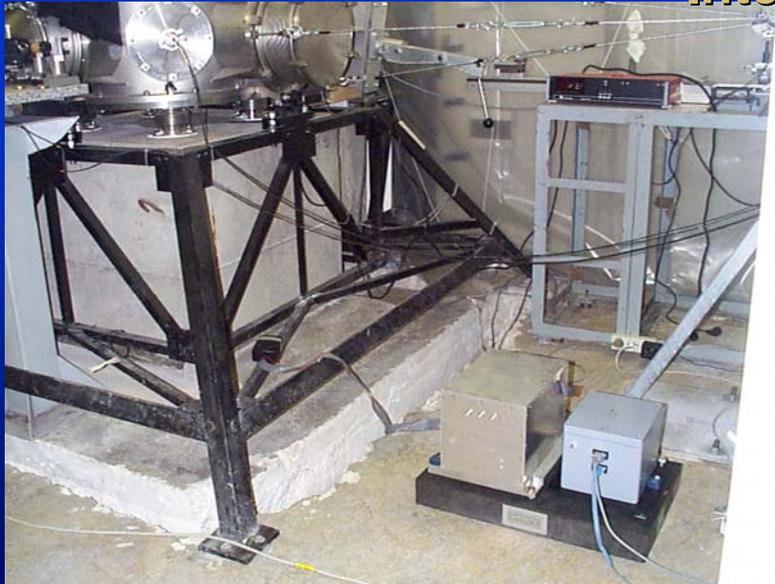
Vertical component of the seismic noise recorded at the MEDNET stations



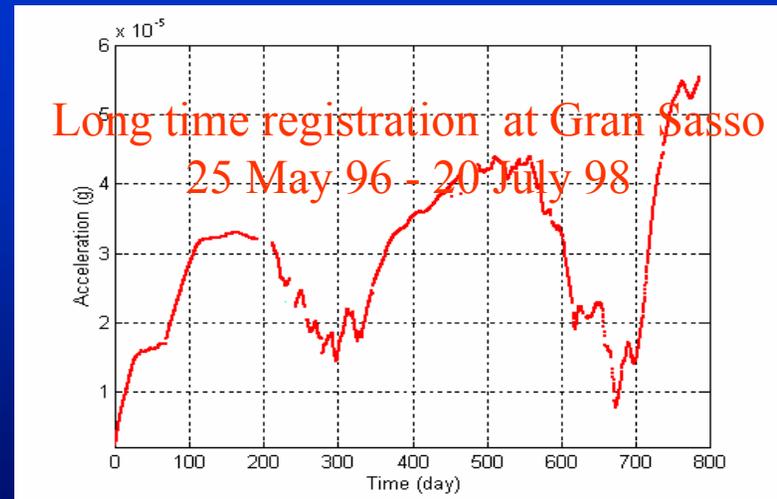
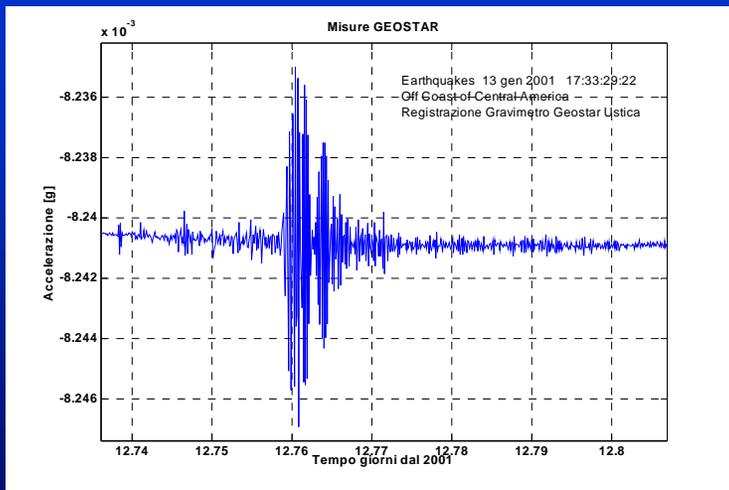
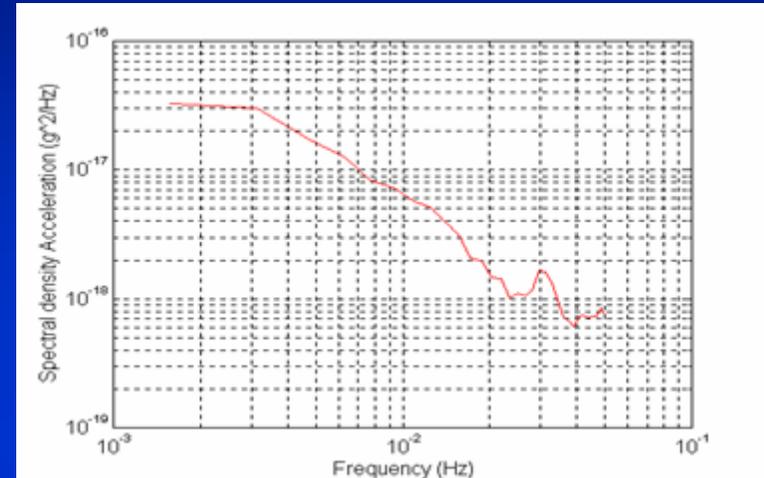
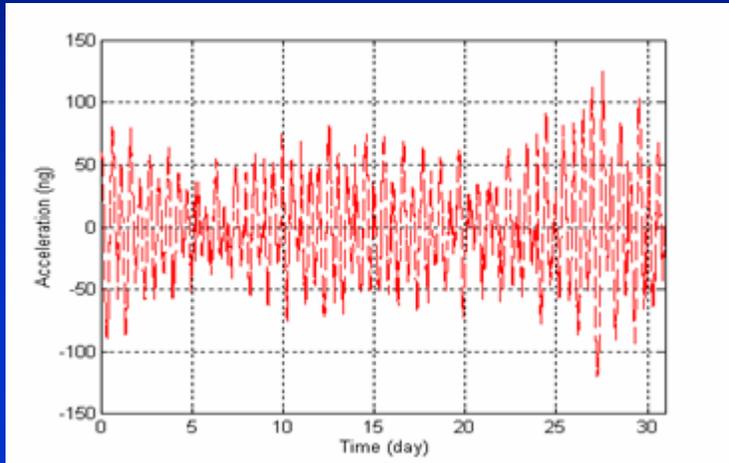
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Interferometer

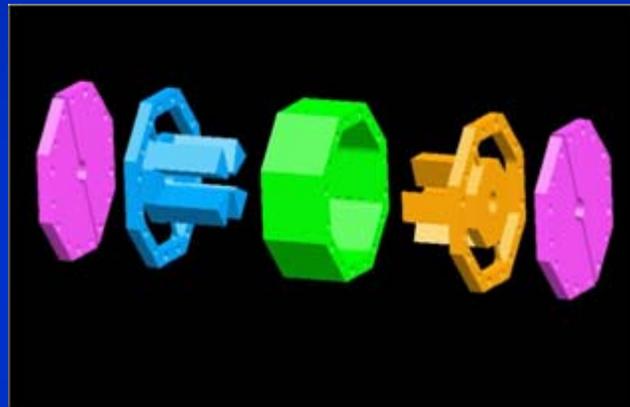
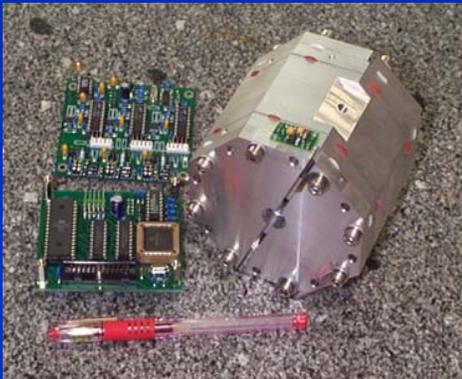


Geophysical Measurements

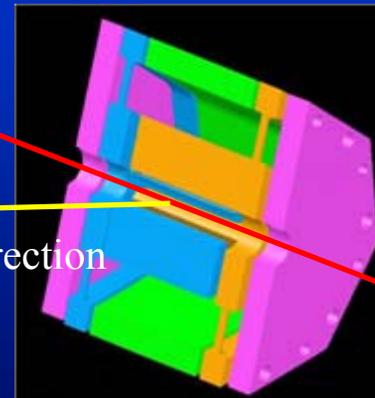
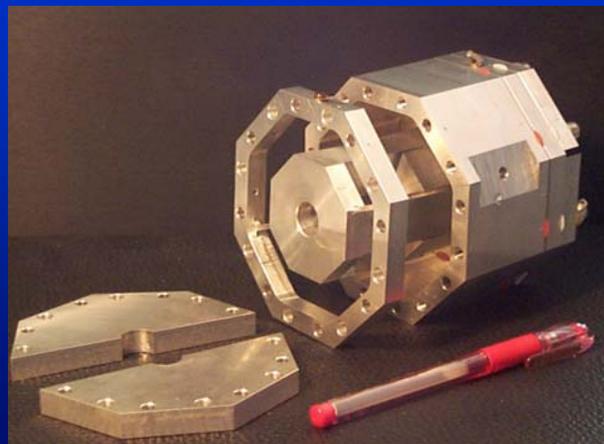


Experimental results with a differential accelerometer prototype

The first differential accelerometer prototype built at IFSI/CNR:



Exploded view of the differential accelerometer prototype



Cross section of the (assembled) differential accelerometer prototype

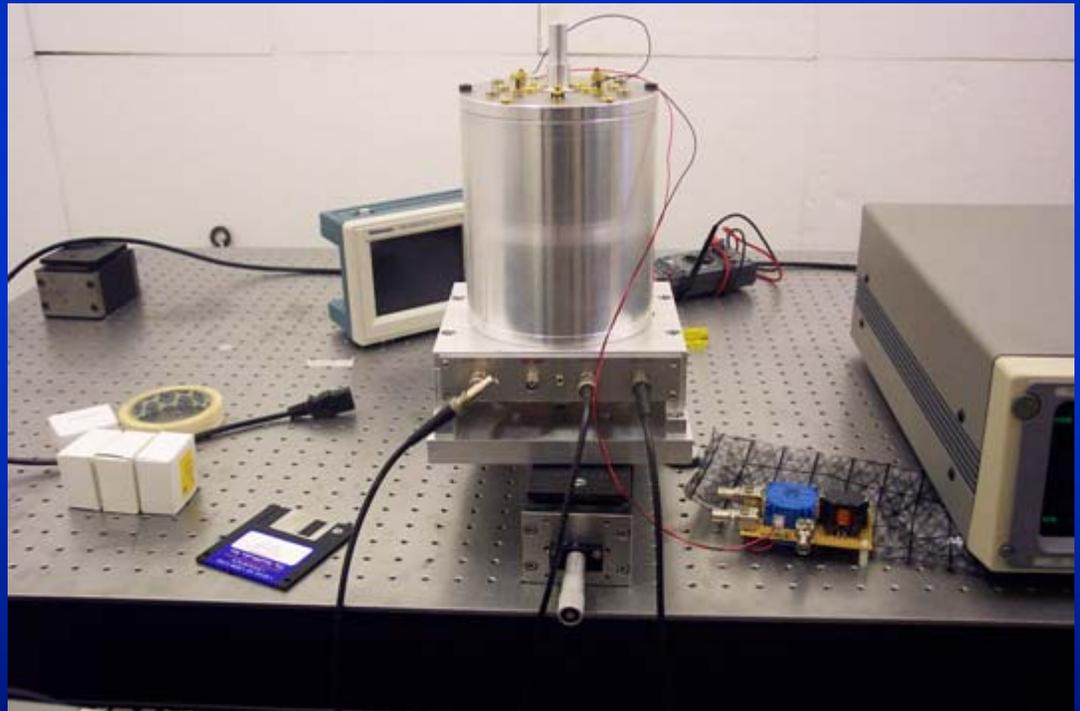
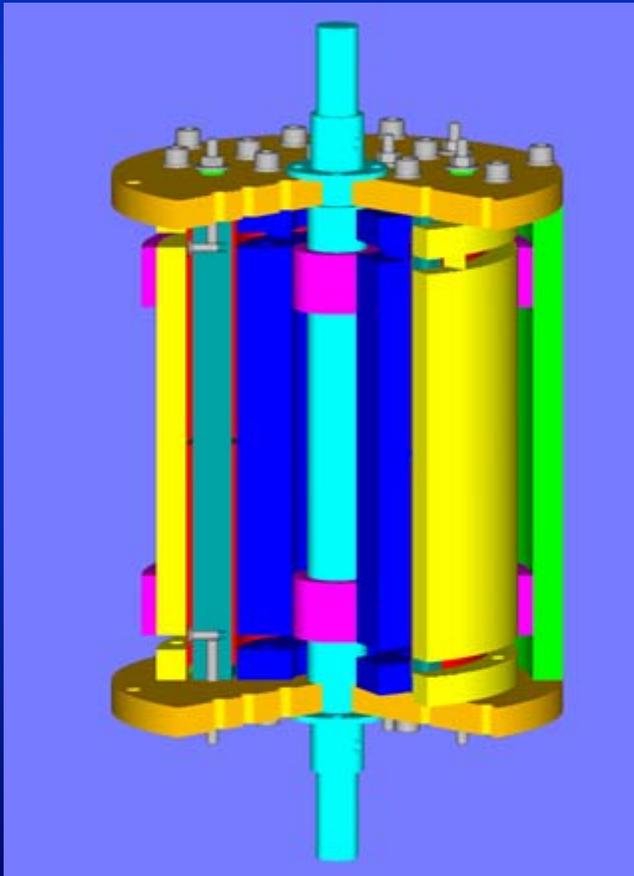
Sensitive-axis direction

Spin-axis direction

Each sensing mass has to fixed capacitors plates for the signal pickup.

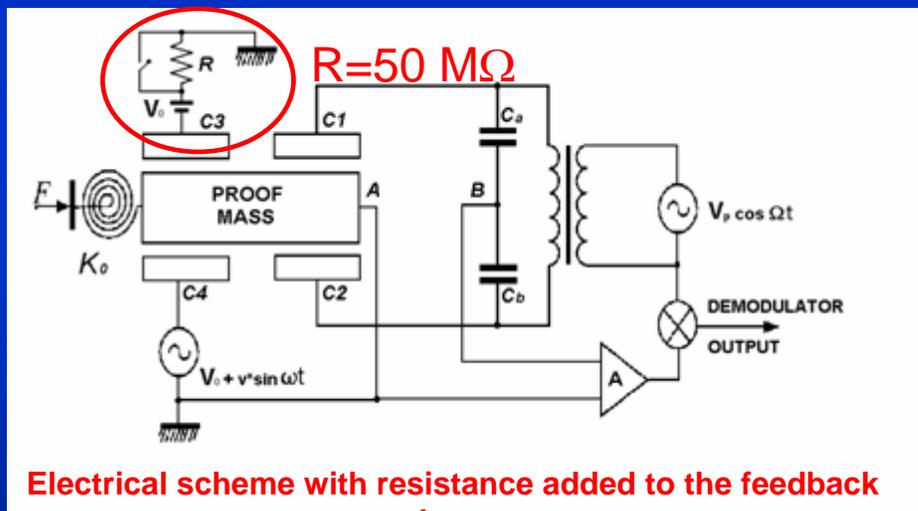
New configuration of the differential accelerometer

The second differential accelerometer prototype built at IFSI/CNR.

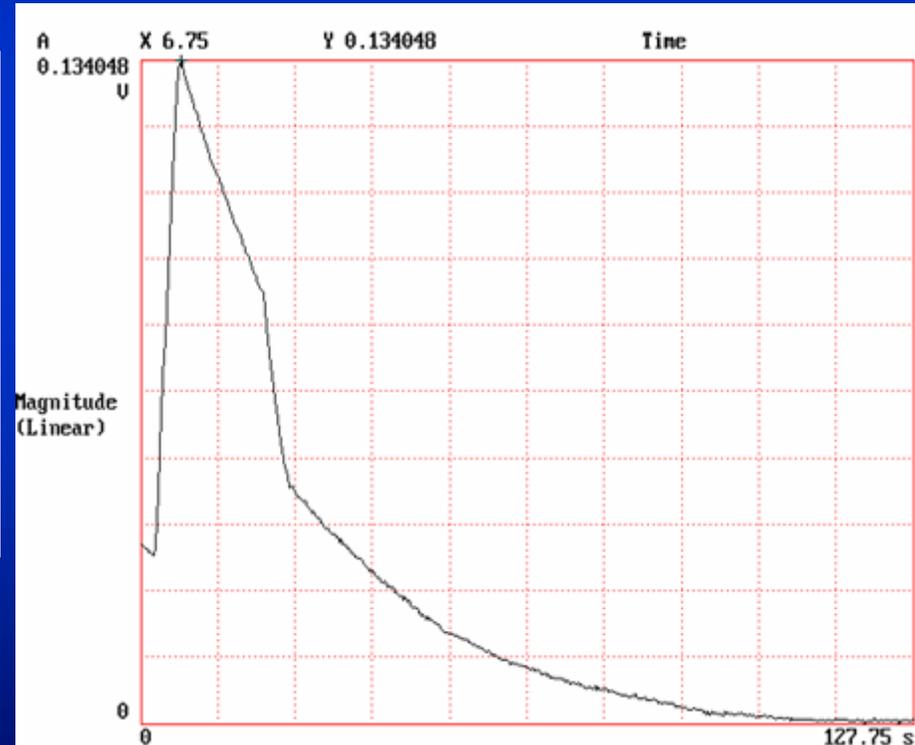


Experimental results with a differential accelerometer prototype

Abatement of the natural dynamics excited by the instrument release into the capsule.



Electrical scheme with resistance added to the feedback loop

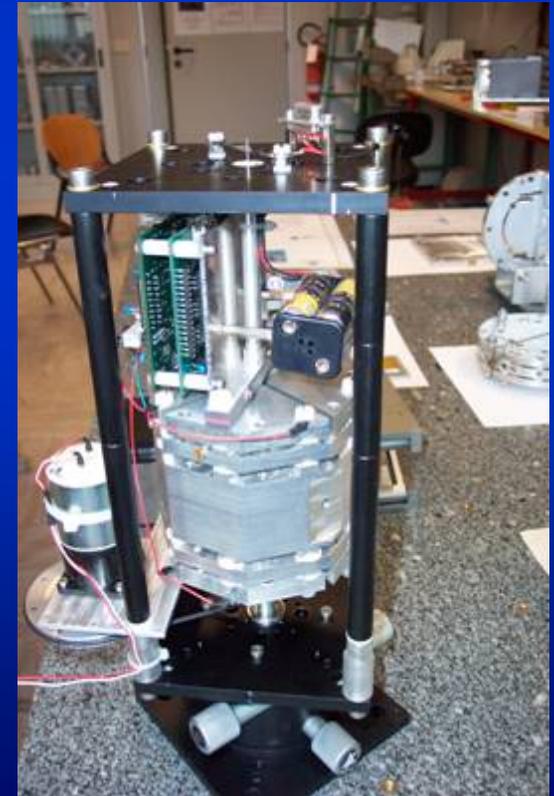
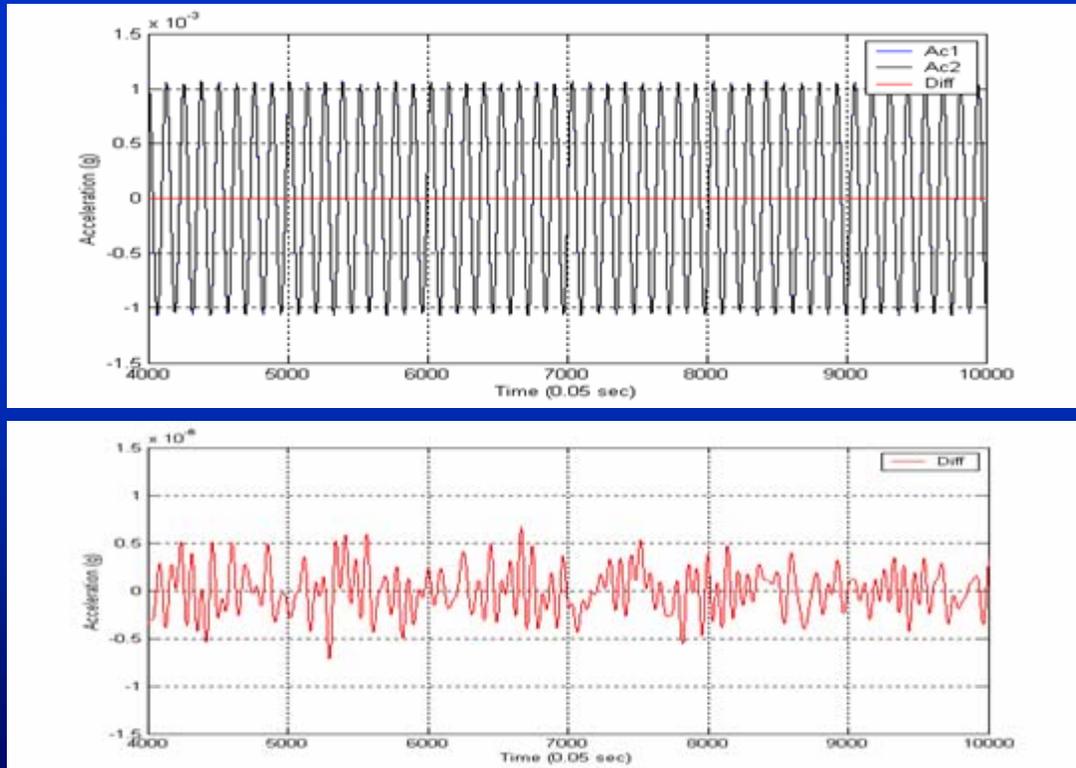


$$\frac{1}{Qt} = \frac{1}{Qm} + \frac{1}{Qe} \quad \frac{1}{Qe} = \beta \frac{\omega_0 RC}{1 + (\omega_0 RC)^2} \quad \beta = \frac{C \cdot E^2}{M \cdot \omega_0^2}$$

Experimental results with a differential accelerometer prototype

Rejection of the common-mode signals.

One important characteristic of a differential accelerometer is its ability to reject perturbations that are not differential, i.e., common-mode disturbances. This ability is quantified by the common-mode rejection factor (**CMRF**).

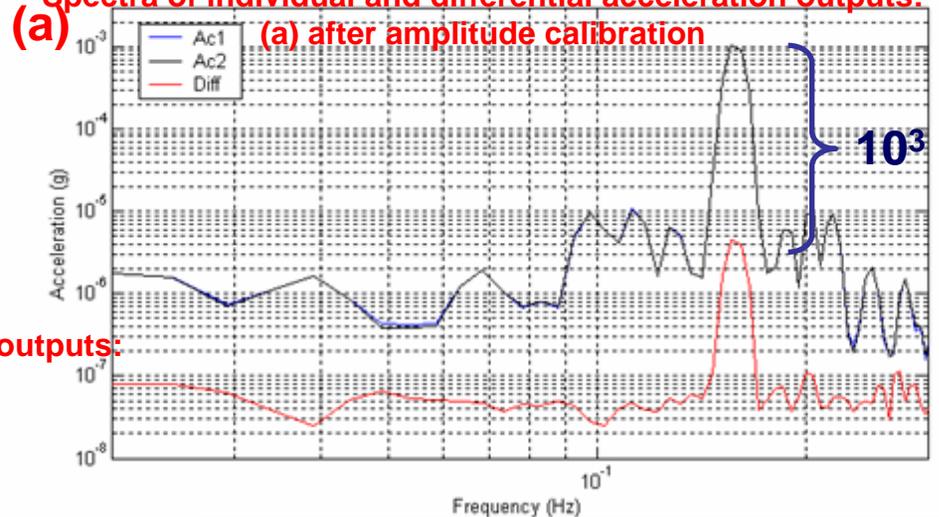


Experimental results with a differential accelerometer prototype

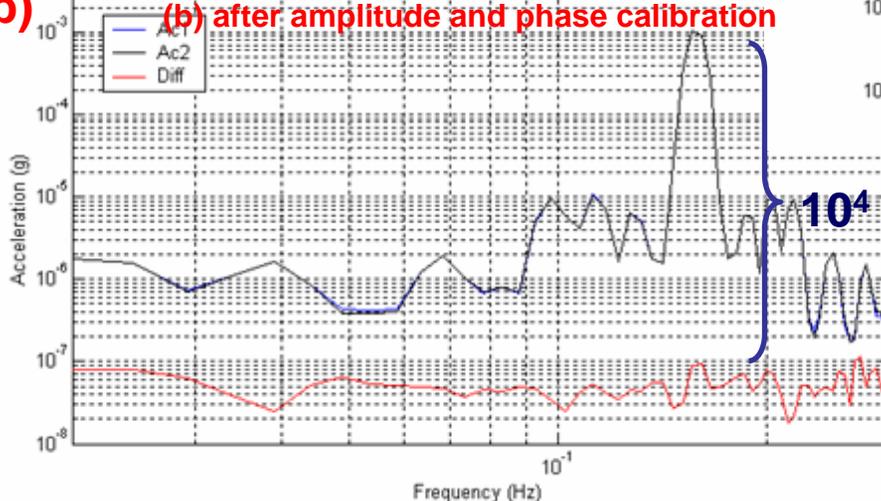
Rejection of the common-mode signals.

Figure (b) shows that after calibrating for amplitude and phase a 10^4 attenuation is readily obtained for the differential signal. This level of attenuation is effective not only at the perturbation frequency of 0.15 Hz but also over a larger frequency band.

Spectra of individual and differential acceleration outputs:



(b) Spectra of individual and differential acceleration outputs: (b) after amplitude and phase calibration



An attenuation of 10^4 or equivalently a common-mode rejection factor of 10^4 meets the present requirement on the **CMRF** for the proposed tests of the **WEP**.

Conclusions

- **Advantages**
 - **Reusability and easy access to experiment**
 - **Low cost**
 - **Strong gravity signal (i.e., 1 g)**
 - **Noise level comparable to drag-free satellites**
- **Disadvantages**
 - **Short integration time**
- **In summary**
 - **Estimated accuracy in testing the WEP several parts in 10^{-15} with 95% confidence level**
 - **Potential accuracy improvement of 2 orders of magnitude with respect to the state of the art**

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