

HGHG Schemes for Short Wavelengths

Agostino Marinelli (LNF, INFN),

R. Bonifacio (INFN)

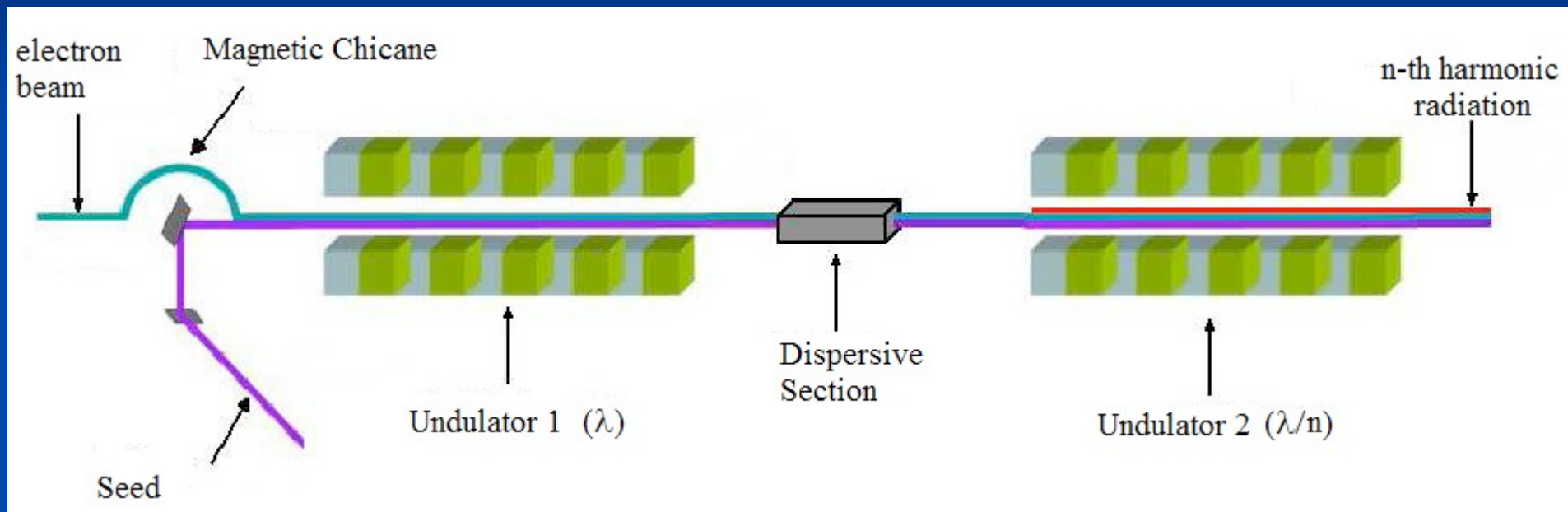
G. Robb (University of Strathclyde)

Cristina Vaccarezza (LNF, INFN)

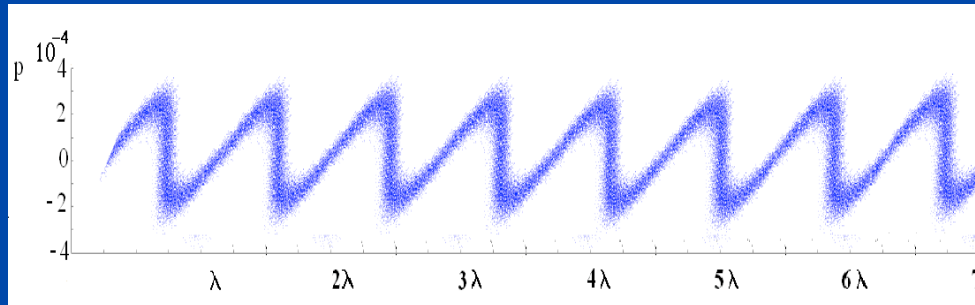
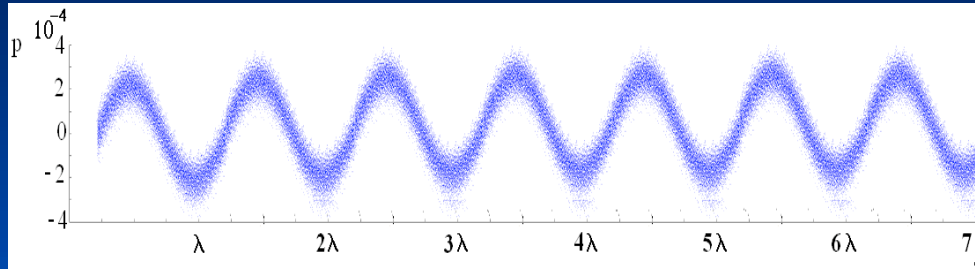
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- Preliminary design of a single stage HGHG scheme for SPARX**
- Possible improvements**
- Conclusions**

HGHG: High Gain Harmonic Generation



The Dispersive Section



$$b_n = J_n\left(n\Delta p \frac{d\theta}{dp}\right) \exp\left(-1/2\left(n\sigma_p \frac{d\theta}{dp}\right)^2\right)$$

$$d\theta/dp_{\text{opt}} = 1 / \Delta p$$

$$b_{n,\text{opt}} \simeq \max[J_n] \exp\left(-1/2\left(n \frac{\sigma_p}{\Delta p}\right)^2\right)$$

To have significant
harmonic bunching

$$\Delta p \sim n \sigma_p$$

Energy Spread Effects

In order to have significant bunching on
the n-th harmonic:

$$\Delta p \sim n \sigma_p$$

Efficient FEL process in the radiator if:

$$\Delta p \ll \rho$$

Thus:

$$\sigma_p \ll \rho/n$$

Shot Noise Effects

-Modulator



$$P_{seed} \gg P_{sh} = \frac{3^{3/4} 4\pi \rho_{mod}^2 W_b}{N_\lambda \sqrt{\pi \bar{z}_{mod}}}$$

FEL process driven by both external seed and shot-noise

-Radiator



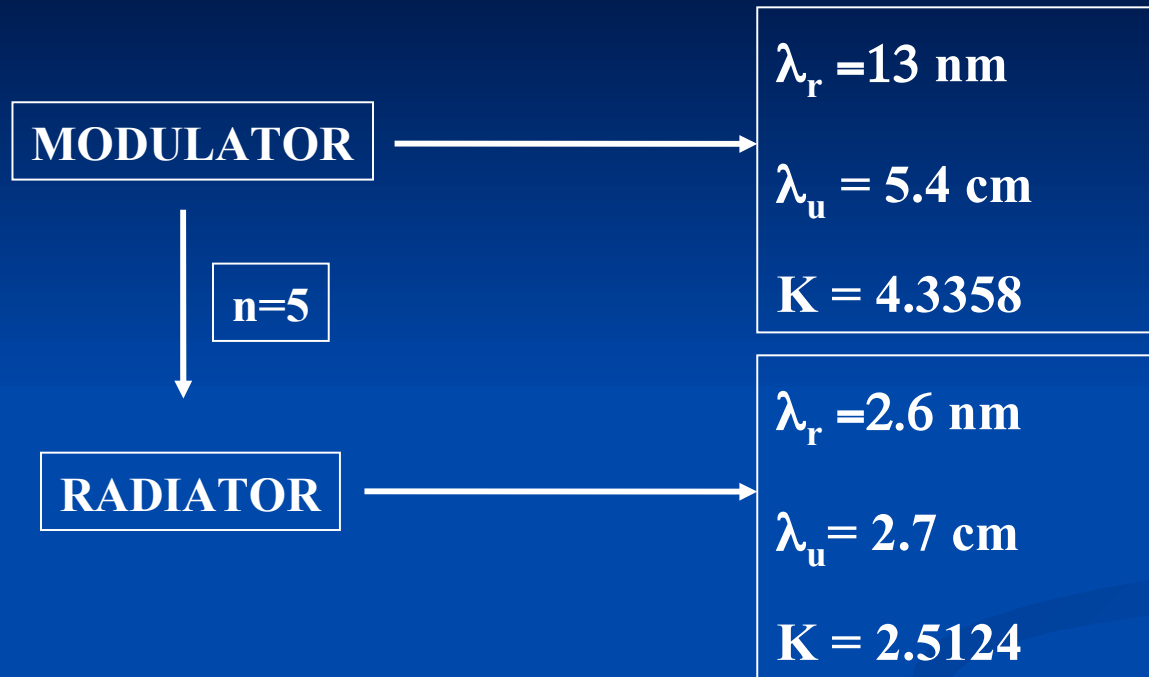
$$|b_{0,n,c}|^2 \gg |b_{sh}|^2 = \frac{3^{3/4} 4\pi \rho_{rad}}{N_{\lambda/n} \sqrt{\pi \bar{z}_{rad}^{sat}}}$$

FEL process driven by both coherent harmonic bunching and shot-noise

Design Guidelines

- Choose a sufficiently high seed power to overcome shot noise effects in the modulator
- Choose a sufficiently high harmonic bunching factor to overcome shot-noise effects in the radiator
- Use an acceptable energy modulation
- Design the modulator and the dispersive section to fulfill previous choices

Undulators



Electron Beam (SPARX case)

$E=2.3$ GeV

$\varepsilon = 1$ mm mrad

$\sigma_x = \sigma_y = 4.2 \cdot 10^{-5}$ m

$I=2.4$ kA

$\sigma_p = 10^{-4}$

Method

- **3-D Time Dependent Simulations with GENESIS 1.3**
- **Undesired effects evaluated individually**
- **Joint effects evaluated on the final configuration**

$$P_{\text{seed}} > 30 \text{ kW}$$

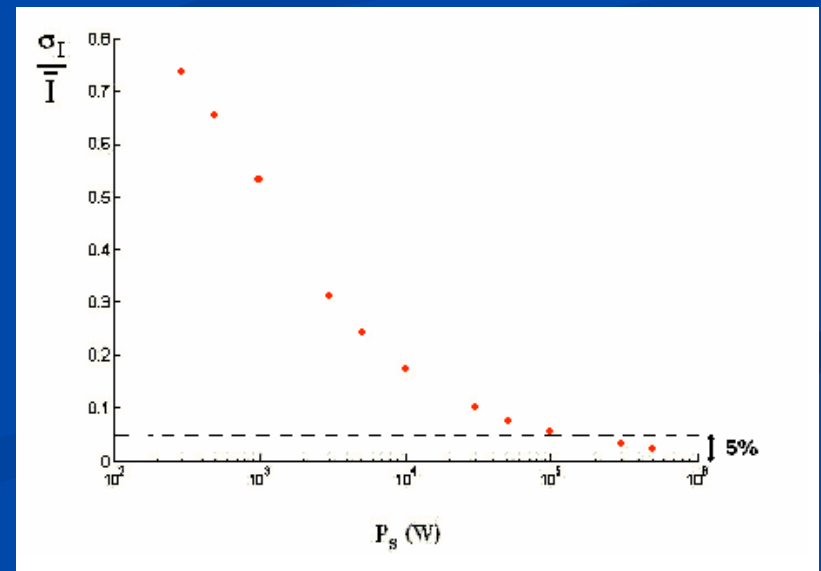
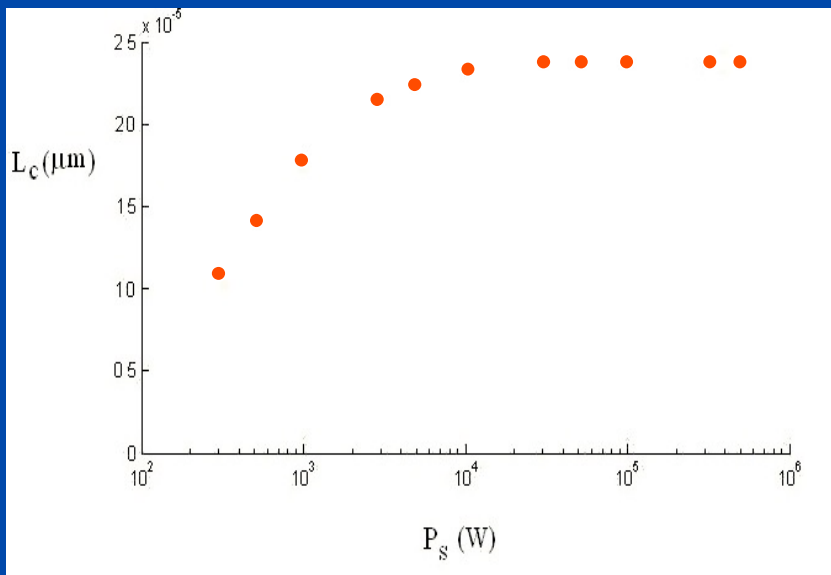
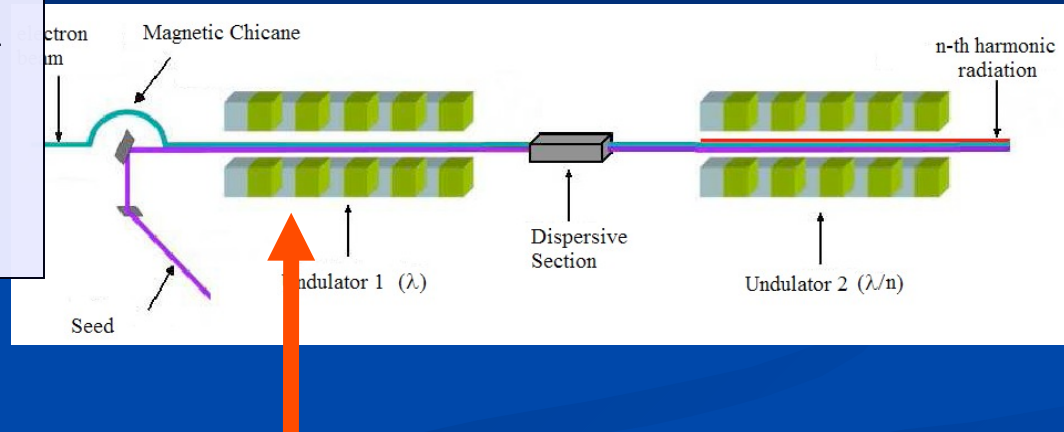
(first order)

$$P_{\text{seed}} > 300 \text{ kW}$$

(second order)

electron and seed beams

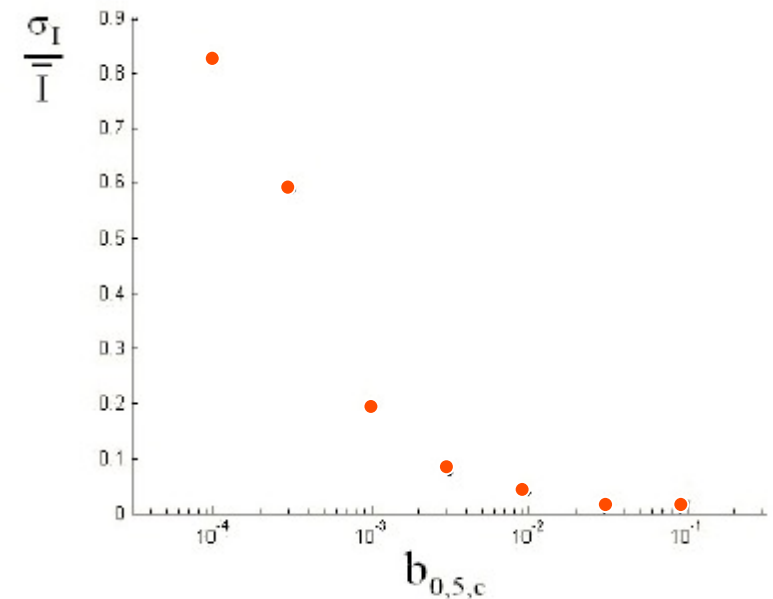
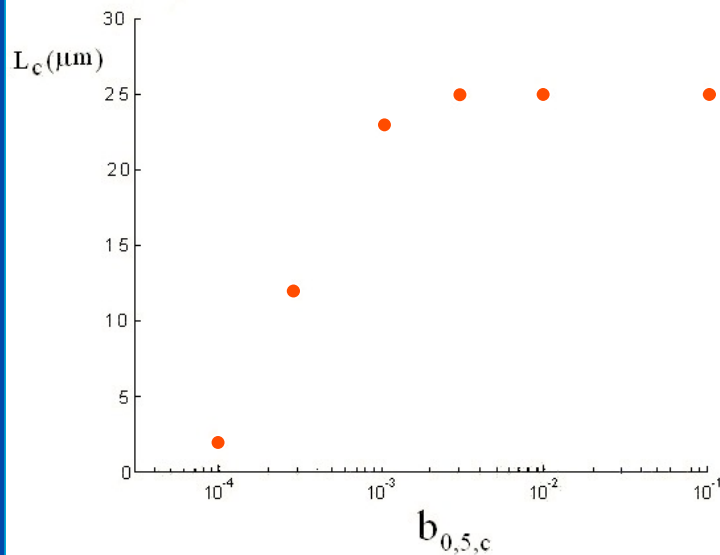
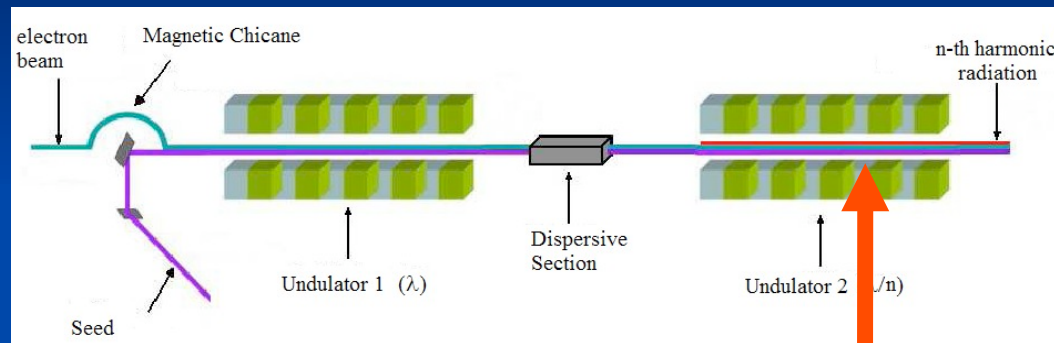
Free properties in the modulator



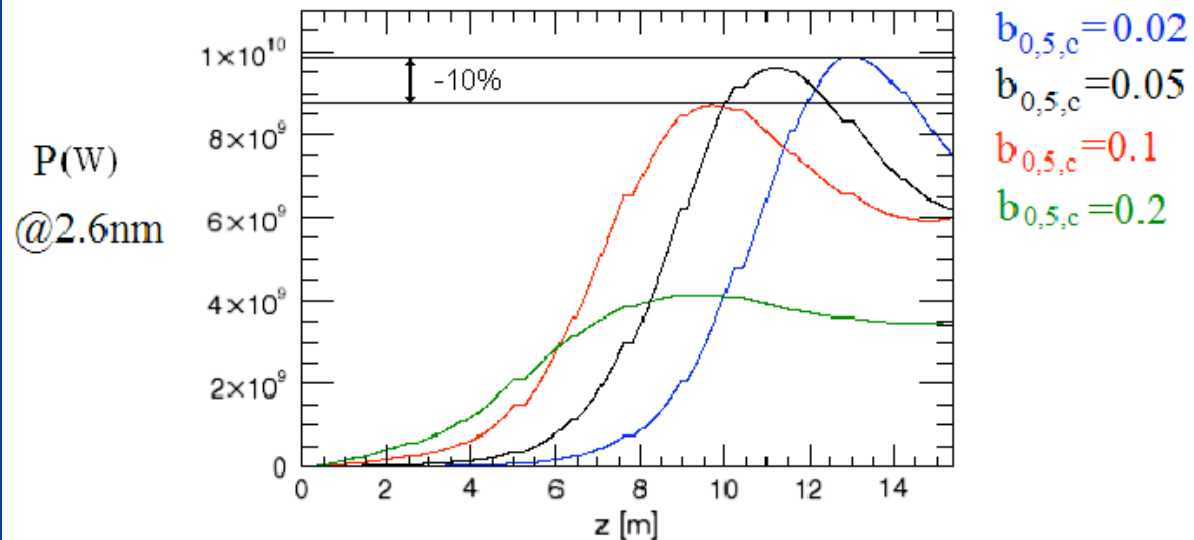
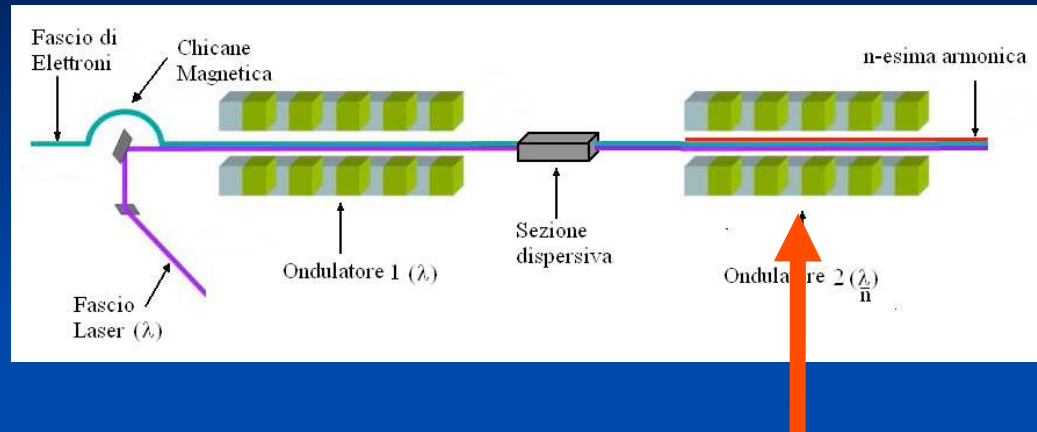
$$b_5 > 0.03$$

(first and second order temporal coherence)

coherence properties in the
radiator
("fresh beam")



Energy Spread effects

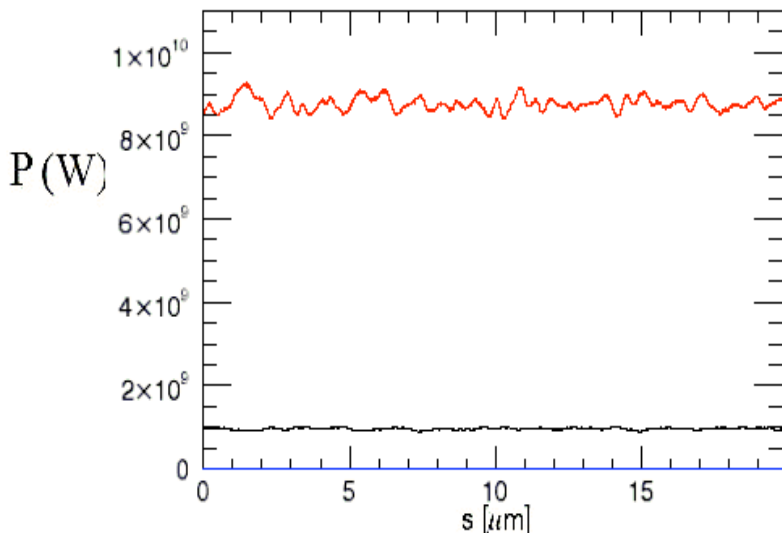


Time Dependent Simulations

2 cases

$P_s = 300 \text{ kW}$, $b_5=0.1$

$L_c=2/3 L_b$, $\sigma_I/I=1.9\%$



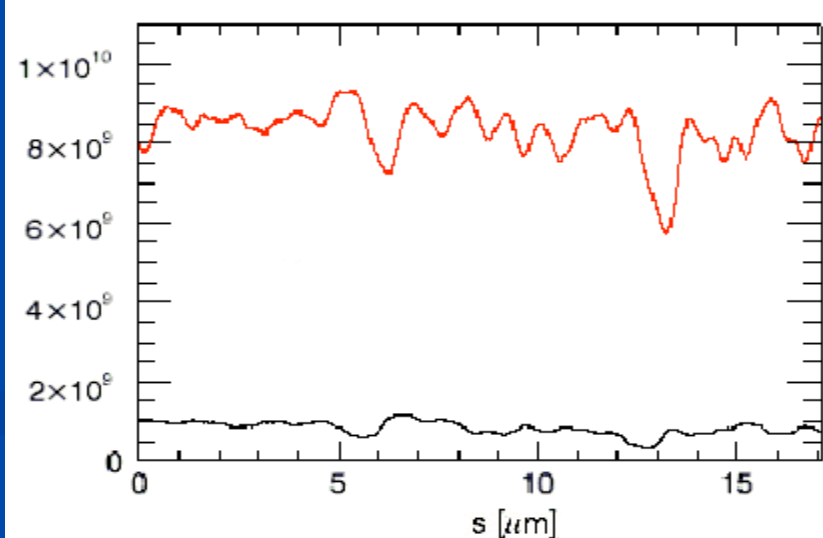
$z=9.5\text{m}$
(saturation)

$z=5\text{m}$

$z=0$

$P_s = 30 \text{ kW}$, $b_5=0.1$

$L_c=0.9 * 2/3 L_b$, $\sigma_I/I=8.8\%$



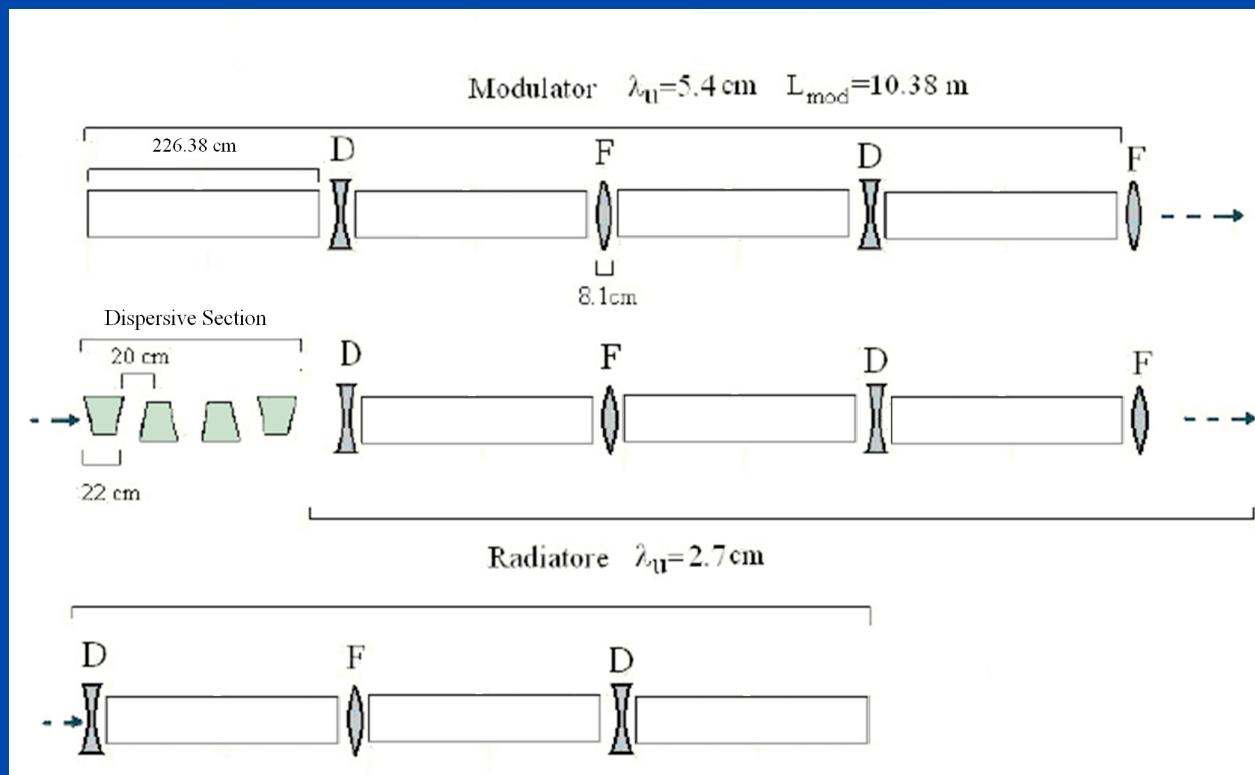
Possible HGHG scheme for SPARX

$$P_{s_{PEAK}} = 50 \text{ kW}$$

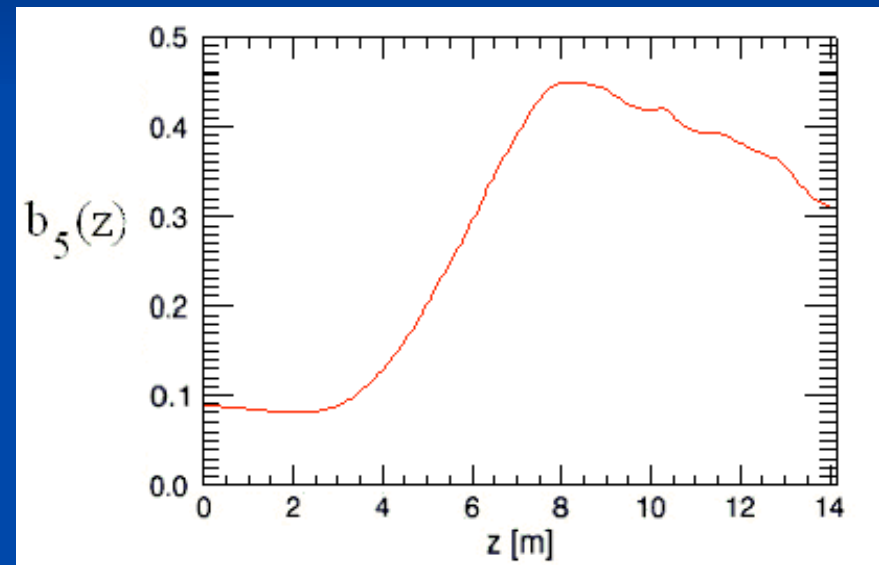
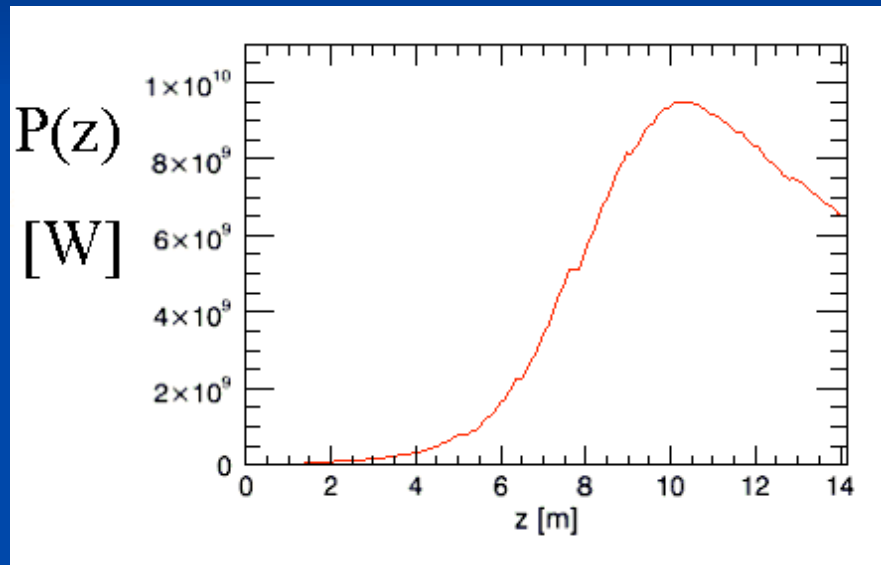
$$b_{5IN} = 0.08$$

$$T_{FWHM} = 70 \text{ fs}$$

(Feasible with HHG)



Peak Power and Bunching Along the Radiator (2.6 nm)



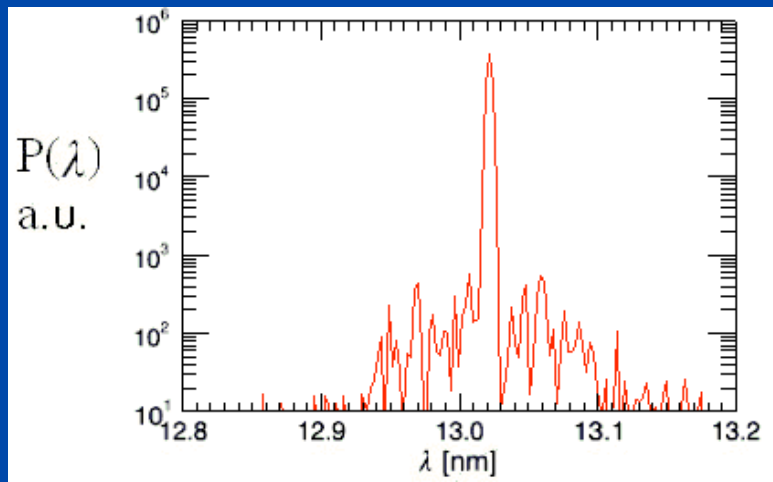
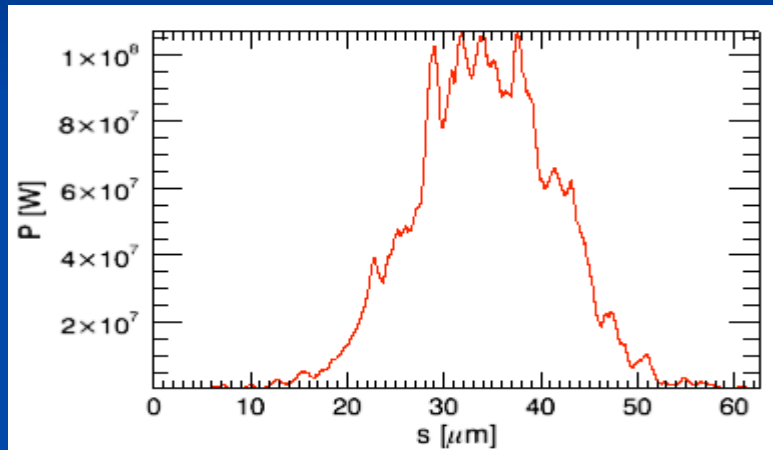
Saturation in 10 m

Gaussian Beams

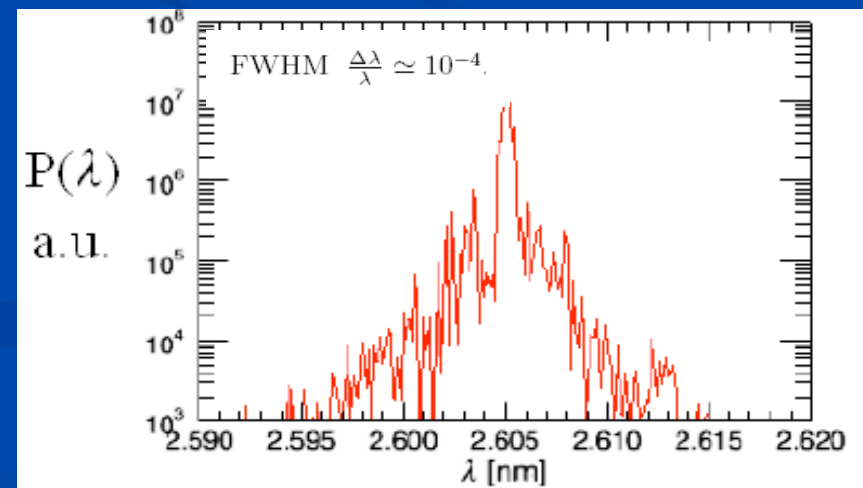
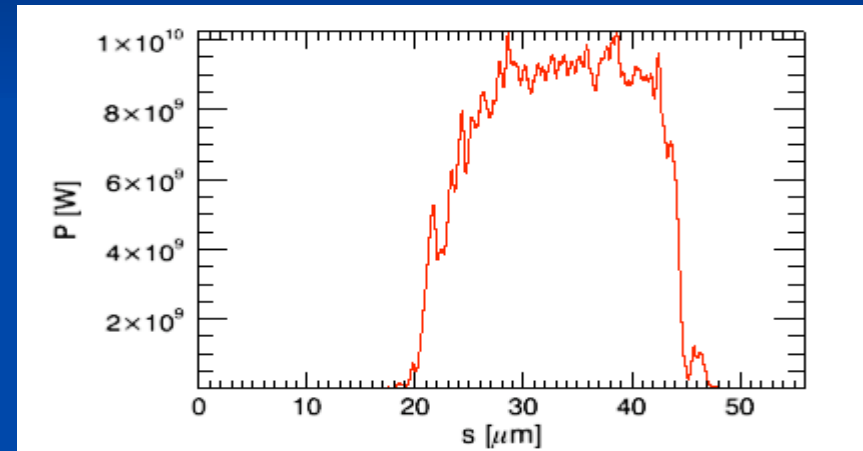
(both radiation and electrons)

50kW Seed Peak Power (realistic with HHG in gases)

1 st Harmonic



5 th Harmonic (saturation)



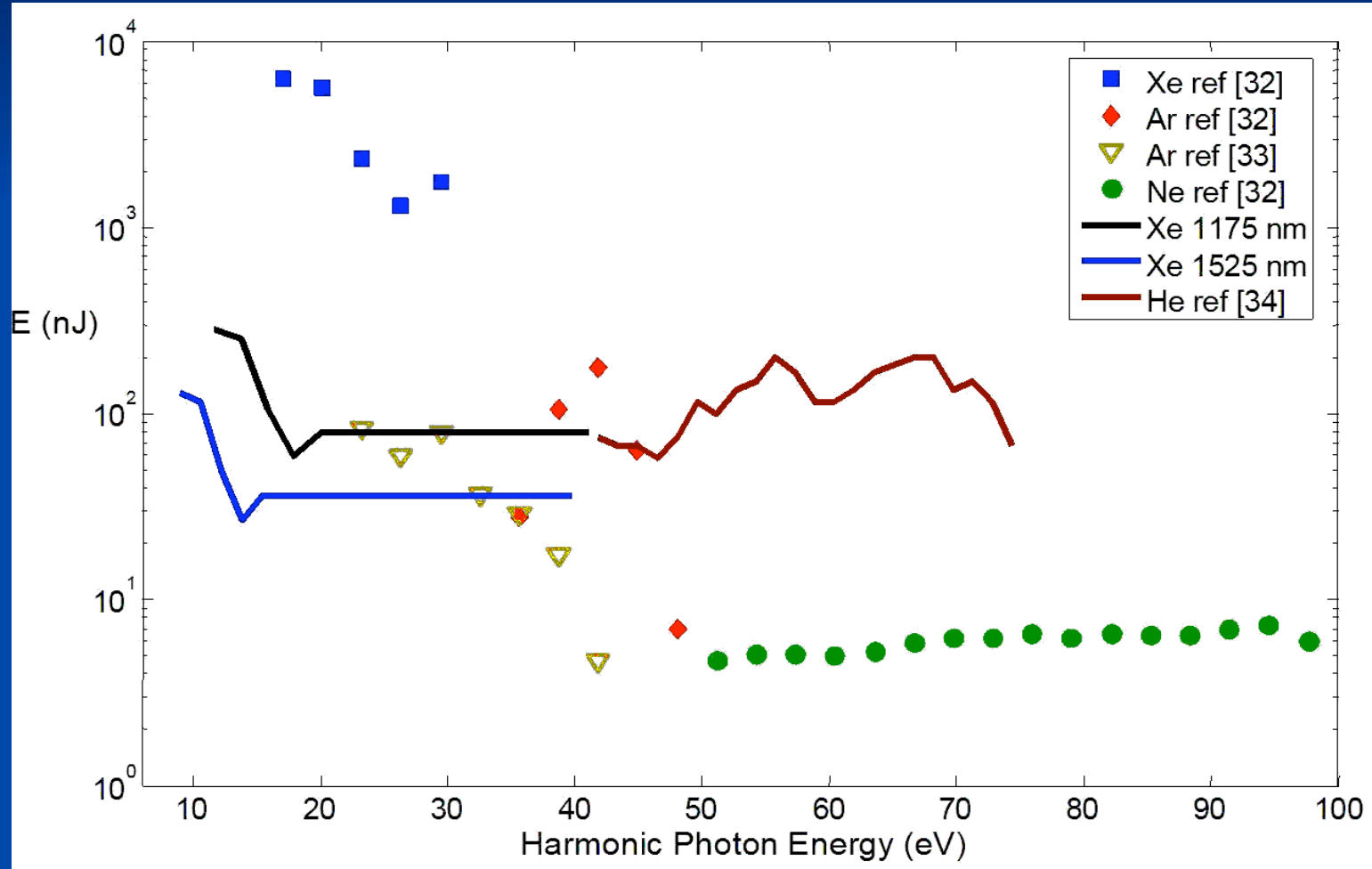
How Can We Do Better With a Single Stage HGHG?

Shot noise is the main issue in HGHG schemes at

X-UV wavelengths:

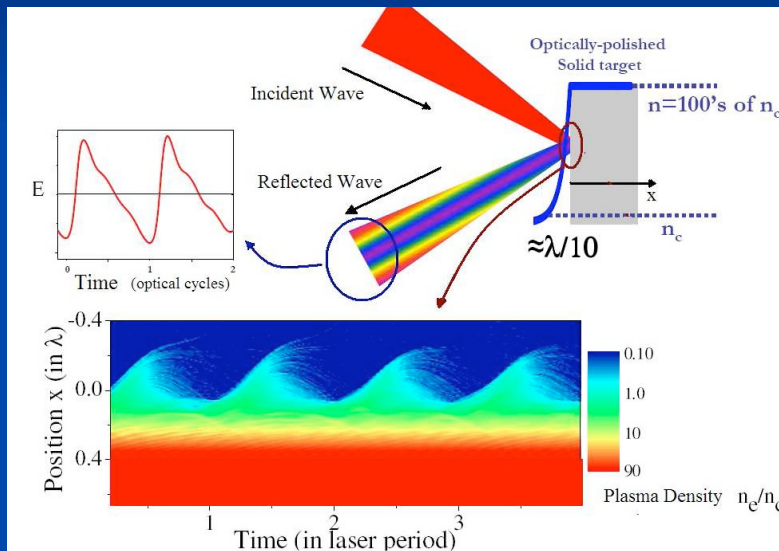
- Alternative seeding sources**
- Decreasing the equivalent shot-noise power**

HHG in gases

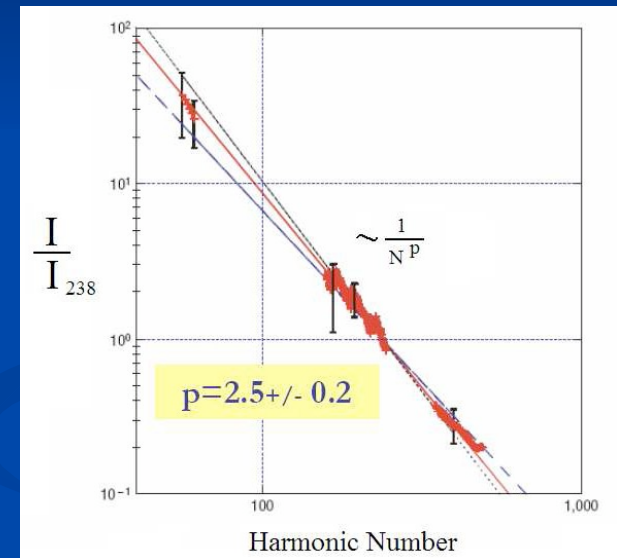


Alternative Seeding Sources: Relativistic Oscillating Mirror

Thaury et al., Nature Physics 3, p. 424 (2007)



B. Dromey et al, Nature Physics 2, p. 456 (2006)



0.2 mJ @ 17 nm
0,07 mJ @ 4 nm
(t=600 fs)

$\eta \sim 10^{-6} \pm 1$ (0.07-0.7 mJ) and $3 \times 10^{-5} \pm 1$ (0.2-20 mJ)
 at 4 and 17 nm respectively

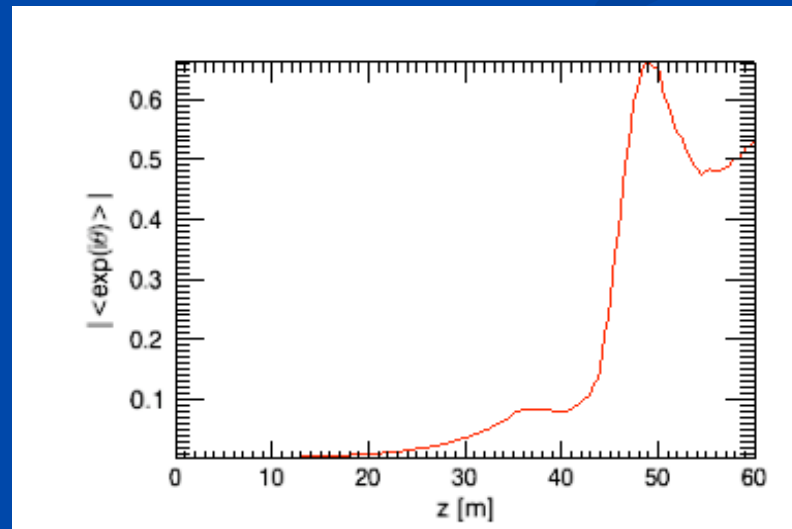
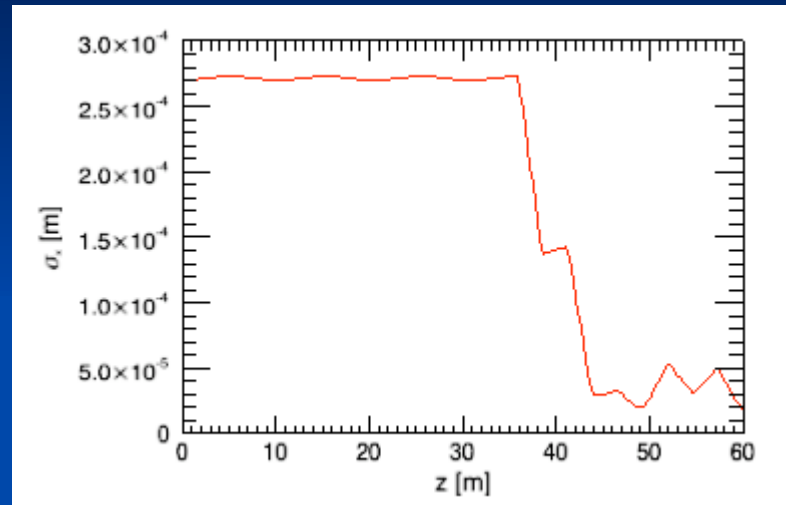
Low Noise Seeding

$$P_{sh} = \frac{3^{3/4} 4\pi \rho^2 W_b}{N_\lambda \sqrt{\pi \bar{z}}}$$

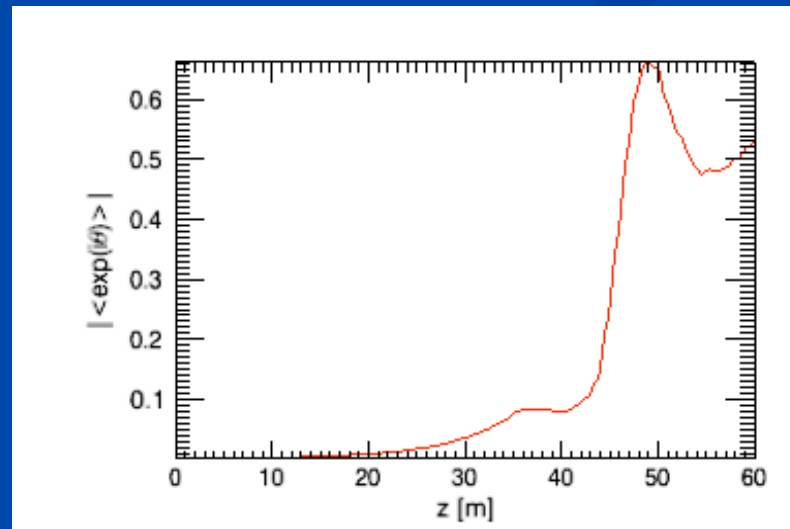
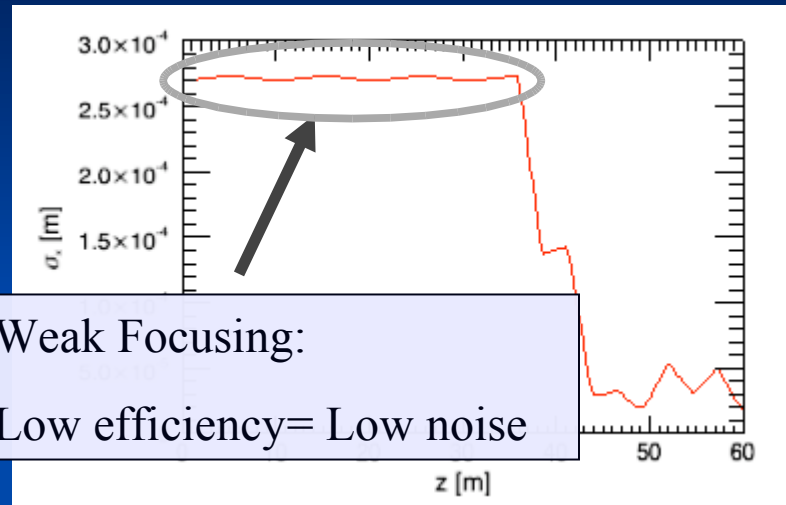
$$\rho \propto \gamma_r^{-1} \sigma_e^{-1/3} I^{1/3} a_u^{2/3} \lambda_u^{2/3}$$

$$P_{sh} \propto \sigma_e^{-2/3}$$

Low Noise Seeding

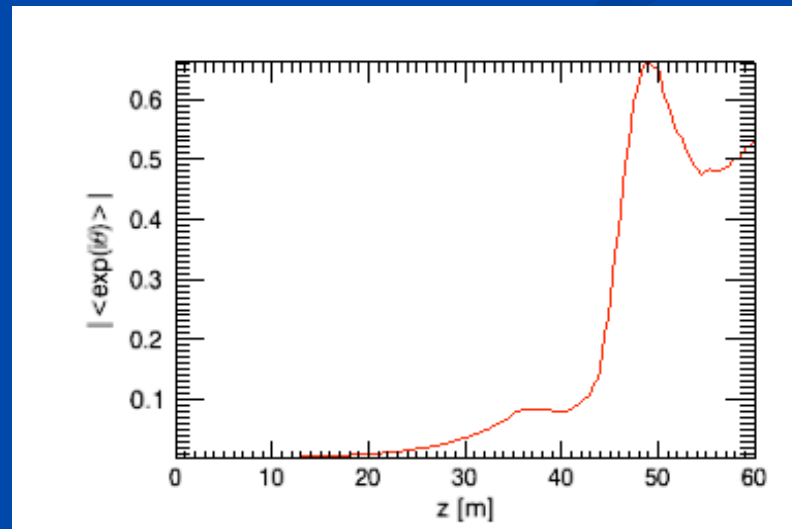
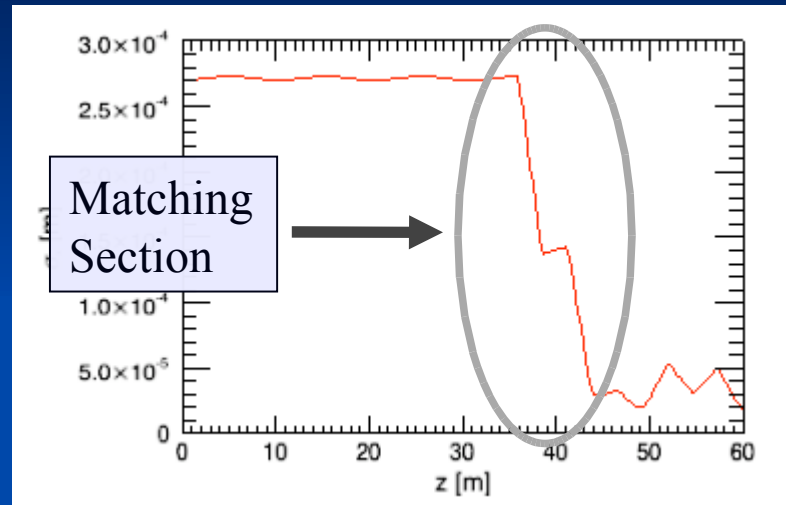


Low Noise Seeding



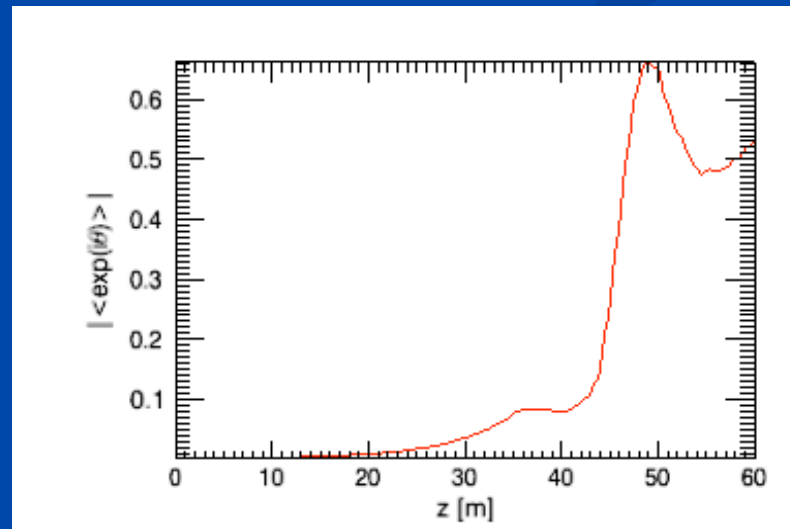
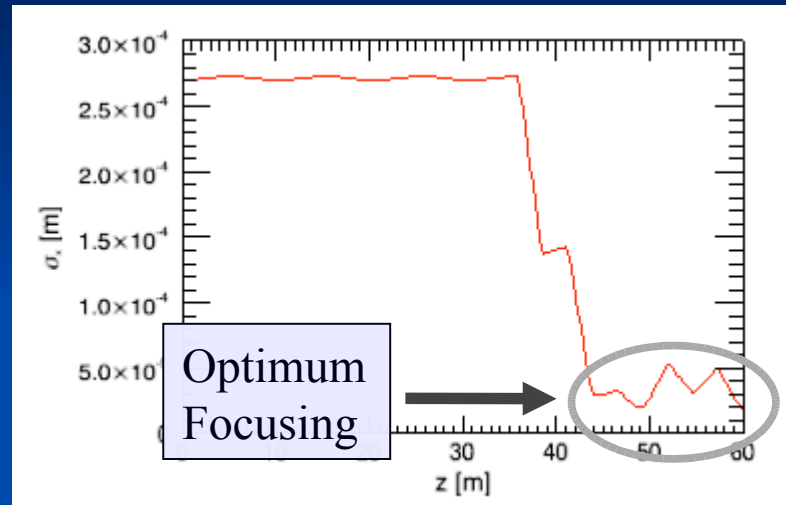
$$P_{sh} \propto \sigma_e^{-2/3}$$

Low Noise Seeding



$$P_{sh} \propto \sigma_e^{-2/3}$$

Low Noise Seeding



$$P_{sh} \propto \sigma_e^{-2/3}$$

Low Noise Seeding

Suitable for:

- HGHG modulator**
- Seeding at shorter wavelengths**

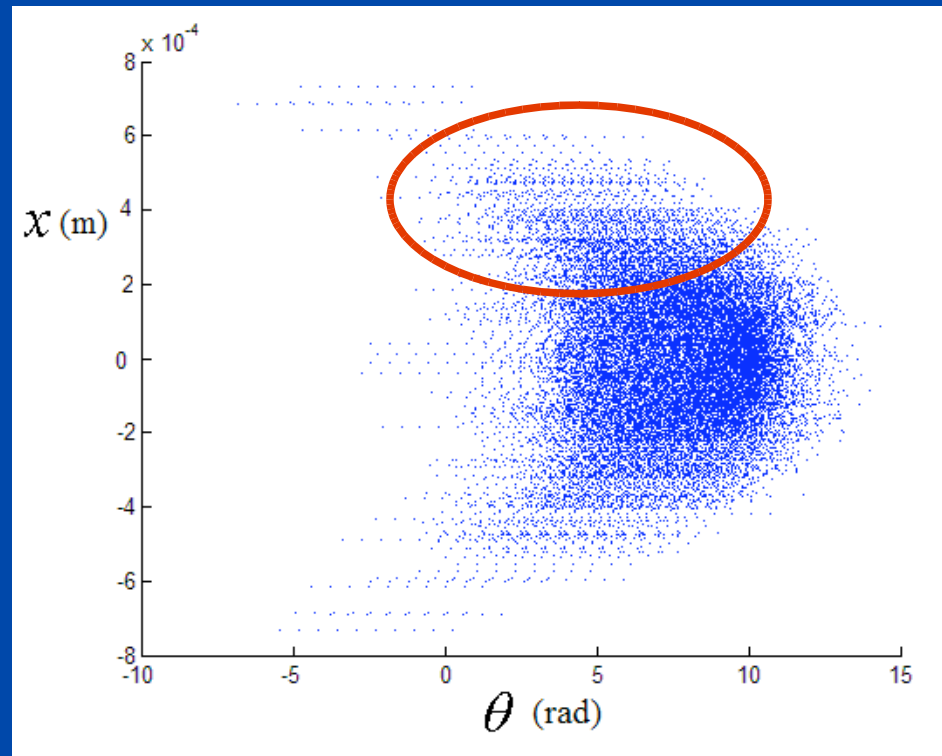
Problems:

- Longer undulator! (costs, alignment...)**
- Bunched beam transport issues**

Low Noise Seeding

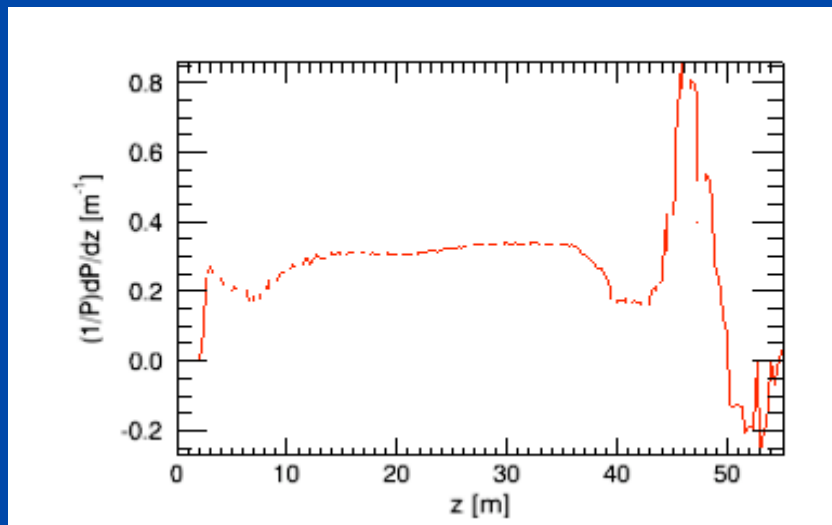
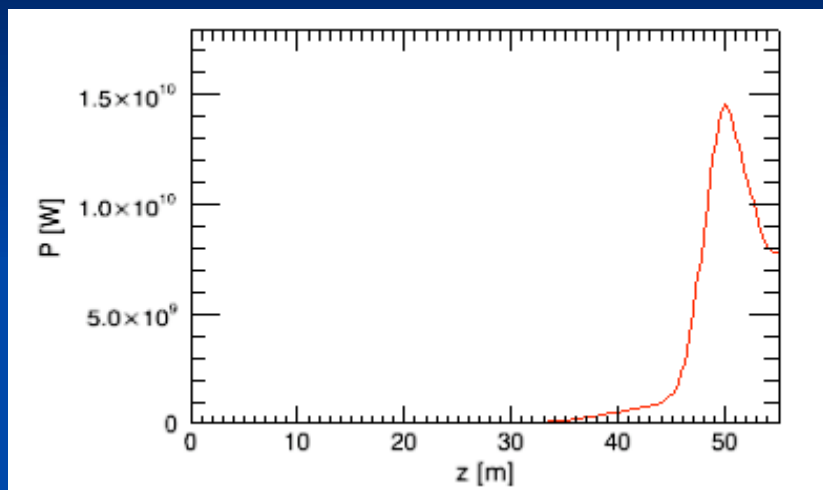
External particles get a stronger transverse kick in the matching section and slip backwards in phase:

bunching factor decreases!

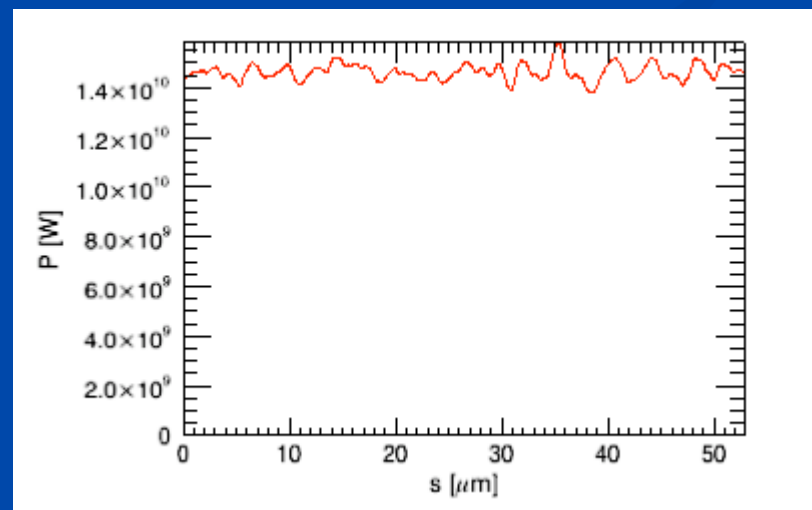


Low Noise Seeding

Example : 30kW seed



2% Intensity
Fluctuations



Conclusions

- A method for the design of a single stage HGHG has been discussed
- Preliminary study on a possible HGHG scheme for SPARX has been carried out
- Studies on possible improvements are ongoing

Acknowledgments

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