

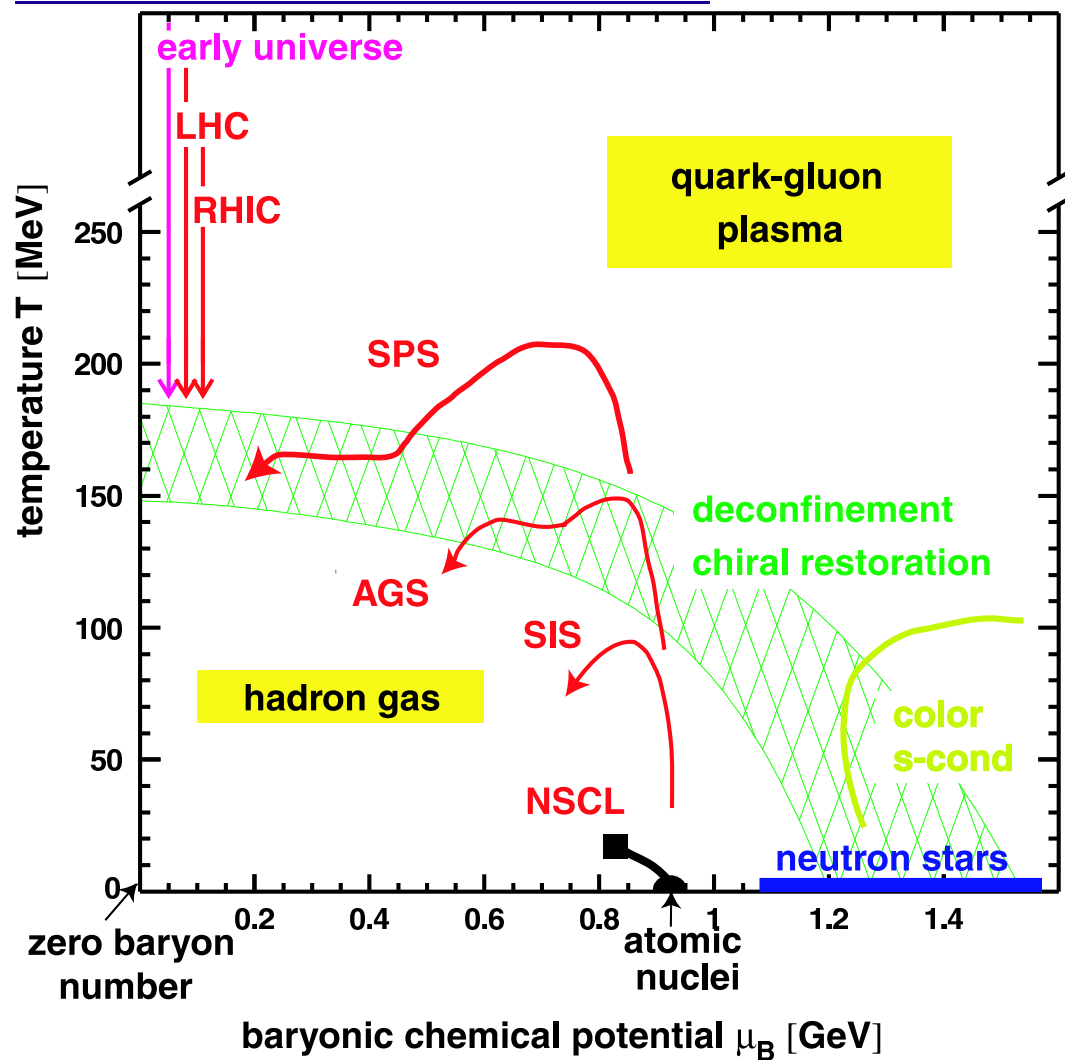
First Workshop
on
Quark-Hadron Duality and the Transition to pQCD
Laboratori Nazionali di Frascati 6-8 June 2005

Quark Gluon Plasma and Hadron Gas
on the Lattice
Maria-Paola Lombardo

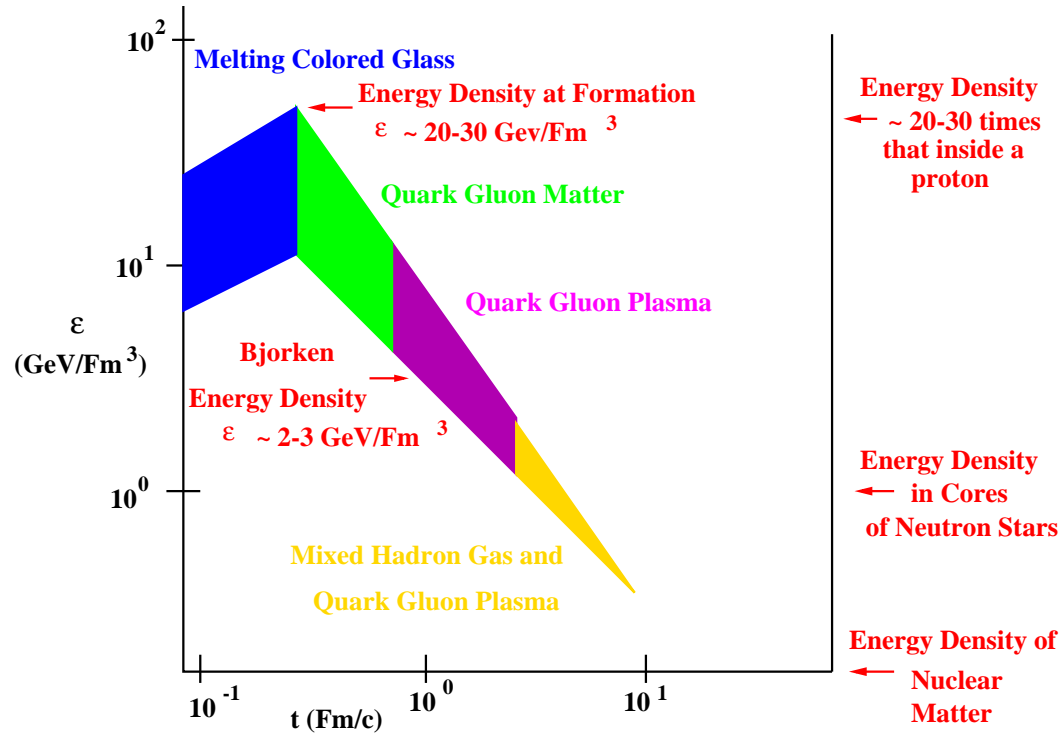
An informal overview geared towards Nuclear Experimental Colleagues

- The Critical Line
- **The Hot Phase : Approaching a Quark Gluon Plasma**
- **The Hadronic Phase and The Resonance Gas Model**
- Summary, the Main Caveat and a Major Challenge

The QCD phase diagram



Real time evolution:



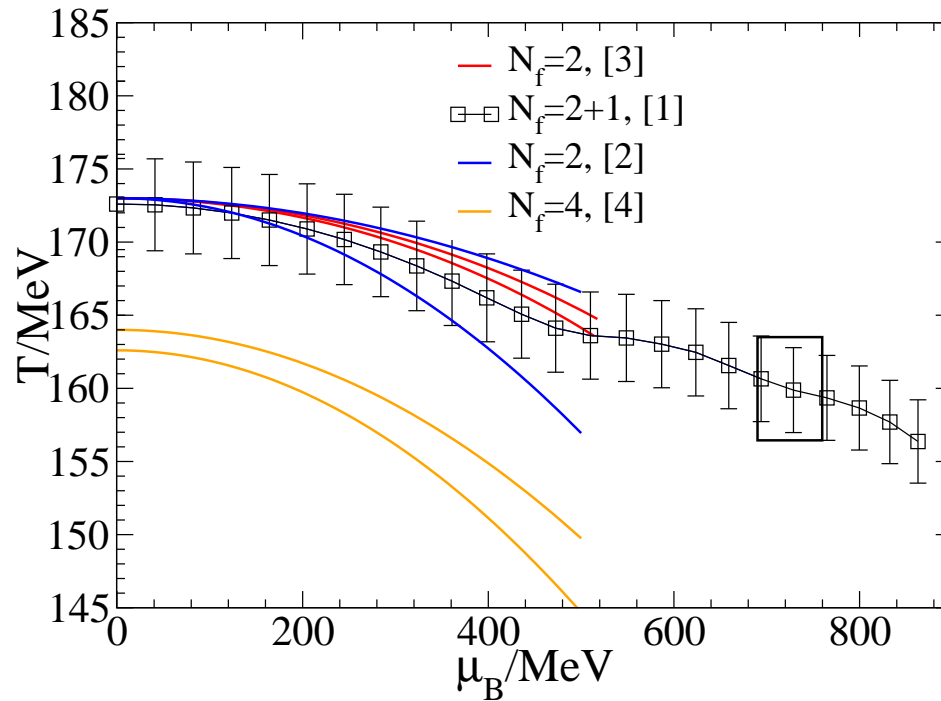
Picture from Blaizot, Iancu 2004

Lattice studies = equilibrium studies :

Thermodynamics and spectrum; hope that quark gluon plasma will equilibrate during the evolution; equilibrium solution are steady state solution of the dynamical Fokker Planck operator; lattice calculations will help validanting simple models which can be studied out of equilibrium

The Critical Line, 2003

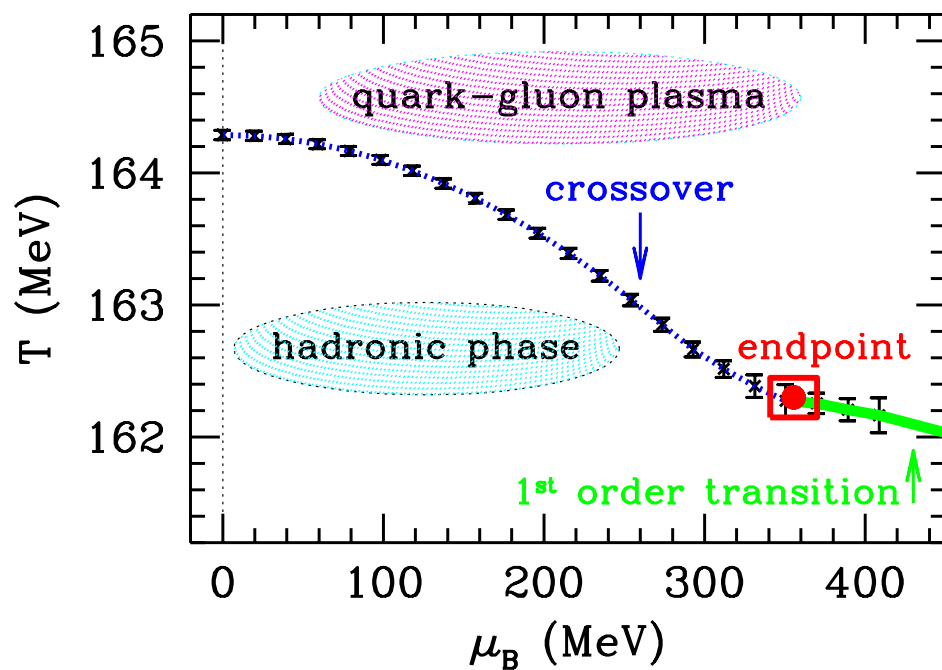
From O. Philipsen and E. Laermann *Ann. Rev. Nucl. Part. Phys.* 2003



1. Fodor Z and Katz SD, *JHEP* 0203:014 (2002).
2. Allton CR et al., *Phys. Rev. D* 66:074507 (2002).
3. de Forcrand P and Philipsen O, *Nucl. Phys. B*642:290 (2002).
4. D'Elia M and Lombardo MP, *Phys. Rev. D* 1:074507 (2003).

The critical line, 2004

Z. Fodor, S. Katz 2004



Question 1. *Sensitivity to quark mass values*

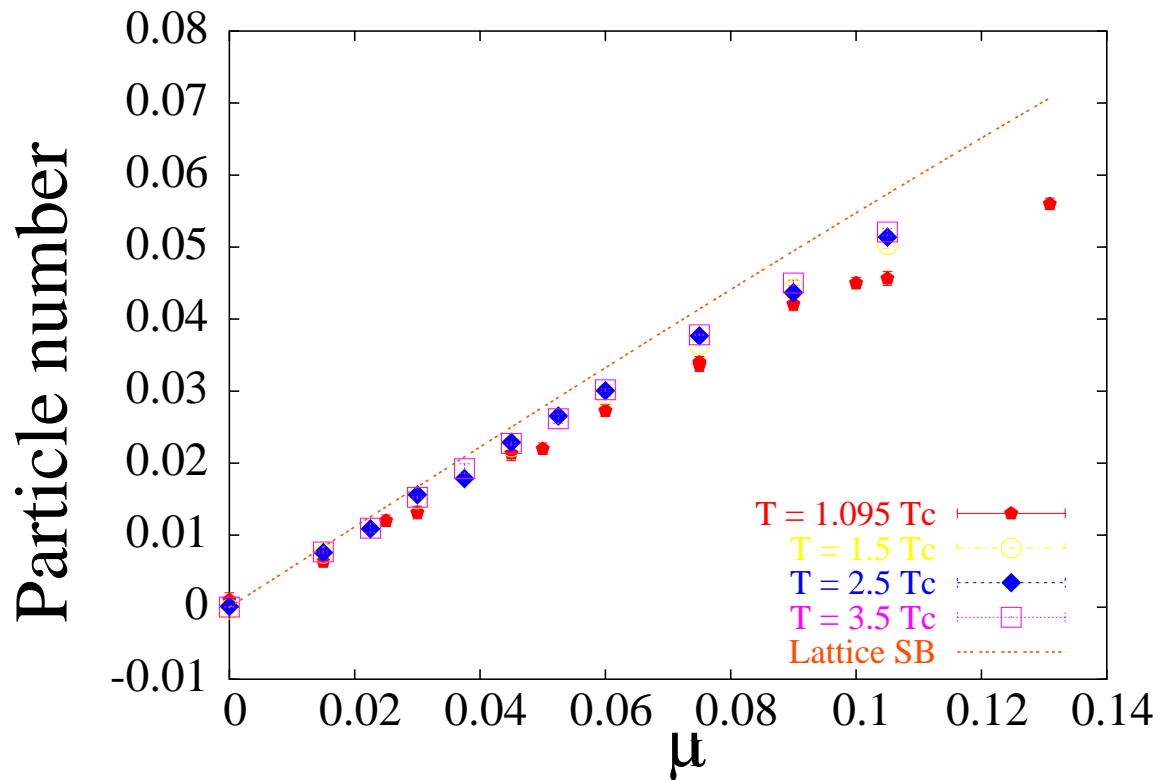
Question 2. *Systematics not fully under control*

The Hot Phase
and
the approach to a Quark Gluon Plasma

Monitoring the approach to a free gas of quarks and gluons

$$P(T, \mu) = \frac{\pi^2}{45} T^4 \left(8 + 7N_c \frac{n_f}{4} \right) + \frac{n_f}{2} \mu^2 T^2 + \frac{n_f}{4\pi^2} \mu^4 .$$

$\dot{=}$
analytic continuation from real to imaginary μ_B of the Stephan-Boltzmann lattice result



Corrections to Free Field

A. Vuorinen 2004:

$$P(T, \mu) = \frac{\pi^2}{45} T^4 \left(8 + 7N_c \frac{n_f}{4} \right) + \frac{n_f}{2} \mu^2 T^2 + \frac{n_f}{4\pi^2} \mu^4 + \dots$$

Alternatively (Rafelski, Letessier 2003, Quasiparticle models)

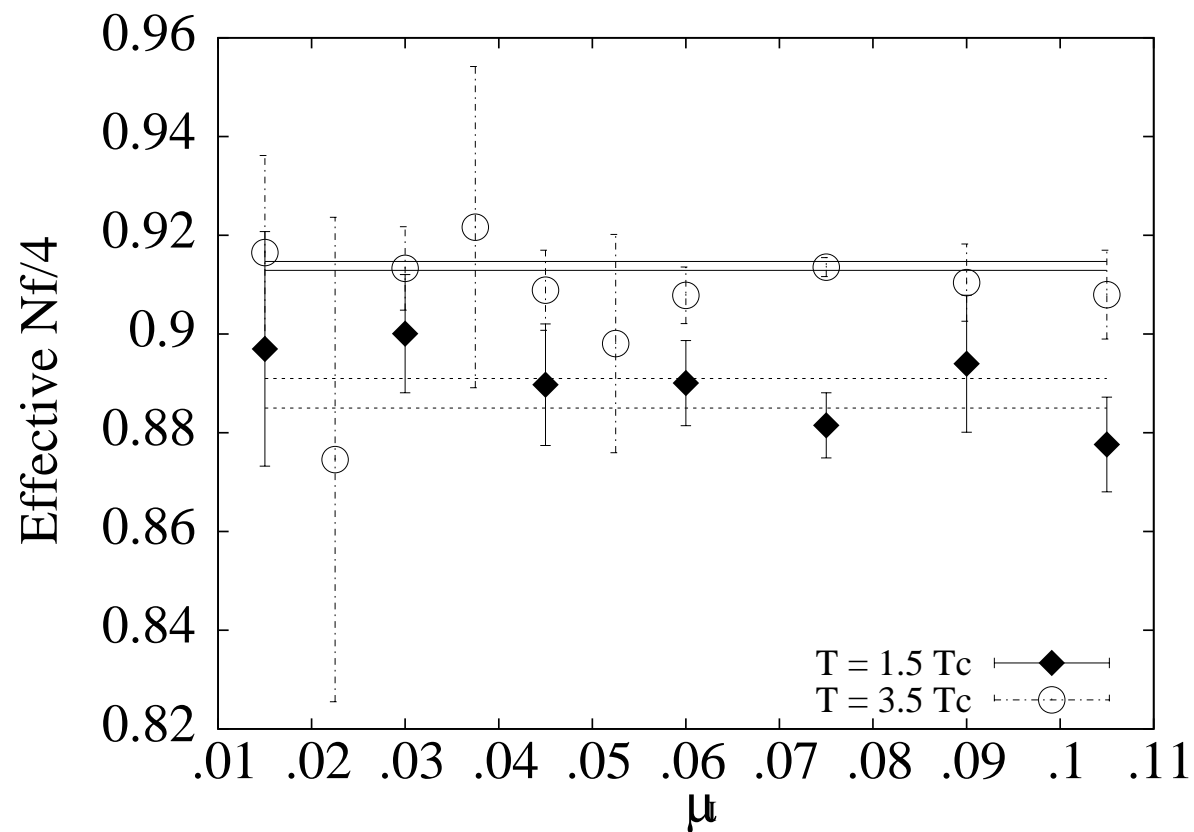
$$P(T, \mu) = f(\mu) \left(\frac{\pi^2}{45} T^4 \left(8 + 7N_c \frac{n_f}{4} \right) + \frac{n_f}{2} \mu^2 T^2 + \frac{n_f}{4\pi^2} \mu^4 \right)$$

Trivial possibility: $f(\mu)$ is a constant .

Possible interpretation: a free field with an effective number of flavors N_{eff} different from N_f

$$P(T, \mu) - P(T, 0) = (N_{eff}/n_f) \left(\frac{n_f}{2} \mu^2 T^2 + \frac{n_f}{4\pi^2} \mu^4 \right) = \left(\frac{N_{eff}}{2} \mu^2 T^2 + \frac{N_{eff}}{4\pi^2} \mu^4 \right)$$

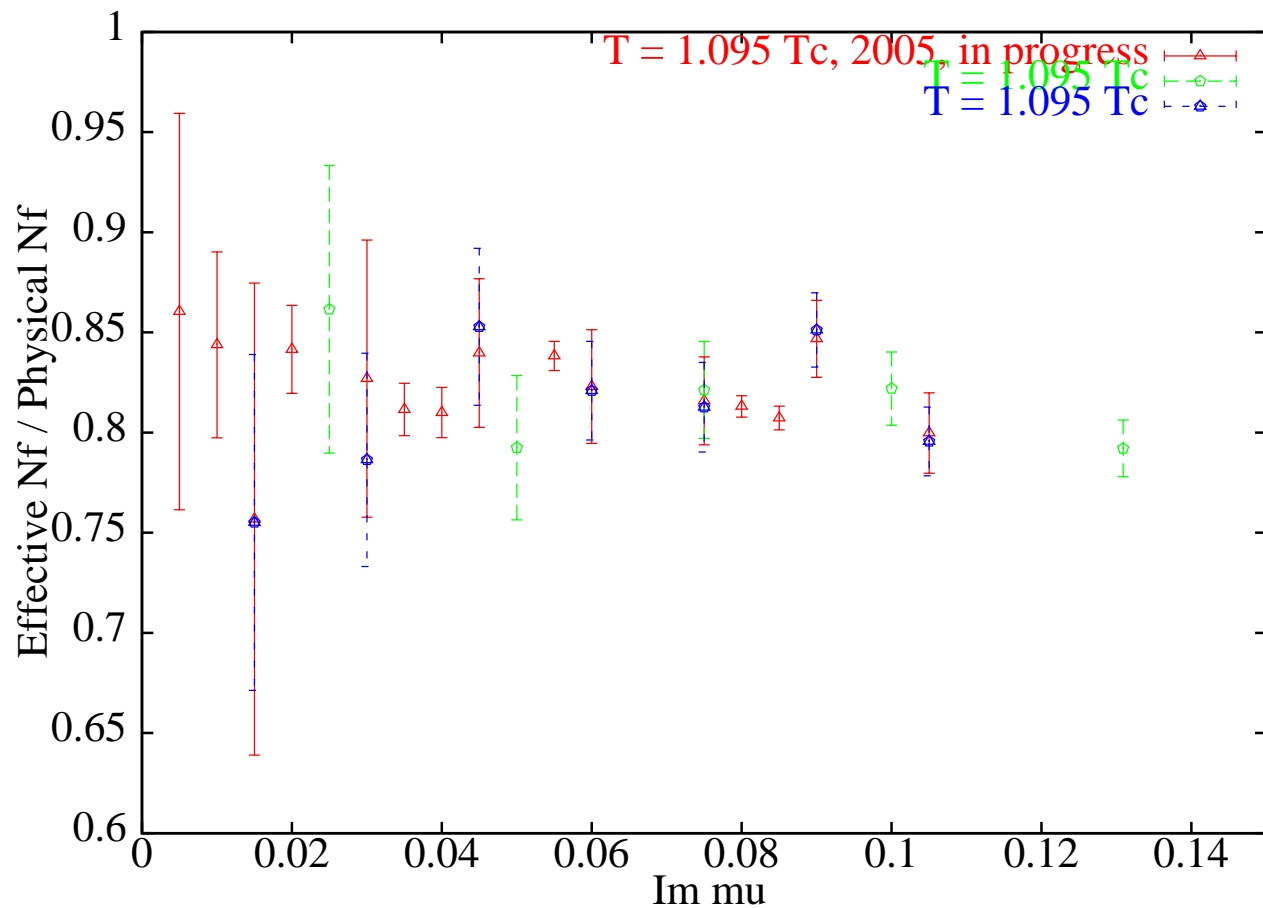
$f(\mu) = (N_{eff}/N_f)$ estimated on the lattice appear to be a constant for $T \geq 1.5T_c \neq 1$ i.e. $N_{eff} \neq N_f$



$T_c < T < 1.5T_c$: a Strongly Coupled Quark Gluon Plasma?

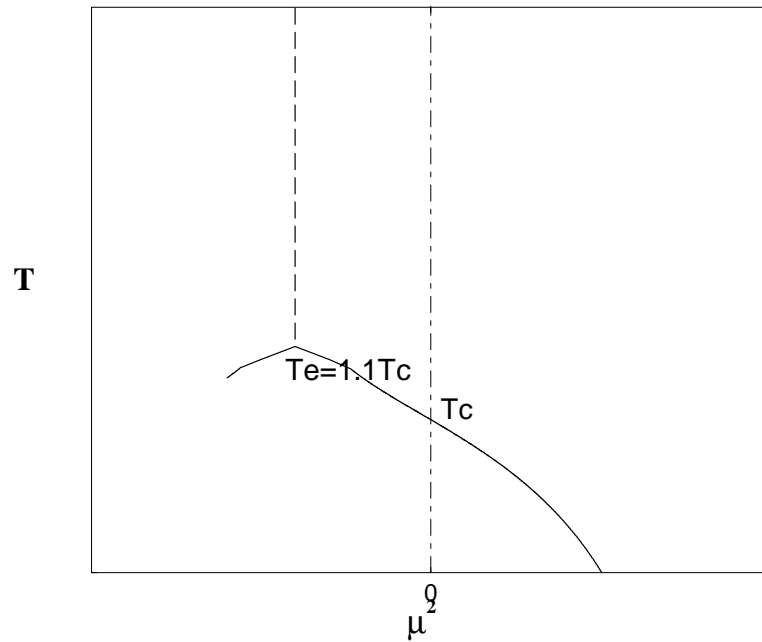
Possible non perturbative behaviour right above T_c

F. Di Renzo, M. D'Elia, MpL, in progress



Interplay of thermodynamics and critical behaviour for

$$T_C < T < T_E \simeq 1.1T_c$$



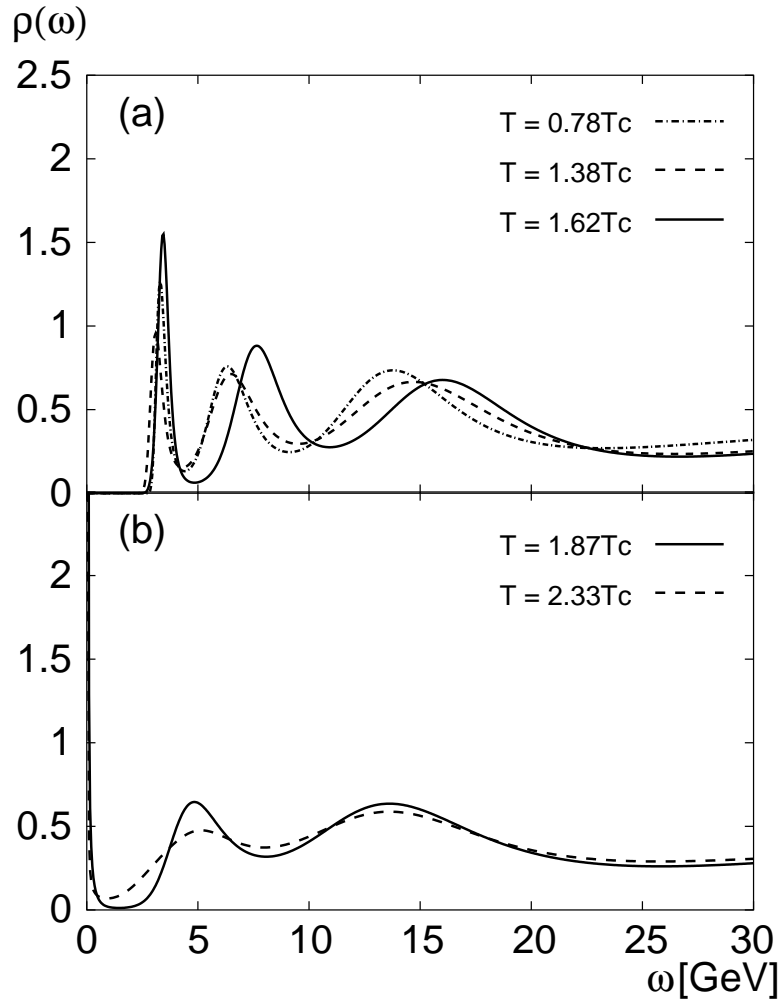
Phase diagram in the T, μ^2 plane

$$\log P(\mu, T) \propto (\mu - \mu_c)^\eta$$

Incompatible with a free field for continuous transitions, and for first order transitions of finite strength

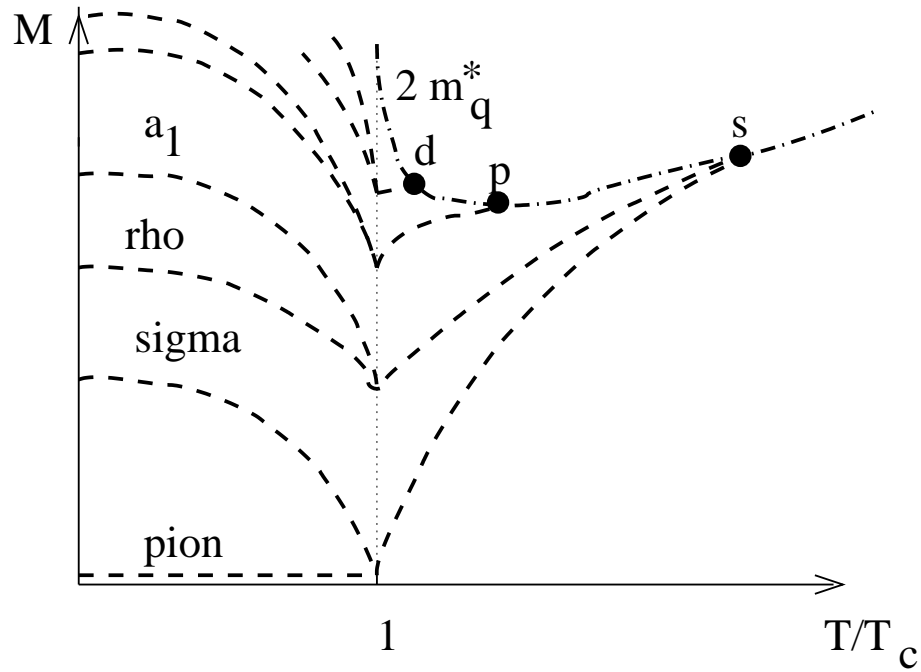
Survival of bound states at for $T_c < T < 1.6T_c$

Y. Asakawa, T.Hatsuda



J/Psi Spectral Functions

Bound States and S(trongly interactive) Quark Gluon Plasma



Shuryak, Zahed, 2002,2003, 2004

*The Hadronic Phase and the Hadron Resonance
Gas Model*

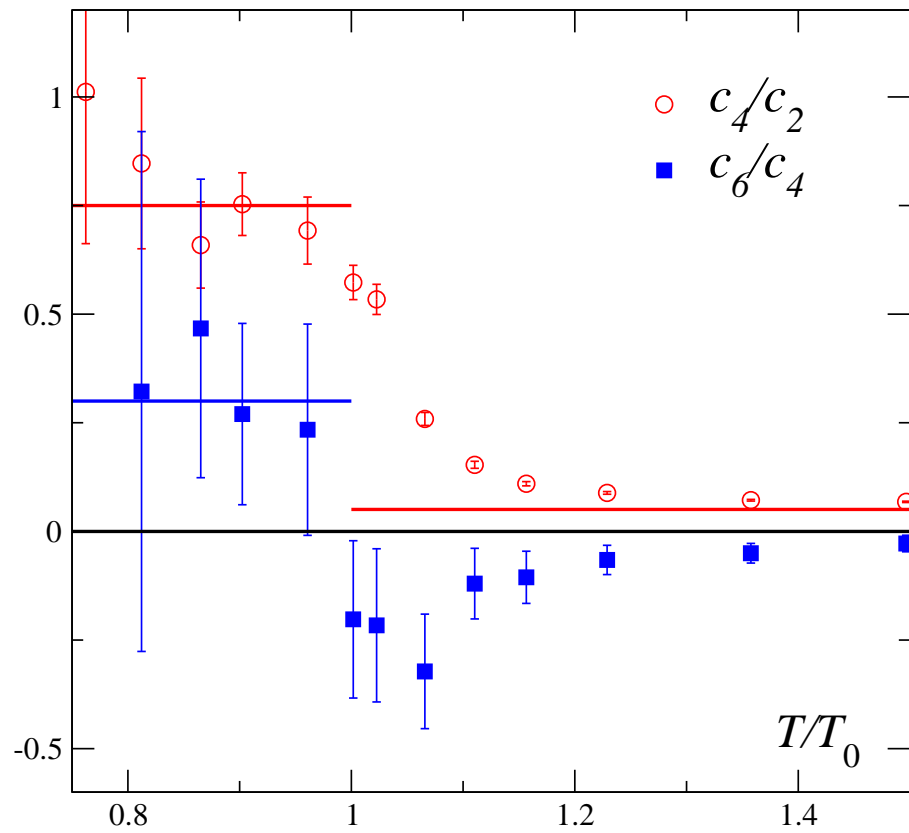
The *Hadron Resonance Gas* model might provide a description of QCD thermodynamics in the confined, hadronic phase of QCD

$$\frac{P(T, \mu) - P(T, 0)}{T^4} \simeq F(T) \left(\cosh\left(\frac{\mu_B}{T}\right) - 1 \right)$$
$$F(T) \simeq \int dm \rho(m) \left(\frac{m}{T}\right)^2 K_2\left(\frac{m}{T}\right)$$

The Bielefeld Strategy

$$\frac{\Delta p(T, \mu_q)}{T^4} \simeq \sum_{n=1}^{n=3} c_{2n}(T) \left(\frac{\mu_q}{T}\right)^{2n} .$$

up to $O(\mu_q^6)$ order.



F. Karsch, K. Redlich and A. Tawfik (2003)

Hadron Resonance Gas: a simple strategy:

(D'Elia, MpL, 2002, 2004)

Observables are periodic and continuous for imaginary chemical potential. (Roberge, Weiss, 1986)

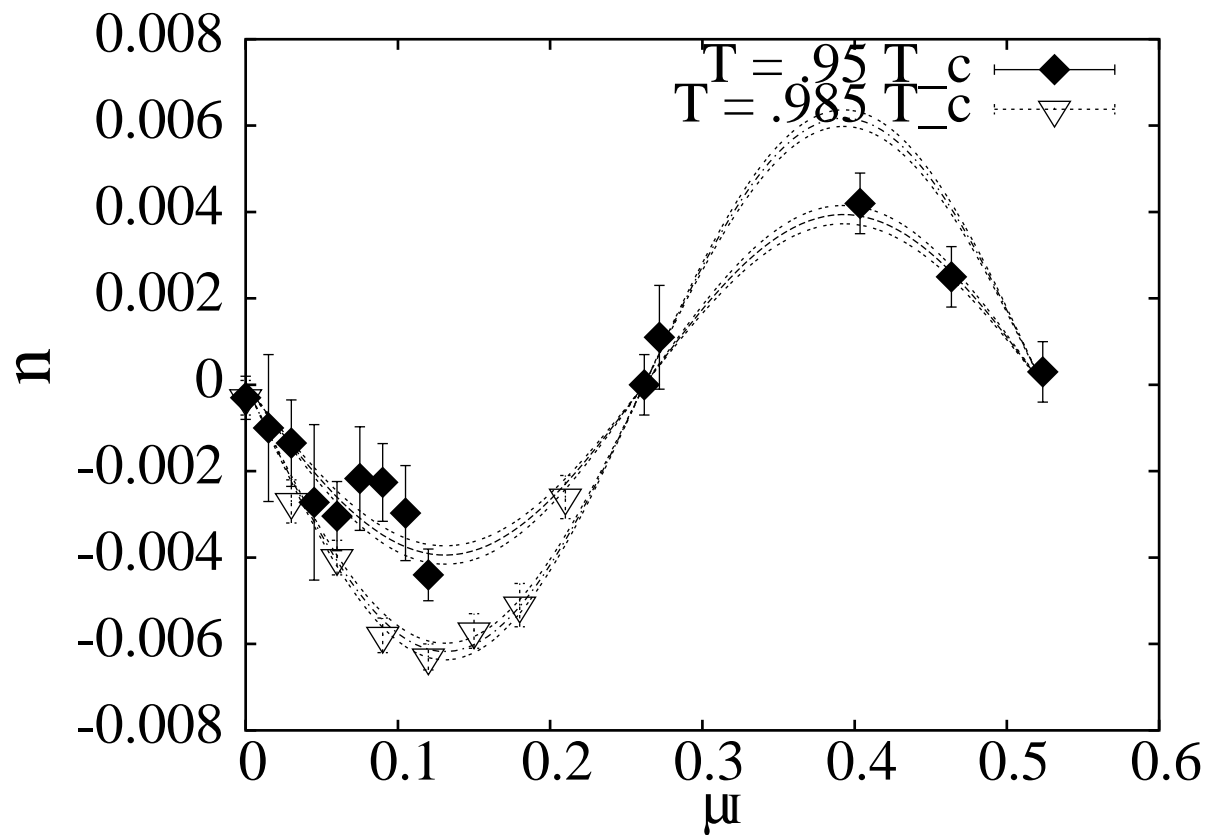
$$O_e = ae_F + \sum be_F \cos(N_c N_t \mu)$$

$$O_o = ao_F + \sum bo_F \sin(N_c N_t \mu)$$

When HRG holds true, one term in the Fourier series should suffice. ($\sinh(x) \rightarrow \sin(x)$)

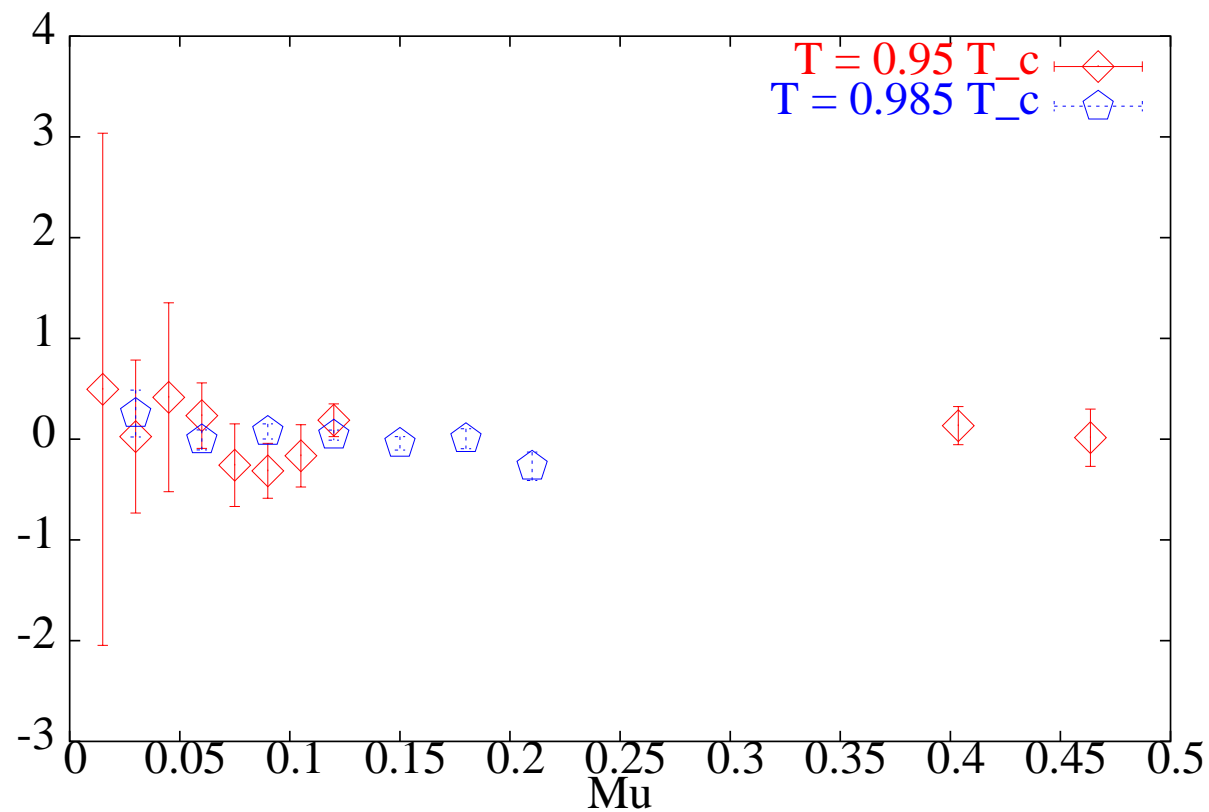
$$n(\mu) = \frac{\partial P(\mu)}{\partial \mu} = K \sin(N_c N_t \mu)$$

HRG accurate up to $T \simeq .985T_c$



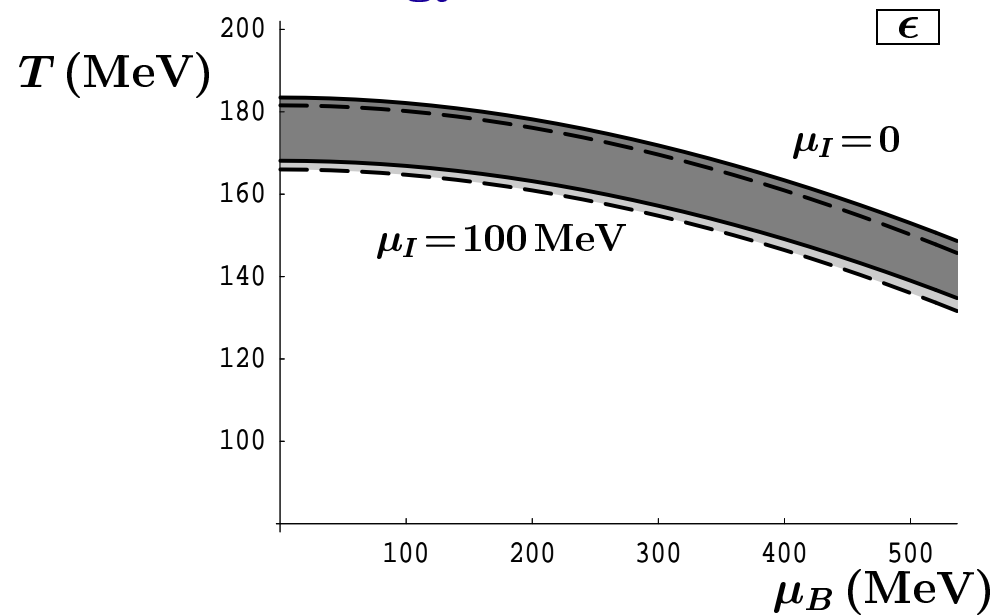
(No) Mismatch wrt HRG up to $T \simeq 0.985T_c$: direct check in an 'effective mass analysis' style:

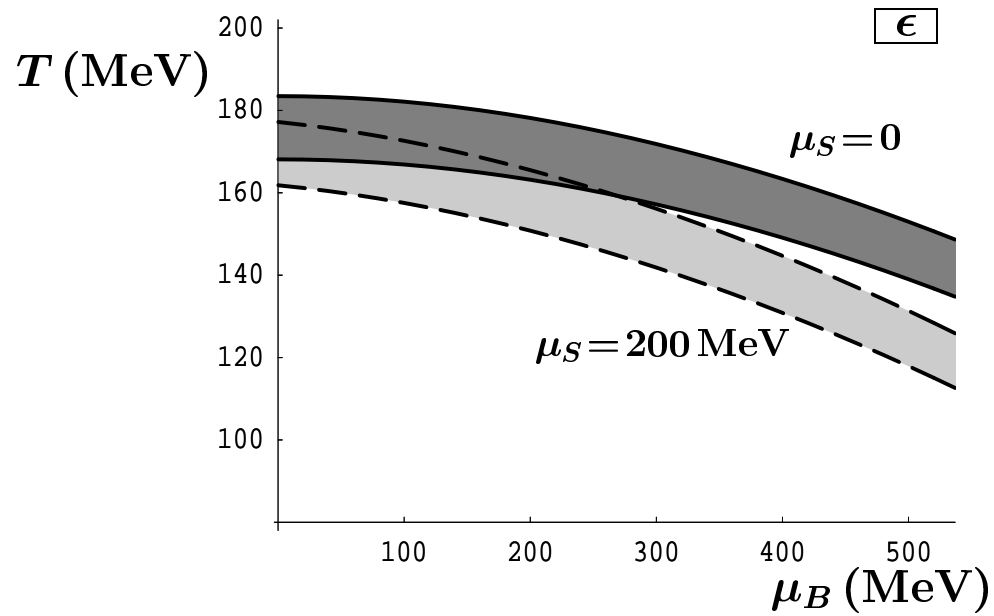
$$\text{Mismatch} = n(\mu) / \sin(N_c N_t \mu) - k$$



The Critical Line from HRG

Kogut and Toublan (2004) use the hadron resonance gas model with a fixed energy criterium to draw the phase diagram:

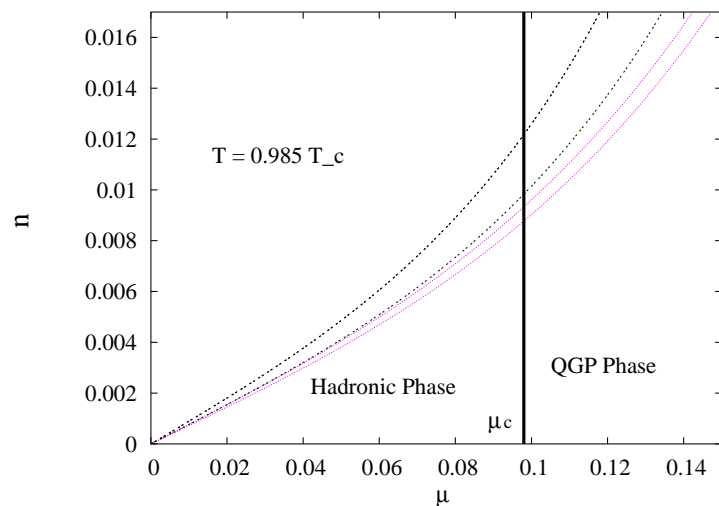




The critical temperature as a function of μ_B is determined by lines of constant energy density: $\epsilon \simeq 0.5 - 1.0 \text{ GeV}/\text{fm}^3$. .

Critical density from the lattice

D'Elia, MpL 2004



$$n(i\mu) = a_1 \sin(i\mu N_c N_T) + a_2 \sin(i2\mu N_c N_T)$$

Analytic continuation **up to** $\mu = \mu_c(T)$:

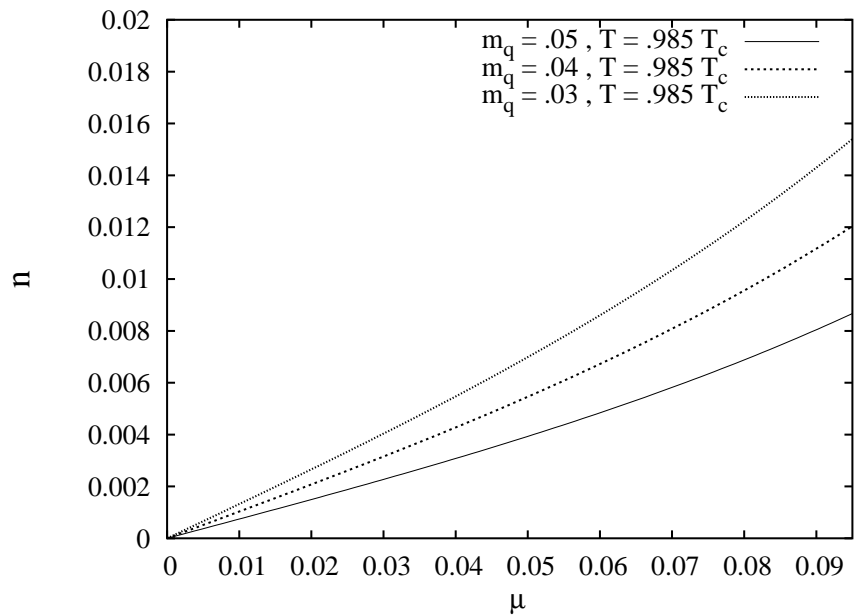
$$n(\mu) = a_1 \sinh(\mu N_c N_t) + a_2 \sinh(i2\mu N_c N_T)$$

Critical density at $T = .985 T_c$ $n_c(\mu_c)/T^3 \simeq 0.5$

Mass dependence of the Critical Density is Sizeable

From **derivatives**: (Maxwell Relations)

$$\partial \langle \bar{\psi} \psi \rangle / \partial \mu = \partial n(\mu) / \partial m$$



$$\frac{\Delta n(\mu, m_q)}{n(\mu, m_q)} \simeq 4.03 \Delta m_q / T$$

Summary I

Caveat: Lattice simulations still need being tuned towards physical values of the quark masses, and the continuum limit

Summary II : Results

★ **Critical line:** slope nicely determined, endpoint still has to settle down.

★ **Revenge of Nuclear Physics !:**

The hadronic phase easier than expected, well described by a simple gas of resonances up to $T \simeq 0.98T_c$:

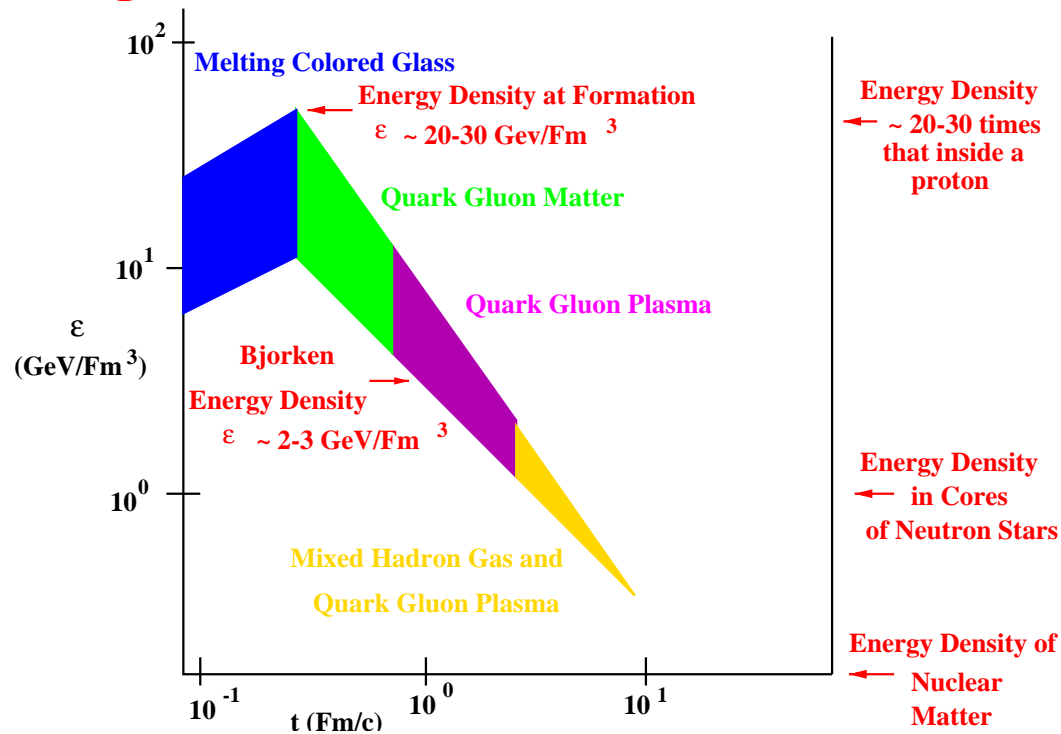
★ Region above T_c richer than expected

Strongly Interactive Quark Gluon Plasma

1. Thermodynamics highly nonperturbative.
2. Persistence of bound states
3. Influence of the critical line at negative μ_B^2

Summary III

Main challenge : Link the Static Properties measured on the Lattice with the Real Time evolution during the Collision



Picture from Blaizot, Iancu 2004