

# Rare hadronic B decays

Lluïsa-Maria Mir

Lawrence Berkeley National Laboratory

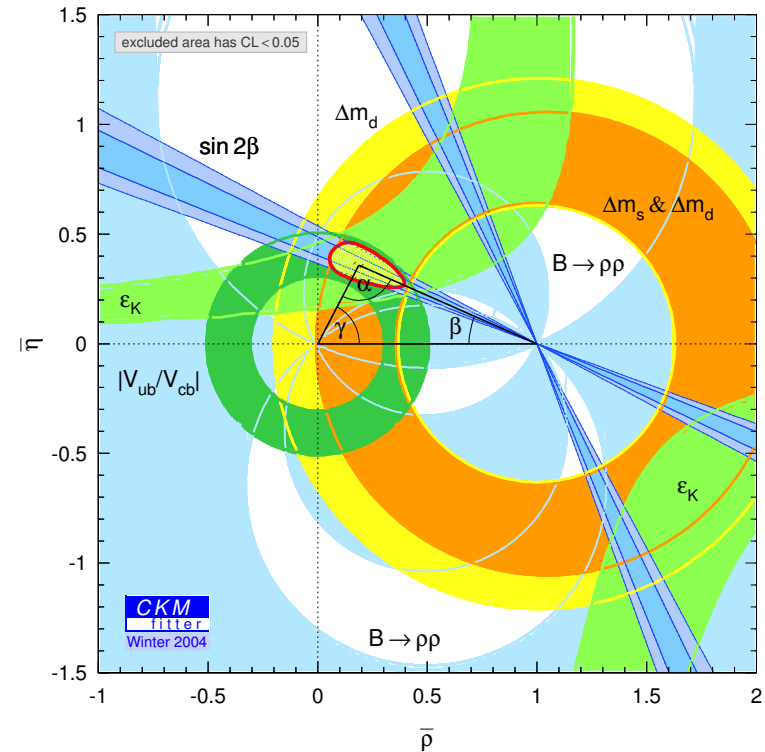


*BABAR* Collaboration

- Introduction
- Analysis method
- Charmless hadronic **B** decays
- Decays covered in the talk
  - $B^0$  decays to two isoscalars
  - $B \rightarrow KKK$
  - $B \rightarrow \phi K^*$
- Summary

# Introduction

- Good agreement between theory (**Standard Model**) and experimental results up to now
- Look for deviations from S.M. in processes with small rates:
  - **CKM**-suppressed decays
  - Penguin-loop dominated decays
- What to do? Measure
  - Rates, kinematical distributions
  - Time dependent **CP**
  - Time integrated (direct) **CP**
- Disagreements  $\left\{ \begin{array}{l} \text{– Improved theoretical calculations} \\ \text{– New Physics} \end{array} \right.$



# Analysis method

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- For fully reconstructed events ( $e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ ) use  $E_{\text{beam}}$  to constrain **mass** and **energy** of the reconstructed **B**

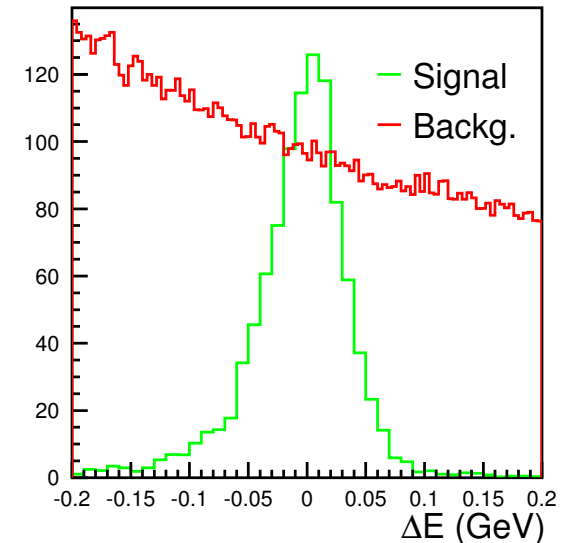
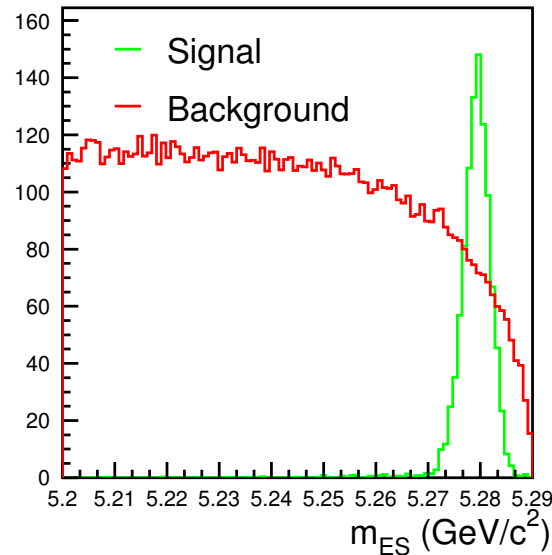
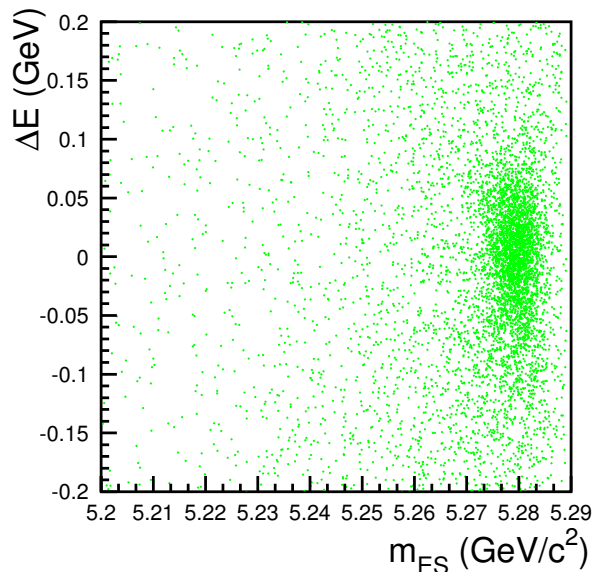
For signal

$$\Delta E = E_B^* - E_{\text{beam}}^*$$

$$= 0$$

$$m_{\text{ES}} = \sqrt{E_{\text{beam}}^{*2} - |\vec{p}_B|^2}$$

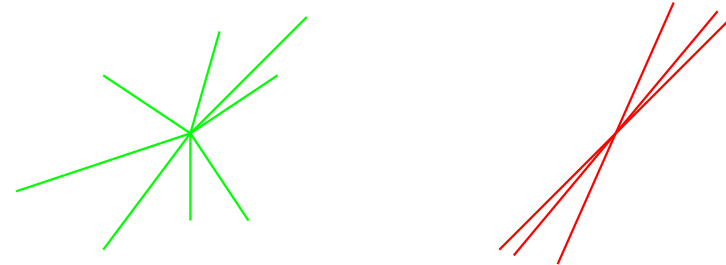
$$= m_B$$



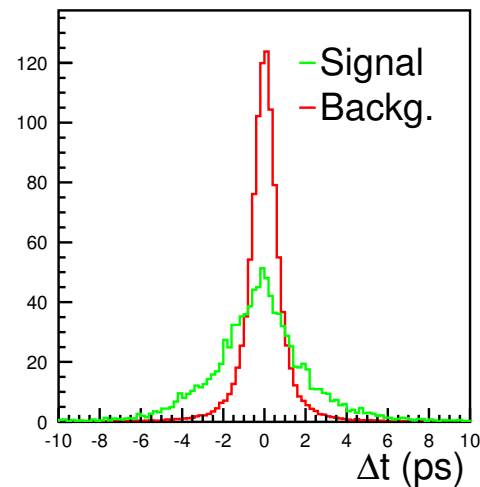
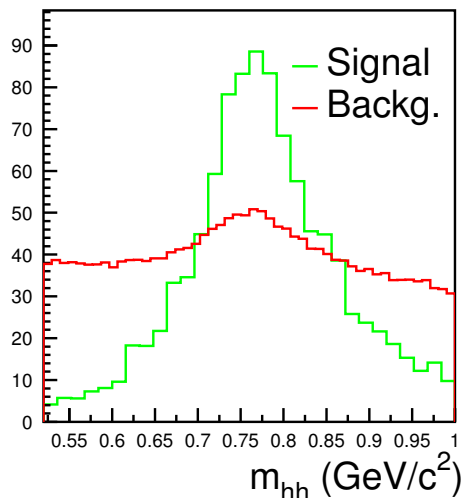
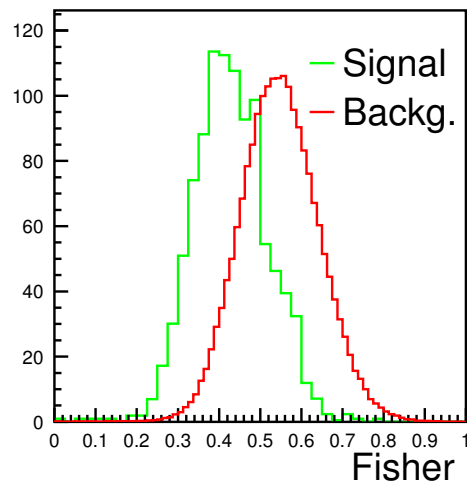
# Analysis method

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- Event shape:
  - **Signal:**  $\Upsilon(4S) \rightarrow B\bar{B}$  almost at rest
  - **Background:** “jetty”
  - Use Fisher, Neural Net



- Resonance masses, decay angles, etc.
- Time-dependent measurements: B-flavour,  $\Delta t = t_{B_1} - t_{B_2}$



- $B_d^0$  time-dependent asymmetry:

$$f_{\pm}(\Delta t) = \frac{\exp \frac{-|\Delta t|}{\tau_{B^0}}}{4 \tau_{B^0}} [1 \pm S \sin(\Delta m_d \Delta t) \mp C \cos(\Delta m_d \Delta t)]$$

CPV in interference  
mixing / no-mixing

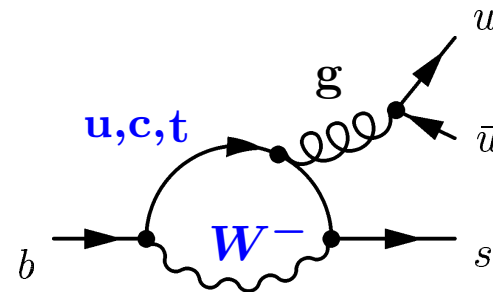
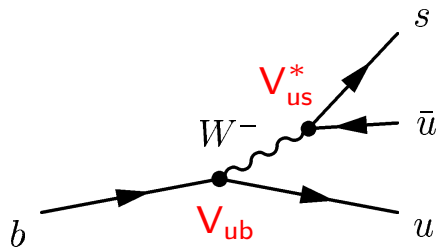
CPV in decay

- $S$  depends on CP-content and quark-level amplitudes of final state
- $C = -\mathcal{A}_{CP} = 0$  (SM)
- Likelihood fit with  $m_{ES}$ ,  $\Delta E$ ,  $\mathcal{F}$ , mass and  $\cos \theta$  of resonances PDFs
- Add  $\Delta t$  and tagging for time-dependent measurements
- Likelihood fit with signal, continuum, BB background categories

# Rare hadronic B decays

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- CKM suppressed **tree** decays and significant **penguin** contributions



- Decays **rare** but **abundant!**
  - Scalar-Pseudoscalar ( $f_0, a_0$ ) ( $\pi, K$ )
  - Pseudoscalar-Pseudoscalar ( $\pi, K$ ) ( $\pi, K$ )
  - Isoscalar ( $\eta, \eta', \omega, \phi$ ) ( $\eta, \eta', \omega, \phi$ )
  - Pseudoscalar-Vector ( $\pi, K, \eta, \eta'$ ) ( $\phi, \rho, \omega, K^*$ )
  - Three-body (Combinations of  $\pi$  and  $K$ )
  - Vector-Vector ( $\rho\rho, \rho K^*, \phi K^*$ )

# Decay modes covered in this talk

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- $B^0$  decays to two isoscalars
  - Bound on the “tree pollution” on the  $B \rightarrow \eta' K_S^0$  decay
- CP-violation in  $B \rightarrow KKK$ 
  - Disagreement in  $\sin 2\beta$  between  $b \rightarrow s$  penguin and charmonium modes?
- Full angular analysis in  $B \rightarrow \phi K^*$ 
  - A window to new physics?

# $B^0 \rightarrow$ two isoscalars branching fractions

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- Measure  $(\eta, \eta', \omega, \phi)$   $(\eta, \eta', \omega, \phi)$  combinations except  $\omega\omega, \omega\phi$
- Predictions  $\left\{ \begin{array}{l} - \text{Flavour SU(3)} \\ - \text{Factorization and specific } B \rightarrow \text{light-meson form-factors} \\ - \text{pQCD} \end{array} \right.$
- Precise experimental measurements to test accuracy of predictions
- Time evolution of  $B^0 \rightarrow \phi K_S^0$  and  $B^0 \rightarrow \eta' K_S^0$ :
  - $S = \sin 2\beta$  if decays dominated by one single penguin amplitude (SM)
  - $\Delta S = (S - \sin 2\beta) \leq 2|\xi_{\eta' K_S}|$
- Grossman-Ligeti-Nir-Quinn bound:

$$|\xi_{\eta' K_S}| < \left| \frac{V_{us}}{V_{ud}} \right| \left[ 0.59 \sqrt{\frac{\mathcal{B}(\eta' \pi^0)}{\mathcal{B}(\eta' K^0)}} + 0.33 \sqrt{\frac{\mathcal{B}(\eta \pi^0)}{\mathcal{B}(\eta' K^0)}} + 0.14 \sqrt{\frac{\mathcal{B}(\pi^0 \pi^0)}{\mathcal{B}(\eta' K^0)}} + \right. \\ \left. 0.53 \sqrt{\frac{\mathcal{B}(\eta' \eta')}{\mathcal{B}(\eta' K^0)}} + 0.38 \sqrt{\frac{\mathcal{B}(\eta \eta)}{\mathcal{B}(\eta' K^0)}} + 0.96 \sqrt{\frac{\mathcal{B}(\eta \eta')}{\mathcal{B}(\eta' K^0)}} \right]$$

# $B^0 \rightarrow$ two isoscalars branching fractions

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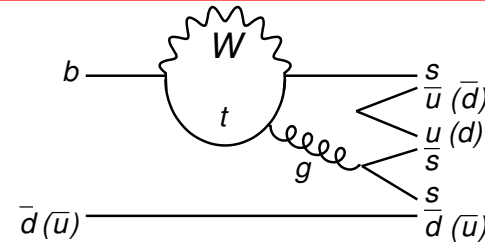
- Recall (BaBar)  $\left\{ \begin{array}{l} S_{\text{charmonium}} = 0.741 \pm 0.067 \pm 0.032 \text{ (82 fb}^{-1}\text{)} \\ S_{\eta'K_S} = 0.02 \pm 0.34 \pm 0.03 \text{ (82 fb}^{-1}\text{)} \\ S_{\phi K_S} = 0.47 \pm 0.34^{+0.08}_{-0.06} \text{ (108 fb}^{-1}\text{)} \end{array} \right.$
- Results with 82 M  $B\bar{B}$ :

Mode	$S(\sigma)$	$\mathcal{B}(10^{-6})$	UL ( $10^{-6}$ )	UL ( $10^{-6}$ ) (CLEO)
$\eta\eta$	0.0	$-0.9^{+1.6}_{-1.4} \pm 0.7$	2.8	18
$\eta\eta'$	0.3	$0.6^{+2.1}_{-1.7} \pm 1.1$	4.6	27
$\eta'\eta'$	0.4	$1.7^{+4.8}_{-3.7} \pm 0.6$	10	47
$\eta\omega$	<b>4.3</b>	$4.0^{+1.3}_{-1.2} \pm 0.4$	6.2	12
$\eta'\omega$	0.0	$-0.2^{+1.3}_{-0.9} \pm 0.4$	2.8	60
$\eta\phi$	0.0	$-1.4^{+0.7}_{-0.4} \pm 0.2$	1.0	9
$\eta'\phi$	0.8	$1.5^{+1.8}_{-1.5} \pm 0.4$	4.5	31
$\phi\phi$	0.3	$0.3^{+0.7}_{-0.4} \pm 0.1$	1.5	12

BaBar, submitted to Phys. Rev. Lett. hep-ex/0403046

- GLNQ bound on  $|\xi_{\eta'K_S}|$  improved from 0.36 to 0.17

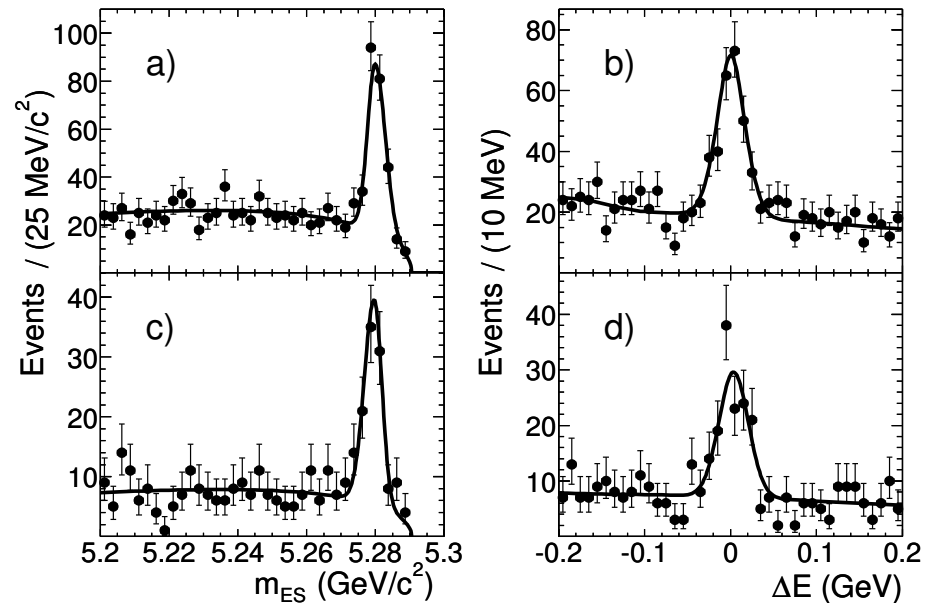
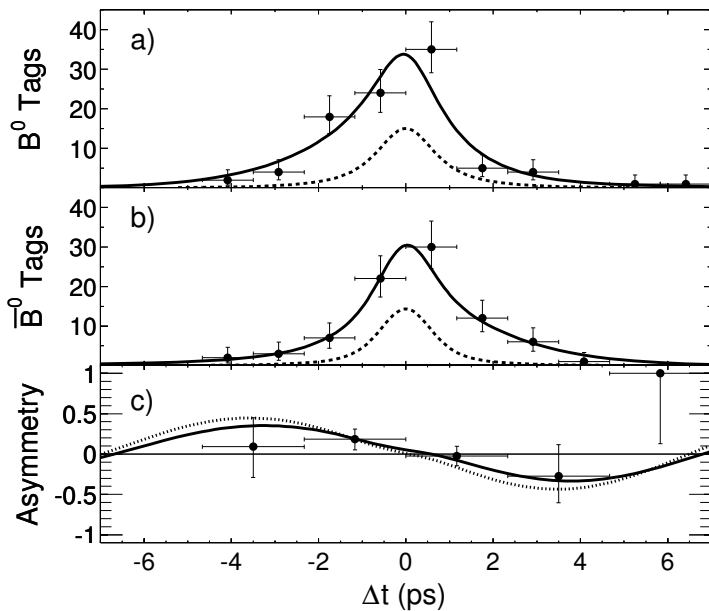
- Dominated by  $b \rightarrow s\bar{s}s$  gluonic penguin



- 2.7  $\sigma$  discrepancy BaBar/Belle in  $S_{\phi K_S^0}$
- $B^0 \rightarrow K^+K^-K_S^0$  integrated over all phase-space:
  - Pro: More precise than  $B^0 \rightarrow \phi K_S^0$  (more statistics)
  - Con: CP-content of final state unknown *a priori*

- Measure
  - $\mathcal{B}(B^0 \rightarrow K^+K^-K_S^0)$  and  $\mathcal{B}(B^+ \rightarrow K^+K_S^0K_S^0)$
  - $B^+ \rightarrow K^+K_S^0K_S^0$  charge asymmetry
  - CP-content of  $B^0 \rightarrow K^+K^-K_S^0$
  - $B^0 \rightarrow K^+K^-K_S^0$  time-dependent asymmetry

- Get  $\mathcal{B}$  with a likelihood fit using  $m_{ES}$ ,  $\Delta E$  and  $\mathcal{F}$
- $B^+ \rightarrow K^+K_S^0K_S^0$  charge asymmetry:  $\mathcal{A}_{CP} = \frac{\Gamma_{K^-K_S^0K_S^0} - \Gamma_{K^+K_S^0K_S^0}}{\Gamma_{K^-K_S^0K_S^0} + \Gamma_{K^+K_S^0K_S^0}}$
- $B^0 \rightarrow K^+K^-K_S^0$  CP-content:  $f_{\text{even}} = \frac{N_{CP}}{N} = 2 \frac{\Gamma(B^+ \rightarrow K^+K_S^0K_S^0)}{\Gamma(B^0 \rightarrow K^+K^-K_S^0)}$
- Use  $\Delta t$  for CP(t)-asymmetry fit ↖ from isospin symmetry



- Results with 124 M  $B\bar{B}$ :

CP: This sample has  $B^0 \rightarrow \phi K_S^0$  removed:  $|m_{K^+K^-} - m_\phi| > 15 \text{ MeV}/c^2$

	$(K^+K^-K^0)^{CP}$	$(K^+K^-K^0)^{all}$	$K^+K_S^0K_S^0$
$\mathcal{B} (10^{-6})$	$20.2 \pm 1.9 \pm 1.4$	$23.8 \pm 2.0 \pm 1.6$	$10.7 \pm 1.2 \pm 1.0$
$f_{even}$	$0.98 \pm 0.15 \pm 0.04$	$0.83 \pm 0.12 \pm 0.03$	-
$S$	$-0.56 \pm 0.25 \pm 0.04$	-	$-0.16 \pm 0.35$
$C$	$-0.10 \pm 0.19 \pm 0.10$	-	$-0.08 \pm 0.22$
$A_{CP}$	-	-	$-0.04 \pm 0.11 \pm 0.02$

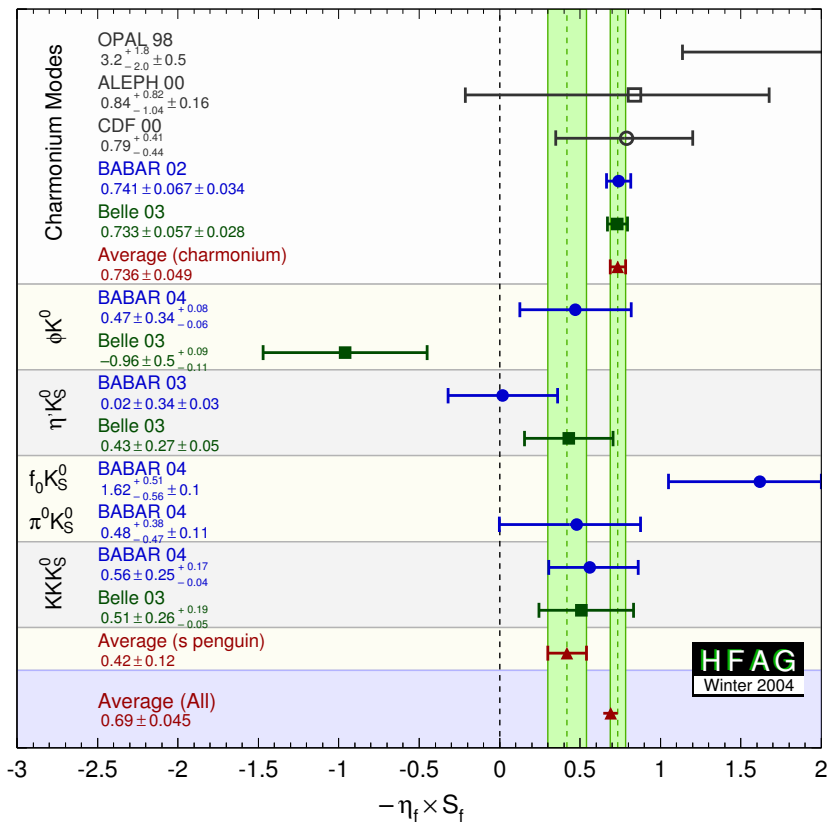
- $C = 0 \rightarrow S = -\sin 2\beta = 0.57 \pm 0.26 \pm 0.04_{-0}^{+0.17}$

CP-content

BABAR, *sub. to Phys. Rev. Lett. hep-ex/0406005*

# B and CPV in $B^0 \rightarrow K^+K^-K_S^0$ and $B^+ \rightarrow K^+K_S^0K_S^0$

$-\eta_f \times S_f$	$\phi K^0$	$KKK_S^0$
BABAR	$0.47 \pm 0.34^{+0.08}_{-0.06}$	$0.56 \pm 0.25 \pm 0.04^{+0.17}_{-0.00}$
Belle	$-0.96 \pm 0.50^{+0.09}_{-0.11}$	$0.51 \pm 0.26 \pm 0.05^{+0.18}_{-0.00}$
Average	$0.02 \pm 0.29$ (0.28 stat only)	$0.54 \pm 0.18^{+0.17}_{-0.00}$ (0.18 stat only)

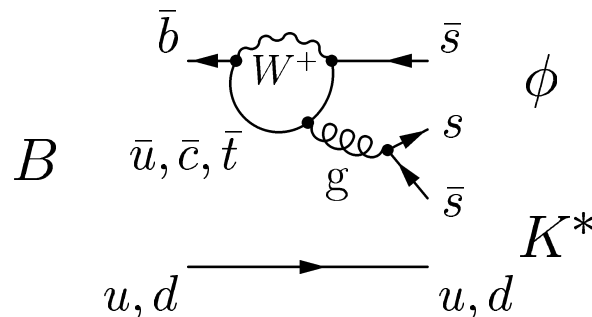


Disagreement between  $b \rightarrow s$  penguin dominated and charmonium modes of  $\sim 2.4 \sigma$

# Full angular analysis $B \rightarrow \phi K^*$

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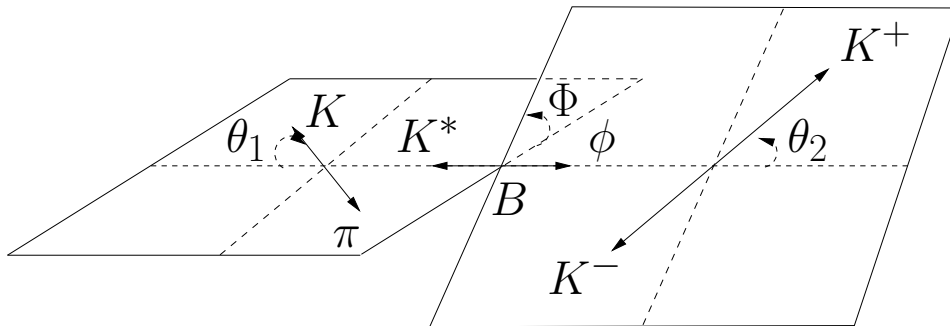
- Decays to two **vector** mesons reveal fundamental dynamics
  - **Successes**:  $\sin 2\alpha$  from  $B \rightarrow \rho\rho$
  - **Surprises**: Longitudinal **polarization** in  $B \rightarrow \phi K^*$  smaller than **SM** prediction
- Hint of **new** physics?
  - $B \rightarrow \phi K^*$  is a pure penguin loop



- Perform **full angular analysis**

# Full angular analysis $B \rightarrow \phi K^*$

- Angular distribution of  $B \rightarrow VV$  unknown *a priori*



$$\frac{1}{\Gamma} \frac{d^3\Gamma}{d \cos \theta_1 d \cos \theta_2 d\Phi} = \frac{9}{8\pi} \frac{1}{|A_0|^2 + |A_{+1}|^2 + |A_{-1}|^2} \times$$

$$\left\{ \begin{aligned} & \frac{1}{4} \sin^2 \theta_1 \sin^2 \theta_2 (|A_{+1}|^2 + |A_{-1}|^2) + \cos^2 \theta_1 \cos^2 \theta_2 |A_0|^2 + \\ & \frac{1}{2} \sin^2 \theta_1 \sin^2 \theta_2 [\cos 2\Phi \operatorname{Re}(A_{+1}A_{-1}^*) - \sin 2\Phi \operatorname{Im}(A_{+1}A_{-1}^*)] - \\ & \frac{1}{4} \sin 2\theta_1 \sin 2\theta_2 [\cos \Phi \operatorname{Re}(A_{+1}A_0^* + A_{-1}A_0^*) - \sin \Phi \operatorname{Im}(A_{+1}A_0^* - A_{-1}A_0^*)] \end{aligned} \right\}$$

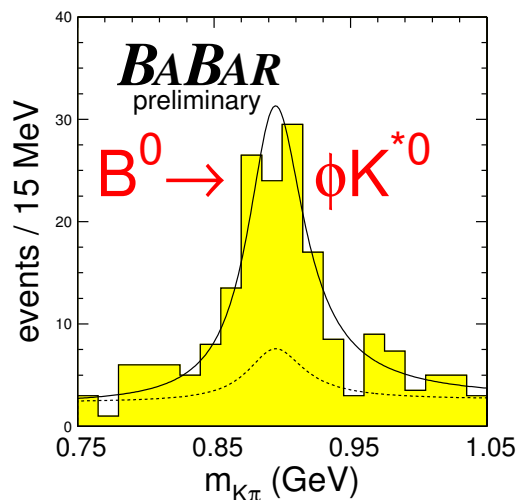
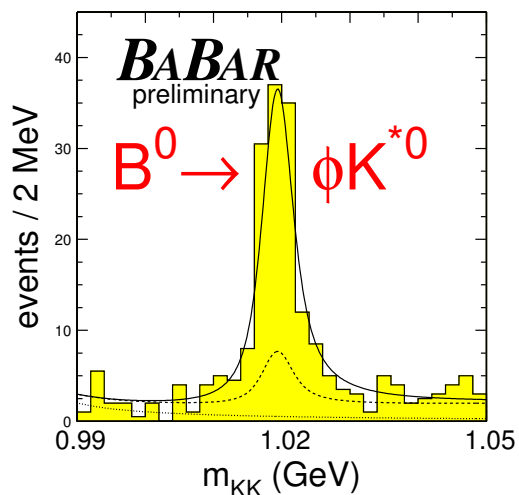
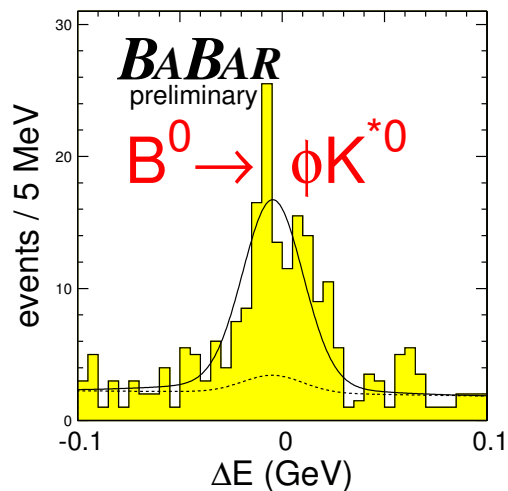
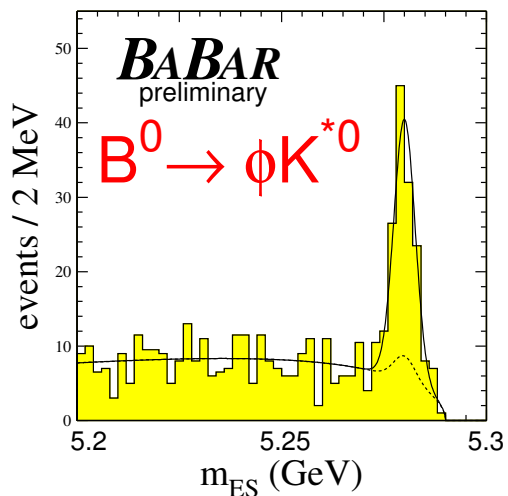
$$A_{\parallel} = \frac{A_{+1} + A_{-1}}{\sqrt{2}}, \text{ CP-even}$$

$$A_{\perp} = \frac{A_{+1} - A_{-1}}{\sqrt{2}}, \text{ CP-odd}$$

# Full angular analysis $B \rightarrow \phi K^*$

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- With 124 million  $B\bar{B}$ :  $n_{\text{sig}} = 129 \pm 14 \pm 9$



# Full angular analysis $B \rightarrow \phi K^*$

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$n_{\text{sig}}$	$129 \pm 14 \pm 9$
$f_{\parallel}$	$0.52 \pm 0.07 \pm 0.02$
$f_{\perp}$	$0.27 \pm 0.07 \pm 0.02$
$\phi_{\parallel}$	$2.63^{+0.24}_{-0.23} \pm 0.04$
$\phi_{\perp}$	$2.71^{+0.22}_{-0.24} \pm 0.03$
$\mathcal{A}_{\text{CP}}$	$-0.12 \pm 0.10 \pm 0.03$
$\mathcal{A}_{\text{CP}}^0$	$-0.02 \pm 0.12 \pm 0.01$
$\mathcal{A}_{\text{CP}}^{\perp}$	$-0.10^{+0.25}_{-0.27} \pm 0.04$
$\Delta\phi_{\parallel}$	$0.38^{+0.23}_{-0.24} \pm 0.04$
$\Delta\phi_{\perp}$	$0.30^{+0.24}_{-0.22} \pm 0.03$
$\mathcal{A}_{\text{T}}^{\parallel}$	$+0.02 \pm 0.05 \pm 0.01$
$\mathcal{A}_{\text{T}}^0$	$+0.11 \pm 0.07 \pm 0.01$

$$\mathcal{A}_{\text{T}} = (\mathbf{q}_1 - \mathbf{q}_2) \cdot \mathbf{p}_1 \times \mathbf{p}_2$$

$$f_{\parallel} = 1 \text{ up to } \mathcal{O}(1/M_{\text{B}}^2) \text{ M. Suzuki Phys. Rev. D } \mathbf{66} \text{ 054018 (2002)}$$

$n_{\text{sig}}$ : total number of events

$f_{\parallel} = \frac{|A_0|^2}{\sum_m |A_m|^2}$ : longitudinal fraction

$f_{\perp} = \frac{|A_{\perp}|^2}{\sum_m |A_m|^2}$ : transverse CP-odd fraction

$\phi_{\parallel} = \arg(A_{\parallel}) - \arg(A_0)$  (CP-even)

$\phi_{\perp} = \arg(A_{\perp}) - \arg(A_0)$ : (CP-odd)

$\mathcal{A}_{\text{CP}} = \frac{n_{\text{sig}}^+ - n_{\text{sig}}^-}{n_{\text{sig}}^+ + n_{\text{sig}}^-}$ : direct CP-asymmetry

$\mathcal{A}_{\text{CP}}^0 = \frac{f_{\parallel}^+ - f_{\parallel}^-}{f_{\parallel}^+ + f_{\parallel}^-}$ : longitudinal asymmetry

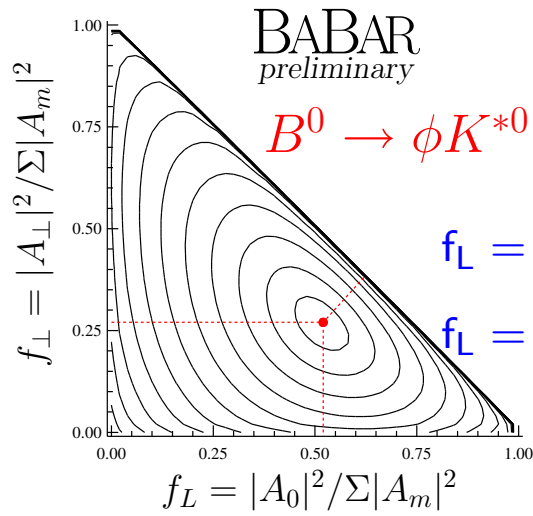
$\mathcal{A}_{\text{CP}}^{\perp} = \frac{f_{\perp}^+ - f_{\perp}^-}{f_{\perp}^+ + f_{\perp}^-}$  (CP-odd)

$\Delta\phi_{\parallel} = \frac{1}{2}(\phi_{\parallel}^+ - \phi_{\parallel}^-)$  (CP-even)

$\Delta\phi_{\perp} = \frac{1}{2}(\phi_{\perp}^+ - \phi_{\perp}^-)$  (CP-odd)

$\mathcal{A}_{\text{T}}^{\parallel,0} = \frac{1}{2} \left( \frac{\text{Im}(A_{\perp}^+ A_{\parallel,0}^{+*})}{\sum |A_m^+|^2} + \frac{\text{Im}(A_{\perp}^- A_{\parallel,0}^{-*})}{\sum |A_m^-|^2} \right)$

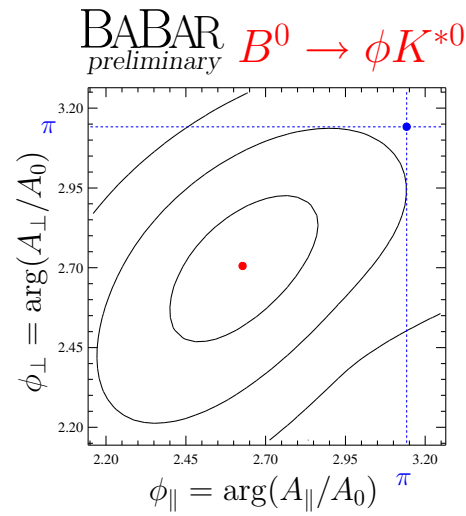
# Full angular analysis $B \rightarrow \phi K^*$



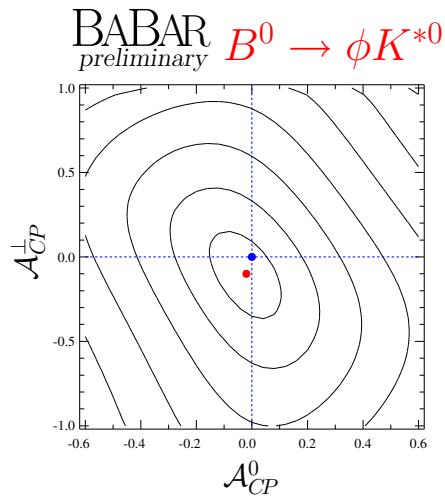
Puzzle:

$$f_L = 0.98 \text{ (} B \rightarrow \rho\rho \text{)}$$

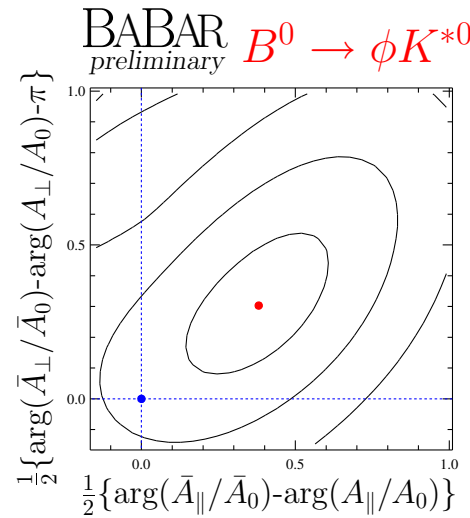
$$f_L = 0.50 \text{ (} B \rightarrow \phi K^* \text{)}$$



Weak evidence for FSI ( $2.3 \sigma$ )



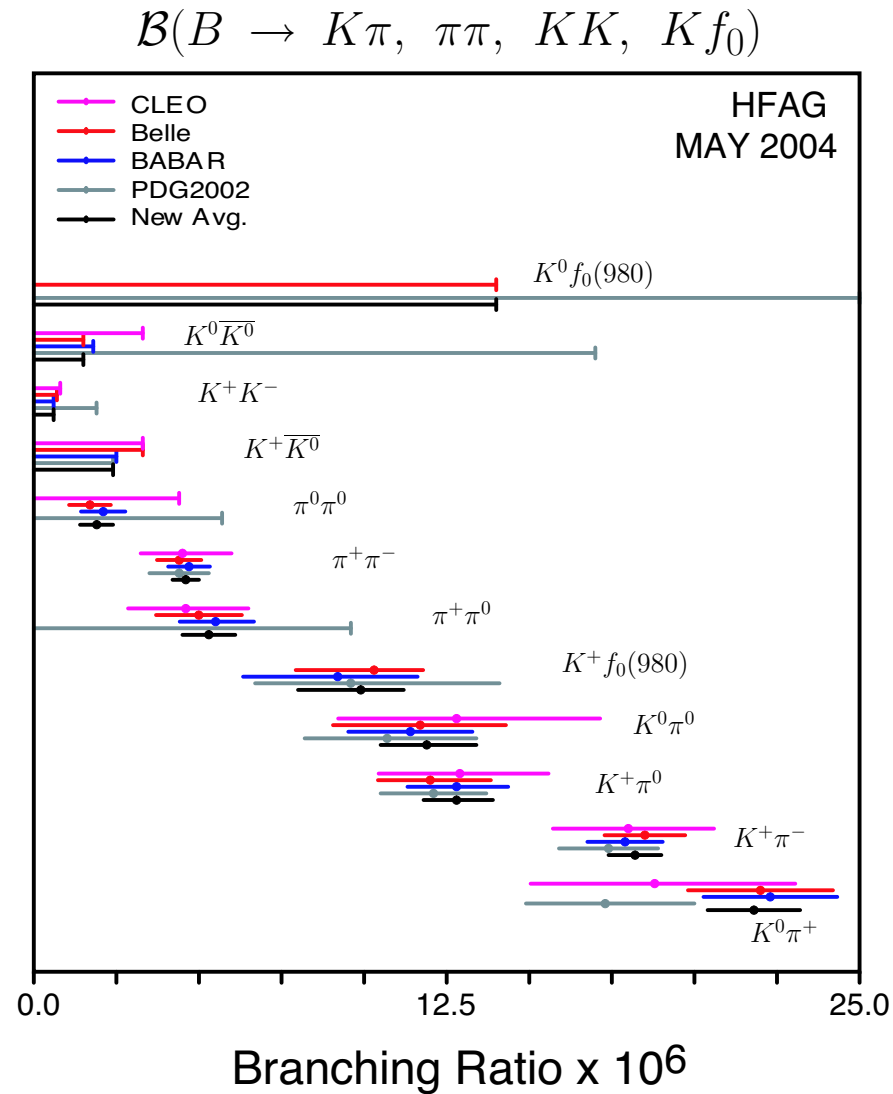
No significant direct CP violation



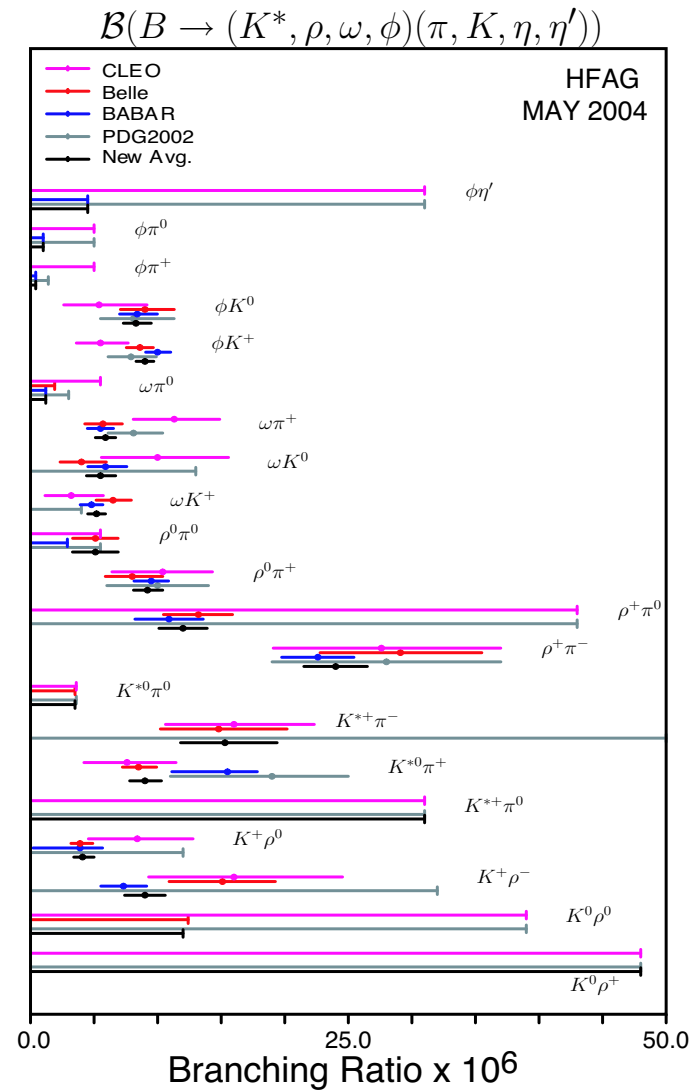
Triple-product asymmetry ( $1.7 \sigma$ )

- B-factories provide huge amount of B mesons
  - Many rare-decay first-time observations
  - B.R. measurements more precise
  - Limits on B.R. tightened
- Rare decays are a window for new physics
  - $f_L(\phi K^{*0}) = 0.52 \pm 0.07 \pm 0.02$  (S.M. predicts 1)
- No violation of SM found yet
  - Good agreement BABAR/Belle in  $S_{KKK}$
- More data to come

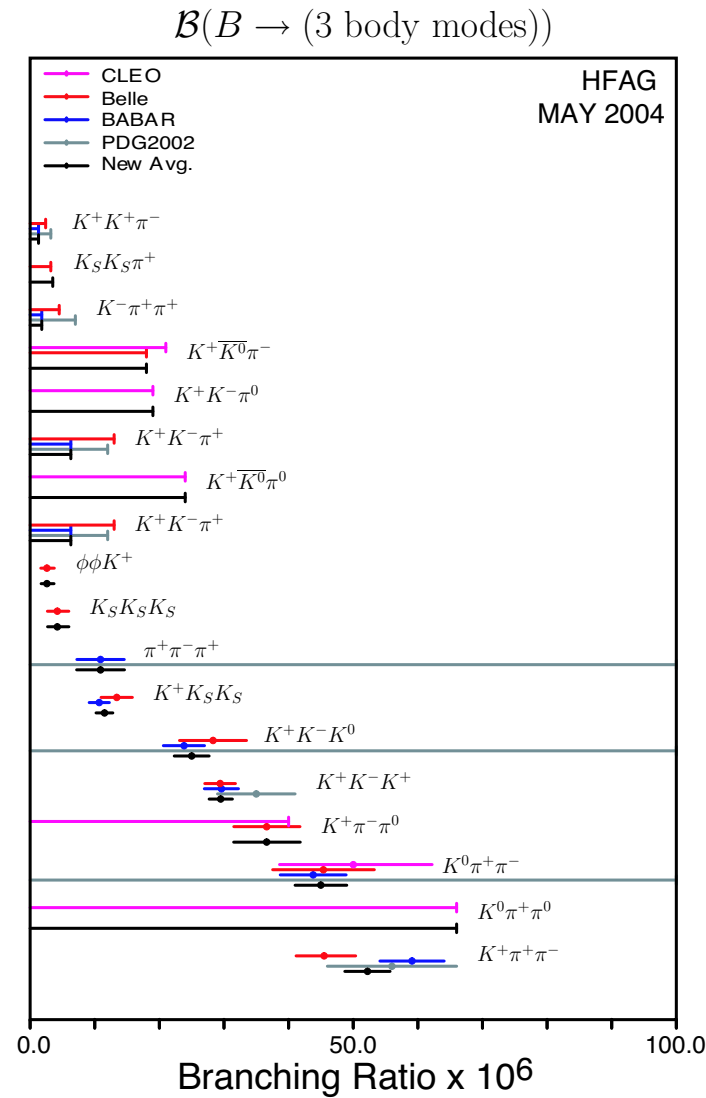
# Two-body involving pions and kaons



# B $\rightarrow$ PV



# Three-body decays



# B $\rightarrow$ VV

