

# Updated results from CMD-2

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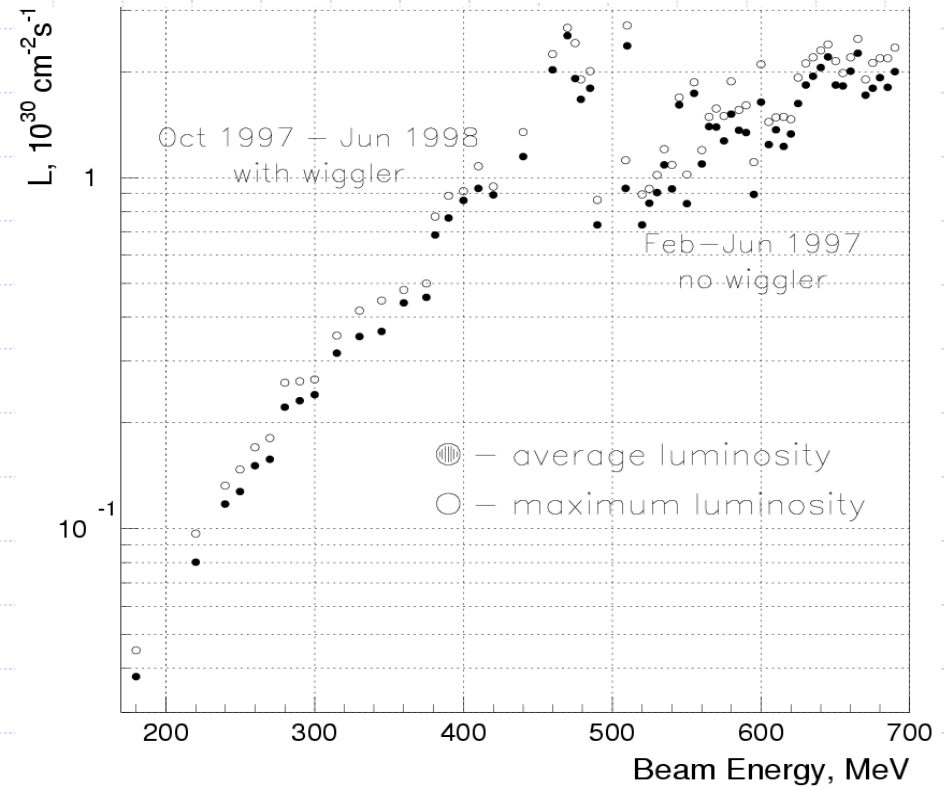
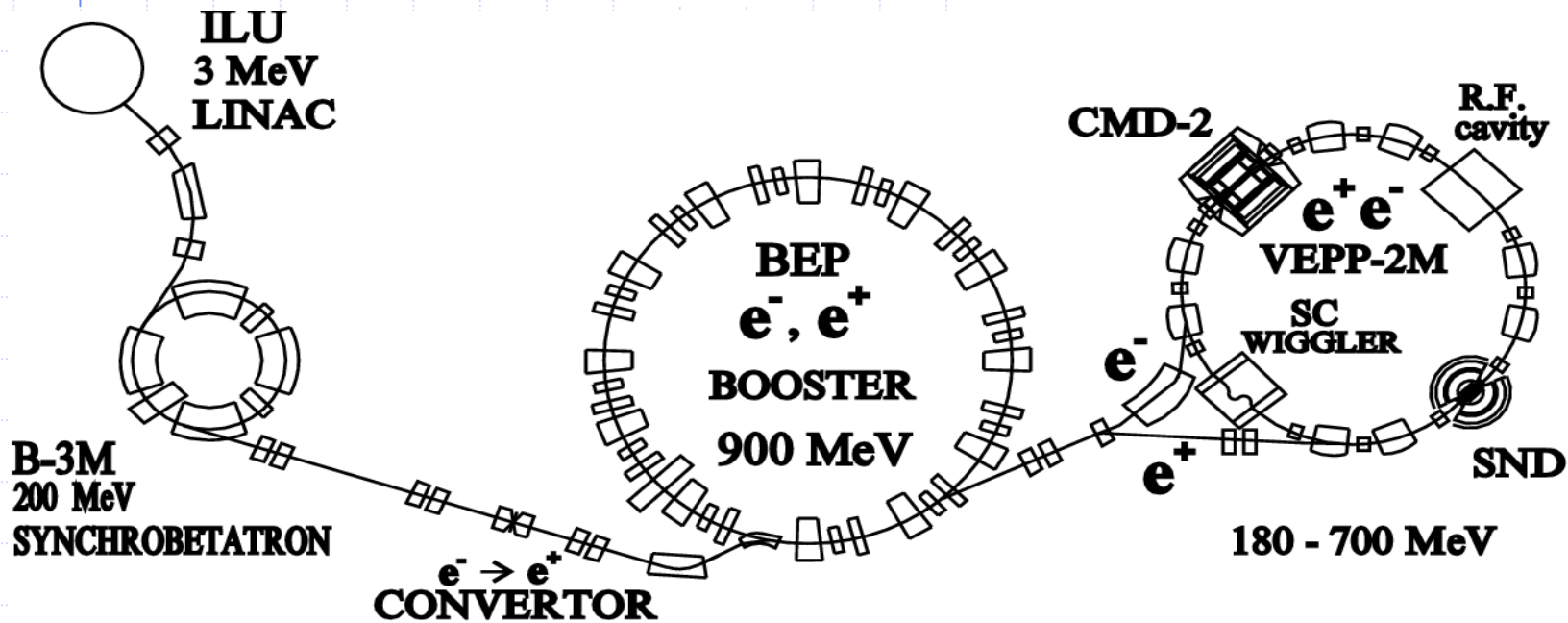
# Outline

- CMD-2 and SND detectors at VEPP-2M
- Calculations of cross sections  $e^+e^- \rightarrow e^+e^-(\gamma), \mu^+\mu^-(\gamma), \pi^+\pi^-(\gamma)$   
comparison with other programs
- “Dressed” and “bare” cross sections
- Updated results from CMD-2

# VEPP-2M collider

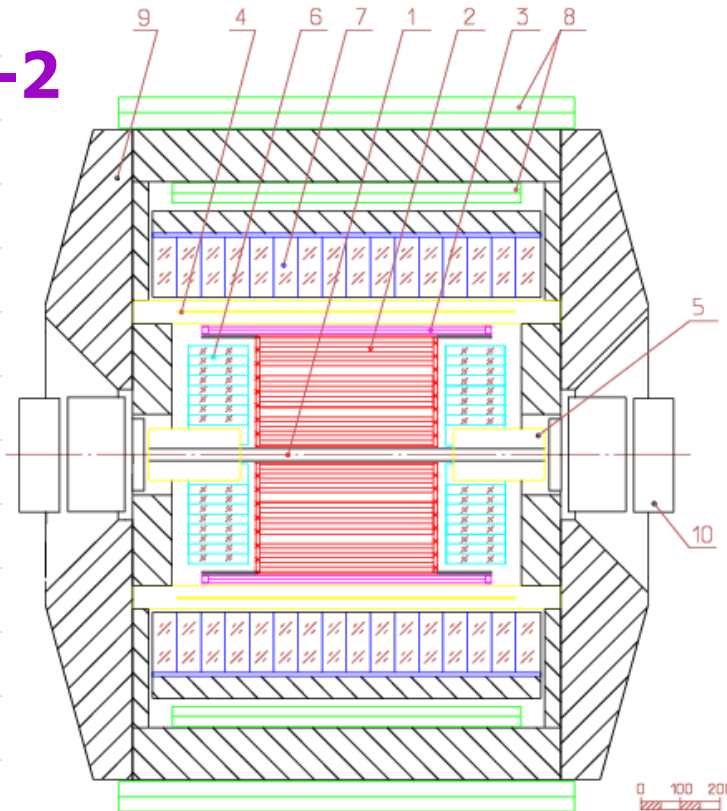
Operating 1974 - 2000

With  $L_{\text{peak}} \sim 3 \times 10^{30} \text{ cm}^{-2} \text{ s}^{-1}$   
VEPP-2M is a pre- $\phi$ -factory



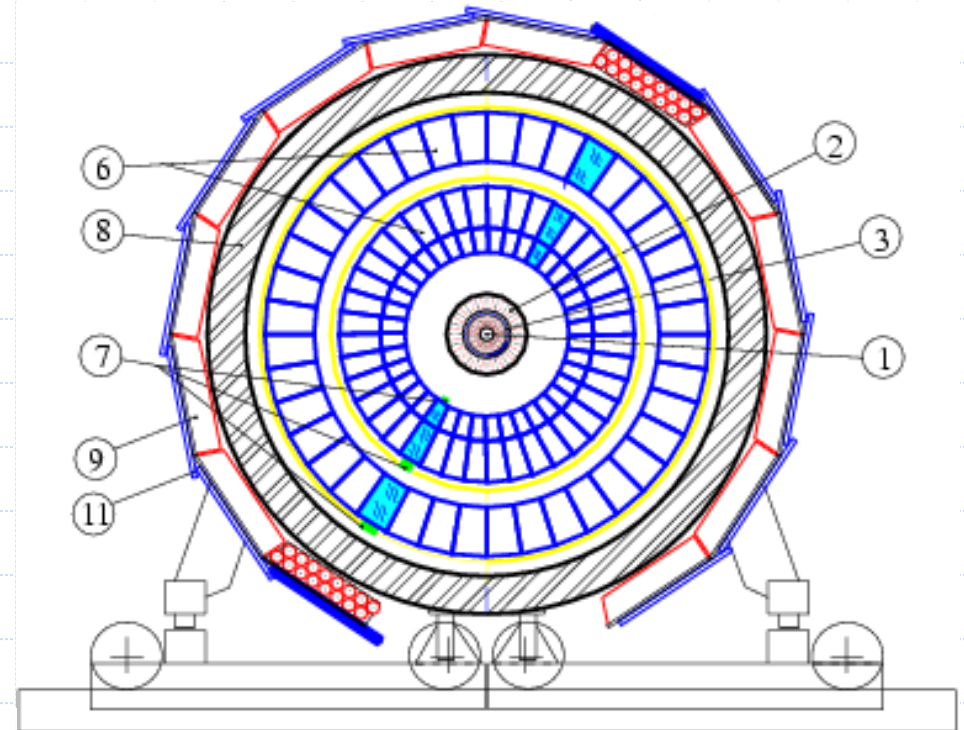
# Last generation of detectors at VEPP-2M

**CMD-2**



1 – vacuum chamber; 2 – drift chamber; 3 – Z-chamber; 4 – main solenoid; 5 – compensating solenoid; 6 – BGO calorimeter; 7 – CsI calorimeter; 8 – muon range system; 9 – yoke; 10 – quadrupoles

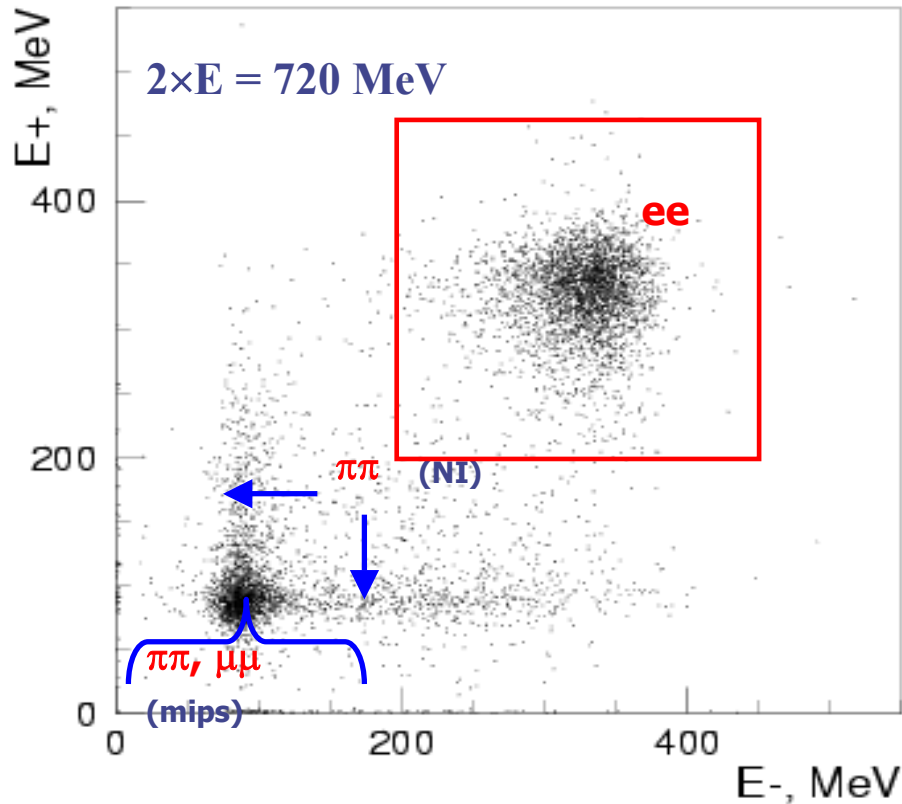
**SND**



1 – vacuum chamber; 2 – drift chambers; 3 – internal scintillating counter; 6 – NaI crystals; 7 – vacuum phototriodes; 8 – absorber; 9 – streamer tubes; 11 – scintillator plates;

# Luminosity measurement

$$L = \frac{N_{ee}}{\sigma(e^+e^- \rightarrow e^+e^-(\gamma))}$$

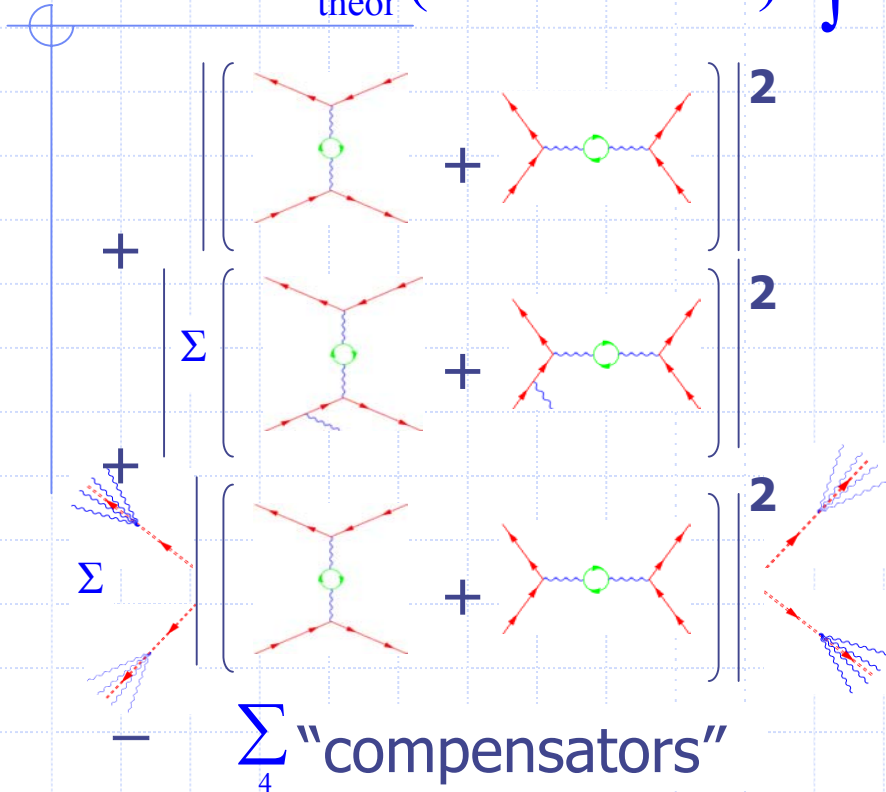


## Getting number of $N_{ee}$

- Select collinear events in tracking system
- Separate  $e^+e^-$  events by energy deposition in CsI calorimeter
  - Crude separation – number of events in red box
  - More precise separation – unbinned fit of energy distribution

# $e^+e^- \rightarrow e^+e^-$ cross section calculation

$$\sigma_{\text{theor}}^{\text{vis}}(e^+e^- \rightarrow e^+e^-) = \int \dots \int \frac{D(z_1) \dots D(z_4) \sigma(z_1, z_2, s)}{|1 - \Pi(z_1, z_2, s)|^2} dz_1 \dots dz_4$$



vacuum polarization by **leptons** and **hadrons** is included by each diagram

precise matrix element for one photon at large angle relatively to initial or final particle ( $\theta > \theta_0, E > \Delta E$ )

along initial or final particles ( $\theta < \theta_0$ )  
 "jets" described by

$D(z)$  – function giving the probability for electron to have an energy

$$E_e = z \times E_{\text{beam}}$$

E.A.Kuraev and V.S.Fadin,  
 Sov.Jorn.Nucl.Phys. 41(1985)466

where

$$\text{"compensator"} = \int_0^\pi \left( \frac{d\sigma}{d\Omega} \right)_\gamma d\Omega_\gamma - \int_0^{\theta_0} \left( \frac{d\sigma}{d\Omega} \right)_\gamma d\Omega_\gamma$$

all terms  $\left( \frac{\alpha}{\pi} \ln \frac{s}{m_e^2} \right)^{n_\gamma}$   
 are taken into account  
 in D functions

accuracy  
 estimation  
 $\sim 0.2\%$

is required to remove from  $D(z)$  the part of cross section caused by emission of one photon at large angles

A.B.Arbutov, E.A.Kuraev et al., JHEP 10 (1997)  
 Mod.Phys.Lett., A13 (1998) 2305

# $e^+e^- \rightarrow e^+e^-$ code comparison with BHWIDE

S.Jadach, W.Placzek,  
B.F.L.Ward hep-ph/9608412

In our selection criteria

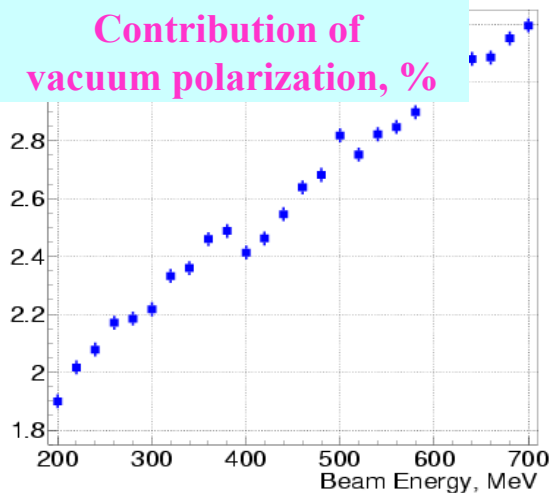
$$\Delta\theta < 0.25$$

$$\Delta\phi < 0.15$$

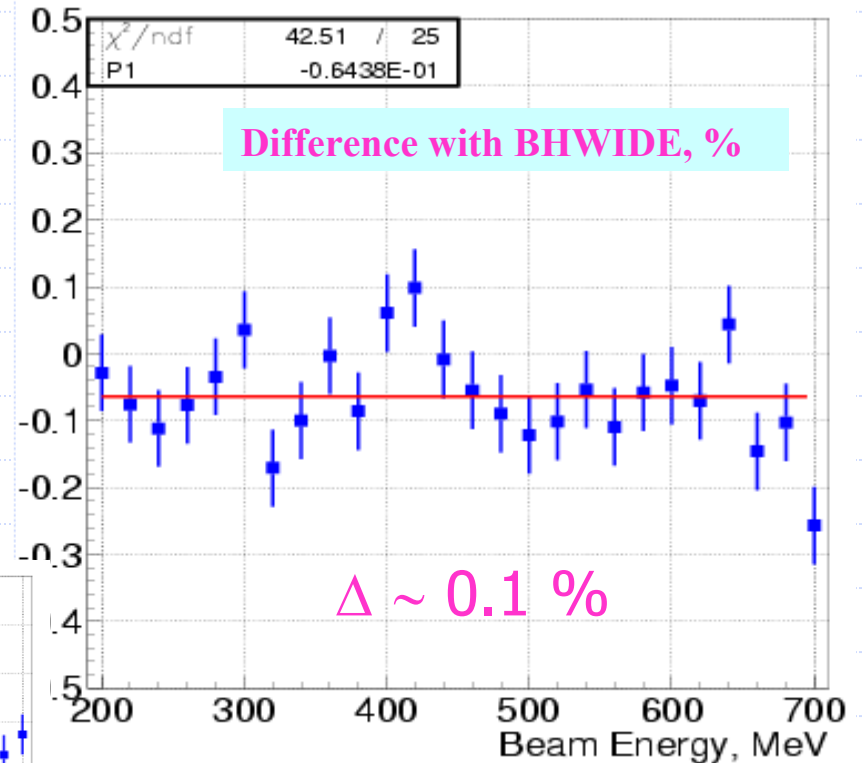
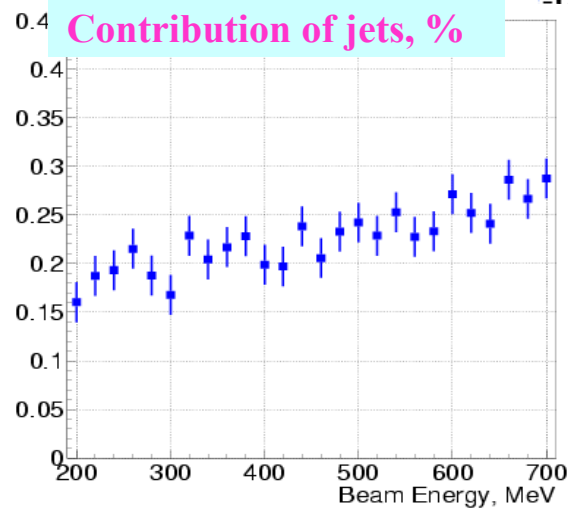
$$1.1 < \theta_{\text{final}} < \pi - 1.1$$

$$P_{\perp}^{\pm} > 90 \text{ MeV}/c$$

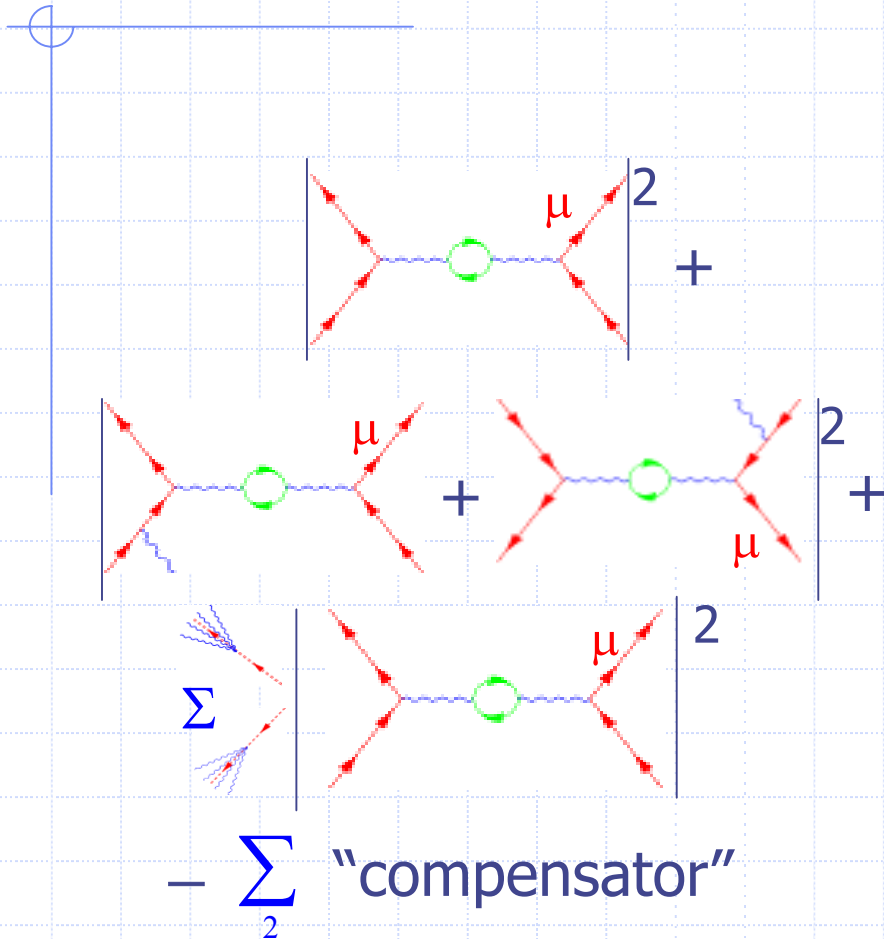
Contribution of  
vacuum polarization, %



Contribution of jets, %



# $e^+e^- \rightarrow \mu^+\mu^-$ cross section calculation



vacuum polarization by **leptons**  
and **hadrons** is included by each diagram

precise matrix element for one photon at large angle  
relatively to initial particle ( $\theta > \theta_0, E > \Delta E$ )

one photon for FSR + Interference

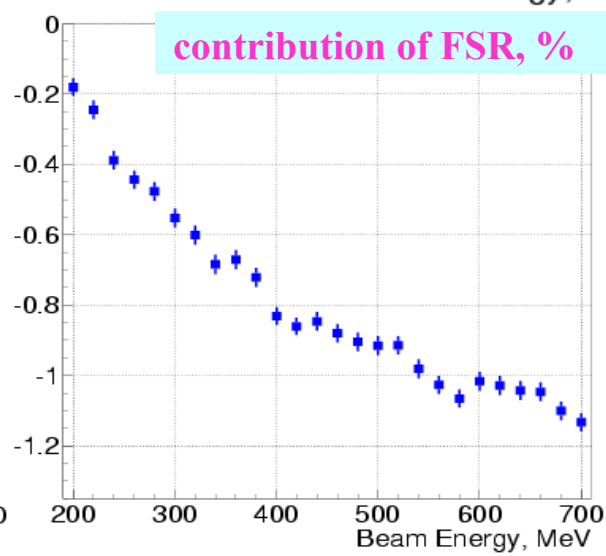
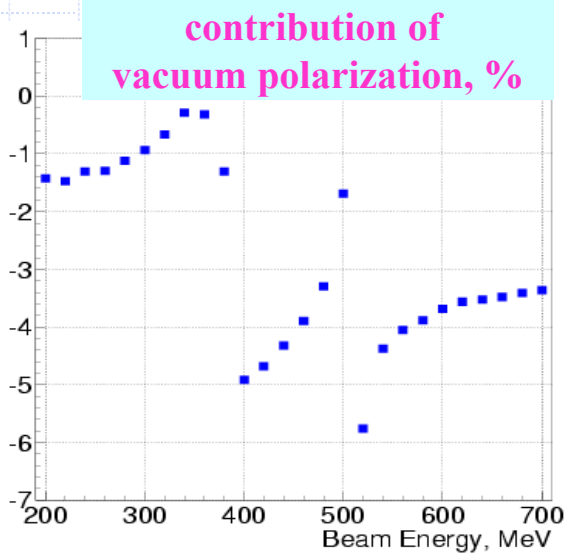
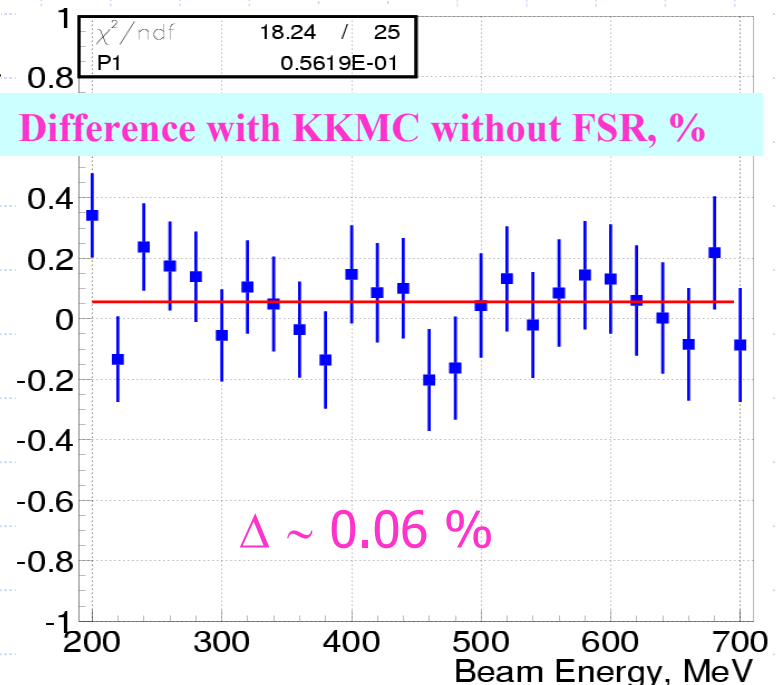
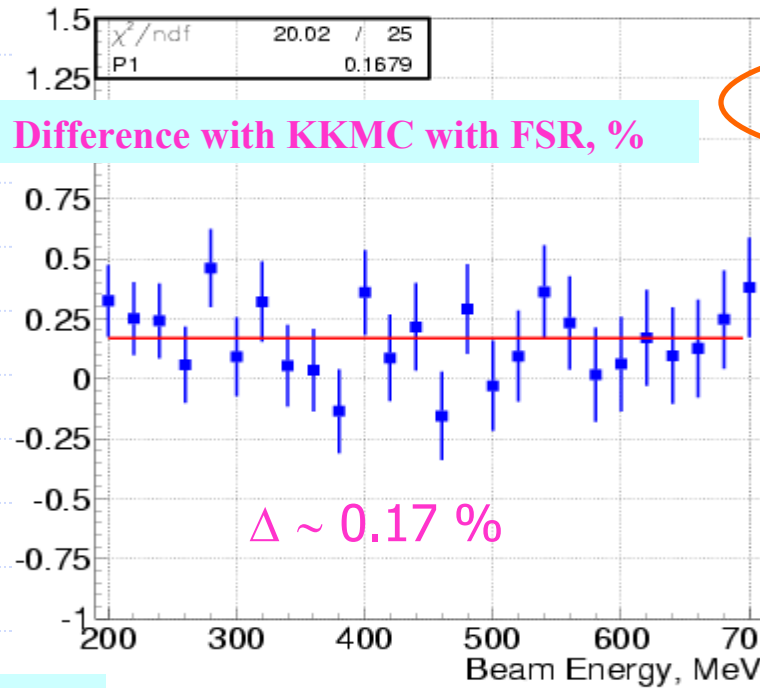
along initial particles ( $\theta < \theta_0$ ) - "jets"

accuracy estimation  $\sim 0.2\%$

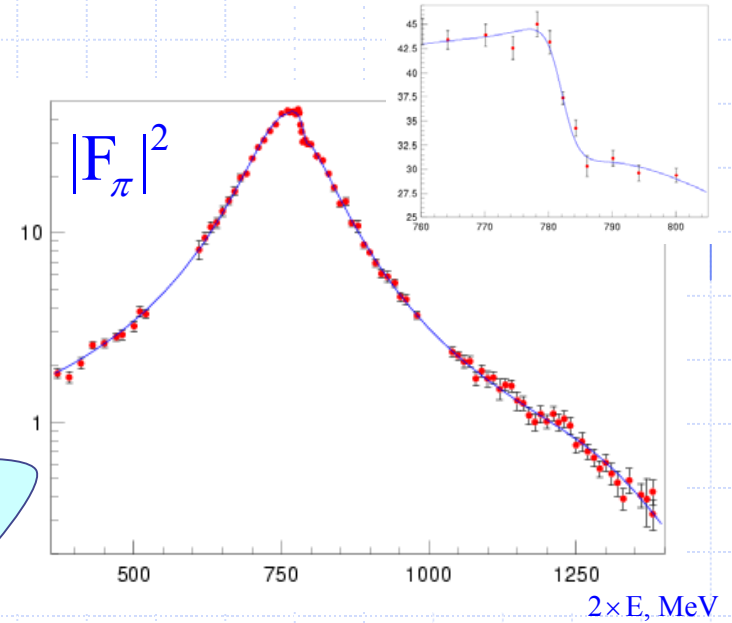
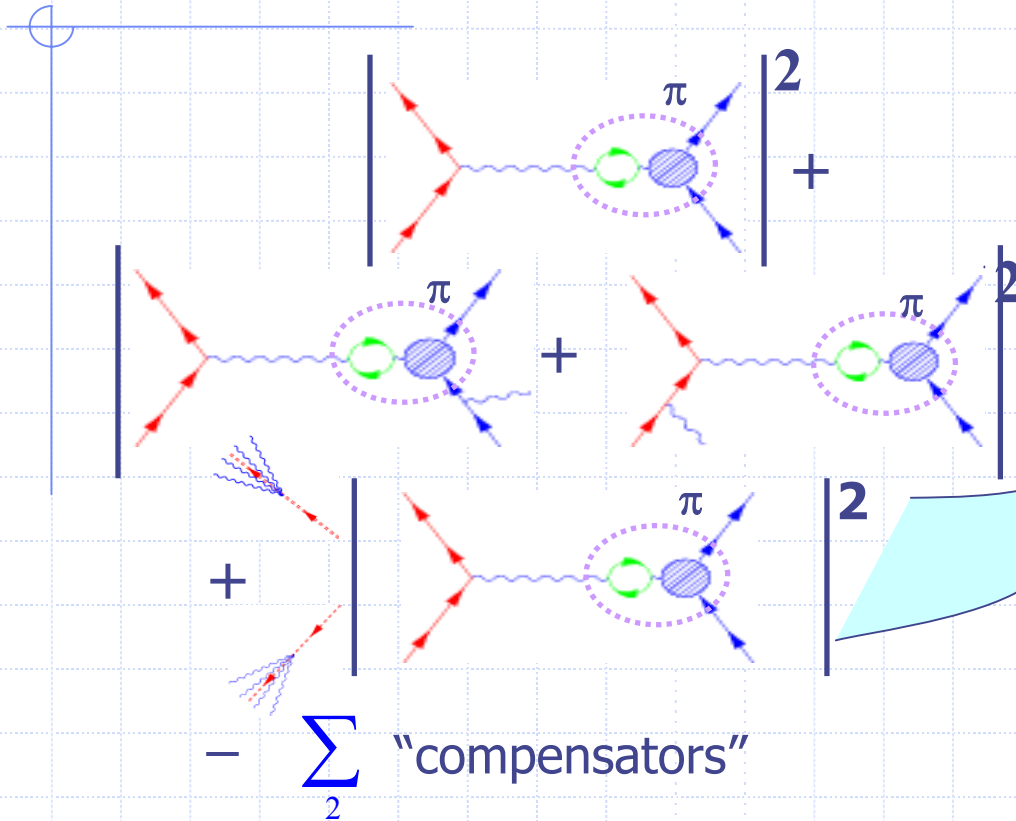


# $e^+e^- \rightarrow \mu^+\mu^-$ code comparison with KKMC

S. Jadach, B.F.L. Ward, Z. Was, *Comput. Phys. Commun.* 130:260-325, 2000, hep-ph/9912214



# $e^+e^- \rightarrow \pi^+\pi^-$ cross section calculation



**Polarization of vacuum by leptons and hadrons is included in resonance: "dressed" cross section**

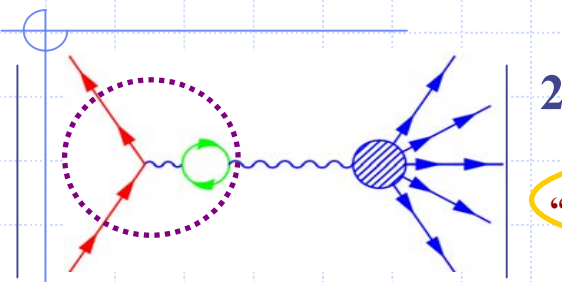
$$|F_\pi|_{\text{exp}}^2 = \frac{\sigma_{\text{exp}}^{\text{vis}}(e^+e^- \rightarrow \pi^+\pi^-)}{\sigma_{\text{theor}}^{\text{vis}}(e^+e^- \rightarrow \pi^+\pi^-) / |F_\pi|_{\text{test}}^2}$$

**$e^+e^- \rightarrow \pi^+\pi^-$  code comparison with ...?**

**No program with the same or better precision**

# What is R(s) in dispersion relations?

$$\sigma_{\text{theor}}^{\text{vis}}(e^+e^- \rightarrow \text{hadrons}) = \int \dots \int \frac{D(z_1)D(z_2)\sigma(z_1, z_2, s)}{|1 - \Pi(z_1, z_2, s)|^2} dz_1 dz_2$$



“bare” cross section

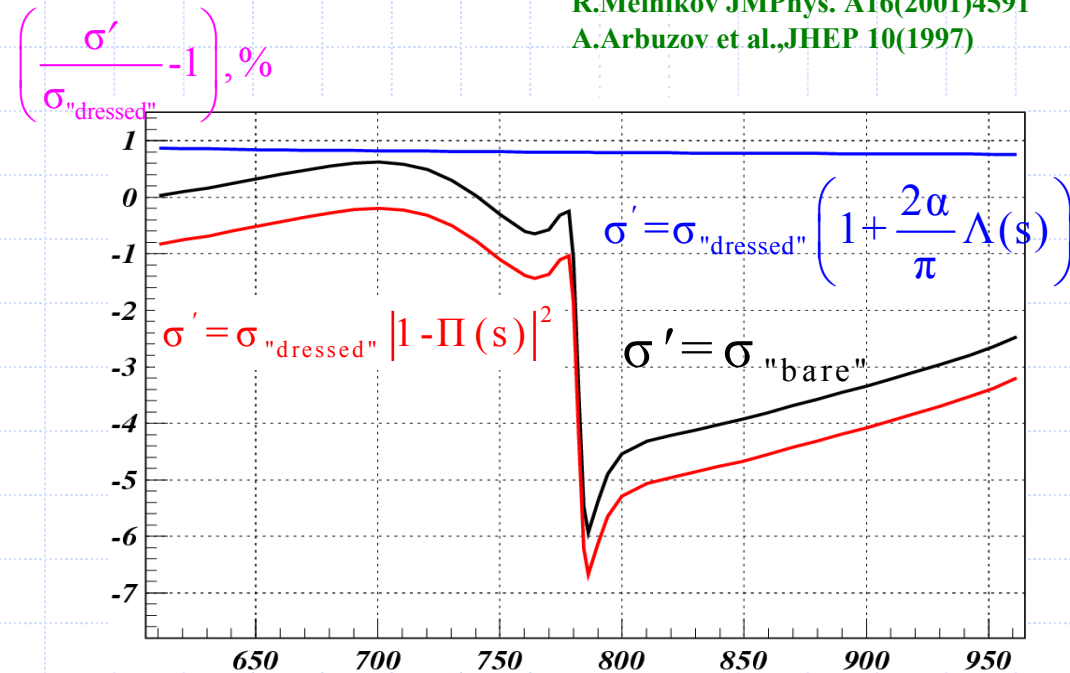
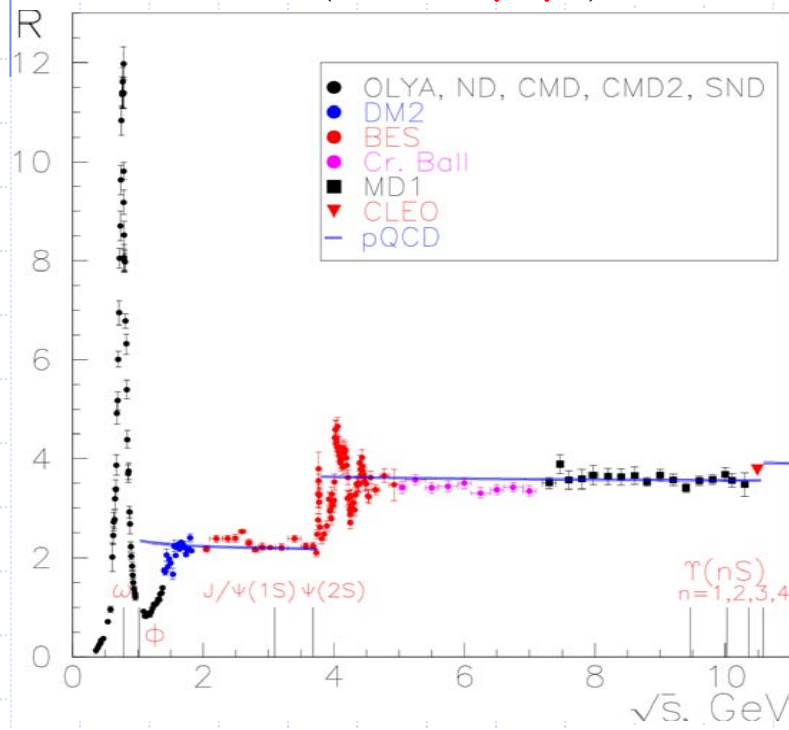
$$R^{\pi\pi}(s) \propto |F_\pi(s)|^2 |1 - \Pi(s)|^2 \left( 1 + \frac{2\alpha}{\pi} \Lambda(s) \right)$$

“removing” of VP

“including” of FSR

$$R(s) \equiv \frac{\sigma(e^+e^- \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$

A.Hoefler et al., hep-ph/0107154  
 R.Melnikov JPhys. A16(2001)4591  
 A.Arbutov et al., JHEP 10(1997)



# Photon vacuum polarization

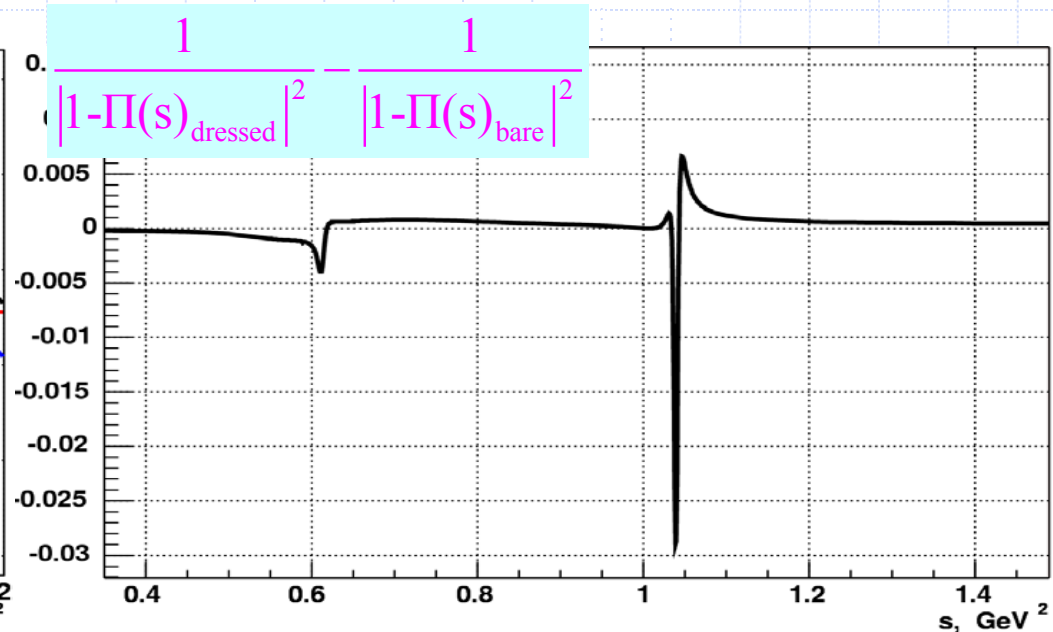
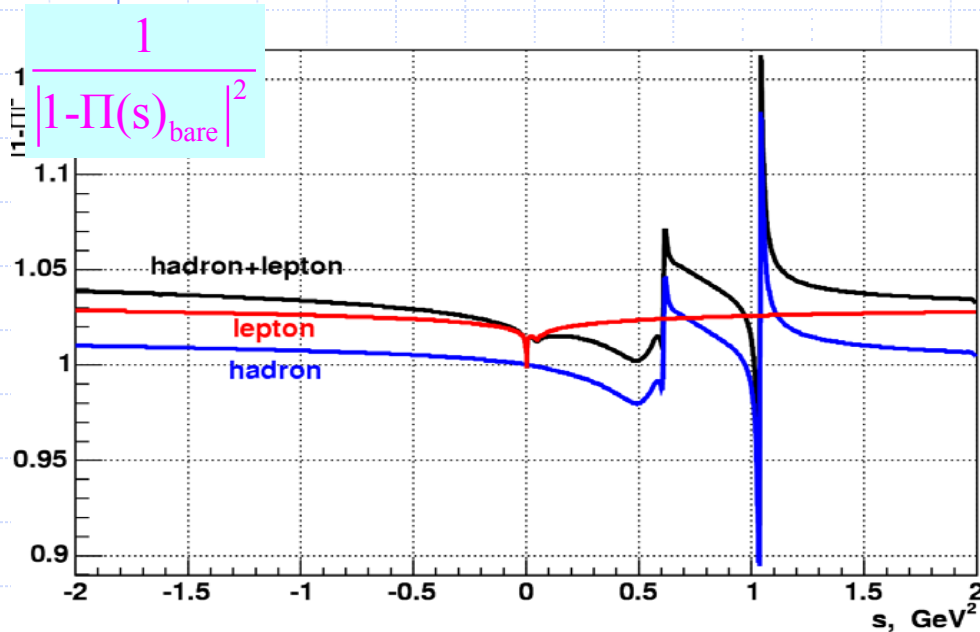
All available  $e^+e^-$  data were used to calculate dispersion integral

$$\Pi_l(s) = \left(\frac{\alpha}{\pi}\right) \Pi_1(s) + \left(\frac{\alpha}{\pi}\right)^2 \Pi_2(s) + \dots$$

$\sim 10^{-2}$ 
 $\sim 3 \times 10^{-5}$

$$\Pi(s) = \Pi_l(s) + \Pi_h(s)$$

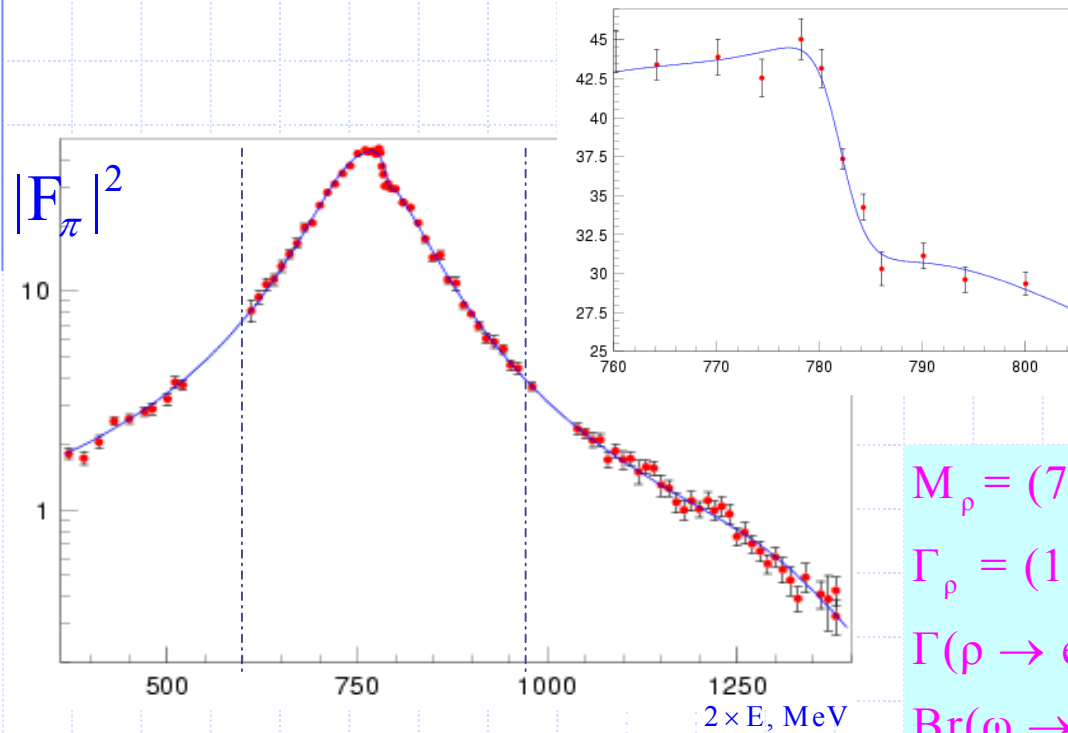
$$\Pi(s) = \frac{s}{4\pi^2\alpha} \left( \text{P} \int_{4m_\pi^2}^{\infty} \frac{\sigma_{e^+e^- \rightarrow \gamma^* \rightarrow \text{final}}(s') ds'}{s-s'} - i\pi\sigma_{e^+e^- \rightarrow \gamma^* \rightarrow \text{final}}(s) \right)$$





R.R.Akhmetshin et al., PL B 527(2002) 161

R.R.Akhmetshin et al., hep-ex/0308008



$$L = 317.3 \text{ nb}^{-1}$$

114000  $\pi^+\pi^-$  events in  $\rho$  m

$$M_\rho = (775.65 \pm 0.64 \pm 0.50) \text{ MeV} (\downarrow 0.54\sigma)$$

$$\Gamma_\rho = (143.85 \pm 1.33 \pm 0.80) \text{ MeV} (\downarrow 0.39\sigma)$$

$$\Gamma(\rho \rightarrow e^+e^-) = (7.06 \pm 0.11 \pm 0.05) \text{ keV} (\uparrow 1.7\sigma)$$

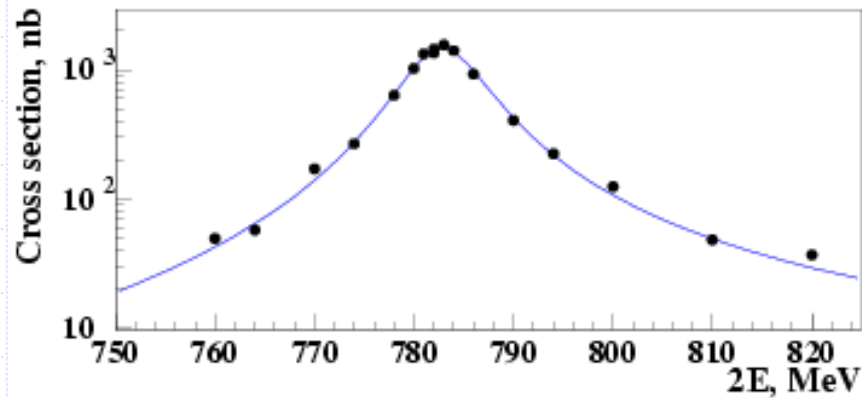
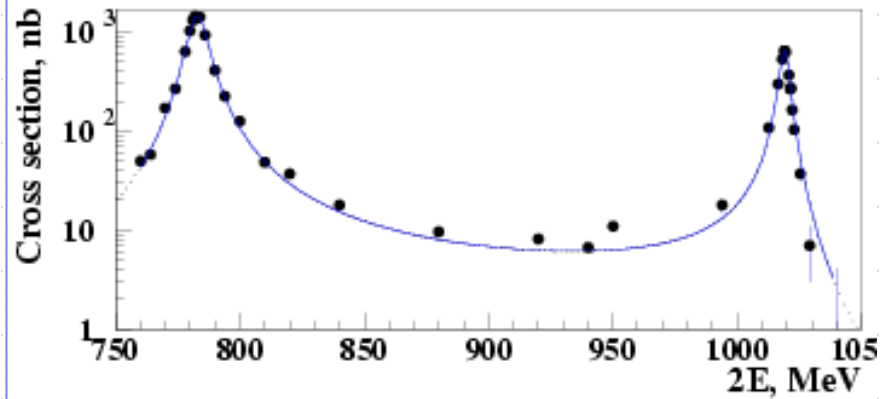
$$\text{Br}(\omega \rightarrow \pi^+\pi^-) = (1.30 \pm 0.24 \pm 0.05) \% (\text{nc})$$

$$\arg \delta = 13.3^\circ \pm 3.7^\circ \pm 0.2^\circ (\text{nc})$$



R.R.Akhmetshin et al., PL B 476(2000) 33

R.R.Akhmetshin et al., hep-ex/0308008



$$L = 119.6 \text{ nb}^{-1}$$

11200  $\pi^+\pi^-\pi^0$  events in  $\omega$  meson

$$M_\omega = (782.68 \pm 0.09 \pm 0.04) \text{ MeV} (\downarrow 0.3 \sigma)$$

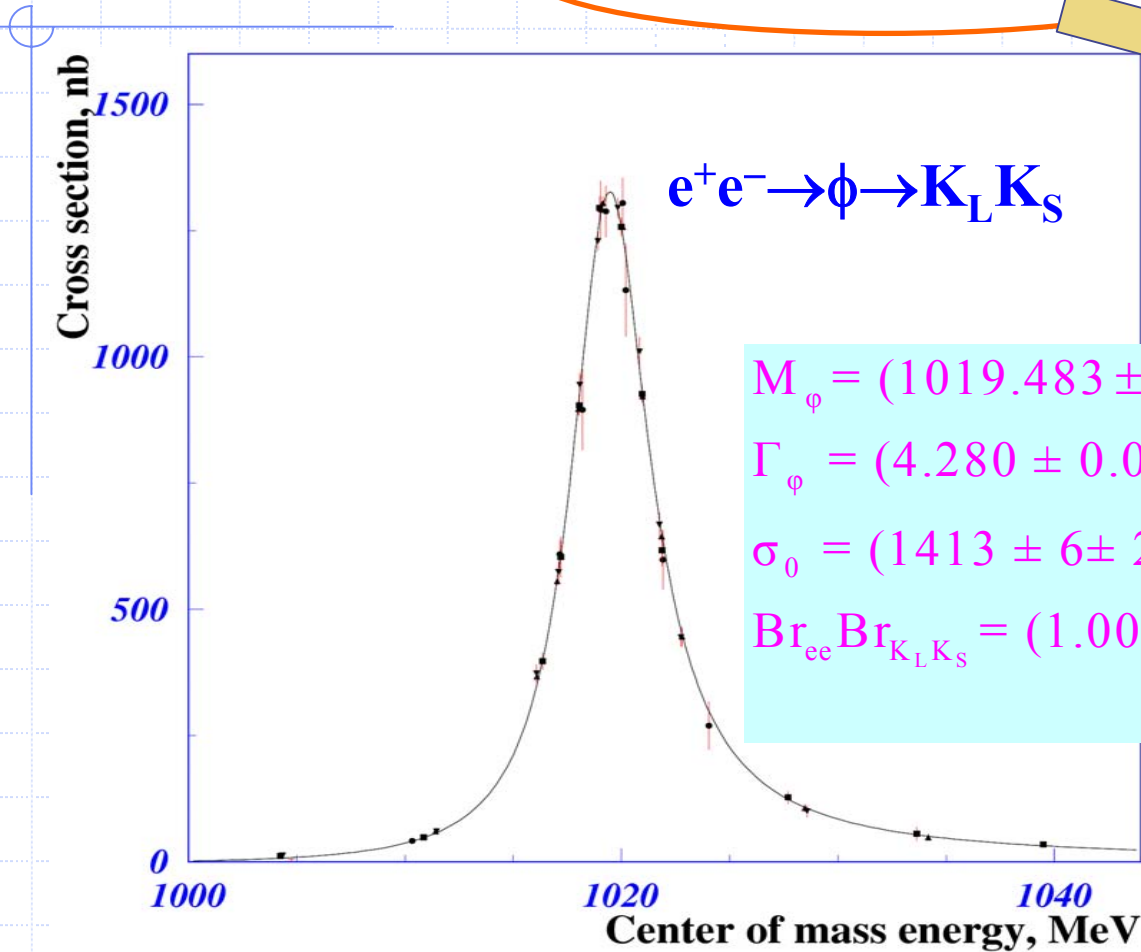
$$\Gamma_\omega = (8.68 \pm 0.23 \pm 0.10) \text{ MeV (nc)}$$

$$\sigma_0 = (1495.6 \pm 25.5 \pm 19.4) \text{ nb} (\uparrow 1.2\sigma)$$

$$e^+e^- \rightarrow \phi \rightarrow K_L K_S$$

R.R.Akhmetshin et al., PL B 466(1999) 385

R.R.Akhmetshin et al., hep-ex/0308008



$$M_\phi = (1019.483 \pm 0.011 \pm 0.025) \text{ MeV (nc)}$$

$$\Gamma_\phi = (4.280 \pm 0.033 \pm 0.025) \text{ MeV (nc)}$$

$$\sigma_0 = (1413 \pm 6 \pm 24) \text{ nb } (\uparrow 1.6\sigma)$$

$$\text{Br}_{ee} \text{Br}_{K_L K_S} = (1.001 \pm 0.004 \pm 0.017) \times 10^{-4} (\uparrow 1.6\sigma)$$

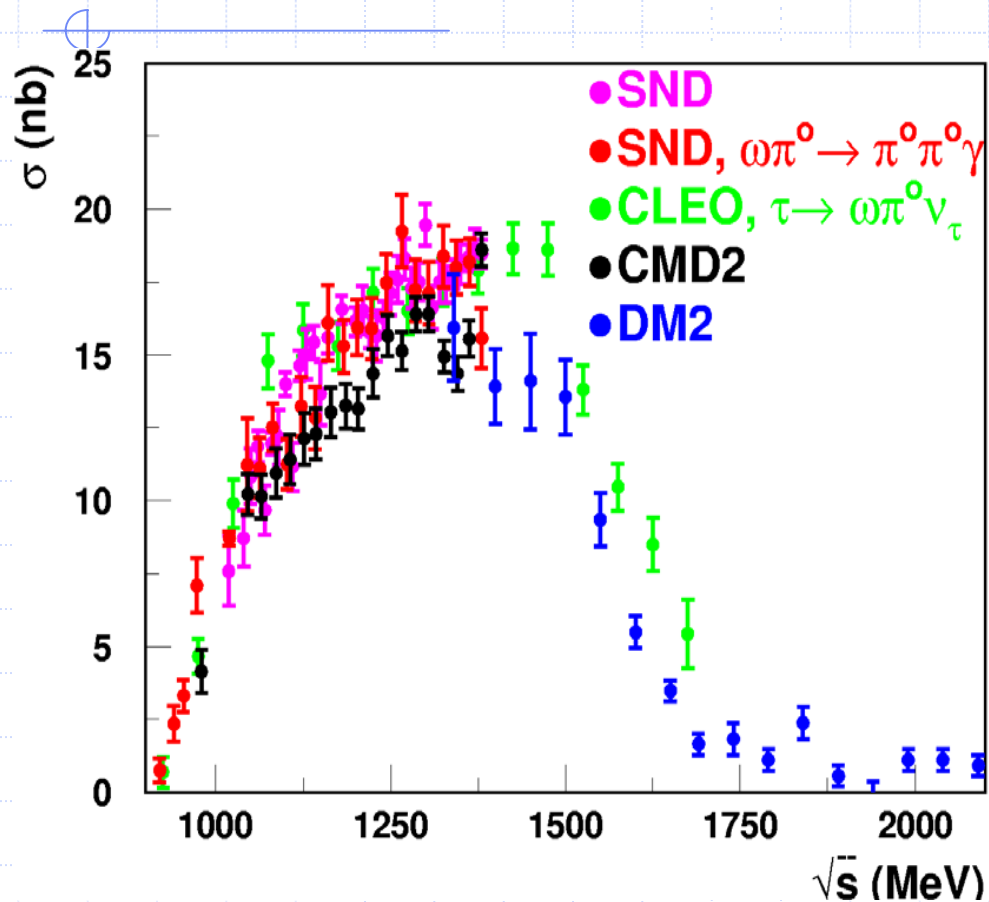
$$L = 1294 \text{ nb}^{-1}$$

$$2.72 \times 10^5 K_L K_S \text{ events}$$



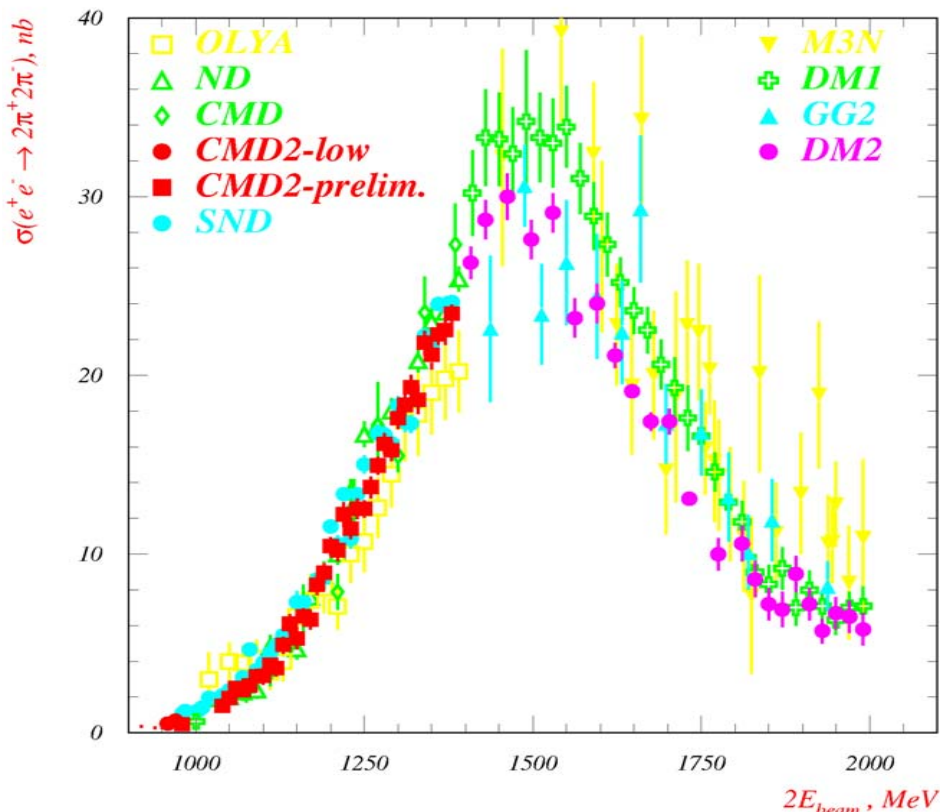
$$e^+e^- \rightarrow 4\pi$$

$$e^+e^- \rightarrow \omega\pi^0, \omega \rightarrow \pi^+\pi^-\pi^0$$



CMD-2 data in  $4\pi$  channel is lower!

$$e^+e^- \rightarrow 2\pi^+2\pi^-$$



After reanalysis CMD-2 data  
 agrees with SND data  
 To be published in PL

# Neutral kaon mass measurement (preliminary)

$$\int L dt \simeq 355 \text{ nb}^{-1}, e^+e^- \rightarrow K_S^0 K_L^0, K_S^0 \rightarrow \pi^+\pi^-, N_{K_S^0} = 4.9 \cdot 10^4$$

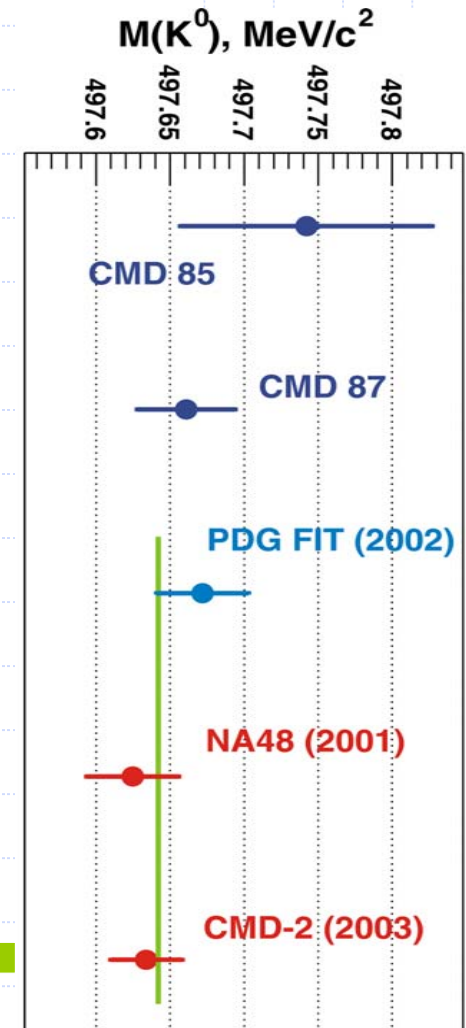
Resonant depolarization beam energy measurement

Systematic due to initial state radiative corrections, beam energy measurement and nonlinearity shift are energy dependent

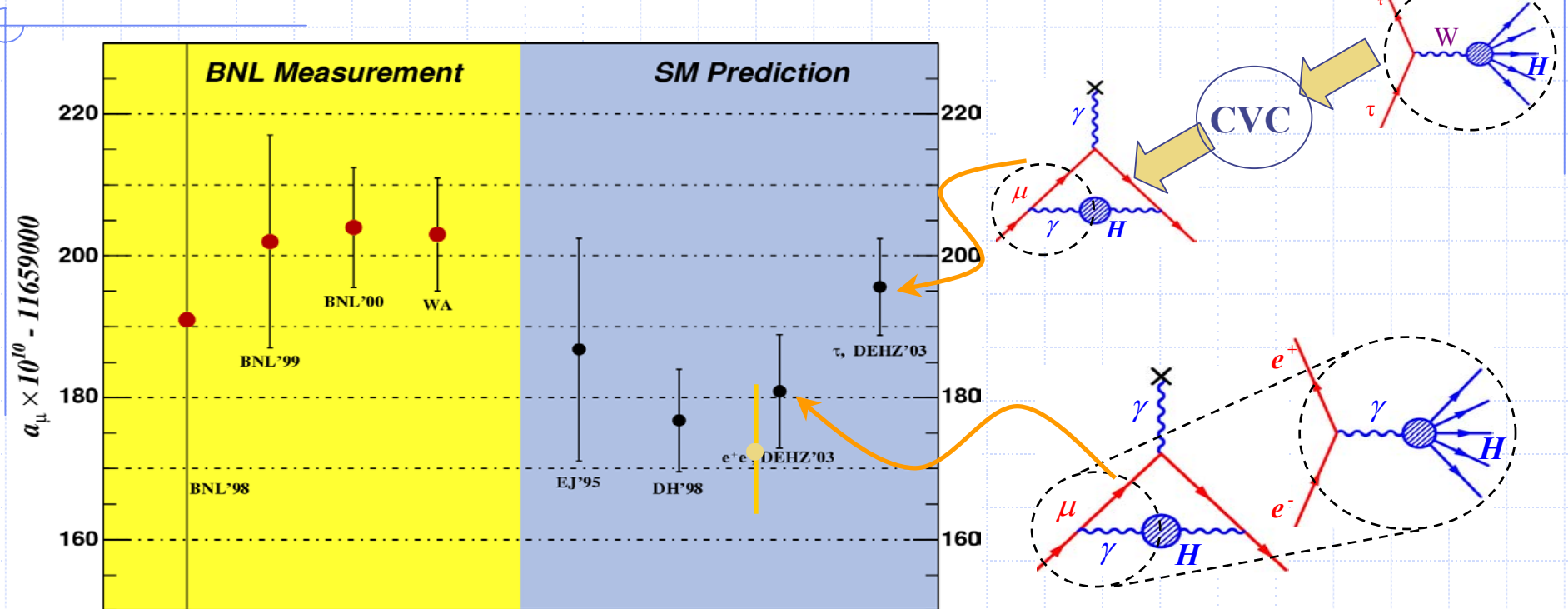
Systematic source	Shift, keV	Error, keV
Beam energy measurement		13 ÷ 19
Energy calibration model dependency		3
Radiative corrections to initial state	− (80 ÷ 630)	2 ÷ 12
Beam energy spread correction	+ 3	0.3
Radiative corrections to final state	− 6	6
Nonlinearity shift	60 ÷ 140	6 ÷ 15
Correction for pion decay in flight	+ 4	3
Background		4
Z-chamber thermal expansion		3
Selection criteria		6
Fit bounds		8
Charged pion mass uncertainty		0.04

$$M_{K_S^0} = 497.634 \pm 0.016 \pm 0.019 \text{ MeV}/c^2$$

$$M_{K_S^0}^{(fit)} = 497.642 \pm 0.016 \text{ MeV}/c^2$$



# g-2 of muon



$e^+e^- \rightarrow \text{hadrons}$      $a_\mu(\text{exp}) - a_\mu(\text{theor}) = (22.1 \pm 11.3) \times 10^{-10} \text{ (1.9 } \sigma)$

$\tau \rightarrow \text{hadrons} + \nu_\tau$      $a_\mu(\text{exp}) - a_\mu(\text{theor}) = (7.4 \pm 10.5) \times 10^{-10} \text{ (0.7 } \sigma)$

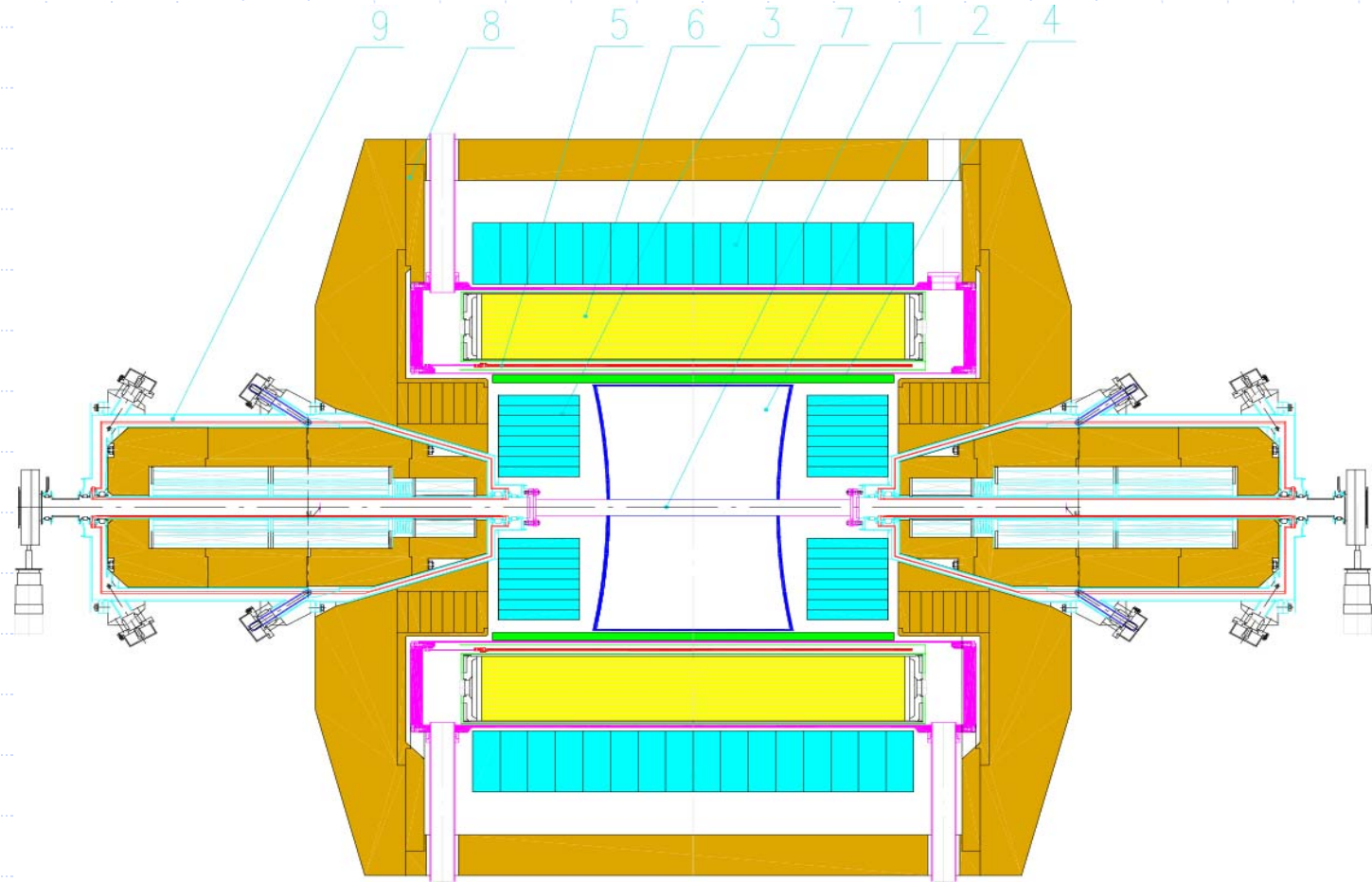
# Conclusion

- Codes for calculations of  $e^+e^- \rightarrow e^+e^-(\gamma)$ ,  $e^+e^- \rightarrow \mu^+\mu^-(\gamma)$ ,  $e^+e^- \rightarrow \pi^+\pi^-(\gamma)$  cross sections with accuracy 0.2%
- “Dressed” cross sections for dynamic studies, “bare” cross sections for dispersion relations
- Updated results have been published [hep-ex/0308008](https://arxiv.org/abs/hep-ex/0308008)
- Good agreement between SM calculations for  $(g-2)_\mu$  based on  $e^+e^- \rightarrow \text{hadrons}$  and  $\tau \rightarrow \nu_\tau \text{hadrons}$  with experimental value

# CMD-3

System	CMD-2	CMD-3
Drift chamber	512 sensitive wires, $\sigma_{R-\phi}=250 \mu\text{m}$ , $\sigma_Z=5 \text{ mm}$ , $\sigma_\theta=1.5 \times 10^{-2}$ , $\sigma_\phi=7 \times 10^{-3}$ , $\sigma_{dE/dx}=0.2 \times E$	1218 sensitive wires, $\sigma_{R-\phi}=140 \mu\text{m}$ , $\sigma_Z=2 \text{ mm}$ , $\sigma_\theta=7 \times 10^{-3}$ , $\sigma_\phi=4 \times 10^{-3}$ , $\sigma_{dE/dx}=0.15 \times E$
Z-chamber	Double layers proportional chamber with cathode strips, anode wires are combined to $2 \times 32$ sectors, number of cathode strips – 512, $\sigma_Z=2 \text{ mm}$ , $\sigma_t=5 \text{ ns}$ , $\Omega=0.8 \times 4\pi$ steradian.	
Barrel Calorimeter	892 CsI crystals in 8 octants, readout – PMT, thickness – $8.1 X_0$ , $\sigma_E/E=8.5\%$ at $100 \div 700 \text{ MeV}$ , $\sigma_{\phi,\theta}=0.03 \div 0.02 \text{ rad}$ .	1152 CsI crystals in 8 octants, readout – PIN photodiodes, $0.4 \text{ m}^3 \text{ LXe}$ , thickness – $5 X_0 + 8.1 X_0 = 13.1 X_0$ , $\sigma_E/E=4.7 \div 3\%$ at $100 \div 900 \text{ MeV}$ , $\sigma_{\phi,\theta}=0.005 \text{ rad}$ .
Endcap Calorimeter	680 BGO crystals in 2 endcaps readout – vacuum phototriodes, thickness – $13.4 X_0$ , $\sigma_E/E=8 \div 4\%$ at $100 \div 700 \text{ MeV}$ , $\sigma_{\phi,\theta}=0.03 \div 0.02 \text{ rad}$ .	680 BGO crystals in 2 endcaps readout – PIN photodiodes, thickness – $13.4 X_0$ , $\sigma_E/E=8 \div 3.5\%$ at $100 \div 900 \text{ MeV}$ , $\sigma_{\phi,\theta}=0.03 \div 0.02 \text{ rad}$ .
Range system	Streamer tubes, 2 double layers, $\sigma_Z=5 \text{ cm}$	Plastic scintillator counters, $\sigma_t < 1 \text{ ns}$
Superconductive solenoid	Magnetic field 1 T, thickness $0.38 X_0$	Magnetic field 1.5 T, thickness $0.18 X_0$

# CMD-3



1 – vacuum chamber; 2 – drift chamber; 3 – BGO calorimeter; 4 – Z-chamber; 5 – main solenoid; 6 – LXe calorimeter; 7 – CsI calorimeter; 8 – yoke; 9 – compensating solenoid;

# CMD-3

