

# NA48 results on $K^0$ rare decays



## Secretariat

Manuela Giabbai, Lia Sabatini  
INFN-LNF

## Organizing Committee

R. Baldini (INFN-LNF)  
S. Bertolucci (Chairman) (INFN-LNF)  
M. Biagini (INFN-LNF)  
G. Isidori (INFN-LNF)

F. Closse (Oxford University)  
E. De Sanctis (INFN-LNF)  
D. Drechsel (Mainz University)  
P. Franzini (Università Roma1)  
C. Guaraldo (INFN-LNF)  
J. Jowett (CERN)  
J. Lee Franzini (INFN-LNF)

**Augusto Ceccucci/CERN**

G. Isidori (INFN-LNF)  
G. Pancheri (INFN-LNF)  
M. Serio (INFN-LNF)  
M. Zobov (INFN-LNF)

J. Seeman (SLAC)  
S. Serci (INFN-Cagliari)  
E. Solodov (BINP)  
C. Zhang (IHEP)

**CERN-NA48 Collaboration: Cambridge, CERN,  
Chicago, Dubna, Edinburgh, Northwestern, Ferrara,  
Florence, Mainz, Orsay, Perugia, Pisa, Saclay, Siegen,  
Turin, Vienna, Warsaw**

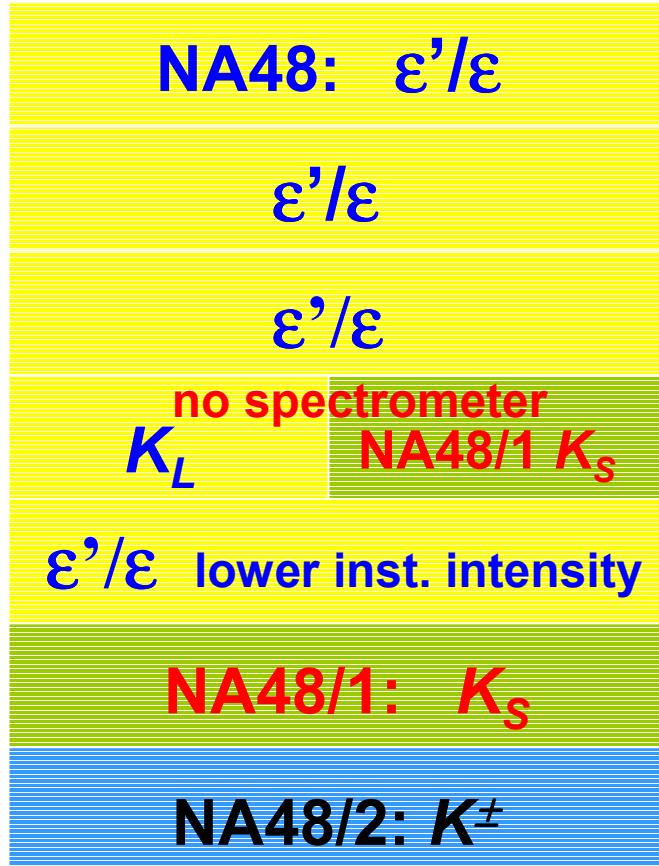
Sponsored by:



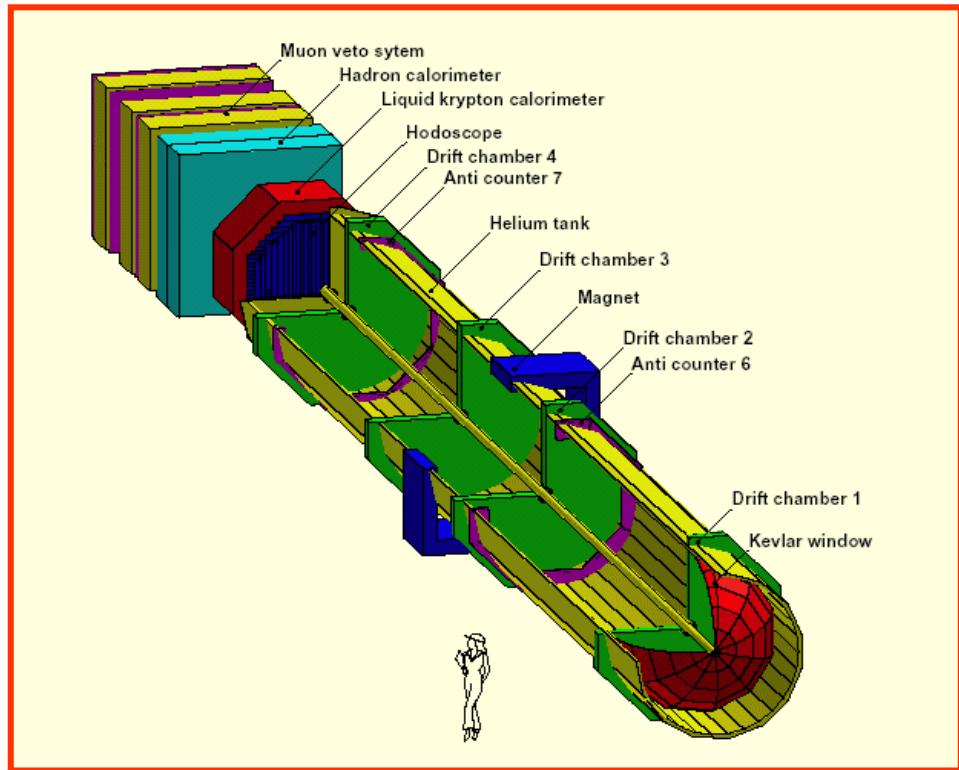
# Outline

- **Testing SM with Rare Kaon Decays**
  - $K_S \rightarrow \pi^0 ee$  2002 data
- **Other tests of CP and CPT symmetry**
  - $K_{L,S} \rightarrow \pi\pi ee$  1998-1999 data
  - $K_S \rightarrow 3\pi^0$  2000 data
- **Non-Leptonic decays**
  - $K_{S,L} \rightarrow \gamma\gamma$  2000 data
  - $K_{S,L} \rightarrow \pi^0\gamma\gamma$  1998-1999 ( $K_L$ ); 2000 ( $K_S$ )
- **Outlook**

# NA48 Detector & Data Taking



1997  
1998  
1999  
2000  
2001  
2002  
2003

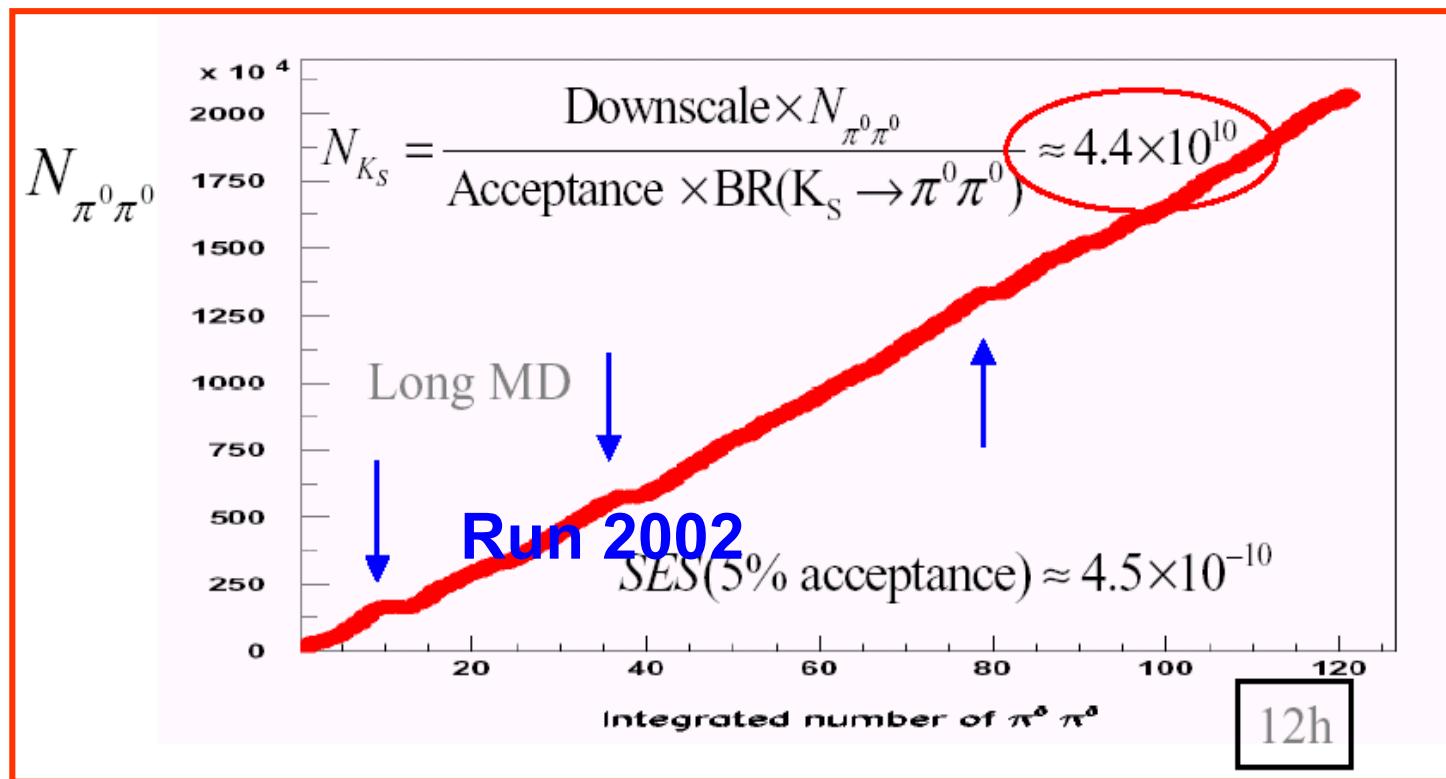


Kaons produced by 450(400) GeV  
protons from the CERN SPS on Be target:  
 $E_K \sim 110$  GeV  
**FAR ( $K_L$ ) beam ~ 120 m long**  
**NEAR ( $K_S$ ) beam ~ 6 m long**

# NA48/1

## $K_S$ and neutral hyperon decays

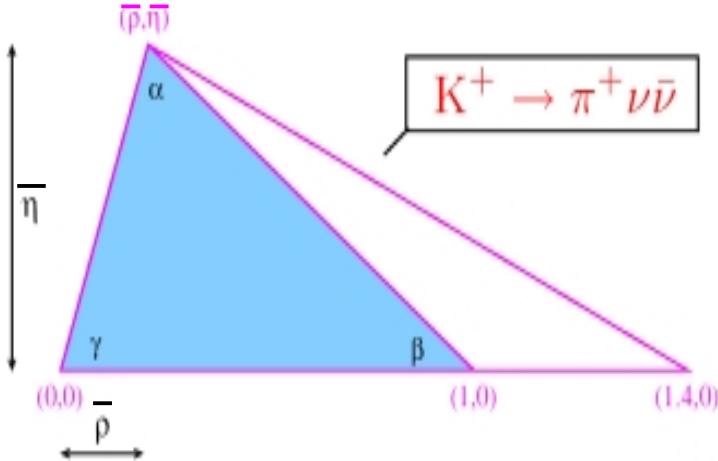
- Upgraded read out
- High intensity short neutral beam from the CERN-SPS
- Run in 2000 (only  $\gamma$ s) and 2002



## CP-Violation

# Kaon Rare Decays and the SM

$K_L \rightarrow \pi^0 \nu \bar{\nu}$     **(holy grail)**  
 $K_L \rightarrow \pi^0 e^+ e^-$      $\left\{ \begin{array}{l} K_S \rightarrow \pi^0 e^+ e^- \\ K_L \rightarrow \pi^0 \gamma \gamma \\ K_L \rightarrow ee\gamma\gamma \end{array} \right.$



$K_L \rightarrow \mu^+ \mu^-$      $\left\{ \begin{array}{l} K_L \rightarrow \gamma\gamma, K_L \rightarrow e^+ e^- \gamma \\ K_L \rightarrow e^+ e^- e^+ e^-, e^+ e^- \mu^+ \mu^- \end{array} \right.$

$J_{CP}=2\times(\text{Triangle Area})$  is the unique measure of CP-Violation in SM

$$J_{CP} = \text{Im}(V_{ud}^* V_{us} V_{ts}^* V_{tb}) \sim \cos\theta_c \sin\theta_c \text{Im } \lambda_t$$

In the Wolfenstein parameterisation ( $\lambda, A, \bar{\eta}, \bar{\rho}$ ):

$$\text{Im } \lambda_t = A^2 \lambda^5 \bar{\eta}, \quad \text{Re } \lambda_t = A^2 \lambda^5 \bar{\rho}$$

# Theory of $K_L \rightarrow \pi^0 ee$ ( $\mu\mu$ )

- Complete re-analysis of the decay:  
(Buchalla, D'Ambrosio, Isidori, hep-ph/0308008)  BDI
- Short Distance (Direct CP-Violation)
  - From Standard Model fit:  $Im \lambda_t = (1.36 \pm 0.12) 10^{-4}$  (CKM)
  - $B(K_L \rightarrow \pi^0 ee)_{CPV-dir} = (2.4 \pm 0.2) \times 10^{-12} \times (Im \lambda_t / 10^{-4})^2 = (3.2 \pm 0.4) \times 10^{-12}$
- Indirect CP-Violation
  - $BR(K_L \rightarrow \pi^0 ee)_{CPV-ind} \sim 1/330 BR(K_s \rightarrow \pi^0 ee)$
  - Direct and Indirect CP-Violating components interfere
- CP-Conserving contribution
  - Need model ind. 3 par. fit (Gabbiani, Valencia, PRD 64 2001)
  - $BR_{CPC} < 3 \times 10^{-12}$  (conservative, BDI)
    - They fix the 3 counterterms from  $K_L \rightarrow \pi^0 \gamma\gamma$  and  $K_s \rightarrow \gamma\gamma$

# Experiment: $K_L \rightarrow \pi^0 ee$ ( $\mu\mu$ )

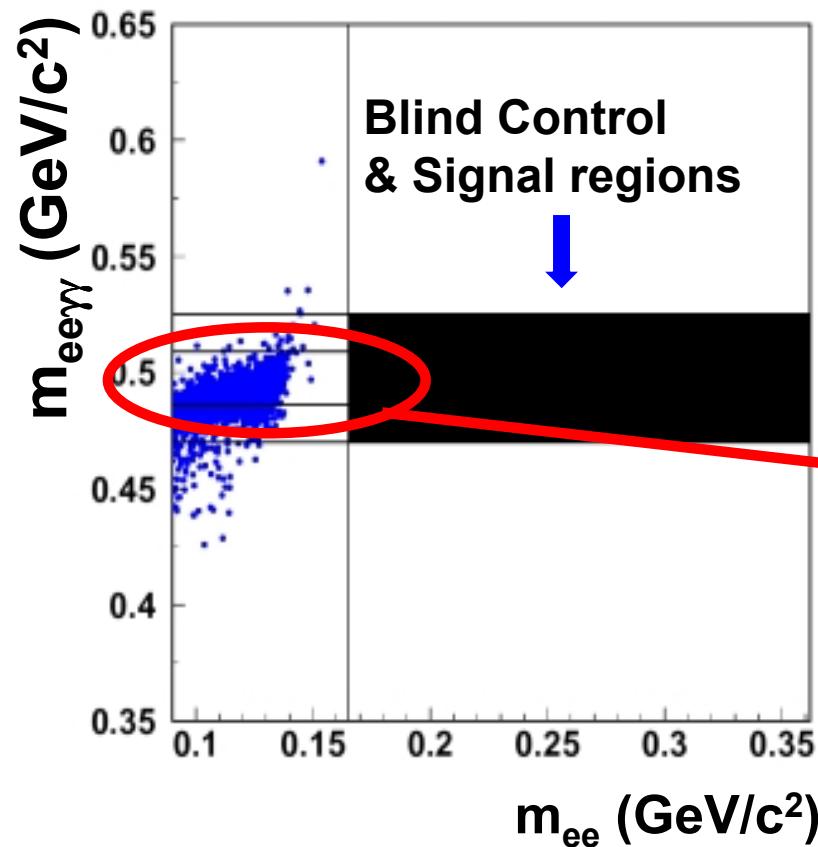
E799-II (KTeV)

Mode	Upper Limit 90% CL	Ref.
$K_L \rightarrow \pi^0 ee$	$< 5.1 \times 10^{-10}$	PRL86 (2001) 97 data
	$< 2.8 \times 10^{-10}$	Preliminary 97+99
$K_L \rightarrow \pi^0 \mu\mu$	$< 3.8 \times 10^{-10}$	PRL84 (2000)

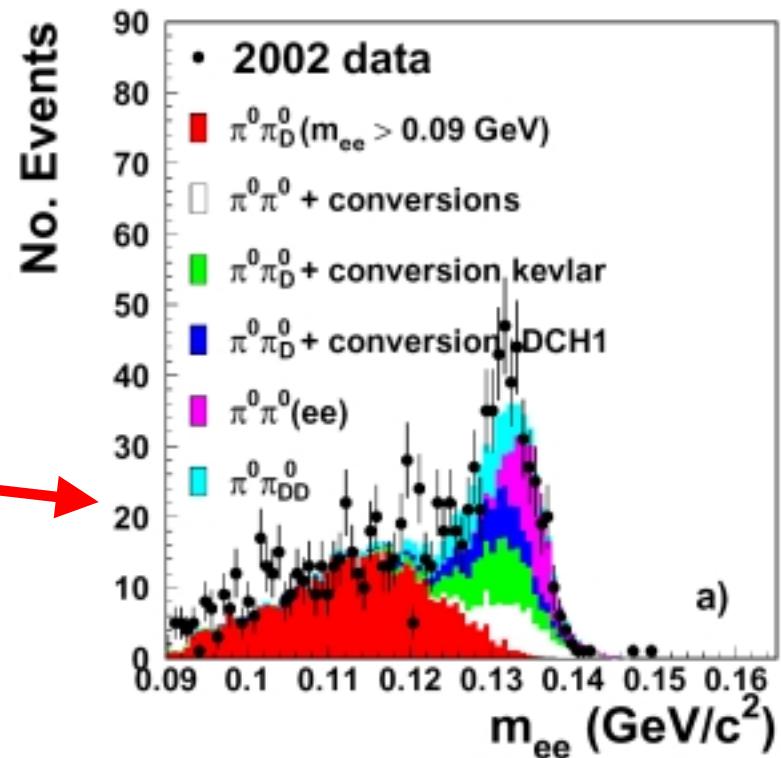
- **Irreducible background:**  $K_L \rightarrow ee(\mu\mu)\gamma\gamma$  (Greenlee, 1990)
  - Same final state as the signal, only  $\gamma\gamma$  mass resolution and kinematics are available to suppress these backgrounds
  - To keep it to the ~1 event level the acceptance is quite reduced
  - Possible future searches will be background dominated

# $K_S \rightarrow \pi^0 ee$

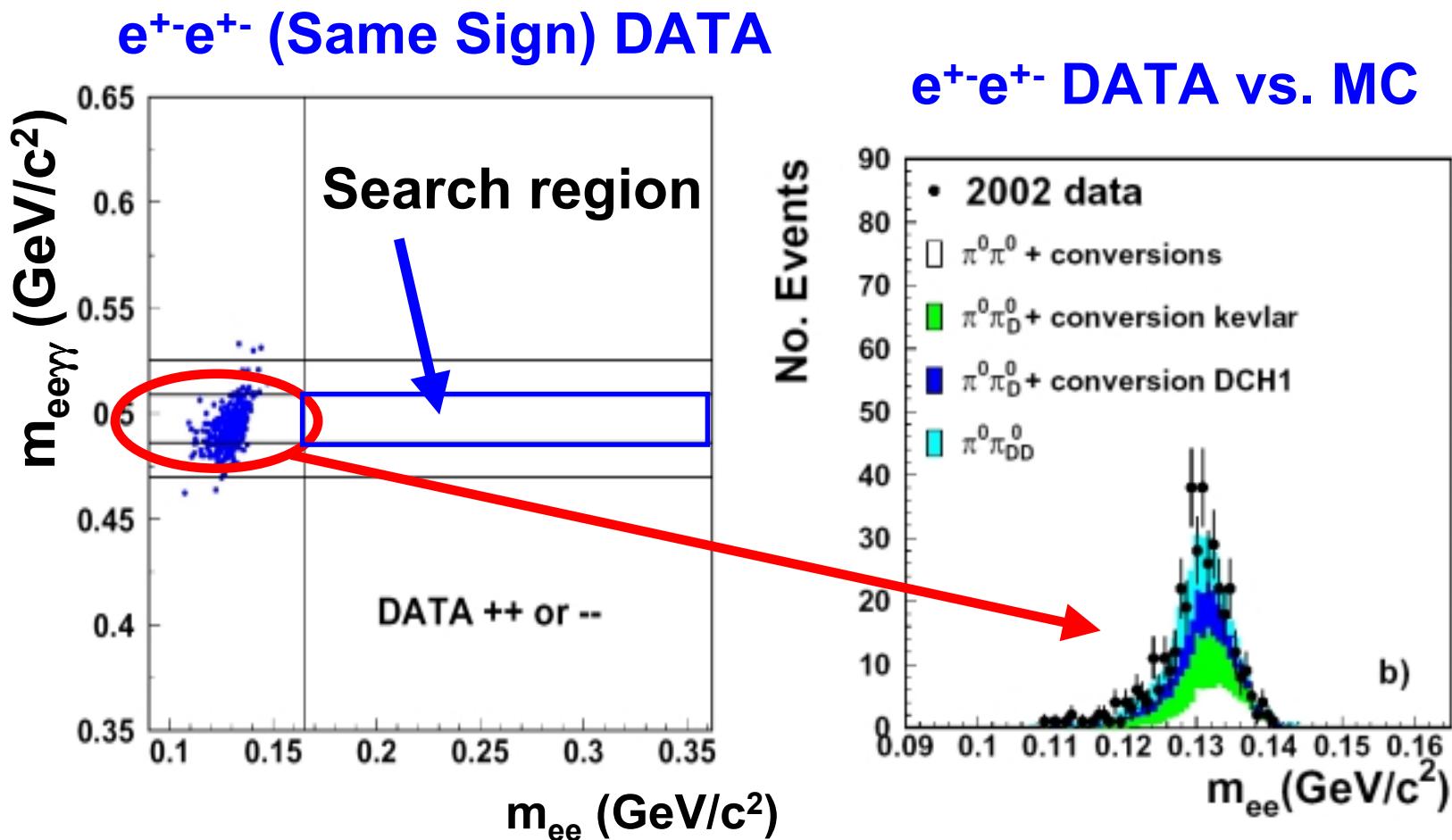
e<sup>+</sup>-e<sup>+</sup> (Odd Sign) DATA



e<sup>+</sup>-e<sup>+</sup> DATA vs. MC

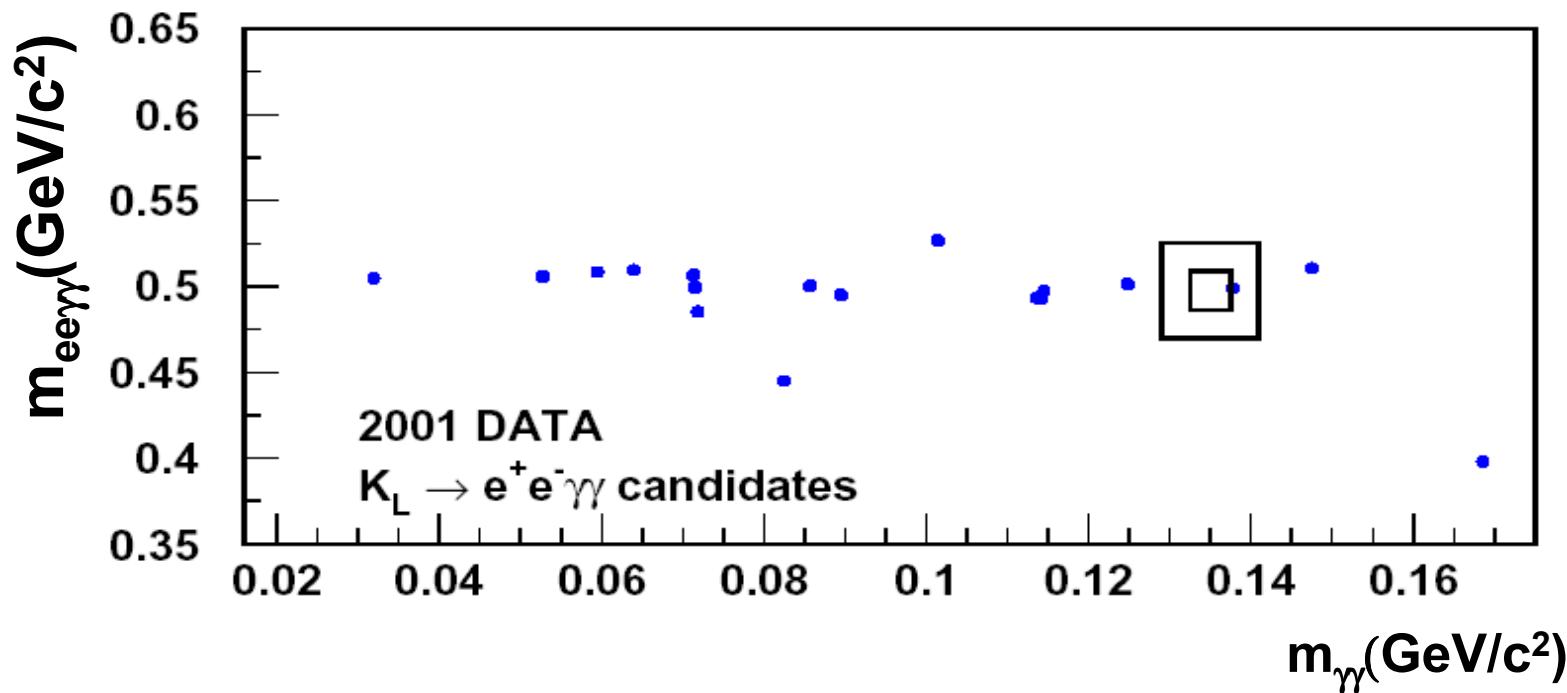


# $K_S \rightarrow \pi^0 ee$



$$K_S \rightarrow \pi^0 ee$$

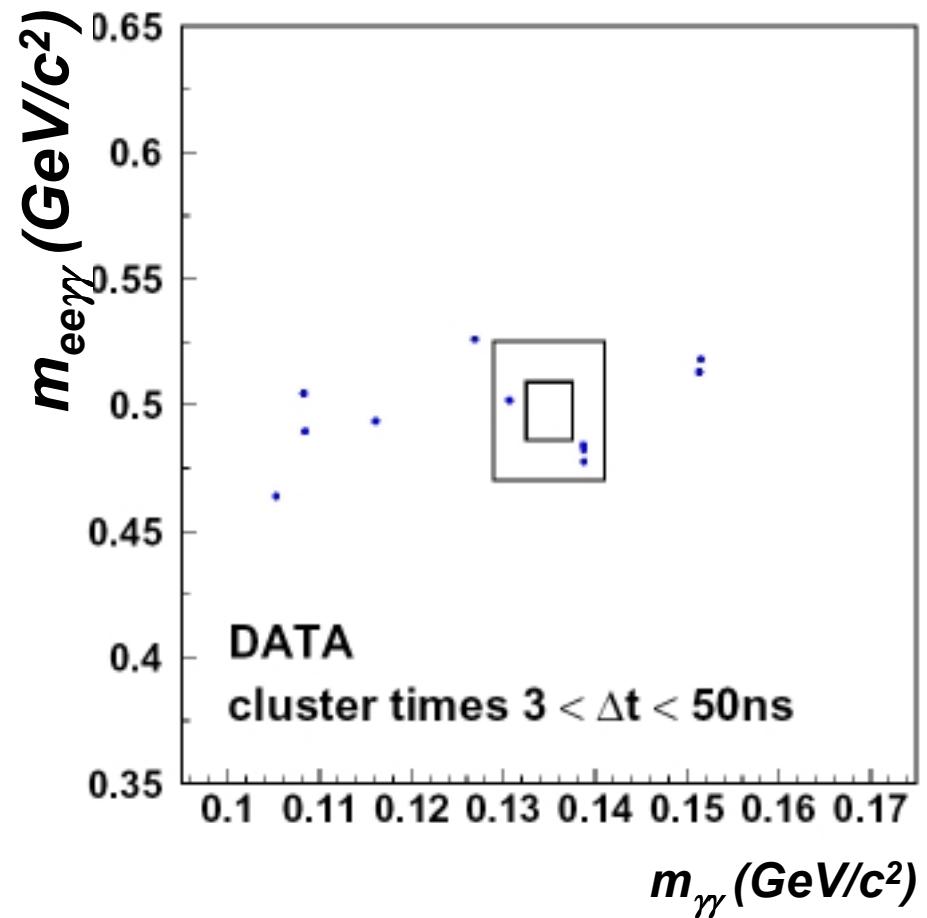
Background from  $K_{L,S} \rightarrow ee\gamma\gamma$ :  
measured using NA48  $K_L$  data from 2001  
 $N(K_L \rightarrow ee\gamma\gamma, 2001) \approx 10 \times N(K_{L,S} \rightarrow ee\gamma\gamma, 2002)$



$$K_S \rightarrow \pi^0 ee$$

## Accidental backgrounds

- DC proton beam
- Read out window:  $\sim 200\text{ns}$
- Use time side band to measure background from time-overlapping fragments from different decays
- Major component:
  - $e\pi\nu + \pi^0\pi^0(\pi^0)$
  - Confirmed relaxing E/P cuts



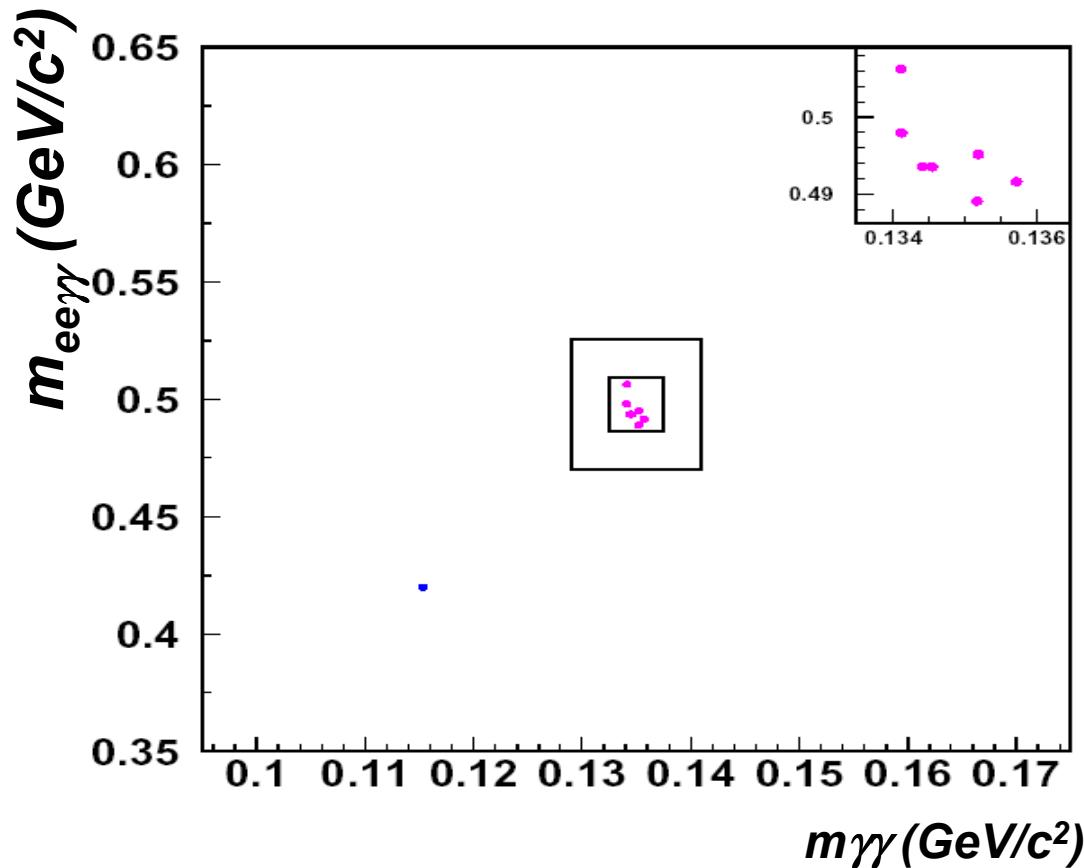
# $K_S \rightarrow \pi^0 ee$

## SUMMARY OF BACKGROUNDS:

Source	Control Region	Signal region
$K_S \rightarrow \pi^0 D \pi^0 D$	0.03	<0.01
$K_{L,S} \rightarrow ee\gamma\gamma$	0.11	0.08
$\pi e\nu + 2\pi^0(\pi^0)$	0.19	0.07
<b>Total</b>	<b>0.33</b>	<b>0.15<sup>+0.10</sup><sub>-0.04</sub></b>

- Many other sources investigated and found to be negligible (e,g neutral cascade decays)
- Blind analysis: Control and signal region remained masked until the study of the background was finished

# $K_S \rightarrow \pi^0 ee$



• 7 candidates in the signal region

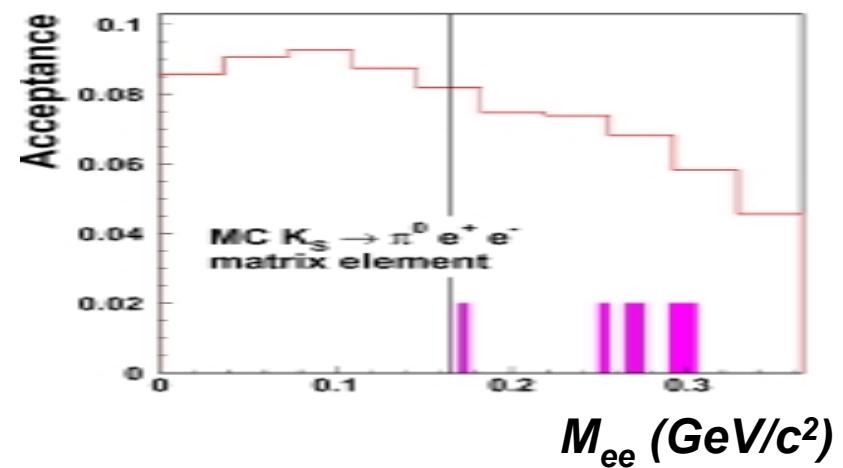
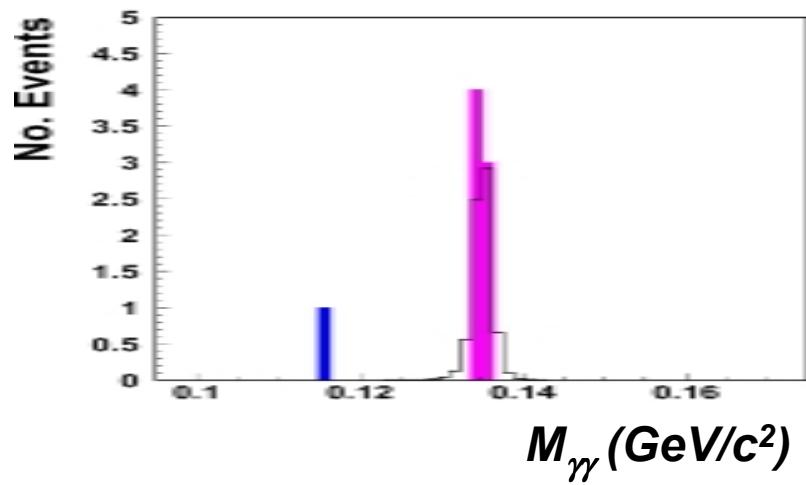
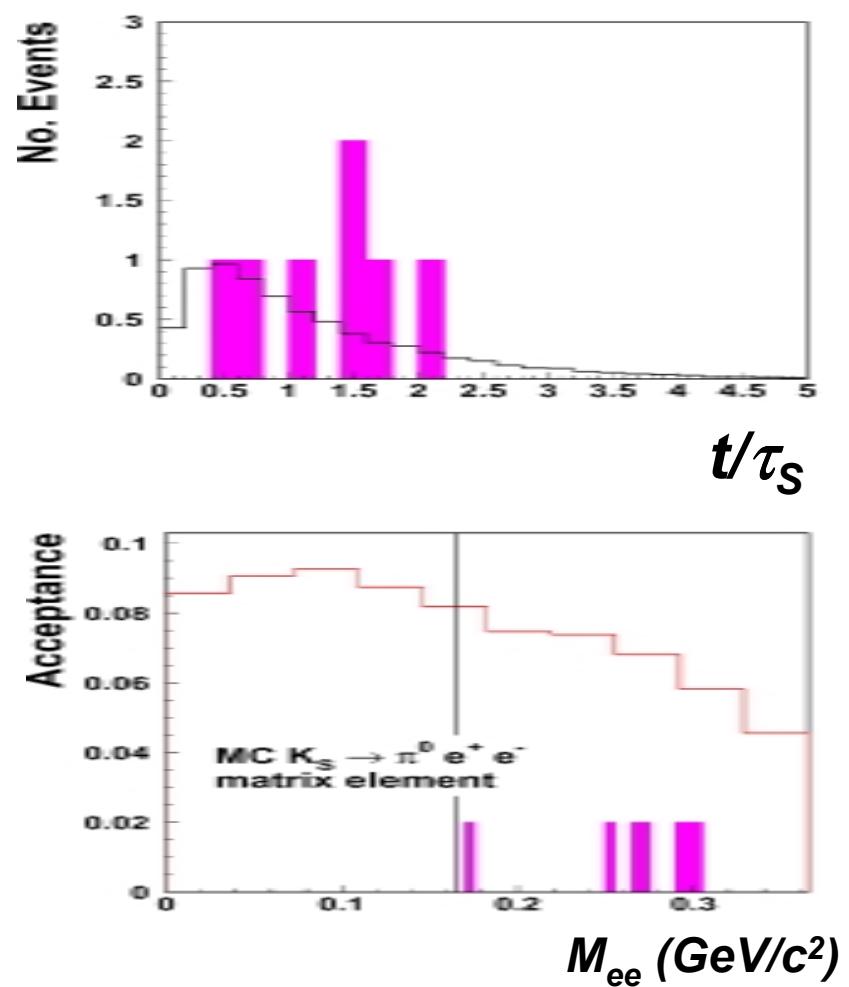
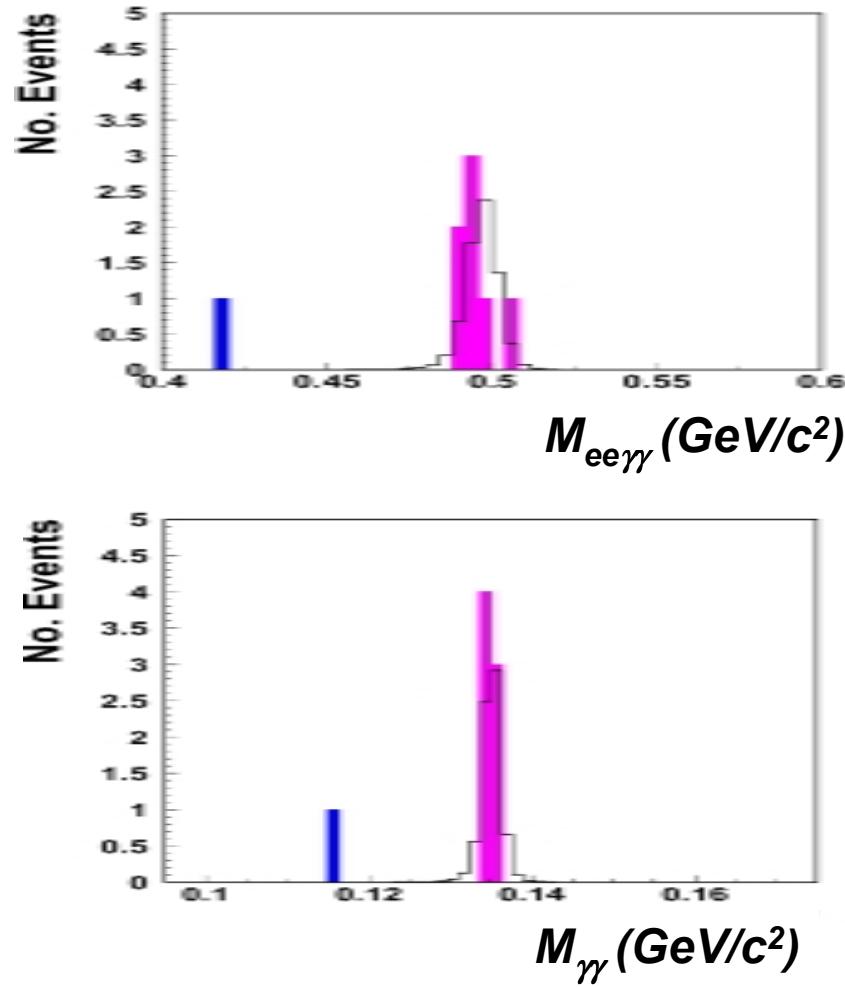
- 0 in control region
- Background 0.15

The probability that all 7 events are background is  $\sim 10^{-10}$



First observation of  $K_S \rightarrow \pi^0 ee$

# The 7 $K_S \rightarrow \pi^0 ee$ candidates



# $K_S \rightarrow \pi^0 ee$

Accepted for publication by PLB

$$BR(K_S \rightarrow \pi^0 ee, m_{ee} > 165 \text{ MeV}/c^2) = (3.0^{+1.5}_{-1.2}(\text{stat}) \pm 0.1(\text{syst})) \times 10^{-9}$$

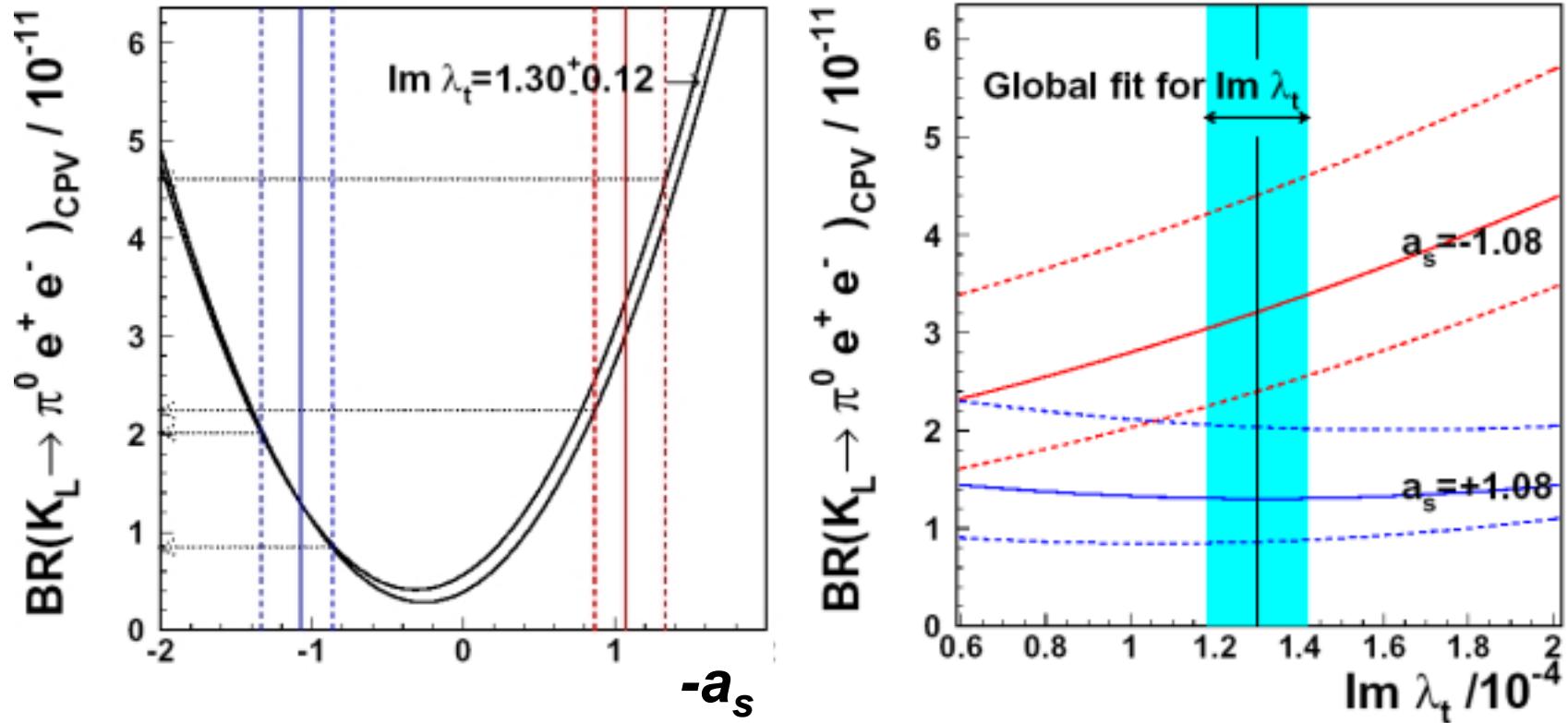
- Assuming vector interaction and unity form factor:

$$BR(K_S \rightarrow \pi^0 ee) = (5.8^{+2.8}_{-2.3}(\text{stat}) \pm 0.8(\text{syst})) \times 10^{-9}$$

- In remarkable agreement with L. Sehgal prediction:  $\sim 5.5 \times 10^{-9}$   
NP B19 (1970)
- In the notation of D'Ambrosio et al. JHEP 08 (1998) 004):
- $BR(K_S \rightarrow \pi^0 ee) \sim 5 |a_s|^2$

$$|a_s| = 1.06^{+0.26}_{-0.21} (\text{stat}) \pm 0.05 (\text{syst})$$

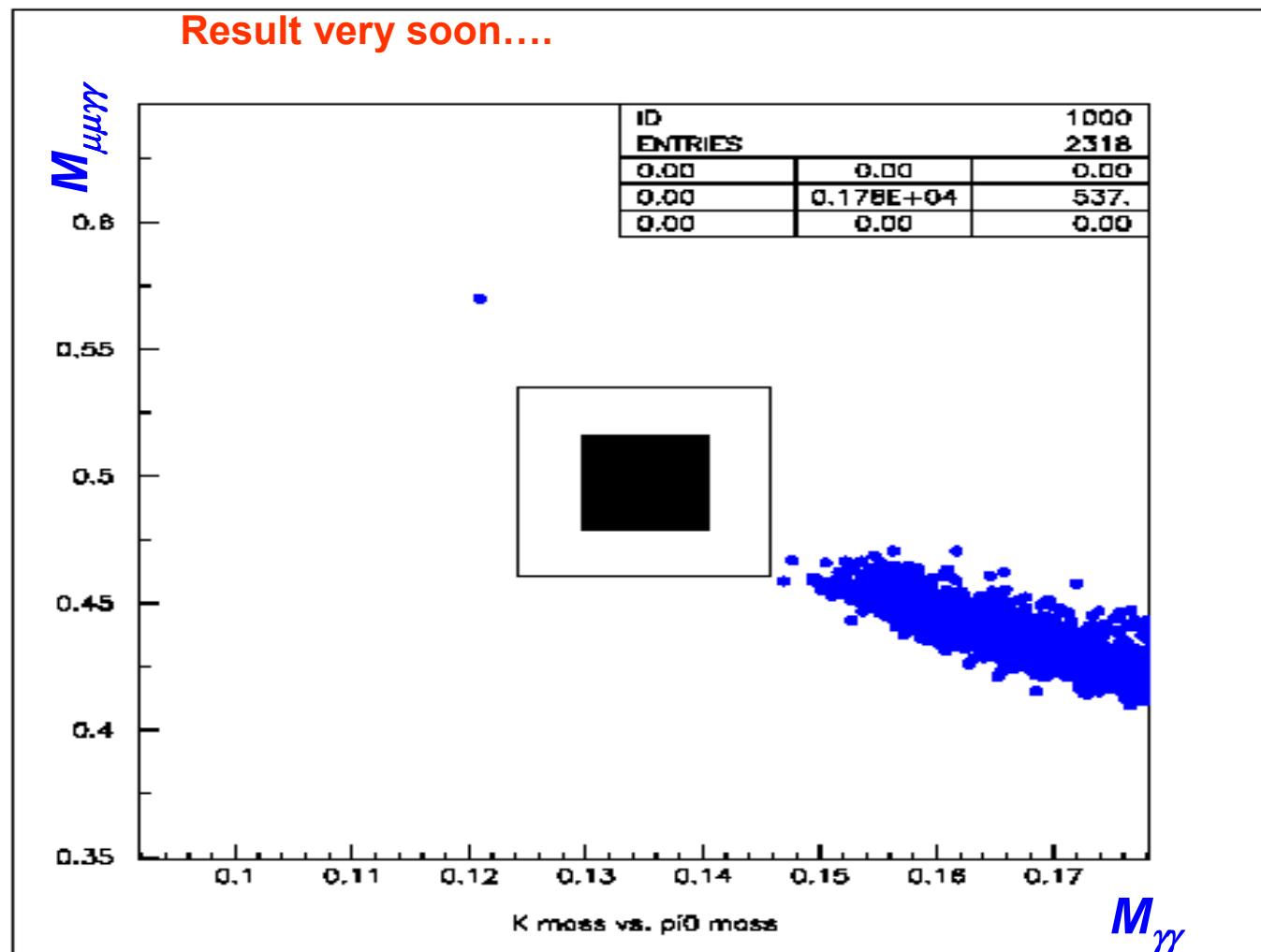
# Sensitivity to $\text{Im } \lambda_t$



$$B(K_L \rightarrow \pi^0 e^+ e^-)_{\text{CPV}} \times 10^{12} \approx 15.3 a_s^2 - 6.8 a_s \frac{\text{Im}(\lambda_t)}{10^{-4}} + 2.8 \left( \frac{\text{Im}(\lambda_t)}{10^{-4}} \right)^2$$

IF the interference is constructive some sensitivity to  $\text{Im } \lambda_t$  is retained

$$K_S \rightarrow \pi^0 \mu\mu$$

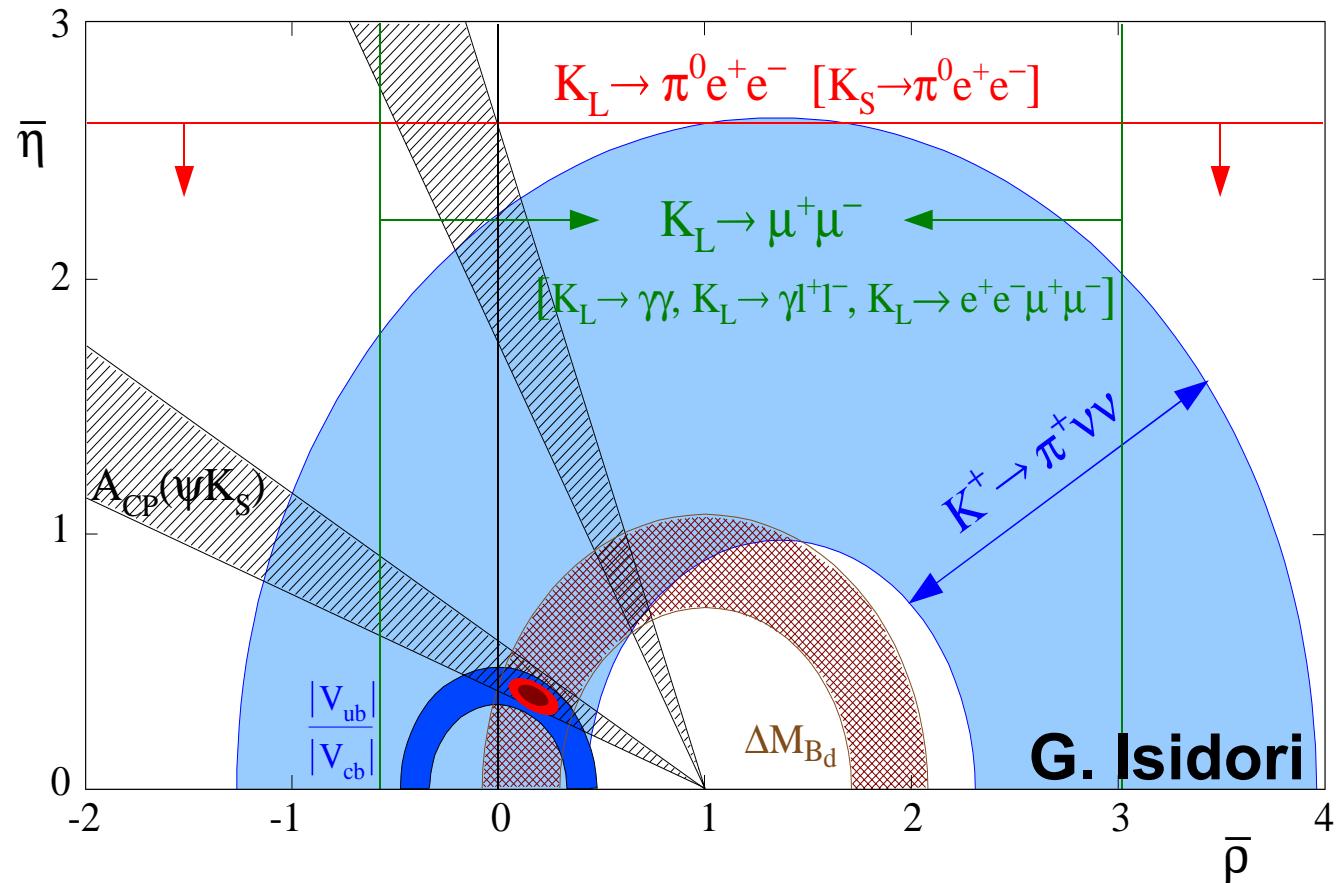


# $K_L \rightarrow \pi^0 ee(\mu\mu)$ Perspectives

\*Admittedly aggressive Road Map\*

- **Detector  $\sigma(\gamma\gamma) \times 2$** 
  - Very ambitious, KTeV/NA48 already state of the art
- **$K_S$ - $K_L$  time dependent interference  $\times 2$** 
  - Position experiment between 9 and 16  $K_S$  lifetimes  
(hep-ph/0107046)
- **$K_S$ - $K_L$  time independent interference  $\times 3$** 
  - Assume constructive interference (theoretically preferred)
- **Data Taking  $\times 5$** 
  - Run in “factory mode”. After all E799-II run only for a few months to collect  $\sim 7 \times 10^{11}$   $K_L$  decays
- **Beam intensity  $\times 4$** 
  - Need  $\sim 10^{12}$  protons/sec, slowly extracted, high energy, DC
- **Tot  $\sim \times 240 \rightarrow$  sens $\sim \times 15$** 
  - close the gap between current upper limit and SM
- **Where? When?**

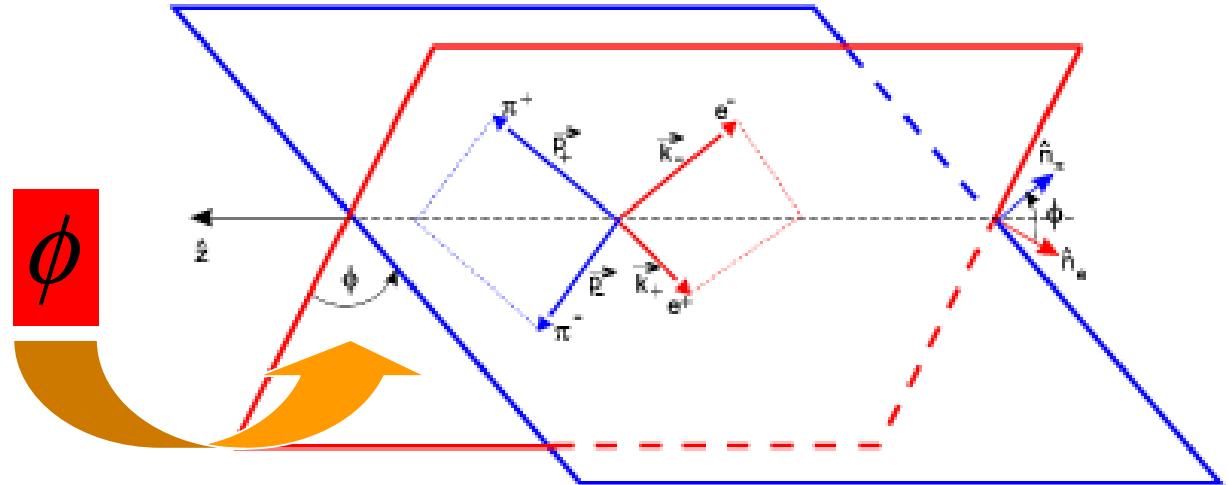
# Current Status



STILL A LARGE WINDOW OF OPPORTUNITY EXISTS

# Motivation for $K_L \rightarrow \pi\pi\gamma^*$ measurement

Interference between IB and DE in  $K_L \rightarrow \pi\pi\gamma^*$  gives rise to CPV asymmetry in  $\phi$  distribution



$$\frac{d\Gamma}{d\phi} = \Gamma_1 \cos^2 \phi + \Gamma_2 \sin^2 \phi + \Gamma_3 \sin \phi \cos \phi$$

**CP-odd:**

$$CP[\sin \phi \cos \phi] = -\sin \phi \cos \phi$$

**COUNT:**

$$N_+ \equiv N(\cos \phi \sin \phi > 0)$$

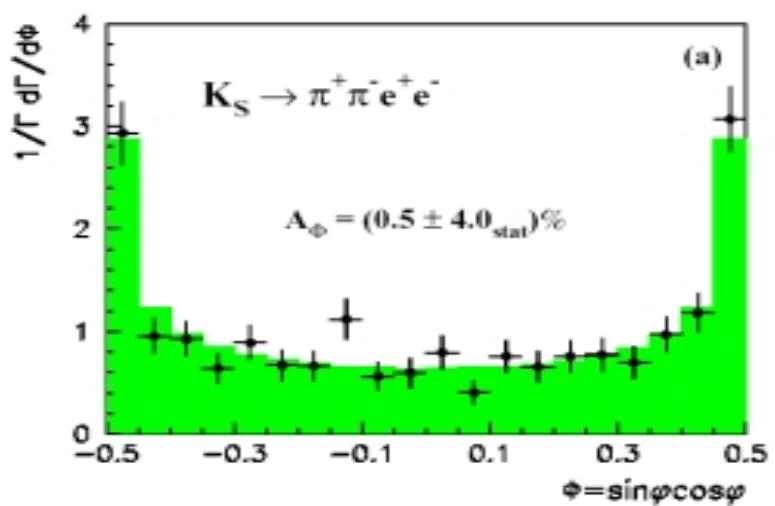
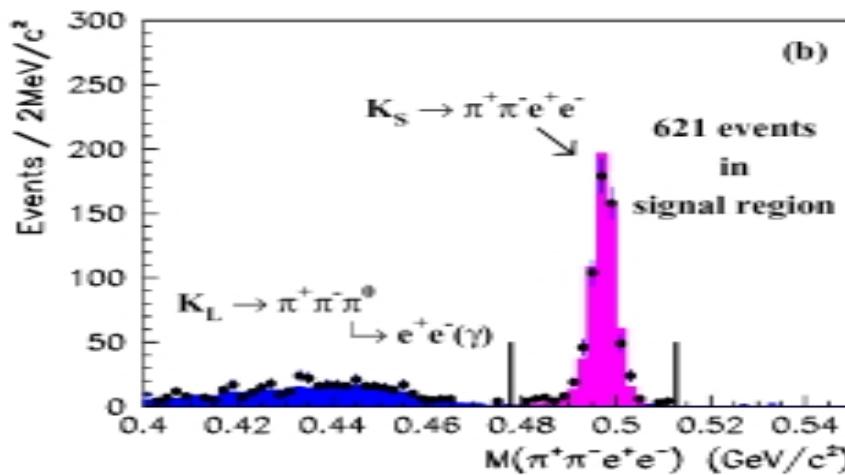
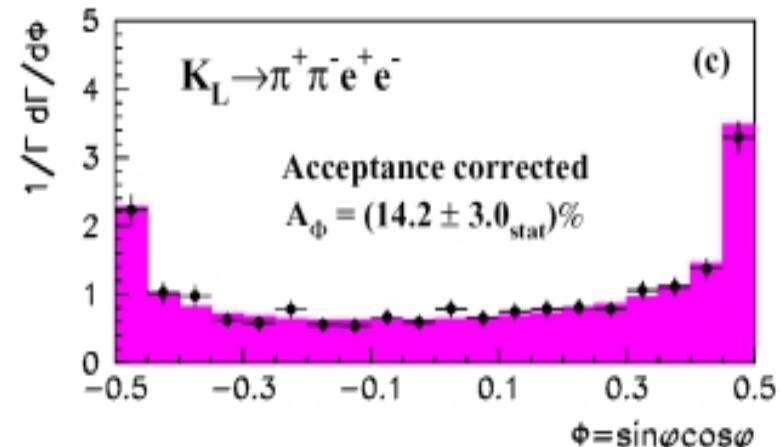
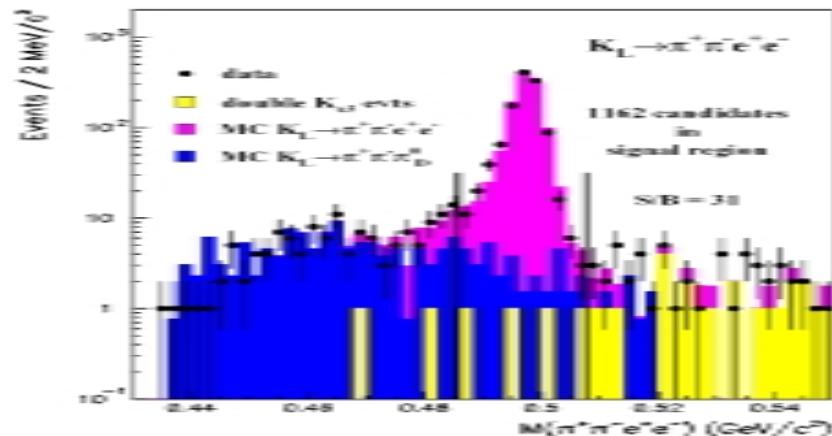
$$N_- \equiv N(\cos \phi \sin \phi < 0)$$

**CALCULATE:**

$$A = \frac{N_+ - N_-}{N_+ + N_-}$$

← Predicted: 14%,  
 $BR=3.1 \cdot 10^{-7}$ .  
*L.M.Sehgal, M.Wanniger, 1992*

# $K_{L,S} \rightarrow \pi\pi ee$



# $K_{L,S} \rightarrow \pi\pi ee$ branching ratios

The events are normalised to reconstructed Dalitz decays with the known  
 $BR = (1.5 \pm 0.05) \times 10^{-3}$

$K_L :$

$$BR = (3.08 \pm 0.09_{\text{stat}} \pm 0.15_{\text{syst}} \pm 0.10_{\text{norm}}) \times 10^{-7}$$
$$= (3.08 \pm 0.20) \times 10^{-7}$$

$K_S :$

621 evts.

$$BR_{1999} = (4.71 \pm 0.23_{\text{stat}} \pm 0.16_{\text{syst}} \pm 0.15_{\text{norm}}) \times 10^{-5}$$

$$BR_{1998} = (4.5 \pm 0.7_{\text{stat}} \pm 0.4_{\text{syst}}) \times 10^{-5}$$

$$= (4.69 \pm 0.30) \times 10^{-5}$$

Used to estimate:  $BR(K_L \rightarrow \pi\pi ee)_{IB} = (1.4 \pm 0.1) \times 10^{-7}$

# $K_S \rightarrow 3\pi^0$

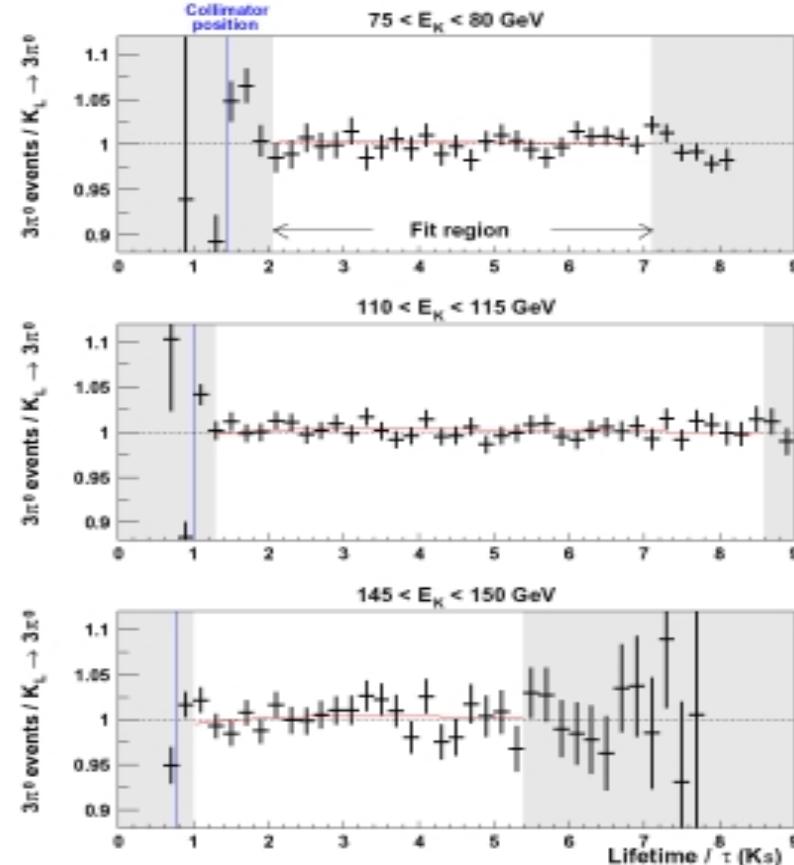
$$\eta_{000} = \frac{A(K_s \rightarrow 3\pi^0)}{A(K_L \rightarrow 3\pi^0)}$$

CP-Violating  
In SM  $\eta_{000} \sim \epsilon$

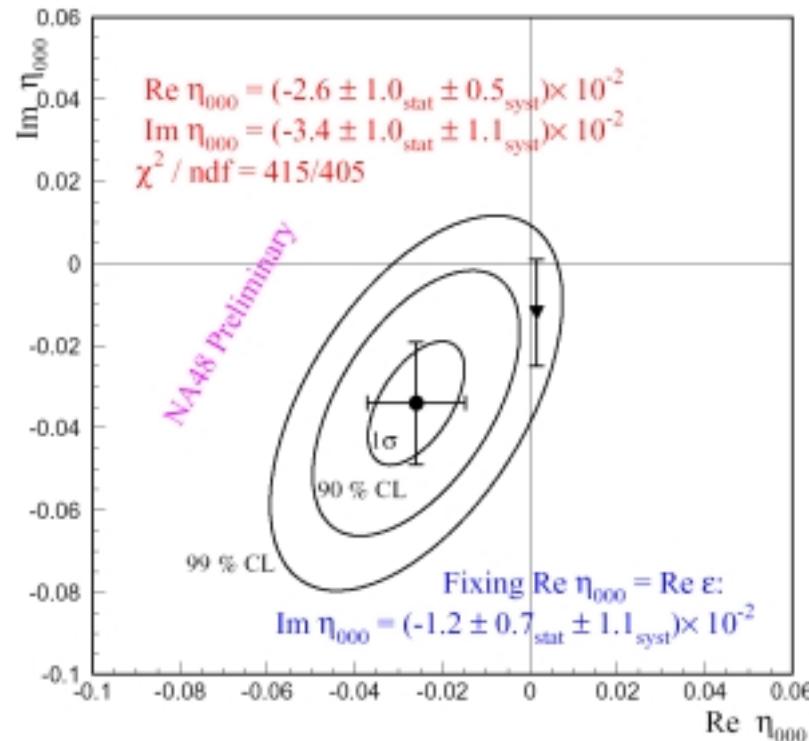
- Near Beam
  - NA48/1 (2000)  $\sim 6.5 \cdot 10^6 3\pi^0$
- Far Beam:
  - NA48 2000  $> 10^7 K_L \rightarrow 3\pi^0$
  - To normalise the acceptance
- Analysis in bins of energy

$$f(E, t) = \frac{NEAR}{FAR} = A(E) \left[ 1 + |\eta_{000}|^2 e^{(\Gamma_L - \Gamma_S)t} + 2D(E) e^{\frac{1}{2}(\Gamma_L - \Gamma_S)t} (\text{Re}\eta_{000} \cos \Delta m t - \text{Im}\eta_{000} \sin \Delta m t) \right]$$

D(E) is the  $K^0 \bar{K}^0$  dilution (from NA31)



# $K_S \rightarrow 3\pi^0$

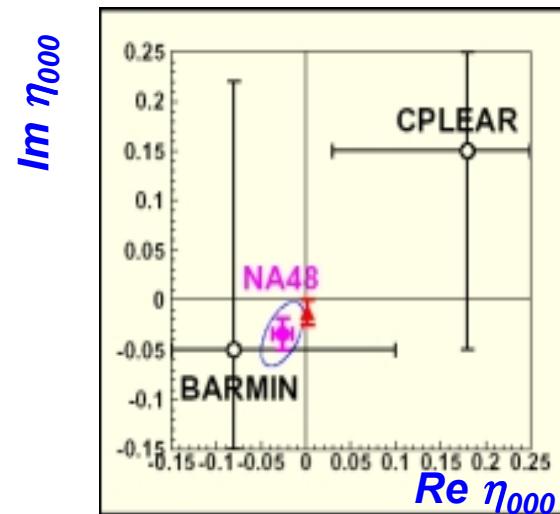


CPT TEST:  $K_L \sim (\varepsilon + \delta_{\text{CPT}}) K_1 + K_2$   
 $K_S \sim K_1 + (\varepsilon - \delta_{\text{CPT}}) K_2$

From the 2 parameter fit,  
using BS unitarity relation:

$$\text{Im } \delta_{\text{CPT}} = (-1.2 \pm 3.0) \times 10^{-5}$$

Assuming CPT conservation in decay:  
 $M(K^0) - M(\bar{K}^0) = (-1.7 \pm 4.2) \times 10^{-19} \text{ GeV}/c^2$

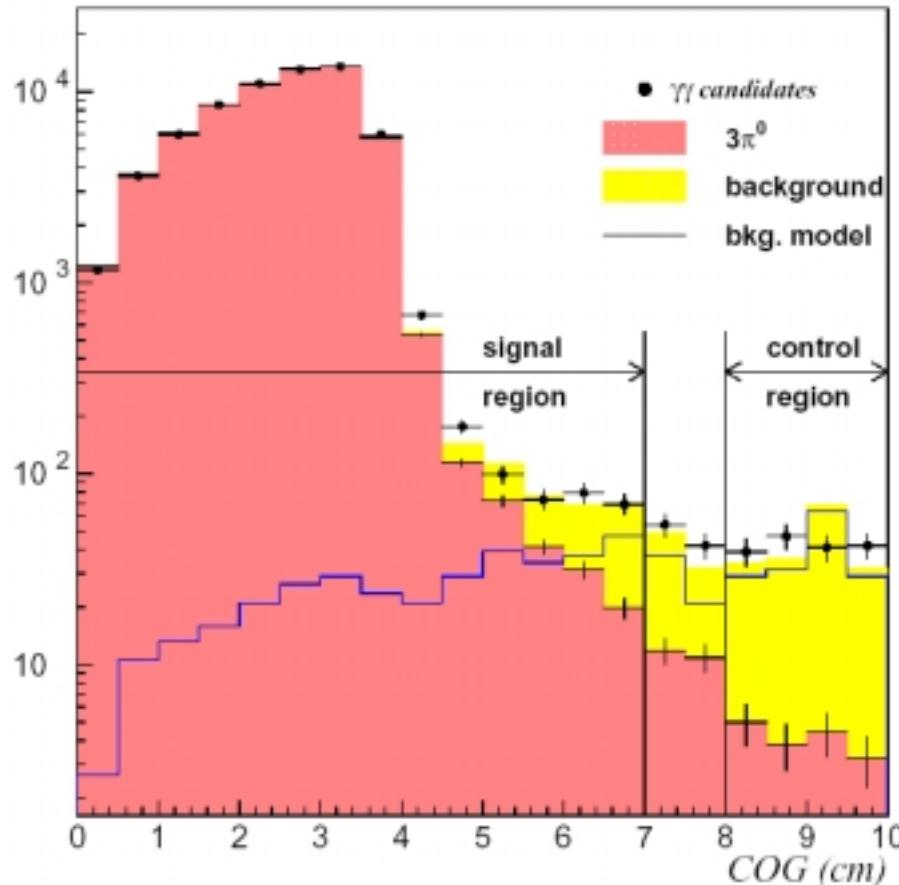


From one parameter fit:

$$BR(K_S \rightarrow 3\pi^0) < 3.0 \times 10^{-7} \text{ 90%CL}$$

$$BR_{SM} \sim 3 \times 10^{-9}$$

# $K_L \rightarrow \gamma\gamma$

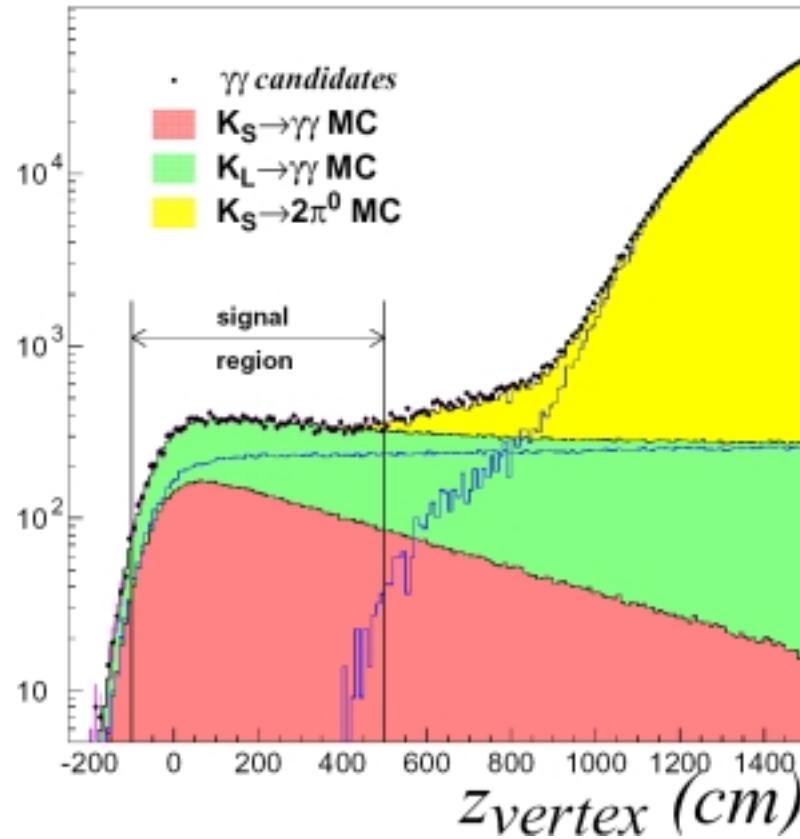


- **Data 2000**
  - sub-sample of  $K_L$  data
- **Background:**
  - Hadronic origin
  - $0.6 \pm 0.3 \%$
- **Main systematics:**
  - calorimeter response for the acceptance calculation

$$\Gamma(K_L \rightarrow \gamma\gamma) / \Gamma(K_L \rightarrow \pi^0\pi^0\pi^0) = (2.81 \pm 0.01_{\text{stat}} \pm 0.02_{\text{syst}}) \times 10^{-3}$$

4 times better precision than PDG:  $(2.77 \pm 0.08) \times 10^{-3}$

# $K_S \rightarrow \gamma\gamma$

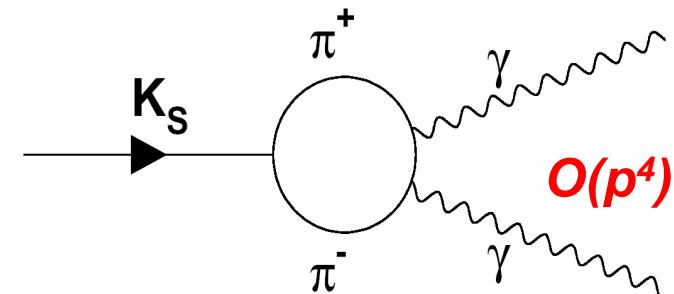
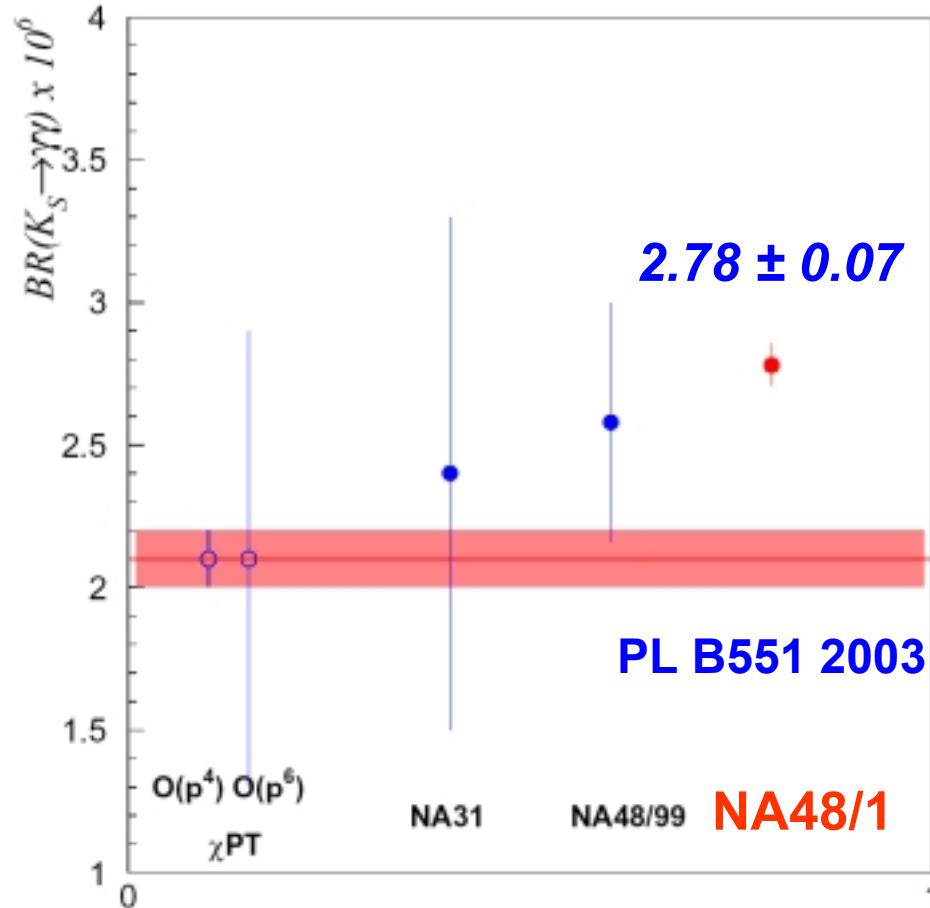


- **Impose  $m_K$  to compute decay vertex**
- **Background due to missing particles shifted downstream**
- **Keep short decay region (~5m)**
- **Total background ~ 4%**
- **Subtract  $K_L \rightarrow \gamma\gamma$  measuring the  $K_L \rightarrow 3\pi^0$  flux and using newly measured  $BR(K_L \rightarrow \gamma\gamma)$**

$$BR(K_S \rightarrow \gamma\gamma) = (2.78 \pm 0.06_{stat} \pm 0.03_{syst} \pm 0.02_{ext}) \times 10^{-6}$$

PLB 551 (2003)

# $K_S \rightarrow \gamma\gamma$ measurements



The NA48/1 result has an accuracy better than 3%

It differs by 30% from  $O(p^4)$  prediction of CHPT

Used to fix one  $O(p^6)$  counterterm:

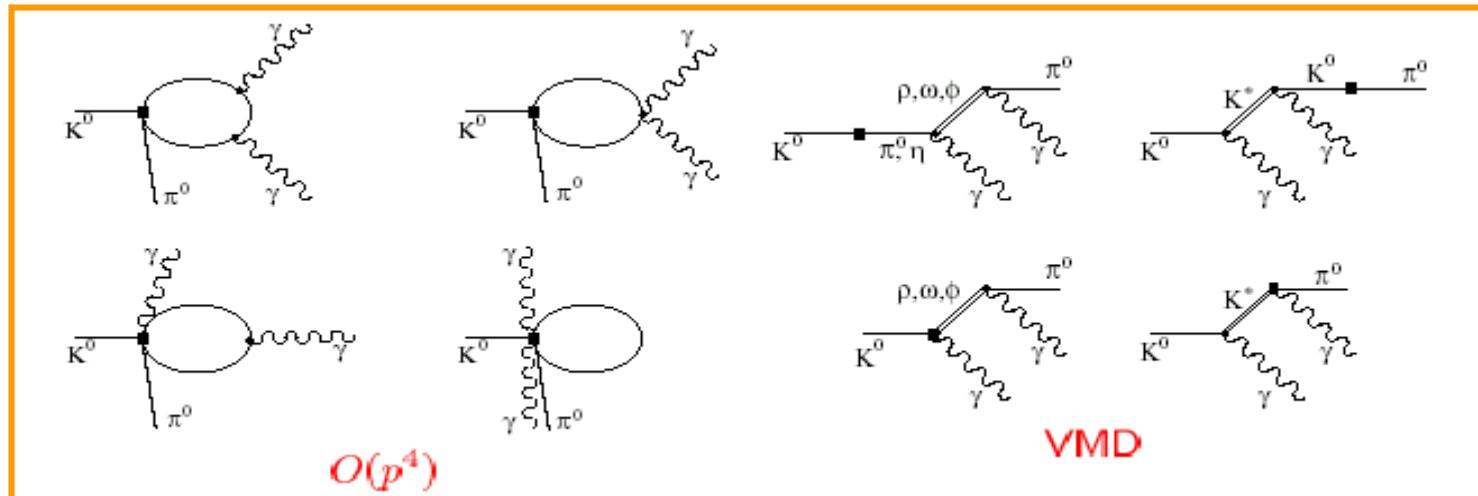
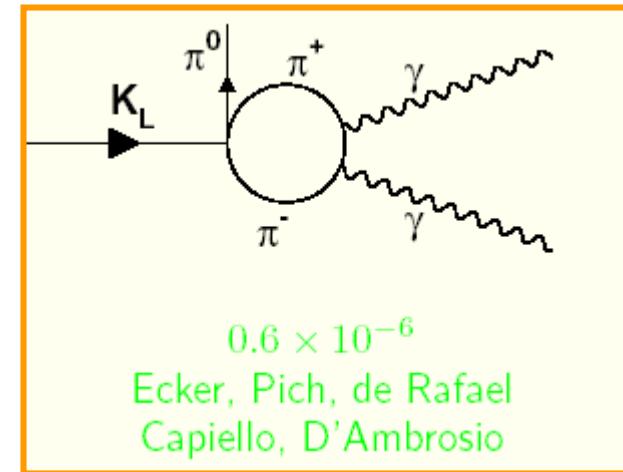
$$8m_K^2/F_\pi^2 a_1 = 1.0 \pm 0.3$$

BDI (hep-ph/0308008)

# $K_L \rightarrow \pi^0 \gamma \gamma$ decay

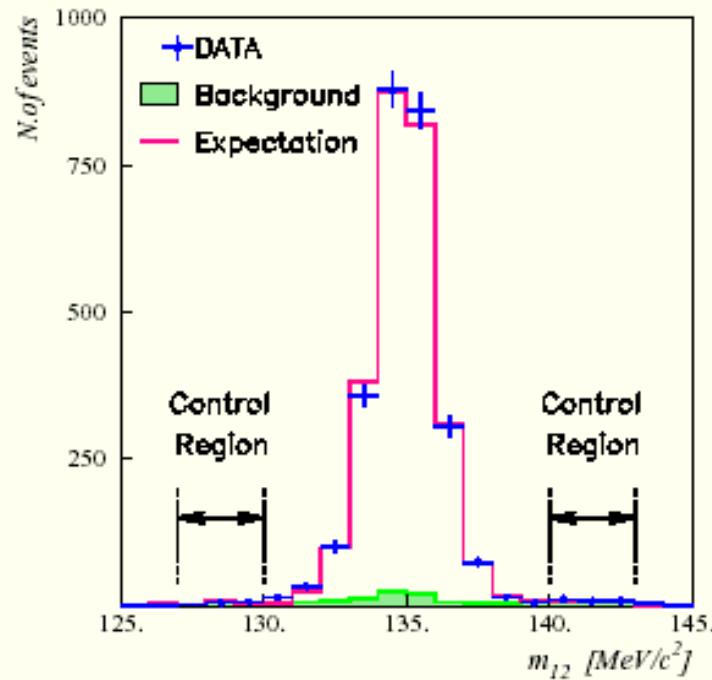
- Only 1/3 of the measured  $K_L \rightarrow \pi^0 \gamma \gamma$  rate is predicted by  $O(p^4)$ .

- The rate can be reproduced at  $O(p^6)$  including vector mesons exchange.
- The VMD contribution is parametrised by  $a_V$ , which has to be experimentally determinated.

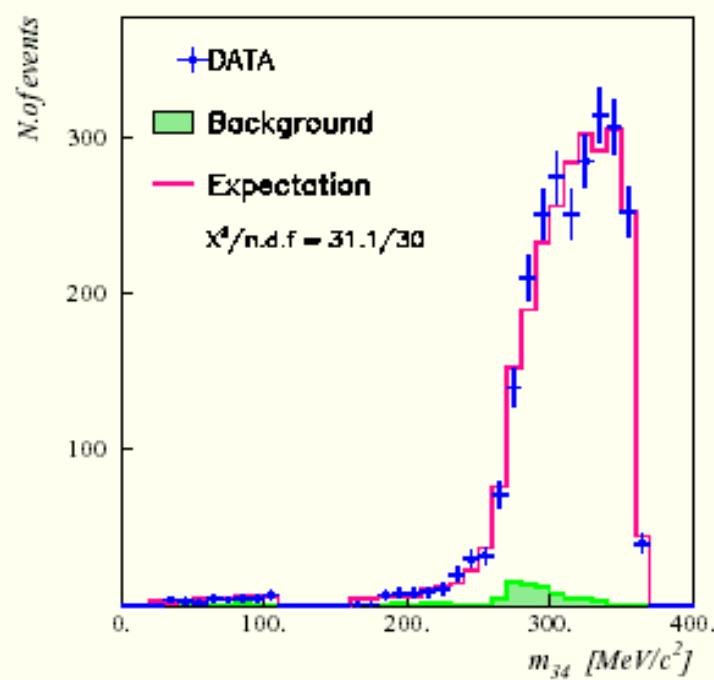


# $K_L \rightarrow \pi^0 \gamma \gamma$

$m_{\gamma\gamma}$  for the  $\pi^0$  candidates



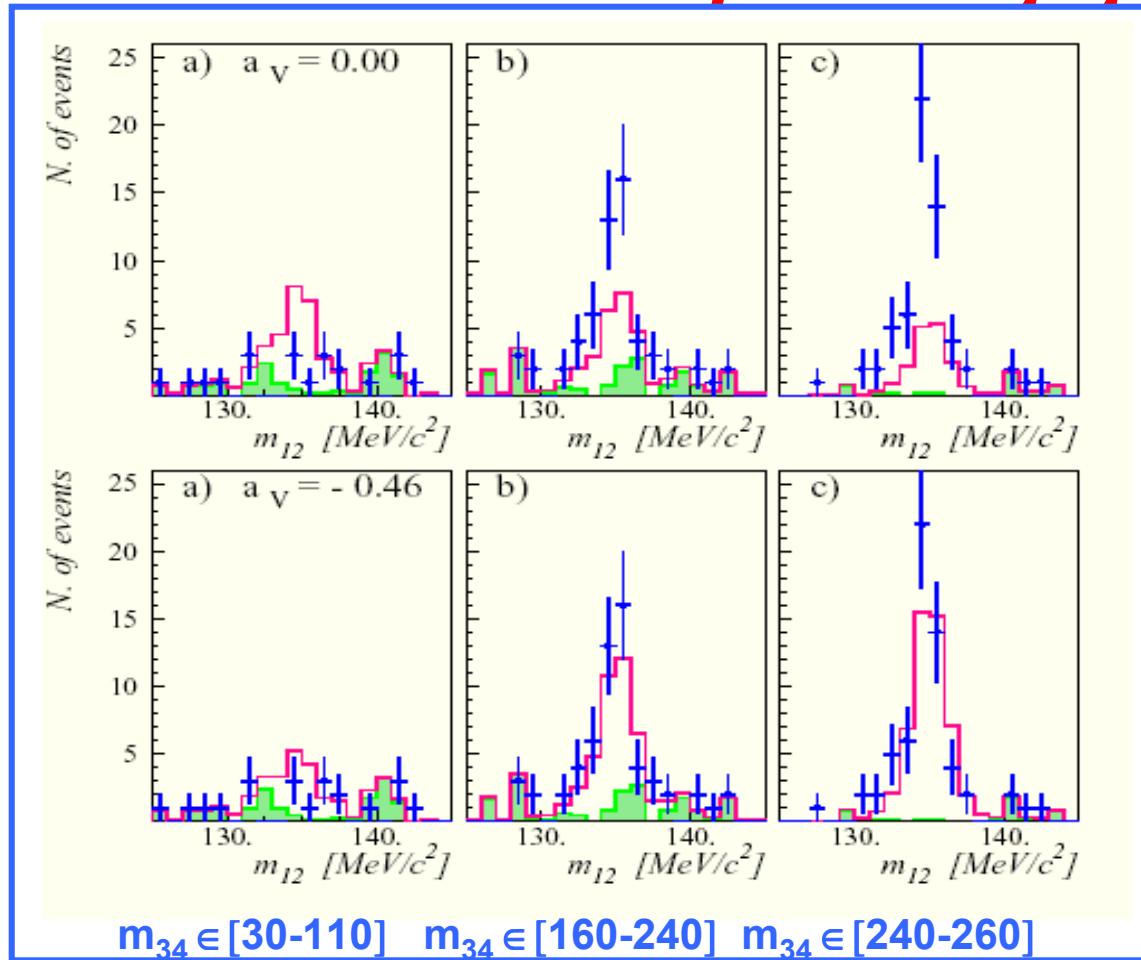
$m_{\gamma\gamma}$  for the two non-  $\pi^0$  photons



$$a_v = -0.46 \pm 0.03_{\text{stat}} \pm 0.04_{\text{syst}}$$

$$BR(K_L \rightarrow \pi^0 \gamma \gamma) = (1.36 \pm 0.03_{\text{stat}} \pm 0.03_{\text{syst}} \pm 0.03_{\text{norm}}) \times 10^{-6}$$

# $K_L \rightarrow \pi^0 \gamma \gamma$

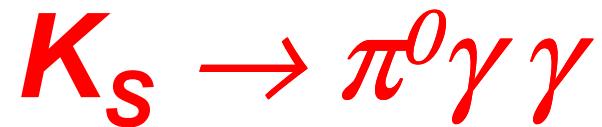


⇒ Implies very small  
CP conserving  
amplitude in  
 $K_L \rightarrow \pi^0 e^+ e^-$

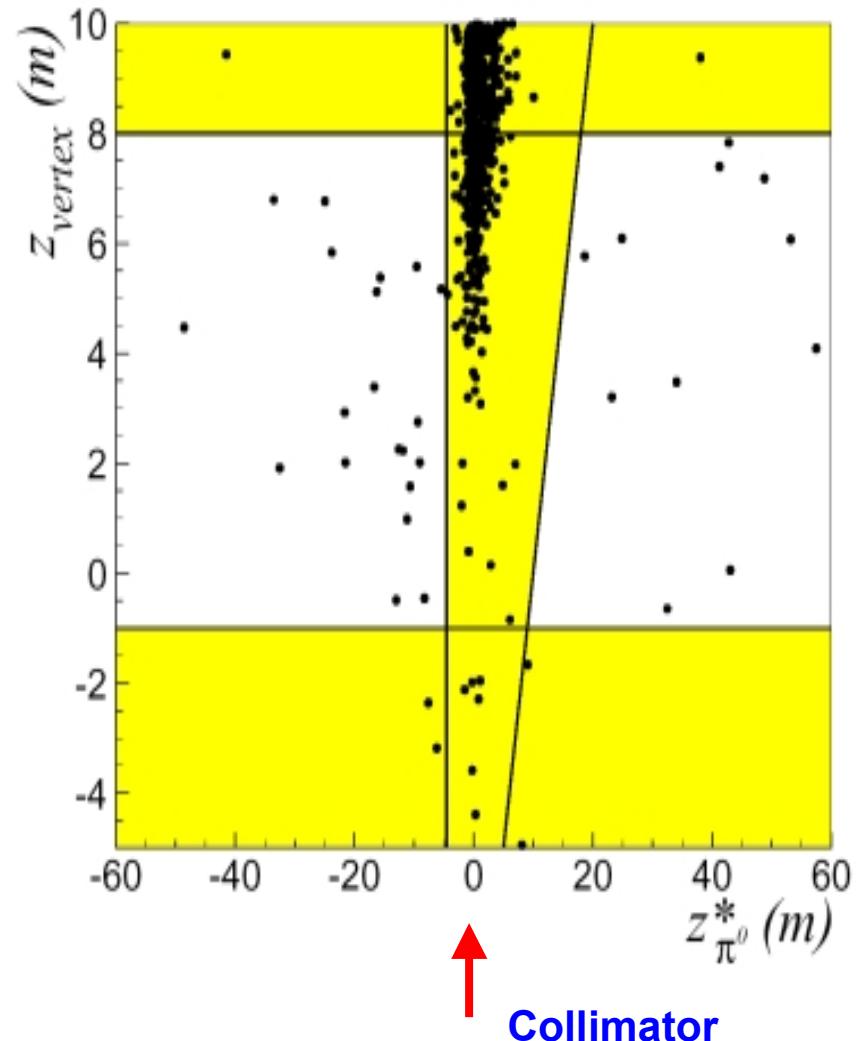
KTeV results (PRL 83 (99) 917):

$$a_v = -0.72 \pm 0.05_{stat} \pm 0.06_{syst}$$

$$BR(K_L \rightarrow \pi^0 \gamma \gamma) = (1.68 \pm 0.07_{stat} \pm 0.08_{syst}) \times 10^{-6}$$



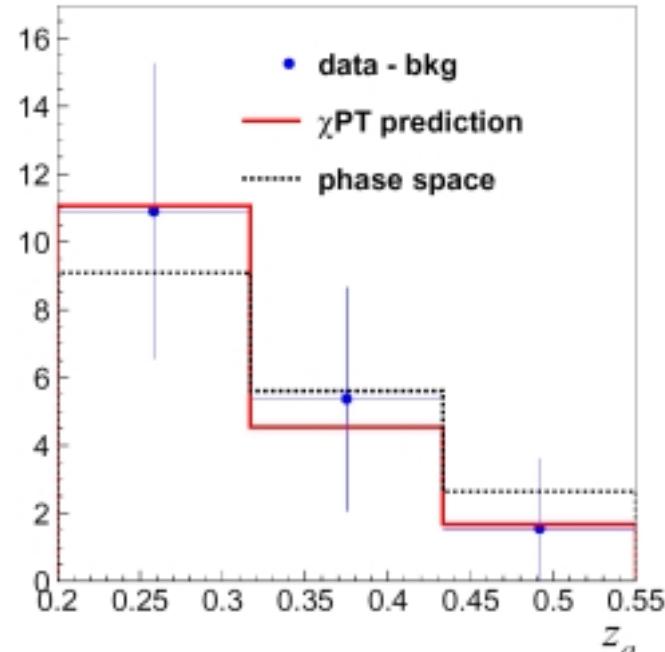
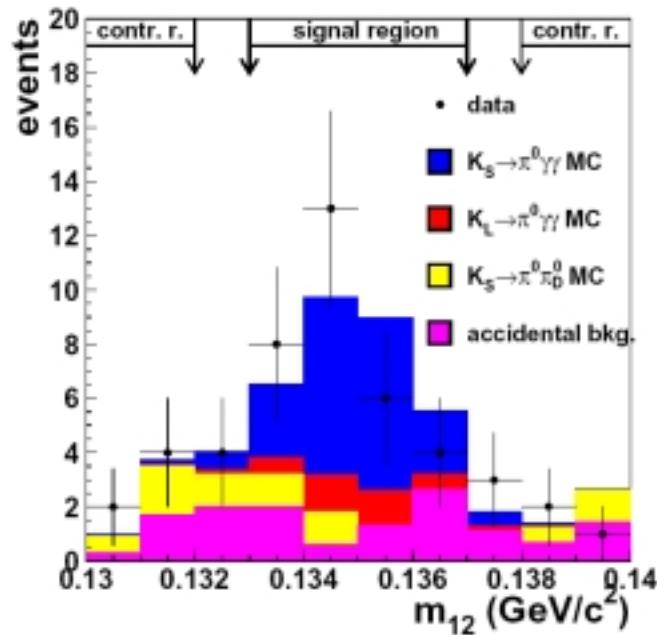
- The rejection of the Dalitz decays is complicated since no drift chambers were available during Y2K
- Fiducial region:  $-1 \leftrightarrow 8$  m
- $Z_{\pi^0}^*$  = vertex reconstructed pairing 2  $\gamma$  assuming  $\pi^0$  mass
- Impose  $m_K$  to reconstruct decay vertex
- Events from Kaon decays with missing particles are reconstructed downstream



# $K_S \rightarrow \pi^0 \gamma \gamma$

first observation

CERN-EP/2003-052 (hep-ex/0309022)



$$Z_q = q^2/M_K^2$$

$$BR(K_S \rightarrow \pi^0 \gamma \gamma, Z_q > 0.2) = (4.9 \pm 1.6_{\text{stat}} \pm 0.9_{\text{syst}}) \times 10^{-8}$$

CHPT predicts (Ecker, Pich and De Rafael, PLB 189 1987):

$$BR(K_S \rightarrow \pi^0 \gamma \gamma)_{zq > 0.2} = 3.8 \times 10^{-8}$$

# Outlook

- NA48
  - $\varepsilon'/\varepsilon$ 
    - Experiment is complete: Direct CP-violation demonstrated to >6 standard deviations  $\text{Re } \varepsilon'/\varepsilon = 14.7 \pm 2.2 \times 10^{-4}$
  - Rare  $K_L$  decays
    - expects results on  $K_L$  Dalitz decays ( $K_L \rightarrow ee\gamma$ ,  $K_L \rightarrow eeee$ ) and  $Ke4$
- NA48/1
  - Expect new results soon, in particular:
    - $K_S \rightarrow \pi^0 \mu\mu$  (VERY SOON!)
    - Semi-leptonic Neutral Cascade decays
- NA48/2
  - charged kaons (see Marco Sozzi's report)
- NA48/3 ??
  - CERN is currently the only place where high energy kaon beams could be employed to exploit:
    - Very good energy resolution (essential for  $K_L \rightarrow \pi^0 ee (\mu\mu)$ )
    - Very good photon vetoing (essential for  $K \rightarrow \pi \nu\nu$ )

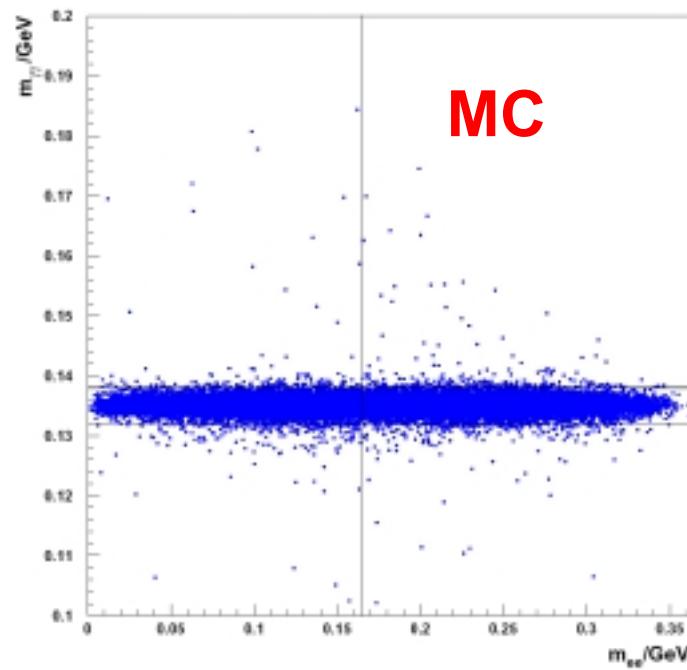
# Why study Rare Kaon Decays

- **Search for explicit violation of Standard Model**
    - Lepton Flavour Violation (e.g. BNL-E865, BNL-E871)
  - **Probe the flavour sector of the Standard Model**
    - FCNC (e.g. BNL-E787)
  - **Test fundamental symmetries**
    - CP, CPT
  - **Study the strong interactions at low energy**
    - Chiral Perturbation Theory
- 
- I will give a review of recent results obtained by NA48 ( $K_L$ ) and NA48/1 ( $K_S$ )
    - $K_S$  rare decays ( $BR \leq 10^{-8}$ ) start to be studied

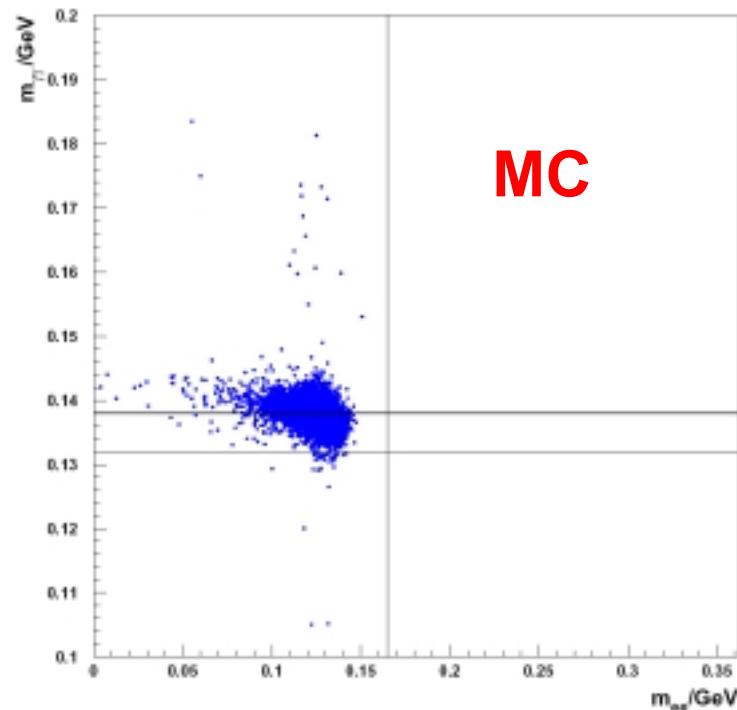
# **Spare Material**

# $K_S \rightarrow \pi^0 ee$

$K_S \rightarrow \pi^0 ee$



$K_S \rightarrow \pi^0 \pi^0_D \rightarrow \gamma \gamma ee(\gamma)$

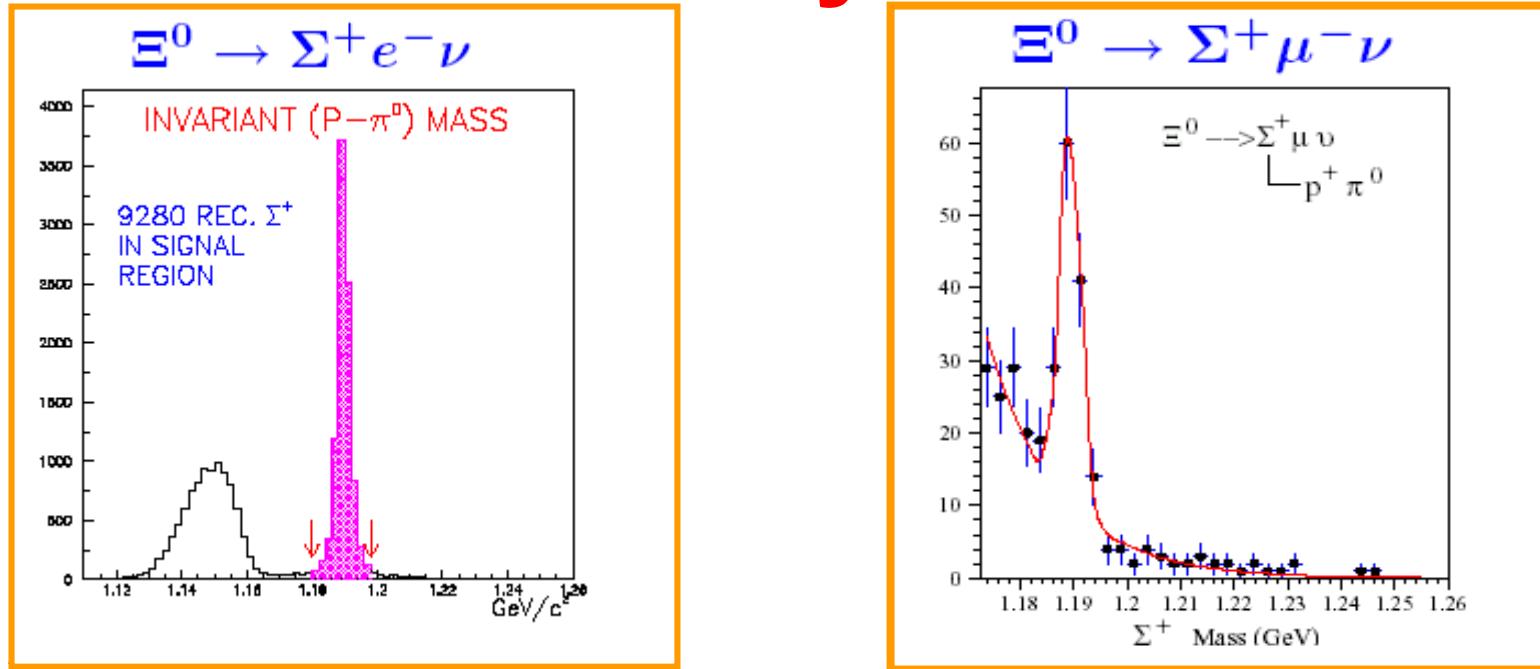


- To reject the  $K_S \rightarrow \pi^0 \pi^0_D$  decays that may mimic  $K_S \rightarrow \pi^0 ee$  if a  $\gamma$  is lost, a cut  $m_{ee} > 0.165 \text{ GeV}/c^2$  is applied

# Chiral Perturbation Theory

- ChPT is the effective field theory of the Standard Model at low energy ( $E < 1$  GeV region of non-perturbative QCD)
- Chiral symmetry of the QCD Lagrangian is spontaneously broken  
⇒ degree of freedom of the theory are eight pseudoscalar Goldstone bosons ( $\pi, \eta, K$ )
- Processes described in perturbative expansion of momenta and masses
- Higher order boson loops are divergent, but compensated by counter-terms with (empirically determinated) effective couplings
- $K_{L,S} \rightarrow \pi^0 \gamma \gamma$ ,  $K_{L,S} \rightarrow \gamma \gamma$  are good tools to probe ChPT

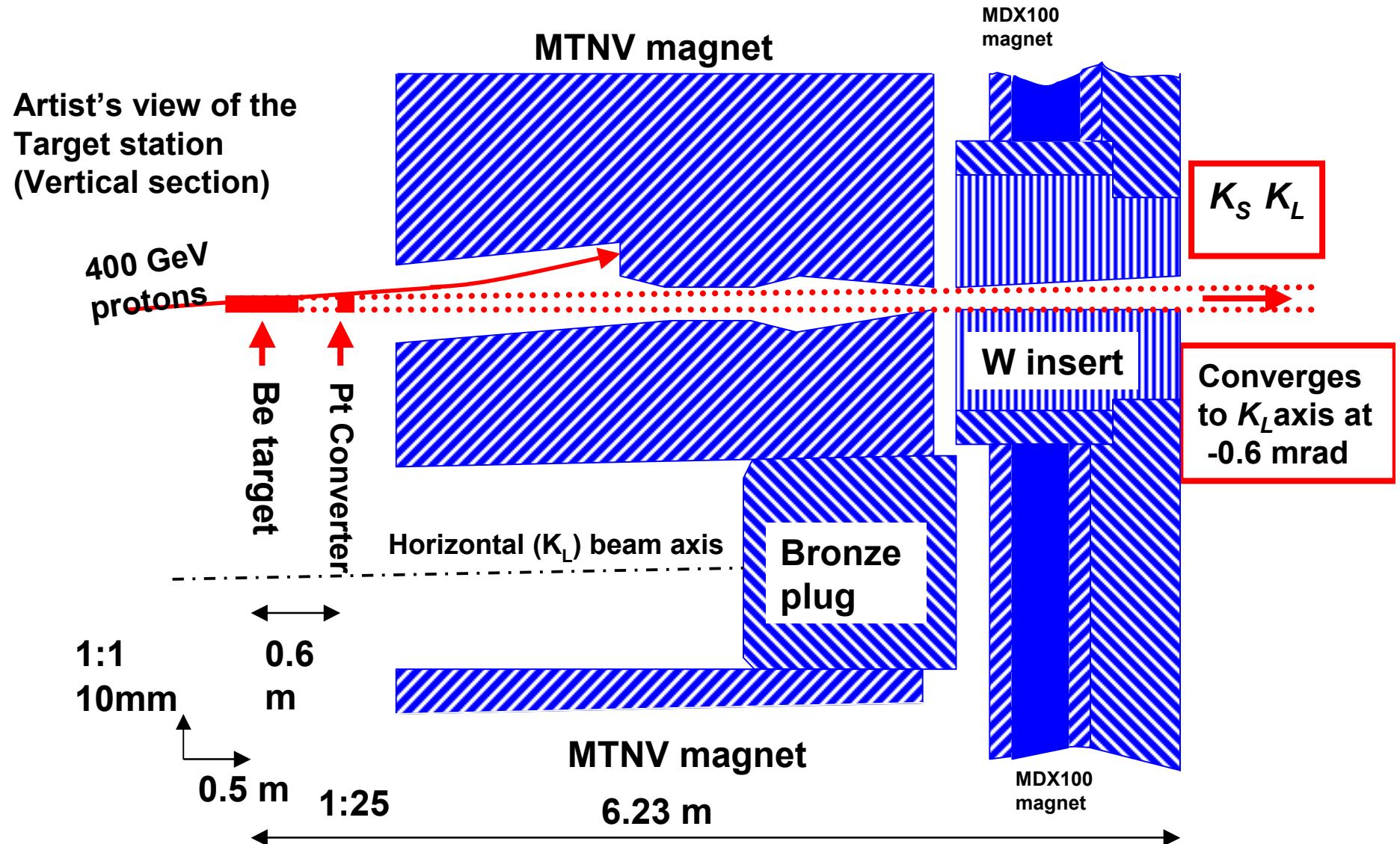
# $\Xi^0$ beta decays : $\Xi^0 \rightarrow \Sigma l \nu$

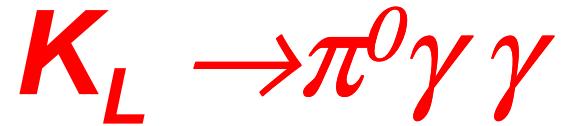


Study the rate and the form-factors (  $V_{us}$  )

- Run 2002 not optimized for hyperons
- $\Xi^0 \rightarrow \Sigma e \nu$  clean sample: Signal/Back  $\sim 40$ ,  $\sim 9000$  events after cuts
- Currently published sample (KTeV): BR 176 evts, FF 487
- $\Xi^0 \rightarrow \Sigma \mu \nu$  first experimental evidence

# CERN-NA48/1: High Intensity $K_S$





Rare process without a clear signature. Data from 1998 and 1999  $\varepsilon'/\varepsilon$  runs.

- **Background sources :**
  - $K_L \rightarrow \pi^0 \pi^0$  with mis-reconstructed showers;  $m_\pi^0$  mass cut ; residual background evaluated from the tagged  $K_S \rightarrow \pi^0 \pi^0$  events  $(0.16 \pm 0.08) \%$
  - $K_L \rightarrow \pi^0 \pi^0 \pi^0$  with missing or overlapping showers; shower width cut and vertex position cut assuming background hypothesis; residual background evaluated from a MC sample of  $3 \times 10^9$  events  $(2.74 \pm 0.42) \%$
  - **pile-up events** e.g. two decays occurring within 3 ns; quantified from the tails of the  $R_{cog}$  distribution from good  $\pi^0 \pi^0$  events  $(0.32 \pm 0.21) \%$

# NA48: all $\varepsilon'/\varepsilon$ results

From 2001 data:

$$\text{Re}(\varepsilon'/\varepsilon) = (13.7 \pm 2.5_{\text{stat}} \pm 1.1_{\text{syst,stat}} \pm 1.5_{\text{syst}}) \times 10^{-4}$$

Combining with 97+98+99 result

$$\text{Re}(\varepsilon'/\varepsilon) = (15.3 \pm 1.6_{\text{stat}} \pm 1.3_{\text{syst,stat}} \pm 1.6_{\text{syst}}) \times 10^{-4}$$

$$\boxed{\text{Re}(\varepsilon'/\varepsilon) = (14.7 \pm 1.3_{\text{stat}} \pm 1.0_{\text{syst,stat}} \pm 1.5_{\text{syst}}) \times 10^{-4}}$$

# NA48 (2001): systematics on R

Table 1

Corrections and systematic uncertainties on the double ratio  $R$  (2001 data)

	in $10^{-4}$		
$\pi^+\pi^-$ trigger inefficiency	+5.2	$\pm 3.6$	(stat)
AKS inefficiency	+1.2	$\pm 0.3$	
Reconstruction of $\pi^0\pi^0$	-	$\pm 5.3$	
Reconstruction of $\pi^+\pi^-$	-	$\pm 2.8$	
Background to $\pi^0\pi^0$	-5.6	$\pm 2.0$	
Background to $\pi^+\pi^-$	+14.2	$\pm 3.0$	
Beam scattering	-8.8	$\pm 2.0$	
Accidental tagging	+6.9	$\pm 2.8$	(stat)
Tagging inefficiency	-	$\pm 3.0$	
Acceptance statistical	+21.9	$\pm 3.5$	(stat)
Acceptance systematic	+21.9	$\pm 4.0$	
Accidental activity intensity difference	-	$\pm 1.1$	
Accidental activity illumination difference	-	$\pm 3.0$	(stat)
$K_S$ in time activity	-	$\pm 1.0$	
Total	+35.0	$\pm 11.0$	

# Conclusions

- The field of kaon rare decays is quite active
- New experimental initiatives are planned
- Significant tests of the SM are to be expected by the end of the decade

High Energy  
Frontier            Rare Processes

# SM Master Formula for $\epsilon'/\epsilon$

$$\frac{\epsilon'}{\epsilon} = e^{i\phi} \frac{G_F \omega}{2|\epsilon| \operatorname{Re} A_0} \operatorname{Im} \lambda_t \left[ \Pi_0 (1 - \Omega_{IB}) - \frac{1}{\omega} \Pi_2 \right]$$

$$\omega = \frac{A(K_S \rightarrow \pi\pi, I=2)}{A(K_S \rightarrow \pi\pi, I=0)} \approx 0.045 \quad \phi = \frac{\pi}{2} + \delta_2 - \delta_0 \approx 0^\circ$$

$$\Pi_0 = \frac{1}{\cos \delta_0} \sum_i y_i \operatorname{Re} \langle Q_i \rangle_0 \quad \Pi_2 = \frac{1}{\cos \delta_2} \sum_i y_i \operatorname{Re} \langle Q_i \rangle_2$$

- 1976 Ellis, Gaillard and Nanopoulos:  $\epsilon'/\epsilon > 0$  is expected in the CKM description
- Gluonic Pinguins can lead to large  $\epsilon'/\epsilon$
- Large top mass → contribution of EW Pinguins leads to cancellations
- Short distance physics is in the Wilson Coefficients  $y_i$  computed to NLO (Buras et al., Martinelli et al.)
- Low energy physics in the hadronic matrix elements  $Q_i$ : to be reliably calculated by lattice QCD **WHEN?**
- Current Predictions of  $\epsilon'/\epsilon$  in SM range from  $-4$  to  $+40 \times 10^{-4}$

# CP-Violation in SM

A phase in the quark-quark current leads to  
CP-Violation (Kobayashi, Maskawa, 1973)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

$N_g=2 \quad N_{phase}=0 \Rightarrow \text{No CP-Violation}$

$N_g=3 \quad N_{phase}=1 \Rightarrow \text{CP-Violation Possible}$

$$\sum_{i=u,c,t} V_{ij} V_{ik}^* = \sum_{i=u,c,t} V_{ji}^* V_{ki} = \delta_{jk}$$

**6 unitarity relations  
(triangles in the complex plane)**

$J_{CP}=2\times(\text{Triangle Area})$  Is the unique measure of CP-Violation in SM

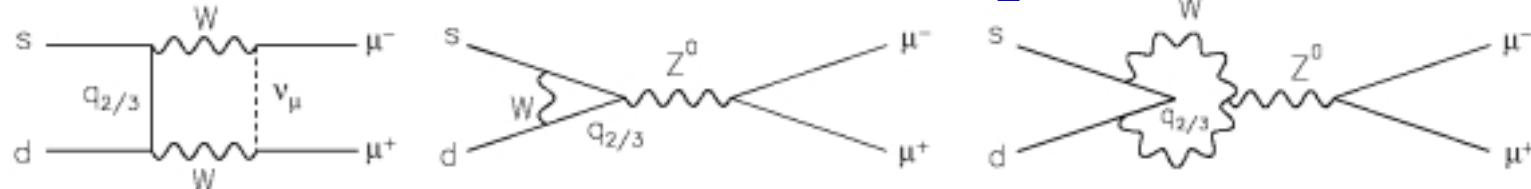
$$J_{CP} = \text{Im}(V_{ud}^* V_{us} V_{ts}^* V_{td}) = \text{Im}(\lambda_u^* \lambda_t) \sim \sin \theta_c \cos \theta_c \text{Im}(\lambda_t)$$

# Consistency of CKM picture

- **Paradigm shift:**
  - **Old question:** (before the  $\varepsilon'/\varepsilon$  and  $B \rightarrow J/\Psi K_s$  asymmetry measurements):
    - Is CKM **the source** of CP-violation?
  - **New question:**
    - Is CKM **the only** source of CP-violation?
- **Decisive tests must have small theoretical errors**
  - The opportunity is to compare information from  $K$  rare decays and  $B$  mesons

# Kaon Dalitz decays: Motivation

Short distance contributions to  $K_L \rightarrow \mu\mu$  sensitive to  $\text{Re } \lambda_t$

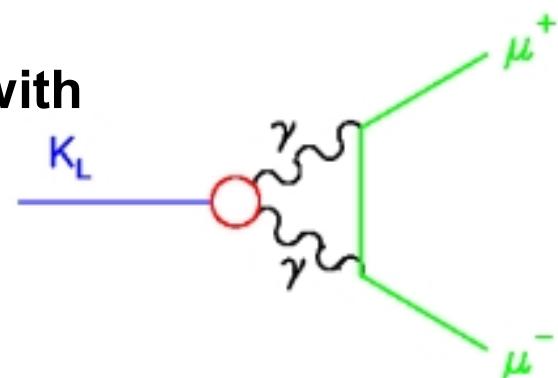


$$B_{SD}(K_L \rightarrow \mu\mu) = \frac{\tau_{K_L}}{\tau_{K^+}} \frac{\alpha^2 B(K_{\mu 2})}{\pi^2 \sin^4 \theta_W |V_{us}|^2} |Y_c \text{Re} \lambda_c + Y_t \text{Re} \lambda_t|^2 = 1.51 \times 10^{-9} A^4 (\rho_0 - \bar{\rho})^2$$

Buchalla & Buras 1994

Long distance contributions:

- Absorptive part ( $\text{Im } A\gamma\gamma$ ) is dominant (2 real photons)
- Dispersive part ( $\text{Re } A\gamma\gamma$ ) depends on the  $K\gamma^*\gamma^*$  form factors that can be studied with the Dalitz decays:
  - Is much less under control
  - Can interfere with the SD piece



# Form Factors $K_{\gamma^*\gamma^{(*)}}$

- **BMS (Bergström, Massó, Singer, 1983)**

$$f(q^2, 0)_{BMS} = 1 + (1 - 3.1 \alpha_K^*) \frac{q^2}{m_\rho^2} + O((q^2)^2 / m_\rho^4)$$

- **DIP (D'Ambrosio, Isidori, Portoles, 1997)**

$$f(q_1^2, q_2^2)_{DIP} = 1 + \alpha \left( \frac{q_1^2}{q_1^2 - m_\rho^2} + \frac{q_2^2}{q_2^2 - m_\rho^2} \right) + \beta \frac{q_1^2 q_2^2}{(q_1^2 - m_\rho^2)(q_2^2 - m_\rho^2)}$$

$$\alpha = -1 + (3.1 \pm 0.5) \alpha_K^*$$

# $K_L \rightarrow \pi^0 \nu \nu$ (reminder)

- Theoretical error ~2%:
  - Purely CP-Violating (Littenberg, 1989)
  - Totally dominated from t-quark
  - Computed to NLO in QCD (e.g. Buchalla Buras, 1999)
  - No long distance contribution SM~ $3 \times 10^{-11}$
- Experimentally: 2/3 invisible final state !!
- Best limit from KTeV using  $\pi^0 \rightarrow e e \gamma$  decay

$$BR(K^0 \rightarrow \pi^0 \nu \nu) < 5.9 \times 10^{-7} \text{ 90% CL}$$

Still far from the model independent limit:

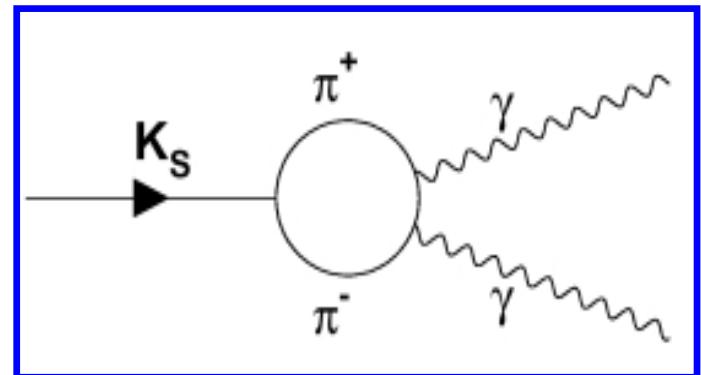
$$BR(K^0 \rightarrow \pi^0 \nu \nu) < 4.4 \times BR(K^+ \rightarrow \pi^+ \nu \nu) \sim 7 \times 10^{-9}$$

Grossman & Nir, PL B407 (1997)

# NA48/1 $K_S \rightarrow \gamma\gamma$

- ◆ Decays into neutral final states :  $O(p^2) = 0$

- $O(p^4)$  unambiguously predicted by ChPT loop diagram to better than 5% without counter terms:  
**Theory:  $BR(K_S \rightarrow \gamma\gamma, O(p^4)) = 2.1 \cdot 10^{-6}$**



- ◆ Older NA48 measurement of  $K_S \rightarrow \gamma\gamma$  branching ratio based on 2 days of test-run in 1999 with high intensity  $K_S$  :  
 $(2.6 \pm 0.4) \times 10^{-6}$  PLB 493 (2000)

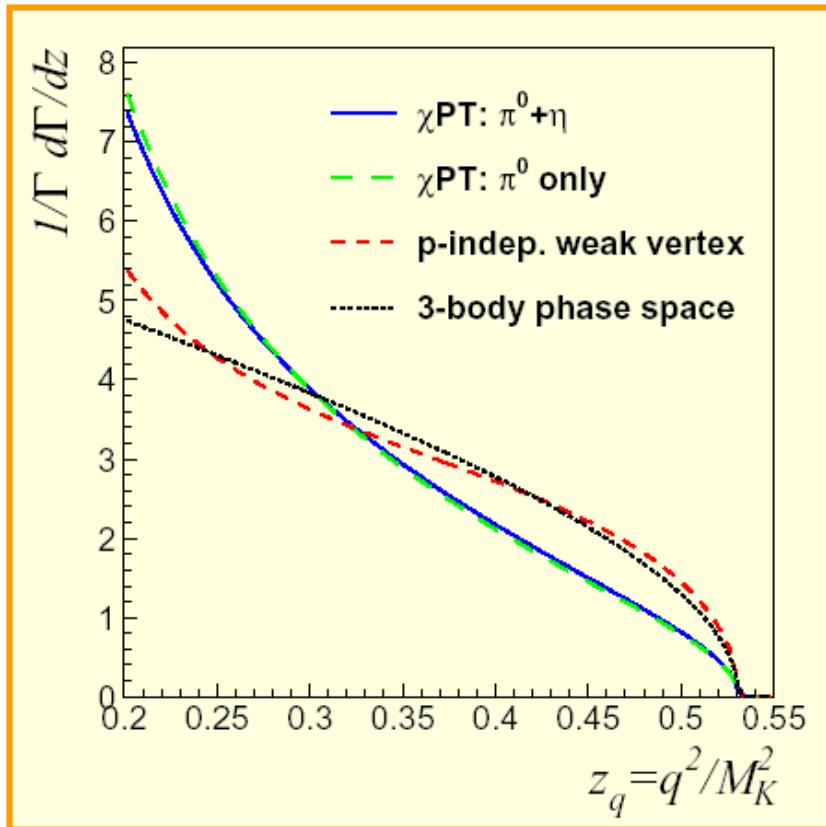
No indication of  $O(p^6)$  contributions

# NA48/1: $K_S \rightarrow \pi^0 \gamma \gamma$

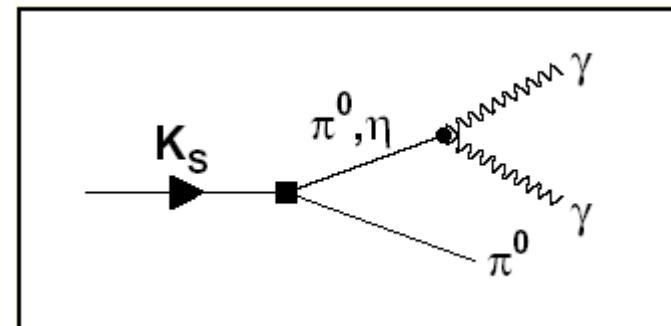
© Previous limit (NA48):

$$\text{BR}(K_S \rightarrow \pi^0 \gamma \gamma, z_q > 0.2) < 3.3 \times 10^{-7} \text{ at 90% CL}$$

© ChPT predicts (Ecker, Pich, De Rafael - PLB 189 (1987)):



$$\text{BR}(K_S \rightarrow \pi^0 \gamma \gamma)_{z_q > 0.2} = 3.8 \times 10^{-8}$$



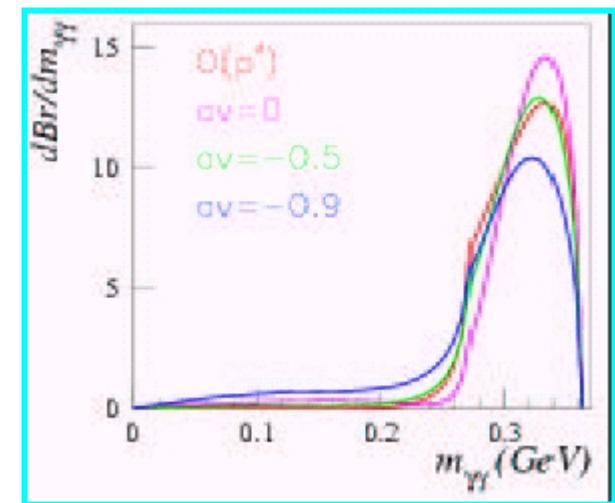
© momentum dependence  
of the weak vertex

→ Chiral structure of the  
weak vertex can be tested  
from  $z_q = (m_{34}/m_K)^2$   
distribution

$$K_L \rightarrow \pi^0 \gamma \gamma$$

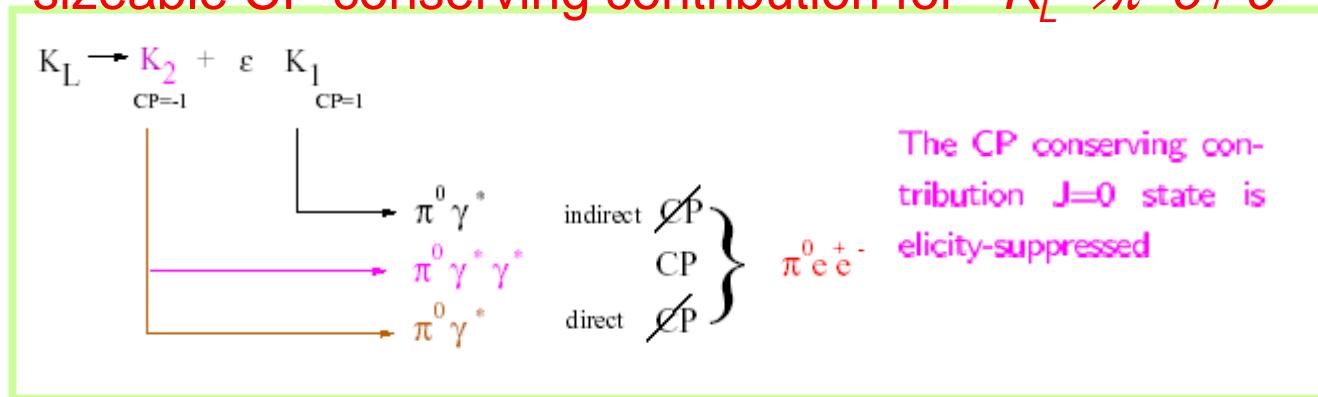
The  $a_v$  can be extracted from the tail

$$m_{\gamma\gamma} < 2 m_{\pi^0}$$

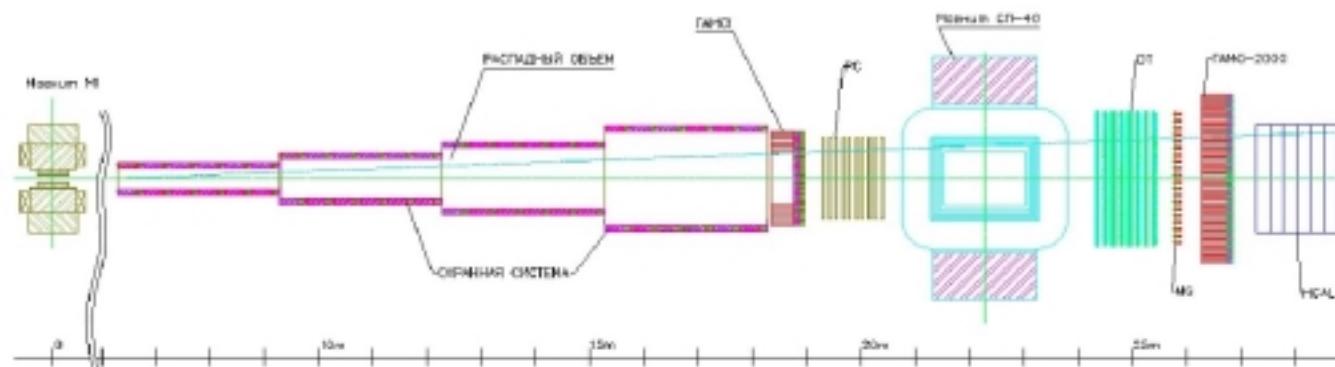


- The  $a_v$  contribution leads to a CP conserving component to  $K_L \rightarrow \pi^0 e^+ e^-$ :
- $\text{BR}(K_L \rightarrow \pi^0 e^+ e^-)_{\text{CP}} = 1.24 \times 10^{-12}$  for  $a_v = -0.7$   
D'Ambrosio, Portoles NP B492 417
- The VMD mechanism could enhance the state  $J=2$  for the two photons

⇒ sizeable CP conserving contribution for  $K_L \rightarrow \pi^0 e^+ e^-$

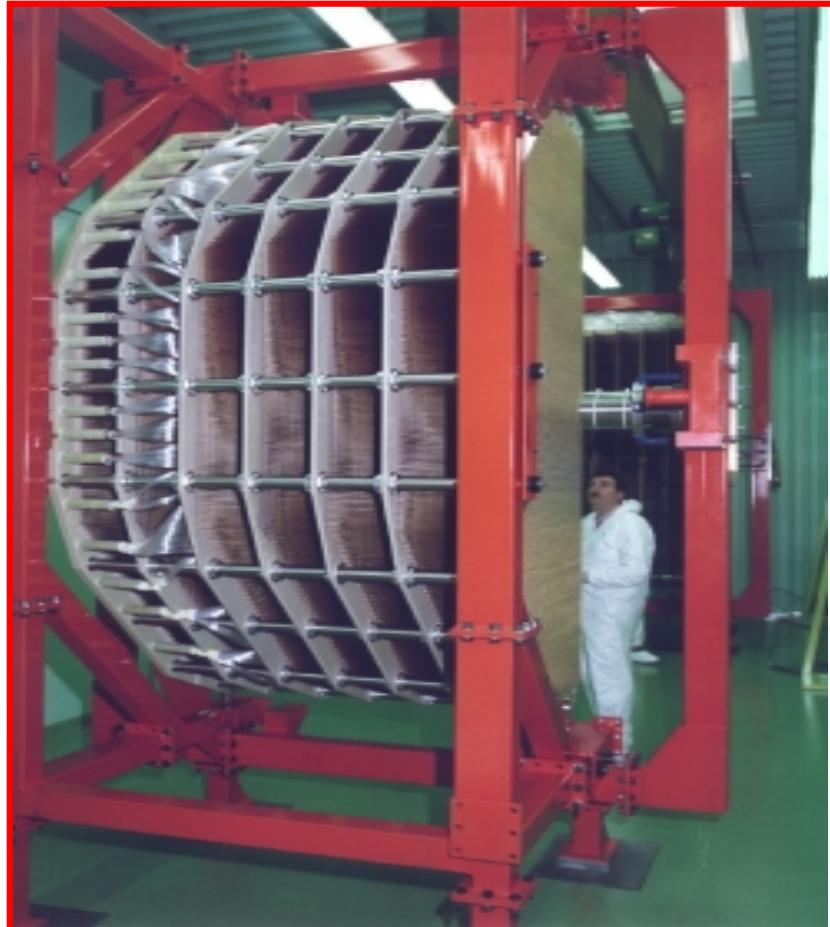


# OKA @ Protvino - $K^\pm$

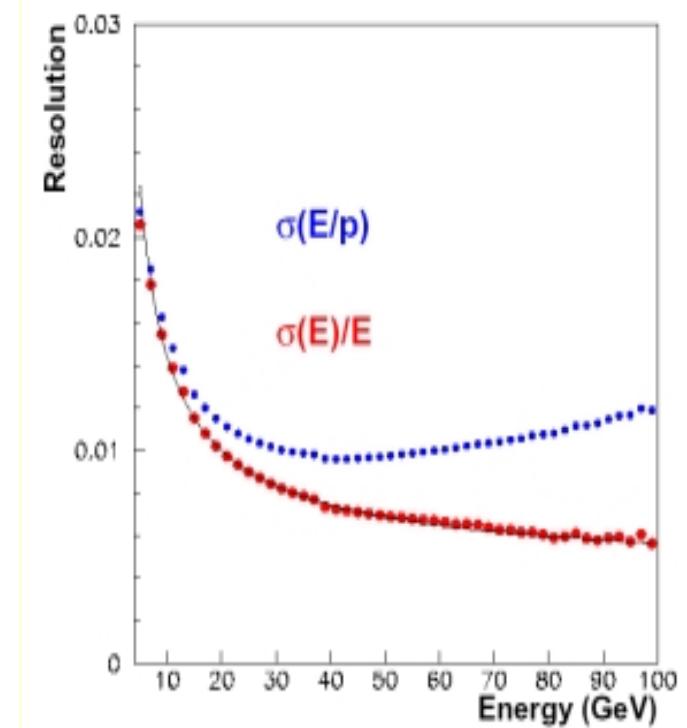


**New RF-separated beam at U-70 PS in construction  
15 GeV/c kaons, alternating  $K^+$  or  $K^-$   
Magnetic detector evolved from ISTRA+, GAMS  
In preparation, expected 2004  
Measurement of  $3\pi$  Dalitz plot asymmetries @  $1 \times 10^{-4}$   
T-odd correlations, search for New Physics in  $K_{l2}$  decays**

# Liquid Krypton Calorimeter



9 m<sup>3</sup> of Lkr (13212 cells)  
1.25 m depth (27 X<sub>0</sub>)

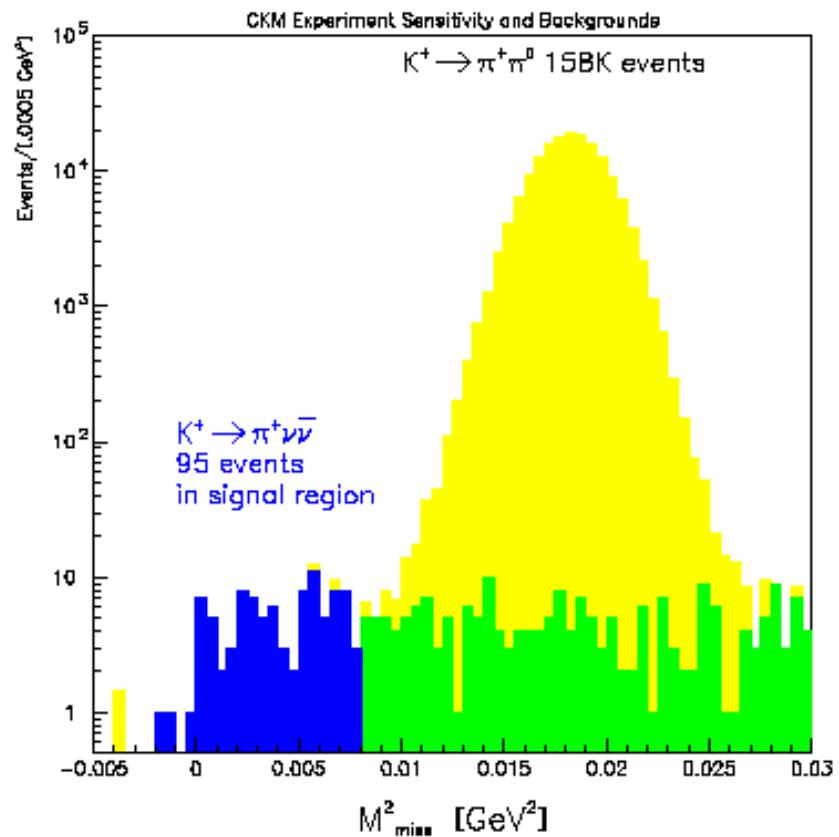


$$\sigma(E)/E = 3.2\%/\sqrt{E} \oplus 9 \% /E \oplus 0.42\%$$
$$\sigma(m_{\gamma}) \sim 1 \text{ MeV}/c^2; \sigma(t) \sim 600 \text{ ps}$$

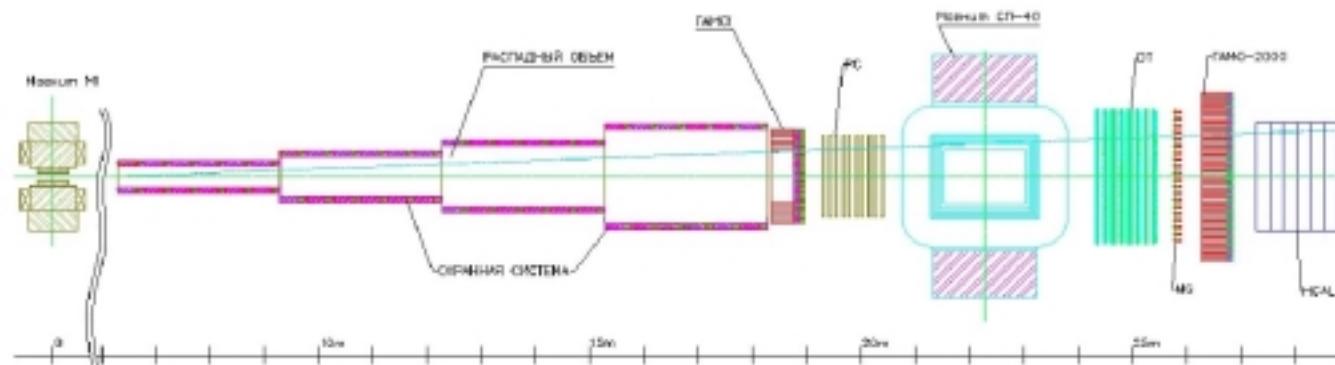
# CKM@FNAL-MI (2009)

- **SCRF 13 cell cavity**
  - Built full size prototype
- **Photon vetoes**
  - Measured inefficiency for 1GeV  $\gamma$ :  $5 \times 10^{-6}$
  - $\times 6$  better than needed
- **Straw tubes**
  - Demonstrated operation in vacuum
  - Same performance as in air
- **Simulation of “triggerless DAQ”**
- **Awaiting approval ratification by P5**

From CKM proposal



# OKA @ Protvino - $K^\pm$



New RF-separated beam at U-70 PS in construction  
15 GeV/c kaons, alternating  $K^+$  or  $K^-$   
Magnetic detector evolved from ISTRA+, GAMS  
In preparation, expected 2004  
Measurement of  $3\pi$  Dalitz plot asymmetries @  $1 \times 10^{-4}$   
T-odd correlations, search for New Physics in  $K_{l2}$  decays