

# ADVANCES in COHERENT BREMSSTRAHLUNG and LPM – EFFECT STUDIES

(in commemoration of the 100th anniversary from the birth of L. D. Landau)

N. F. Shul'ga

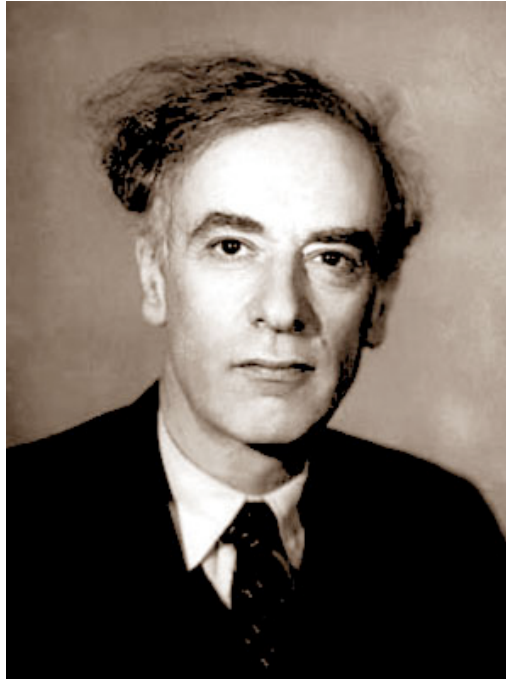
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- Landau in Kharkov (1932-1937)
- CB theory and its problems
- Semiclassical and classical theory of CB and experiment
- LPM-effect in amorphous media and in crystals
- CB at high energy
- CB in deformed crystals

# LEV LANDAU (1908-1968)

(in commemoration of 100<sup>th</sup> anniversary from the birth)



- Nobel prize 1962
- The head of the theoretical department in Ukrainian Physical Technical Institute (Kharkov) from 1932 to 1937

# Ukrainian Physical-Technical Institute UPhTI was founded 30 October 1928.

(Now National Science Center “Kharkov Institute of Physics and  
Technology”)



prof. I.Obreimov was the first director of UPhTI. (1928-1931).  
He organized the first theoretical department in the USSR (1928).

## Prof. D.Ivanenko

He was the first head of Theoretical Department UPhTI (1928-1931)



Prof. D.Ivanenko

He was arrested in 1935 as a “socially dangerous element”  
“... They remembered him his non-proletarian origin... accused him of  
contacts with foreigners, knowledge of foreign languages...”

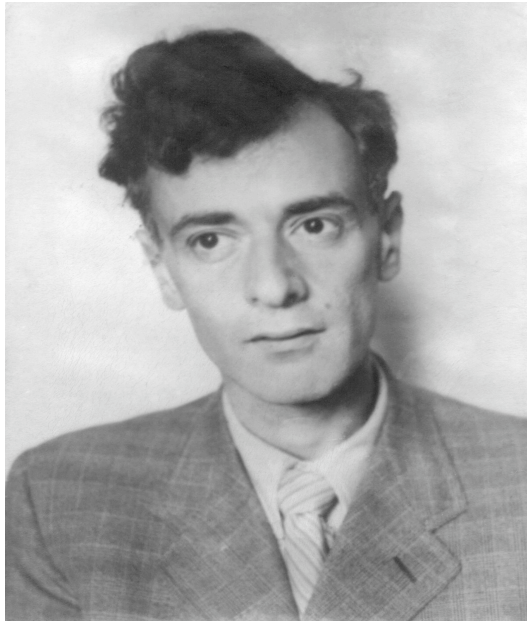
(Ivanenko's wife)

In 1931, I.Obreimov proposed to lead the theoretical department of UPhTI to P.Dirac, then to P.Ehrenfest...

They agreed to be the members of the academic council of UPhTI and proposed for this position L.Landau, who was unemployed in that time for about one year

# Lev Landau

The head of theoretical department UPhTI from 1932 to 1937.



- Creation of the school for theoretical physics
- Creation of the course of theoretical physics since 1935

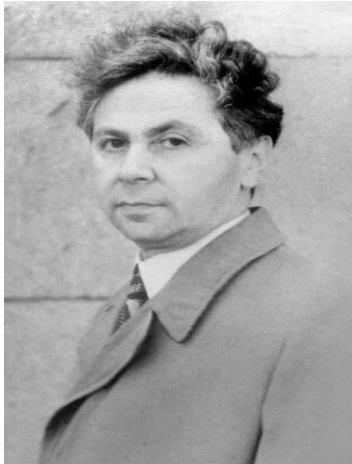
**Mechanics (with L.Pyatigorskii)**

**Statistical physics (with E.Lifshitz)**

**Electrodynamics (started with L.Pyatigorskii)**

- Third international Theoretical Physics Conference (1934)
- Revision of the system of teaching the course of physics

## School of Landau (UPhTI -1934)



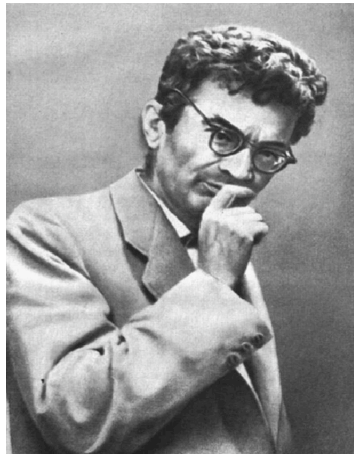
A.Kompaneetz



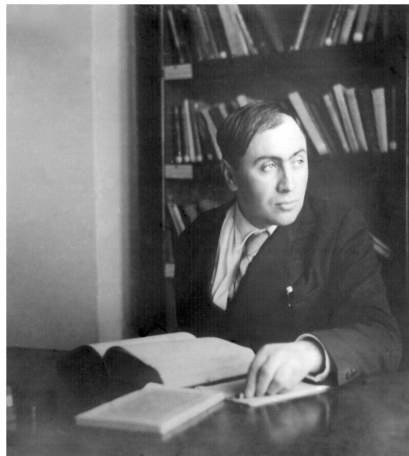
E.Lifshitz



A.Akhiezer



I.Pomeranchuk



L.Pyatigorskii



L.Tisza

E.Teller recommended him<sup>7</sup>  
to work in Kharkov

# Kharkov, UPhTI (1930's)

P.Dirac – member of the scientific council of UPhTI

P.Kapitza, G.Gamov, P.Erenfest – scientific consultants of UPhTI

F.Hautermans – staff of UPhTI (30-е годы)

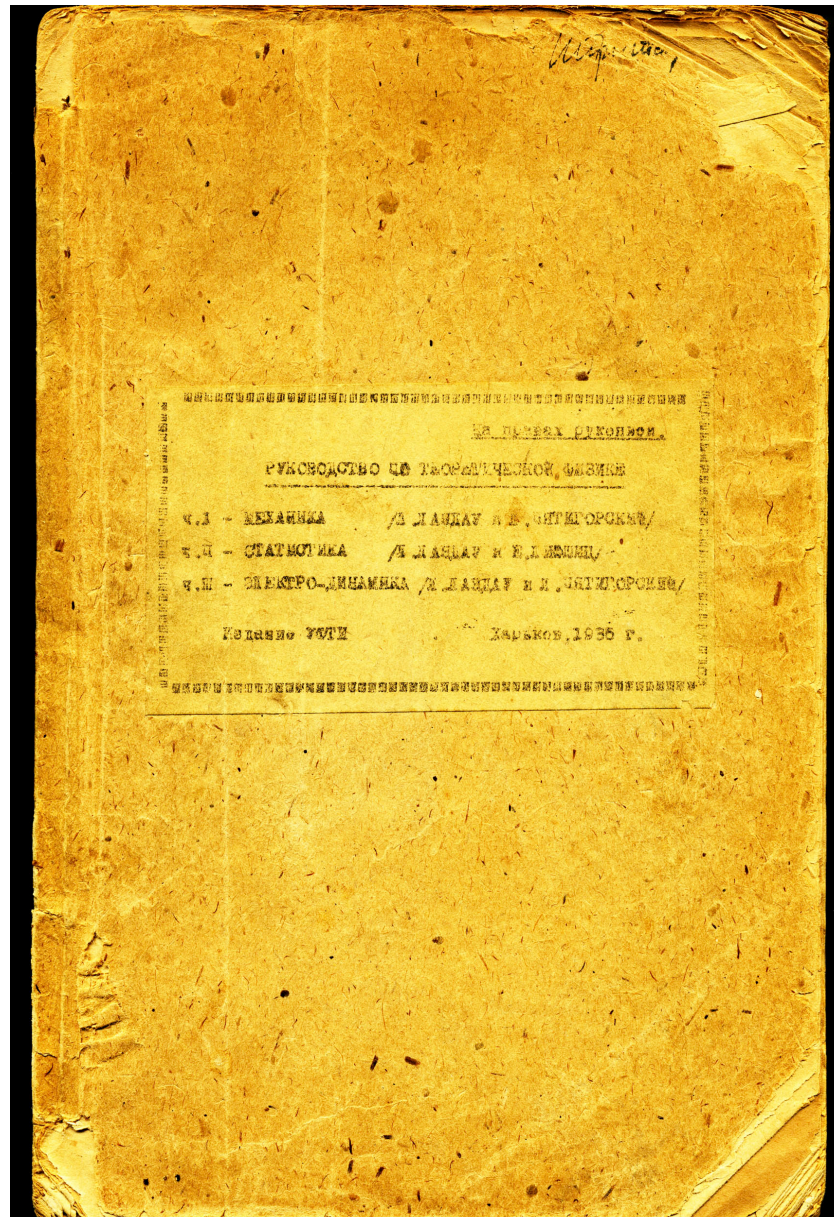
W.Weisskopf – staff of UPhTI (1933-1934)

«I could not get a job in England, neither in France. 1933 I leaved... for Kharkov, where it was possible to get a job, which provided me with means of subsistence.».

*W.Weisskopf*

N.Bohr, R.Peierls, V.Fock, B.Podolskii, Yu.Rumer,... .  
also came to Kharkov and worked in UPhTI for a long time





Course of theoretical physics. Kharkov, 1935



### III International Conference on theoretical Physics


(Kharkov, 1934)



*«Осторожно, кусается!»*  
( Be careful, bites! )

## L.Landau and N.Bohr



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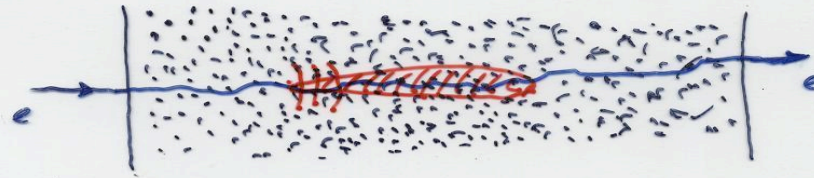
**Thick books are a cemetery where ideas of the past  
which had served their time are buried**

**L.Landau**

**(Господи, прости им, не ведают, что творят)  
«God, absolve them 'cause they know not what they do**

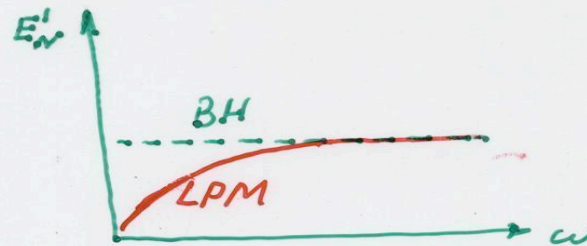
**L.Landau**

## LPM – effect (1953)



$$\frac{dE_{BH}^{(N)}}{d\omega} = N \frac{dE^{(1)}}{d\omega}$$

Landau – Pomeranchuk 1953



**Discussion: E.Feinberg and M.Ter- Mikaelian with  
L.Landau and I. Pomeranchuk (1952)**

**T. - M. – Interference radiation by ultrarelativistic electrons  
in crystals.**

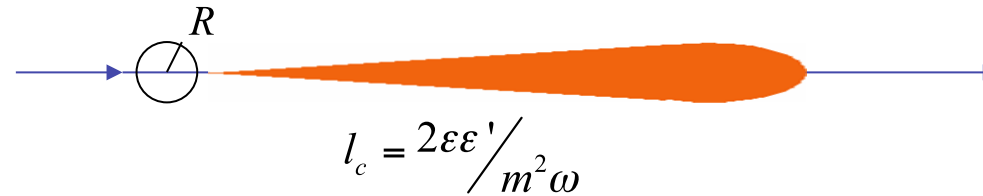
**Landau – That is impossible because the interference  
effect is possible only for**

$$\lambda = \frac{\hbar}{p} \geq a \quad , \quad \text{but not for } \lambda \ll a$$

---

**The discussion was stopped.**

# Coherent length (Ter-Mikaelian, 1953)



$$d\sigma \approx \int d^2q_{\perp} \int_{q_{\min}}^{\infty} dq_{\parallel} \frac{q_{\perp}^2}{q_{\parallel}^2} |U_q|^2$$

$$\varepsilon = \varepsilon' + \omega, \quad \mathbf{p} = \mathbf{p}' + \mathbf{k} + \mathbf{q}$$

$$r_{\parallel eff} \approx q_{\parallel eff}^{-1} \approx l_c = 2\varepsilon\varepsilon' / m^2\omega$$

$$l_c = \frac{2\varepsilon\varepsilon'}{m^2\omega}$$

$$r_{\perp eff} \approx \frac{1}{q_{\perp eff}} \approx R$$

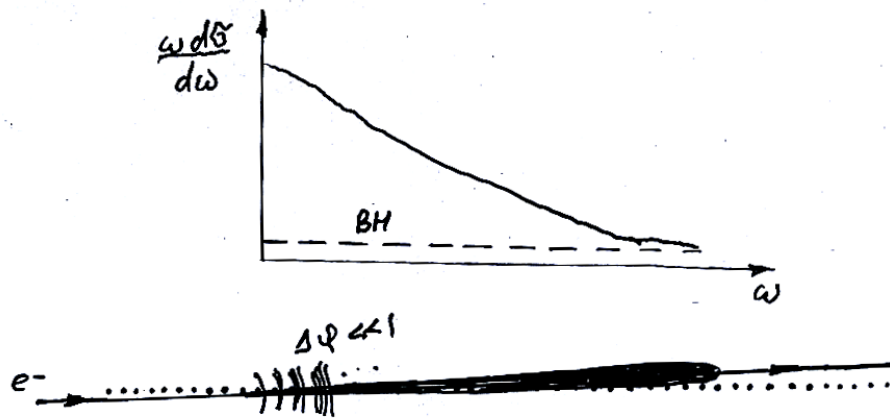
$$\varepsilon = 100 \text{ Mev} \quad \omega = 100 \text{ kev} \quad l_c \approx 10^{-4} \text{ cm}$$

$$\varepsilon = 100 \text{ Mev} \quad \lambda \approx 1 \text{ cm} \quad l_c \approx 10^3 \text{ m!!!}$$

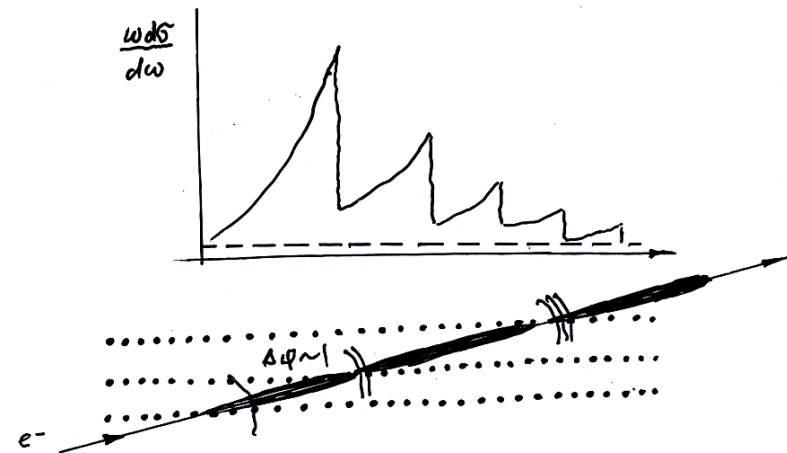


# Coherent length

(Ter-Mikaelian 1953 – crystal, Landau-Pomeranchuk 1953 – amorphous media)



Coherent effect



Coherence + Interference

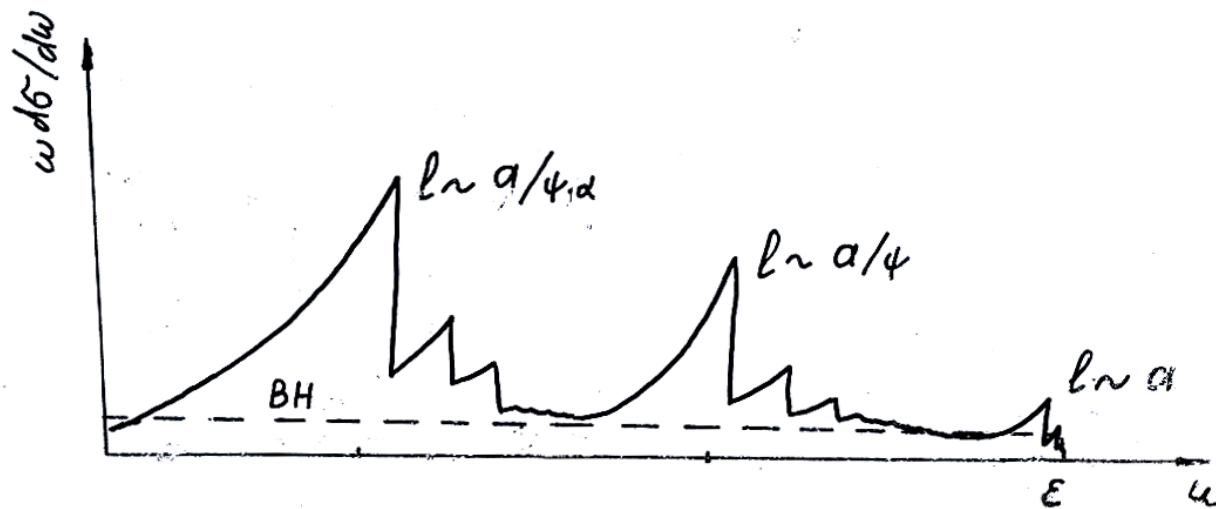
Landau was agreed that Ter-Mikaelian's results were correct, but he said that it is needed to use another way for describing this effect 17

# Coherent Bremsstrahlung Theory

(Ferretti 1950, Ter-Mikaelian 1952, Überall 1956, 1960)



$$d\tilde{\sigma}_{\text{atom}} \sim \dots \int d^3q \dots \longrightarrow d\tilde{\sigma}_{\text{crystal}} \sim \dots \sum_{\vec{g}} \dots$$



Akhiezer, Shul'ga 1982

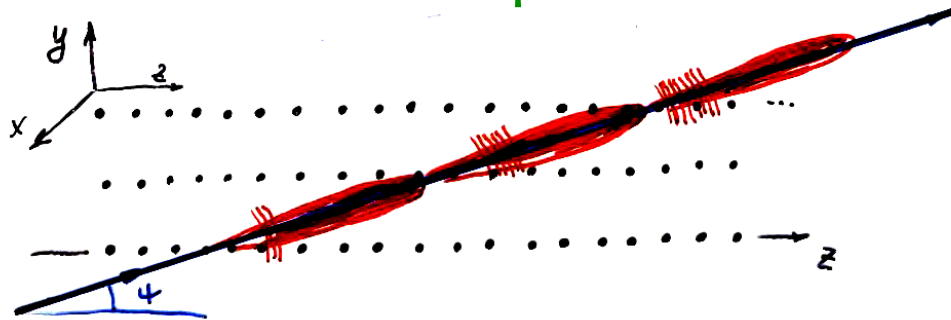
$$l_c = \frac{2\varepsilon\varepsilon'}{m^2\omega} \sim a$$



CB – type B

$$g_z = \frac{2\pi}{a} = \frac{\omega m^2}{2\varepsilon\varepsilon'}$$

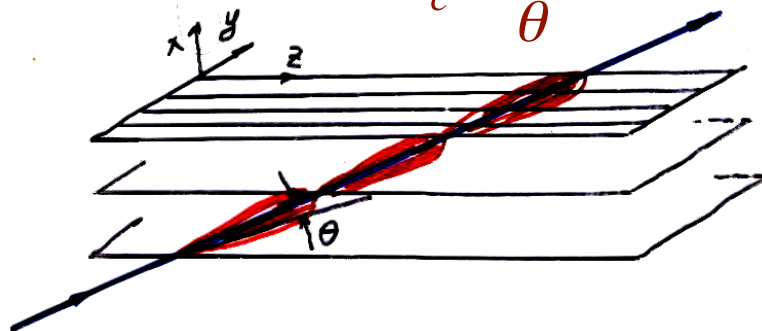
$$l_c = \frac{a}{\psi}$$



CB – row effect

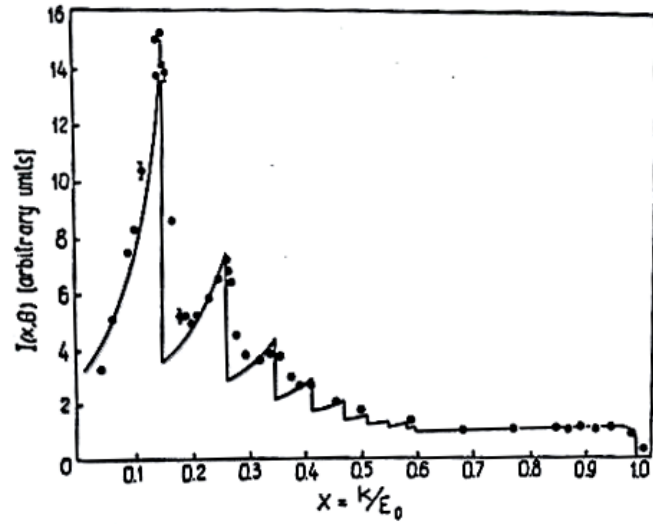
$$\psi \frac{2\pi}{a} = \frac{\omega m^2}{2\varepsilon\varepsilon'}$$

$$l_c = \frac{a}{\theta}$$

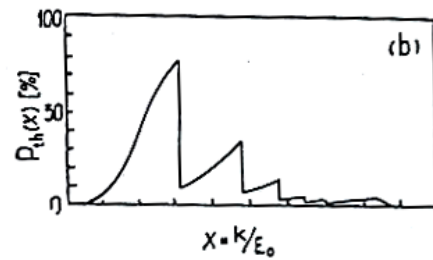
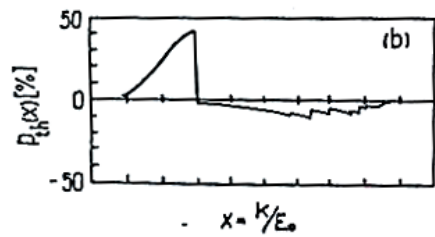
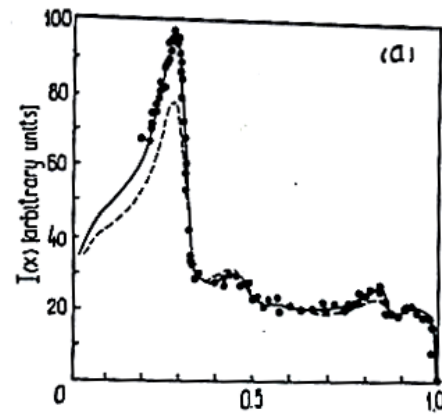
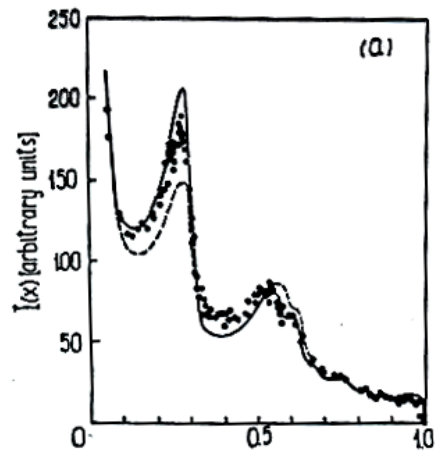


CB – point effect

$$\theta \frac{2\pi}{a} = \frac{\omega m^2}{2\varepsilon\varepsilon'}$$



Frascati  
 $\varepsilon = 1 \text{ GeV}$ ,  $\theta = 4,6 \text{ mrad}$

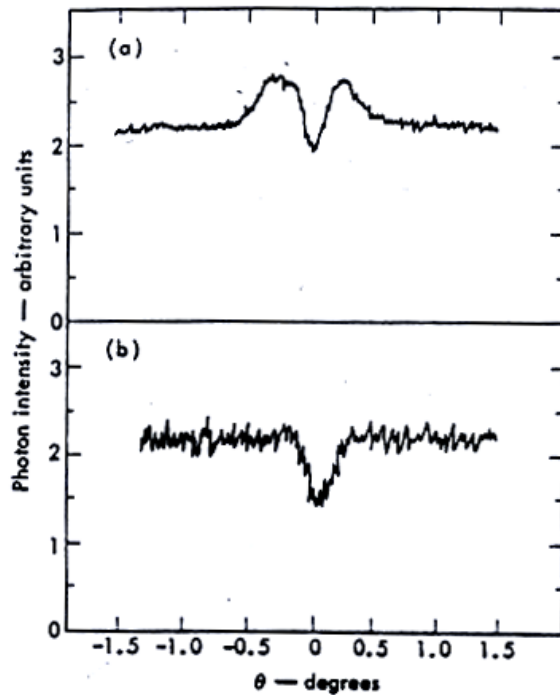


DESY  
 $\varepsilon = 4,8 \text{ GeV}$ ,  $\theta = 3,4 \text{ mrad}$

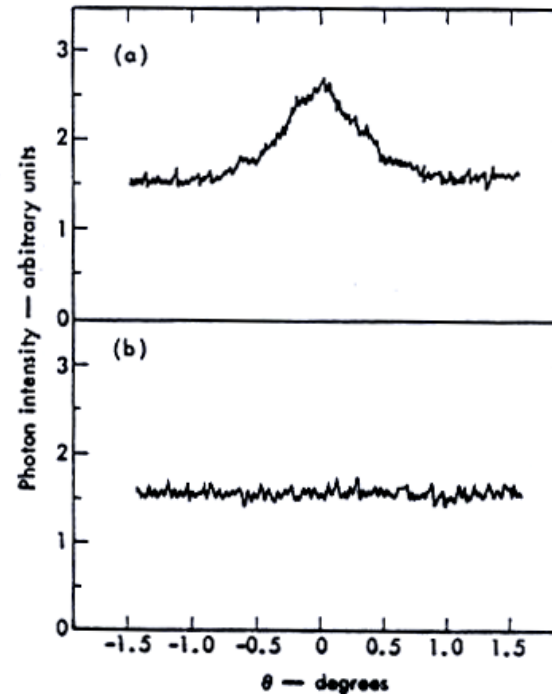
# Problems of CB theory

- $e^+e^-$  - dependence
- second and higher Born approximations are increased quickly
- The validity conditions of F – T - Ü method
- Ter-Mikaelian - Überall methods
- $dE/d\omega \rightarrow \infty$  for  $\psi \rightarrow 0$  at  $\omega \cong \omega_{\max}$

# Channeling and Coherent Bremsstrahlung for relativistic positrons and electrons (USA Lawrence lab, Livermore lab, 1970)



positrons



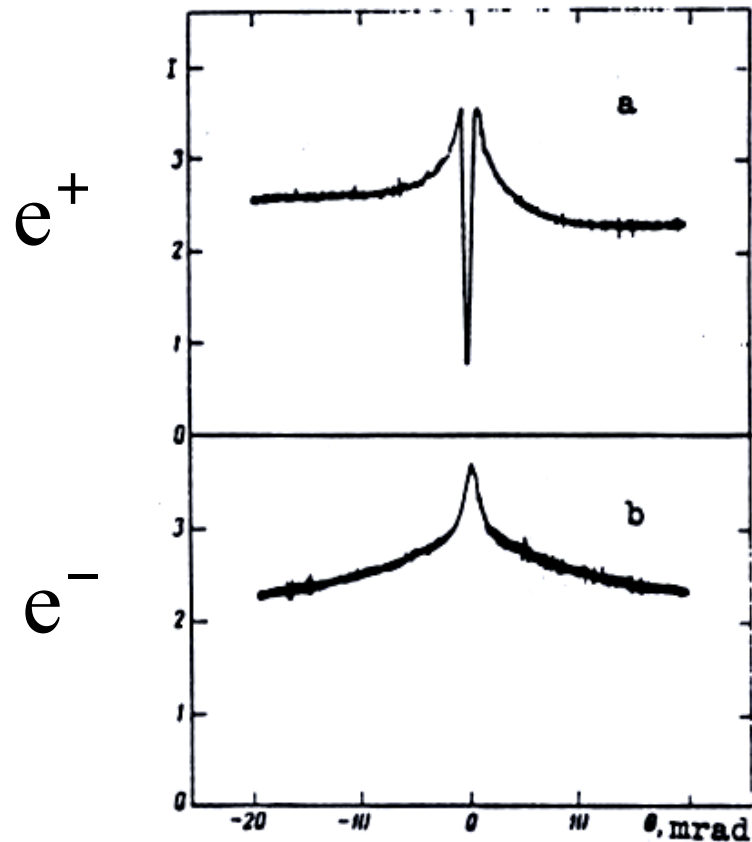
electrons

$$\varepsilon = 28\text{MeV}, \quad \text{Si} - \langle 110 \rangle, \quad L = 53\mu\text{m}$$

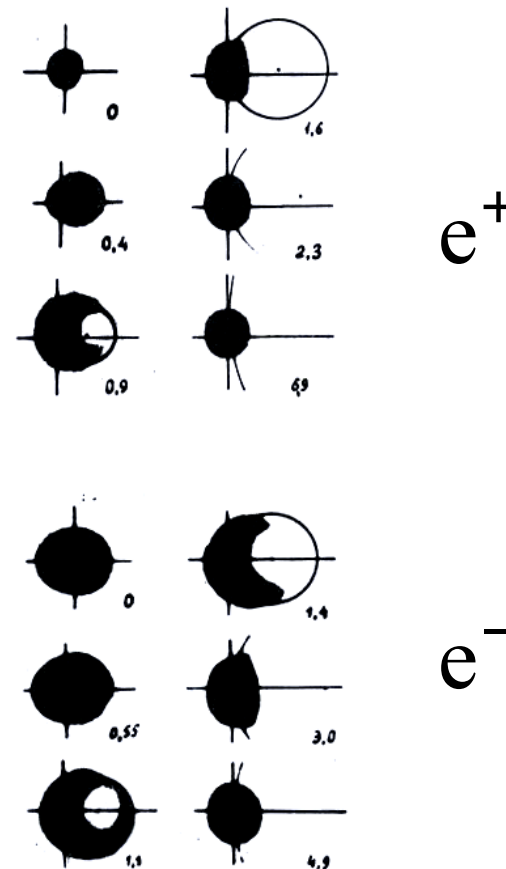
# Channeling and Coherent Bremsstrahlung and Scattering for 1 GeV positrons and electrons

(Ukraine, Kharkov, 1972)

Orientation dependence of the radiation intensity

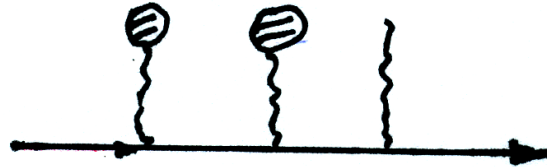


Angular distribution of scattering



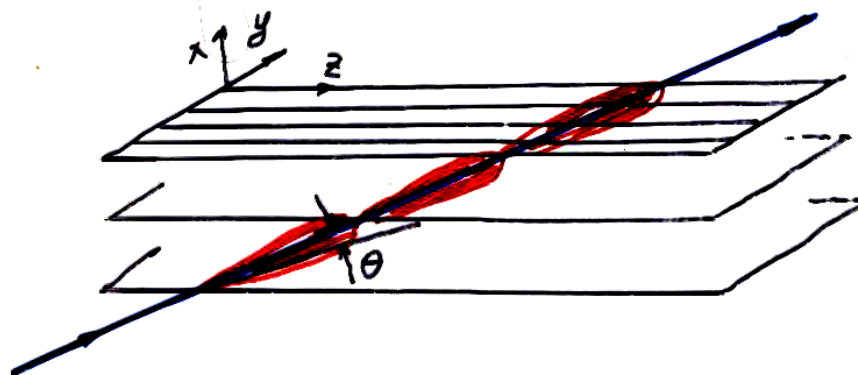
# Second Born approximation in CB theory

A.Akhiezer, P.Fomin, N.Shul'ga (1970)



$$d\sigma_c = d\sigma_{coh}^{Born} \cdot \left( 1 \pm \eta \frac{\theta_c^2}{\theta^2} \right), \quad \hbar\omega \ll \varepsilon$$

$\eta \sim 1$        $\theta_c$  - crytical channelling angle





# Higher Born Approximation in the CB Theory

A.Akhiezer, N.Shul'ga (1975)



$$N_{coh} \sim \min\left(\frac{l_{coh}}{a}, \frac{R}{\psi_a}\right)$$

$$\frac{Ze^2}{\hbar c} \ll 1 \quad \rightarrow \quad N_{coh} \frac{Ze^2}{\hbar c} \sim \frac{R}{\psi a} \frac{Ze^2}{\hbar c} \ll 1 \quad \text{Quickly destroys for } \psi \rightarrow 0$$

## PARADOX

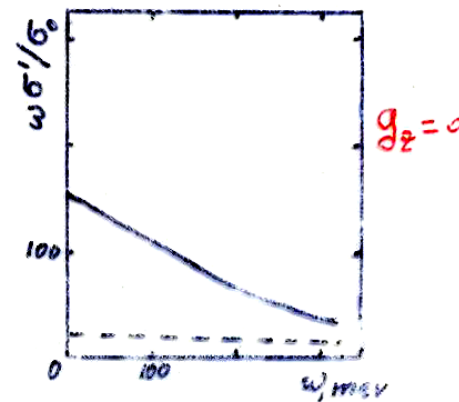
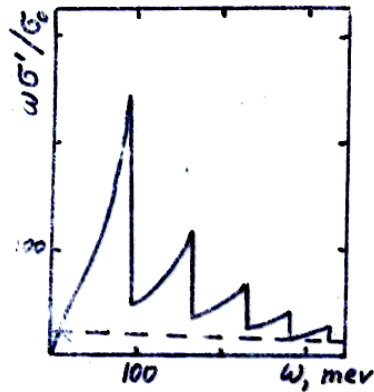
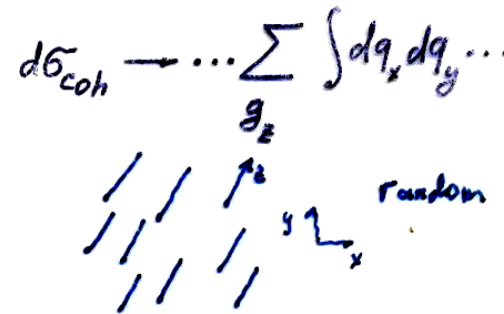
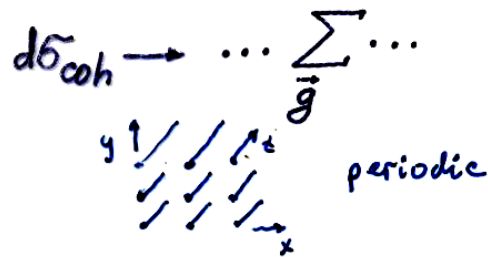
This condition did not fulfill practically for experiments (1960-1970) on verification of F – T – Ü theoretical results.

But the experiments were in good agreement with this theory !!!  
Why ???

# Problem

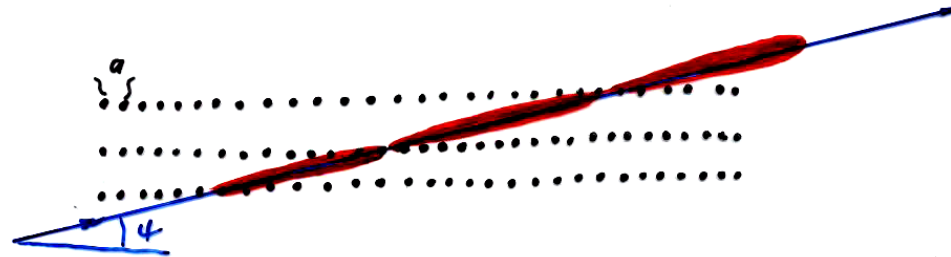
M. Ter-Mikaelian – 1952  
H. Überall – 1960

H. Überall – 1956



$\varepsilon = 1\text{GeV}, \quad Si - \langle 100 \rangle, \quad \psi = 2\text{mrad}$

# Eikonal, Semiclassical, Classical CB Theory



Semiclassical approximation

$$\boxed{\frac{N_c Z e^2}{\hbar c} = \frac{R}{\psi a} \frac{Z e^2}{\hbar c} \gg 1}$$

!!!

Classical  
Electrodynamics

$$N_c \frac{Z e^2}{\hbar c} \gg 1, \quad \hbar \omega \ll \varepsilon$$

$$d\sigma^{(WKB)} = d\sigma \left\{ \vec{r}_{cl}(t) \right\}$$

- Radiation is determined by the classical trajectory !!!
- It is necessary to know the types of particles' motion in crystal
- **Same methods for description of CB and LPM effects !!!**

# Semiclassical Theory of CB in Crystals

A.Akhiezer, N.Shul'ga (1982)

$$d\sigma_{coh}^{(WKB)} = d\sigma_{coh} \cdot \left( 1 + O\left(\frac{\psi_c^2}{\psi^2}, \gamma\theta_{scatt}\right) \right)$$

1. Trajectory is close to rectilinear
2. Dipole approximation

1.  $\psi \leq \psi_c$  – Channeling and above - barrier motion

2.  $\gamma\theta_{scatt} \gg 1$  +  $\left\{ \begin{array}{l} l_c \ll R/\psi \\ l_c \gg R/\psi \end{array} \right.$

synchrotron approx.  
(constant field approx.)

LPM-like effects

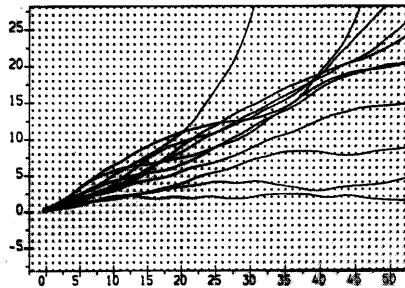
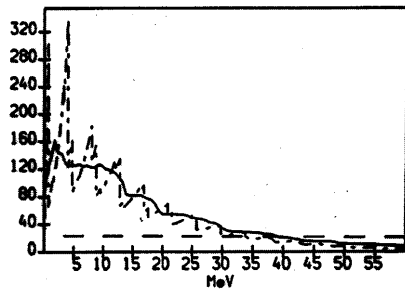
N.Shul'ga (1980)

Semiclassical Theory: V.N. Baier et al. (1990)...

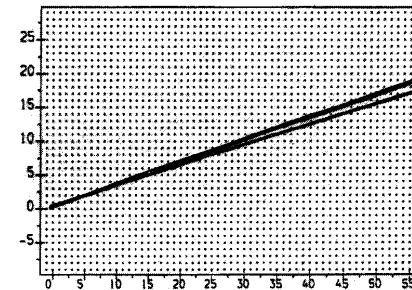
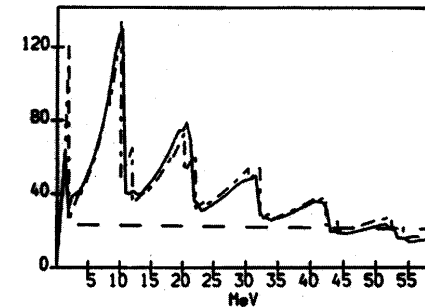
# CB for real trajectories of electrons and positrons in crystals

(V.Truten', N.Shul'ga, 1995 -...)

$$e^- \quad \psi = 2\psi_c$$

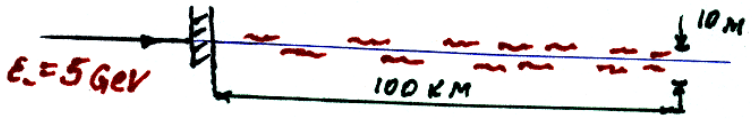
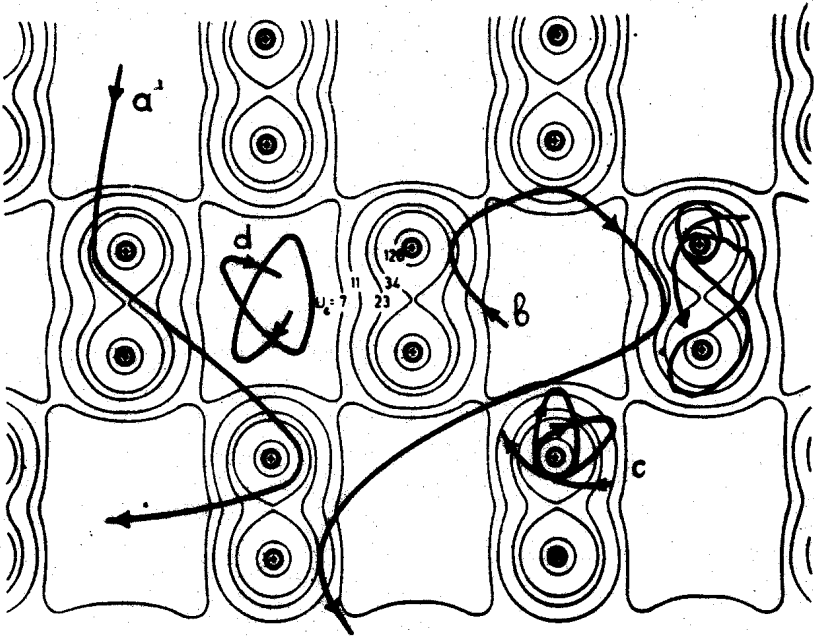
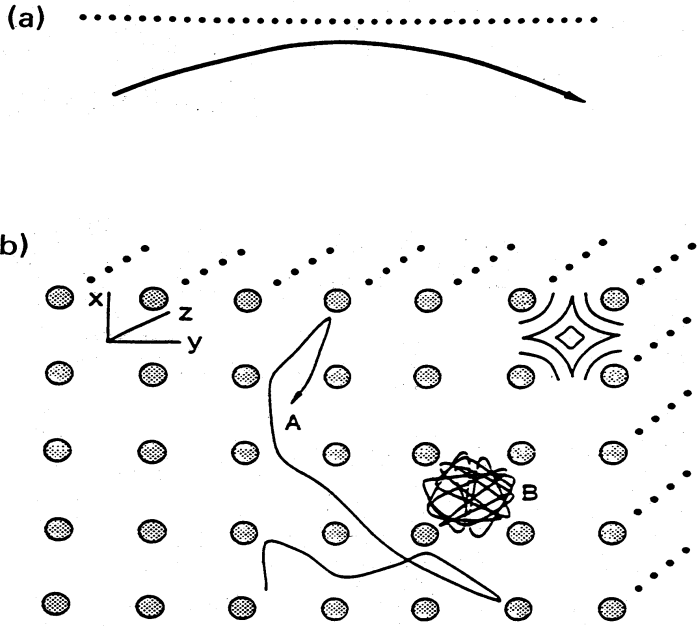


$$e^+ \quad \psi = 5\psi_c$$



H.Überall

# The motion along crystal axis

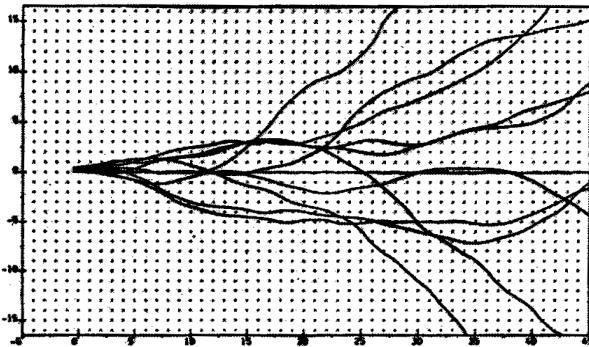
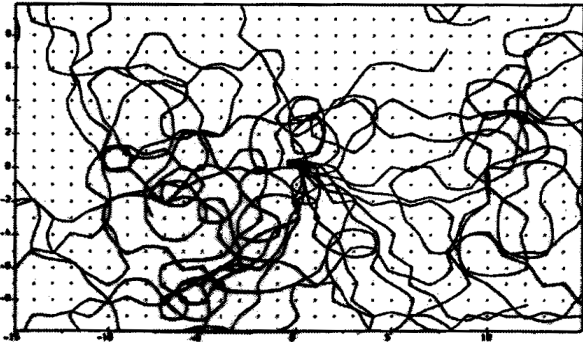


for thick crystals  $\frac{I_{\omega, \vartheta}^{ch}}{I_{\omega, \vartheta}^{am}} \sim 25.000$

# Dynamical chaos phenomenon (Yu.Bolotin, V.Gonchar, N.Shul'ga 1985)

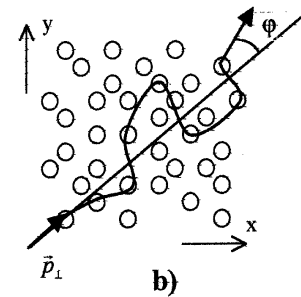
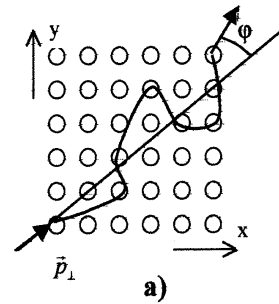
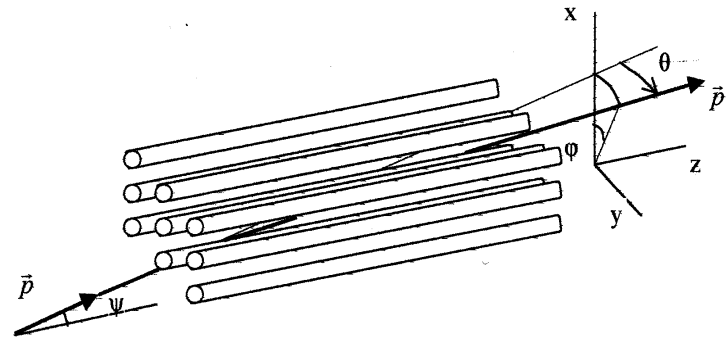
$e^-$

$$\psi = 0,5 \psi_c$$



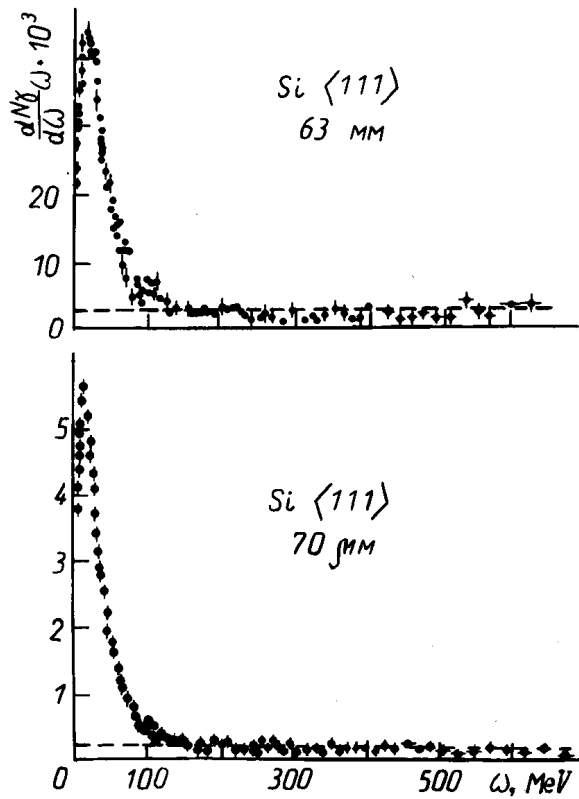
$$\psi = 1,5 \psi_c$$

**Dynamical chaos**

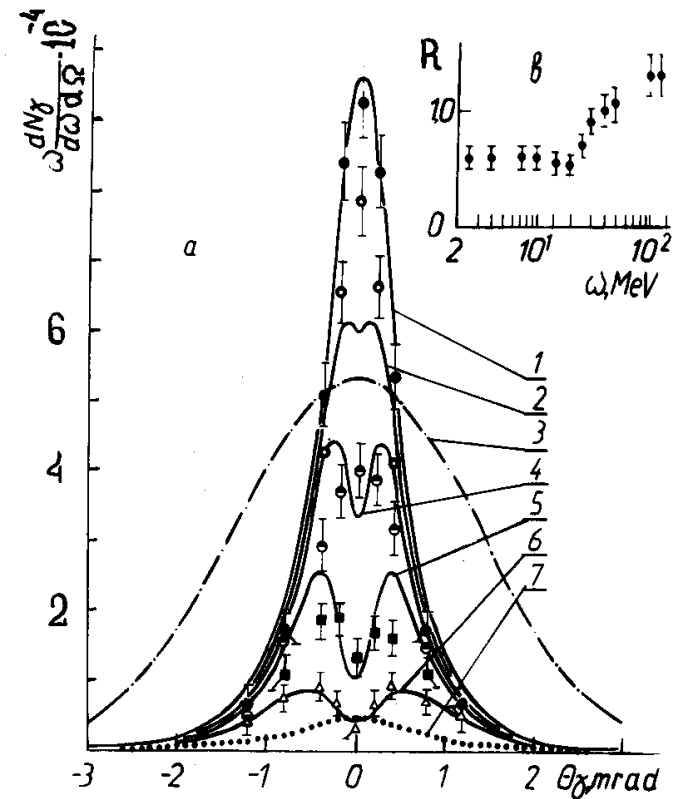


**Multiple scattering**

Theory (Dynamical Chaos Approx.)  
and Experiment for 1,2 GeV electrons  
Kharkov 1990 – ... (Phys.Lett.A, 1991, v.158, 177)



spectrum

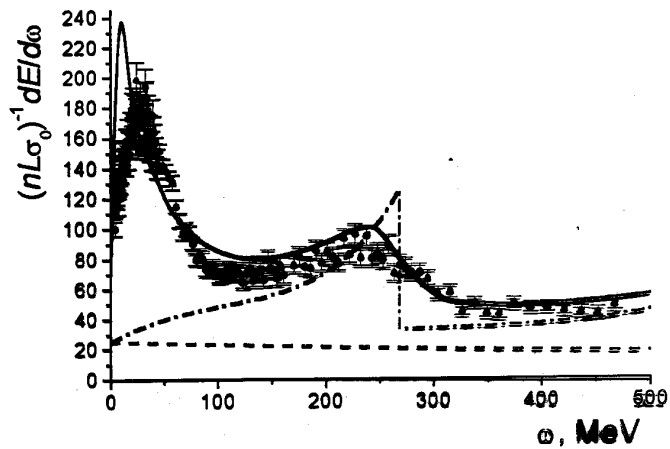
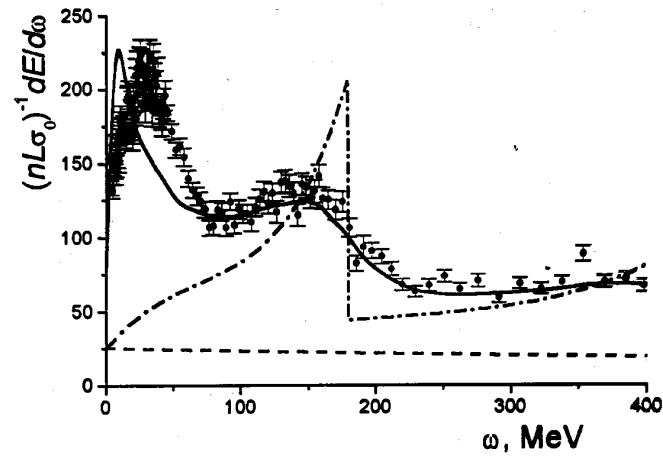


spectral-angular

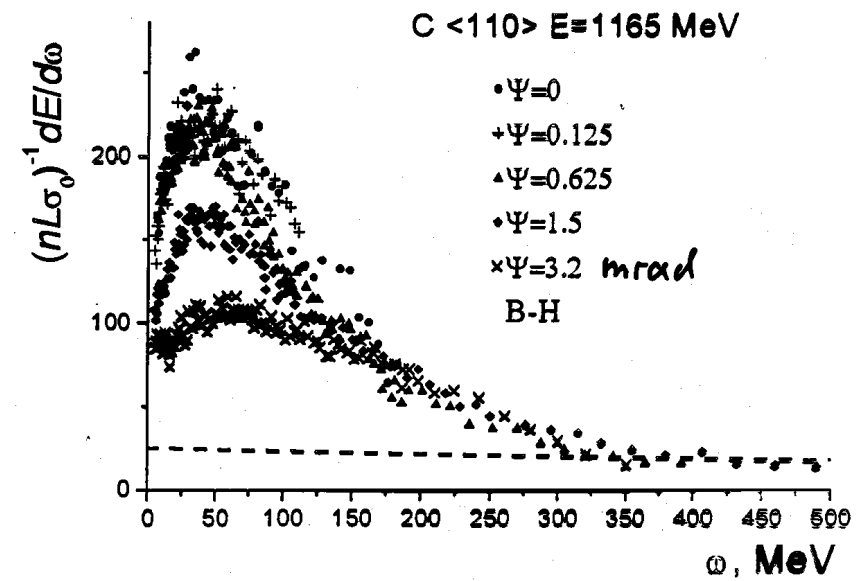


# Theory (real particles' trajectories) – experiment. Kharkov 1990 – ...

$L = 300\mu$



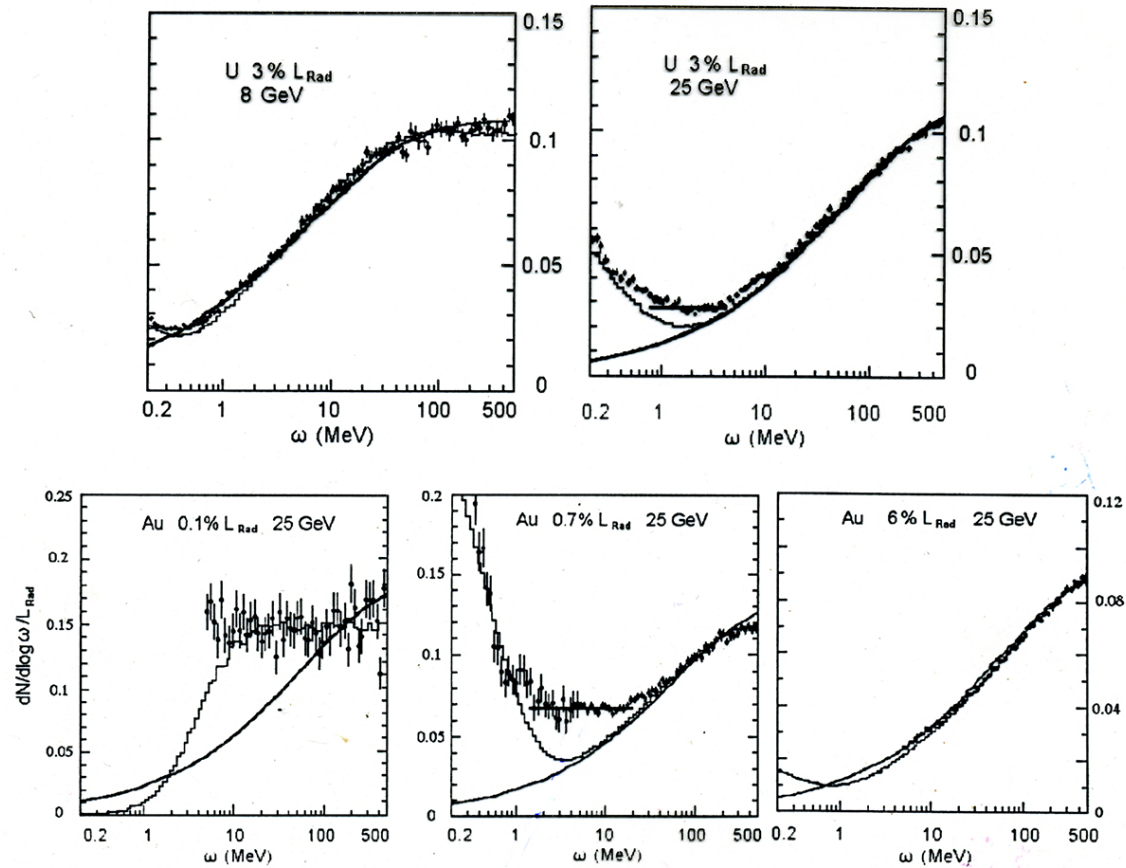
$L = 2cm$



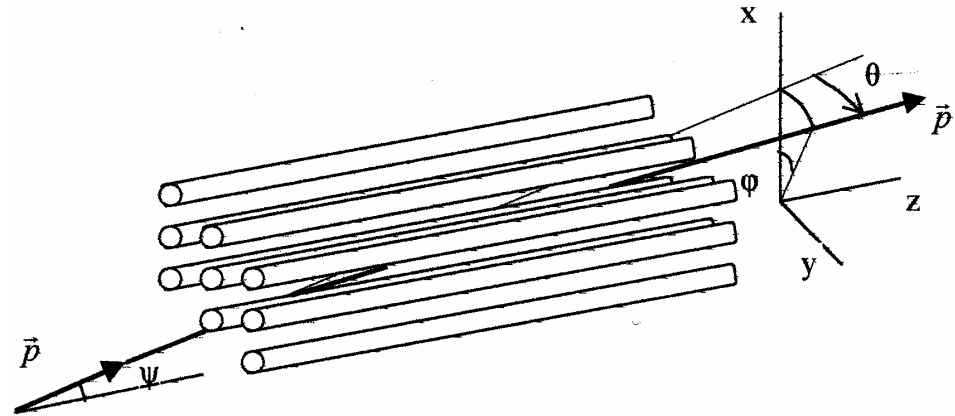
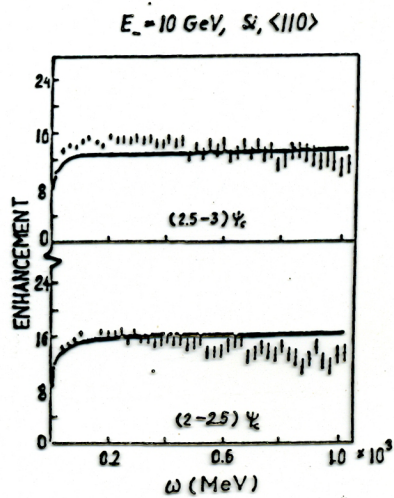
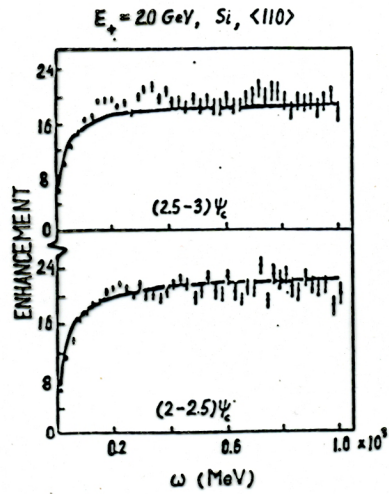
$\varepsilon_- = 1,2 GeV$ , diamond  $\langle 110 \rangle$

# LPM-effect

Effect which was confirmed after 40 years!  
SLAC experiment – 1995

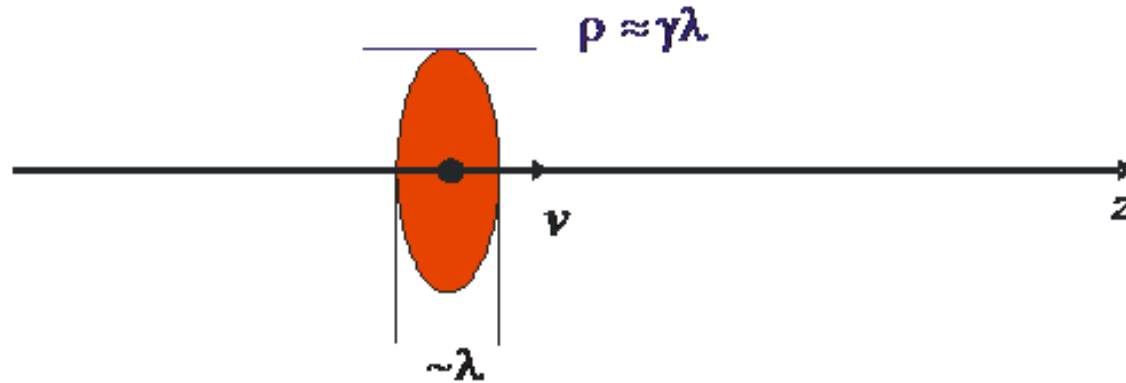


# Influence of Multiple Scattering on CB in Crystals Analogue of LPM-effect



Experiment - J.Bak et al. Nucl.Phys. 1998  
Theory – N. Laskin, N.Shul'ga, Phys.Lett.A, 1989

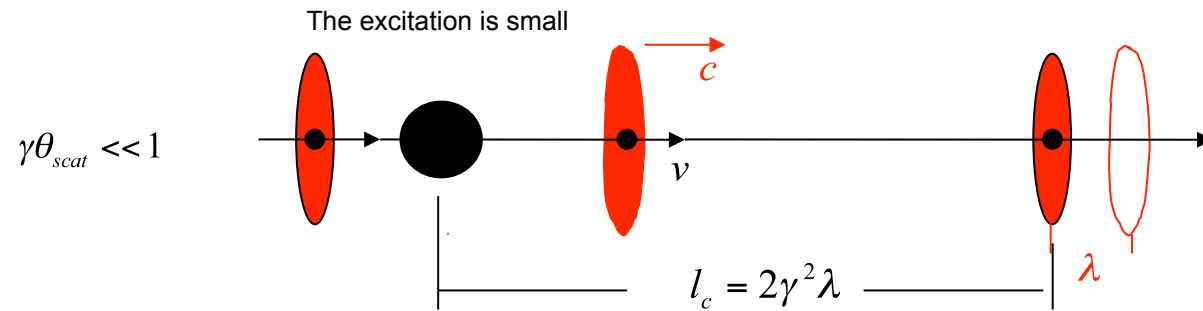
## Relativistic Electron Field Potential



$$c_{\vec{k}} = e^{-ik_z vt} \int d^3r e^{i\vec{k}\vec{r}} \frac{e}{\sqrt{z^2 + \rho^2/\gamma^2}} =$$

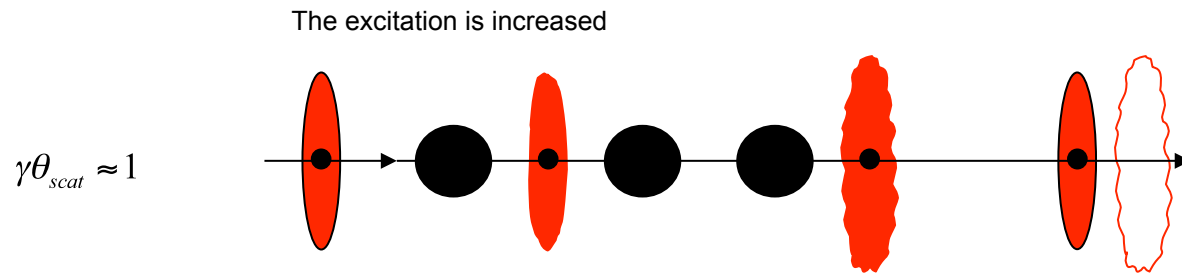
$$= \frac{4\pi\gamma e}{k_{\perp}} e^{-ik_z vt} \int_0^{\infty} dz \cos k_z z e^{-\gamma k_{\perp} z} = 4\pi e \cdot e^{-ik_z vt} \int_0^{\infty} \rho d\rho J_0(k_{\perp}\rho) K_0(k_z \rho/\gamma)$$

# How Does Electron Radiate?



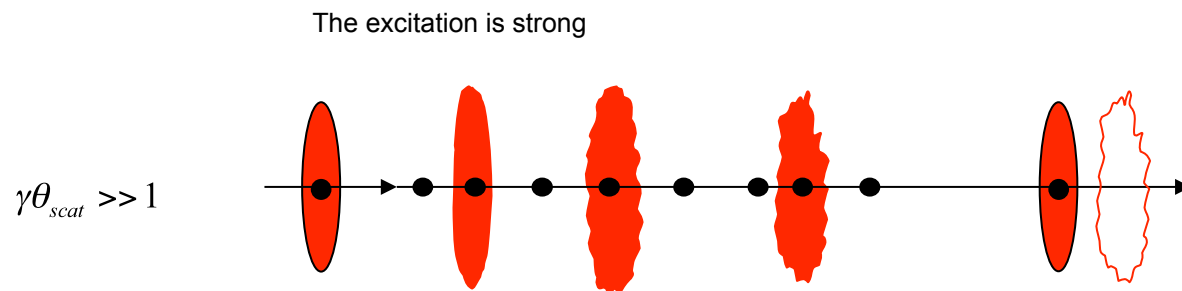
$$v_{rel} = c - v$$

$$\lambda = (c - v)\Delta t_c \rightarrow \Delta t_c \approx 2\gamma^2\lambda$$



$$l_c = 2\gamma^2\lambda$$

$$\varepsilon = 5\text{GeV}$$



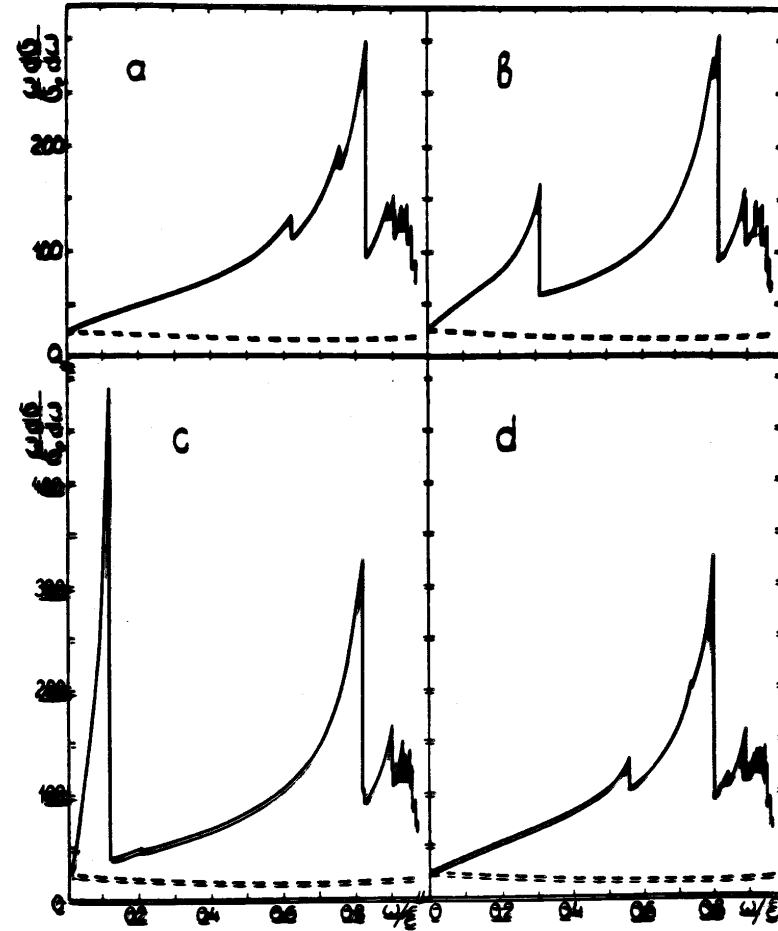
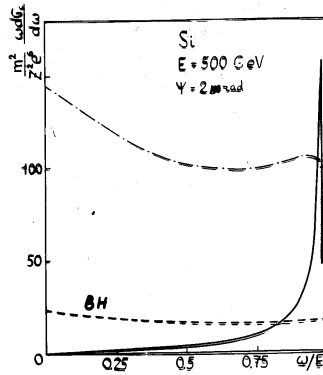
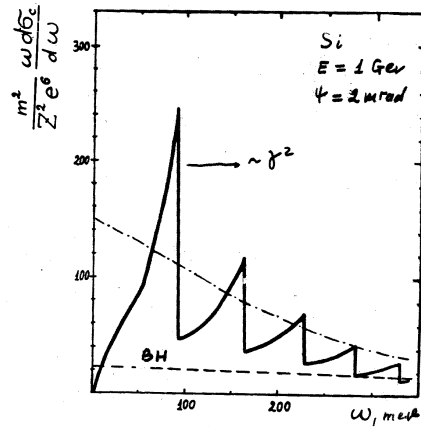
$$l_c \sim 10^{-3}\text{cm} \text{ for } \omega \sim 1\text{ MeV}$$

$$l_c \sim 1\text{cm} \text{ for } \omega \sim 1\text{ KeV}$$

# CB for High Energies (N.Shul'ga, V.Truten', 1992)

fine structure of CB

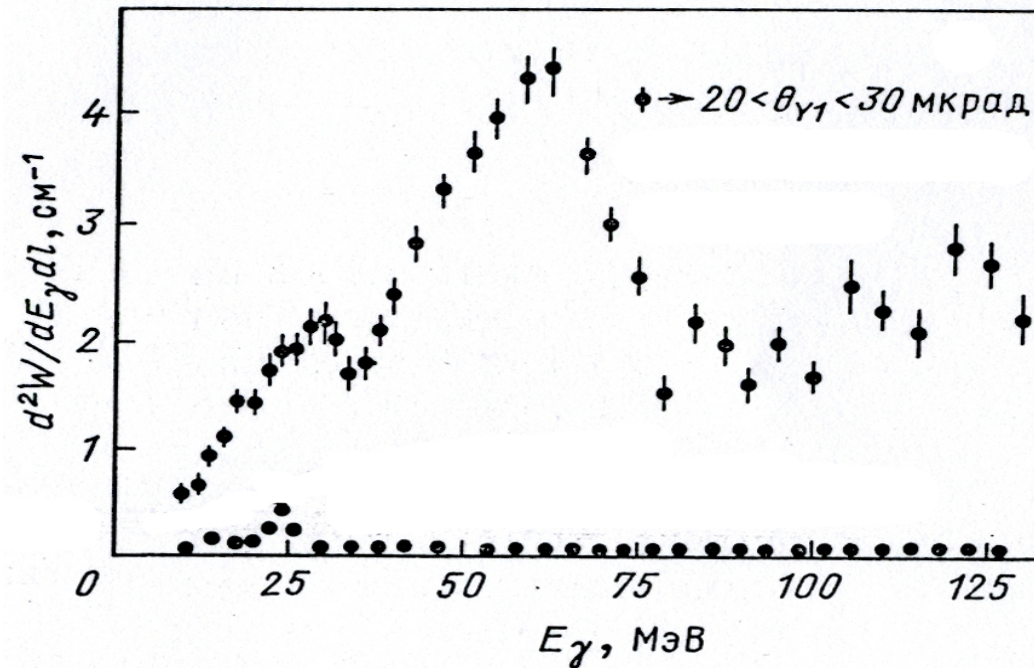
CB



H.Bilokon et al. NIM, 1983

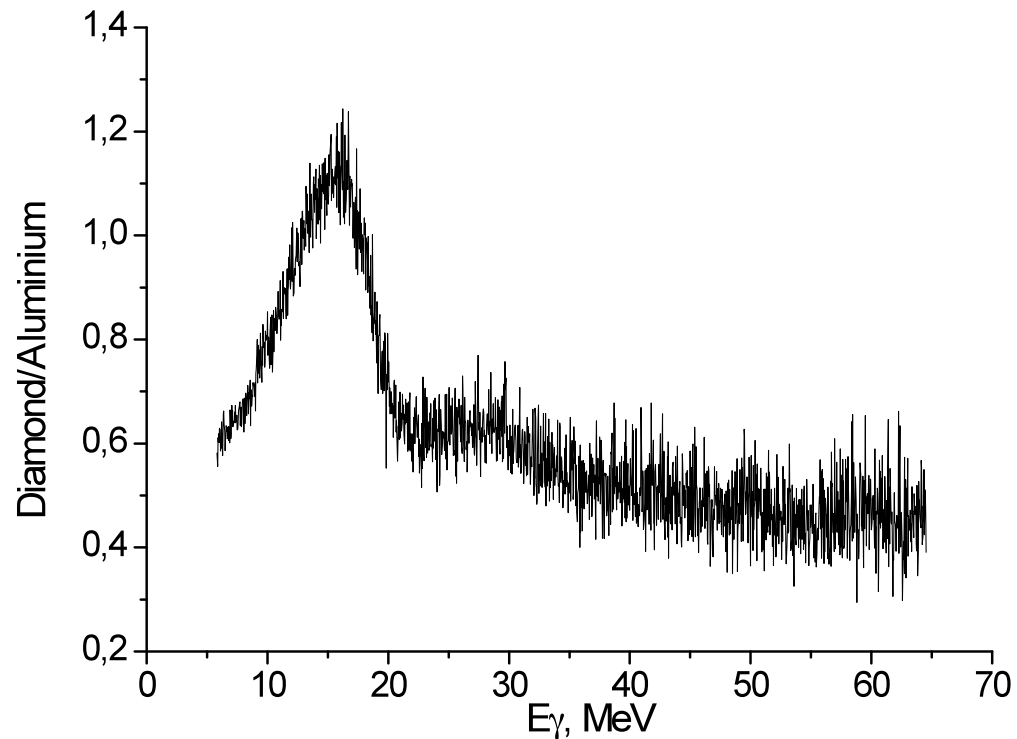
$\epsilon = 150 \text{ GeV}$

# IPHE experiment E.Tsyganov et al, 1982



$\varepsilon_+ = 10 \text{ GeV}$ , *plane channelling*

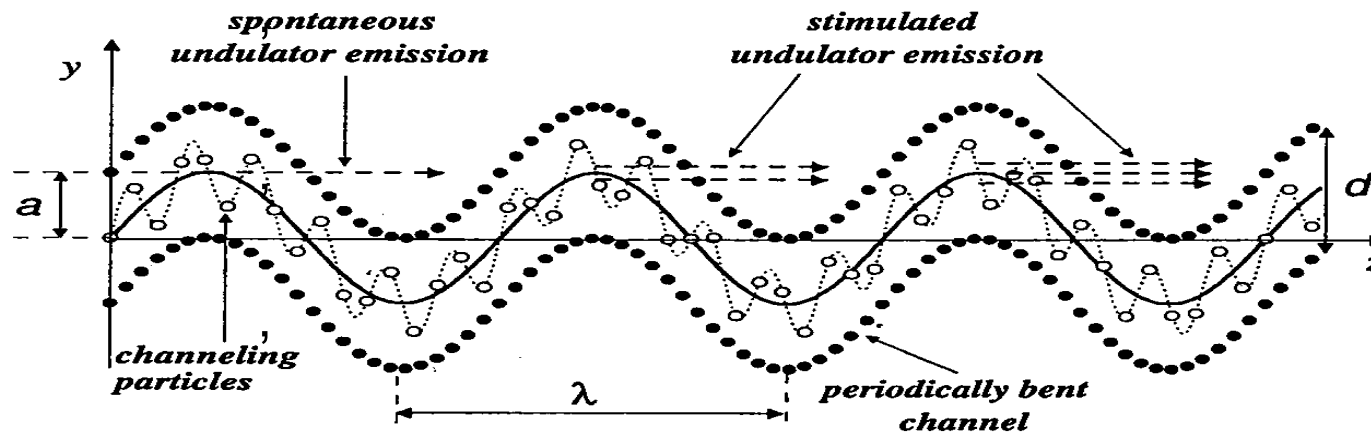
CB for 150 MeV electrons  
2008 Experiment at Max lab (Sweden)



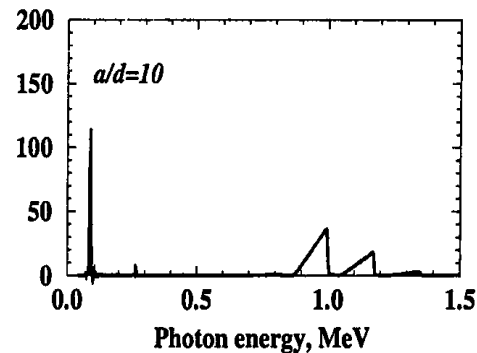
**Fig.10. Spectra of the CB from a diamond crystal of thickness 0.1 mm normalized to the bremsstrahlung spectrum from amorphous Al target. Collimation angle  $\theta_c \sim 0.73\gamma\theta$ . Electron energy is 143.9 MeV.**



# Radiation in the Field of Periodically Deformed Crystal Planes of Atoms at the Channeling



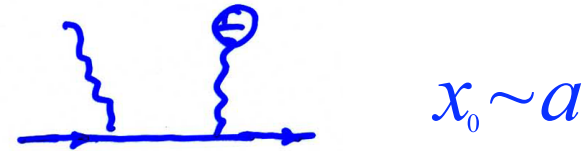
$$d \ll a \ll \lambda \quad d \sim 10^{-8} \text{ cm} \quad a \sim 10 \cdot 10^2 d \quad a \sim 10^{-5} \cdot 10^{-4} \lambda$$



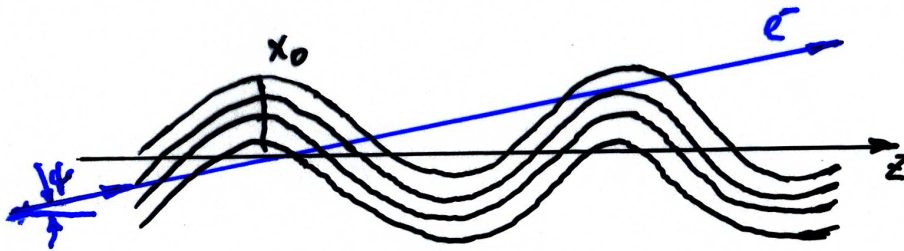
1.L.Sh.Grigoryan, A.R.Mkrtchyan, A.H.Mkrtchyan et al, Nucl. Instr. and Meth. in Physics Research B **173**, 132 (2001).

2.A.V.Korol, A.V.Solov'yov and W.Greiner, Int. J. Mod. Phys. E **13**, 867 (2004).

# Coherent Radiation in Periodically Deformed Crystal Planes



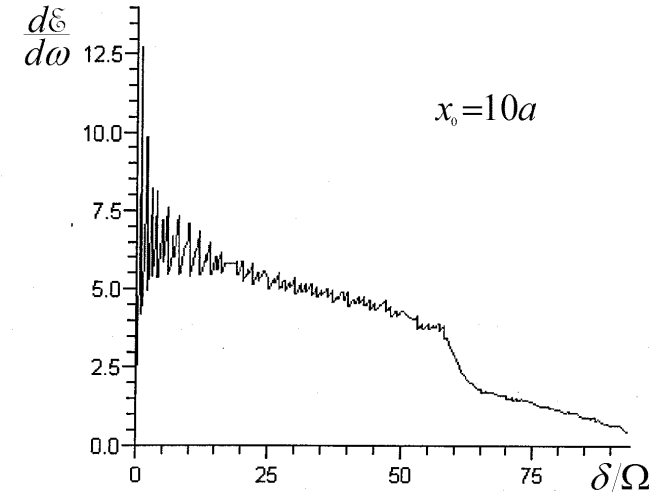
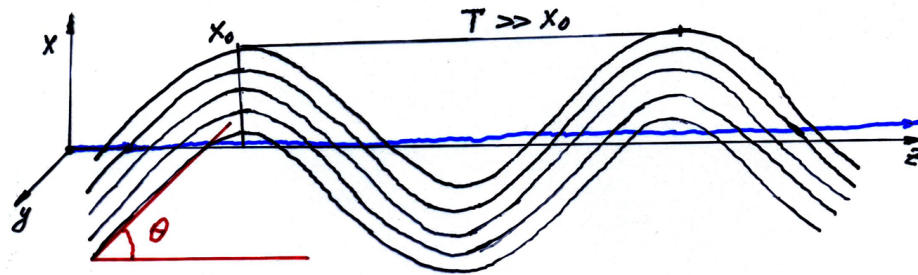
A.Saharian, A. Mkrtchyan  
et al. (2004)



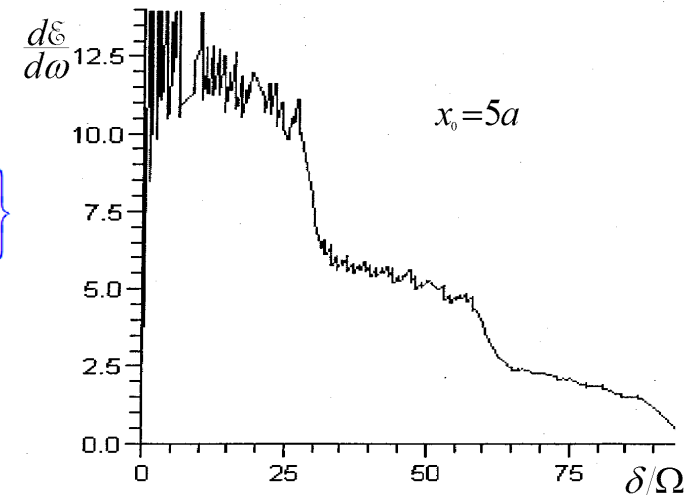
$$x_0 \gg a$$

Born & Semiclassical Approx.  
N.Shul'ga, V. Boyko JETP Lett, 2006

# Coherent Radiation Spectrum by Relativistic Electrons in Periodically Bent Crystal Planes

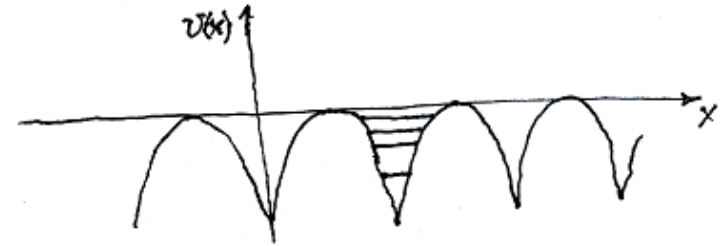


$$\frac{d\xi_c}{d\omega} = N \frac{32\pi^2 Z^2 e^6}{a^3} \frac{\delta}{m^2} \sum_{\Omega n \geq \delta} \sum_{g_x} \frac{g_x^2 J_n^2(g_x x_0)}{(g_x^2 + R^{-2})^2} \frac{1}{(\Omega n)^2} \left\{ 1 - 2 \frac{\delta}{\Omega n} \left( 1 - \frac{\delta}{\Omega n} \right) \right\}$$



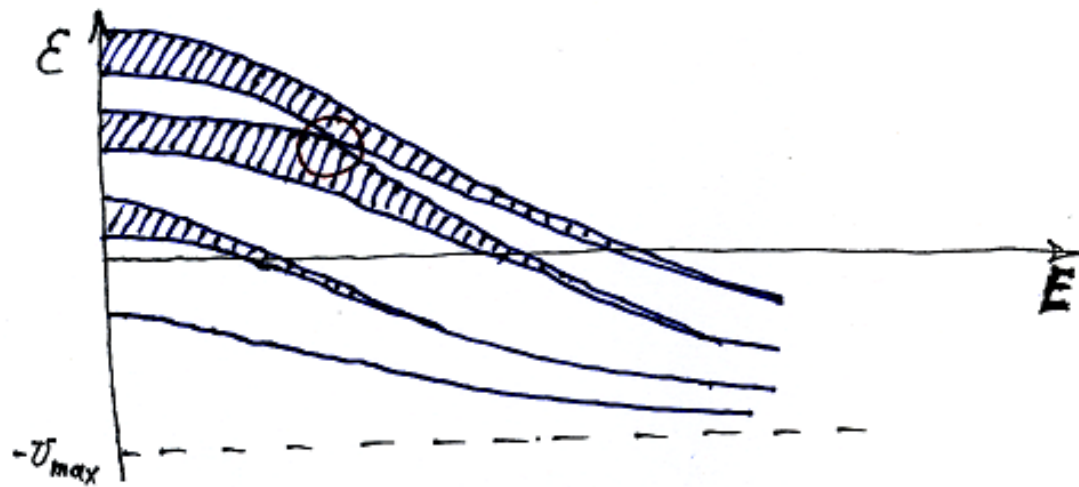
## Energy levels at plane channelling

$$\left[ \frac{\hat{p}_x^2}{2E} + U(x) \right] \psi(x) = \epsilon \psi(x)$$



$$\epsilon_n \text{ from } \oint p(x) dx = 2\pi n \hbar$$

$$n_{\max} \sim \sqrt{E_{\text{MeV}}}$$



# Conclusions

