



# **Muon Channeling and the Need to Investigate Negative Particle Channeling and Collimation**

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# Landscape for TeV-scale channeling

## “Recent” developments

collimation

volume reflection, capture

Vorobiev & Taratin

RHIC

Tevatron

famous CERN H8

short crystals

## LHC collimation

protons from 1-7 TeV

very active ...

## Everything else

extraction, e. g. at LHC

collimation at an ILC, e+-

but really not so hard,

also later

muon collider

even further away

Fermilab 99/069 study

crystal collimation

not appropriate

but may be different at

high energy

# Update on Tevatron crystal collimation studies

## History

2005 – Reproduced RHIC results with “O” crystal

2007 – tried 3 mm, 150  $\mu$ rad bend, problems -...

2008 – “O” back, better goniometer, instrumentation



Mokhov

## T980 – CCE Crystal Collimation Experiment

Fermilab, LARP, CERN, BNL, INFN, IHEP, PNPI, JINR,  
RINP-BSU, Chicago, ...

several phases over 2008-2010 for collimation in 1, 2 planes,  
possible single particle, simulation, etc.

linked with SPS collimation experiment

artificial halo, single particle, ...

Oct. 29 half day workshop at Fermilab on channeling collimation  
in conjunction with LARP CM11 and **session here today**

**Dean Still and others have made significant progress in Sept, Oct.**

## Crystal collimation at LHC: Ralph Assmann's concerns (from Channeling 2006)

Crystals are an interesting advanced technology for phase 2 of LHC collimation. To evaluate benefit in detail the following information is required:

- How to handle different LHC energies from 450 GeV to 7 TeV?
- Probability spectrum for proton deflections (channeling and others). **Include all effects down to  $10^{-5}$  probability!**
- Sensitivity to beam angle and angular spread?
- Number, opening (impedance) and locations of absorbers. Damage limit of crystal for instantaneous shock beam impact (expect  $\sim 3$  MJ,  $0.2 \times 1.0$  mm, 200 ns).
- Damage limit of crystal for integrated dose (expect  $\sim 5 \times 10^{16}$  p/year at 7 TeV).
- Handling of crystal during normal operation: 500 kW power impact.
- Requirements for alignment and operational set-up (tolerances, time, ...)?

(missing from list – crystal questions)

**Recent LHC incident may increase emphasis on collimation even more!**

# Incomplete TeV-scale channeling topics

## **Negative particle channeling and bending**

hadrons, relation to  $e^-$  and channeling radiation

not important for LHC collimation – pp collider

## **Muon channeling for futuristic possibilities**

(collimation for muon colliders – Tollestrup)

# Negative particle channeling

## early eighties thinking:

large discrete angular deflections like external beam.

## collimation is different

any kick, provided it is more than multiple scattering  
multi-pass channeling helps.

high energy helps

**We need more information on negative channeling, negative bending!**

Could one channel and collimate antiprotons at the Tevatron?

Could one collimate  $e^+/e^-$  at ILC?

In TOTEM, etc. at LHC could one deflect negative particles such as antiprotons?

## Functional form of planar dechanneling

$$\lambda_D = 1.62 \frac{\psi_{cp}^2}{\langle \Theta^2 \rangle_c}$$

where

$\psi_{cp}$  is planar critical angle

$\langle \Theta^2 \rangle_c$  is the mean square mult scat angle in channel

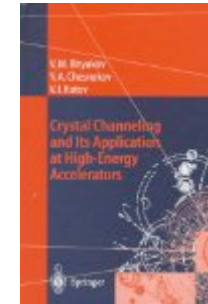
(see Feldman & Appleton, PRB8, 935 (1973), Carrigan FN-454,

Biryukov, Chesnokov, and Kotov (BCK))

For (+) BCK treatment (1.50) leads to:

$$\lambda_D = \frac{256}{9\pi^2} \frac{p v}{\ln(2m_e c^2 \gamma / I) - 1} \frac{a_{TF} d_p}{Z_i r_e m_e c^2}$$

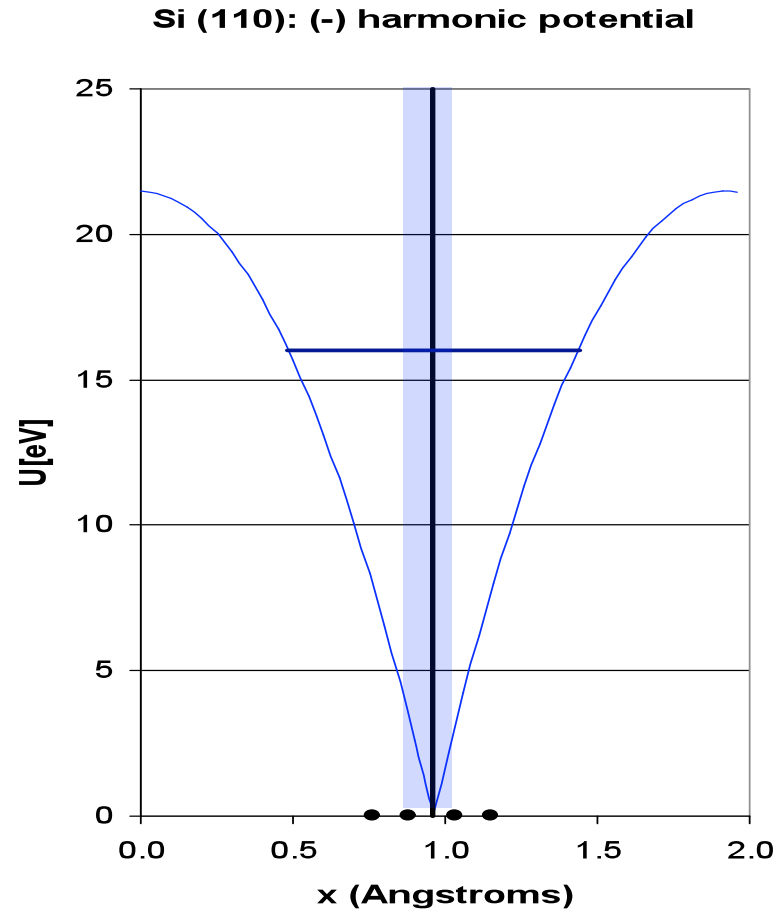
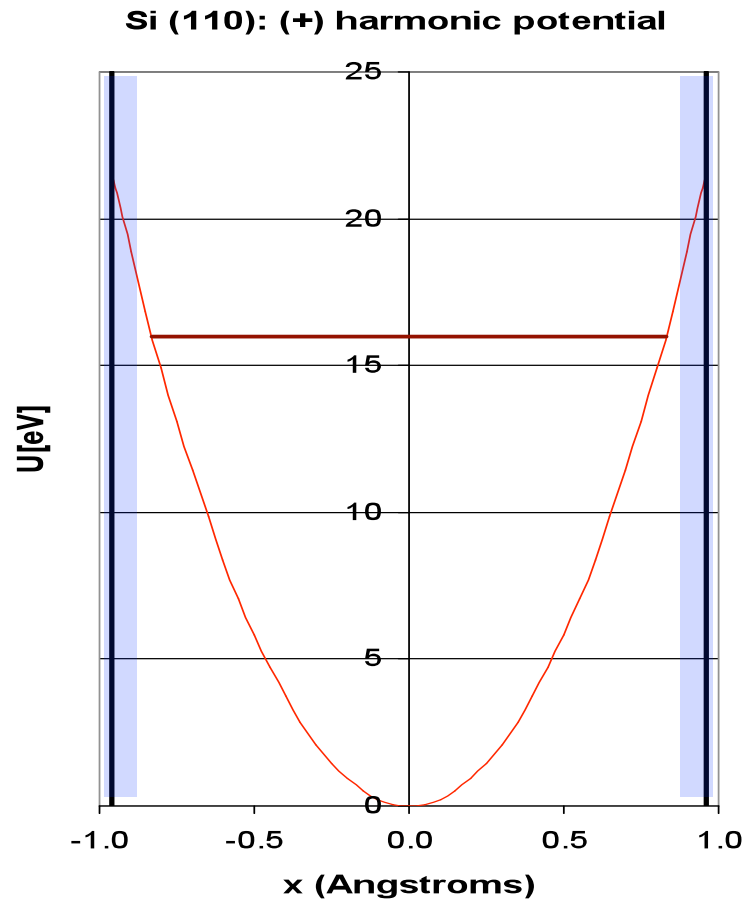
$\lambda_D = 51$  cm for (+) @ 1 TeV (roughly  $\sim E$  - note log term,  $\sim 20\%$  effect)



Biryukov  
Chesnokov

Kotov

# Potentials for + and - particles to get $\psi_p$



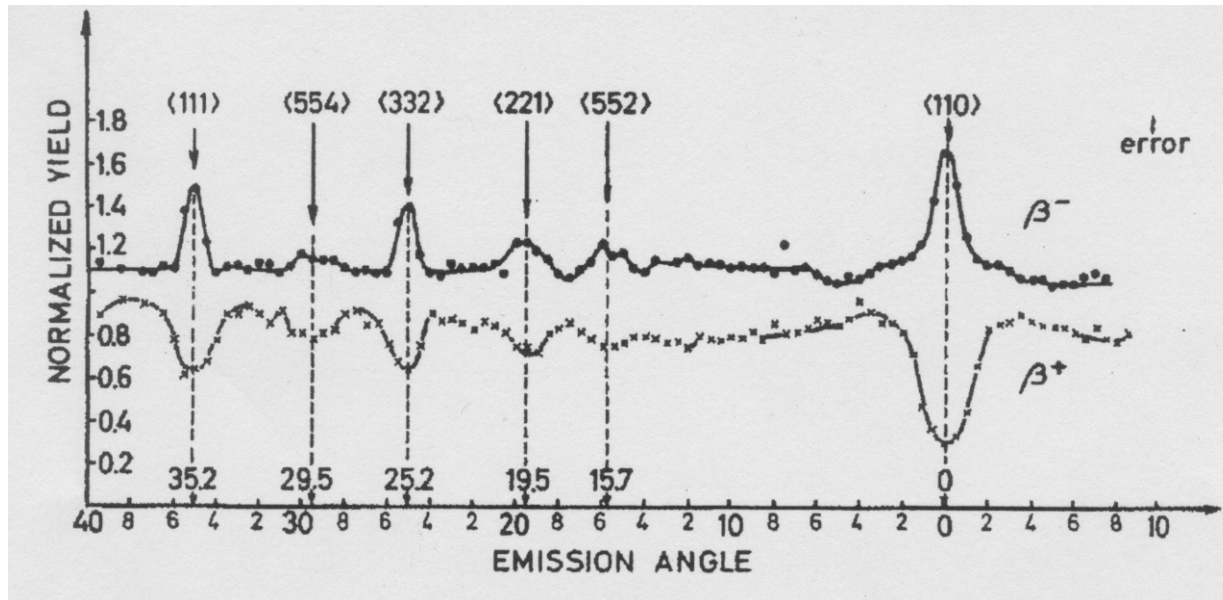
[see, e. g., Taratin and Vorobiev, Phys. Lett A119, 425 (1987)]



## Some Aarhus +/- results showing $\psi^- < \psi^+$

Implanted radioactive  $^{64}\text{Cu}$  in a Cu crystal –

(E. Uggerhoj, Andersen, Can. J. Phy. **46**, 543 (1968))



U. Uggerhoj

Antiproton Channeling at 1.4 MeV (U. Uggerhoj, et al , NIMB207, 402 (2003))

For antiproton axial channeling find critical angle is about 0.6 of the critical angle for protons. Agrees with theoretical calculations

## Negative hadronic channeling

Then for

$$\lambda_D = 1.62 \frac{\psi_{cp}^2}{\langle \Theta^2 \rangle_c} \quad \text{Where } \langle \Theta^2 \rangle_c \text{ follows from}$$

$$\frac{\left. \frac{d^2 \Omega}{dx} \right|_e}{\left. \frac{d^2 \Omega}{dx} \right|_n} = \frac{\left. \frac{d^2 \Omega}{dx} \right|_+}{\left. \frac{d^2 \Omega}{dx} \right|_-} = \frac{(m_e / 2M_i E)(4\pi e^4 / m_e v^2) N Z L_e}{(M_t / M_i E)(4\pi Z^2 e^4 / M_t v^2) N L_n} = \frac{L_e}{2Z L_n} \Rightarrow \frac{X_0^n}{X_0^e}$$

where  $L_i$  are the log terms in multiple scat. Set  $L_n/L_e = 2$ .

Get for 1 TeV as an approximation neglecting details of nuclear density.

$$\lambda_- = \left( \frac{\psi_-}{\psi_+} \right)^2 \frac{\lambda_+}{2Z(L_n/L_e)} = \left( \frac{0.48 A}{0.83 A} \right)^2 \frac{51 \text{ cm}}{2 * 14 * 2} = 3 \text{ mm}$$

## Negative hadronic channeling - continued

But - potential well is not filled with ions, only  $\pm u_T$   
 a weighting might be

$$Z_{eff}^- = \frac{2u_T Z + 2(d_p / 4 - u_T)}{d_p / 2}$$

so that  $Z_{eff} = 3$  rather than 14 for 1 TeV Si(110)  
 giving  $\lambda(1 \text{ TeV}) \sim 14 \text{ mm}$

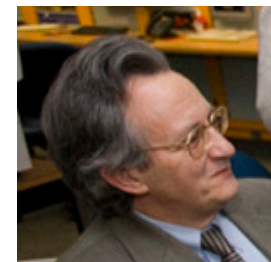
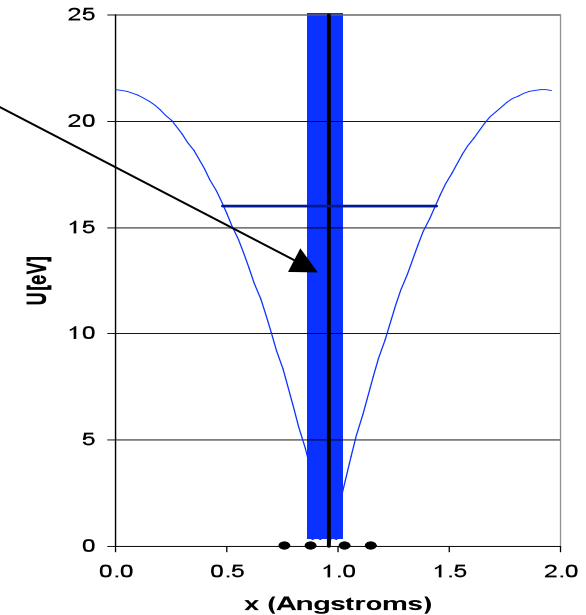
Of course, particle more in center of channel, ...

This range (3 to 14 mm) is short but have used:

3 mm strip crystals

Quasimosaic crystals (.03, 1 mm at CERN H8, H4)

Si (110): (-) harmonic potential



Scandale-H4,H8

# Straight crystal dechanneling for negative particles

Going beyond hand waving (or hand wringing) need:

- a diffusion model treatment for the negative particle case
- or a simulation ala CATCH or BINCOL

Would like array of (+/-)

$$E = 0.07, 0.4, 1, 7 \text{ TeV}$$

$$R = 0.1, 0.25, 0.5 R_T$$



Little experimental information on  
straight negative hadronic dechanneling

## Bending of negative particles

The critical bending or Tsyganov radius is:

$$R_T \approx \frac{pv}{\pi N d_p Z e^2} = \frac{pv(\text{GeV})}{5.7 \text{ GeV/cm} [\text{Si}(110)]}$$

At +1 TeV in Si is ~175 cm (BCK 2.17). For the negative case,

the effective  $d_p$  could be smaller and  $R_T$  larger

The bending dechanneling length is:

$$\lambda_D(pv, R) = \lambda_{D,0} \left(1 - \frac{R_T}{R}\right)^2$$

If  $R \gg R_T$  then for negative particles  $\lambda_D(pv, R)$  will be the negative particle dechanneling length, so **it will be short**

Negative particle bending measurements do give a tool to measure dechanneling in principle



Tsyganov

## Negative hadron bending

Bak et al. did studies of negative particle **axial deflection** at 10 - 12 GeV with pions [S. Anderson et al., Nucl. Phys. B167, 1 (81), J. Bak, et al., Nucl Phys. A389, 533(82)]

Schiott simulated their data using BINCOL in Carrigan and Ellison (*Relativistic Channeling*, NATO 165, Plenum (87)).  
Saw only small effects on order of critical angle.

I extract an upper limit on the bending dechanneling length of O(2 mm) from Baurichter et al. studies of negative  $\pi^-$  **axial deflection** at 200 GeV. [A. Baurichter et al., NIM **B119**, 172 (1996)]

$\sim 0.6 < \lambda_- < 3$  mm from the formula and the ansatz for the planar case.

H4, H8 (Bolognini thesis-fig. 4.21a) gives O(1 mm)  
@150 GeV for (111) in a quasi mosaic crystal

# Negative particle volume reflection

Taratin and Vorobiev (1987)

In computer model positive particle

**deflect  $\sim 2\psi_{cp}$  away from bend**

negative particle somewhat less.



Taratin

Biryukov [2006 – EPAC, Phys. Let B645, 47 (2007)]

Tevatron simulations for proton and antiprotons.

Antiproton effect nearly as strong as proton in volume reflection

Maisheev – analytic treatment

[PRST 10, 084701 (2007)]

This can be used to extrapolate to different energies, radii

Angles for positive case are 1.8 times larger than negative.

**For a contrary view on (-) case see**

**Kovalev arXiv:07073935v2, arXiv:0712.0858v1**

**No experiments have been reported but CERN H4 now has info**

## Negative volume capture

Volume capture deflects in the direction of the bend

Volume capture is a feeding-in process that follows reversibility

This means it will be characterized by a feeding-in length

functionally similar to a dechanneling length

since negative particle dechanneling is stronger

feeding-in will be stronger

but once in a channel particle will also dechannel faster

The theory of negative particle volume capture has apparently not been discussed

However simulations such as Biryukov's should implicitly contain it.

**No experiments have been reported**

[discussions of positive particle volume capture have been given by

Sumbaev (circa 79), Samsonov (C&E-87), and BCK sec 2.3.1]



# Studying negative particle channeling

## Tevatron – anti protons (Dean Still)

- prefer  $<1$  mm thick crystal, 5 mm might work
- redo proton, antiproton helices locally at E0 (goniometer)



Still

- or remove proton store. Both need serious setup
- need a nearby antiproton downstream collimator, detector – something exists at E0 for Tevatron

## Fermilab Meson Area Beams

Meson test beam – a problem is energy fairly low

MIPP – also a problem with low beam energy

# Other possibilities for negative particle channeling

## CERN

H4- this last summer did 150 GeV negative  $\pi$ , k,  $\mu$  mesons  
used thin crystals ( $\sim 1$  mm thick). Also used H8 in fall 2007

## Serpukhov

lower energy beams than CERN

## KEK

ATF – Endo et al, expression of interest – with 1.3 GeV tightly focused  
electron beam  
problem – channeling radiation

# Muon channeling

**Does high energy muon channeling answer fundamental questions?**

Not really!

Point is that dechanneling length does not depend on nuclear interactions

$L_{\text{col}}(\text{Si}) = 30 \text{ cm}$ ,  $L_{+}[\text{Si}(110)] \sim 51 * E(\text{TeV}) \text{ cm}$ , equal at  $\sim 0.6 \text{ TeV}$   
 $L_{-}[\text{Si}(110)] \sim 3 \text{ mm} * E(\text{TeV})$ .

nuclear density higher for negatives  $O(d_p/4u_T)$  or factor of 6

$L_{\text{col}}$  is still 100 times longer at 1 TeV, 15 times at 7 TeV

weakly interacting particle does not teach anything

**Critical energy for muons in Si is 470 GeV**

Bremsstrahlung cross section

$$\sigma_{\mu} = \sigma_e \left( \frac{m_e}{m_{\mu}} \right)^2$$

so much less radiation/unit length

but negative muons in high  $Z^2$  region

## Muon channeling - continued

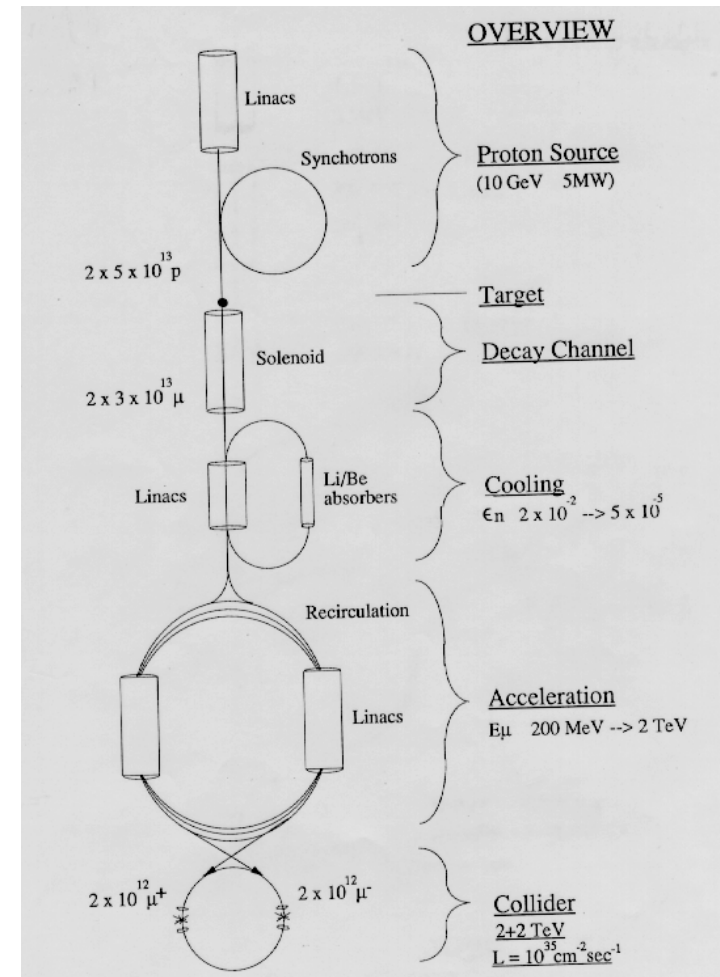
Potentially might be interesting for  
collimation in a **futuristic muon collider**  
or **neutrino factory**

50 on 50 GeV “low” energy muon colliders  
collimation no challenge (see Drozhdin et  
al. FERMILAB-Conf – 99/069)

But for higher energies more of a problem  
short quasimosiac bends using axial  
channeling might begin to be useful

Available information

little experimental muon channeling data,  
mostly from pion implantation  
no theoretical evaluations?



# Muon channeling experiments

## Particle identification

use a hadron absorber in front of detector

typically 8 – 10 nuclear interaction lengths or 1.5 m iron.

At 50 GeV:  $\Theta_{\text{ms}} = 800 \mu\text{rad}$  compared to  $\Psi_{\text{cp}} = 28 \mu\text{rad}$

## Muon beams

Muon beams are tertiary beams

process is  $p \gg \text{pions} \gg \text{muons and neutrinos}$

(450 GeV)      (50 GeV)      (<25 GeV)

Need space for pion decay

but even an ordinary pion beam has some muon contamination

**But** want information at TeV scale!

Rate lower at higher energy, but for channeling may be OK

## Muon experiments at CERN?

per Gatignon: M2/COMPASS @ 160 GeV/c has  $2E^8/\text{spill}$  (+, /3 for -),

$\Theta \sim 600 \mu\text{rad}$ ,  $\sigma \sim 20 \text{ mm}$

I hear that in the H4 run @CERN this summer the beam was 50% muons

# Summary

## Negative hadronic channeling studies interesting for:

planar and axial cases for normal bending

volume reflection

volume capture

Short crystals via anticlasic or quasimosaic techniques important

## Muons:

difficult experimentally but H4 ran last summer @ CERN

not clear there is much interesting channeling physics

no mid-range applications

**For more Fermilab channeling information see:**

**Channeling home:**

[http://home.fnal.gov/~carrigan/Channeling/Channeling\\_master.htm](http://home.fnal.gov/~carrigan/Channeling/Channeling_master.htm)

**Channeling Formulary:**

[http://home.fnal.gov/~carrigan/Channeling/Channeling\\_formulary.htm](http://home.fnal.gov/~carrigan/Channeling/Channeling_formulary.htm)

# Questions?

# Negative hadron and $e^+/e^-$ channeling?

## $e^+/e^-$ channeling

- channeling radiation impact must be considered
- crystal lengths must be short
- not so much dependence on charge
- little or no experimental information at high energy, particularly for bending



## e<sup>+</sup>/e<sup>-</sup> dechanneling lengths (microns, normalized to 1 GeV)

Critical energy for e<sup>+</sup>/e<sup>-</sup> in Si is 53 MeV but not so significant for channeled particle

Process	e <sup>+</sup> dechan (microns)	e <sup>-</sup> dechan (microns)	Energy MeV	Comment	Author
Planar theory	500		1000	Si(110),1/2	Belosh. & Trik
	700	130 qua, 13 pure	1000	Si(110),1/e	Belosh. & Kom.
Planar experiment	1100 (60 – oc len)	660 (36)	54	Si(110),1/e	Livermore
		88 (31)	350	Si(110),1/e	Komaki
		23 (28)	1200	Si(110),1/e	Adejshvili
Axial theory		13	1000	Si<111>,?	Muralev
		18		Si<111>,1/2	Taratin & Vorob
Axial experiment		32 (39)	1200	Si<111>,1/e	Adejshvili

**Problems: Old and incomplete data!** consistency, agreement of experiments (angular divergence), too little data, statistical estimates on data, theory challenges but some recent work at 5 GeV for undulator possibility (Korol et al. Physics/0412101 v1)

## Summary of coherent bend effects

Effect	Angle dist	Deflection	Magnitude	Comment
<b>Volume reflection</b>	$\Theta_d \sim \varphi_c \sim 1/(p\beta)^{1/2}$	Away from bend	Strength same as channeling	Cumulative with beam passes
<b>Volume capture</b>	Up to full bend	Toward bend	$w_s \sim \text{const} \frac{R}{(p\beta)^{3/2}}$	Small at high energy
<b>Miscut</b>	Lowers deflection	Toward bend	0 to full deflection	
<b>Relaxed bend</b>		Smaller bend		Ruled out by whole arc distribution
<b>Something else</b>				Keep an open mind

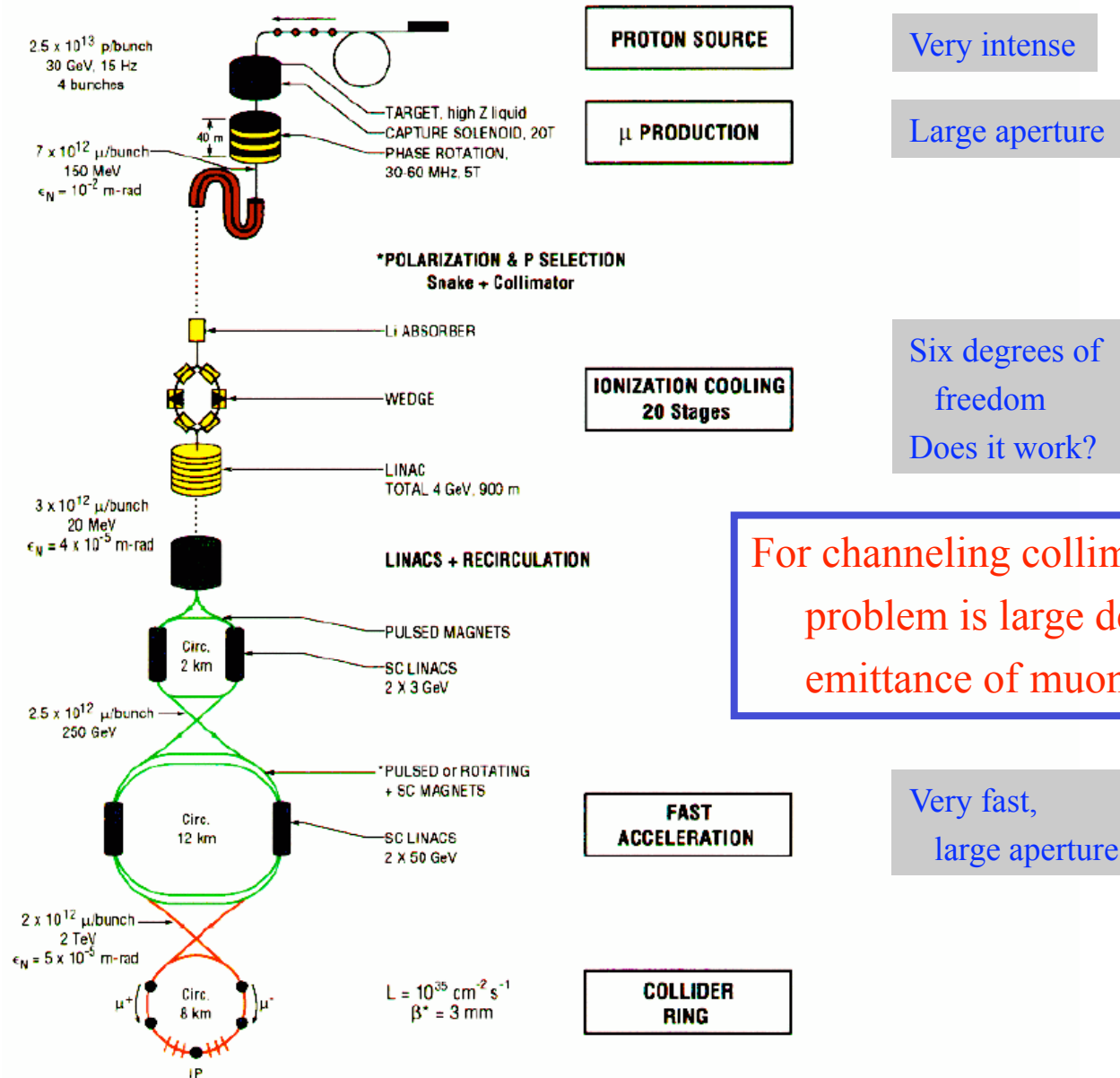
## Electrons

with innovative short bends might be able to do electron bending

**this is a regime where GeV scale machines could contribute  
electron/positron dechanneling below 1 GeV down to 10 – 20 MeV  
old information may not be consistent**

# Muon collider schematic

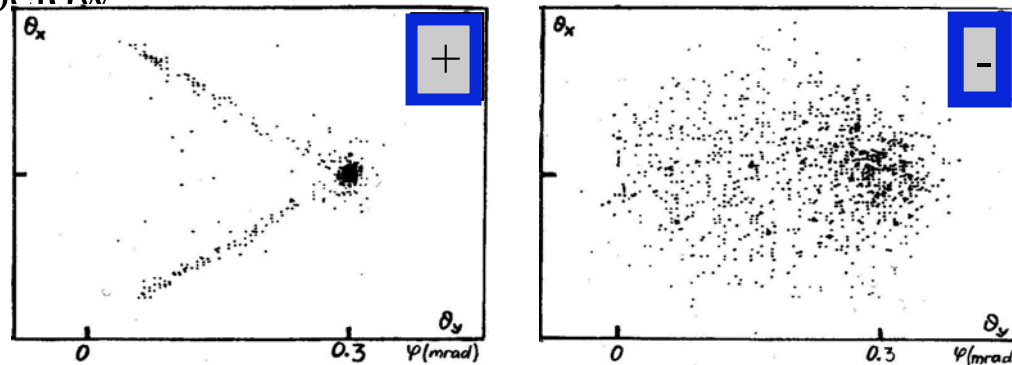
(taken from Bruce King-BNL, 4th International Conference on the Physics Potential and Development of mu+mu- Colliders, San Fransisco, 1997.)



## Negative hadron and e<sup>+</sup>/e<sup>-</sup> channeling -continued

Taratin & Vorobiev, Phys. Lett. A119, 425 (1987) also discuss negative bending **simulation**.

More recently Greenenko and Shul'ga [NIM B90, 179 (94)] studied negative deflection with a **simulation** program. For **axial** channeling at 400 GeV they saw deflection at the same scale as the Schiott simulation. Their distributions for 100 GeV hadrons bent in a 3 cm crystal are shown below:

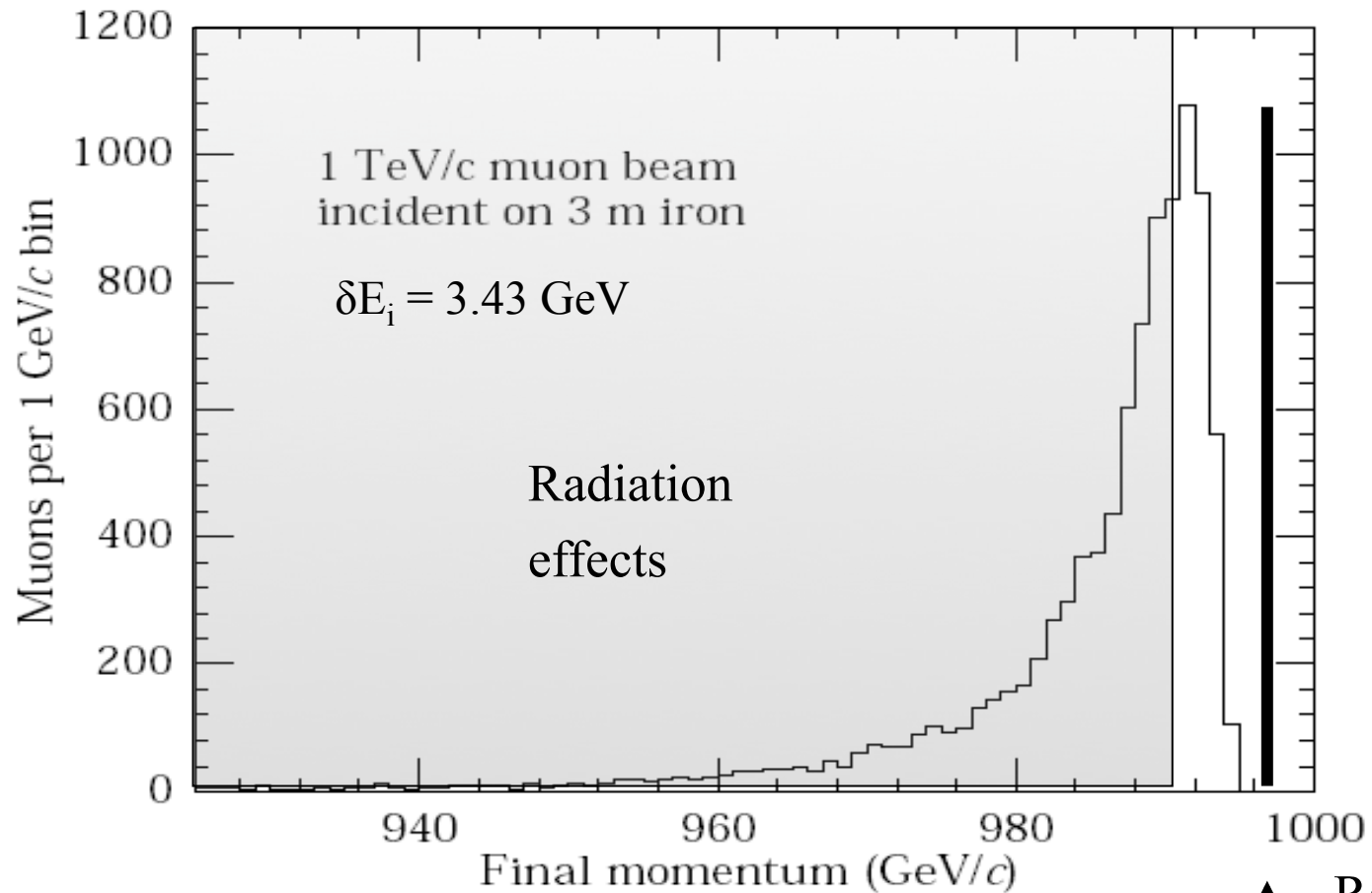


Note that the negative deflection is of the same order as the positive case but very diffuse. **Volume reflection or capture?**

$$\Theta_b = 0.3 \text{ mrad}, \psi_{ca} = 0.04 \text{ mrad}$$

$$\Theta_{\text{axis}} = 0.3 \text{ mrad}$$

# Muon energy loss – small!



Random ion.  
alone

From S. Eidelman, et al, Phys. Lett. **B592**, 1 (2004), see Groom & Klein (99) fig 23.19