

The physics case for a DAΦNE upgrade

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- Introduction

- General considerations about future low–energy experiments
- Dreams & realistic possibilities for DAΦNE [*the Alghero heritage*]

- The unique features of a super Φ –factory for kaon physics

- General considerations

- A few selected examples:

1. CPT tests
2. Interferometry
3. The V_{us} saga
4. Rare (but not impossible...) decays
5. Charge asymmetries, $\pi\pi$ phases *et al.*

- My conclusions

• Introduction

General considerations about future low–energy experiments

Within a few years we shall enter in the **LHC** era

Possible scenarios ~ 2010:

- LHC has started and has clearly seen signals of NP
- LHC has started but has not seen any clear NP signal
- [*LHC has not started yet...*]

Within all these scenarios still important & interesting
to perform high–precision low–energy experiments

Some of the main arguments why it is still important to perform high-precision low-energy experiments in the LHC era:

→ No competition with LHC as far as the NP search is concerned [with some remarkable exception], but full complementarity for the identification of the symmetries of the NP model

I. Study of rare & forbidden processes: $(g-2)_\mu$, $K \rightarrow \pi\nu\nu$, CPT, ...

→ Several SM parameters [Yukawa sector], which are likely to play a fundamental role in the identification of the underlying theory, can only be measured at low energies

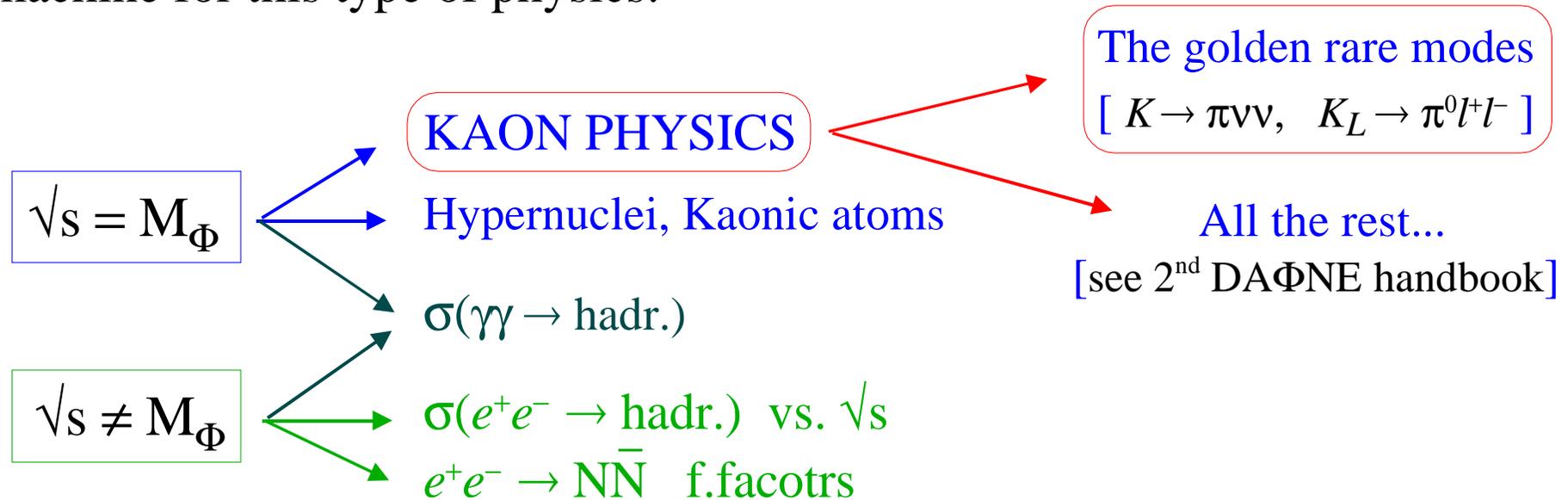
II. Precision measurements of V_{CKM} , m_q , α_i

→ There are still interesting aspects of non-perturbative QCD which are not fully understood and need to be investigated

III. CHPT studies for K & π decays, exotic bound states [had. atoms, hypernuclei], e^+e^- & $\gamma\gamma \rightarrow \text{hadr.}$ form factors, ...

Dreams & realistic possibilities for DAΦNE

In principle an e^+e^- machine with flexible c.o.m. energy up to $\sqrt{s} \sim 2.5$ GeV and very high luminosity at the Φ peak would be an ideal machine for this type of physics:



The Alghero Conference
[www.lnf.infn.it/conference/d2]

Highlights of the kaon–physics program @ Φ –factory vs. luminosity:

10^0 fb^{-1}
 $[\approx 10^9 K\bar{K}]$

\approx KLOE
 now

V_{us} from K_{l3} @ 10^{-3} (CKM);
 rare K_S decays down to $\text{BR} \sim 10^{-8}$ (CHPT/CPT);
 10^{-2} bounds on $K_S \rightarrow \pi l \nu$ charge asym. (CPT)
 :

10^1 fb^{-1}
 $[\approx 10^{10} K\bar{K}]$

original
 KLOE
 program

$\text{Re}(\epsilon'/\epsilon)$ @ 10^{-4} (direct CPV);
 $K_{L,S}$ interf. $\Rightarrow \text{Im}(\epsilon'/\epsilon)$ @ 10^{-2} (CPT);
 $\pi\pi$ phases from K_{l4} @ % level (QCD vacuum)
 :

10^2 fb^{-1}
 $[\approx 10^{11} K\bar{K}]$
 $[10^{34} \text{ cm}^{-2} \text{ s}^{-1}]$

CPT tests @ unprecedented level of precision via
 rare K_S & $K_{L,S}$ interferences;
 search for exotic direct CPV in K^\pm asym. and rare K_L decays
 :

10^3 fb^{-1}
 $[\approx 10^{12} K\bar{K}]$

frontier
 of
 flavor
 physics

sensitivity to $K_L \rightarrow \pi^0 \nu \nu$ (& $K_L \rightarrow \pi^0 e e$) at the SM level:
 region of high discovery potential for non–standard sources
 of CPV via new tests of the CKM mech. in the kaon system

\Rightarrow very interesting also in a long–term perspective \Leftarrow

10^4 fb^{-1}

:

$K_L \rightarrow \pi^0 \nu \bar{\nu}$ cannot be measured

It has been said so often:

$$\Im V_{td} V_{ts}^* = A^2 \lambda^5 \eta = 25.6 \sqrt{\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu})}$$

$$\text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) = 3 \times 10^{-11}$$

$10 \text{ eV} / 3 \times 10^{-11} = 3.3 \times 10^{11} \text{ K's}$. @1% dec/ ϕ , need $100 \times 3.3 \times 10^{11} = 3.3 \times 10^{13} \phi$'s or $1.1 \times 10^{13} \mu\text{b}^{-1}$. In one year, need $\mathcal{L} = 10^6 \mu\text{b}^{-1}/\text{s}$ or $\mathcal{L} = 1 \times 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$. For one hundred events, $\mathcal{L} = 1 \times 10^{37} \text{ cm}^{-2} \text{ s}^{-1}$ or 10 year running.

J_{12}

$$h = A^2 \lambda^5 \eta (\times 10)$$

$$\lambda(1 - \lambda^2/2)$$

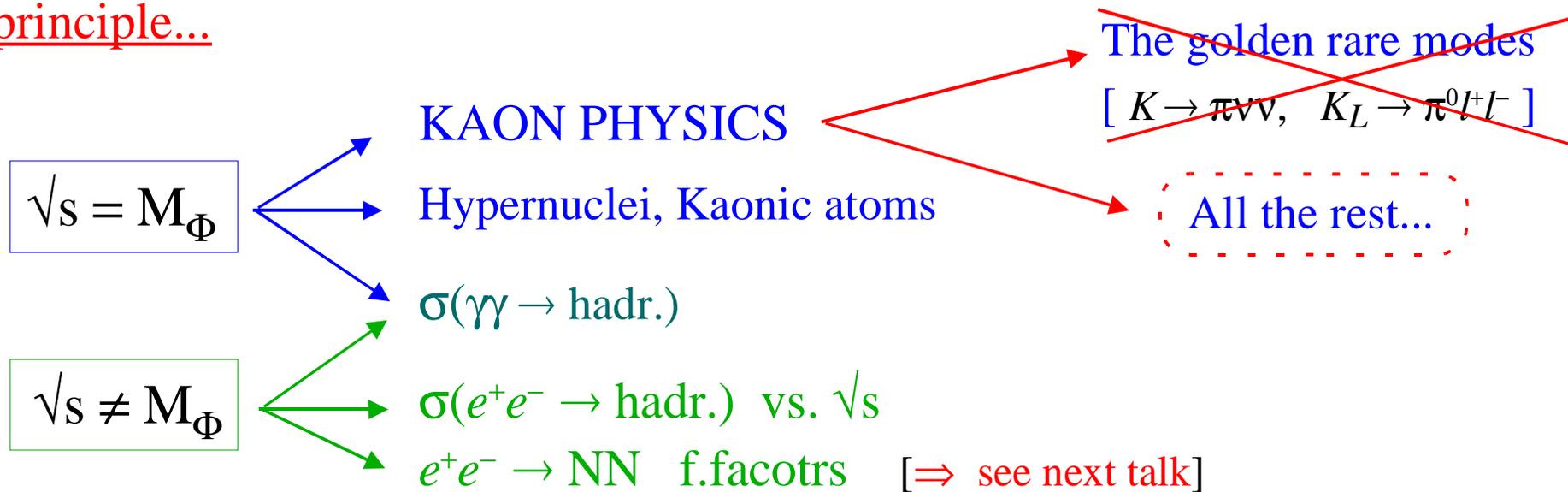
To get η need λ and A !

$\delta(A^2 \lambda^5) / (A^2 \lambda^5) \sim 5.6\%$, K. Schubert, LP03. Optimistic?



Dreams & realistic possibilities for DAΦNE

In principle...



In practice we need to take into account that:

- If $L < 10^{35} \text{ cm}^{-2}\text{s}^{-1} \Rightarrow$ No chance for the rare golden modes
[even if enhanced over SM expectations]
- Strong external competition on almost all the remaining items from other machines/experiments
- Serious internal (time) competition between the Φ & non- Φ options
[extrapolate from the present DAΦNE situation...]

- The unique features of a (super) Φ -factory for kaon physics

General considerations:

$$\Phi \rightarrow K^+K^- (50\%), K_L K_S (34\%), \dots$$

- Pure K_S beam [K_L tag] \Rightarrow Rare K_S decays [so far, the most used feature by KLOE]
- $K_L K_S$ in a pure quantum state [$L=1$] \Rightarrow Neutral kaon interferometry
- Kaon beams of known momentum \Rightarrow Great advantage for any K^\pm & K_L decay with missing energy
- K^+K^- & $K_L K_S$ in the same detector \Rightarrow Useful for CHPT & K^\pm CPV studies

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N.B.: Kaon physics has also a unique *theoretical advantage* :

several systematic theoretical tools [CHPT, Lattice, OPE, ...] able to match [not always, but in most cases...] the challenge of high-precision experiments

A few selected examples:

1. CPT tests

CPT symmetry is linked to the basic mathematical tools that we use in particle physics:

$$\text{QFT} + \text{Lorentz invariance} + \text{Locality} \Rightarrow \text{CPT}$$

These tools have intrinsic limitations [we are not able to include gravity in consistent way] \Rightarrow we should expect ~~CPT~~ at some level

But we do not have a consistent & predictive theory if we abandon these tools \Rightarrow hard to define a reference scale/size for ~~CPT~~



$$|M_{\bar{K}} - M_K| < 10^{-18} M_K \quad \text{suggestive...}$$

but not to be over-emphasized

Main message: Kaon physics offer an ideal framework to test CPT
reference scale set by the most significant experimental bounds

1.1 The charge asymmetry in $K_S \rightarrow \pi^\pm l^\mp \nu$

$$\delta_{S,L} = \frac{\Gamma(K_{S,L} \rightarrow l^+ \pi \nu) - \Gamma(K_{S,L} \rightarrow l^- \pi \nu)}{\Gamma(K_{S,L} \rightarrow l^+ \pi \nu) + \Gamma(K_{S,L} \rightarrow l^- \pi \nu)} = 2 \operatorname{Re}(\epsilon) \pm \text{CPT}$$

Assuming ~~CPT~~ only in \bar{K} -K mixing:

$$\frac{|M_{\bar{K}} - M_K|}{M_K} < 5 \times 10^{-15} |\delta_L - \delta_S|$$

$$\delta_S = (-2 \pm 9 \pm 6) \times 10^{-3} \quad [\text{KLOE '04}]$$

$$\delta_L = (3.322 \pm 0.058 \pm 0.047) \times 10^{-3} \quad [\text{KTeV '02}]$$

$$\delta_L = (3.317 \pm 0.070 \pm 0.072) \times 10^{-3} \quad [\text{NA48 '03}]$$

$$\uparrow$$

$$\sim |M_L - M_S| / M_K$$

Reference value for the
ultimate measurement of δ_S



sensitivity on $\frac{|M_{\bar{K}} - M_K|}{M_K}$
in the 10^{-19} range !

1.2 Bell–Steinberger relation

Even if **CPT** is violated, we can assume that unitarity [=the conservation of probability] holds:

$$\begin{aligned}\Gamma_K &= \sum_f A(K \rightarrow f) A(K \rightarrow f)^* \\ \Gamma_{\bar{K}} &= \sum_f A(\bar{K} \rightarrow f) A(\bar{K} \rightarrow f)^*\end{aligned}$$

They should coincide in the limit of exact CPT



$$\left[\frac{\Gamma_L + \Gamma_S}{\Gamma_S - \Gamma_L} + i \tan(\phi_{SW}) \right] \left[\frac{\text{Re}(\epsilon_M)}{1 + |\epsilon_M|^2} + i \text{Im}(\Delta) \right] = \frac{1}{\Gamma_S - \Gamma_L} \sum_f A_L(f) A_S(f)^*$$

A marvelous tool !

- Exact relation in the CPT limit
- Non-vanishing $\text{Im}(D)$ could only be due to
 - violations of CPT
 - violations of unitarity
 - new exotic invisible final states

$$\Delta = \frac{M_{\bar{K}} - M_K}{M_L - M_S} e^{i\phi_{SW}} + \dots$$

$$\phi_{SW} = \arctan \left[\frac{2(M_L - M_S)}{\Gamma_S - \Gamma_L} \right]$$

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 - violations of CPT
 - violations of unitarity
 - new exotic invisible final states

no better place to measure this combination than a Φ factory !

$$|\text{Im}(\Delta)|_{000} < 6.4 \times 10^{-6} \text{ [KLOE '04]}$$

...but still a lot of work to improve the bounds on the full contribution

2. Neutral kaon interferometry

Probably the most characteristic type of measurements for a Φ factory:

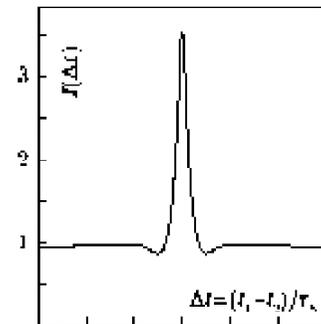
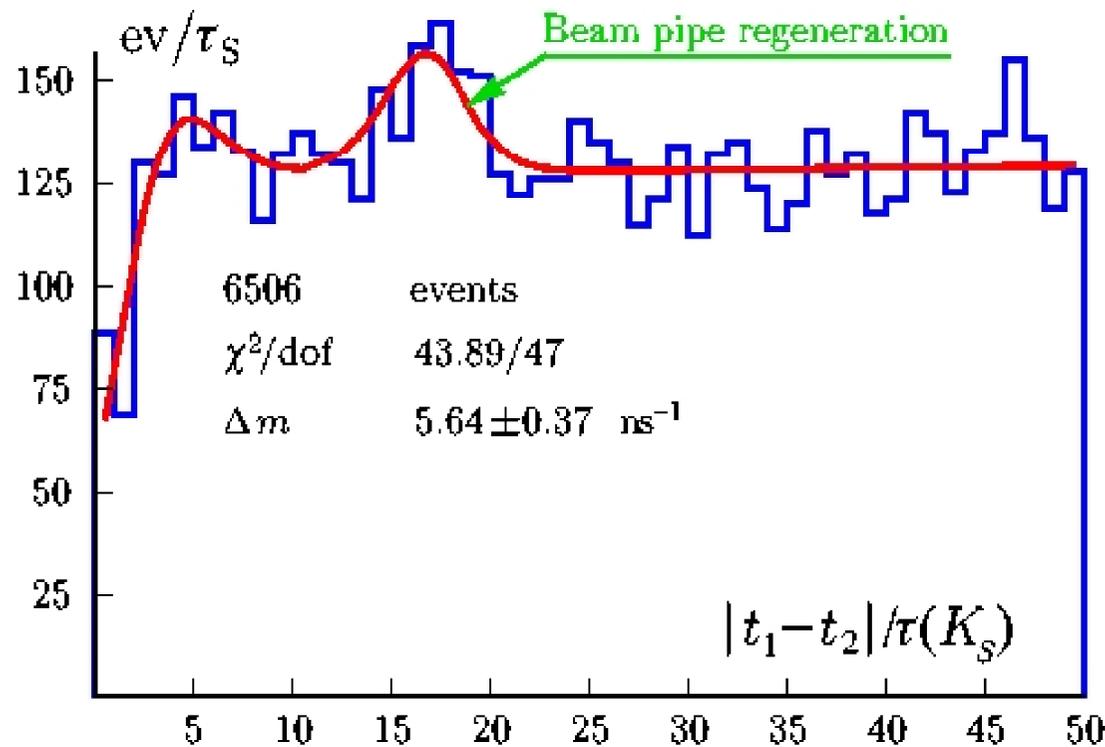
$$P[\Phi \rightarrow K_L K_S \rightarrow a(t_1) b(t_2)] = |A_{Sa}|^2 |A_{Lb}|^2 e^{-\Gamma_S t_1 - \Gamma_L t_2} + |A_{Sb}|^2 |A_{La}|^2 e^{-\Gamma_L t_1 - \Gamma_S t_2} \\ - 2 \operatorname{Re} [A_{Sa} A_{La}^* A_{Lb} A_{Sb}^* e^{+i \Delta m (t_1 - t_2)}] e^{-\Gamma (t_1 + t_2)}$$

Examples of interesting & accessible final states [see 2nd DAΦNE handbook]:

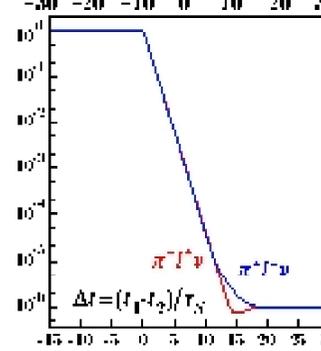
direct access to
(strong & weak) phases

- $(\pi^+ \pi^-) - (\pi^+ \pi^-)$: Δm & $\Gamma_{L,S}$ + η_{\pm} + tests of QM
- $(\pi^+ \pi^-) - (\pi^0 \pi^0)$: $\operatorname{Re}(\epsilon'/\epsilon)$ & $\operatorname{Im}(\epsilon'/\epsilon)$ + $\pi\pi$ phases + tests of CPT & QM
- $(\pi l \nu) - (\pi l \nu)$: tests of CPT
- $(\pi l \nu) - (3\pi)$: $\eta_{3\pi}$ + $\pi\pi$ phases
- $(3\pi) - (3\pi)$: $\eta_{3\pi}$ + $\pi\pi$ phases [different combinations]
- $(2\pi) - (\pi\pi\gamma)$: $\eta_{\pi\pi\gamma}$

➡ Several interesting channels with $L \sim O(100 \text{ fb}^{-1})$



$\phi \rightarrow K_S K_L$
 $\rightarrow \pi e^+ \nu$
 $+ \pi e^- \nu$



$\phi \rightarrow K_S K_L$
 $\rightarrow \pi^+ \pi^-$
 $+ \pi e \nu$

The first example of interference observed in KLOE.

$$e^+ e^- \rightarrow \phi \rightarrow K_S K_L \rightarrow \pi^+ \pi^- + \pi^+ \pi^-$$

$$\Rightarrow \Gamma_S, \Gamma_L, \Delta m, [\Re, \Im(\eta_i, \delta \dots)]$$

$$I(f_1, f_2, \Delta t) = ..2 |\eta_1| |\eta_2| e^{-\Gamma \Delta t / 2} \cos(\Delta m \Delta t + \phi_1 - \phi_2)$$



3. The V_{us} saga

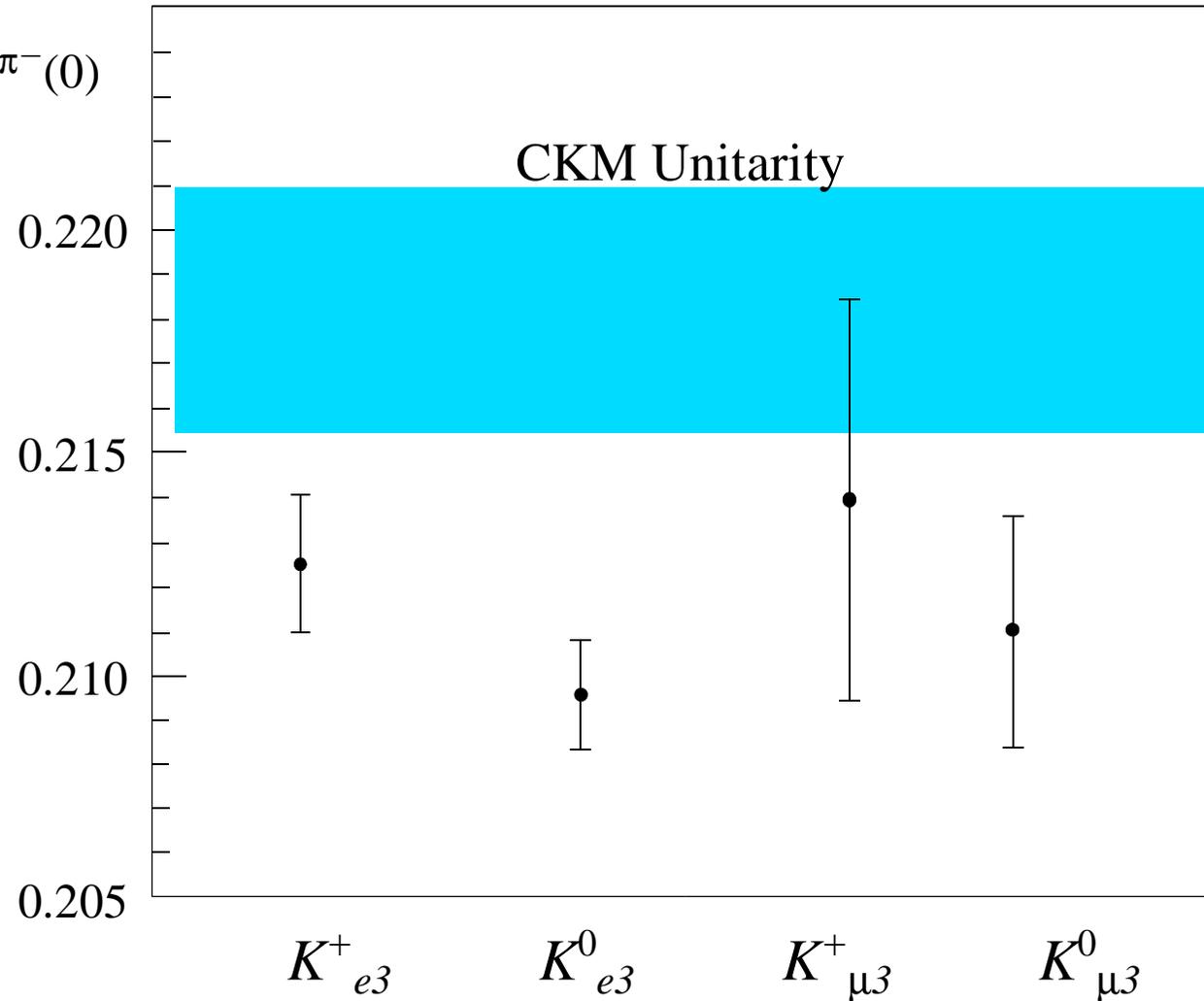
Status in Feb. 2002 [1st CKM Workshop]

- Bad consistency with V_{ud} (unitarity)
- Potentially large SU(2) breaking effects



$$\delta|V_{us}| \approx 2\%$$

dominated by
exp. errors



Status in June 2004:

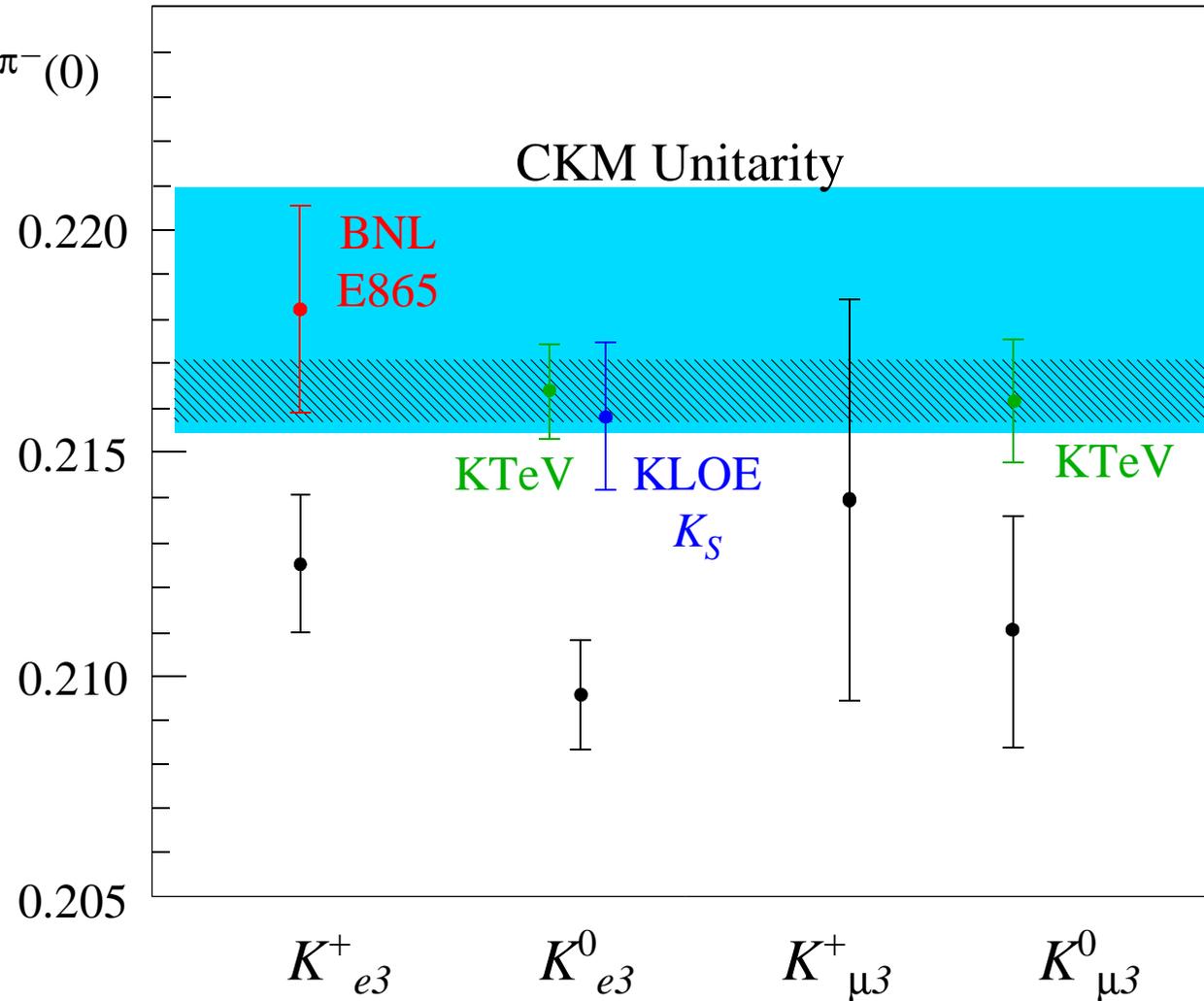
- Consistency with V_{ud} restored



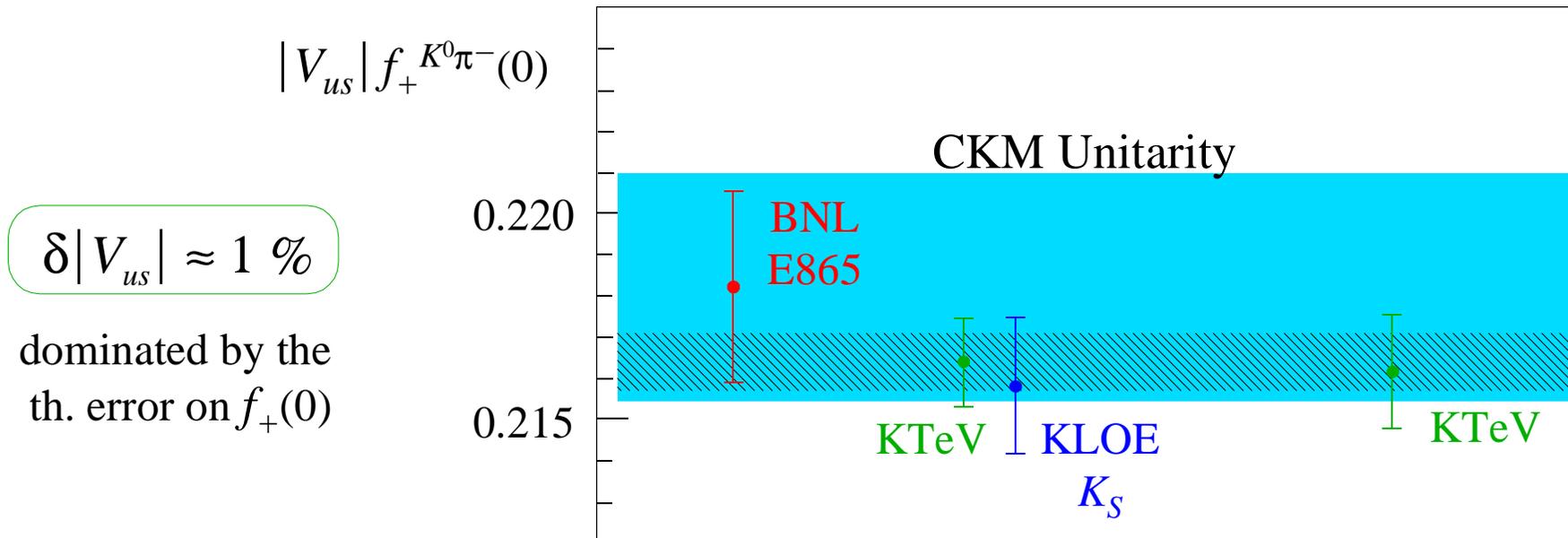
$$\delta |V_{us}| \approx 1\%$$

dominated by the th. error on $f_+(0)$

$$|V_{us}| f_+^{K^0\pi^-}(0)$$



But this is not the end of the story...



→ SU(2) breaking not yet tested at the th. level ($\sim 0.3\%$)

→ Exp. studies of the f.f. beyond the linear approximation are a **key ingredient** to reduce the **th. error on $f_+(0)$** [similar to the hadronic moments in $B \rightarrow X l \nu$]

$$f_0(x, y) = 1 + \lambda_0 x + \delta y^2 + \lambda_2 x^2 + \dots$$

$x = (p_K - p_\pi)^2 / m_\pi^2 \Rightarrow$ V. Lubicz & M. Knecht
 $y = (m_K^2 - m_\pi^2) / m_K^2$

$F_K / F_\pi, \lambda_0, \dots$ CHPT [Bijnens & Talavera, *et al.*]

Natural goal
for a **high-** or
medium/high- L
 Φ factory

The ambitious goal of $\delta|V_{us}| \sim 0.1\%$ is not impossible !

4. Rare (but not impossible...) decays

An interesting example:

The $K_L \rightarrow \pi^0 l^+ l^- \oplus K_S \rightarrow \pi^0 l^+ l^- \oplus K_L \rightarrow \pi^0 \gamma \gamma$ system

\Rightarrow L. Sehgal & C. Smith

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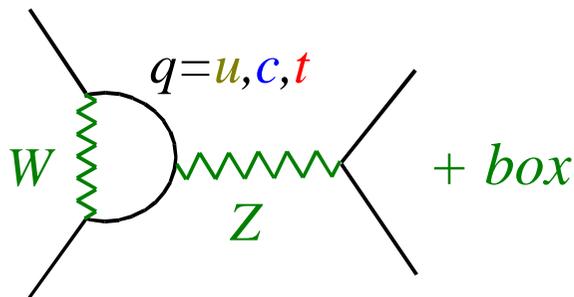
$$B_L(ee)_{SM} = 3.7 \pm 1.0 \times 10^{-11}$$

$$B_L(\mu\mu)_{SM} = 1.5 \pm 0.3 \times 10^{-11}$$

Very interesting goal for future fixed target experiments [NA48/4 ?]

with sizable (35%–45%) contr. from the th. clean & interesting

direct-CPV amplitude



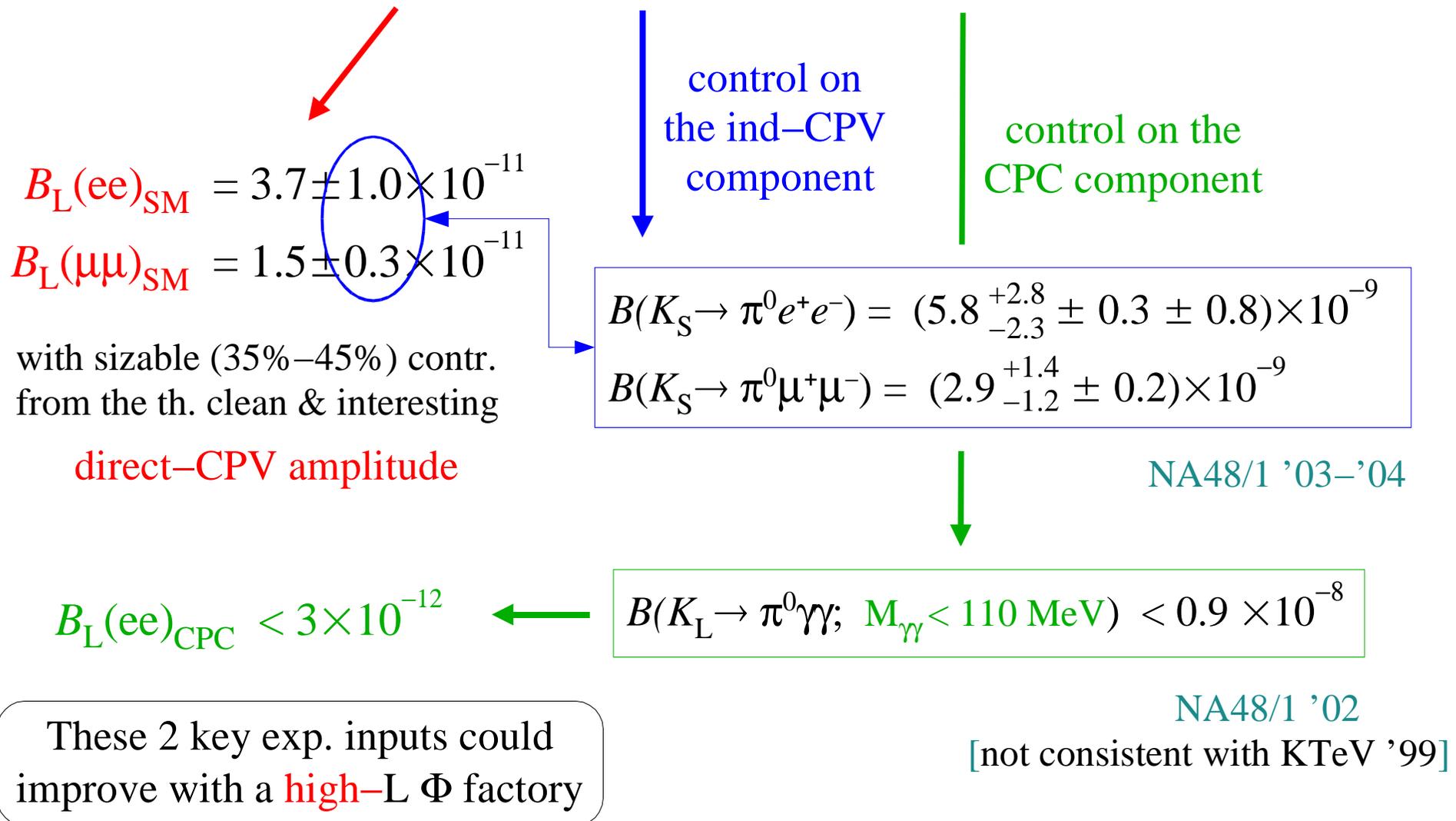
similar to $K_L \rightarrow \pi^0 \nu \nu$, with different NP sensitivity

G.D'Ambrosio, G. Buchalla & G.I. '03
G.I., C. Smith & R. Unterdorfer, '04

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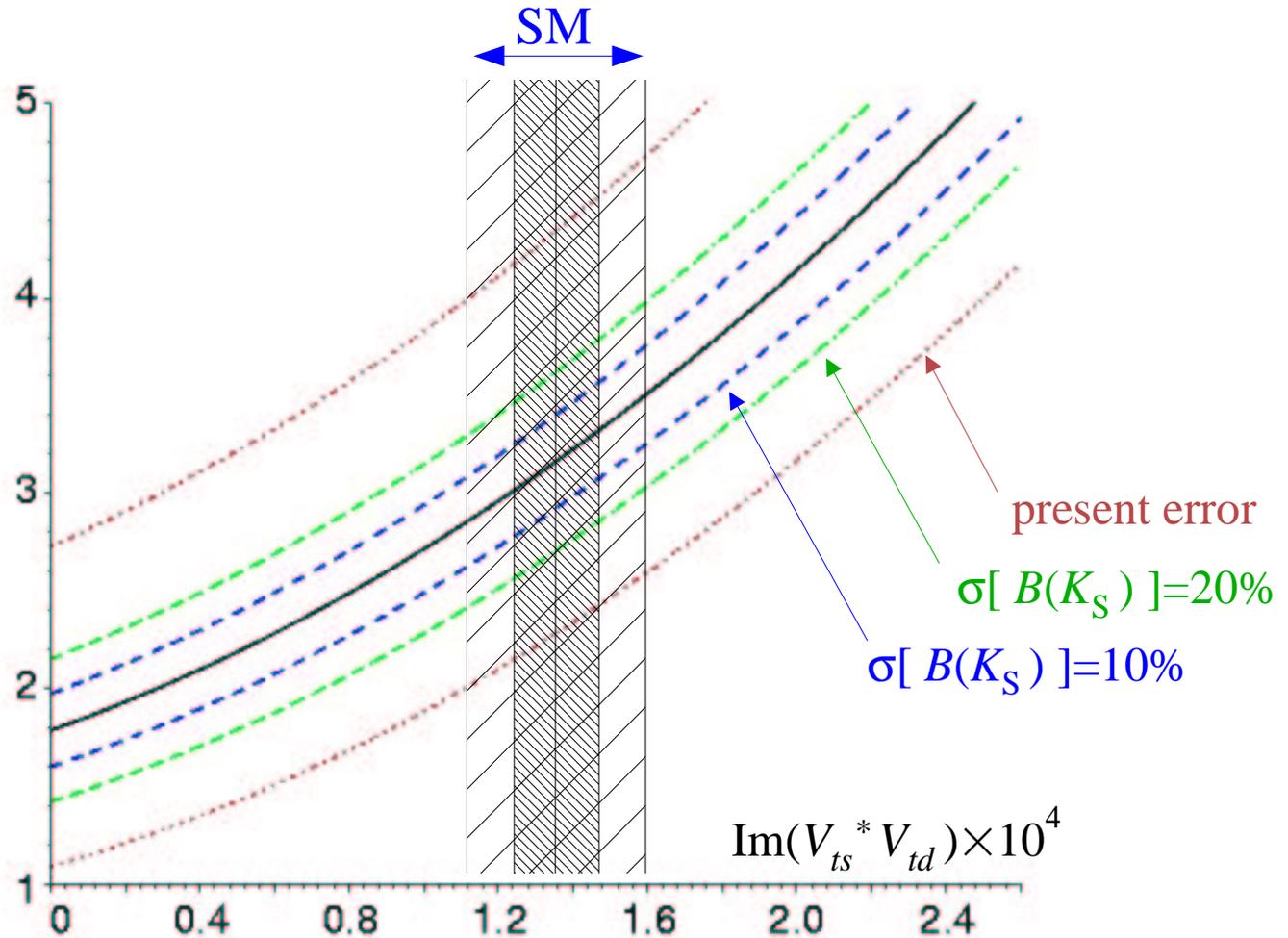
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$$B(K_L \rightarrow \pi^0 e^+ e^-) \times 10^{11}$$

$K_L \rightarrow \pi^0 l^+ l^-$
 represent a very
 interesting opportunity
 for precision tests of
 $\Delta F=1$ $s \rightarrow d$ FCNCs:



Irreducible error $\sim 10\%$

[not as clean as $K_L \rightarrow \pi^0 \nu \nu$, but still extremely interesting + different NP sensitivity]

provided we can measure at a comparable level of accuracy

the corresponding K_S transitions \Rightarrow possible at a super Φ factory with $O(100 \text{ fb}^{-1})$

5.1 Charge asymmetries

$$\Delta_f = \frac{d\Gamma(K^+ \rightarrow f^+) - d\Gamma(K^- \rightarrow f^-)}{d\Gamma(K^+ \rightarrow f^+) + \delta\Gamma(K^- \rightarrow f^-)} \neq 0 \quad \Leftrightarrow \quad \text{direct } \mathcal{CP}$$

Strong competition from NA48/2 and small chances to observe non-zero signals within the SM, but still worth to try...

A particularly interesting case: $K^\pm \rightarrow \pi^\pm \pi^0 \gamma$

[Th. cleaner + more sensitive to New Physics effects than $K \rightarrow 3\pi$]

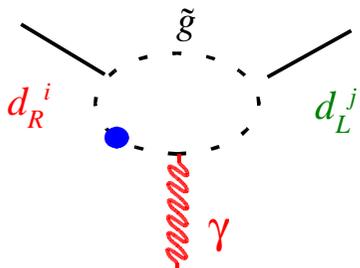
Dalitz-Plot variables:

T_c = charged kaon
kin. energy

$$W^2 = \frac{q p_+ \cdot q p_K}{M_\pi^2 M_K^2}$$

$$\frac{\partial^2 \Gamma}{\partial T_c \partial W^2} = \frac{\partial^2 \Gamma_{IB}}{\partial T_c \partial W^2} \left[1 + \Re \left(\frac{E_{DE}}{A_{2\pi}} \right) W^2 + O(W^4) \right]$$

$$\mathcal{CP} \Rightarrow \frac{\partial^2 \Gamma / \partial T_c \partial W^2 - \partial^2 \bar{\Gamma} / \partial T_c \partial W^2}{\partial^2 \Gamma / \partial T_c \partial W^2 + \partial^2 \bar{\Gamma} / \partial T_c \partial W^2} = \Omega W^2 + \dots$$



$$\Omega_{\text{SM}} \sim 10^{-5}$$

$$\Omega_{\text{SUSY}} \sim 10^{-4} \text{ [chromag. op. saturates } \epsilon'/\epsilon \Leftrightarrow \text{realistic models]}$$

$$\Omega_{\text{SUSY}} \sim 10^{-3} \text{ [large cancellations in } \epsilon'/\epsilon \Leftrightarrow \text{possible, not natural]}$$

5.2 $\pi\pi$ phases *et al.*

There are many interesting aspects of QCD at low energies which can still be studied in the kaon sector [most notable example: the precise determination of $\pi\pi$ phases from K_{14}^{\pm}]

Many of them are described in the 2nd DAΦNE Handbook, others strategies have recently been inspired by the new precise NA48/2 data [e.g. the extraction of $\pi\pi$ phases from $K_{3\pi}$ \Rightarrow Cabibbo's talks], probably even more are still to come...



Not easy to anticipate the potential impact of a future DAΦNE upgrade in this context

but there are good chances for substantial contributions

• My conclusions

The physics case of a high-intensity Φ factory with $10^{33} < L [\text{cm}^{-2}\text{s}^{-1}] < 10^{34}$ is certainly interesting and worth to be explored

Not a unique outstanding goal, but a series of interesting meas. in the K sector:

- clear targets [V_{us} & K_{13} f.f., rare (K_S) decays, CPT tests]
 - less clear targets [K^\pm -asym., interferometry, K_{14} , ...]
⇒ more work on real data needed to better quantify the potential impact
- + the usual non-K program at the Φ [worth to think about $\gamma\gamma \rightarrow \pi\pi$]

This of course does not mean that the high-energy option is not interesting

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However... ★ The most clear goals in the high-L option will be less interesting if the time scale is too long [strong competition within the field of flavour physics]

★ The high-L option is extremely challenging from the exp. point of view [huge statistics & high precision] ⇒ a too long interruption of the kaon program could be dangerous

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In addition to the natural machine and experimental considerations
the time schedule of this program represents a **key point**

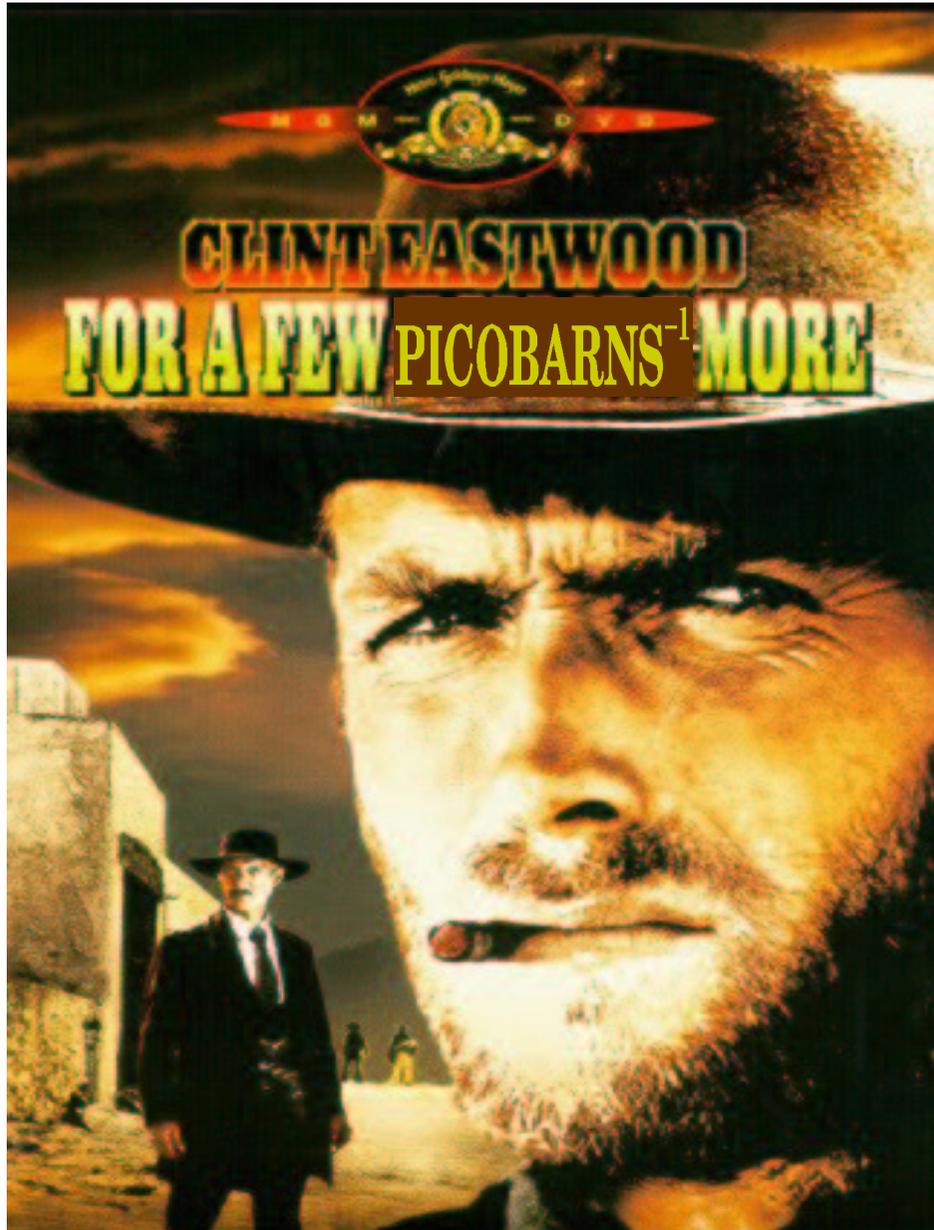
Rare Kaon decays

– The Good, The Bad, The Ugly –
George Redlinger



The physics case for DAΦNE upgrade

– For a few picobarns⁻¹ more –



Rare Kaon decays

– The Good, The Bad, The Ugly –

