

DAPHNE 2004

Precision spectroscopy of pionic atoms:  
from pion mass evaluation  
to tests of chiral perturbation theory

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In collaboration with

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IMEP, Österreichisch Akademie der Wissenschaften, Wien, Austria

# Why pionic atoms

## Pionic atoms:

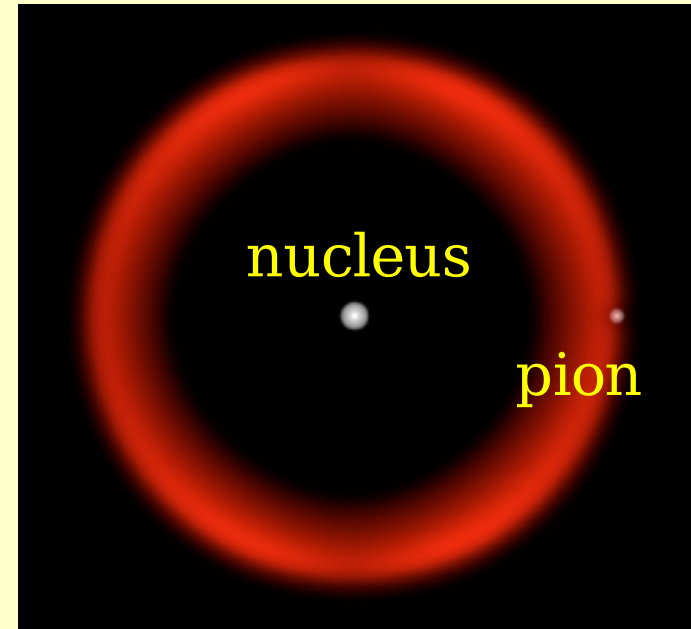
- Nucleus + pion = bound system

## Characteristics:

- Pion lifetime = 20 ns
- Pion mass = 273 electron mass

## Interests:

- Measurement of pion mass
- Measurement of the pion-nucleus strong interaction effect (->ChPT)



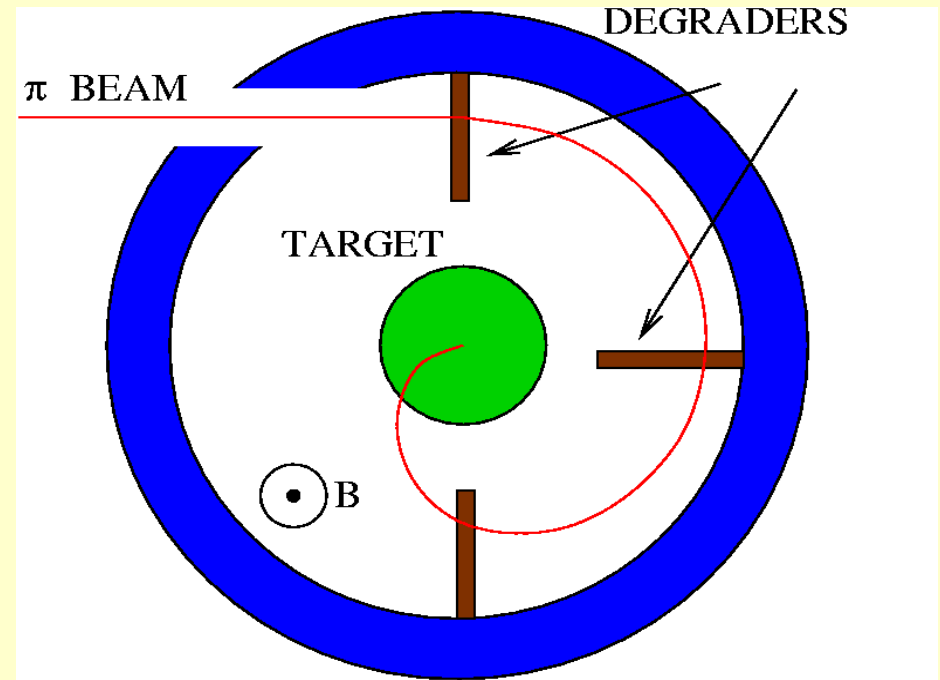
$$E_n = \frac{1}{2n^2} (Z\alpha)^2 m c^2$$

$$r_0 = \frac{\hbar}{Z\alpha m c}$$

$Z$  = nucleus charge,  $m$  = reduced mass

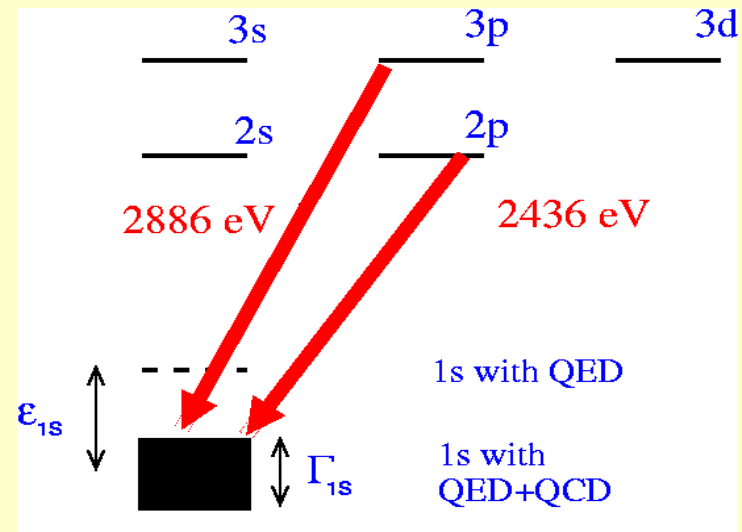
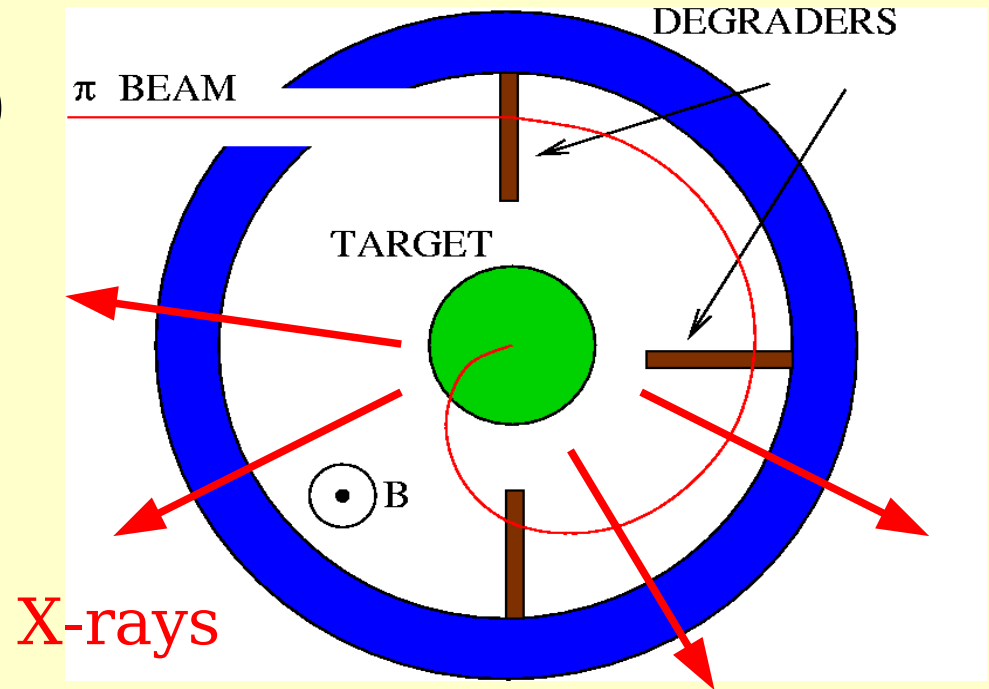
# Pionic atoms production (1)

- **Pions** from PSI facilities  
( $10^8$  pions/sec,  $E_{\text{kin}} = 110$  Mev/c)
- Cyclotronic trap:  
max. magnetic field  $B = 3.5$  Tesla
- Target cell:  
gas temp =  $14^\circ\text{K}$  to amb. temp.  
Eff. Pressure =  $\sim 0$  to 40 bars



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-> pionic atom formation in excited state

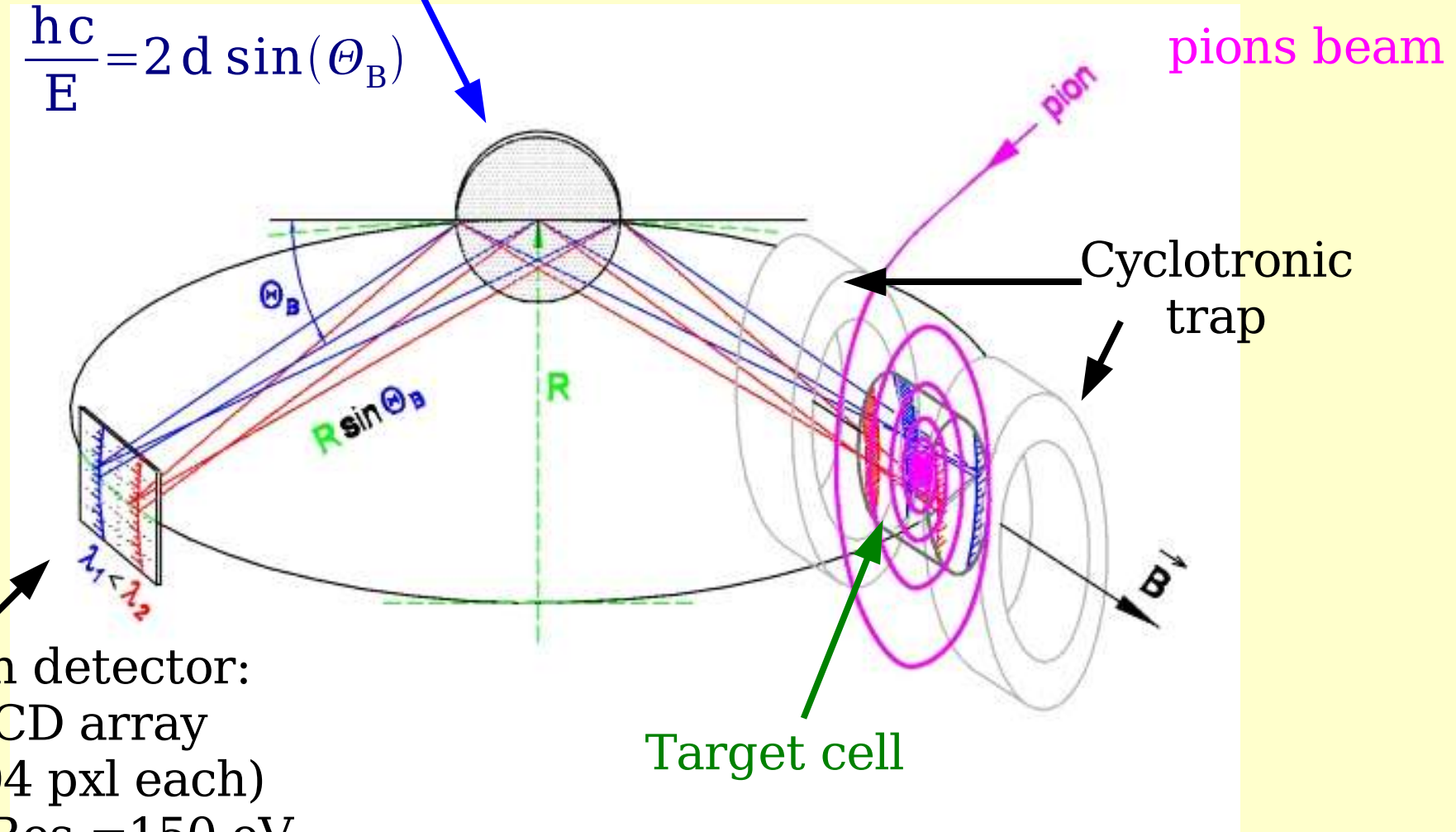
-> radiative cascade with X-ray emission

Energy transition in pionic hydrogen

# Pionic atoms production (2)

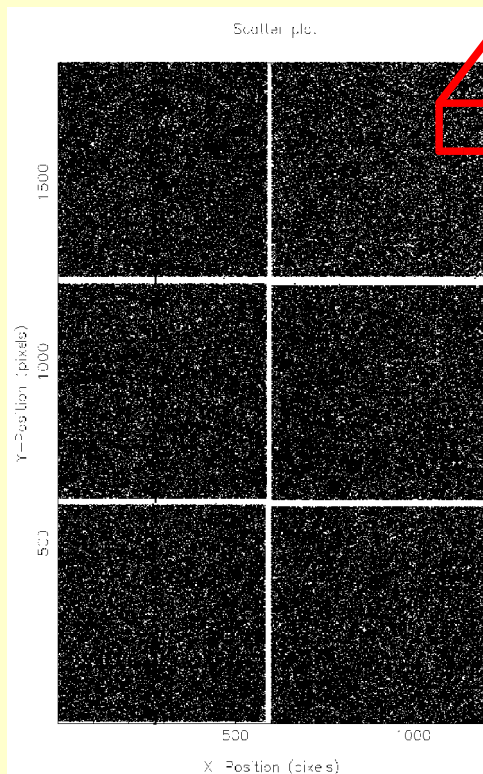
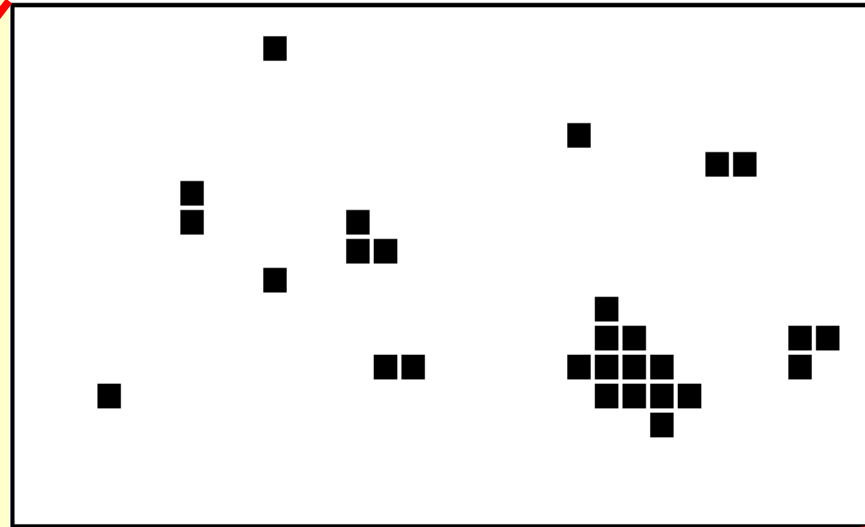
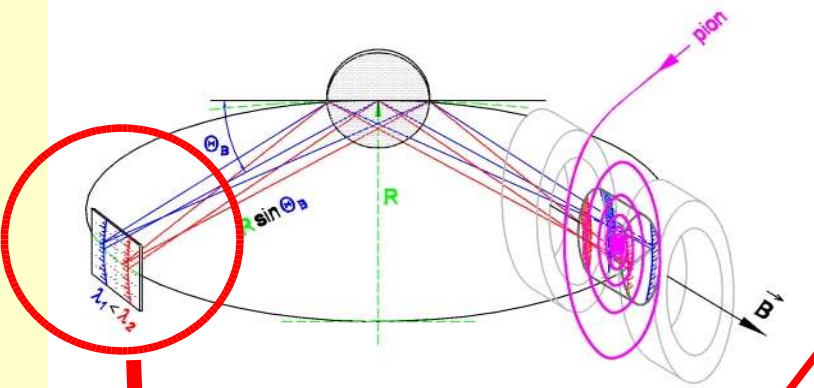
Spherically bent crystal for the Bragg reflection

$$\frac{hc}{E} = 2d \sin(\theta_B)$$

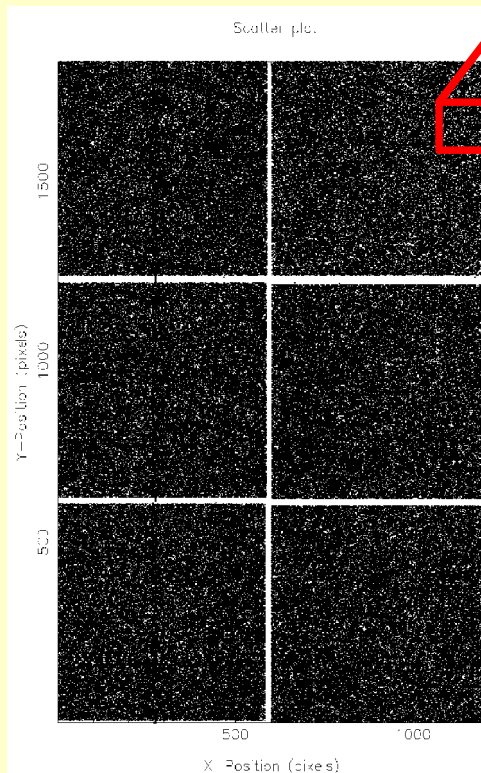
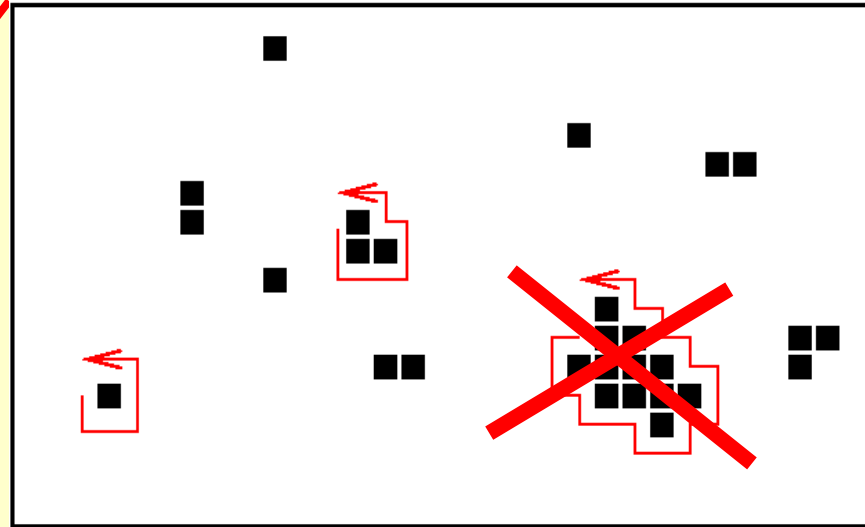
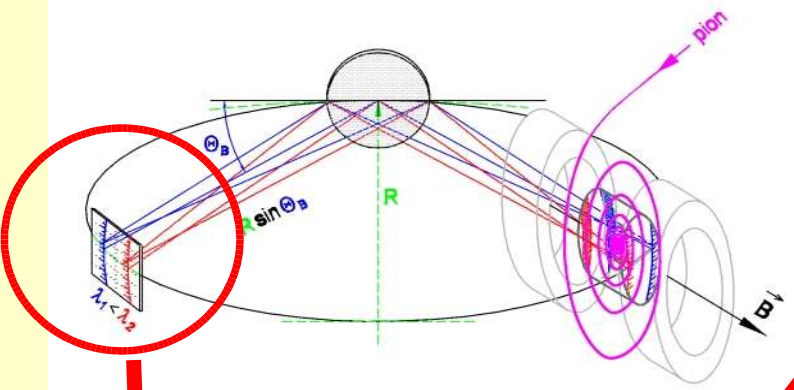


Position detector:  
6 x CCD array  
(610x604 pxl each)  
Energy Res.=150 eV  
@3 keV

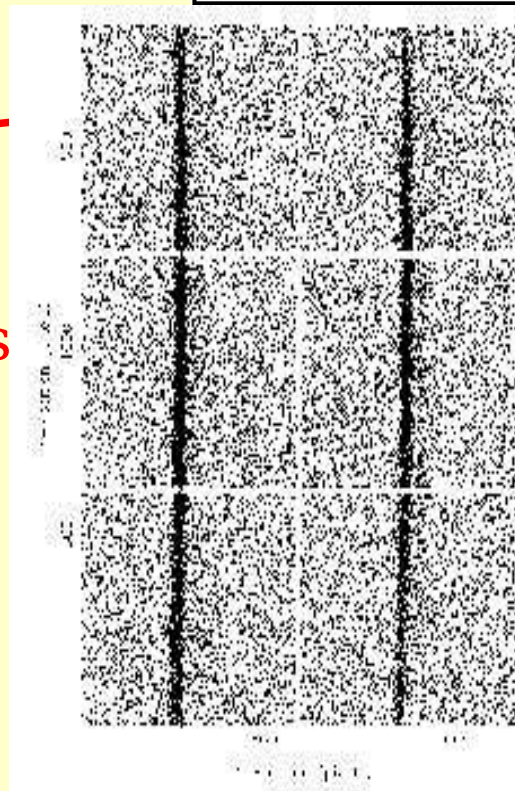
# Detection (1)



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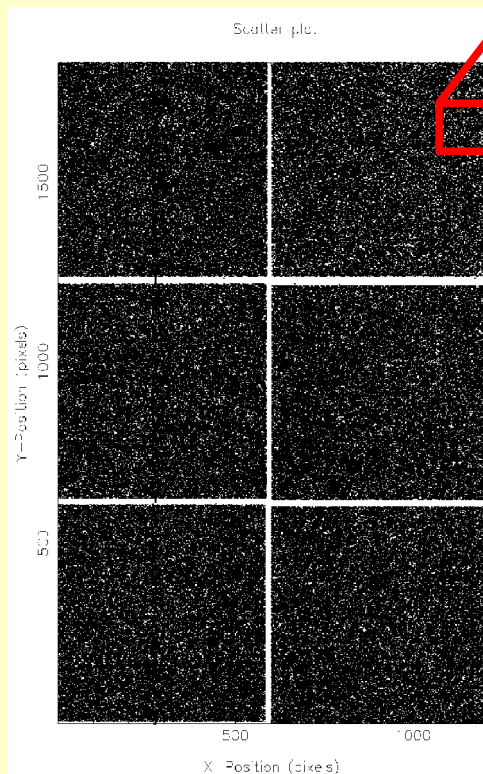
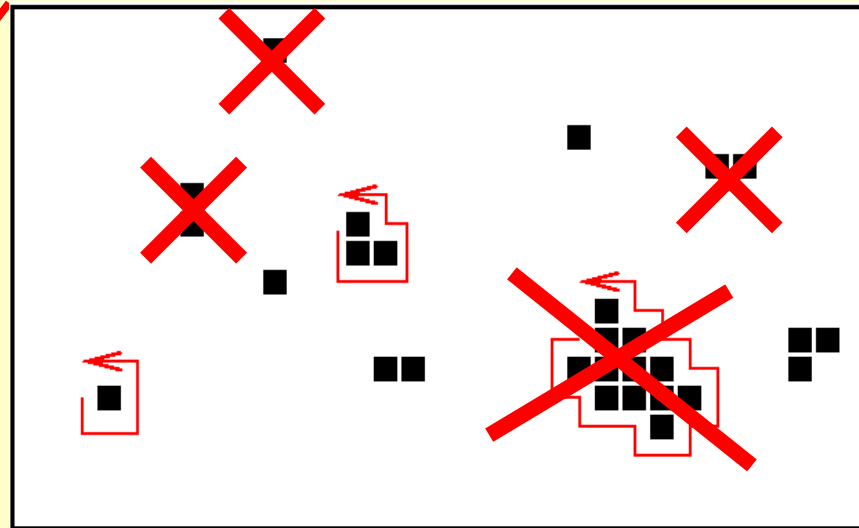
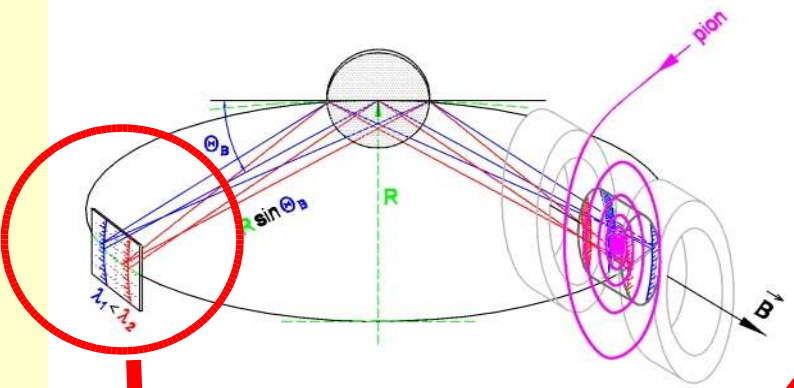


cluster  
analysis  
on

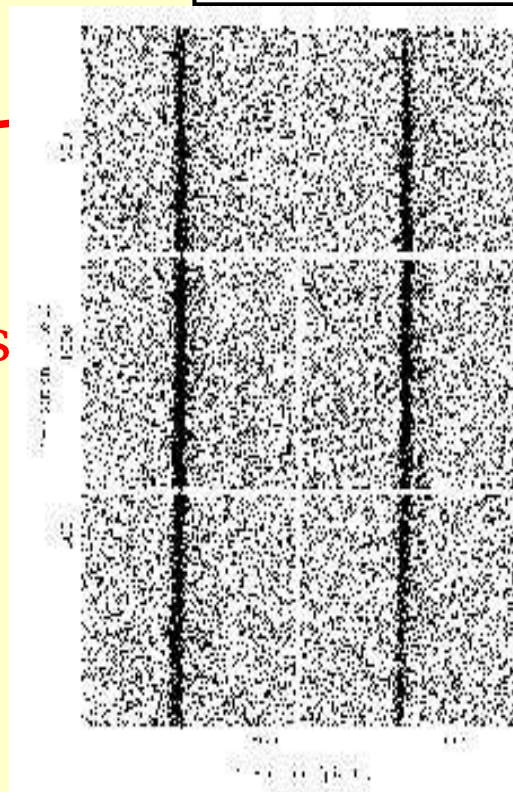




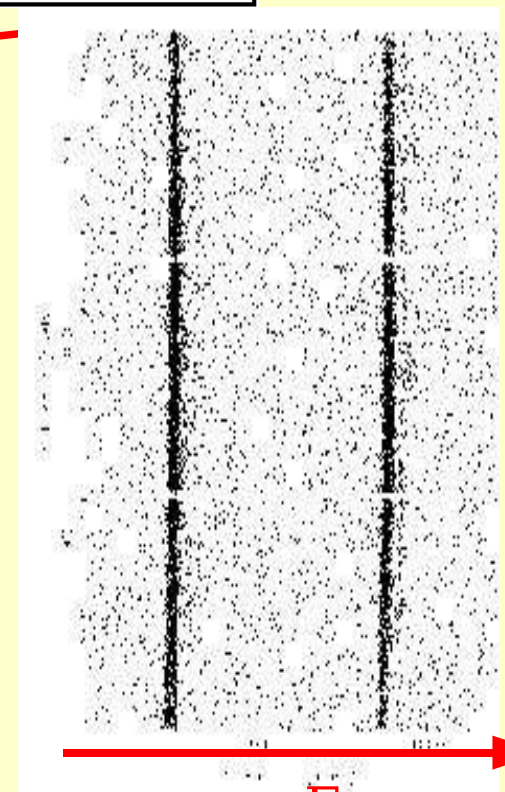
# Detection (1)



cluster analysis on



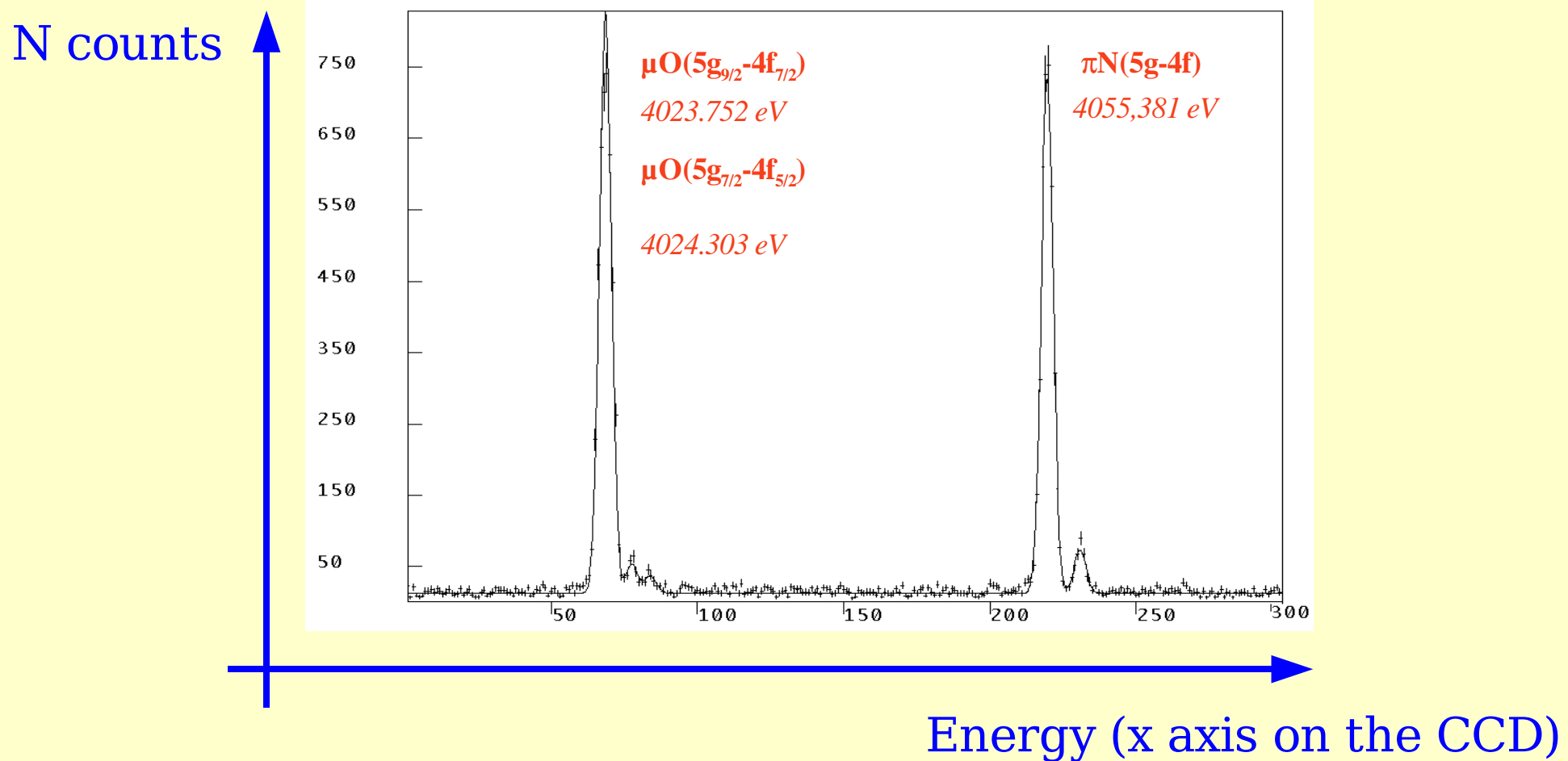
cluster analysis and energy cuts on



Energy

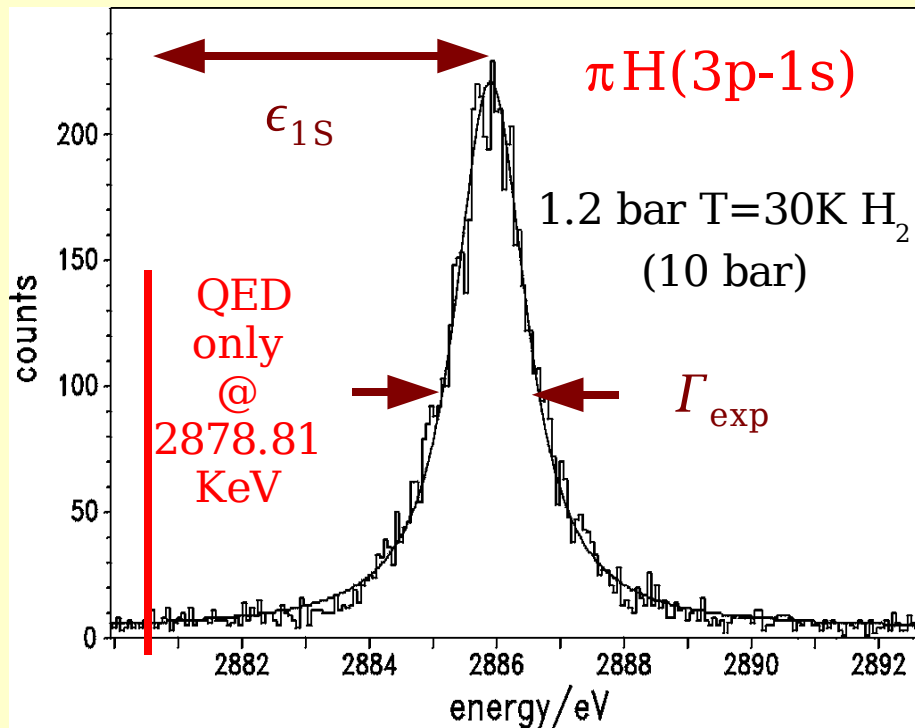


# Detection (2)



- Spectrometer resolution = 0.4 eV
- Peak determination accuracy < 0.05 eV  
(depending on intensity and spectrometer configuration)

# Pionic hydrogen measurements



## Deser's formulas

Line width  $\leftrightarrow$  hadronic cross sections  $\mathbf{a}$

$$\frac{\Gamma_{1S}}{E_{1S}} = 8 \frac{Q_0}{r_B} \left( 1 + \frac{1}{P} \right) \left( \mathbf{a}_{\pi^- p \rightarrow \pi^0 n} (1 - \delta_\Gamma) \right)^2$$

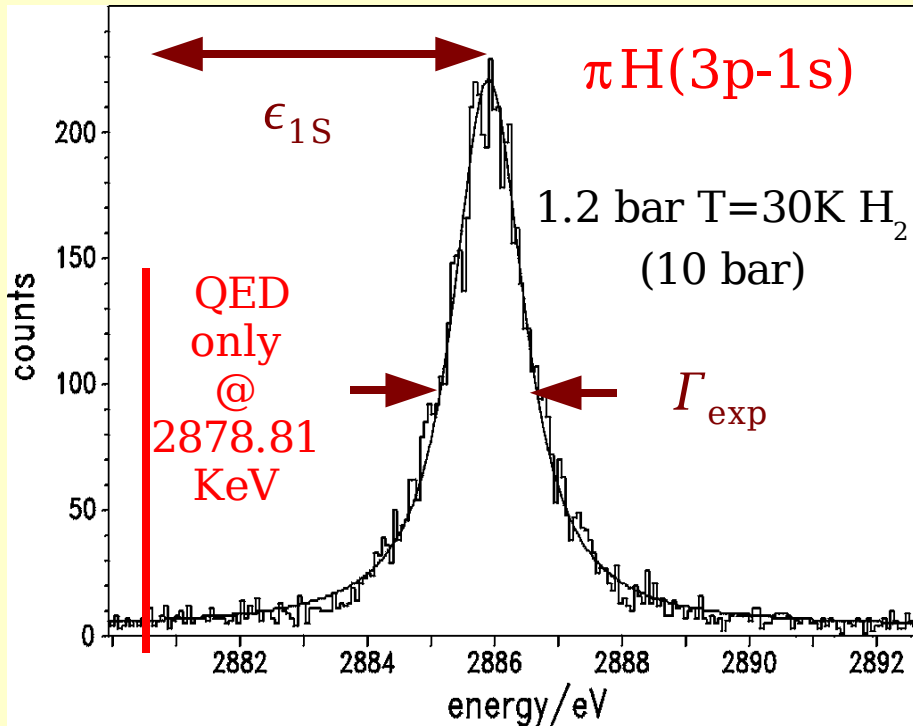
Line shift  $\leftrightarrow$  hadronic cross sections  $\mathbf{a}$

$$\frac{\epsilon_{1S}}{E_{1S}} = \frac{-4}{r_B} \mathbf{a}_{\pi^- p \rightarrow \pi^- p} (1 - \delta_\epsilon)$$

$$\Gamma_{\text{exp}} = \Gamma_{\text{SPECTROMETER}} \otimes \Gamma_{\text{DOPPLER}} \otimes \Gamma_{1S}$$

$\delta_\epsilon, \delta_\Gamma$  = em. corrections [1,2] P = Panofsky ratio,  
 $r_B$  Bohr radius,  $Q_0$  = kinematic factor

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$\delta_\epsilon, \delta_\Gamma = \text{em. corrections [1,2]}$   $P = \text{Panofsky ratio,}$   
 $r_B = \text{Bohr radius, } Q_0 = \text{kinematic factor}$

## Results:

$$\epsilon_{1S} = +7.120 \pm 0.017 \text{ eV, } \Gamma_{1S} = 800 \pm 30 \text{ meV (3-4\%)[3]}$$

[1] T.E.O.Ericson, B.Loiseau and S.Wycech, arXiv:hep-ph/0310134.

[2] J. Gasser et al., Eur. Phys. J. C 26, 13 (2003)

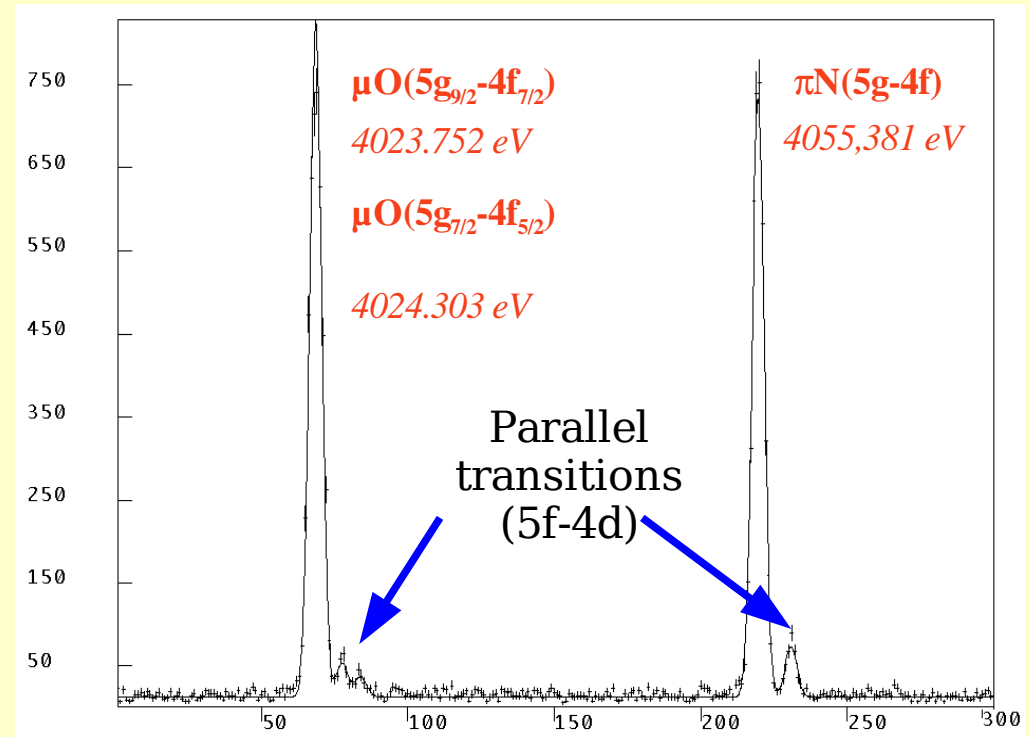
[3] D.Gotta and al. Nucl.Phys.A721, 849 (2003)

# Pion mass measurement

Relative measurement  
between pionic Nitrogen and  
muonic Oxygen transitions

Muon mass error=0.05 ppm

-> pion mass measurement  
with error < 2 ppm



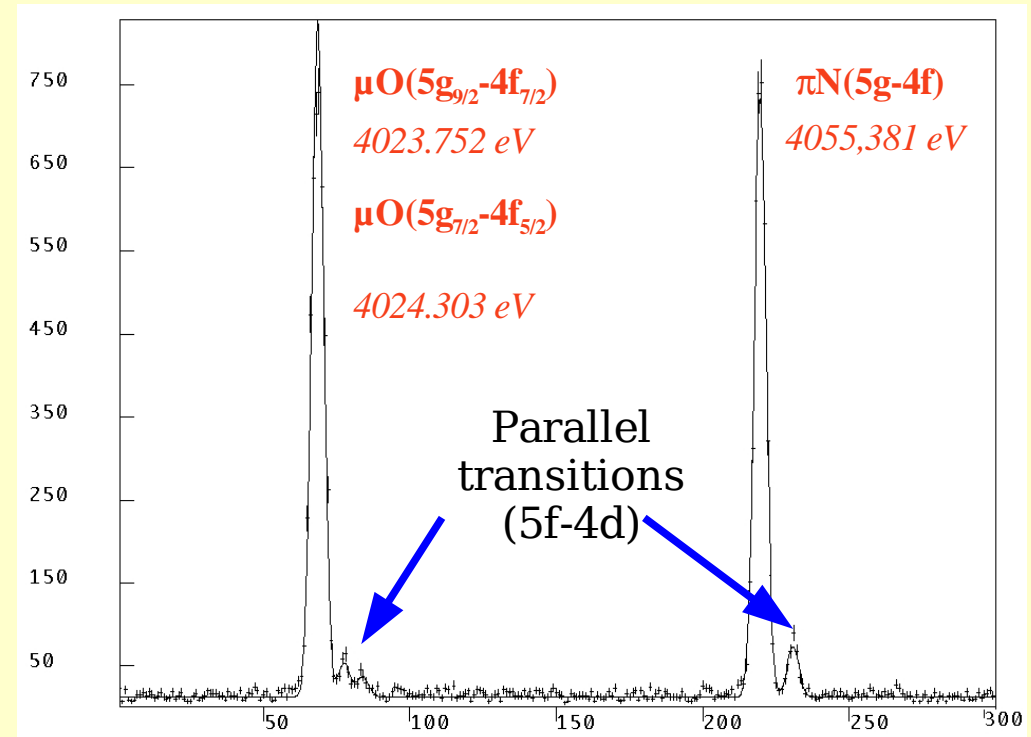
$$\frac{m_{\pi}}{m_{\mu}} = F(\alpha, m_{\text{O}}, m_{\text{N}}) + O\left(\frac{m_{\pi}}{m_{\text{O}}}\right)^3 + O\left(\frac{m_{\mu}}{m_{\text{N}}}\right)^3$$

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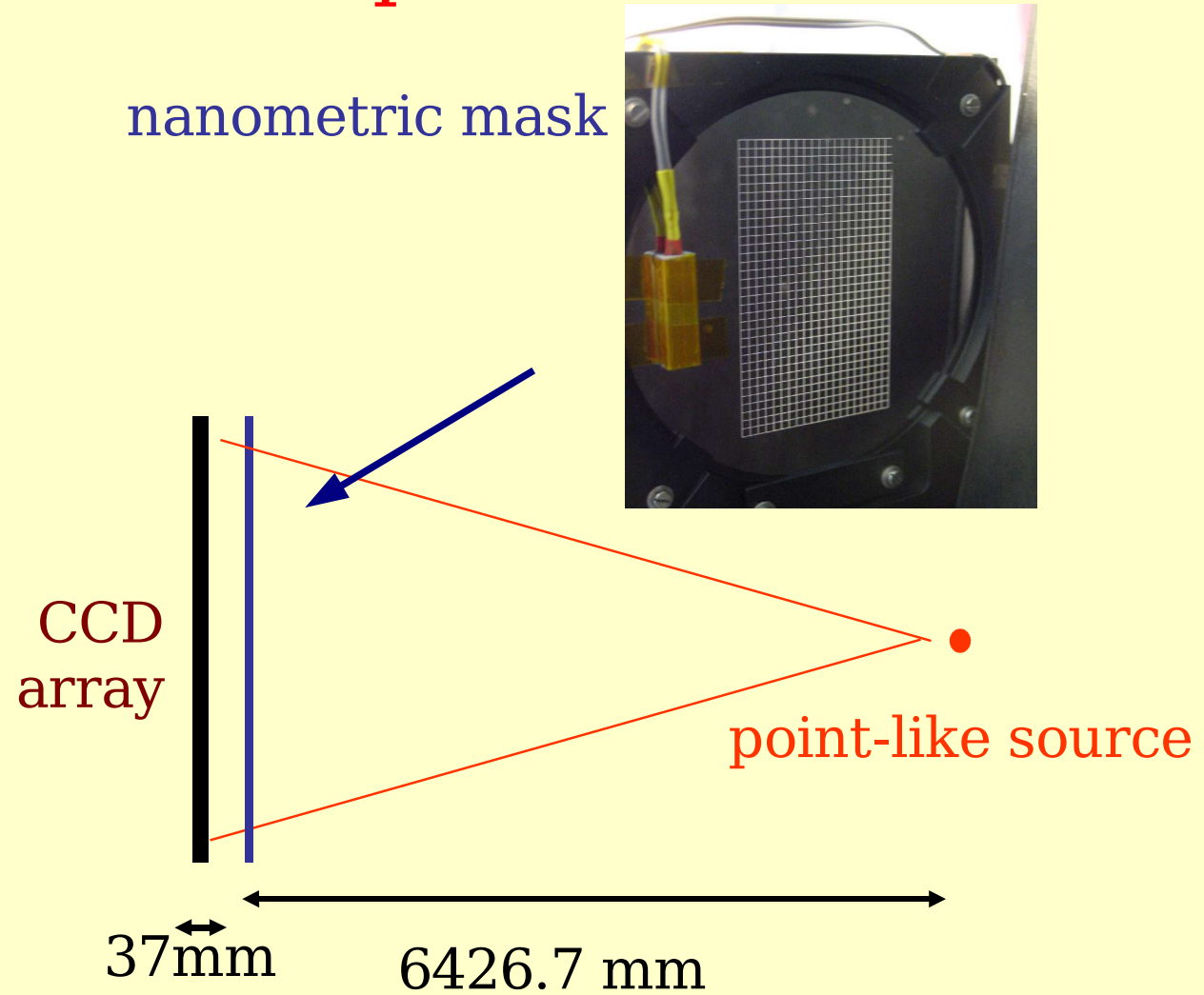


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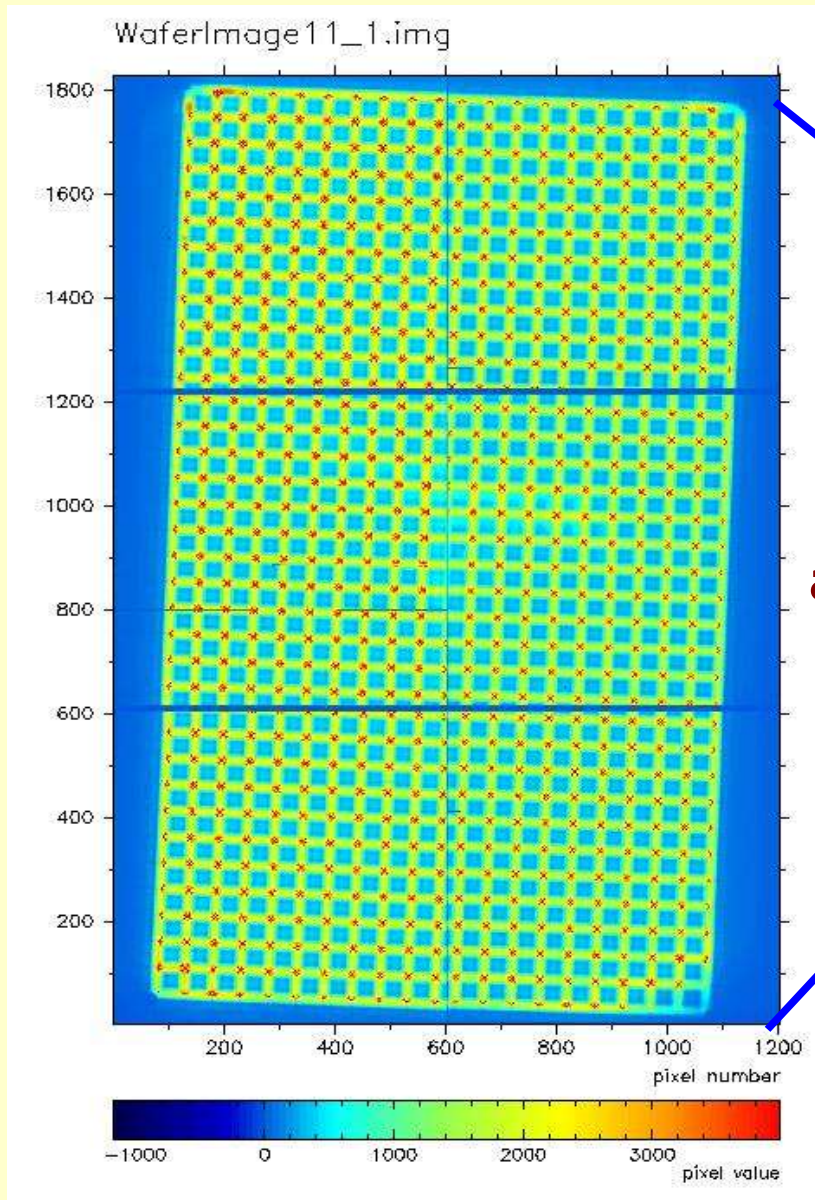
• **Result?** to get the final mass, we need the exact **pixel size** and crystal curvature radius



# Pixel measurement setup



# Pixel measurement setup



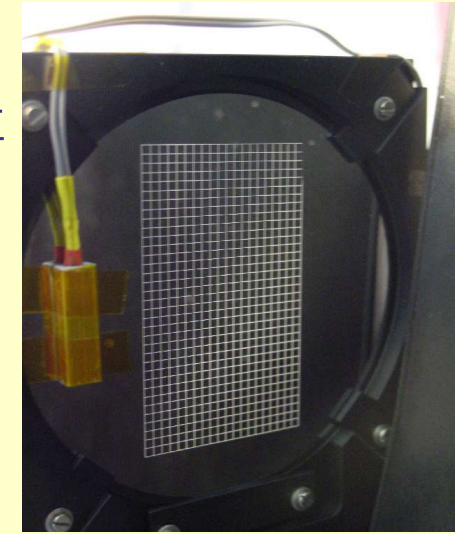
nanometric mask

CCD array

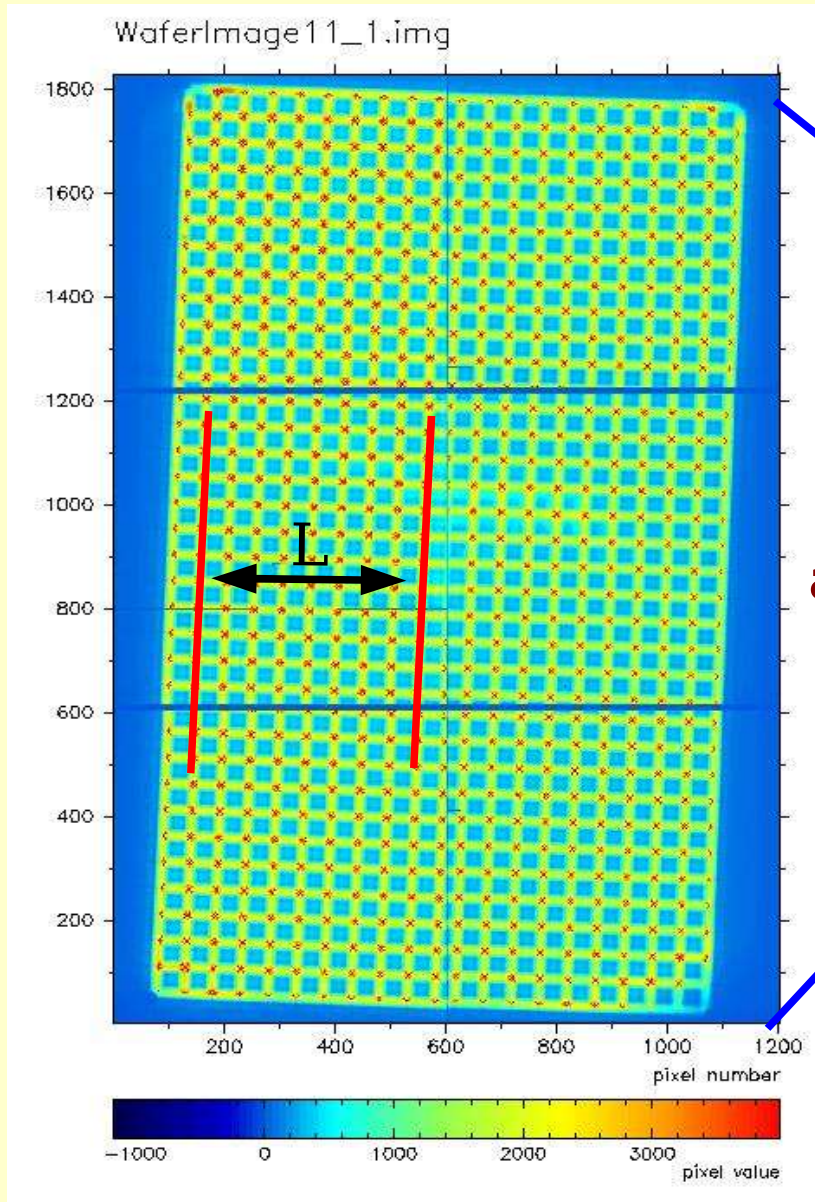
point-like source

37mm

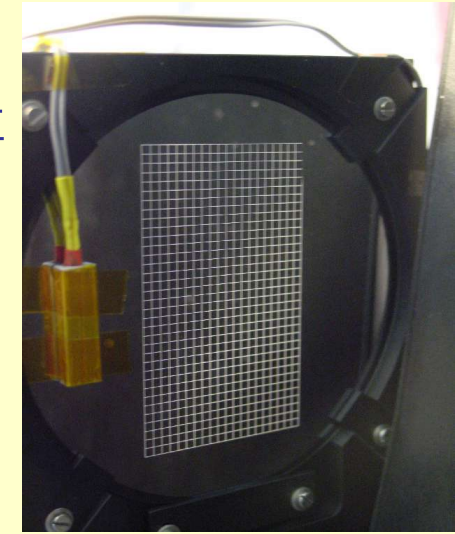
6426.7 mm



# Pixel measurement setup



nanometric mask



CCD array

point-like source

37mm

6426.7 mm

lines fitting (L) -> Pixel size measurement

$39.9943 \pm 0.0035 \mu\text{m}$

# Conclusions and outlooks

## Results:

- $\epsilon_{1S}$  on  $\pi H$ : meas. done:  $\Delta\epsilon_{1S}/\epsilon_{1S}=0.2\%$  (prev. exp.= 0.5%[1])
- $\Gamma_{1S}$  on  $\pi H$ : meas. done:  $\Delta\Gamma_{1S}/\Gamma_{1S}=4\%$  (prev. exp.= 7%[1])
- Ending of pion mass measurement: **expected precision < 2 ppm**  
(end 2004-beginning 2005, PDG2002= 2.5 ppm[2])

## Next steps:

- $\mu H$  measurement for radiative cascade study ( $\Delta\Gamma_{1S}/\Gamma_{1S} \rightarrow 1\%$ )
- $\pi H$  high-statistic run
- $\epsilon_{1S}$  and  $\Gamma_{1S}$  on  $\pi D$ ,  $\pi T$  and  $\pi^3 He$

- [1] H.C.Schroder et al., Phys. Lett.B 469, 25 (1999)  
[2] Particle Data Group, Phys. Rev. D 66, 010001 (2002)

