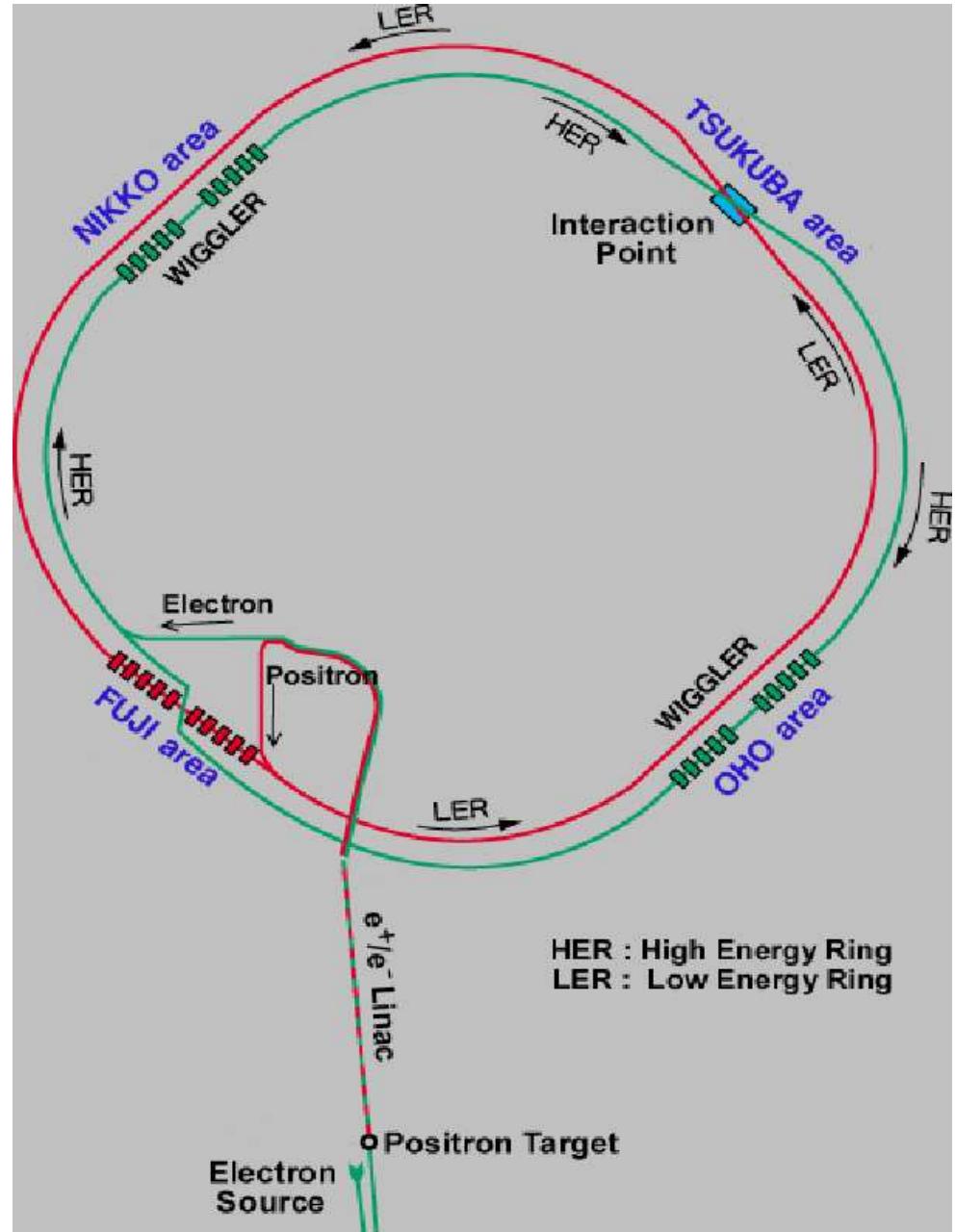


# Measurement of $\phi_3$ using $B^\pm \rightarrow DK^\pm$ with $D \rightarrow K_S\pi^+\pi^-$

Tim Gershon

IPNS, KEK

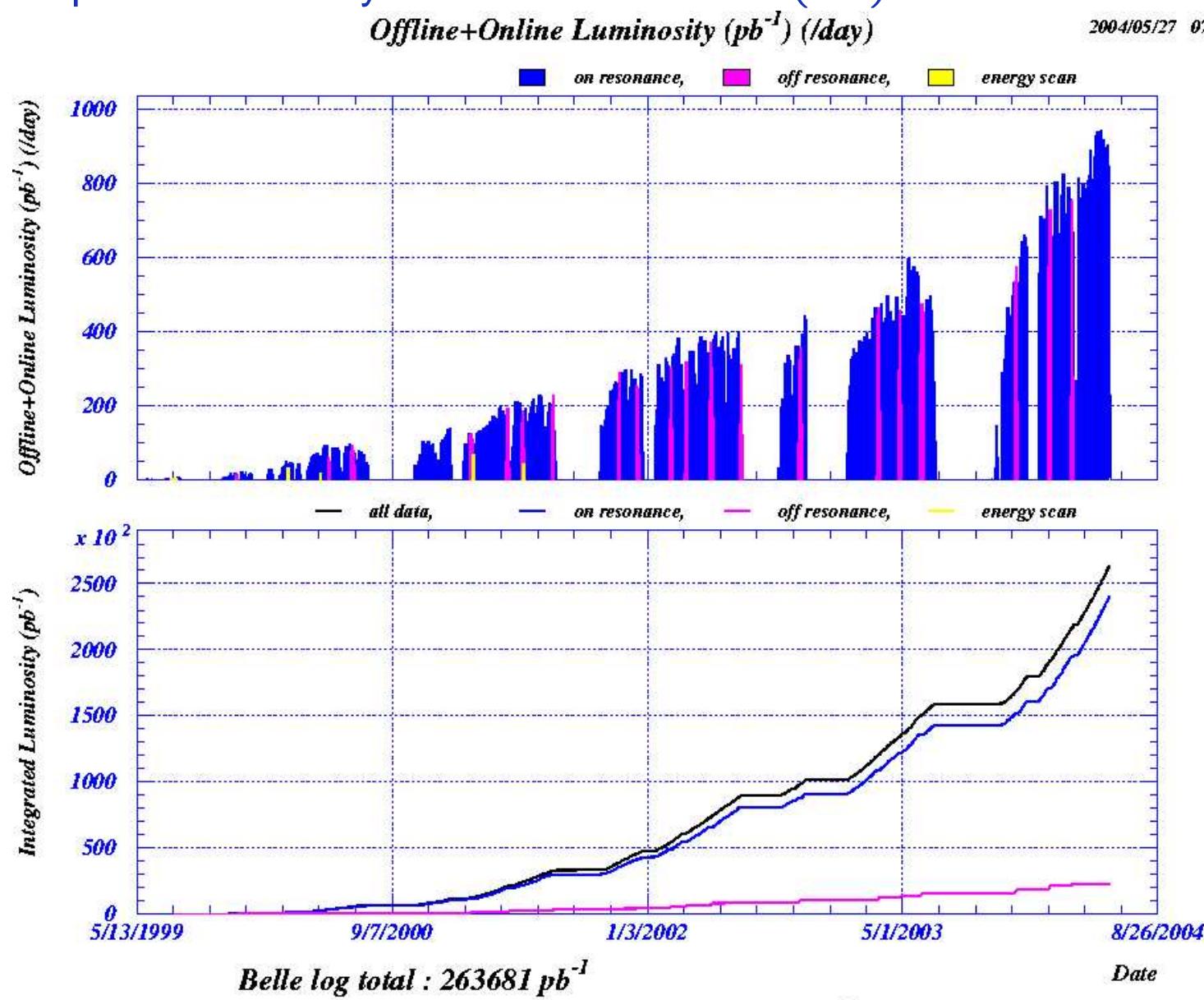
June 7, 2004



# Integrated Luminosity

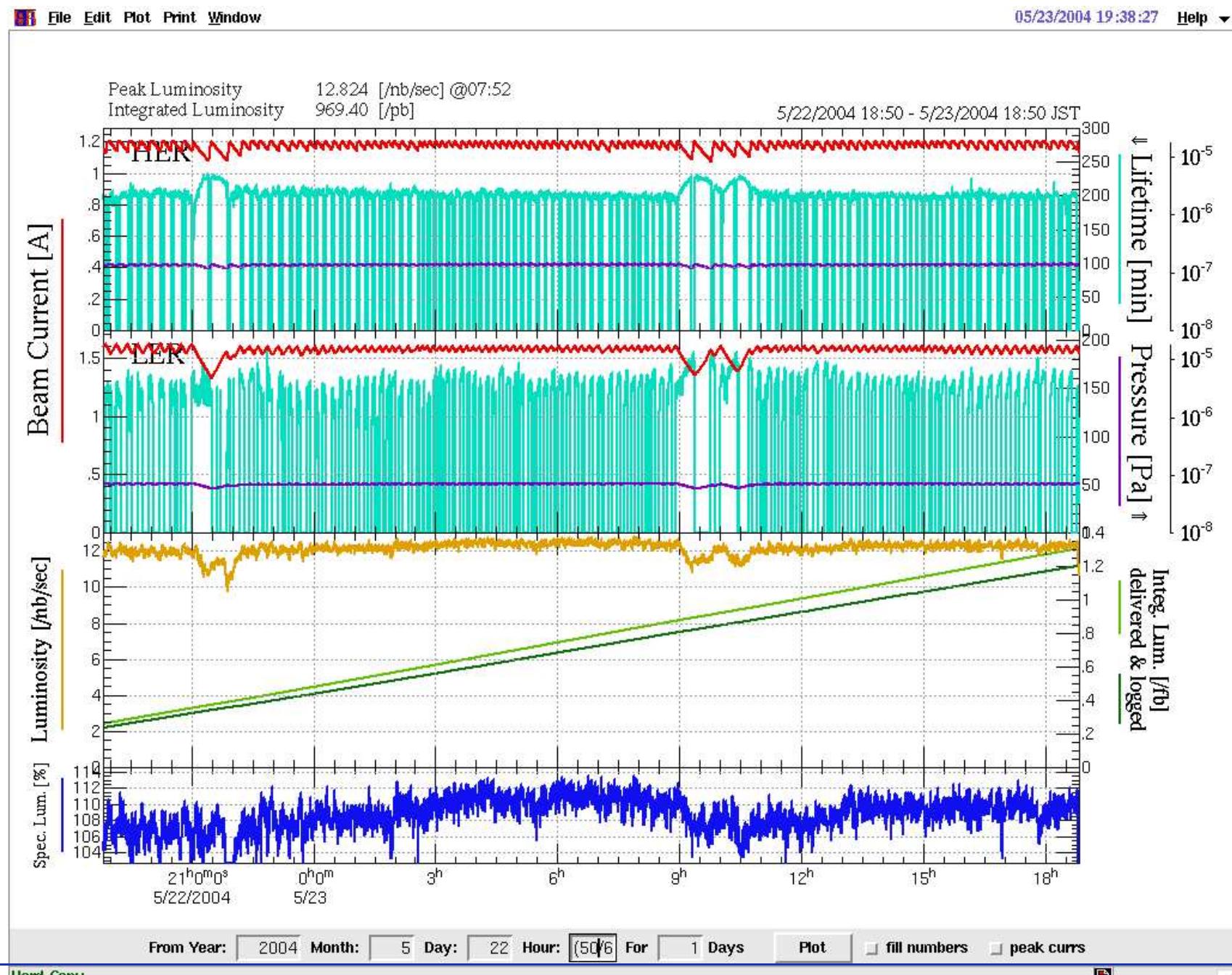


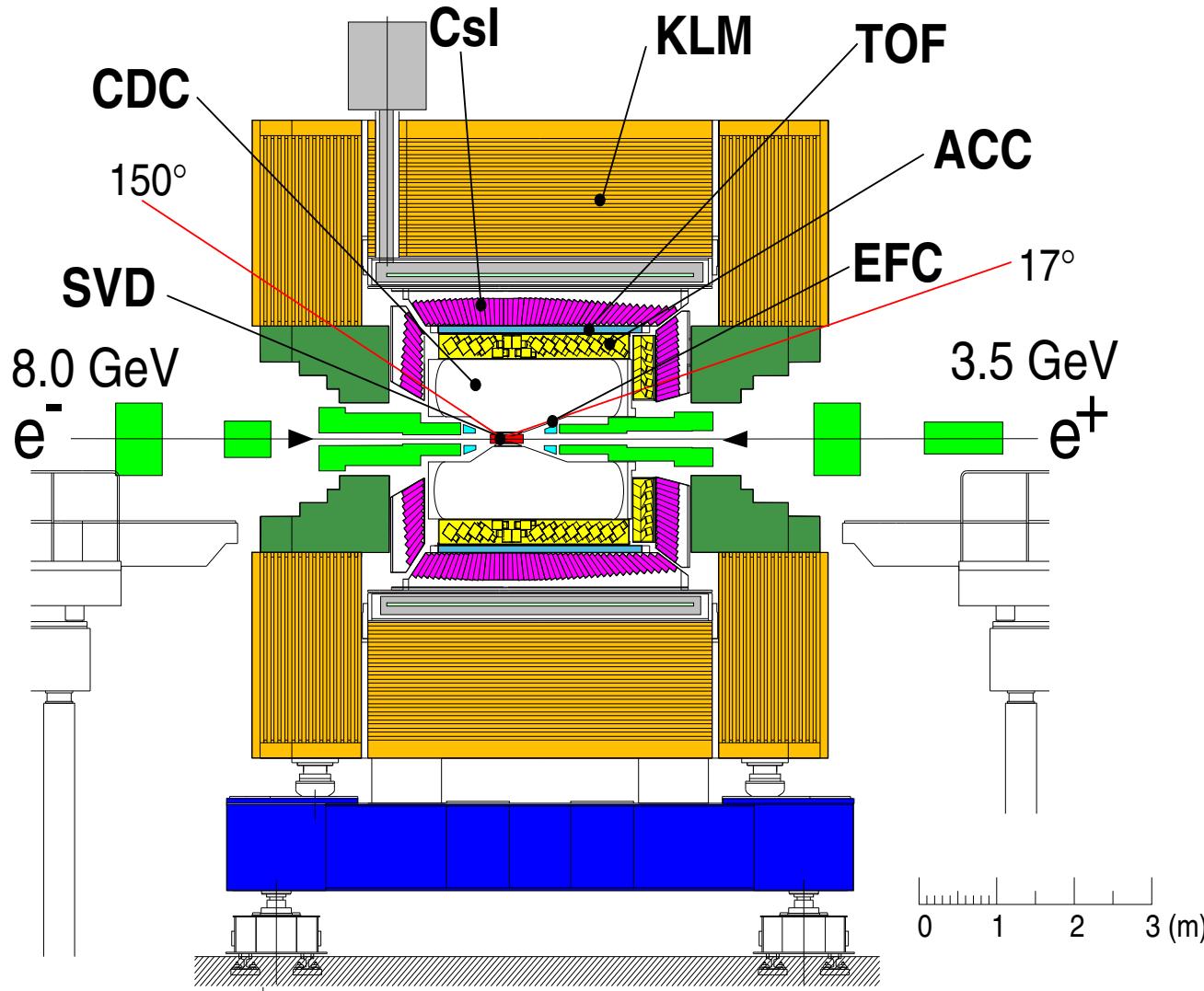
Results presented today use  $140 \text{ fb}^{-1}$  on  $\Upsilon(4S) \cong 150 \times 10^6 B\bar{B}$  pairs



runinfo ver.1.49 Exp3 Run 1 - Exp37 Run 1375 BELLE LEVEL latest

# The Best 24 Hours





- SVD 3 DSSD layers  
 $\sigma \sim 55 \mu\text{m}$  for  $1 \text{ GeV}/c$  @  $90^\circ$
- CDC 50 layers  
 $\sigma_p/p \sim 0.35\%$  @  $1 \text{ GeV}/c$
- $\sigma_\pi(dE/dx) \sim 7\%$
- TOF  $\sigma_t \sim 95 \text{ ps}$
- ACC ( $n = 1.01 \rightarrow 1.03$ )  
 $K/\pi$  separation up to  $3.5 \text{ GeV}/c$
- CsI  $\sigma_E/E_\gamma \sim 1.8\%$  @  $1 \text{ GeV}$
- KLM 14 RPC layers
- 1.5 T magnetic field

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \sim \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

where  $A, \lambda, \rho, \eta$  are Wolfenstein parameters

From unitarity ( $V_{CKM}^* V_{CKM} = 1$ ):

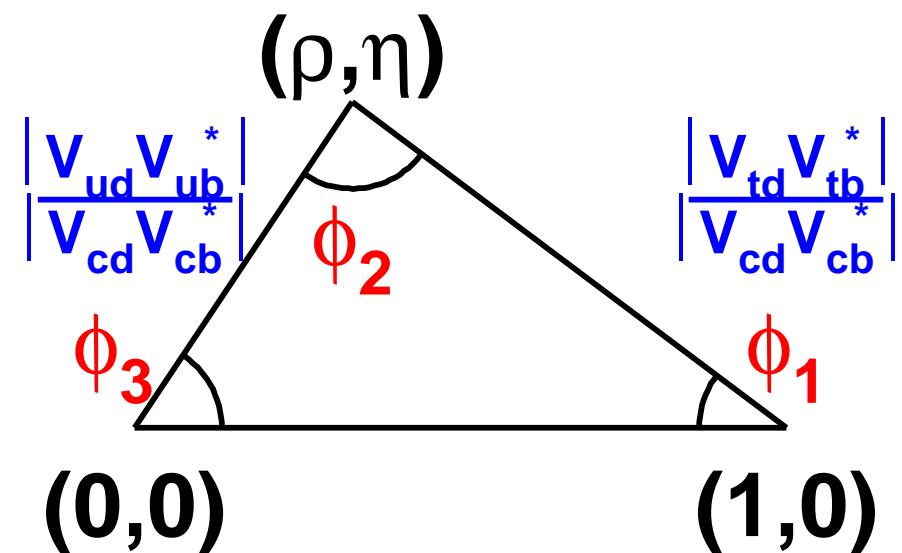
$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

## The Unitarity Triangle

$$\phi_1 \leftrightarrow \beta$$

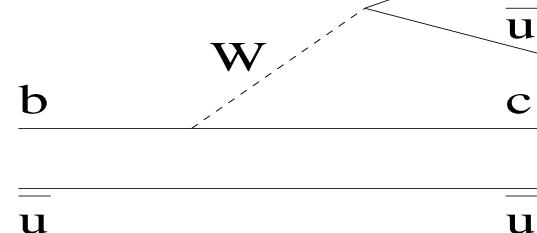
$$\phi_2 \leftrightarrow \alpha$$

$$\phi_3 \leftrightarrow \gamma$$



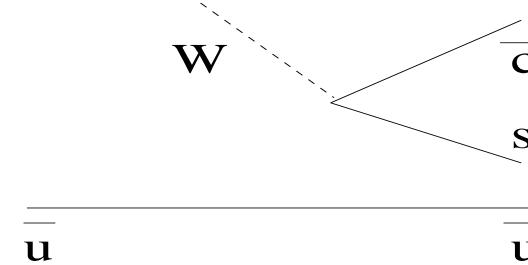
- Can access  $\phi_3$  via interference between  $B^- \rightarrow D^0 K^-$  &  $B^- \rightarrow \bar{D}^0 K^-$
- Reconstruct  $D$  in final states accessible to both  $D^0$  and  $\bar{D}^0$   
eg.  $D_{CP} K^-$  (Gronau, London, Wyler method)
- Can use multibody final states, eg.  $K_S \pi^+ \pi^-$  (first noted by Atwood, Dunietz, Soni)

$$B^- \rightarrow D^0 K^- \sim V_{us} V_{cb}^*$$



COLOUR ALLOWED

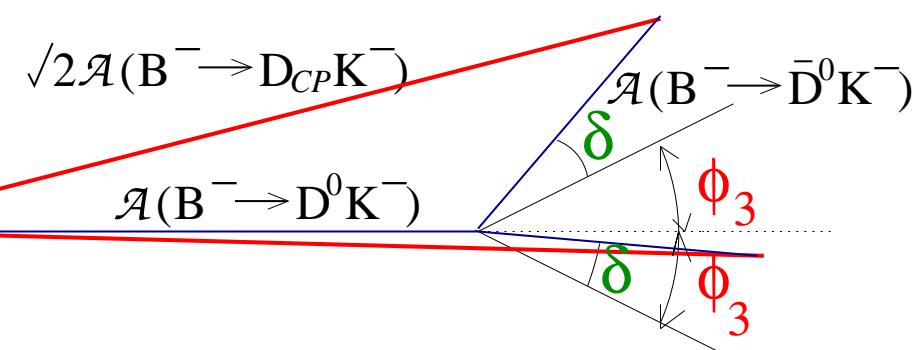
$$B^- \rightarrow \bar{D}^0 K^- \sim V_{cs} V_{ub}^*$$



COLOUR SUPPRESSED

$\mathcal{A}$  — amplitude

$r = \mathcal{A}_{\text{SUPPRESSED}} / \mathcal{A}_{\text{FAVoured}} \sim 0.1 - 0.2$

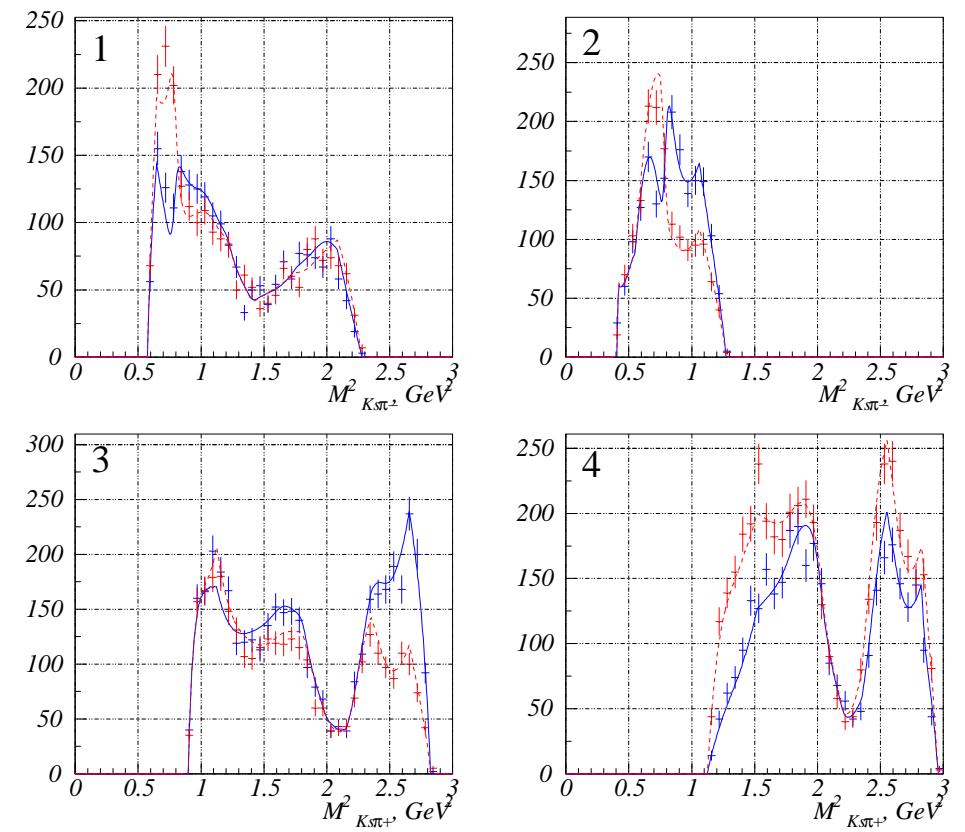
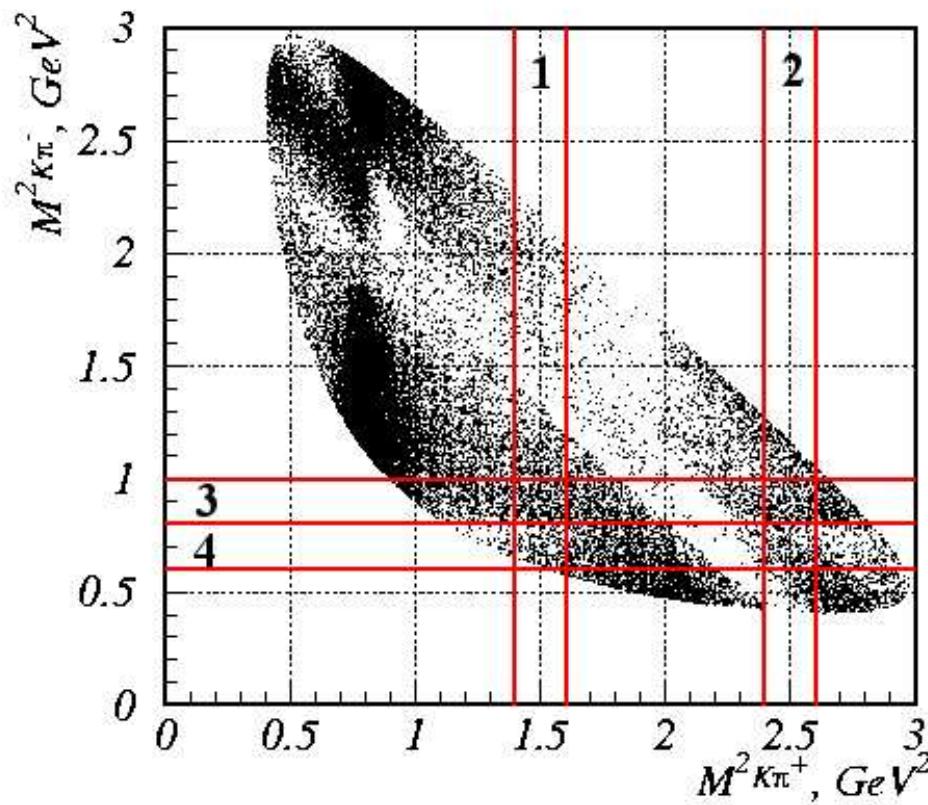


- Consider  $\bar{D}^0 \rightarrow K_S \pi^+ \pi^-$   
→ define amplitude at each Dalitz plot point as  $f(m_+^2, m_-^2)$   
where  $m_+ = m_{K_S \pi^+}$ ,  $m_- = m_{K_S \pi^-}$
- Consider  $D^0 \rightarrow K_S \pi^+ \pi^-$   
→ amplitude at each Dalitz plot point is  $f(m_-^2, m_+^2)$
- $|f(m_+^2, m_-^2)|$  can be measured using flavour tagged  $D$  mesons
- Consider  $B^+ \rightarrow (K_S \pi^+ \pi^-)_D K^+$   
→ amplitude is  $f(m_+^2, m_-^2) + r e^{i(\delta + \phi_3)} f(m_-^2, m_+^2)$
- Consider  $B^- \rightarrow (K_S \pi^+ \pi^-)_D K^-$   
→ amplitude is  $f(m_-^2, m_+^2) + r e^{i(\delta - \phi_3)} f(m_+^2, m_-^2)$
- Can extract  $(r, \delta, \phi_3)$  from  $B^+$  &  $B^-$  data

# Illustration Using Monte Carlo

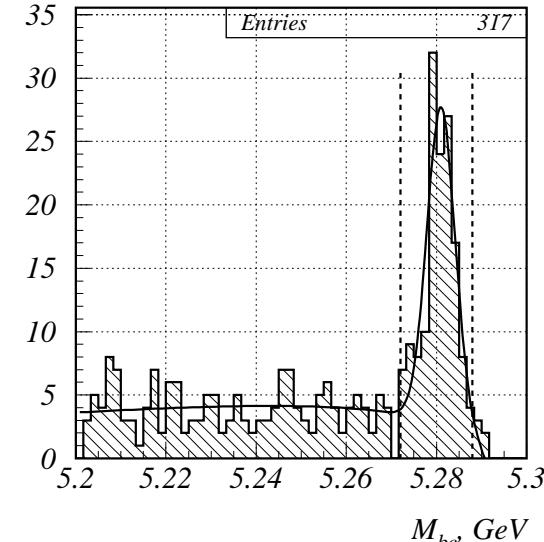
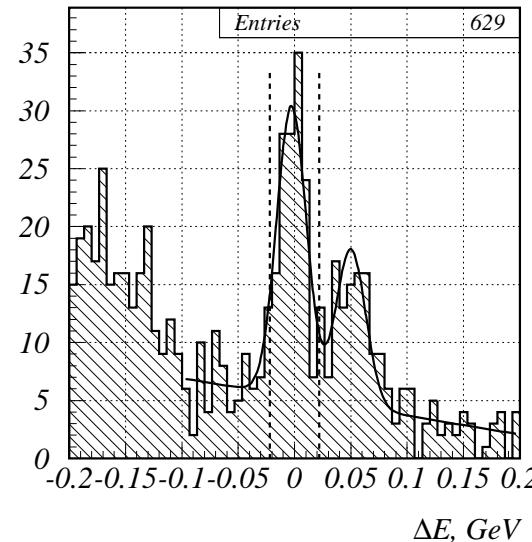


Generated 50,000 decays with  $r = 0.125$ ,  $\delta = 0$ ,  $\phi_3 = 70^\circ$



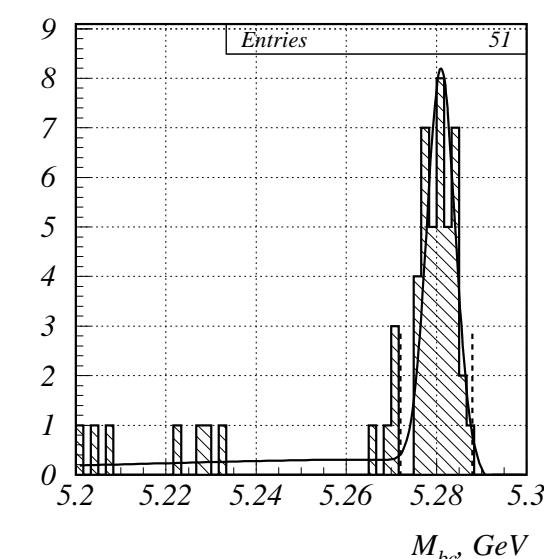
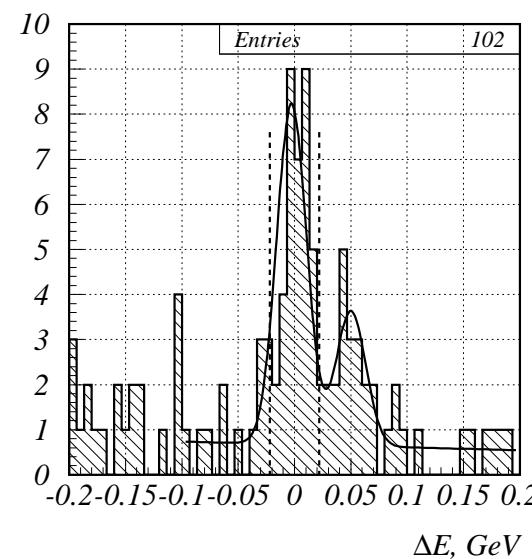
# $B^\pm \rightarrow (K_S\pi^+\pi^-)_D K^\pm$ Selection

$B^\pm \rightarrow DK^\pm$



146 candidate events ( $112 \pm 12$  signal)

$B^\pm \rightarrow D^* K^\pm$



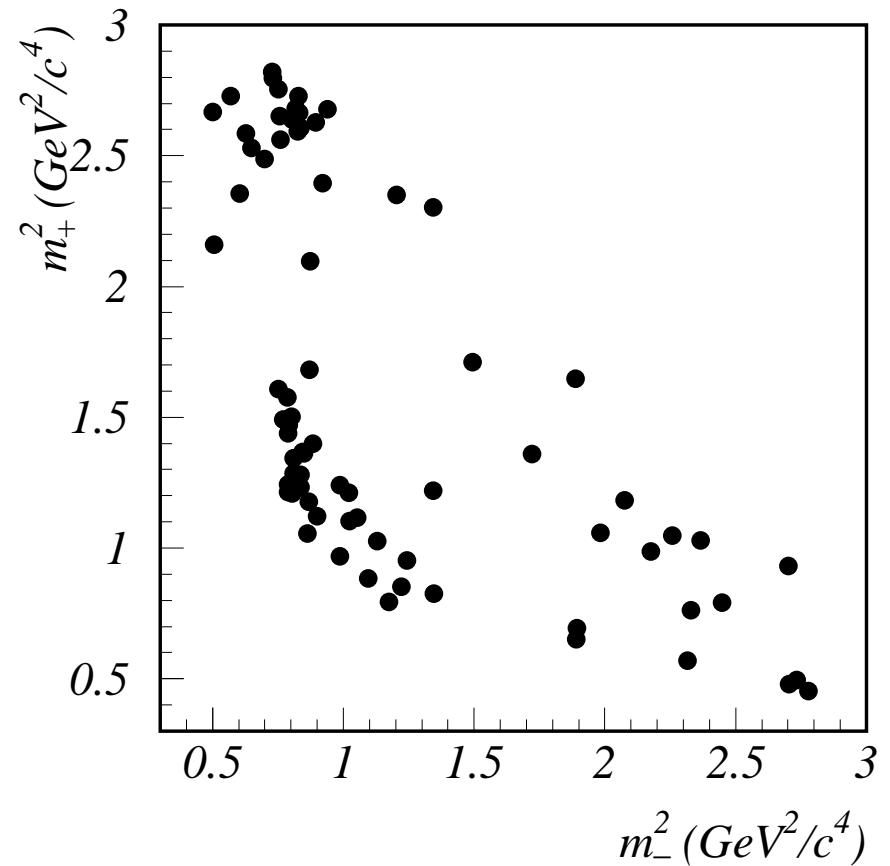
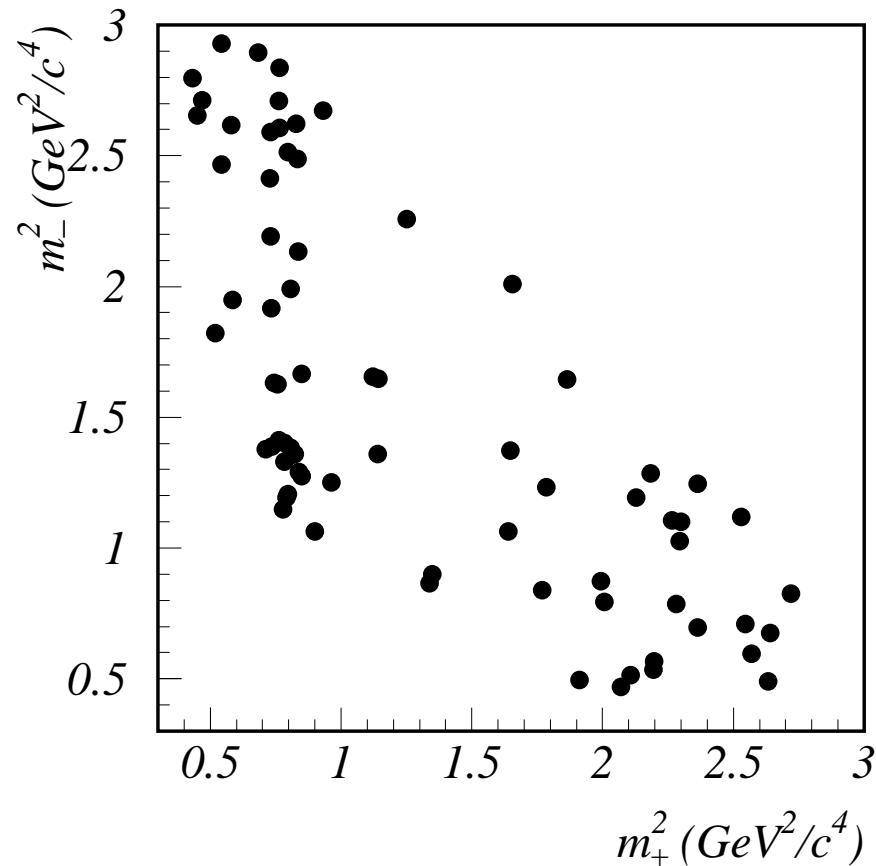
39 candidate events ( $34 \pm 6$  signal)

# $B^\pm \rightarrow (K_S \pi^+ \pi^-)_D K^\pm$ Dalitz Plot Distributions



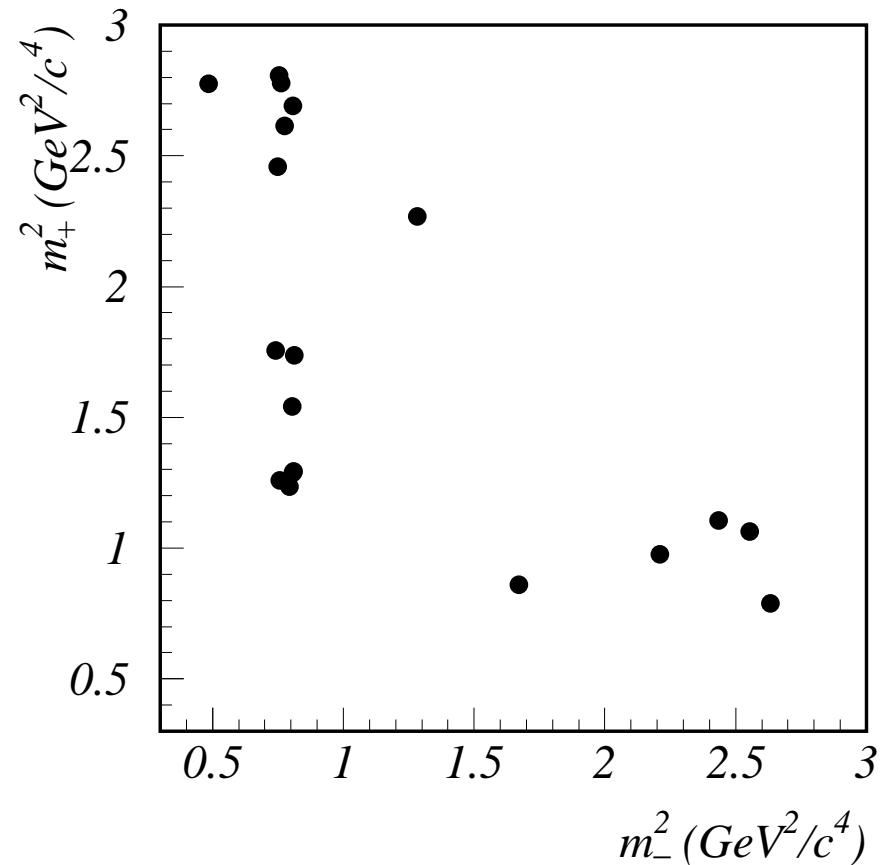
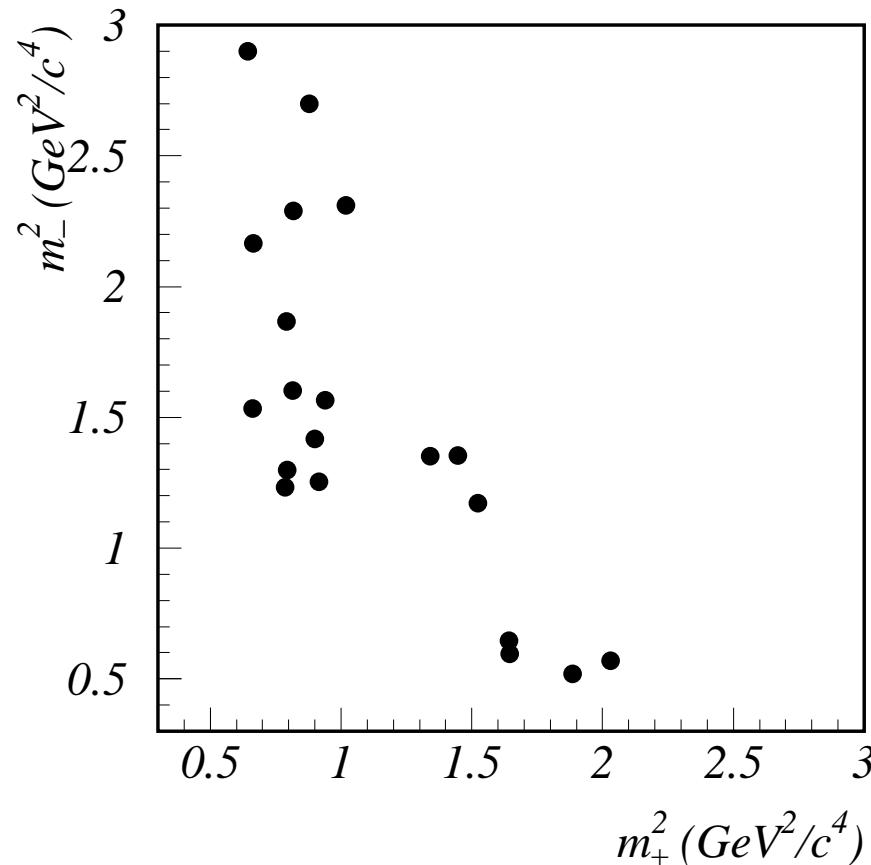
$$M_+ = f(m_+^2, m_-^2) + re^{i(\delta+\phi_3)} f(m_-^2, m_+^2)$$

$$M_- = f(m_-^2, m_+^2) + re^{i(\delta-\phi_3)} f(m_+^2, m_-^2)$$



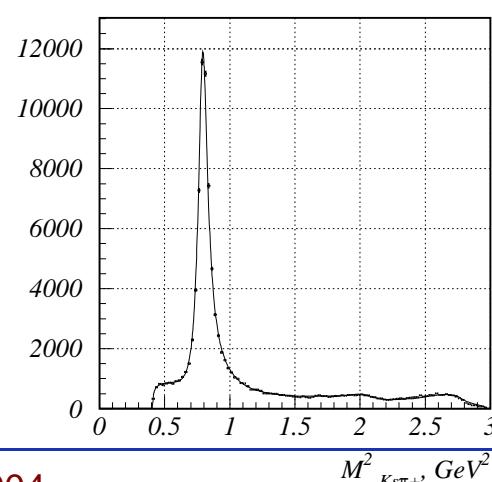
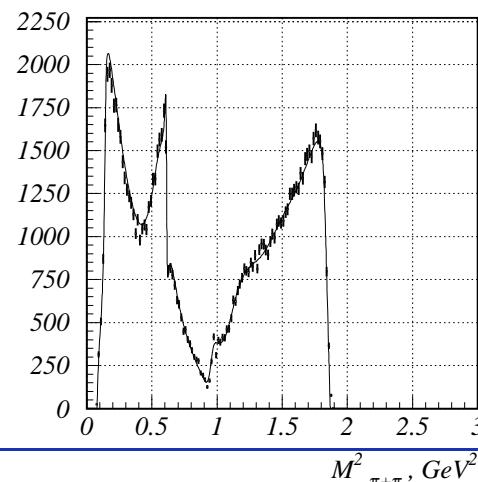
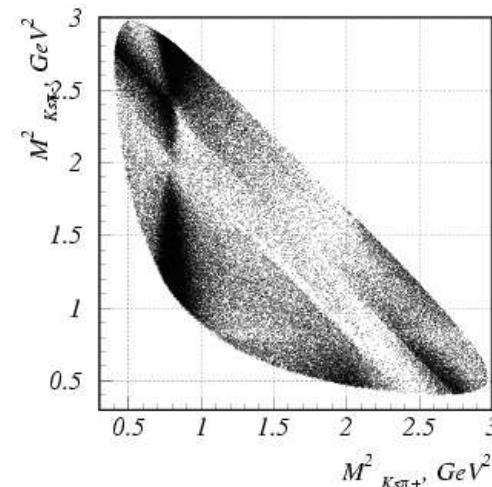
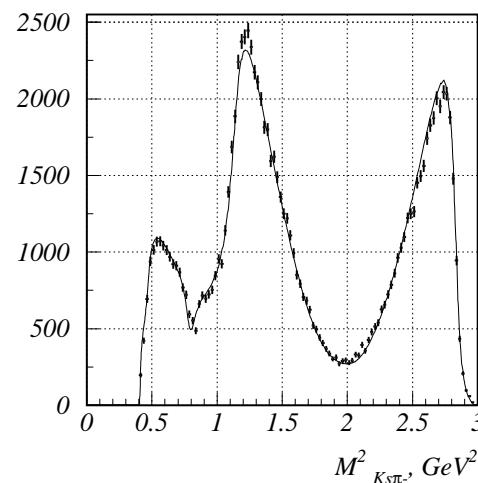
$$M_+ = f(m_+^2, m_-^2) + r e^{i(\delta + \phi_3)} f(m_-^2, m_+^2)$$

$$M_- = f(m_-^2, m_+^2) + r e^{i(\delta - \phi_3)} f(m_+^2, m_-^2)$$



# Extraction of $f(m_+^2, m_-^2)$

- Fit Dalitz plot distribution of tagged  $Ds$
- Tag using charge of  $\pi_s$  in  $D^{*+} \rightarrow D^0 \pi_s^+$
- Used *model* defines phase variation of  $f(m_+^2, m_-^2)$





# Measurement of $f(m_+^2, m_-^2)$ - Results



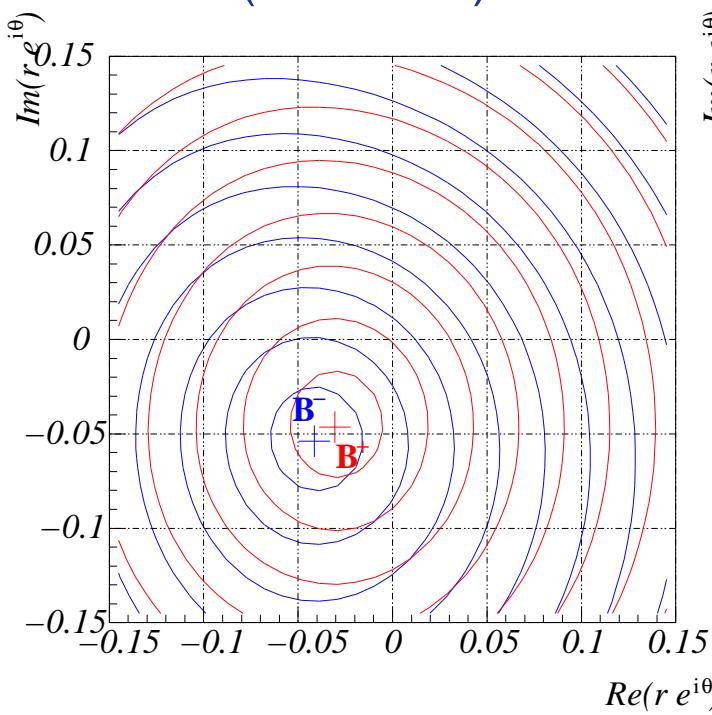
Resonance	Amplitude	Phase (°)
$K^*(892)^-\pi^+$	$1.656 \pm 0.012$	$137.6 \pm 0.6$
$K^*(892)^+\pi^-$	$(14.9 \pm 0.7) \times 10^{-2}$	$325.2 \pm 2.2$
$K_0^*(1430)^-\pi^+$	$1.96 \pm 0.04$	$357.3 \pm 1.5$
$K_0^*(1430)^+\pi^-$	$0.30 \pm 0.05$	$128 \pm 8$
$K_2^*(1430)^-\pi^+$	$1.32 \pm 0.03$	$313.5 \pm 1.8$
$K_2^*(1430)^+\pi^-$	$0.21 \pm 0.03$	$281 \pm 9$
$K^*(1680)^-\pi^+$	$2.56 \pm 0.22$	$70 \pm 6$
$K^*(1680)^+\pi^-$	$1.02 \pm 0.2$	$103 \pm 11$
$K_s\rho^0$	1.0(fixed)	0(fixed)
$K_s\omega$	$(33.0 \pm 1.3) \times 10^{-3}$	$114.3 \pm 2.3$
$K_sf_0(980)$	$0.405 \pm 0.008$	$212.9 \pm 2.3$
$K_sf_0(1370)$	$0.82 \pm 0.10$	$308 \pm 8$
$K_sf_2(1270)$	$1.35 \pm 0.06$	$352 \pm 3$
$K_s\sigma_1$	$1.66 \pm 0.11$	$218 \pm 4$
$K_s\sigma_2$	$0.31 \pm 0.05$	$236 \pm 11$
non-resonant	$6.1 \pm 0.3$	$146 \pm 3$

$$M_{\sigma_1} = 539 \pm 9 \text{ MeV}, \Gamma_{\sigma_1} = 453 \pm 16 \text{ MeV}$$

$$M_{\sigma_2} = 1048 \pm 7 \text{ MeV}, \Gamma_{\sigma_2} = 109 \pm 11 \text{ MeV}$$

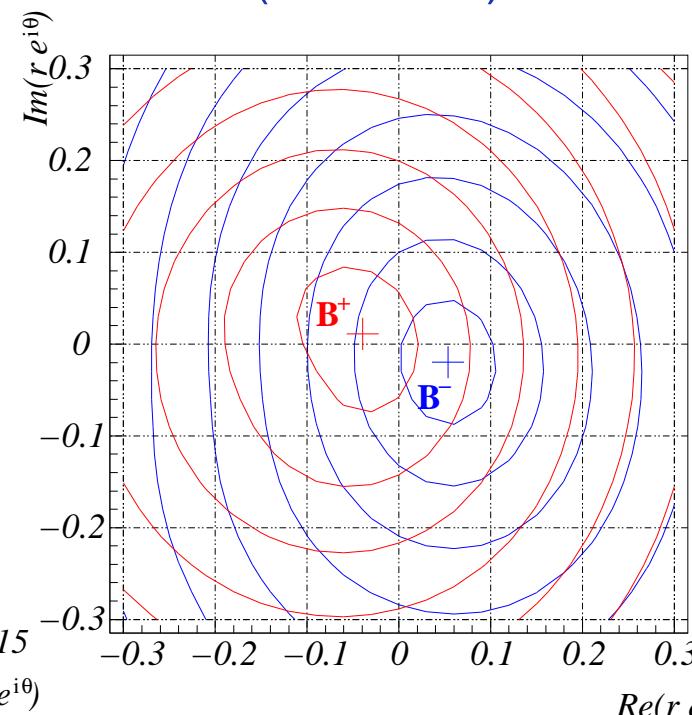
Fit  $B, \bar{B}$  samples separately, float  $r_{\pm} e^{i\theta_{\pm}}$ , where  $\theta_{\pm} = \delta \pm \phi_3$

$$B^{\pm} \rightarrow (K_S \pi^+ \pi^-)_D \pi^{\pm} \quad (r \sim 0.02)$$



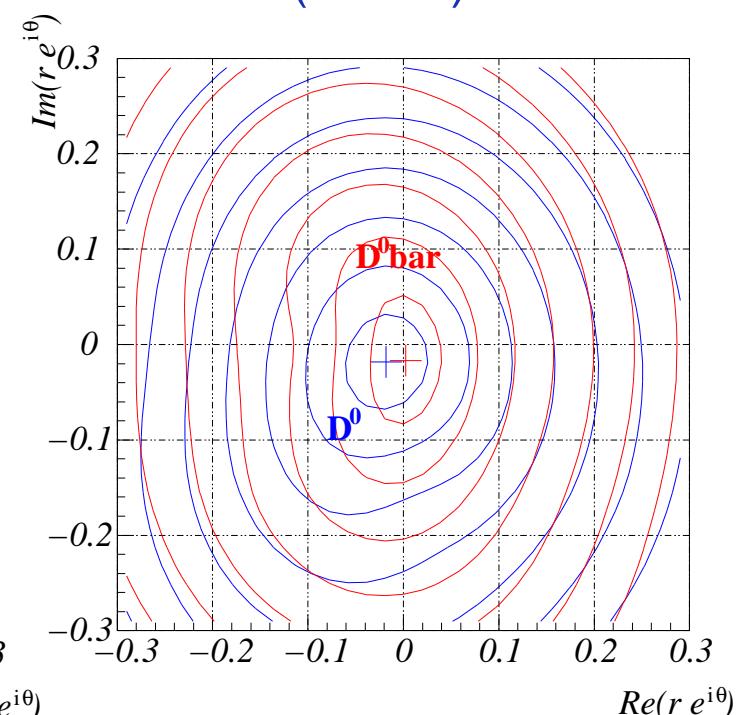
1850 events  
 $2.5\sigma$  away from 0

$$B^{\pm} \rightarrow ((K_S \pi^+ \pi^-)_D \pi^0)_{D^*} \pi^{\pm} \quad (r \sim 0.02)$$



351 events  
consistent with 0

$$B^0 \rightarrow ((K_S \pi^+ \pi^-)_D \pi^-)_{D^{*-}} \pi^+ \quad (r = 0)$$



517 events  
consistent with 0

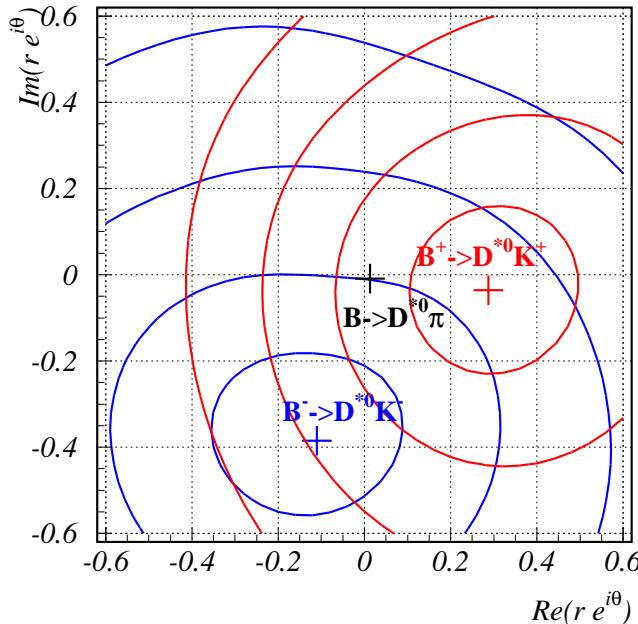
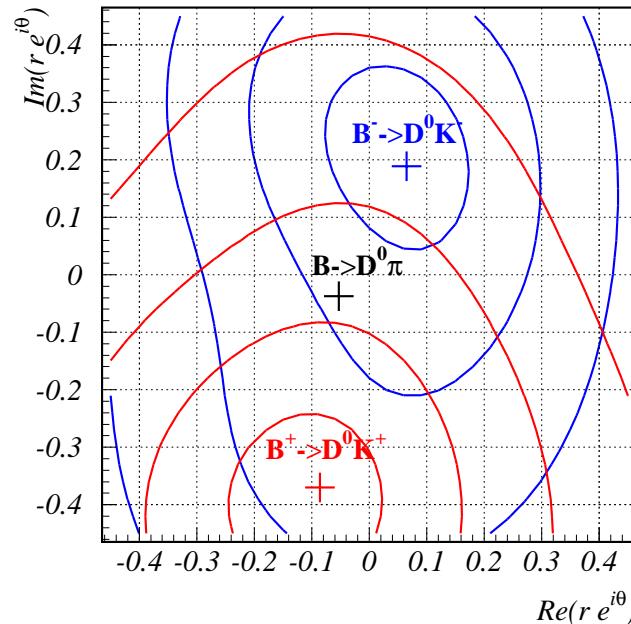
Fit  $B^\pm$  samples separately, float  $r e^{i(\delta \pm \phi_3)}$

$$B^\pm \rightarrow \left( K_S \pi^+ \pi^- \right)_D K^\pm$$

146 candidate events ( $112 \pm 12$  signal)

$$B^\pm \rightarrow \left( \left( K_S \pi^+ \pi^- \right)_D \pi^0 \right)_{D^*} K^\pm$$

39 candidate events ( $34 \pm 6$  signal)



**PRELIMINARY** Results from simultaneous fits ( $B^+$  &  $B^-$ ) (Errors from likelihood curves)

- \*  $r = 0.31 \pm 0.11$
- \*  $\phi_3 = 86^\circ \pm 17^\circ$
- \*  $\delta = 168^\circ \pm 17^\circ$

- \*  $r = 0.34 \pm 0.14$
- \*  $\phi_3 = 51^\circ \pm 25^\circ$
- \*  $\delta = 302^\circ \pm 25^\circ$

# Systematic Errors



	$B^\pm \rightarrow DK^\pm$	$B^\pm \rightarrow D^*K^\pm$
Background shape	4.6°	1.3°
Background fraction	0.1°	0.6°
Efficiency shape	3.5°	0.8°
Momentum resolution	2.5°	2.5°
$B^\pm \rightarrow D\pi^\pm$ test sample bias	11°	11°
Total	13°	11°

$$f(m_+^2, m_-^2) = |f(m_+^2, m_-^2)| e^{i\phi(m_+^2, m_-^2)}$$

- Fit to flavour tagged  $D$  sample measures  $|f(m_+^2, m_-^2)|$   
BUT  $\phi(m_+^2, m_-^2)$  model-dependent
- Estimate model uncertainty by varying model

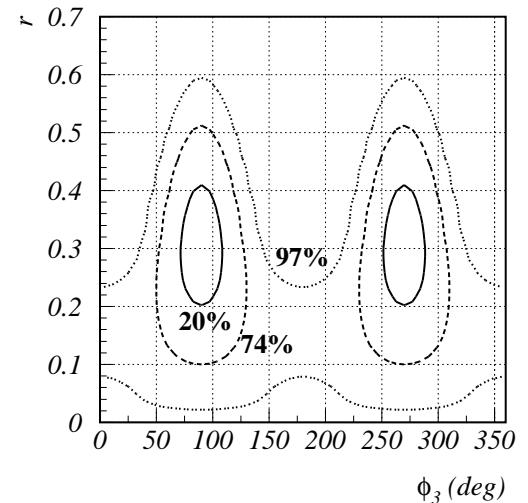
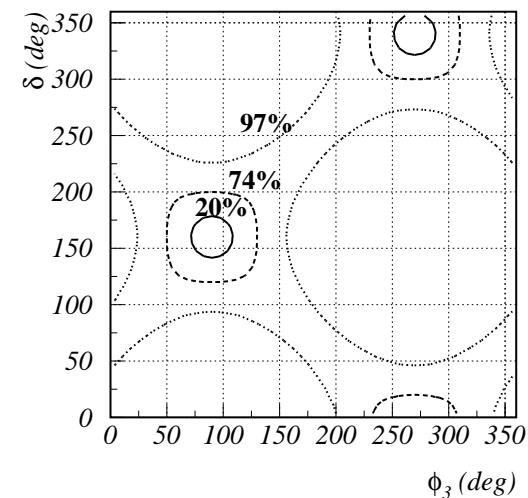
Fit model	$(\Delta\phi_3)_{\text{max}}$
Only $K^*, \rho, \omega, f_0$ non-resonant	$9.9^\circ$
Meson formfactors $F_r = F_D = 1$	$3.1^\circ$
Constant BW width $\Gamma(q^2)$	$4.7^\circ$
No non-resonant amplitude $a_{NR} = 0$	$0.4^\circ$
No $\sigma(500)$	$0.7^\circ$
Total	$11^\circ$

- Consider  $CP$ -tagged  $D$  mesons decaying to  $K_S\pi^+\pi^-$   
→ amplitude is  $f(m_+^2, m_-^2) \pm f(m_-^2, m_+^2)$
- FUTURE: use  $CP$  tagged  $D$  mesons from  $c\tau$  factory ( $\psi'' \rightarrow D\bar{D}$ )  
→ measure  $\phi(m_+^2, m_-^2) \Rightarrow \underline{\text{remove model uncertainty}}$

Avoid using fit likelihood errors → construct PDF for  $(r, \phi_3, \delta)_{\text{true}}$  using Toy MC

$$B^\pm \rightarrow \left( K_S \pi^+ \pi^- \right)_D K^\pm$$

$\phi_3 > 0$  with  $> 94\%$  probability



PRELIMINARY

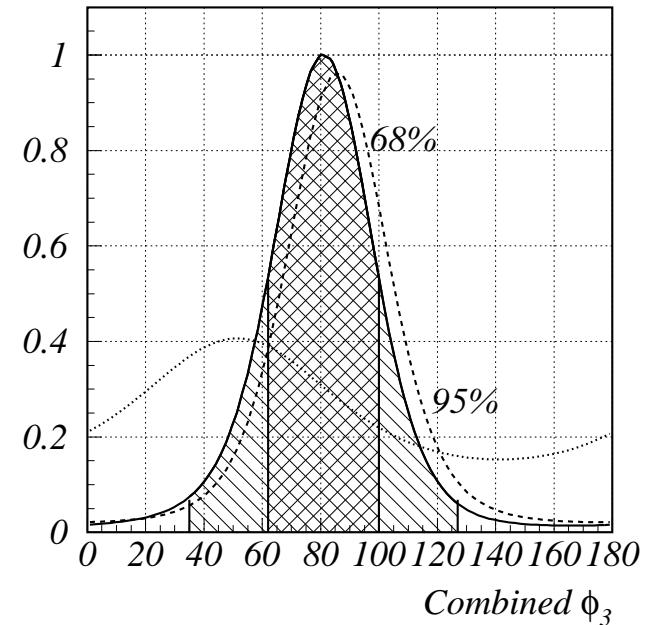
$$B^\pm \rightarrow \left( K_S \pi^+ \pi^- \right)_D K^\pm: \quad \phi_3 = 86^\circ \pm 20^\circ (49^\circ)$$

$$B^\pm \rightarrow \left( \left( K_S \pi^+ \pi^- \right)_D \pi^0 \right)_{D^*} K^\pm: \quad \phi_3 = 51^\circ \pm 47^\circ (82^\circ)$$

Combined:

$$\phi_3 = 81^\circ \pm 19^\circ (46^\circ)_{\text{stat}} \pm 13^\circ_{\text{sys}} \pm 11^\circ_{\text{model}}$$

Errors are 68% (95%) confidence limits



- Novel technique to extract  $\phi_3$  applied to  $140 \text{ fb}^{-1}$  of Belle data
- First **PRELIMINARY** direct measurement of  $\phi_3$ 

$\phi_3 = 81^\circ \pm 19^\circ (46^\circ)_{\text{stat}} \pm 13^\circ_{\text{sys}} \pm 11^\circ_{\text{model}}$
- Model-independent approach exists using  $c\tau$  factory data