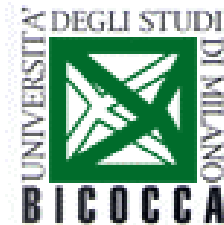


Università degli Studi di Milano Bicocca



Variation of Refractive Index inside an Aerogel Block



Davide Perego

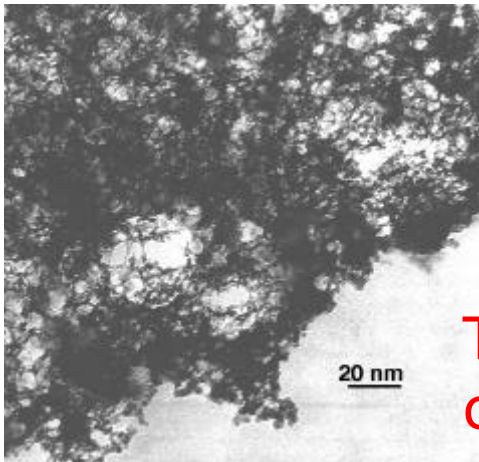
RICH MEETING - CERN - April 21st 2004

Introduction

The Refractive Index of aerogel and its density are related by the following relation:

$$n(\mathbf{l}) = 1 + k(\mathbf{l})r$$

$$k=0.21$$
$$@ \lambda=632 \text{ nm}$$



Local inhomogeneities (occurring during production) lead to variations of the Refractive Index within monoliths

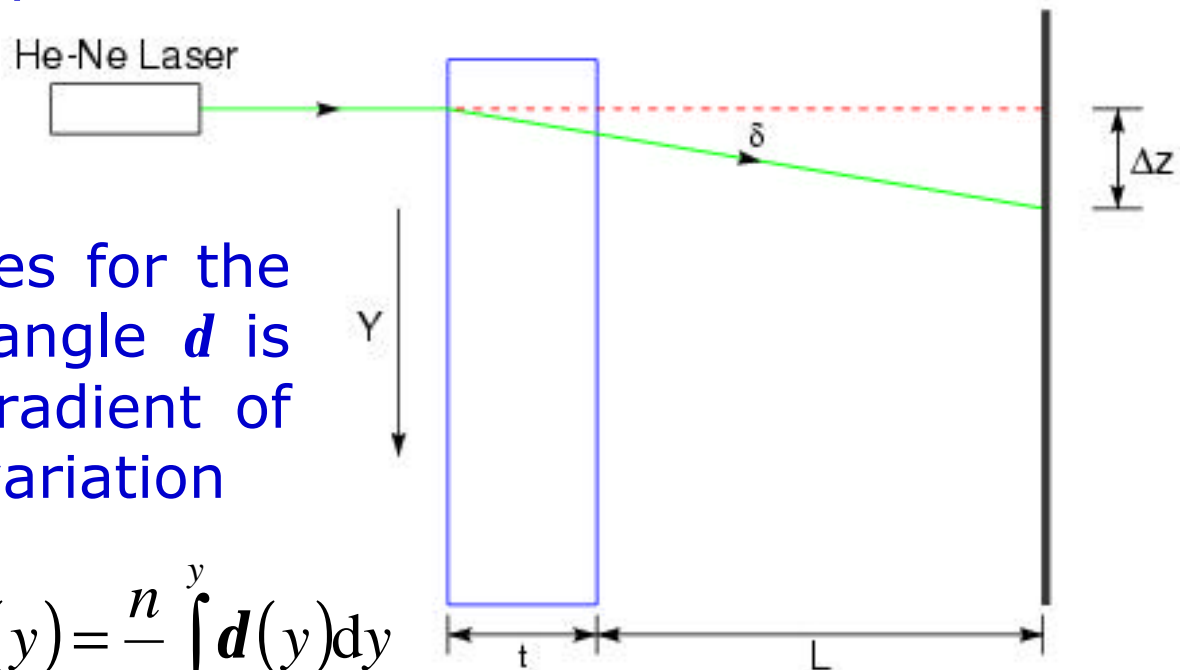
These variations can give non-negligible contribution to the q_C measurement accuracy

Δn_{\max} allowed for LHCb RICH1 aerogel tiles is $\sim 3 \cdot 10^{-4}$, corresponding to Δq_C 1.17 mrad

How such variations can be evaluated? Two methods available: (I) Laser Beam Deflection and (II) APACHE

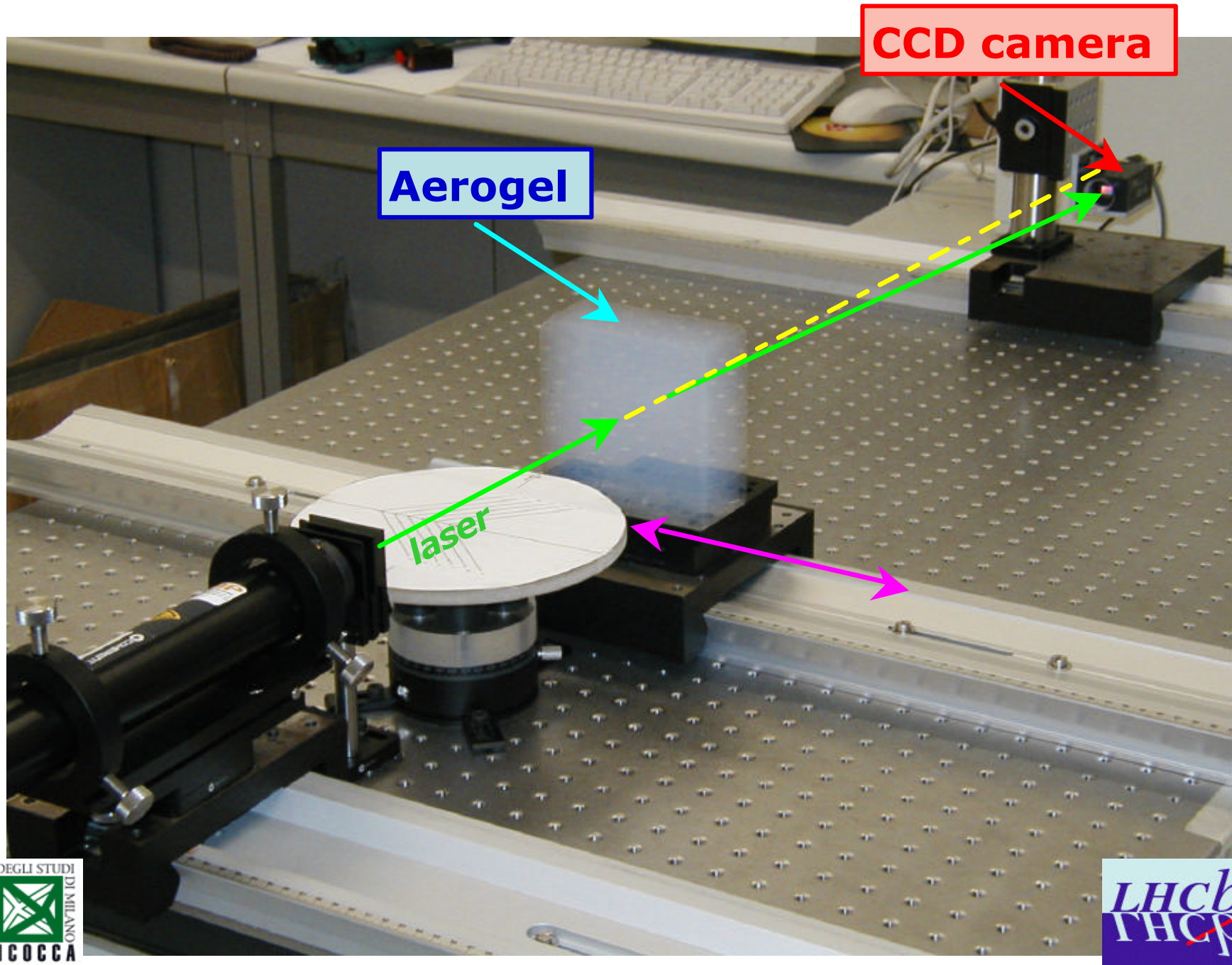
Laser Beam Method

Local variations of the Refractive Index in a uniformly transparent medium are gradient indexes which affect the propagation of laser rays



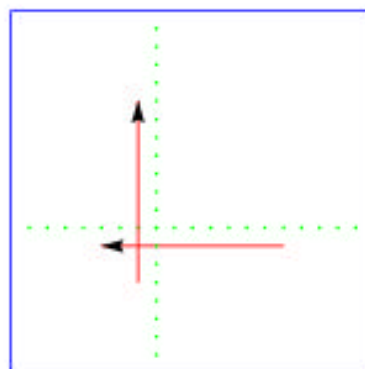
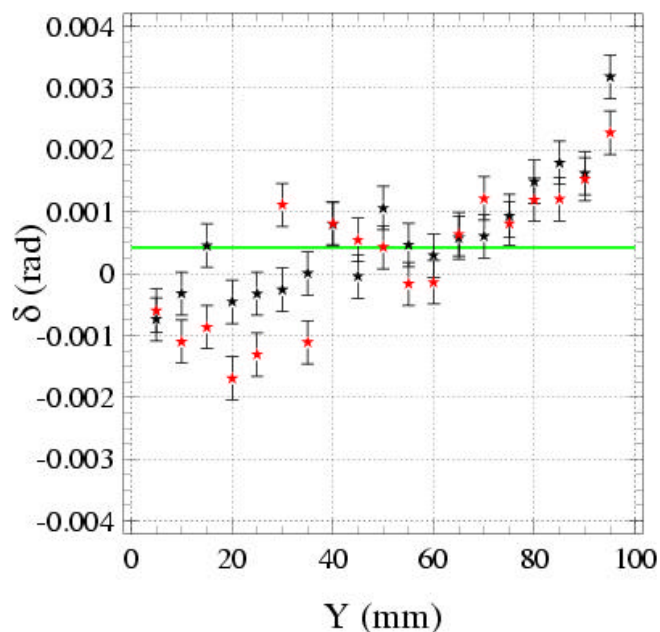
Assuming parallel faces for the block, the deviation angle d is proportional to the gradient of the Refractive Index variation

$$\frac{dn}{dy} \approx \frac{n \cdot d(y)}{t \cdot L} \quad \Rightarrow \quad \Delta n(y) = \frac{n}{t} \int_{y_0}^y d(y) dy$$



Laser Beam Method

Measurements performed with a $100 \times 100 \times 42 \text{ mm}^3$ block & with $L=75.8 \text{ cm}$

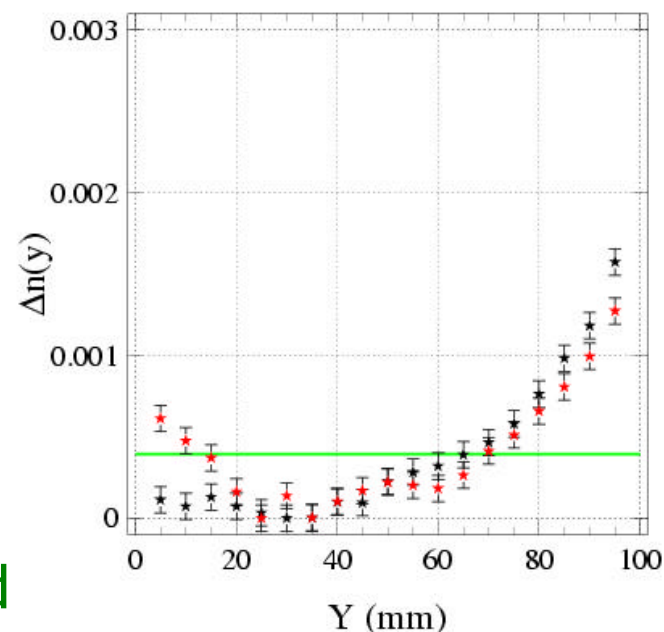


$n = 1.031$

$\lambda = 543.5 \text{ nm}$

$\sigma_{\delta} \sim 0.35 \text{ mrad}$

$\sigma_{\Delta n} \sim 0.8 \cdot 10^{-4}$



$\sigma_n = 4.6 \cdot 10^{-4}$ which means $\sigma_q = 1.8 \text{ mrad}$

APACHE

Why not using a particle beam to characterize Aerogel tiles?

500 MeV electron beam at the **BTF** Beam Test Facility (**DAFNE** LNF-Frascati)



photographic film in a "*proximity focusing*" configuration...

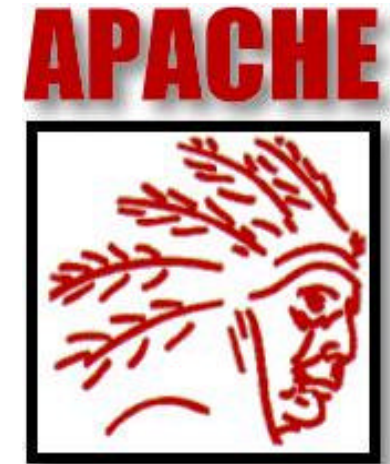
APACHE

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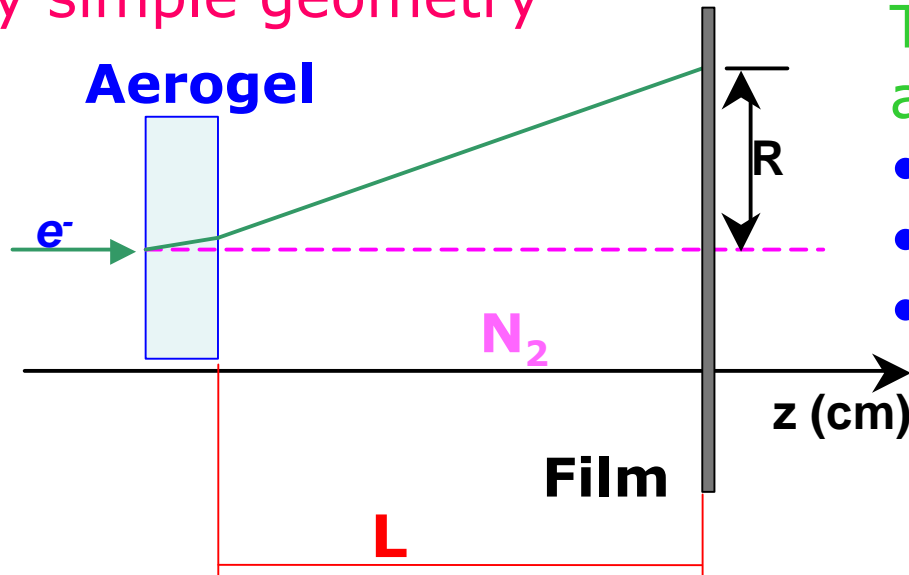


APACHE

Aerogel Photographic Analysis by Cherenkov Emission

APACHE

Very simple geometry

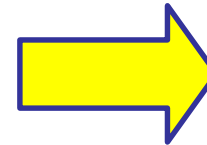


The radius of the ring, R , is a function of:

- Refractive Index $n=n(\lambda)$
- aerogel thickness t
- aerogel-film distance L

The dimensions of the photographic film define the maximum R

8"×10" Kodak TRI-X B/W
8"×10" Kodak EKTACHROME
(wavelength range: 300÷600 nm)

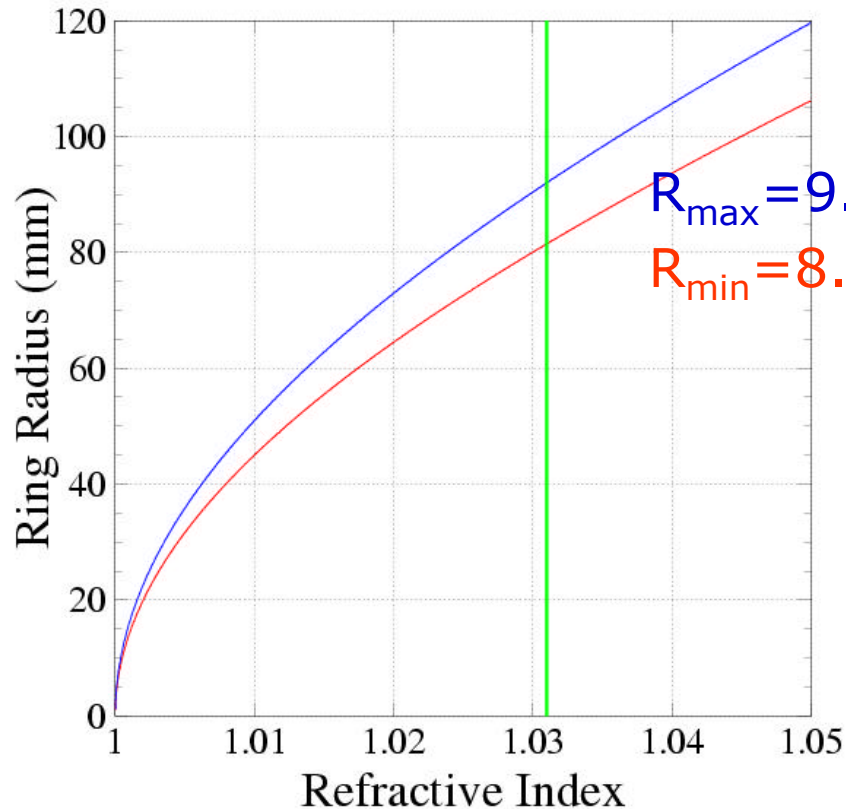


L 30.0 cm

$n \sim 1.031$ with
 $\lambda = 543.5$ nm

APACHE

Assuming a simplified scenario without scattering, chromatic dispersion, absorption effects, etc



$R_{\max} = 9.19 \text{ cm}$
 $R_{\min} = 8.14 \text{ cm}$

Parameters

$n = 1.031$

$\beta = 1$

$t = 4.2 \text{ cm}$

$d = 31.4 \text{ cm}$

$$R_{\min} = L \tan \left[\arcsin \left[n \sin \left(\arccos \left(\frac{1}{nb} \right) \right) \right] \right]$$

$$R_{\max} = R_{\min} + t \tan \left[\arccos \left(\frac{1}{nb} \right) \right]$$

Geant 4

APACHE

Beam & Geometry

520 MeV e^- Beam

$L=31.4$ cm

Beam spot size

$\sigma_x = \sigma_y = 4.0$ mm

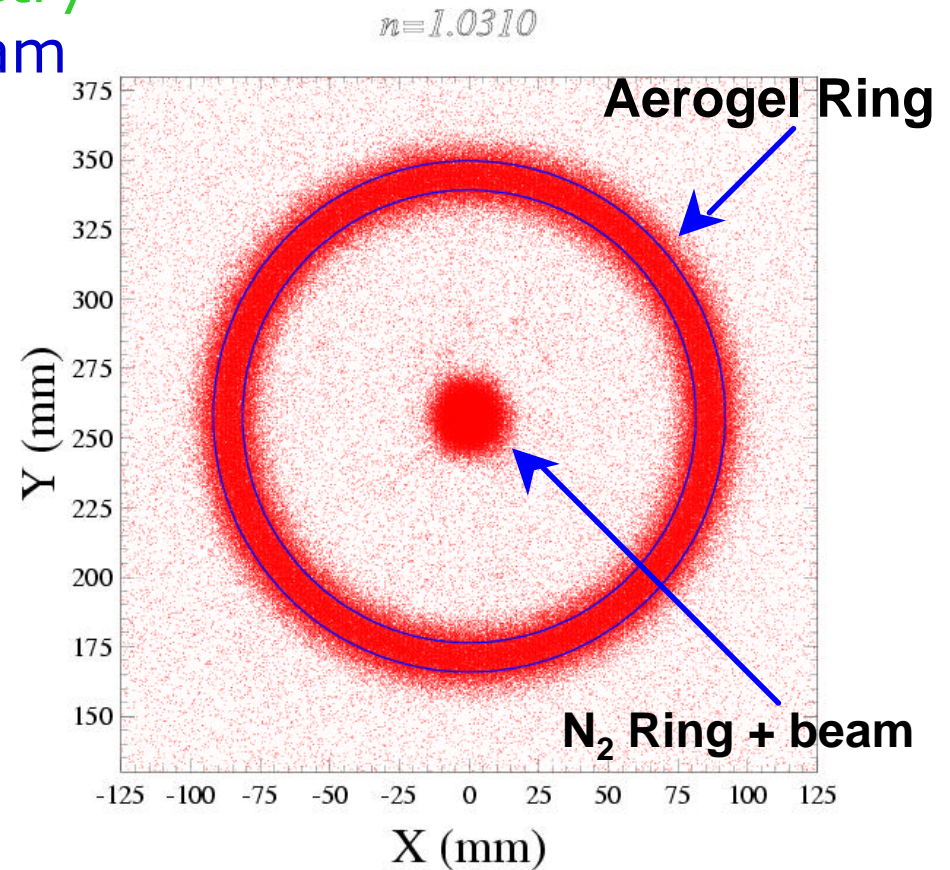
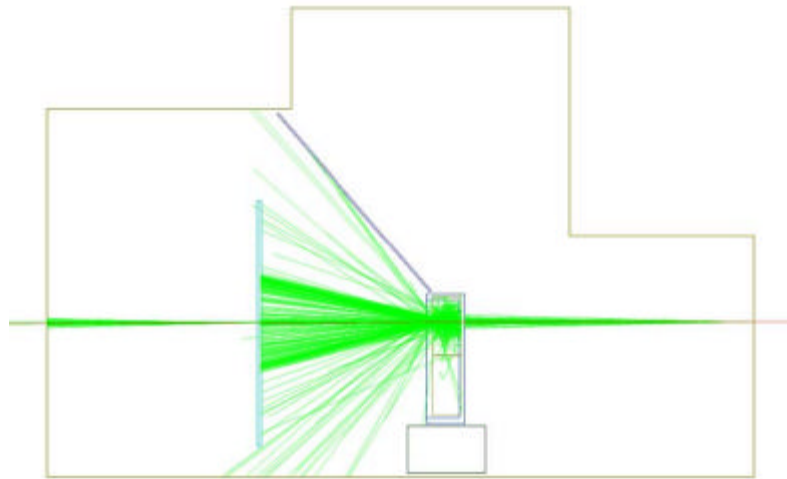
Aerogel

$n=1.031$

$t=4.2$ cm

$A=95.58\%$

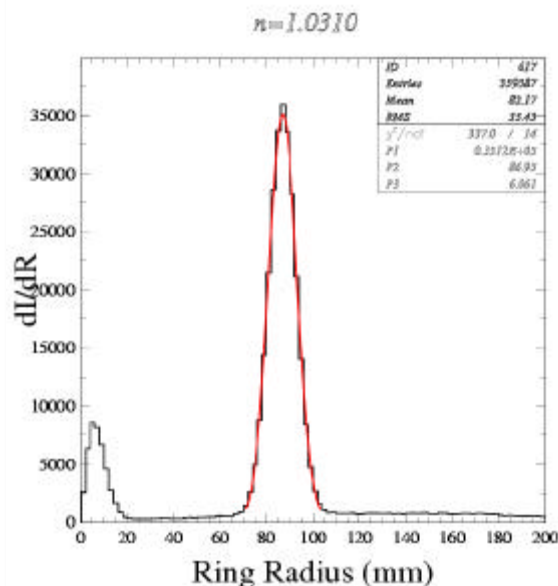
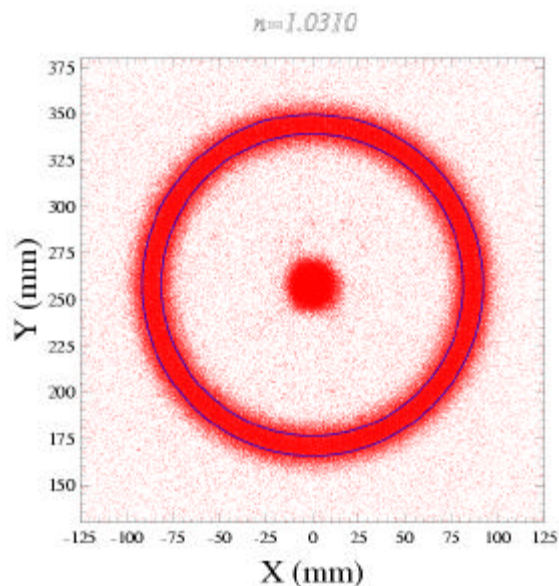
$C=0.0060 \mu\text{m}^4/\text{cm}$



APACHE

Procedure for the analysis of the films:

- digitization with a (8bit) scanner
- subtraction of background
- search of the center of gravity, then integration
- comparison of the positions of peaks for different input n



Geant 4

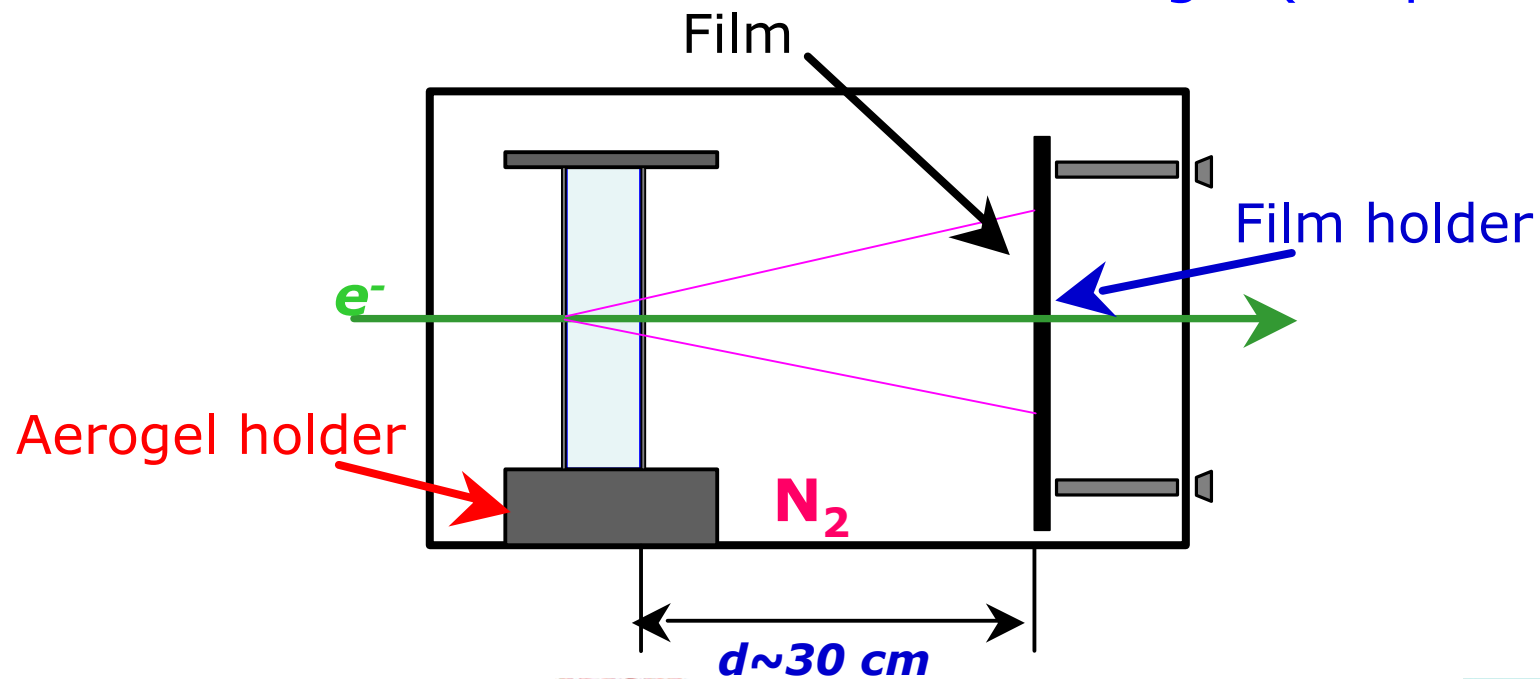
n	R (mm)
1.0307	86.55±0.01
1.0310	86.95±0.01
1.0313	87.41±0.01

Resolution for $3 \cdot 10^{-4}$
 ~ 0.25 mm

APACHE

Experimental Setup:

- portable dark room, $\sim 60 \times 60 \times 60$ cm³
- variable height aerogel holder
- N₂ flux inside the dark room
- 0.1 mm D263 filter downstream the aerogel (UV photons)

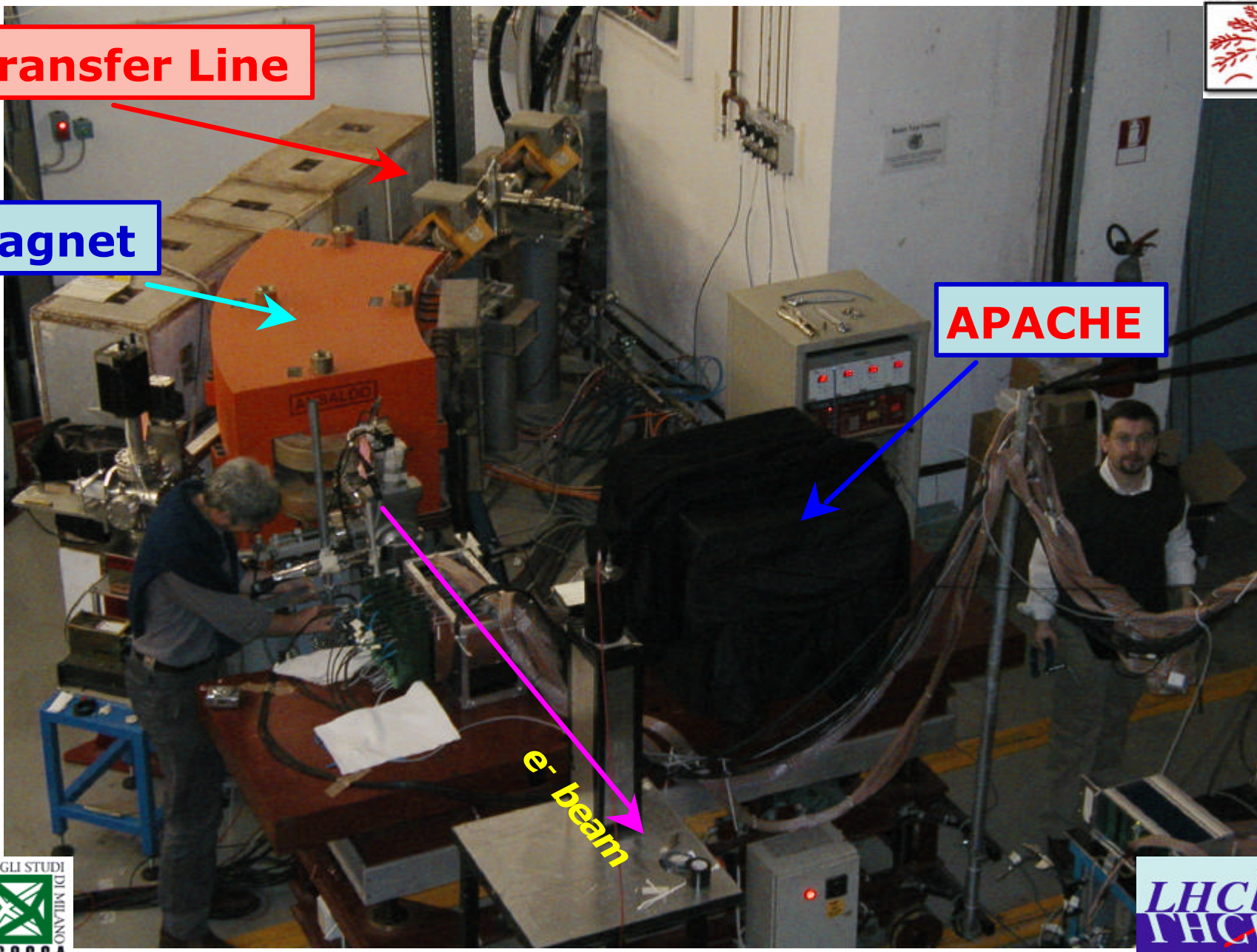


Transfer Line

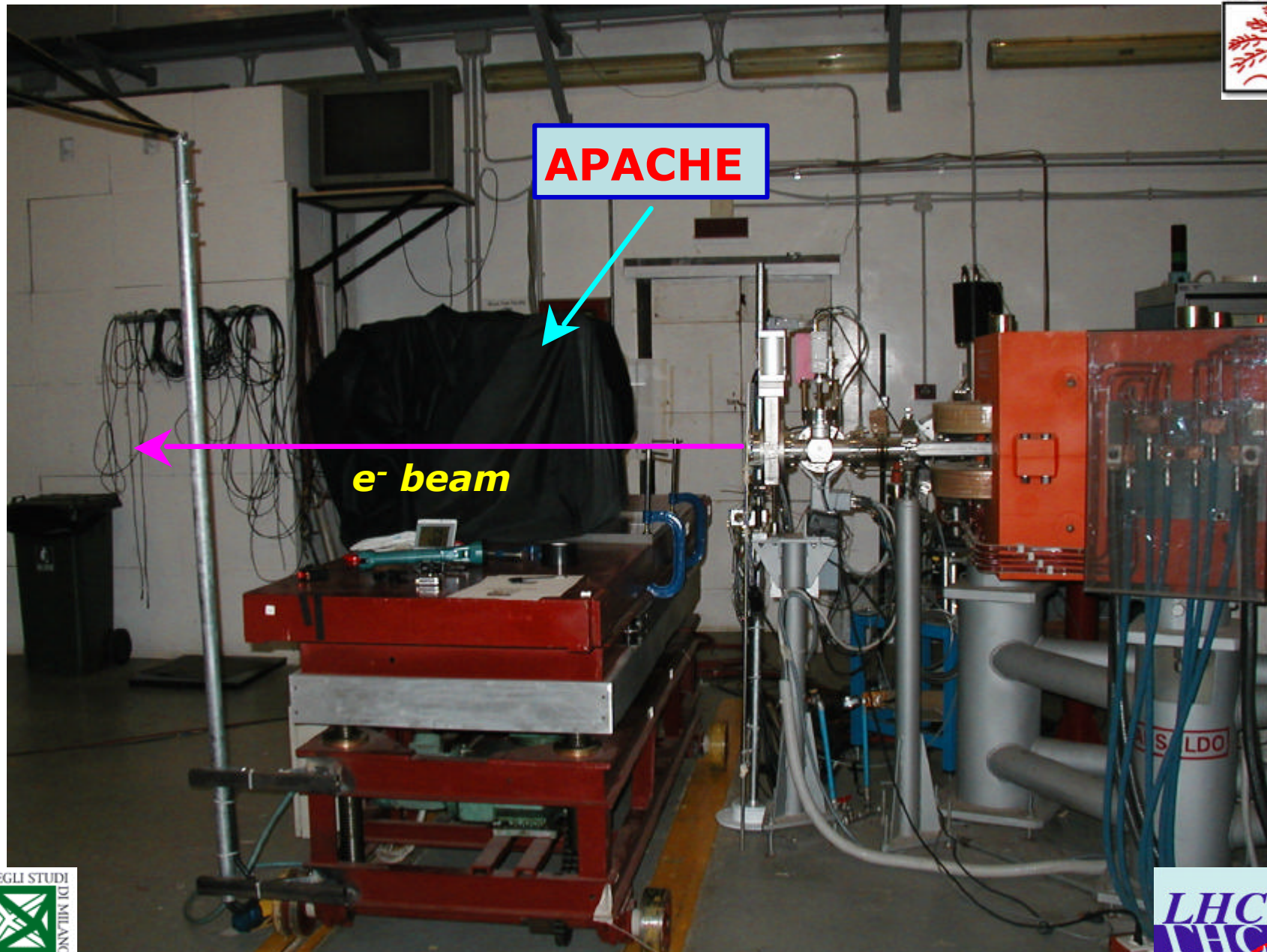
Magnet

APACHE

e⁻ beam



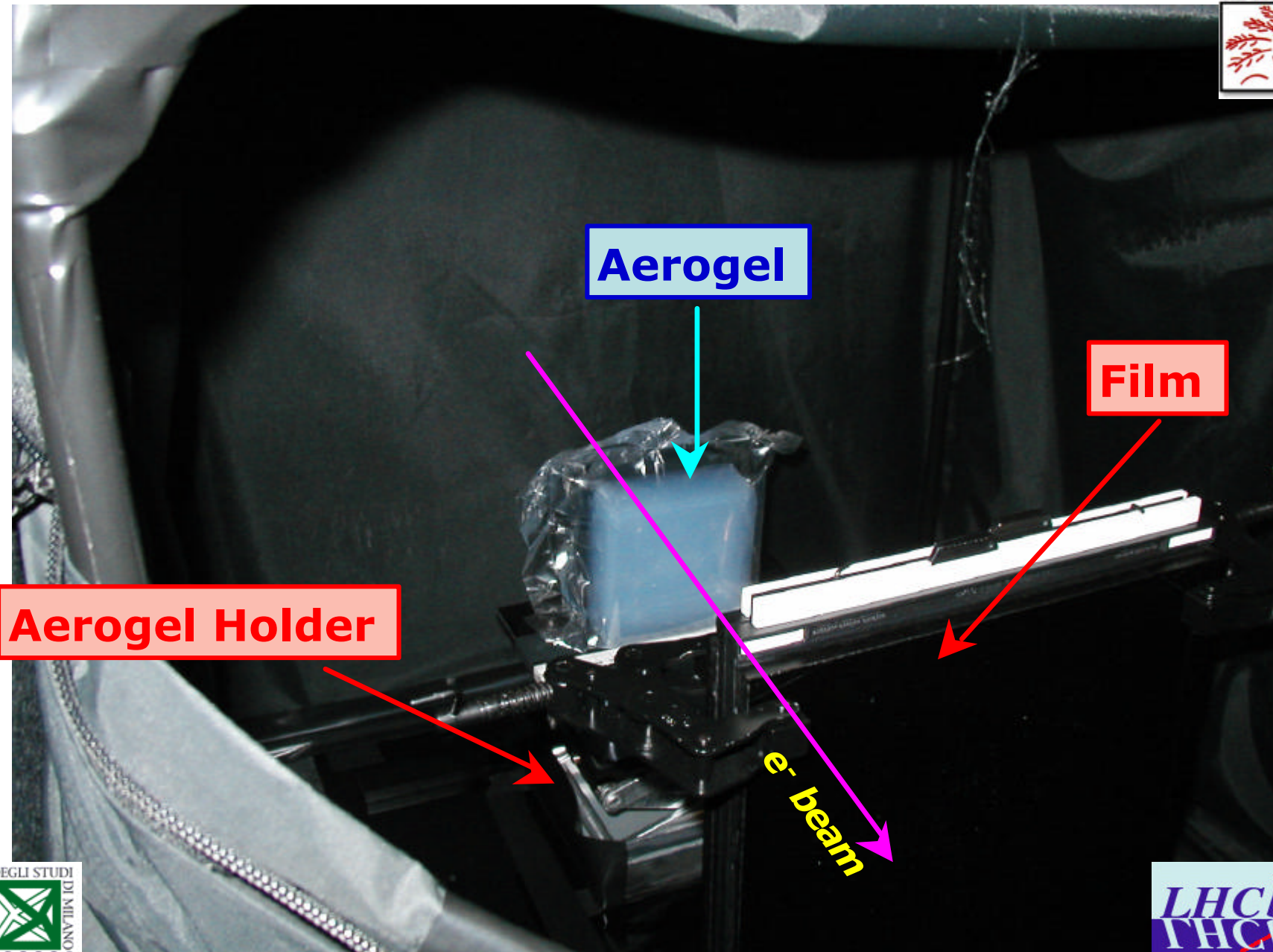
APACHE



APACHE

e- beam





Aerogel Holder

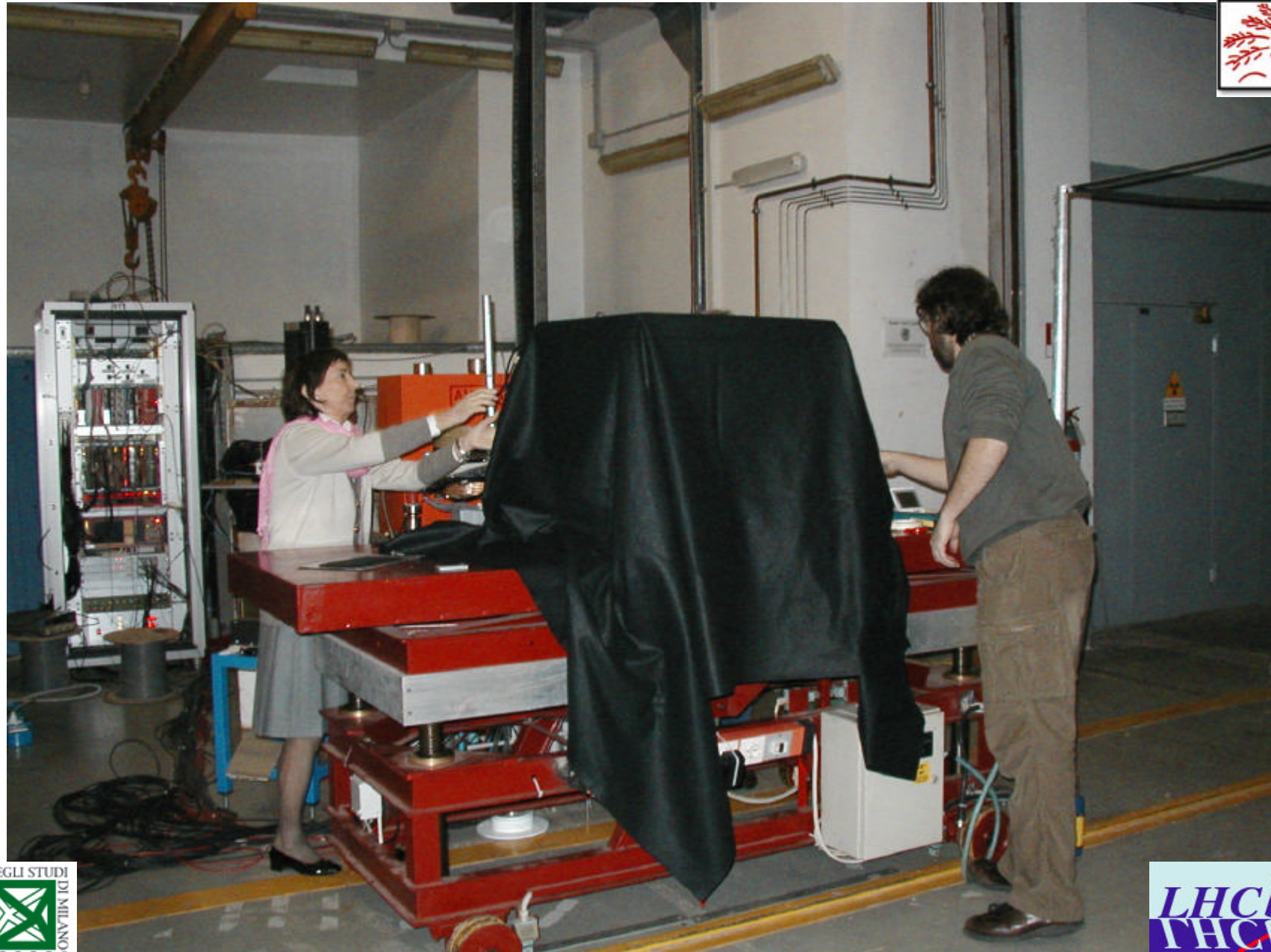
Aerogel

Film

e- beam

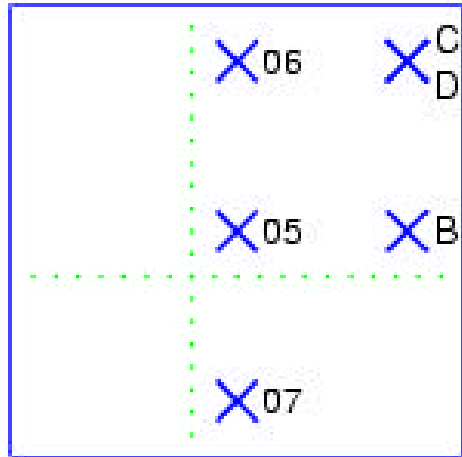
APACHE





APACHE

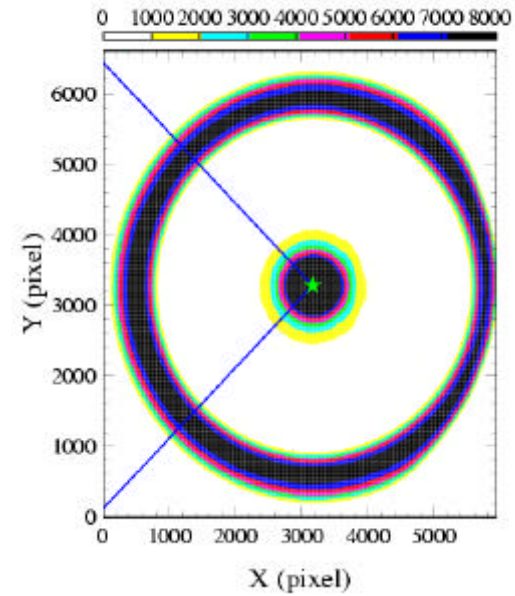
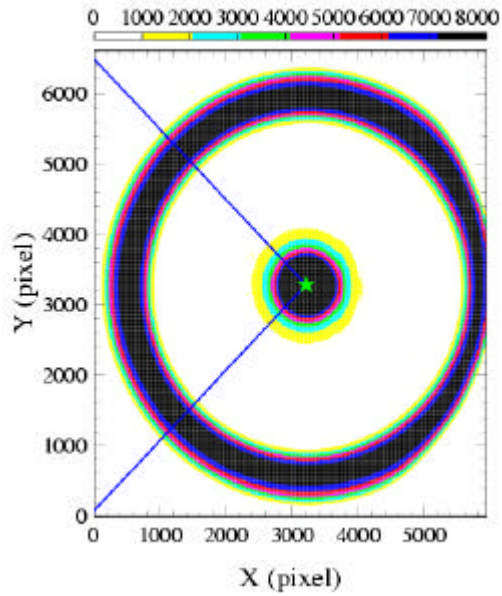
- data taking: March 2004 @ BTF, LNF-Frascati
- $\sim 10^{10}$ electrons/run
- scan on different entrance points
- 0.1 mm D263 filter used for run D (compare to run C)
- films processed by a professional PhotoLab in Frascati
- digitization for the analysis



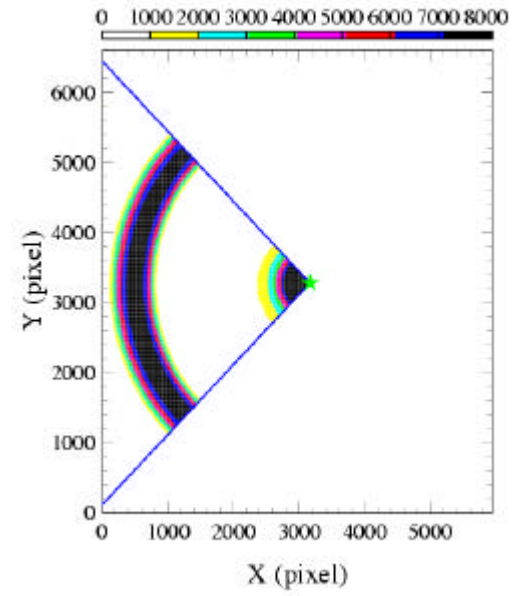
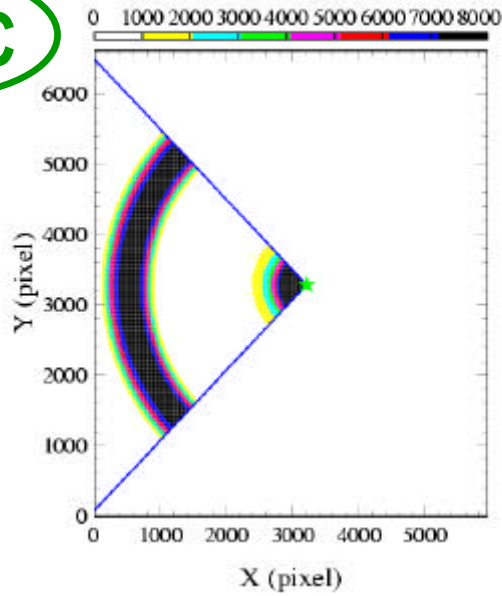
V. Kandinsky,
Einige Kreise (1926)



see the processed films...



Run C



Run D



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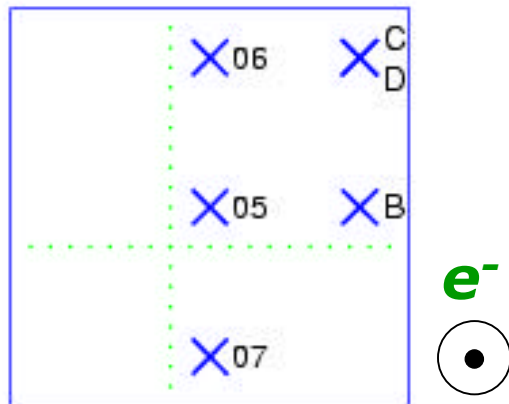


APACHE

There is not yet an analytical description of the shape of the distributions (i.e. how to parametrize the film efficiency, etc)

Preliminary results available with the following methods:

- Gaussian fit restricted to the rising and falling edges of the distributions around the peak
- Center of gravity of the distribution's peaks
- Radius corresponding to the maximum of the differential distributions

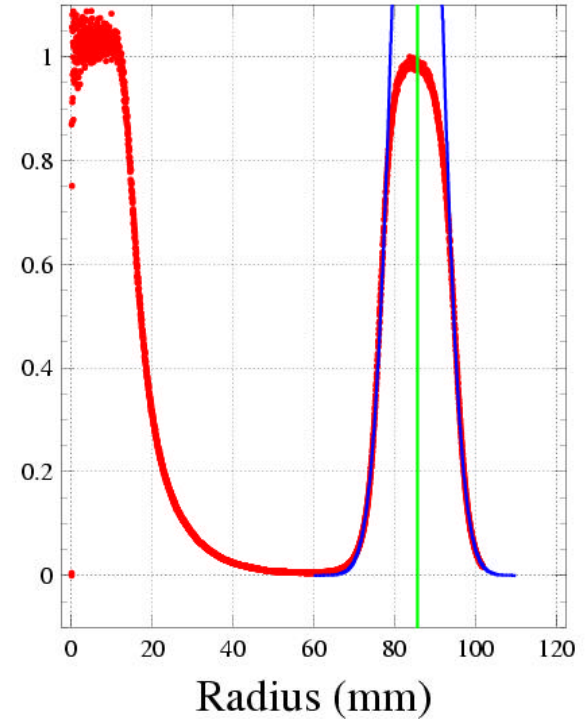
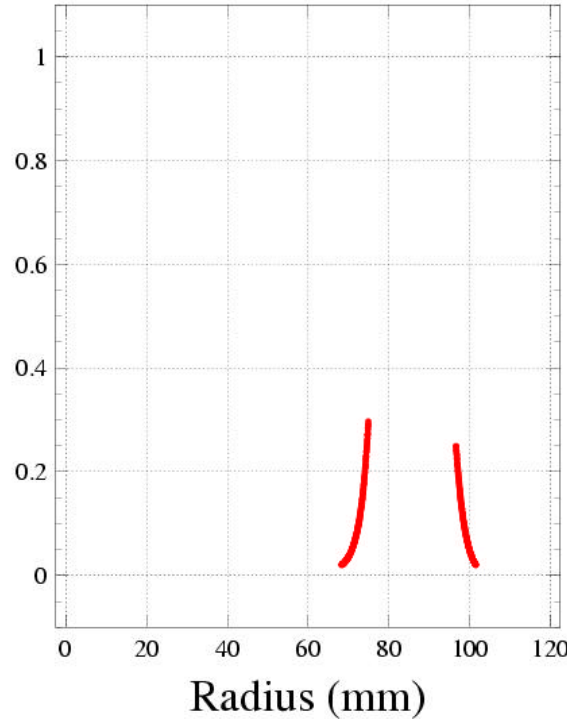
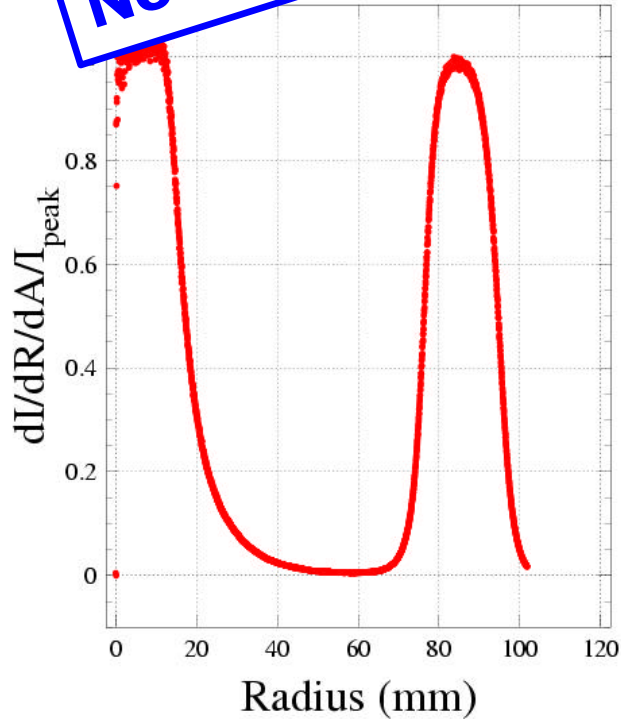


Run	R ₁ (mm)	R ₂ (mm)	R ₃ (mm)
5	85.9±0.1	86.0±0.1	85.2±0.8
6	85.5±0.1	85.0±0.1	84.4±0.3
7	85.3±0.1	84.9±0.1	82.3±0.5
B	85.5±0.1	85.2±0.1	84.7±0.3
C	85.6±0.1	85.3±0.1	84.4±0.3
D	85.6±0.1	85.4±0.1	84.4±0.3

APACHE

Run: C

No filter

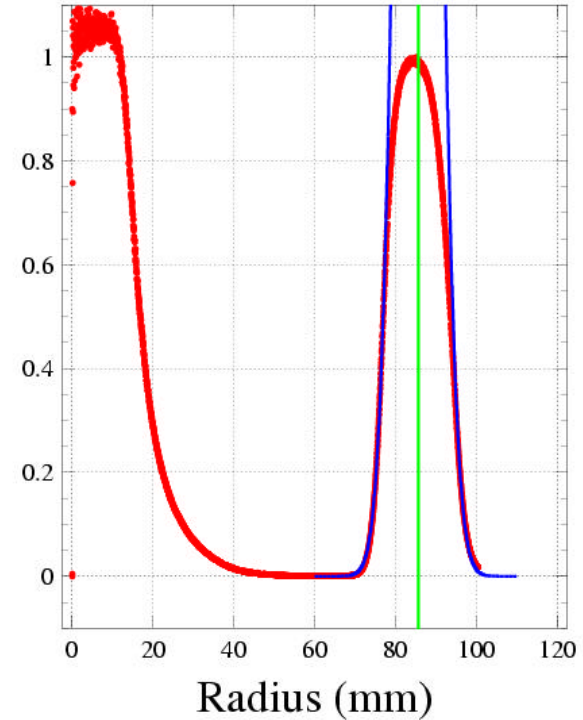
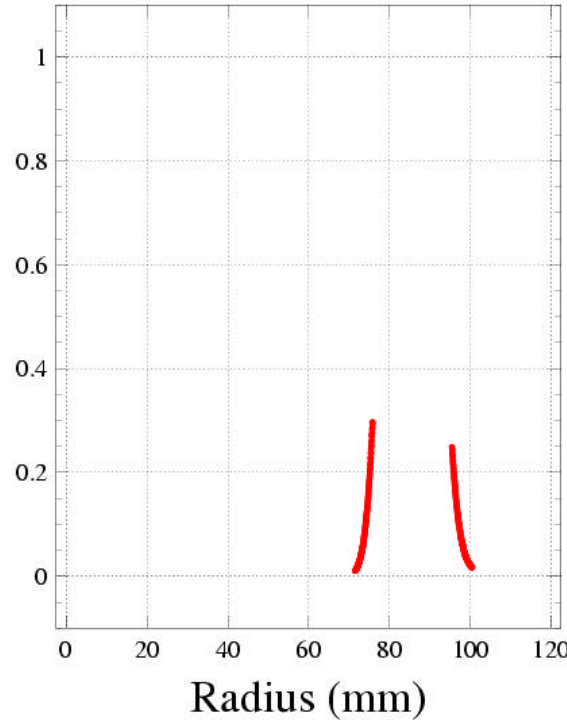
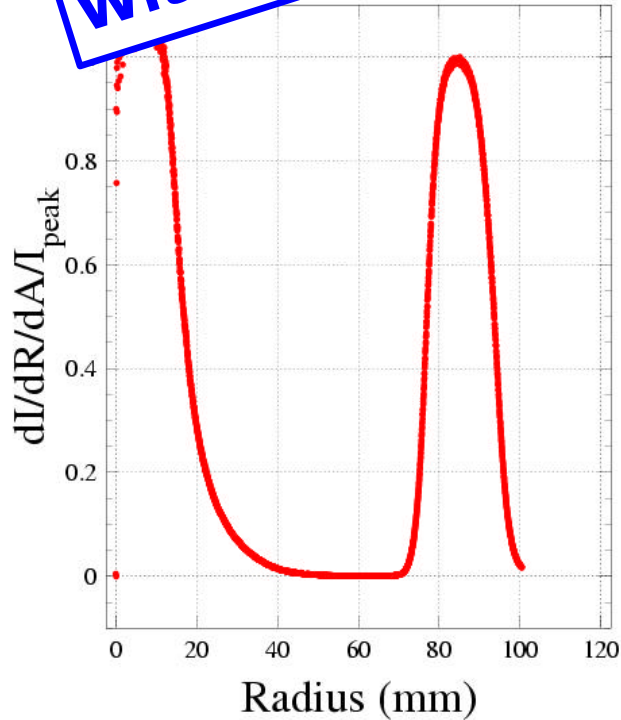


Run No.	R_1 (mm)	R_2 (mm)	R_3 (mm)
C	85.6 ± 0.1	85.3 ± 0.1	84.4 ± 0.3
D	85.6 ± 0.1	85.4 ± 0.1	84.4 ± 0.3

APACHE

Run: D

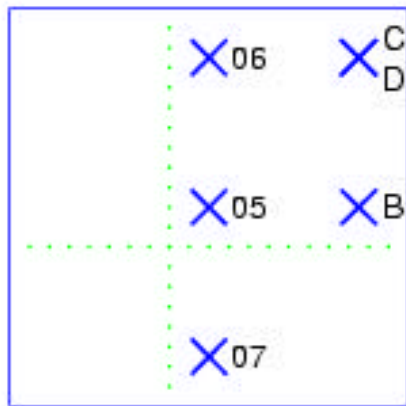
With filter



Run No.	R_1 (mm)	R_2 (mm)	R_3 (mm)
C	85.6 ± 0.1	85.3 ± 0.1	84.4 ± 0.3
D	85.6 ± 0.1	85.4 ± 0.1	84.4 ± 0.3

APACHE

Preliminary Results



e^-



Run	R_1 (mm)	R_2 (mm)	R_3 (mm)
5	85.9 ± 0.1	86.0 ± 0.1	85.2 ± 0.8
6	85.5 ± 0.1	85.0 ± 0.1	84.4 ± 0.3
7	85.3 ± 0.1	84.9 ± 0.1	82.3 ± 0.5
B	85.5 ± 0.1	85.2 ± 0.1	84.7 ± 0.3
C	85.6 ± 0.1	85.3 ± 0.1	84.4 ± 0.3
D	85.6 ± 0.1	85.4 ± 0.1	84.4 ± 0.3

corresponding to

? R_{max}	0.6 ± 0.1	1.1 ± 0.1	2.9 ± 0.9
? $n_{max} (10^{-4})$	3.9 ± 0.7	7.2 ± 0.7	18.9 ± 5.9

The difference between the position of the peaks is assumed to be independent of the detailed shape of distributions



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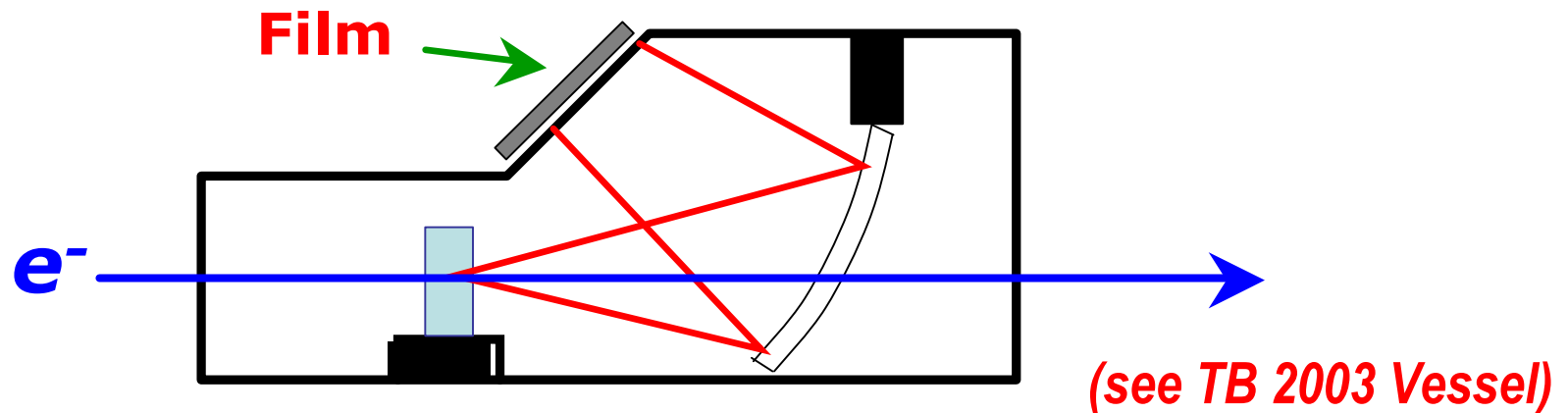
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APACHE

Possible improvements for APACHE:

- use of a spherical mirror tilted wrt the beam axis
 - photographic film in a RICH configuration
 - distortions of the ring due to the spherical aberration
 - no aerogel thickness effects
- separation of the different chromatic components by the use of filters



Summary

- local inhomogeneities of the density lead to variations of n
- the maximum Δn allowed for LHCb aerogel tiles is $\sim 3 \cdot 10^{-4}$
- two methods are presented to evaluate those variations:
 - ✓ Laser Beam Deflection
 - ✓ APACHE
- the results from the two methods **agree** with each other within the experimental resolution
- the APACHE method is very promising and artistic too!

APACHE



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*Special thanks to Giovanni Mazzitelli
&
the Beam Test Facility (LNF Frascati)*



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